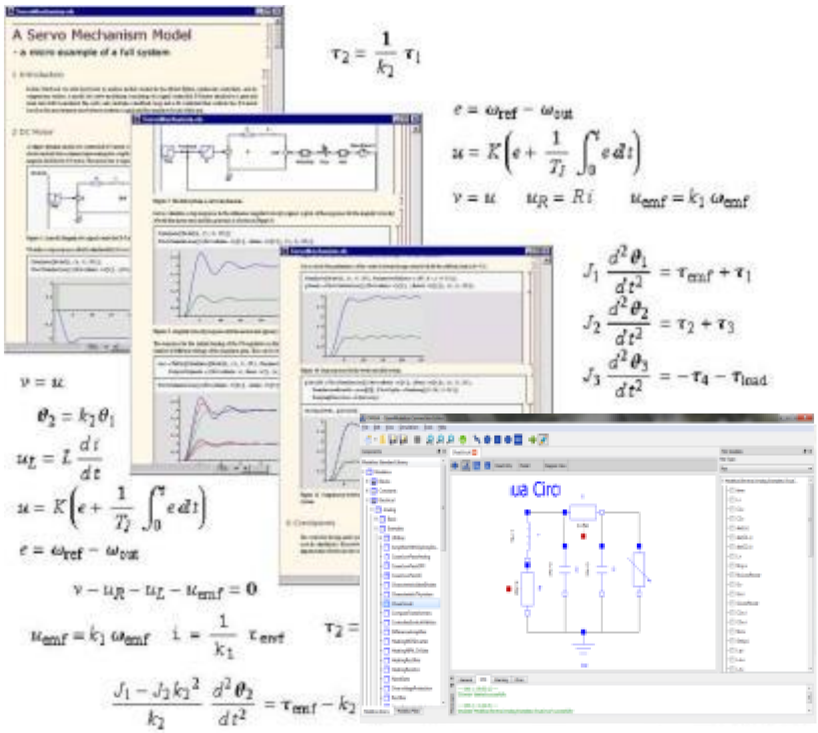
Introduction to Object-Oriented Modeling and Simulation with Modelica and OpenModelica



Tutorial, Version Feb 7, 2017

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Slides

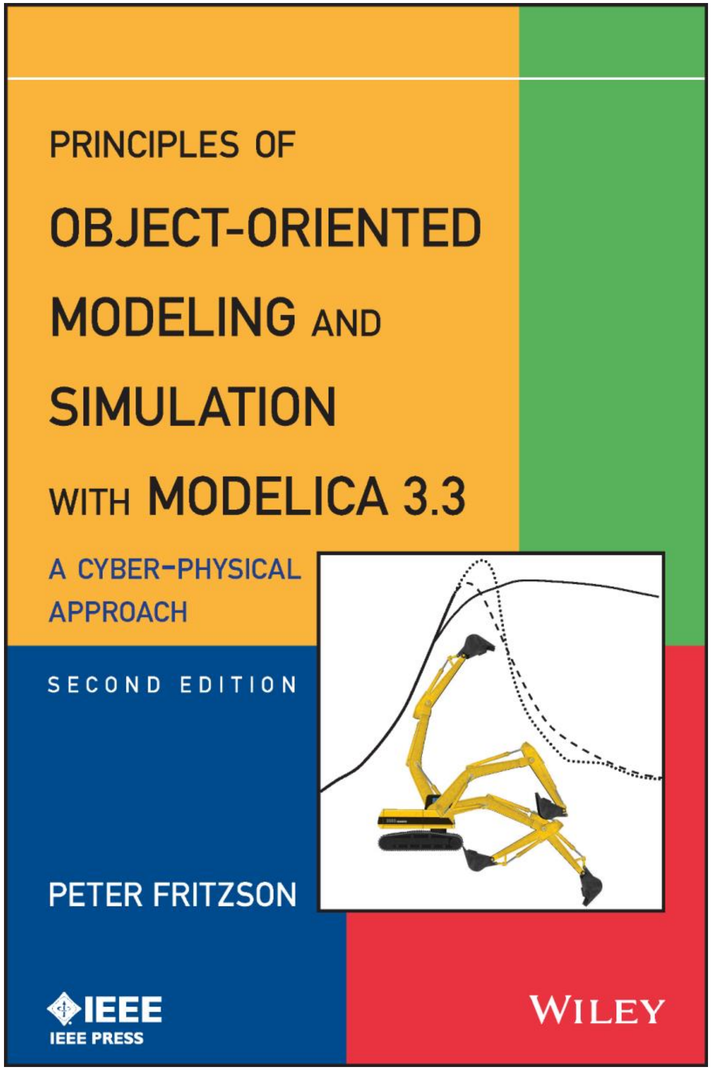
Based on book and lecture notes by Peter Fritzson
Contributions 2004-2005 by Emma Larsdotter Nilsson, Peter Bunus
Contributions 2006-2008 by Adrian Pop and Peter Fritzson
Contributions 2009 by David Broman, Peter Fritzson, Jan Brugård, and Mohsen Torabzadeh-Tari
Contributions 2010 by Peter Fritzson
Contributions 2011 by Peter F., Mohsen T,. Adeel Asghar,
Contributions 2012, 2013, 2014, 2015, 2016 by Peter Fritzson, Lena Buffoni, Mahder Gebremedhin, Bernhard Thiele

Linköpings universitet

2017-02-07

MODELICA

Tutorial Based on Book, December 2014
Download OpenModelica Software



Peter Fritzson

Principles of Object Oriented Modeling and Simulation with Modelica 3.3

A Cyber-Physical Approach

Can be ordered from Wiley or Amazon

Wiley-IEEE Press, 2014, 1250 pages

- OpenModelica
  - www.openmodelica.org
- Modelica Association
  - www.modelica.org

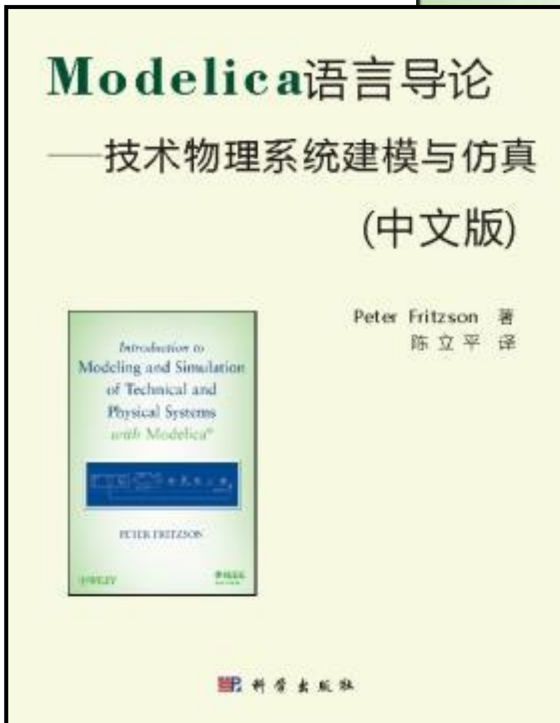
Introductory Modelica Book

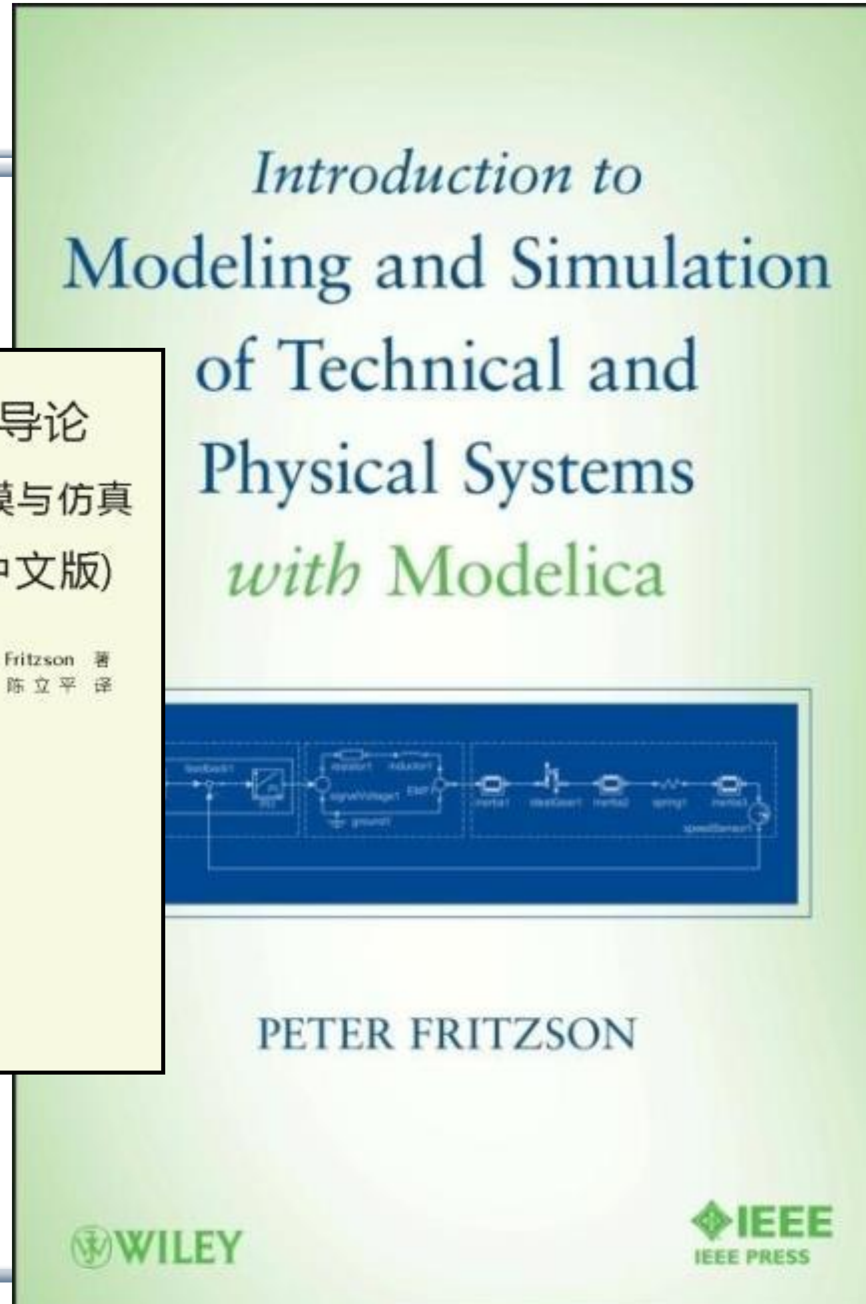
September 2011
232 pages

2015 –Translations available in **Chinese**, **Japanese**, **Spanish**

Wiley
IEEE Press

For Introductory Short Courses on Object Oriented Mathematical Modeling





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- If you want to use the Powerpoint version of these slides in your own course, send an email to: peter.fritzson@ida.liu.se
- Thanks to Emma Larsdotter Nilsson, Peter Bunus, David Broman, Jan Brugård, Mohsen-Torabzadeh-Tari, Adeel Asghar, Lena Buffoni, for contributions to these slides.
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- OpenModelica: www.openmodelica.org

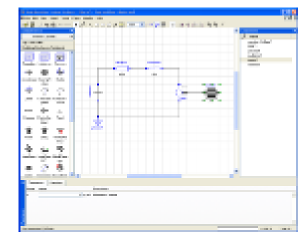
Outline

Part I

Introduction to Modelica and a demo example

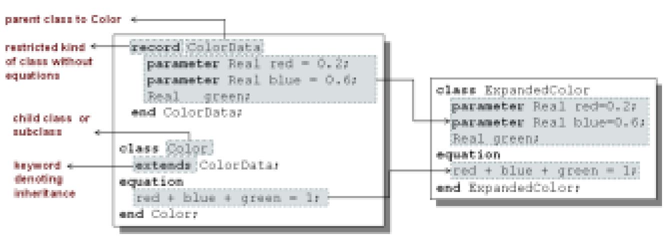
Part II

Modelica environments

Part III

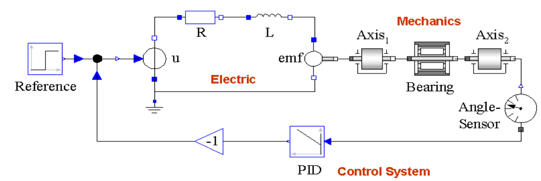
Modelica language concepts and textual modeling



Part IV and Part V

Graphical modeling and the Modelica standard library

Dynamic Optimization



Detailed Schedule (morning version) 09.00-13.00

09:00 - Introduction to Modeling and Simulation

- Start installation of **OpenModelica** including **OMEdit** graphic editor

09:10 - Modelica – The Next Generation Modeling Language

09:25 - *Exercises Part I (15 minutes)*

- Short hands-on exercise on graphical modeling using **OMEdit**– RL Circuit

09:50 – Part II: Modelica Environments and the OpenModelica Environment

10:10 – Part III: Modelica Textual Modeling

10:15 - *Exercises Part IIIa (10 minutes)*

- Hands-on exerciseson textual modeling using the **OpenModelica** environment

10:25 – Coffee Break

10:40 - Modelica Discrete Events, Hybrid, Clocked Properties (Bernhard Thiele)

11:00- *Exercises Part IIIb (15 minutes)*

- Hands-on exercises on textual modeling using the **OpenModelica** environment

11:20– Part IV: Components, Connectors and Connections
- Modelica Libraries

11:30 – *Part V* Dynamic Optimization (Bernhard Thiele)

- Hands-on exercise on dynamic optimization using **OpenModelica**

12:00 – Exercise Graphical Modeling DCMotor using OpenModelica

Software Installation - Windows

- Start the software installation
- Install OpenModelica-1.11.0.exe Download or from the USB Stick

Software Installation – Linux (requires internet connection)

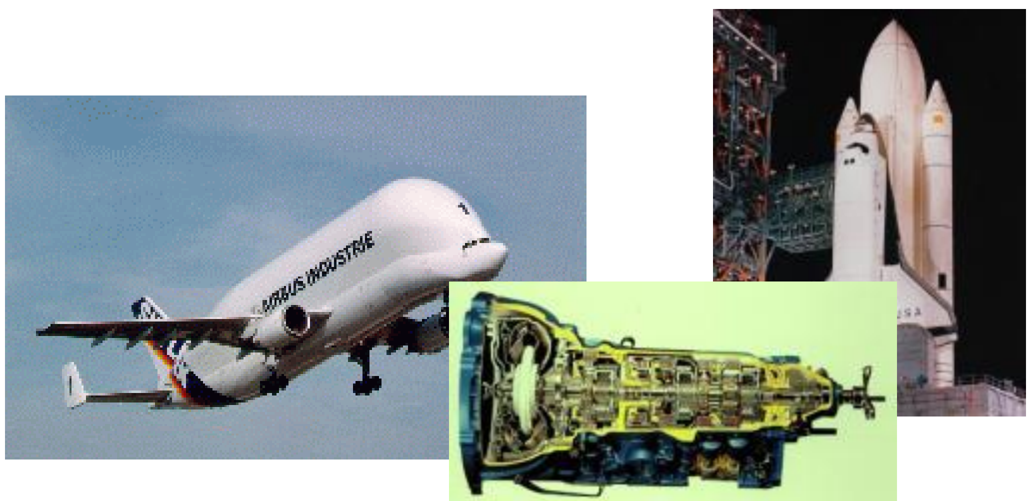
- Go to https://openmodelica.org/index.php/download/download-linux and follow the instructions.

Software Installation – MAC (requires internet connection)

- Go to https://openmodelica.org/index.php/download/download-mac and follow the instructions or follow the instructions written below.
- The installation uses MacPorts. After setting up a MacPorts installation, run the following commands on the terminal (as root):
  - *echo rsync://build.openmodelica.org/macports/ >> /opt/local/etc/macports/sources.conf # assuming you installed into /opt/local*
  - *port selfupdate*
  - *port install openmodelica-devel*

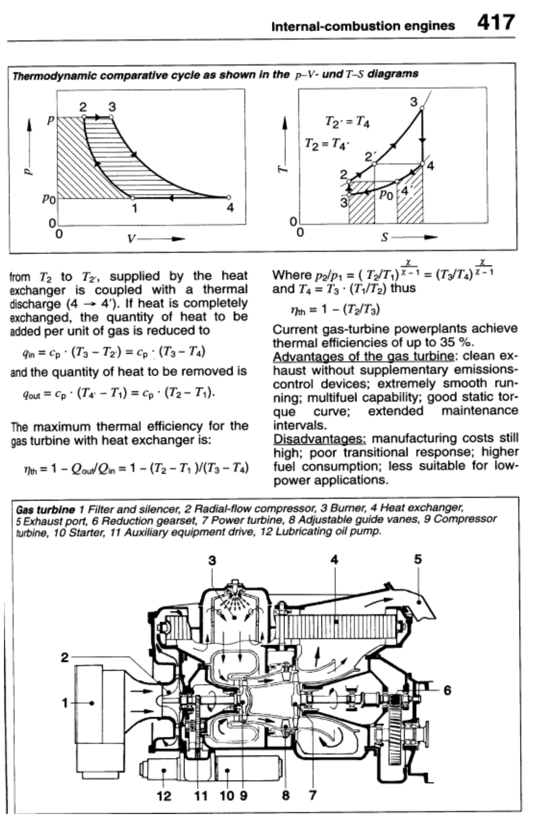
Part I

Introduction to Modelica and a demo example



Modelica Background: Stored Knowledge

Model knowledge is stored in books and human minds which computers cannot access



Internal-combustion engines 417

Thermodynamic comparative cycle as shown in the p–V- und T–S diagrams

from T_2 to $T_{2'}$, supplied by the heat exchanger is coupled with a thermal discharge (4 → 4′). If heat is completely exchanged, the quantity of heat to be added per unit of gas is reduced to

$$q_{in} = c_p \cdot (T_3 - T_{2'}) = c_p \cdot (T_3 - T_4)$$

and the quantity of heat to be removed is

$$q_{out} = c_p \cdot (T_{4'} - T_1) = c_p \cdot (T_2 - T_1).$$

The maximum thermal efficiency for the gas turbine with heat exchanger is:

$$\eta_{th} = 1 - Q_{out}/Q_{in} = 1 - (T_2 - T_1)/(T_3 - T_4)$$

Where $p_2/p_1 = (T_2/T_1)^{\frac{\chi}{\chi-1}} = (T_3/T_4)^{\frac{\chi}{\chi-1}}$ and $T_4 = T_3 \cdot (T_1/T_2)$ thus

$$\eta_{th} = 1 - (T_2/T_3)$$

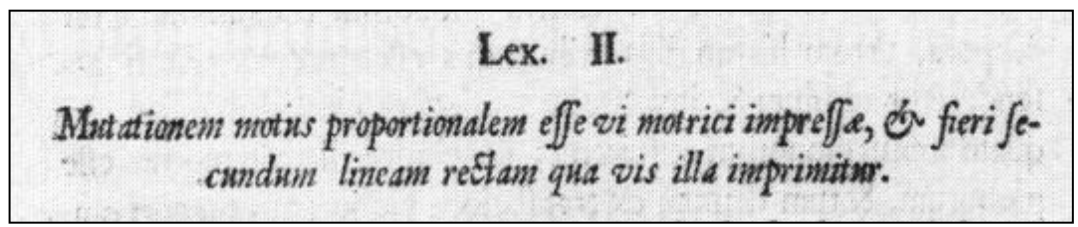
Current gas-turbine powerplants achieve thermal efficiencies of up to 35 %.

Advantages of the gas turbine: clean exhaust without supplementary emissions-control devices; extremely smooth running; multifuel capability; good static torque curve; extended maintenance intervals.

Disadvantages: manufacturing costs still high; poor transitional response; higher fuel consumption; less suitable for low-power applications.

Gas turbine *1 Filter and silencer, 2 Radial-flow compressor, 3 Burner, 4 Heat exchanger, 5 Exhaust port, 6 Reduction gearset, 7 Power turbine, 8 Adjustable guide vanes, 9 Compressor turbine, 10 Starter, 11 Auxiliary equipment drive, 12 Lubricating oil pump.*

“The change of motion is proportional to the motive force impressed“
– Newton

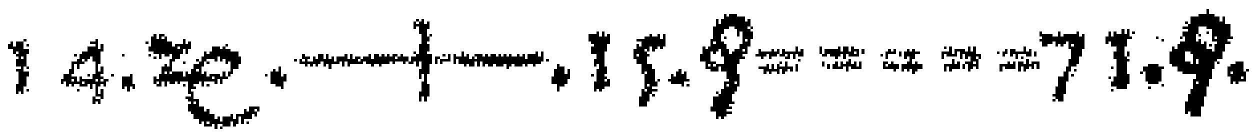


Lex. II.

Mutationem motus proportionalem eſſe vi motrici impreſſæ, & fieri ſecundum lineam rectam qua vis illa imprimitur.

Modelica Background: The Form – Equations

- Equations were used in the third millennium B.C.
- Equality sign was introduced by Robert Recorde in 1557



Newton still wrote text (Principia, vol. 1, 1686)
"*The change of motion is proportional to the motive force impressed*"

CSSL (1967) introduced a special form of "equation":

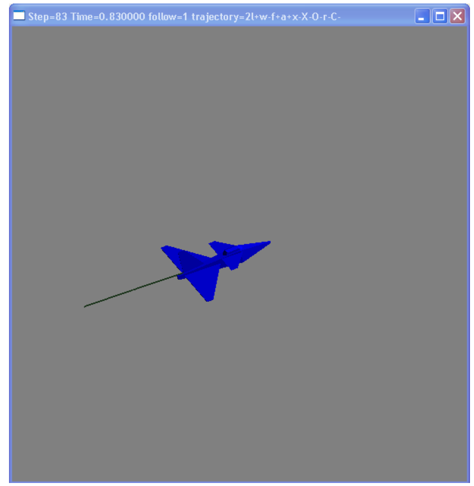
```
variable = expression
v = INTEG(F)/m
```

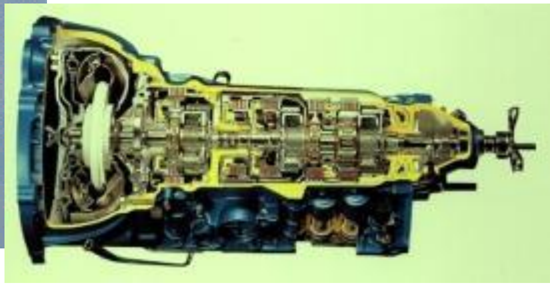
Programming languages usually do not allow equations!

What is Modelica?

A language for modeling of complex cyber-physical systems

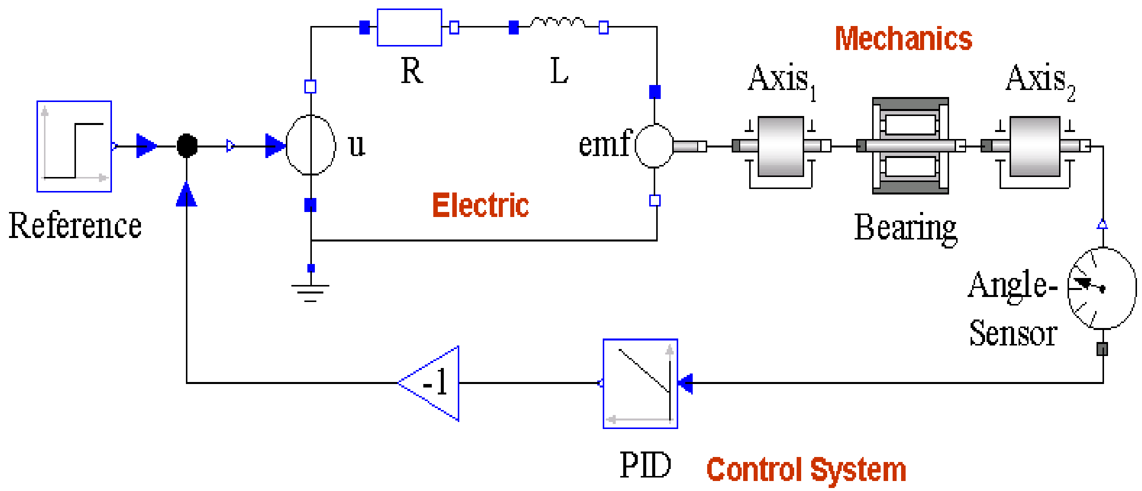
- Robotics
- Automotive
- Aircrafts
- Satellites
- Power plants
- Systems biology





What is Modelica?

A language for modeling of complex cyber-physical systems



Primary designed for **simulation**, but there are also other usages of models, e.g. optimization.

What is Modelica?

A language for modeling of complex cyber-physical systems

i.e., Modelica is **not** a tool

Free, open language specification:


MODELICA

Modelica® - A Unified Object-Oriented Language for Physical Systems Modeling

Language Specification

Version 1.1

Available at: www.modelica.org

Developed and standardized by Modelica Association

There exist several free and commercial tools, for example:

- **OpenModelica from OSMC**
- Dymola from Dassault systems
- Wolfram System Modeler fr Wolfram MathCore
- SimulationX from ITI
- MapleSim from MapleSoft
- AMESIM from LMS
- JModelica.org from Modelon
- MWORKS from Tongyang Sw & Control
- IDA Simulation Env, from Equa
- ESI Group Modeling tool, ESI Group

Modelica – The Next Generation Modeling Language

Declarative language

Equations and mathematical functions allow acausal modeling, high level specification, increased correctness

Multi-domain modeling

Combine electrical, mechanical, thermodynamic, hydraulic, biological, control, event, real-time, etc...

Everything is a class

Strongly typed object-oriented language with a general class concept, Java & MATLAB-like syntax

Visual component programming

Hierarchical system architecture capabilities

Efficient, non-proprietary

Efficiency comparable to C; advanced equation compilation, e.g. 300 000 equations, ~150 000 lines on standard PC

Modelica Acausal Modeling

What is *acausal* modeling/design?

Why does it increase *reuse*?

> The acausality makes Modelica library classes *more reusable* than traditional classes containing assignment statements where the input-output causality is fixed.

Example: a resistor *equation*:

R*i = v;

can be used in three ways:

i := v/R;

v := R*i;

R := v/i;

What is Special about Modelica?

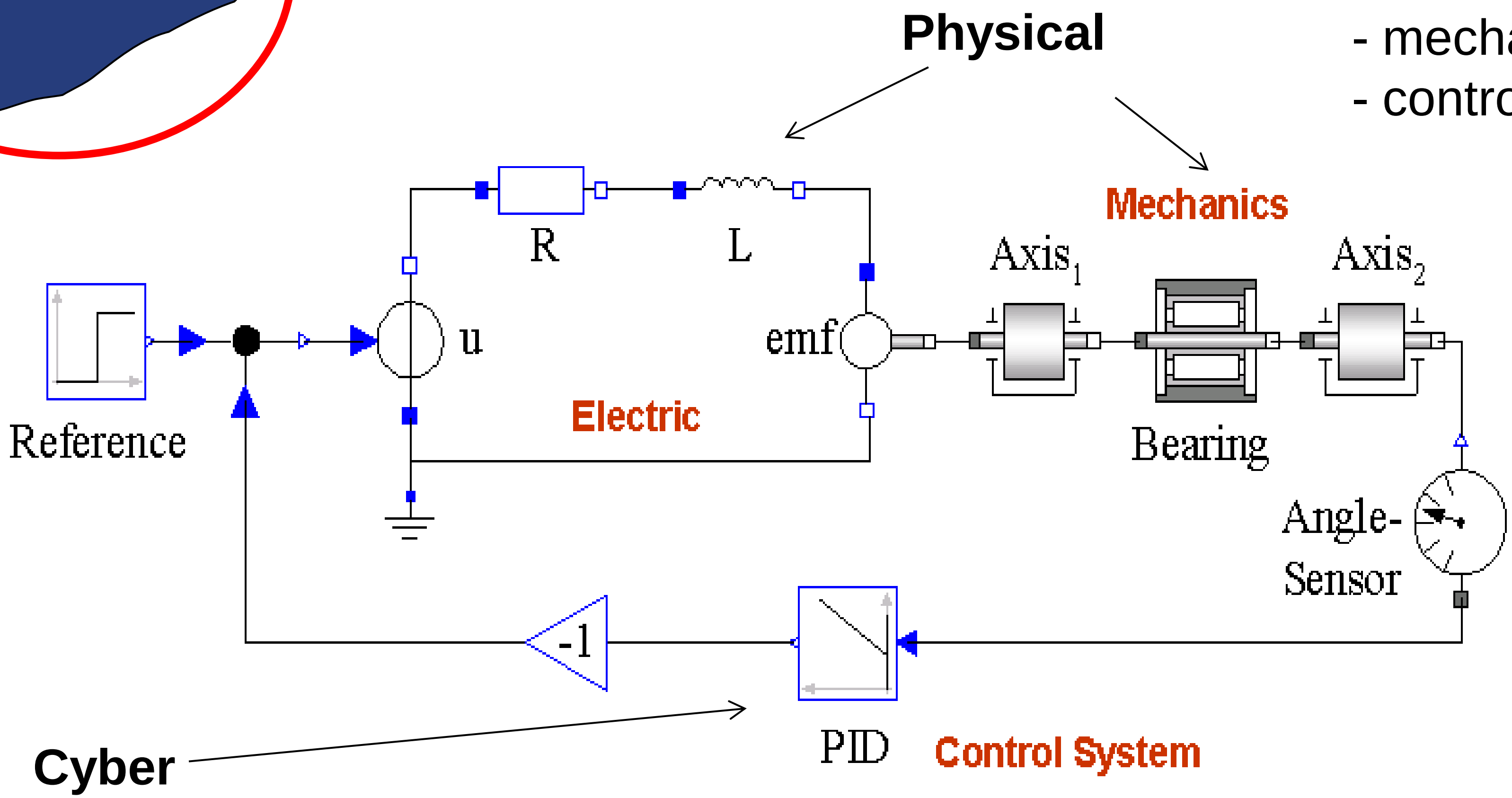
- Multi-Domain Modeling
- Visual acausal hierarchical component modeling
- Typed declarative equation-based textual language
- Hybrid modeling and simulation

What is Special about Modelica?

Multi-Domain Modeling

Cyber-Physical Modeling

3 domains
- electric
- mechanics
- control



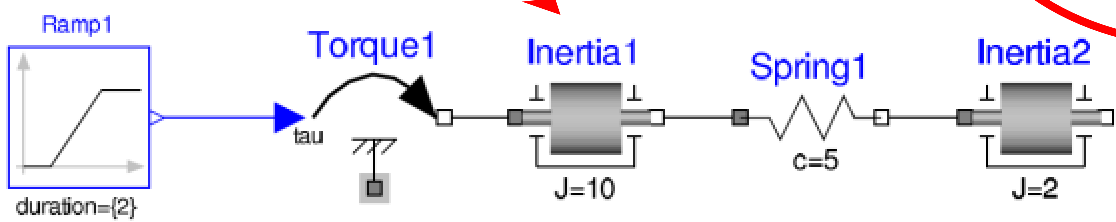
What is Special about Modelica?

Multi-Domain Modeling

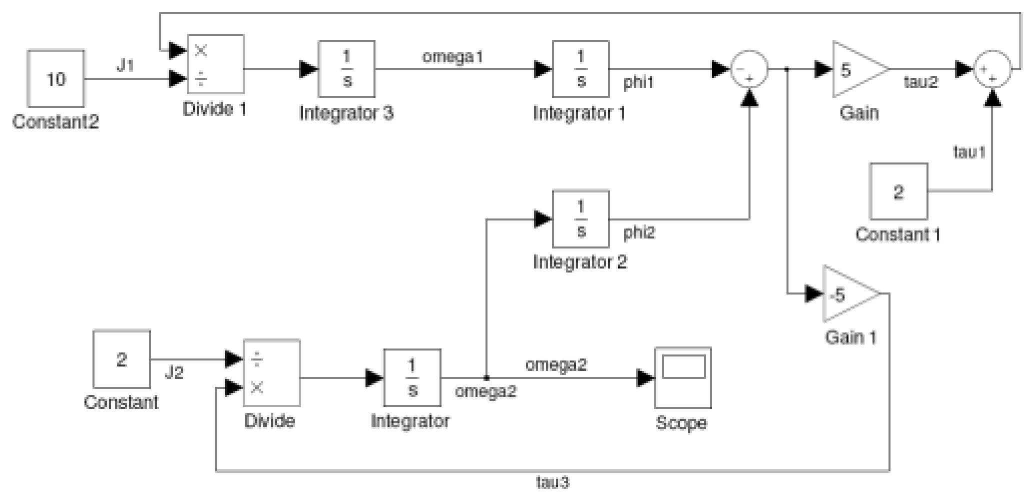
Visual Acausal Hierarchical Component Modeling

Keeps the physical structure

Acausal model (Modelica)



Causal block-based model (Simulink)

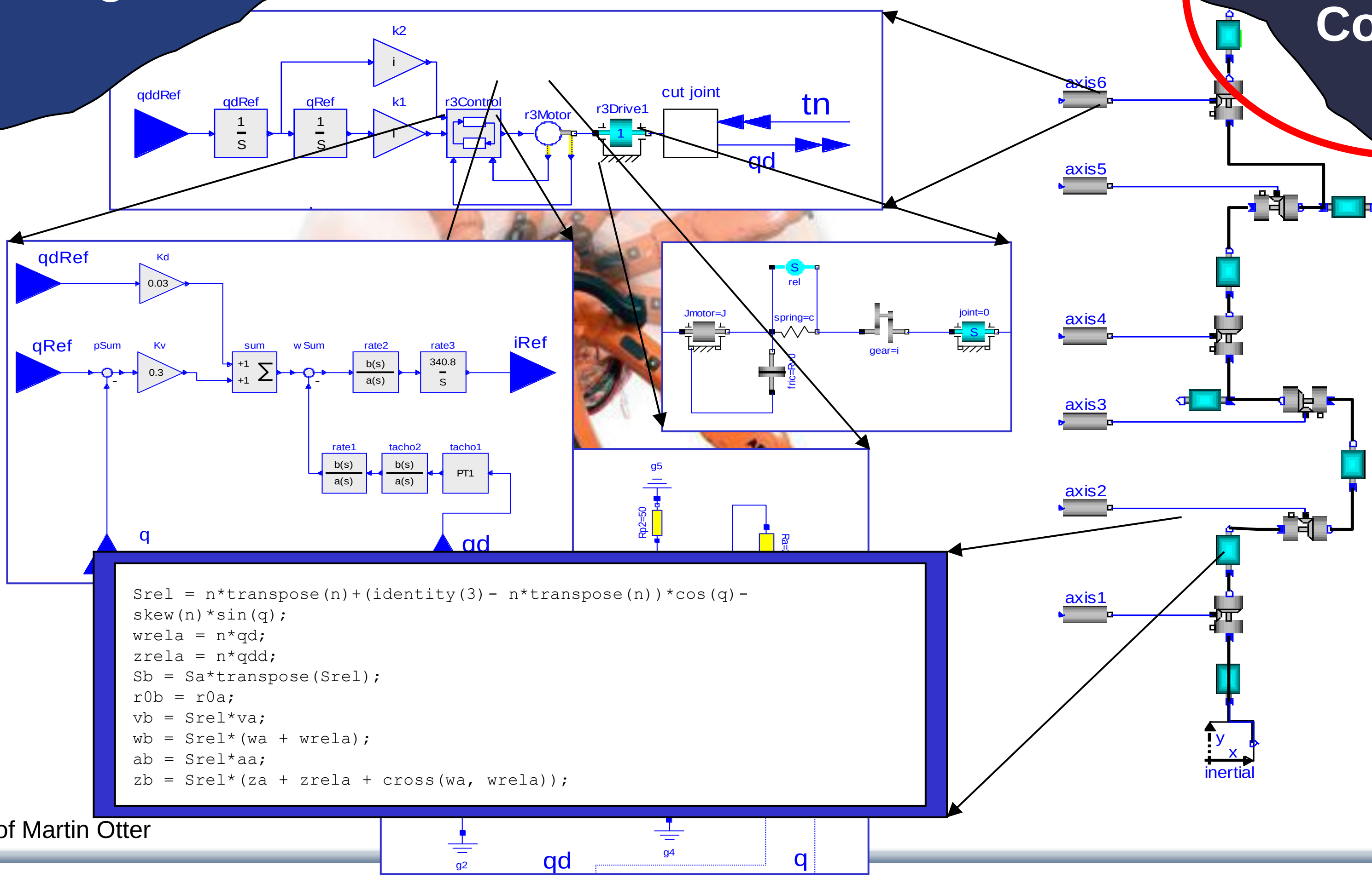


What is Special about Modelica?

Multi-Domain Modeling

Hierarchical system modeling

Visual Acausal Hierarchical Component Modeling



Courtesy of Martin Otter

What is Special about Modelica?

Multi-Domain Modeling

Visual Acausal Hierarchical Component Modeling

A textual *class-based* language
OO primary used for as a structuring concept

Behaviour described declaratively using
- Differential algebraic equations (DAE) (continuous-time)
- Event triggers (discrete-time)

Variable declarations

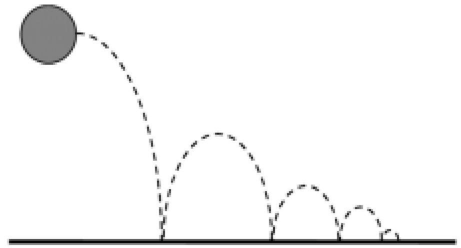
```
class VanDerPol  "Van der Pol oscillator model"
  Real x(start = 1)  "Descriptive string for x";
  Real y(start = 1)  "y coordinate";
  parameter Real lambda = 0.3;
equation
  der(x) = y;
  der(y) = -x + lambda*(1 - x*x)*y;
end VanDerPol;
```

Differential equations

Typed Declarative Equation-based Textual Language

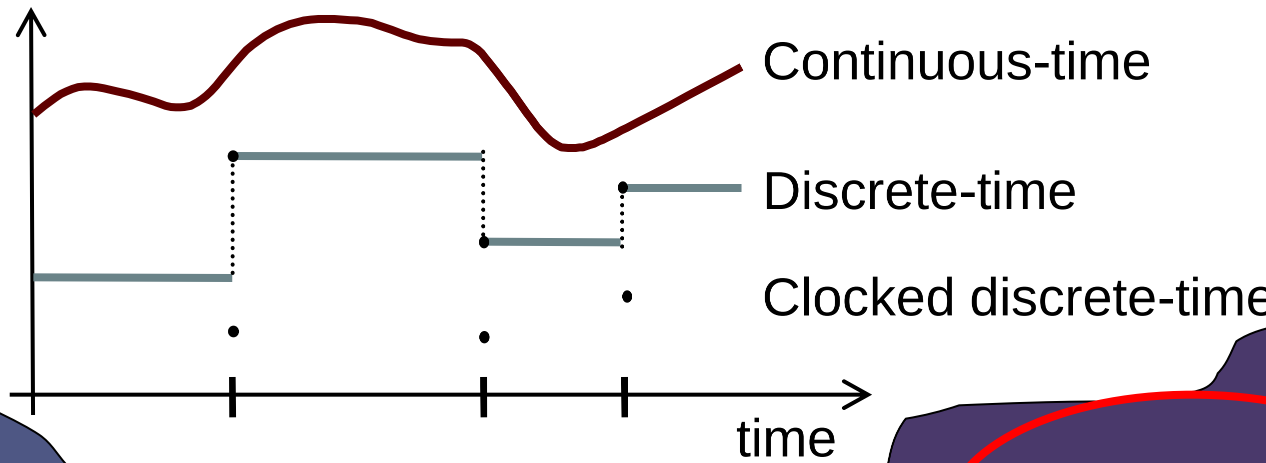
What is Special about Modelica?

Multi-Domain Modeling



Visual Acausal Component Modeling

Hybrid modeling =
continuous-time + discrete-time modeling

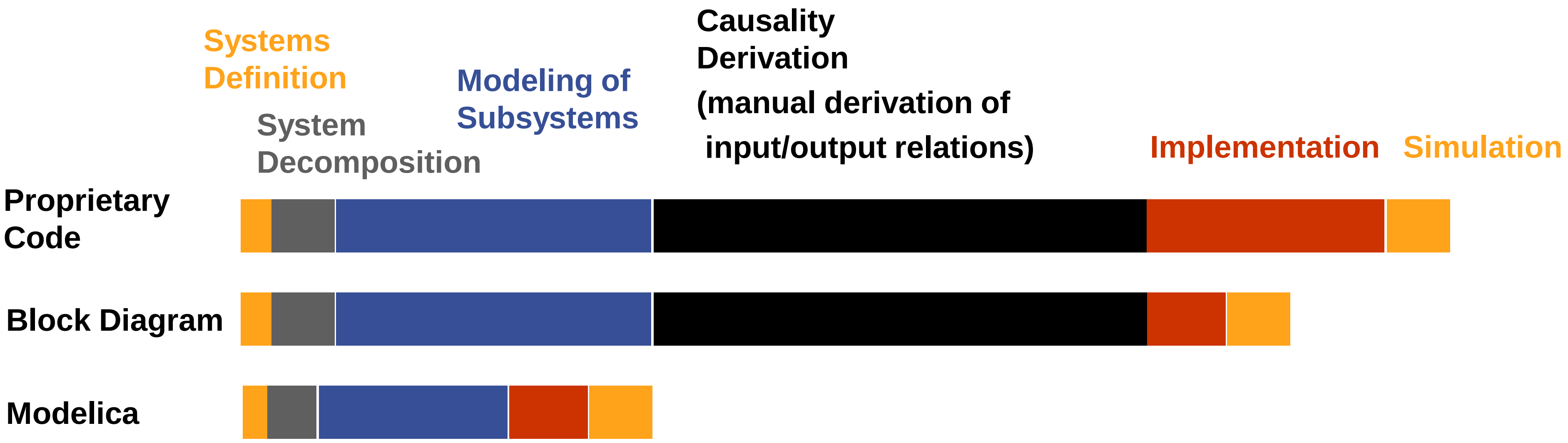


Typed Declarative Equation-based Textual Language

Hybrid Modeling

Modelica – Faster Development, Lower Maintenance than with Traditional Tools

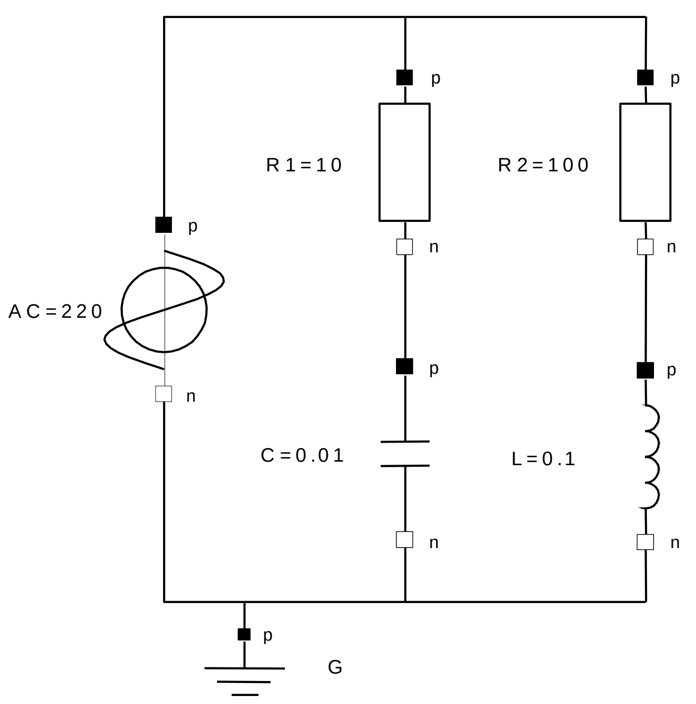
Block Diagram (e.g. Simulink, ...) or
Proprietary Code (e.g. Ada, Fortran, C,...)
vs Modelica



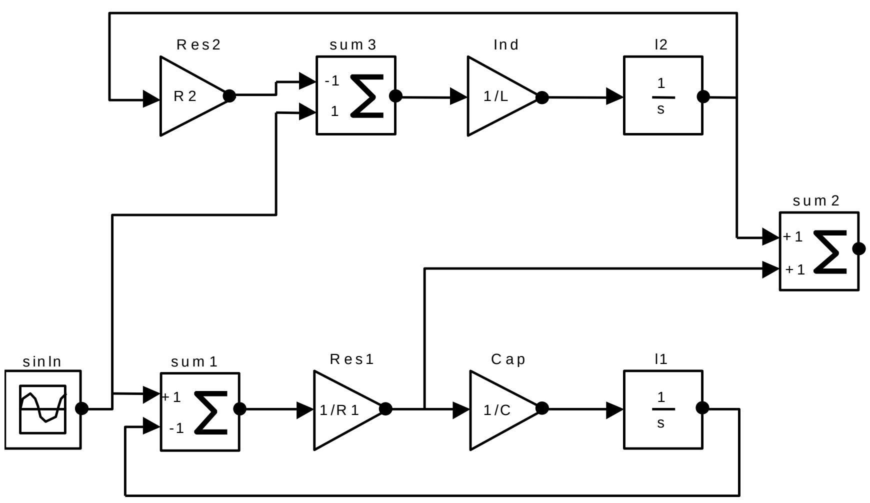
Modelica vs Simulink Block Oriented Modeling
Simple Electrical Model

Modelica:
Physical model – easy to understand

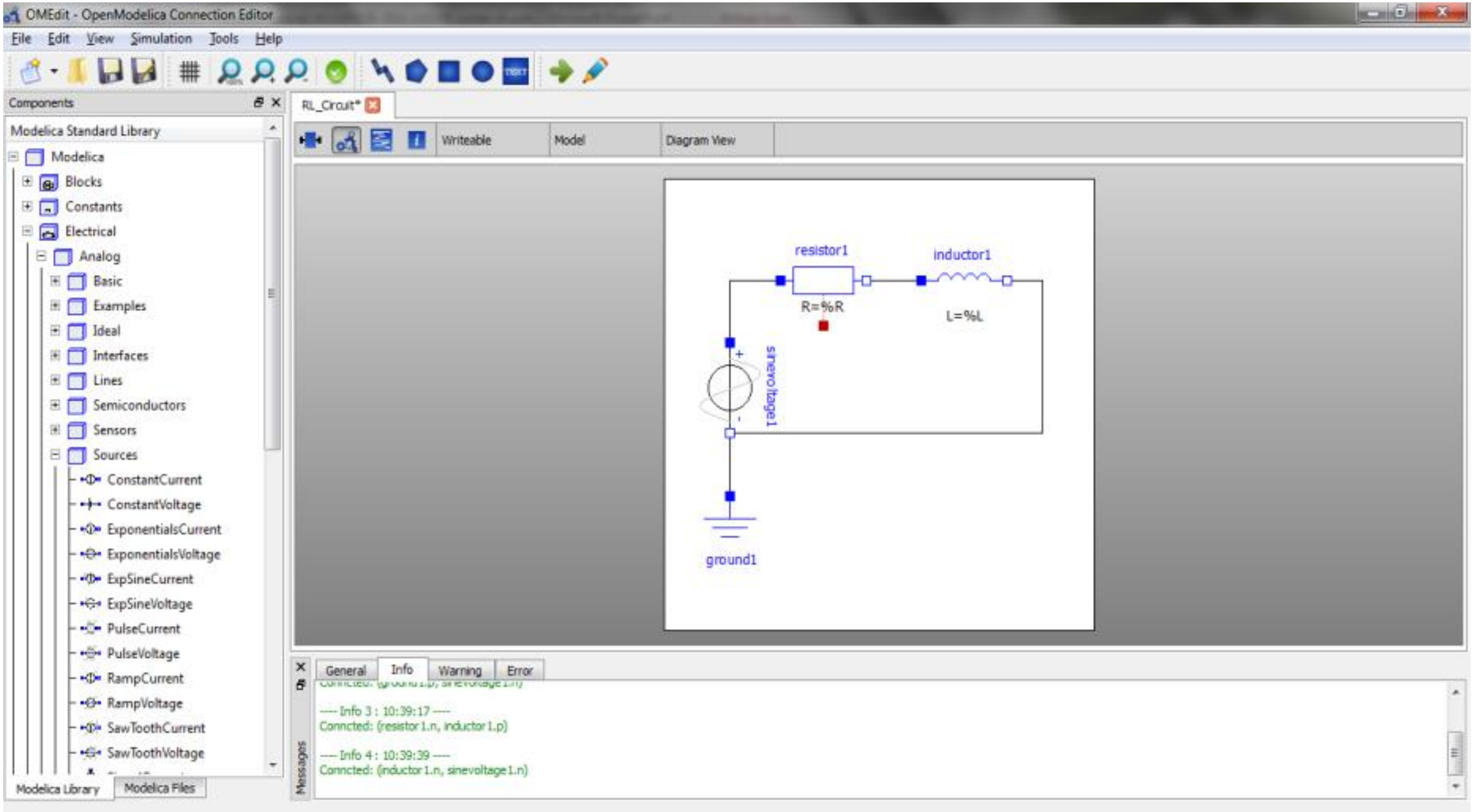
Keeps the physical structure



Simulink:
Signal-flow model – hard to understand



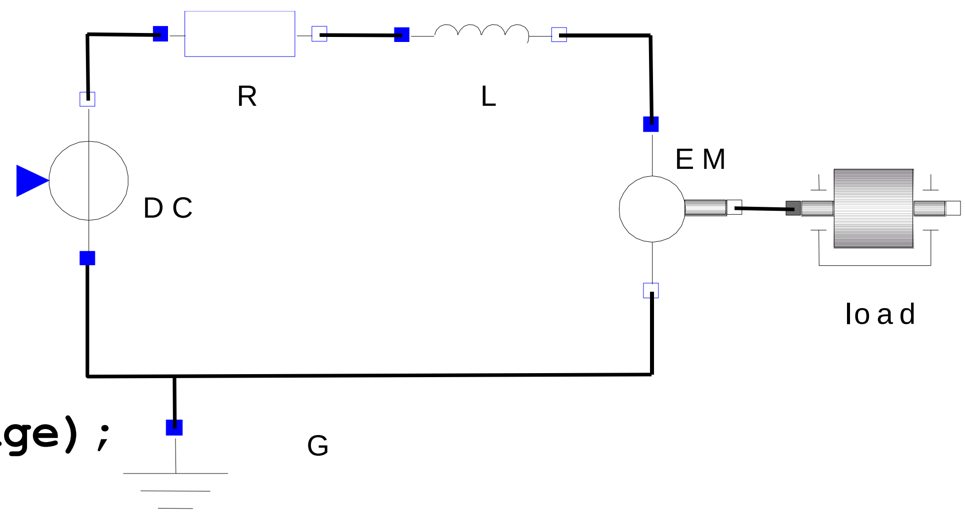
Graphical Modeling - Using Drag and Drop Composition



Multi-Domain (Electro-Mechanical) Modelica Model

- A DC motor can be thought of as an electrical circuit which also contains an electromechanical component

```
model DCMotor
   Resistor R(R=100);
   Inductor L(L=100);
   VsourceDC DC(f=10);
   Ground G;
   ElectroMechanicalElement EM(k=10,J=10, b=2);
   Inertia load;
equation
   connect(DC.p,R.n);
   connect(R.p,L.n);
   connect(L.p, EM.n);
   connect(EM.p, DC.n);
   connect(DC.n,G.p);
   connect(EM.flange,load.flange);
end DCMotor
```



Corresponding DCMotor Model Equations

The following equations are automatically derived from the Modelica model:

```
0 == DC.p.i + R.n.i
DC.p.v == R.n.v

0 == R.p.i + L.n.i
R.p.v == L.n.v

0 == L.p.i + EM.n.i
L.p.v == EM.n.v

0 == EM.p.i + DC.n.i
EM.p.v == DC.n.v

0 == DC.n.i + G.p.i
DC.n.v == G.p.v
```

```
EM.u == EM.p.v - EM.n.v
0 == EM.p.i + EM.n.i
EM.i == EM.p.i
EM.u == EM.k * EM.ω
EM.i == EM.M / EM.k
EM.J * EM.ω == EM.M - EM.b * EM.ω

DC.u == DC.p.v - DC.n.v
0 == DC.p.i + DC.n.i
DC.i == DC.p.i
DC.u == DC.Amp * Sin[2 π DC.f * t]
```

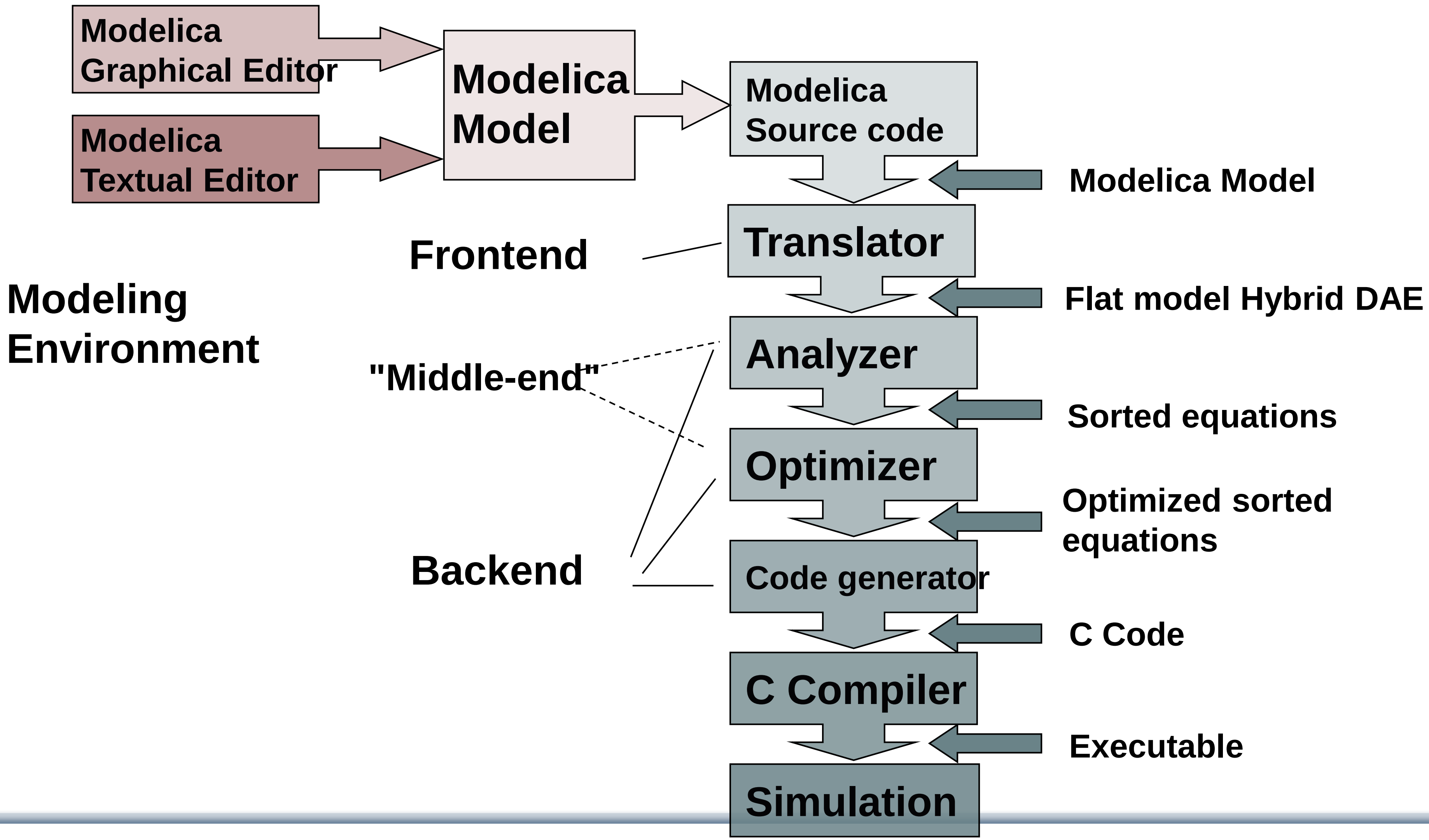
```
R.u == R.p.v - R.n.v
0 == R.p.i + R.n.i
R.i == R.p.i
R.u == R.R * R.i

L.u == L.p.v - L.n.v
0 == L.p.i + L.n.i
L.i == L.p.i
L.u == L.L * L.i'
```

(`load` component not included)

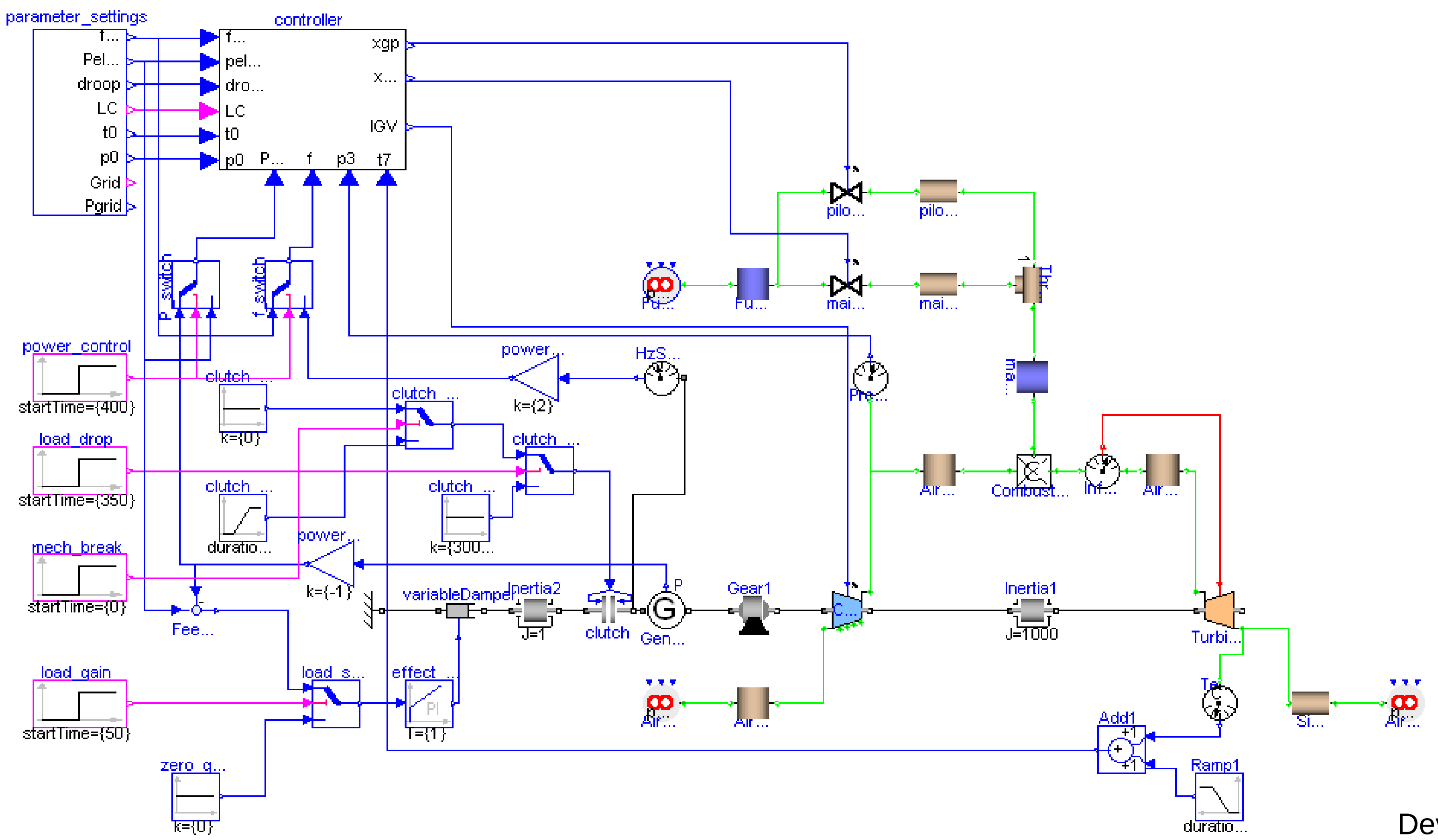
Automatic transformation to ODE or DAE for simulation:

$$\frac{dx}{dt} == f[x, u, t] \qquad g\left[\frac{dx}{dt}, x, u, t\right] == 0$$

Model Translation Process to Hybrid DAE to Code



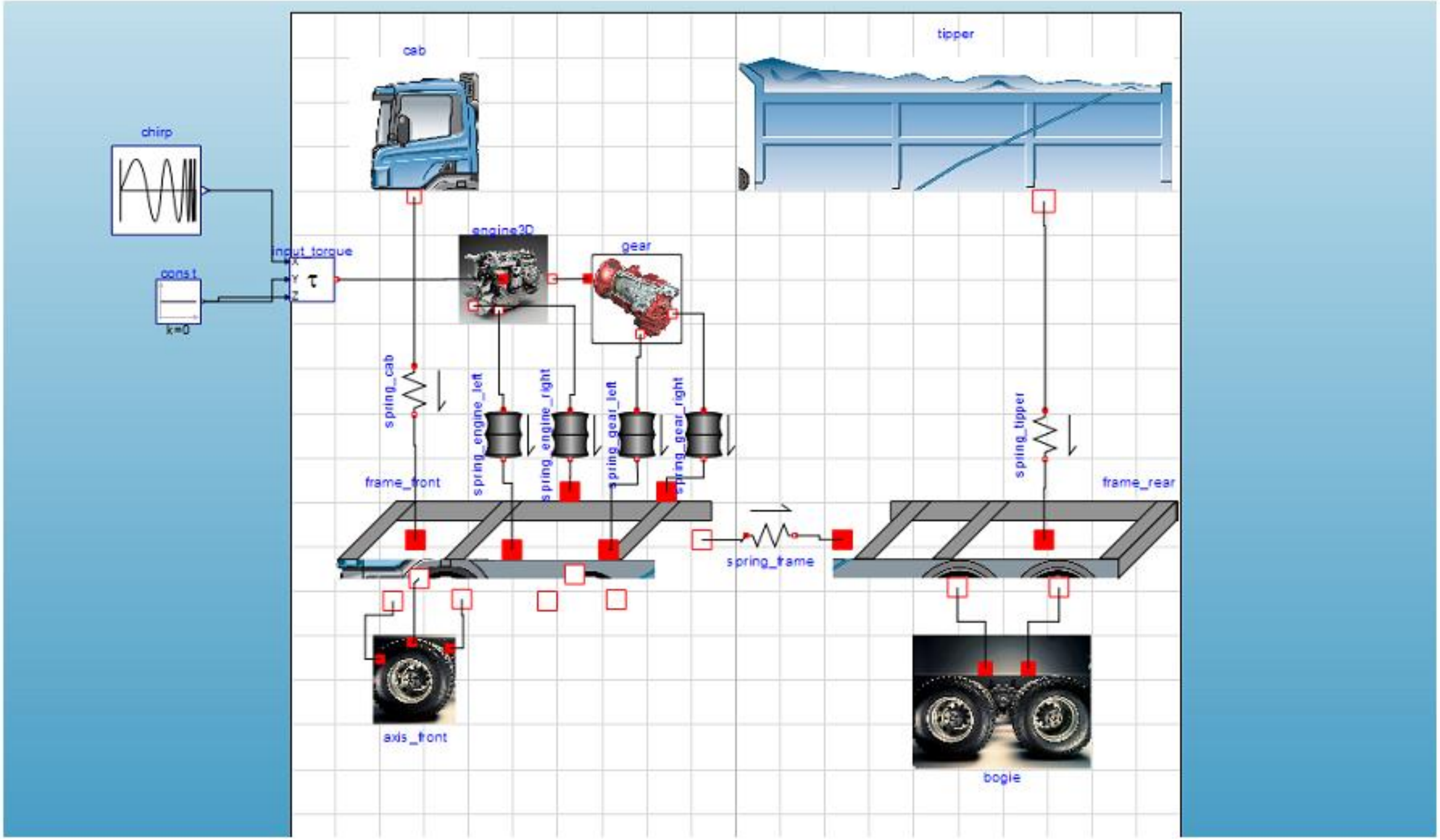
Modelica in Power Generation
GTX Gas Turbine Power Cutoff Mechanism



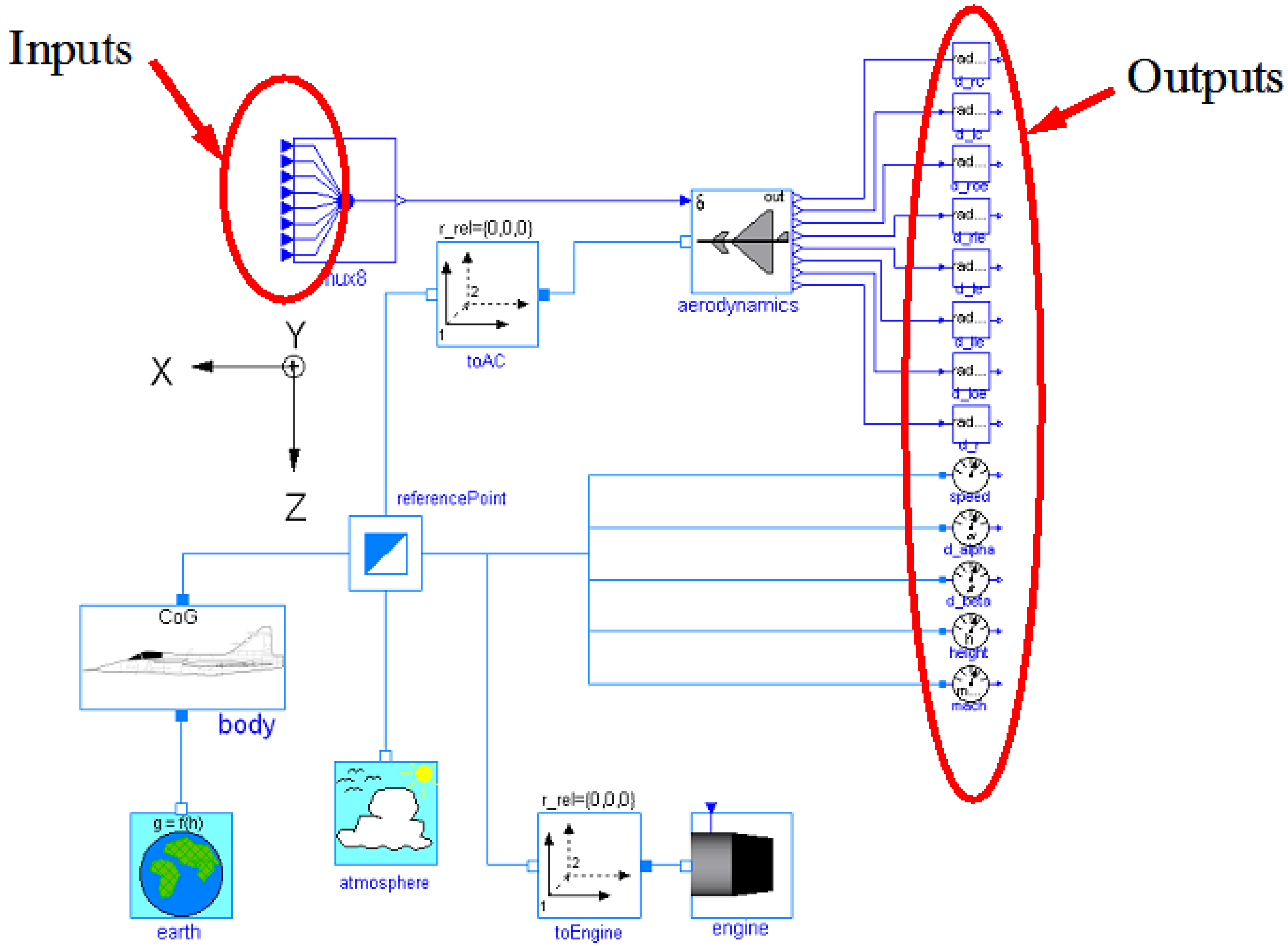
Developed by MathCore for Siemens

Courtesy of Siemens Industrial Turbomachinery AB

Modelica in Automotive Industry

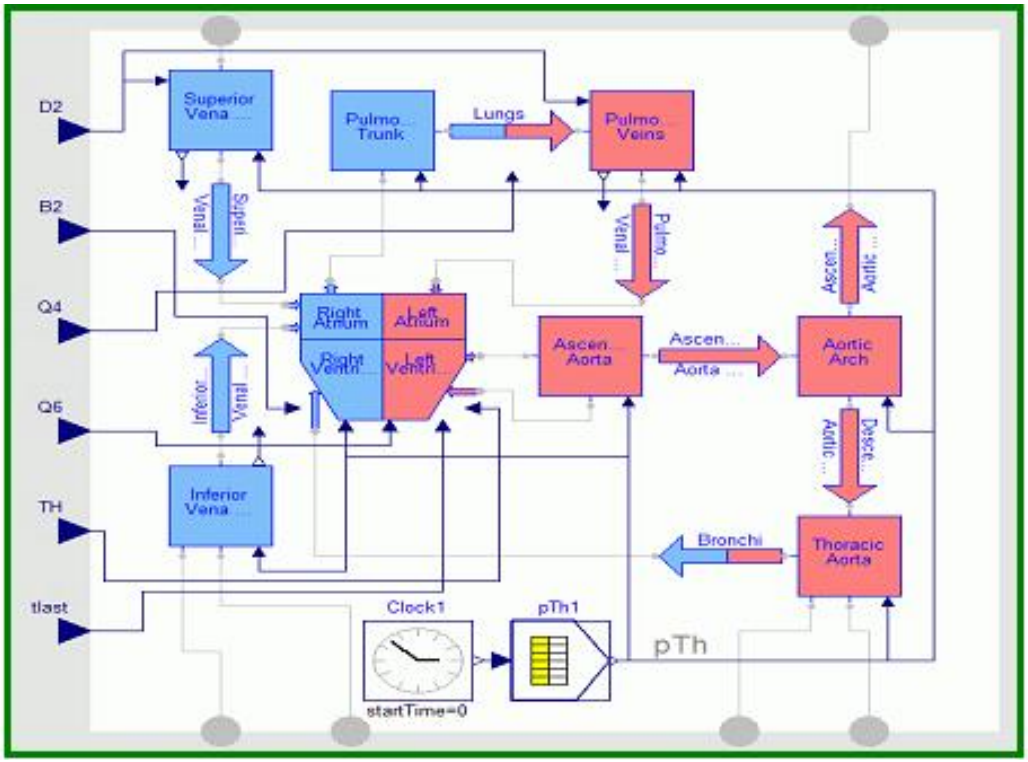


Modelica in Avionics



MODELICA

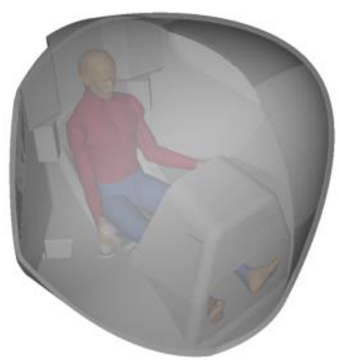
Modelica in Biomechanics



Application of Modelica in Robotics Models Real-time Training Simulator for Flight, Driving

- Using Modelica models generating real-time code
- Different simulation environments (e.g. Flight, Car Driving, Helicopter)
- Developed at DLR Munich, Germany
- Dymola Modelica tool

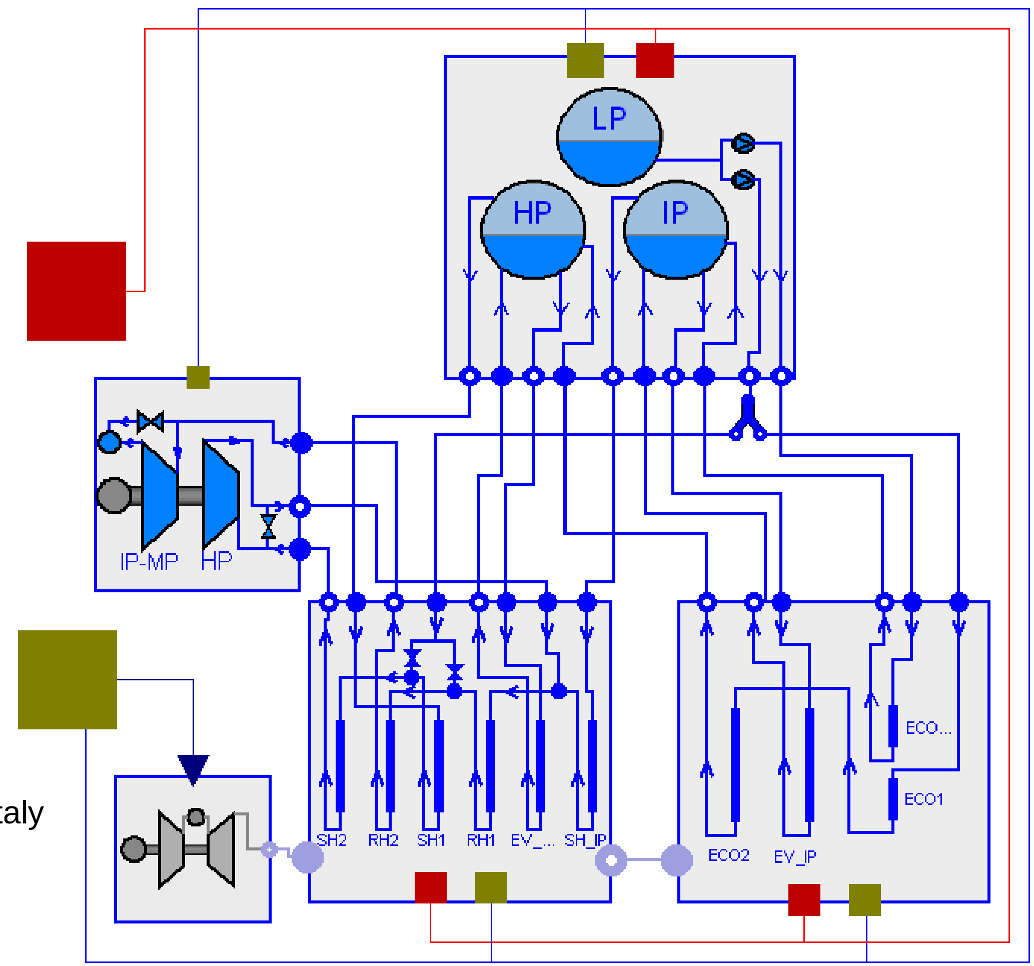
(Movie demo)



Courtesy of Tobias Bellmann, DLR, Oberphaffenhofen, Germany

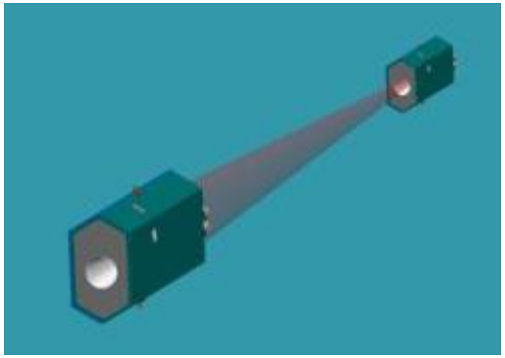
Combined-Cycle Power Plant
Plant model – system level

- GT unit, ST unit, Drum boilers unit and HRSG units, connected by thermo-fluid ports and by signal buses
- Low-temperature parts (condenser, feedwater system, LP circuits) are represented by trivial boundary conditions.
- GT model: simple law relating the electrical load request with the exhaust gas temperature and flow rate.



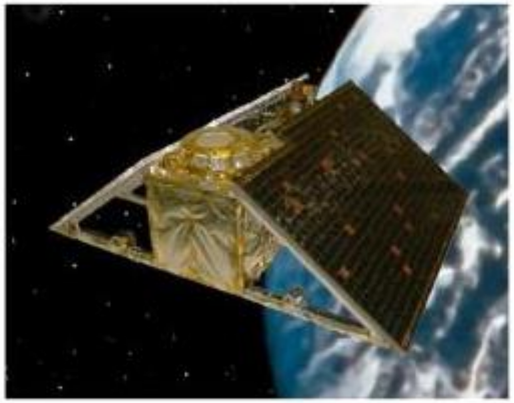
Courtesy Francesco Casella, Politecnico di Milano – Italy and Francesco Pretolani, CESI SpA - Italy

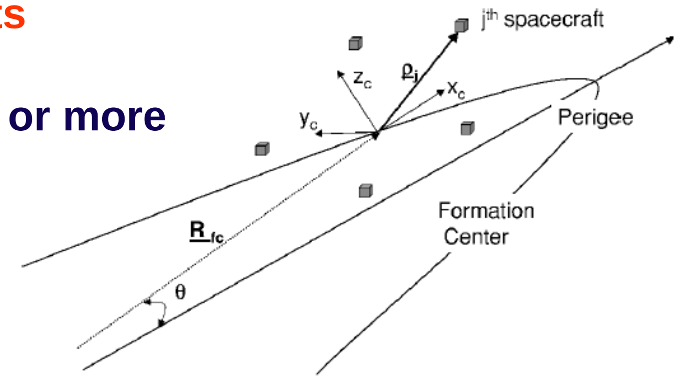
Modelica Spacecraft Dynamics Library



Formation flying on elliptical orbits

Control the relative motion of two or more spacecraft





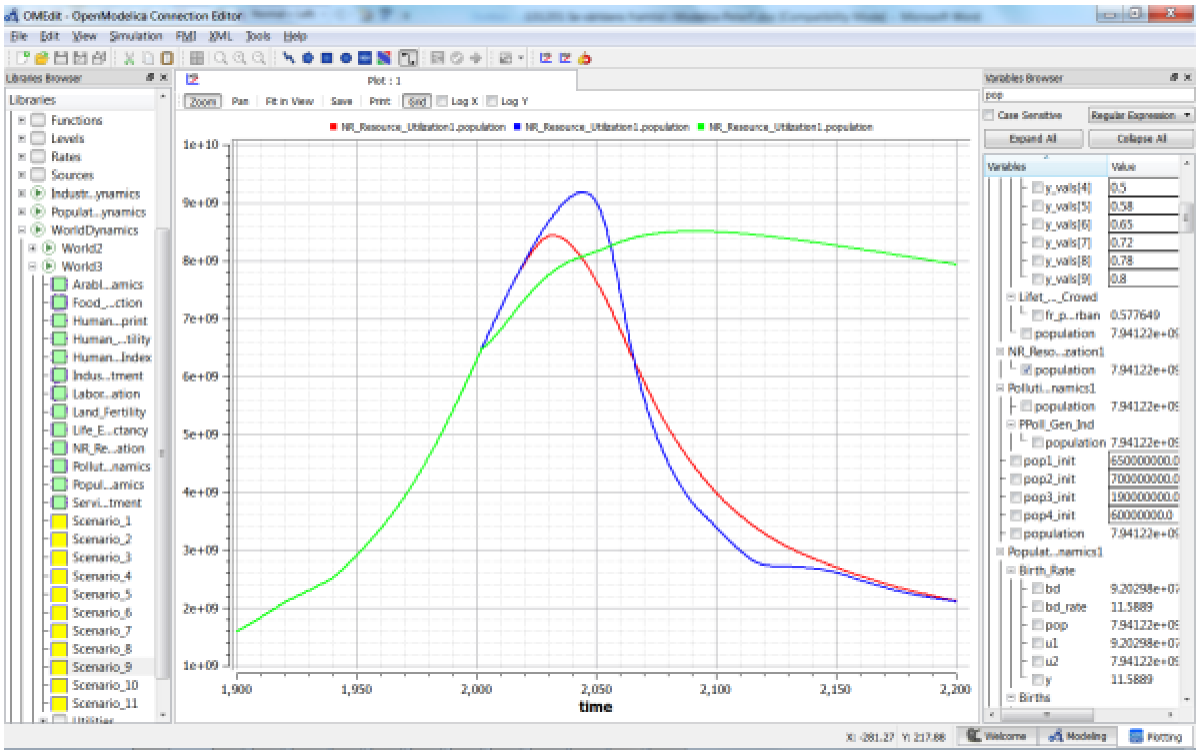
Attitude control for satellites using magnetic coils as actuators

Torque generation mechanism: interaction between coils and geomagnetic field

Courtesy of Francesco Casella, Politecnico di Milano, Italy

System Dynamics – World Society Simulation

Limits to Material Growth; Population, Energy and Material flows



Left. World3 simulation with OpenModelica

- 2 collapse scenarios (close to current developments)
- 1 sustainable scenario (green).

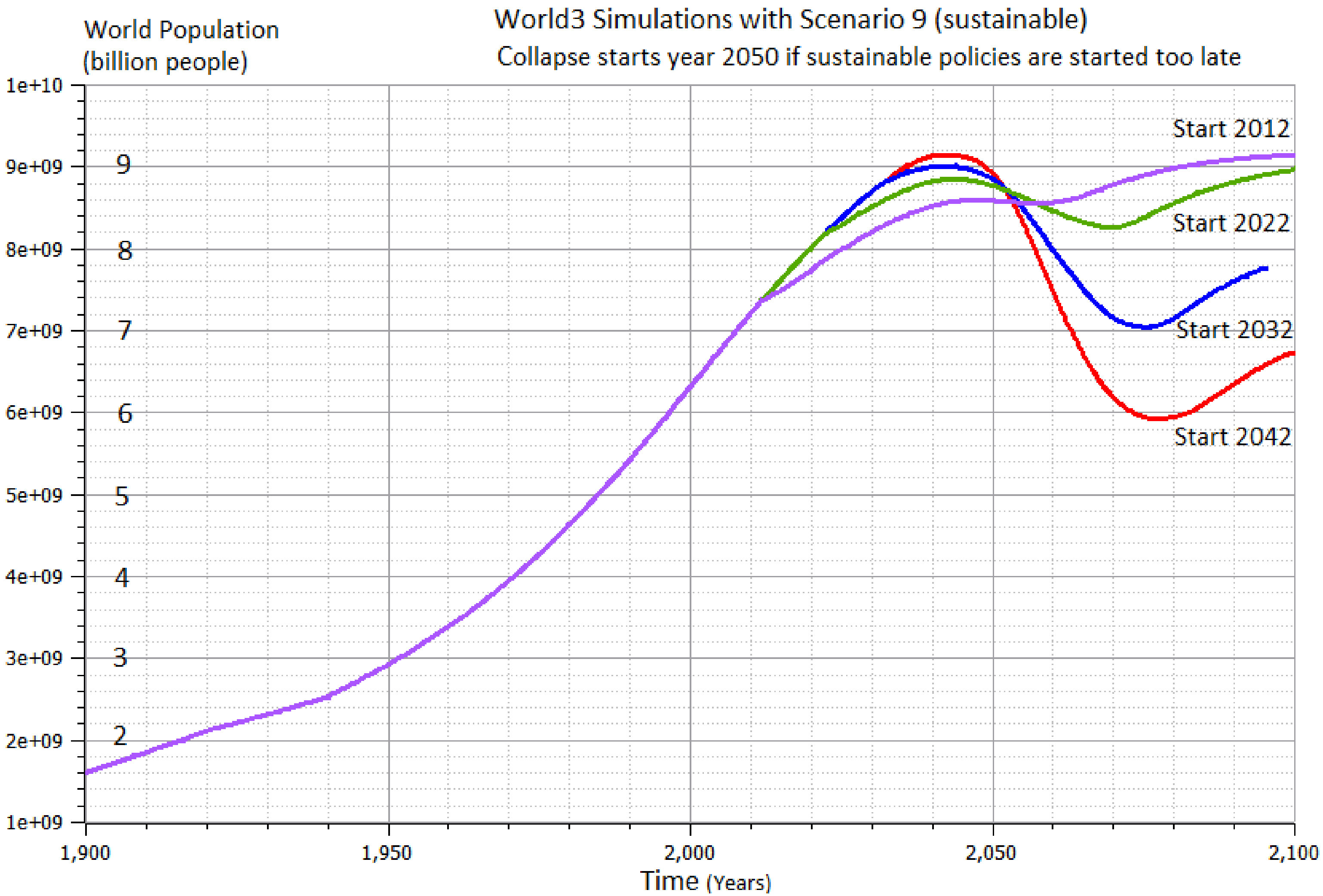
CO2 Emissions per person:

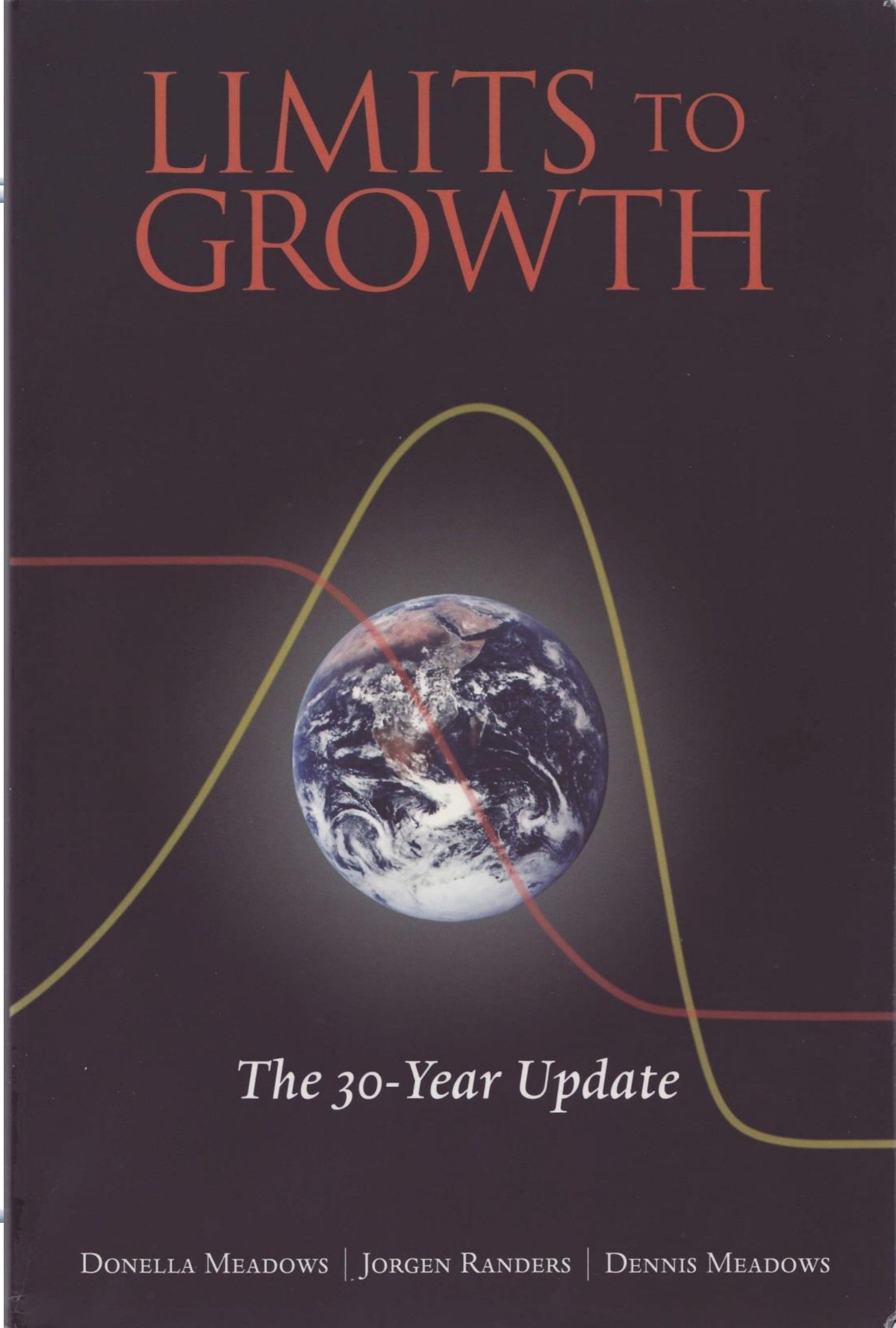
- USA 17 ton/yr
- Sweden 7 ton/yr
- India 1.4 ton/yr
- Bangladesh 0.3 ton/yr

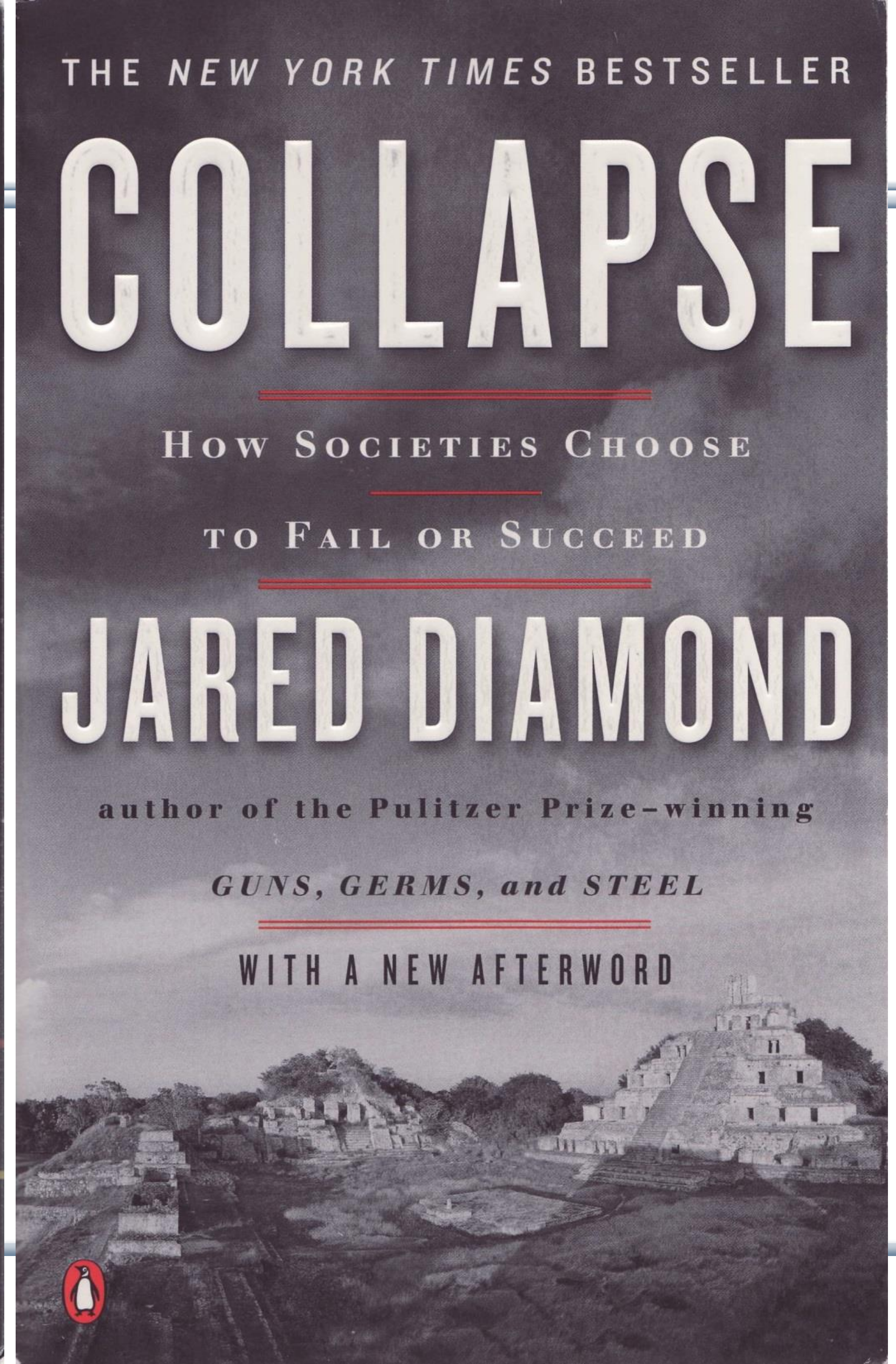
- System Dynamics Modelica library by Francois Cellier (ETH), et al in OM distribution.
- Warming converts many agriculture areas to deserts (USA, Europe, India, Amazonas)
- Ecological breakdown around 2080-2100, drastic reduction of world population
- To **avoid** this: Need for massive investments in sustainable technology and renewable energy sources

MODELICA

World3 Simulations with Different Start Years for Sustainable Policies – Collapse if starting too late




LIMITS TO GROWTH
The 30-Year Update
DONELLA MEADOWS | JORGEN RANDERS | DENNIS MEADOWS


THE NEW YORK TIMES BESTSELLER
COLLAPSE
HOW SOCIETIES CHOOSE
TO FAIL OR SUCCEED
JARED DIAMOND
author of the Pulitzer Prize-winning
GUNS, GERMS, and STEEL
WITH A NEW AFTERWORD

Example Electric Cars
Can be charged by electricity from own solar panels

Renault ZOE; 5 seat; Range:
22kw (2014) vs 40 kw battery (2017)

- EU-drive cycle 210 km, now 400 km
- Realistic Swedish drive cycle:
- Summer: 165 km, now 300 km
- Winter: 110 km, now 200 km

Cheap fast AC chargers (22kw, 43kw)

Tesla model S
range 480 km

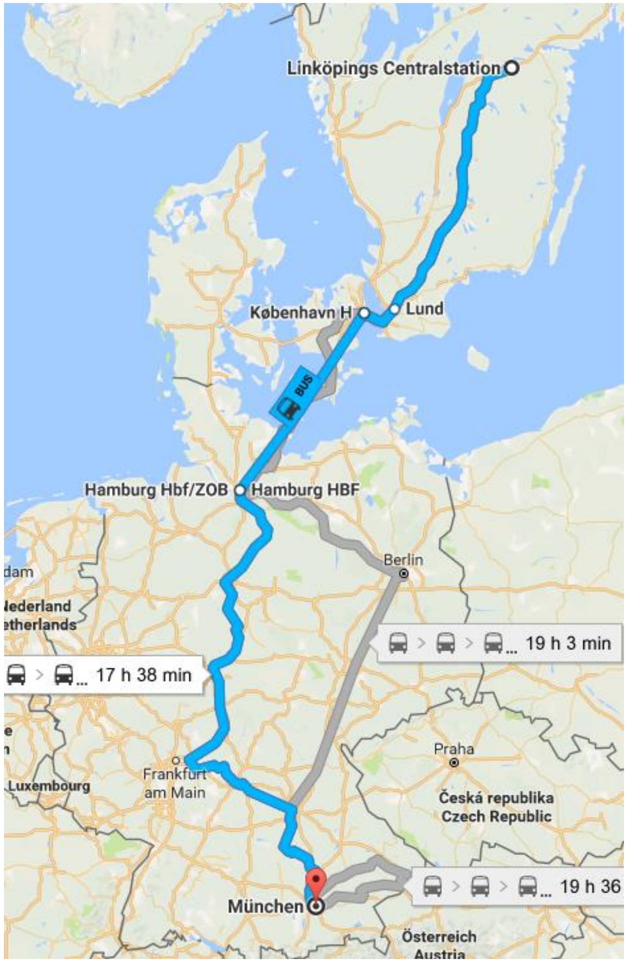
DLR ROboMObil
- experimental electric car
- Modelica models

What Can You Do?
More Train Travel – Less Air Travel

- Air travel by Swedish Citizens – about the same emissions as all personal car traffic in Sweden!
- By train from Linköping to Munich and back – saves almost 1 ton of CO_2e emissions compared to flight
- Leave Linköping 07.00 in Munich 23.14

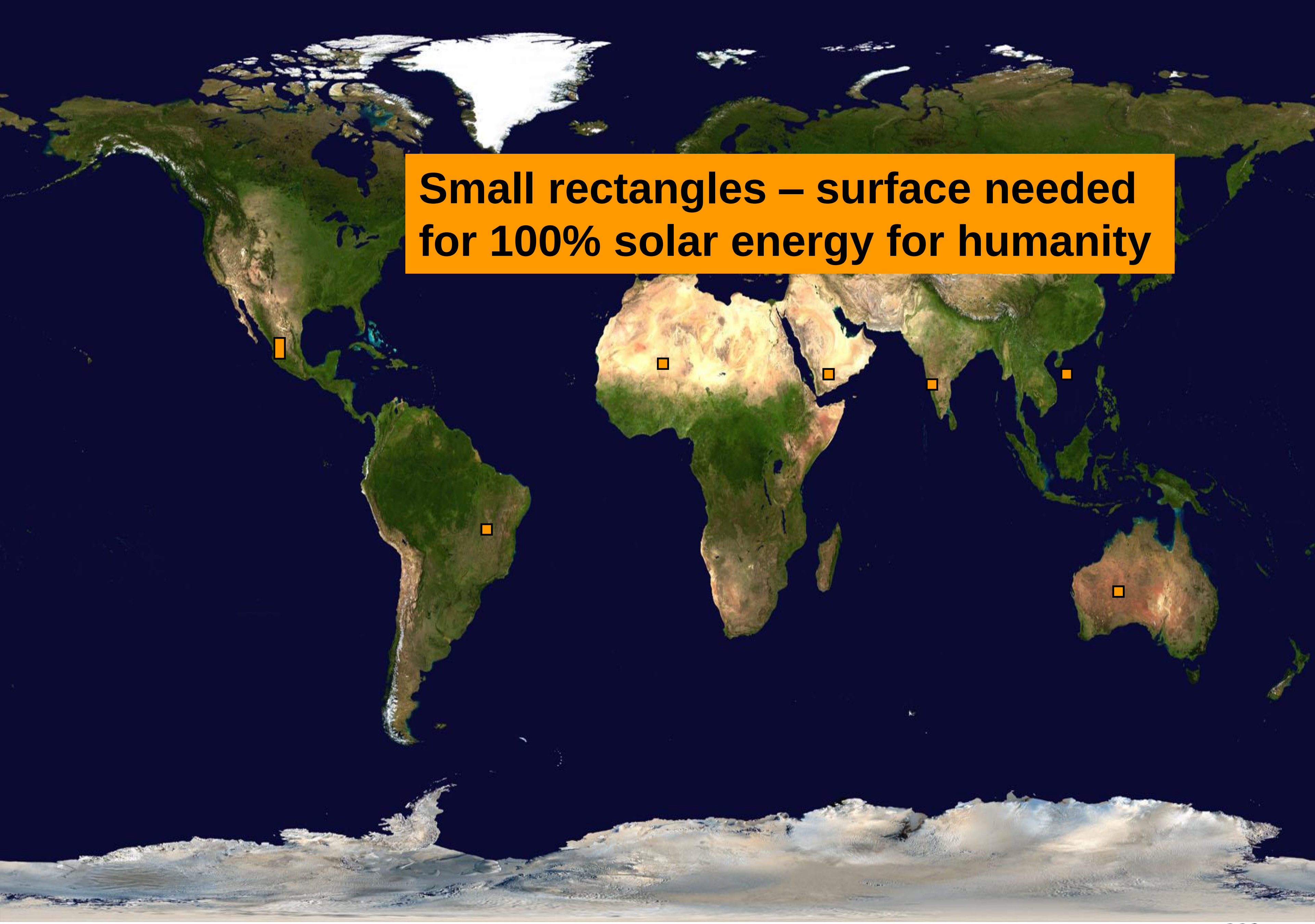
More Examples, PF travel 2016:

- Train Linköping-Paris, Dec 3-6, EU project meeting
- Train Linköping-Dresden, Dec 10-16, 1 week workshop



Train travel Linköping - Munich

Small rectangles – surface needed for 100% solar energy for humanity



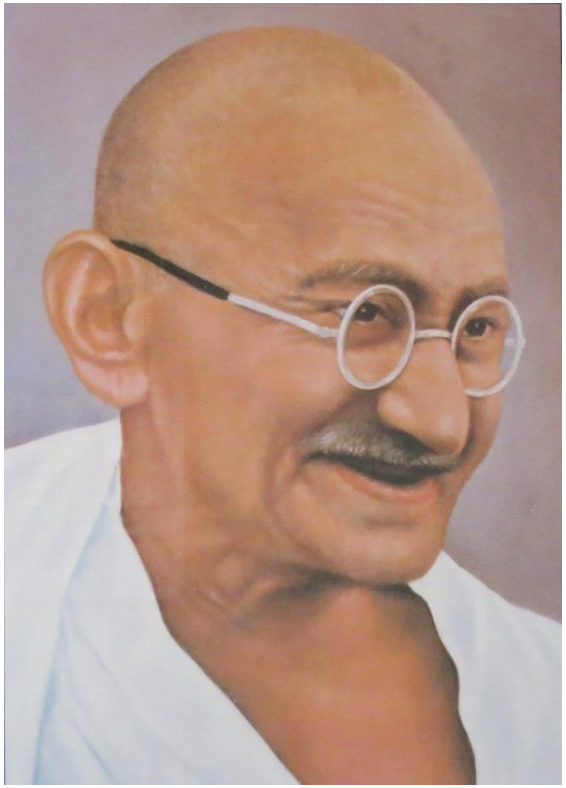
Sustainable Society Necessary for Human Survival

Almost Sustainable

- India, recently 1.4 ton C02/person/year
- Healthy vegetarian food
- Small-scale agriculture
- Small-scale shops
- Simpler life-style (Mahatma Gandhi)

Non-sustainable

- USA 17 ton CO_2, Sweden 7 ton CO_2/yr
- High meat consumption (1 kg beef uses ca 4000 L water for production)
- Hamburgers, unhealthy , includes beef
- Energy-consuming mechanized agriculture
- Transport dependent shopping centres
- Stressful materialistic lifestyle



Gandhi – role model for future less materialistic life style

Brief Modelica History

- First Modelica design group meeting in fall 1996
  - International group of people with expert knowledge in both language design and physical modeling
  - Industry and academia
- Modelica Versions
  - 1.0 released September 1997
  - 2.0 released March 2002
  - 2.2 released March 2005
  - 3.0 released September 2007
  - 3.1 released May 2009
  - 3.2 released March 2010
  - 3.3 released May 2012
  - 3.2 rev 2 released November 2013
  - 3.3 rev 1 released July 2014
  - 3.4 planned spring 2017
- Modelica Association established 2000 in Linköping
  - Open, non-profit organization

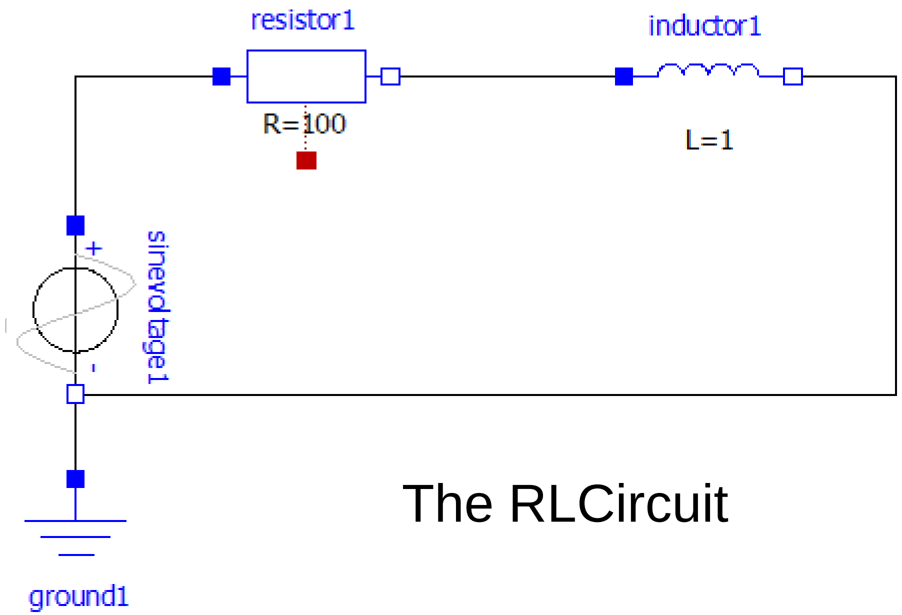
Modelica Conferences

- The 1st International Modelica conference October, 2000
- The 2nd International Modelica conference March 18-19, 2002
- The 3rd International Modelica conference November 5-6, 2003 in Linköping, Sweden
- The 4th International Modelica conference March 6-7, 2005 in Hamburg, Germany
- The 5th International Modelica conference September 4-5, 2006 in Vienna, Austria
- The 6th International Modelica conference March 3-4, 2008 in Bielefeld, Germany
- The 7th International Modelica conference Sept 21-22, 2009 in Como, Italy
- The 8th International Modelica conference March 20-22, 2011 in Dresden, Germany
- The 9th International Modelica conference Sept 3-5, 2012 in Munich, Germany
- The 10th International Modelica conference March 10-12, 2014 in Lund, Sweden
- The 11th International Modelica conference Sept 21-23, 2015 in Versailles, Paris
- The 12th International Modelica conference planned May 15-17, 2017 in Prague, Czech Republic

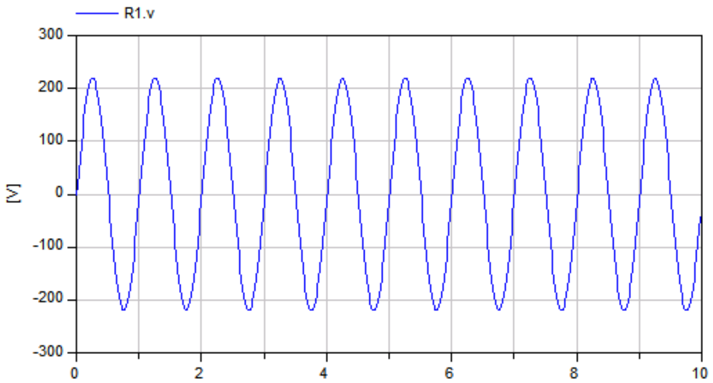
Exercises Part I
Hands-on graphical modeling
(15 minutes)

Exercises Part I – Basic Graphical Modeling

- (*See instructions on next two pages*)
- Start the OMEdit editor (part of OpenModelica)
- Draw the RLCircuit
- Simulate



The RLCircuit



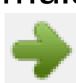
Simulation

Exercises Part I – OMEdit Instructions (Part I)

- Start OMEdit from the Program menu under OpenModelica
- Go to **File** menu and choose **New**, and then select **Model**.
- E.g. write *RLCircuit* as the model name.
- For more information on how to use OMEdit, go to **Help** and choose **User Manual** or press **F1**.

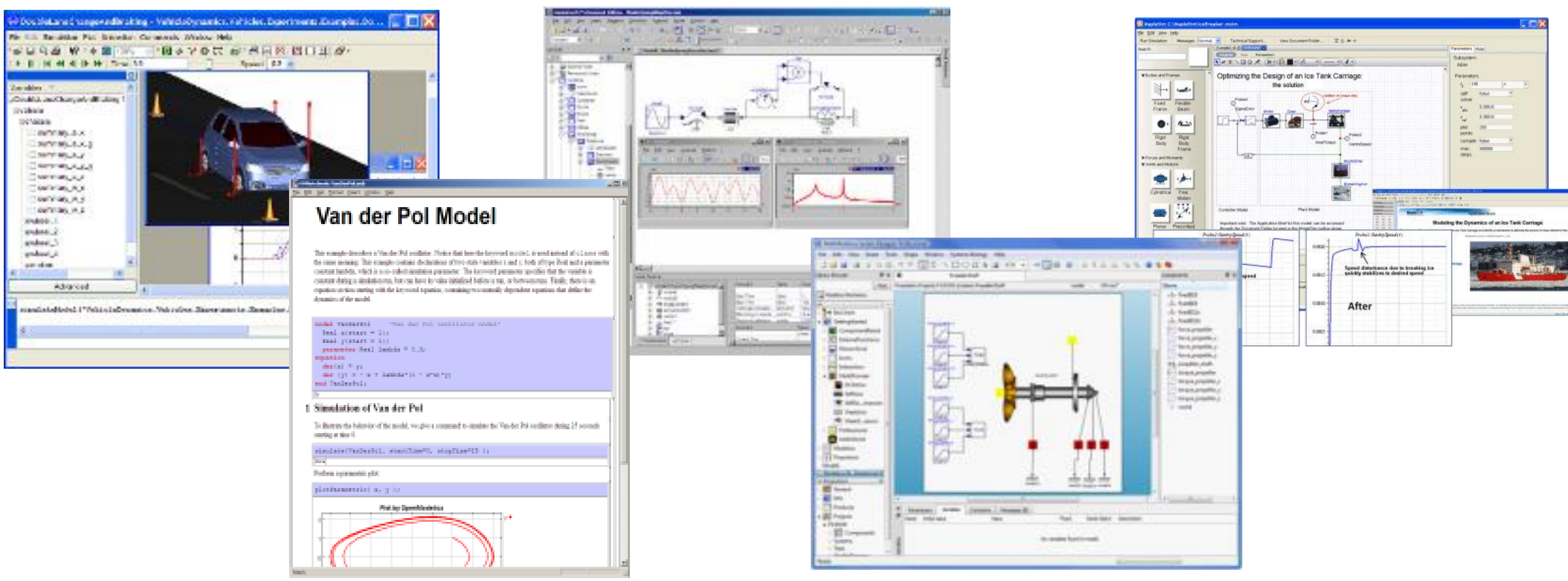
- Under the **Modelica Library:**
  - Contains The standard Modelica library components
  - The **Modelica files** contains the list of models you have created.

Exercises Part I – OMEdit Instructions (Part II)

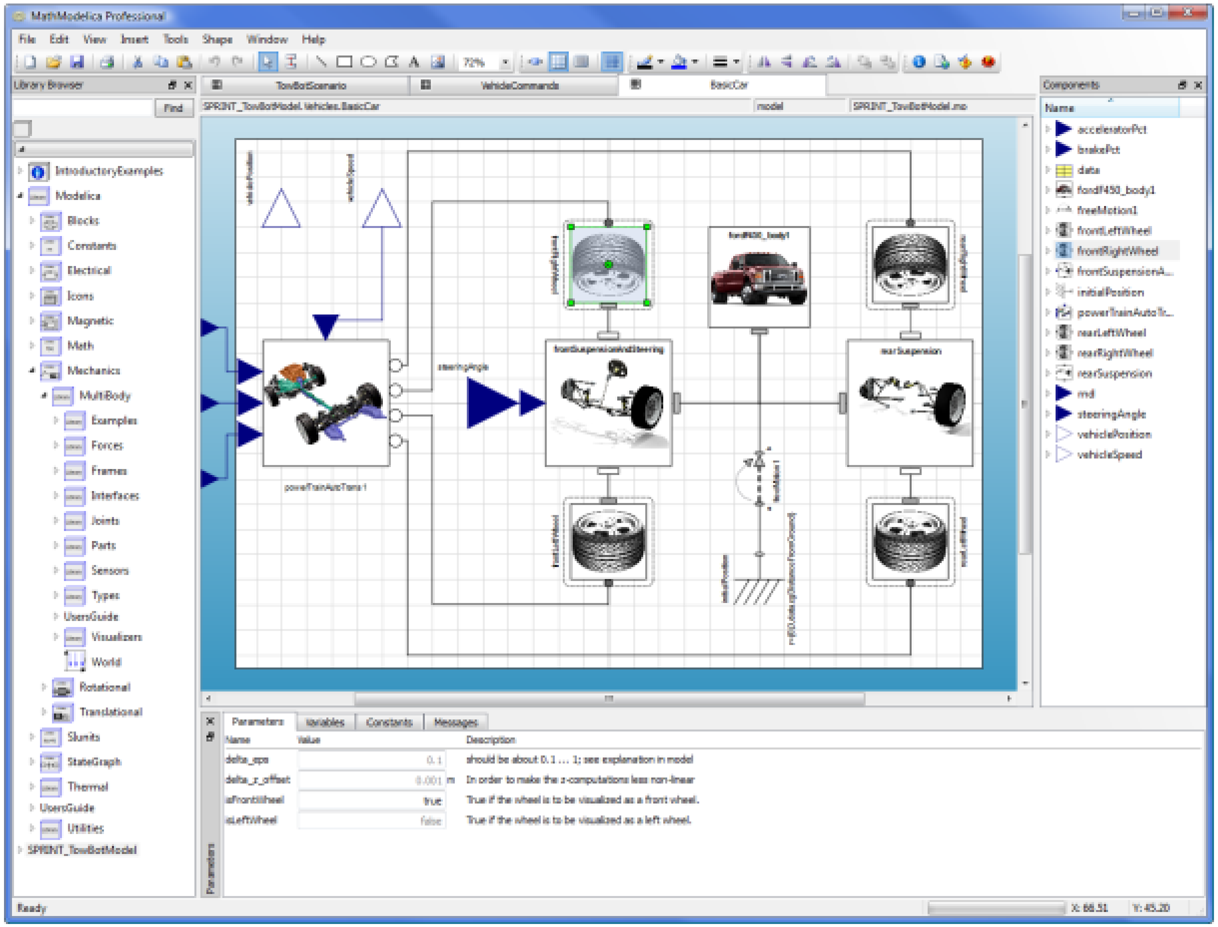
- For the RLCircuit model, browse the Modelica standard library and add the following component models:
  - Add `Ground`, `Inductor` and `Resistor` component models from Modelica.Electrical.Analog.Basic package.
  - Add SineVoltage component model from Modelica.Electrical.Analog.Sources package.
- Make the corresponding connections between the component models as shown in slide 38.
- Simulate the model
  - Go to Simulation menu and choose simulate or click on the simulate button in the toolbar. 
- Plot the instance variables
  - Once the simulation is completed, a plot variables list will appear on the right side. Select the variable that you want to plot.

Part II

Modelica environments and OpenModelica



Wolfram System Modeler – Wolfram MathCore

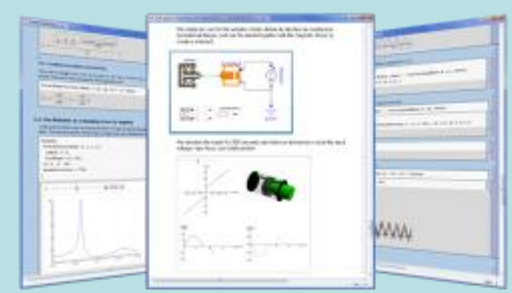


Car model graphical view

Courtesy Wolfram Research

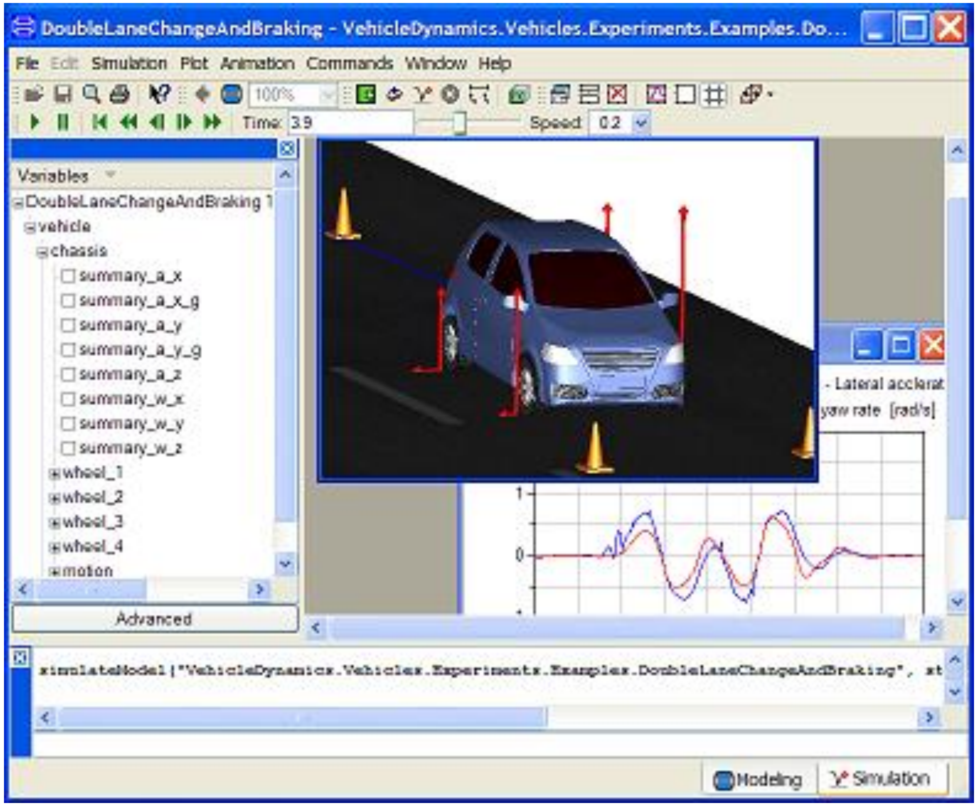
- Wolfram Research
- USA, Sweden
- General purpose
- Mathematica integration
- www.wolfram.com
- www.mathcore.com

Mathematica



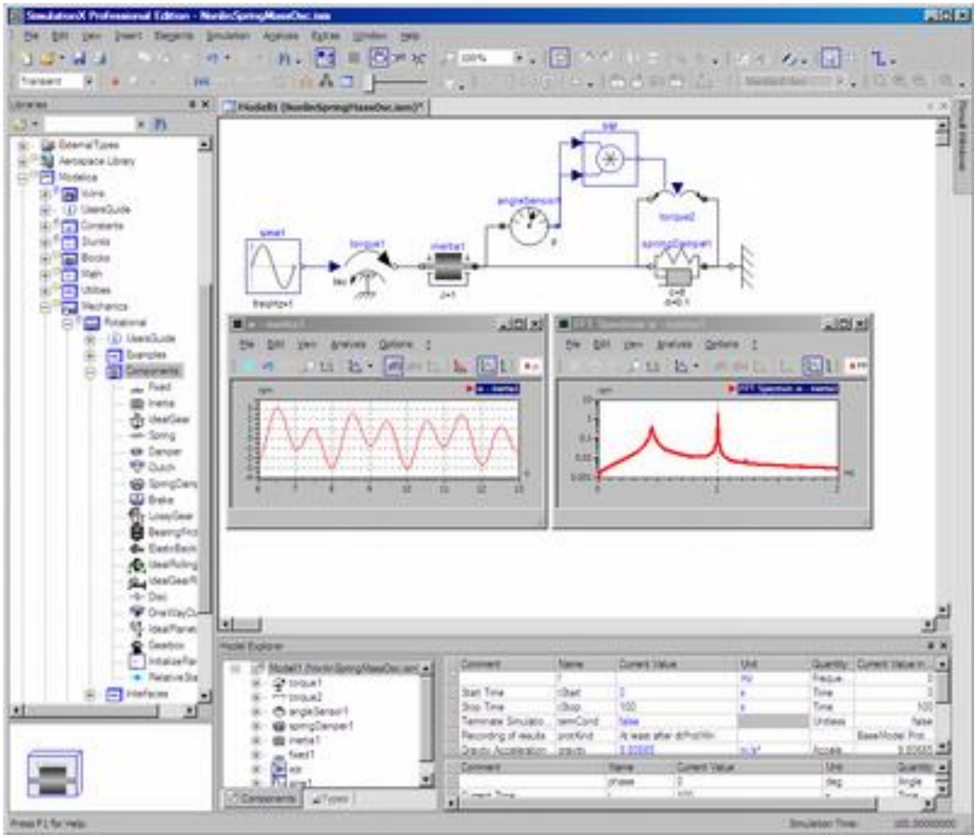
Simulation and analysis

Dymola



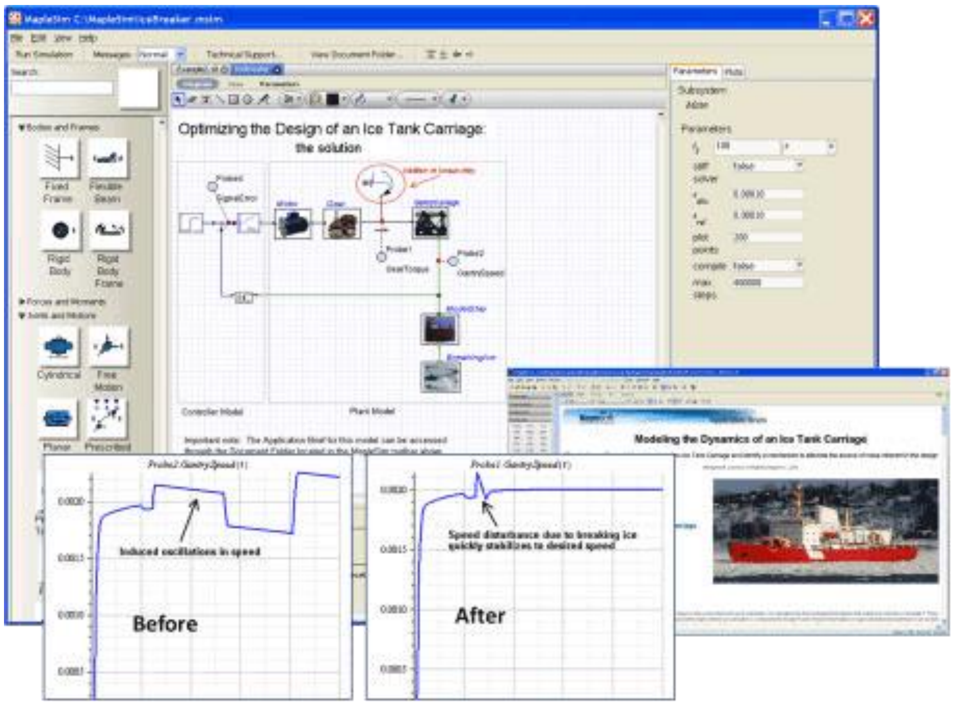
- Dassault Systemes Sweden
- Sweden
- First Modelica tool on the market
- Initial main focus on automotive industry
- www.dymola.com

Simulation X



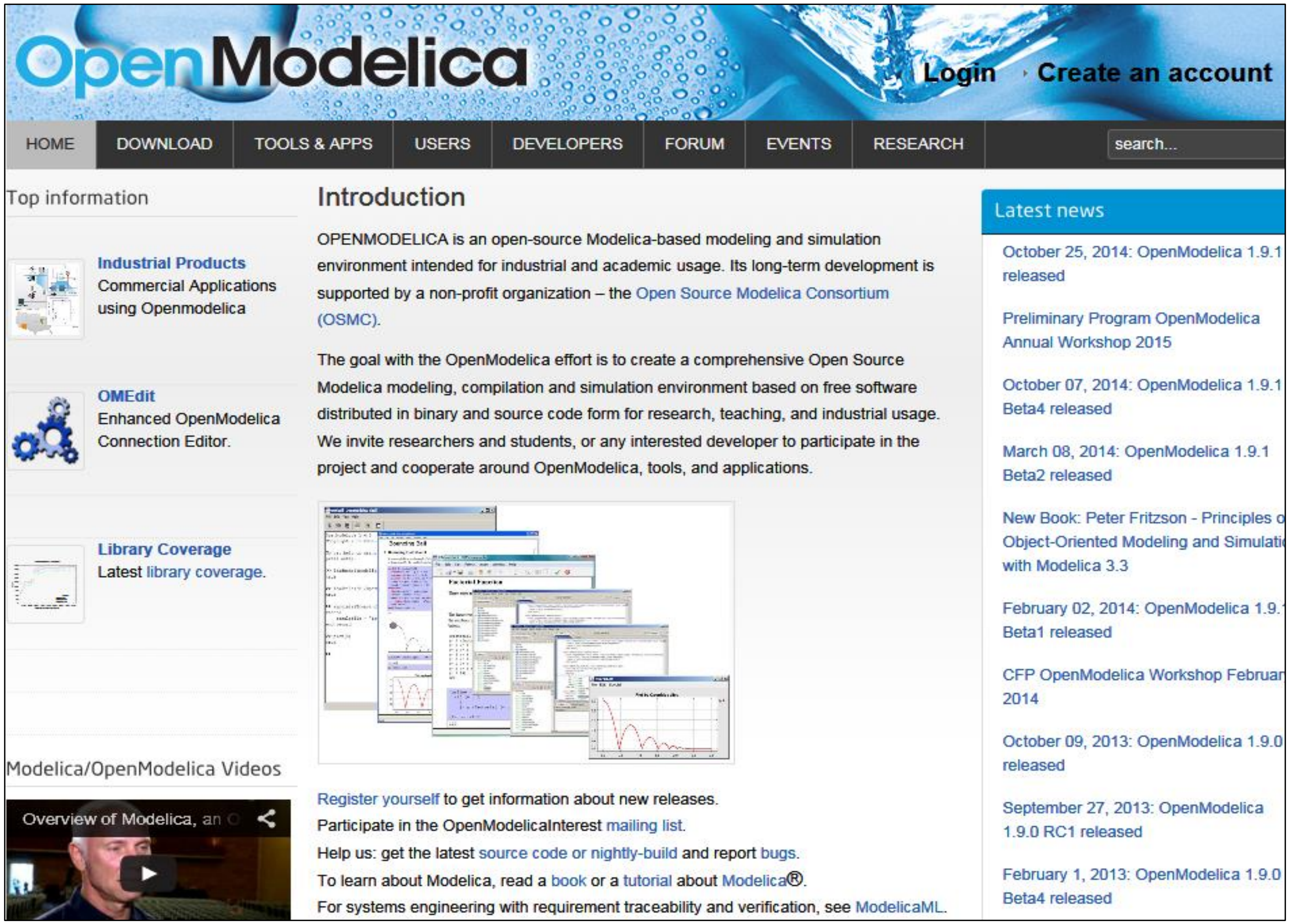
- ITI Gmbh (Just bought by ESI Group)
- Germany
- Mechatronic systems
- www.simulationx.com

MapleSim



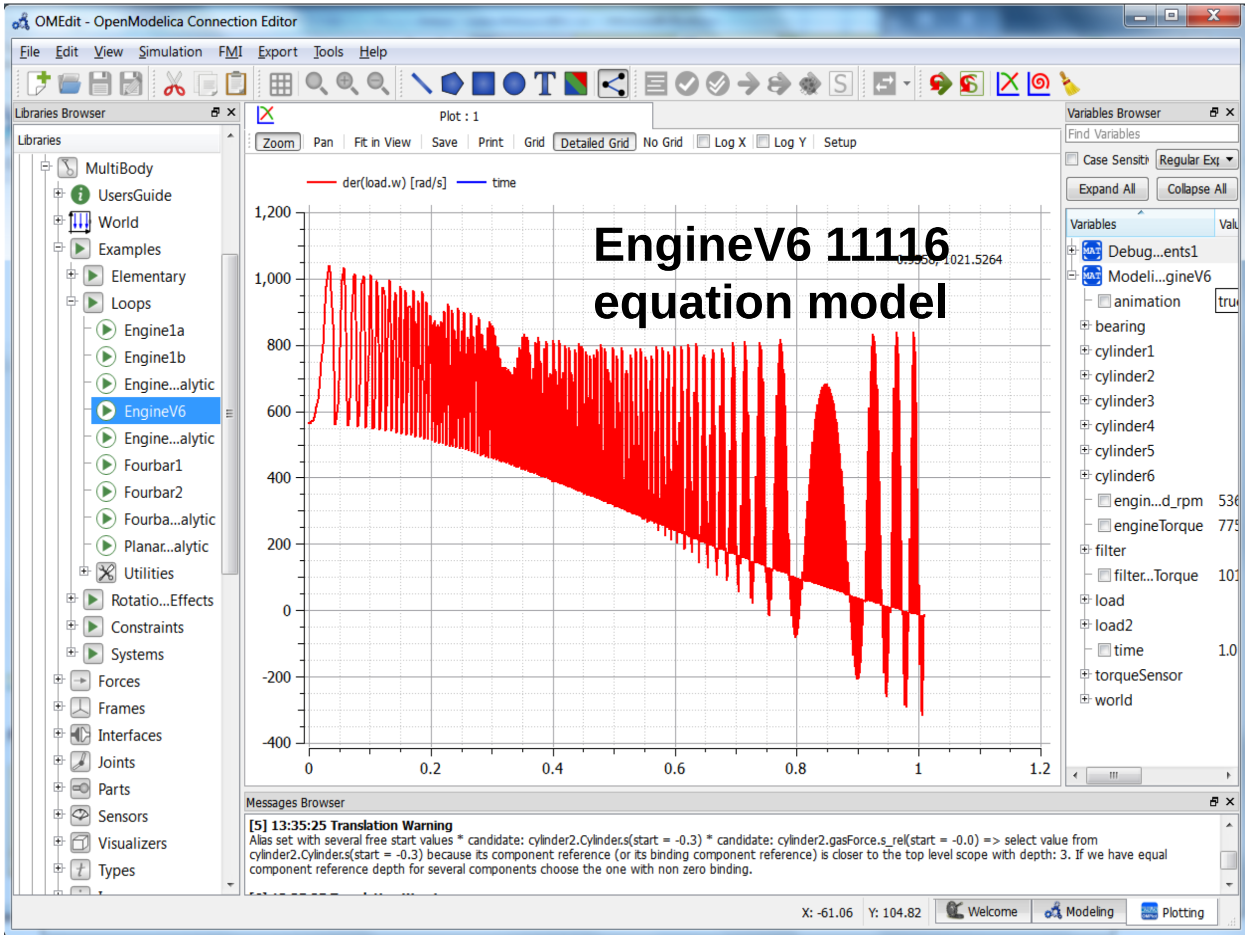
- Maplesoft
- Canada
- Recent Modelica tool on the market
- Integrated with Maple
- www.maplesoft.com

The OpenModelica Environment
www.OpenModelica.org



OpenModelica – Free Open Source Tool
developed by the Open Source Modelica Consortium (OSMC)

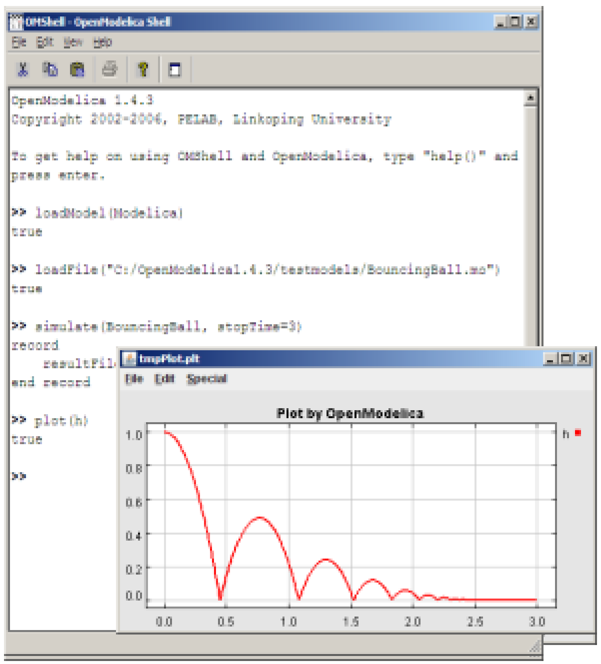
- Graphical editor
- Model compiler and simulator
- Debugger
- Performance analyzer
- Dynamic optimizer
- Symbolic modeling
- Parallelization
- Electronic Notebook and OMWebbook for teaching
- Spokentutorial for teaching

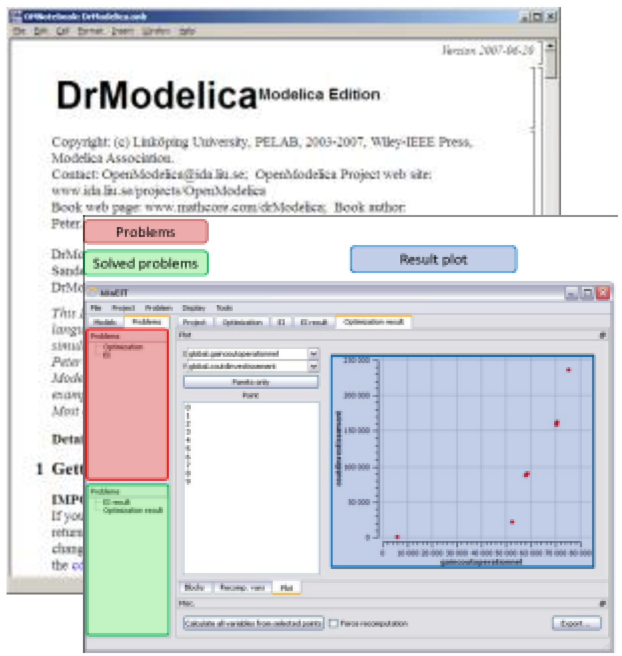


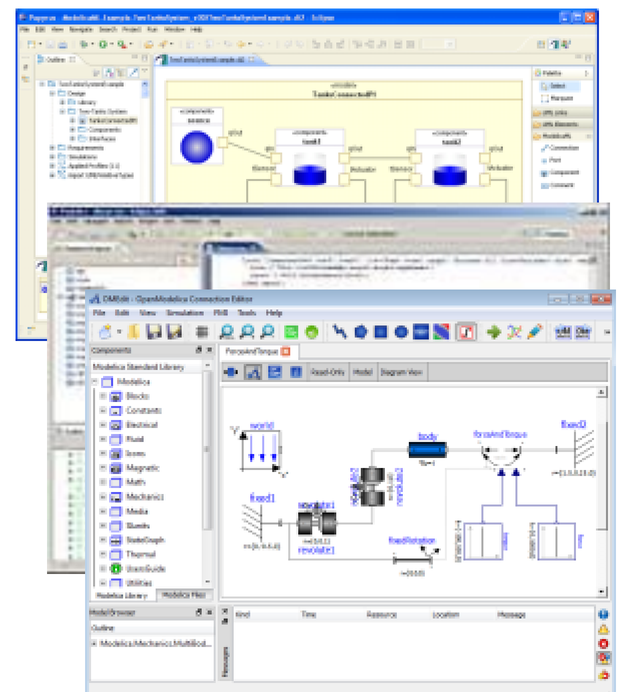
The OpenModelica Open Source Environment
www.openmodelica.org

- Advanced Interactive Modelica compiler (OMC)
  - Supports most of the Modelica Language
  - **Modelica** and **Python scripting**
- Basic environment for creating models
  - **OMShell** – an interactive command handler
  - **OMNotebook** – a literate programming notebook
  - **MDT** – an advanced textual environment in Eclipse

- **OMEdit** graphic Editor
- **OMDebugger** for equations
- **OMOptim** optimization tool
- **OM Dynamic optimizer** collocation
- **ModelicaML** UML Profile
- **MetaModelica** extension
- **ParModelica** extension







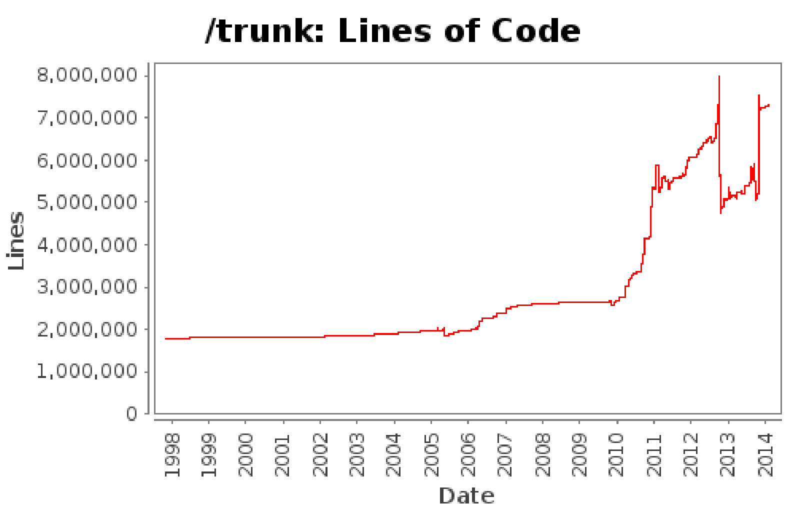
OSMC – International Consortium for Open Source Model-based Development Tools, 46 members Dec 2016

Founded Dec 4, 2007

Open-source community services

- **Website and Support Forum**
- **Version-controlled source base**
- **Bug database**
- **Development courses**
- **www.openmodelica.org**

Code Statistics



Industrial members

- **ABB AB, Sweden**
- **Bosch Rexroth AG, Germany**
- **Brainheart Energy AB, Sweden**
- **Siemens Turbo, Sweden**
- **CDAC Centre, Kerala, India**
- **Creative Connections, Prague**
- **DHI, Aarhus, Denmark**
- **Dynamica s.r.l., Cremona, Italy**
- **EDF, Paris, France**
- **Equa Simulation AB, Sweden**
- **Fraunhofer IWES, Bremerhaven**
- **IFPEN, Paris, France**
- **ISID Dentsu, Tokyo, Japan**
- **Maplesoft, Canada**
- **RTE France, Paris, France**
- **Saab AB, Linköping, Sweden**
- **Scilab Enterprises, France**
- **SKF, Göteborg, Sweden**
- **TLK Thermo, Germany**
- **Sozhou Tongyuan, China**
- **VTI, Linköping, Sweden**
- **VTT, Finland**
- **Wolfram MathCore, Sweden**

University members

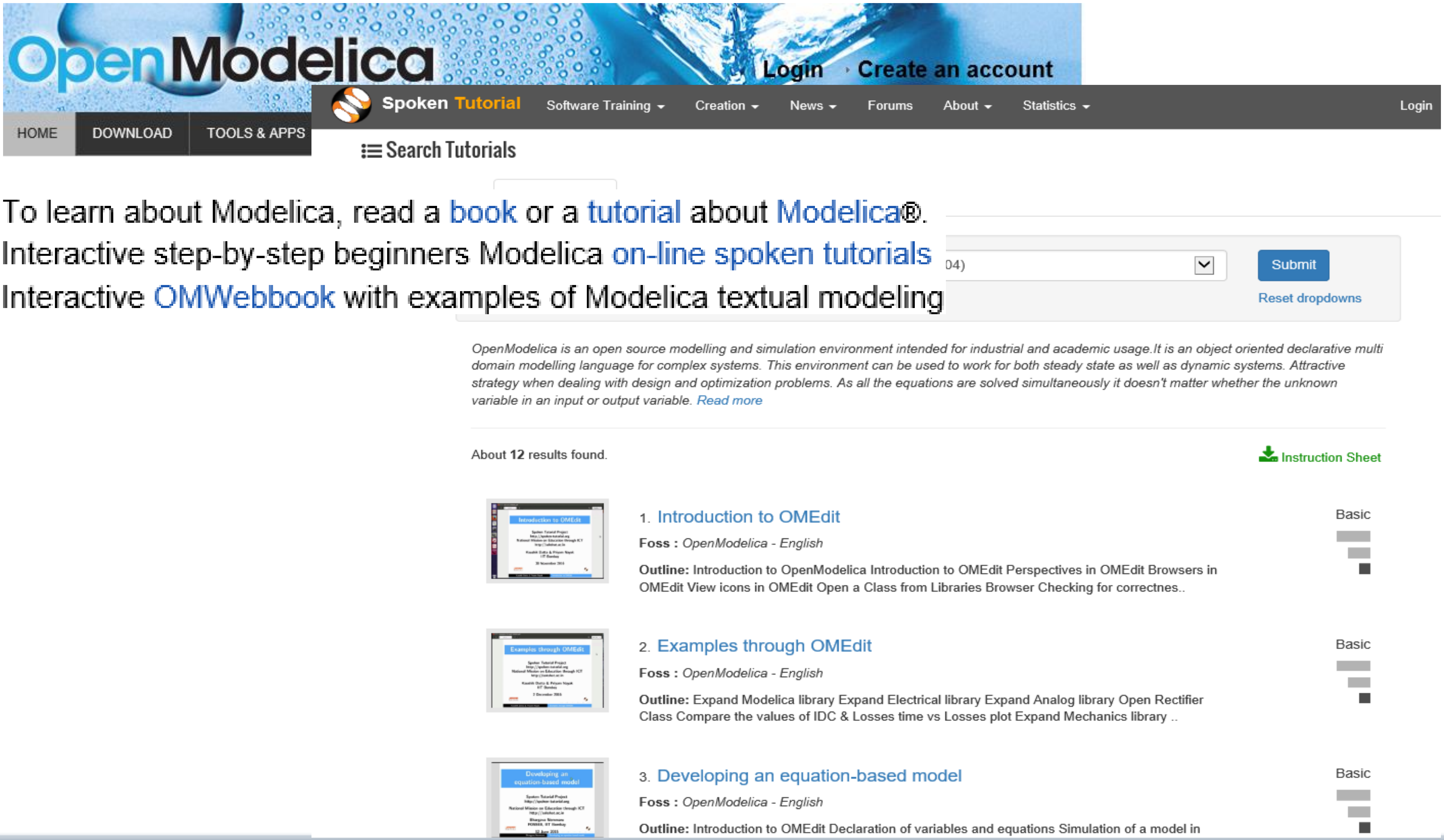
- **FH Bielefeld, Bielefeld, Germany**
- **TU Braunschweig, Germany**
- **University of Calabria, Italy**
- **Univ California, Berkeley, USA**
- **Chalmers Univ Techn, Sweden**
- **TU Dortmund, Germany**
- **TU Dresden, Germany**
- **Université Laval, Canada**
- **Georgia Inst of Technology, USA**
- **Ghent University, Belgium**
- **Halmstad University, Sweden**
- **Heidelberg University, Germany**
- **Linköping University, Sweden**
- **TU Hamburg/Harburg Germany**
- **IIT Bombay, Mumbai, India**
- **KTH, Stockholm, Sweden**
- **Univ of Maryland, Syst Eng USA**
- **Univ of Maryland, CEEE, USA**
- **Politecnico di Milano, Italy**
- **Ecoles des Mines, CEP, France**
- **Mälardalen University, Sweden**
- **Univ Pisa, Italy**
- **StellenBosch Univ, South Africa**
- **Telemark Univ College, Norway**

Interactive OpenModelica Step-by-step Spoken-Tutorial using OMEdit. Link from www.openmodelica.org

To learn about Modelica, read a book or a tutorial about Modelica®.

Interactive step-by-step beginners Modelica on-line spoken tutorials

Interactive OMWebbook with examples of Modelica textual modeling

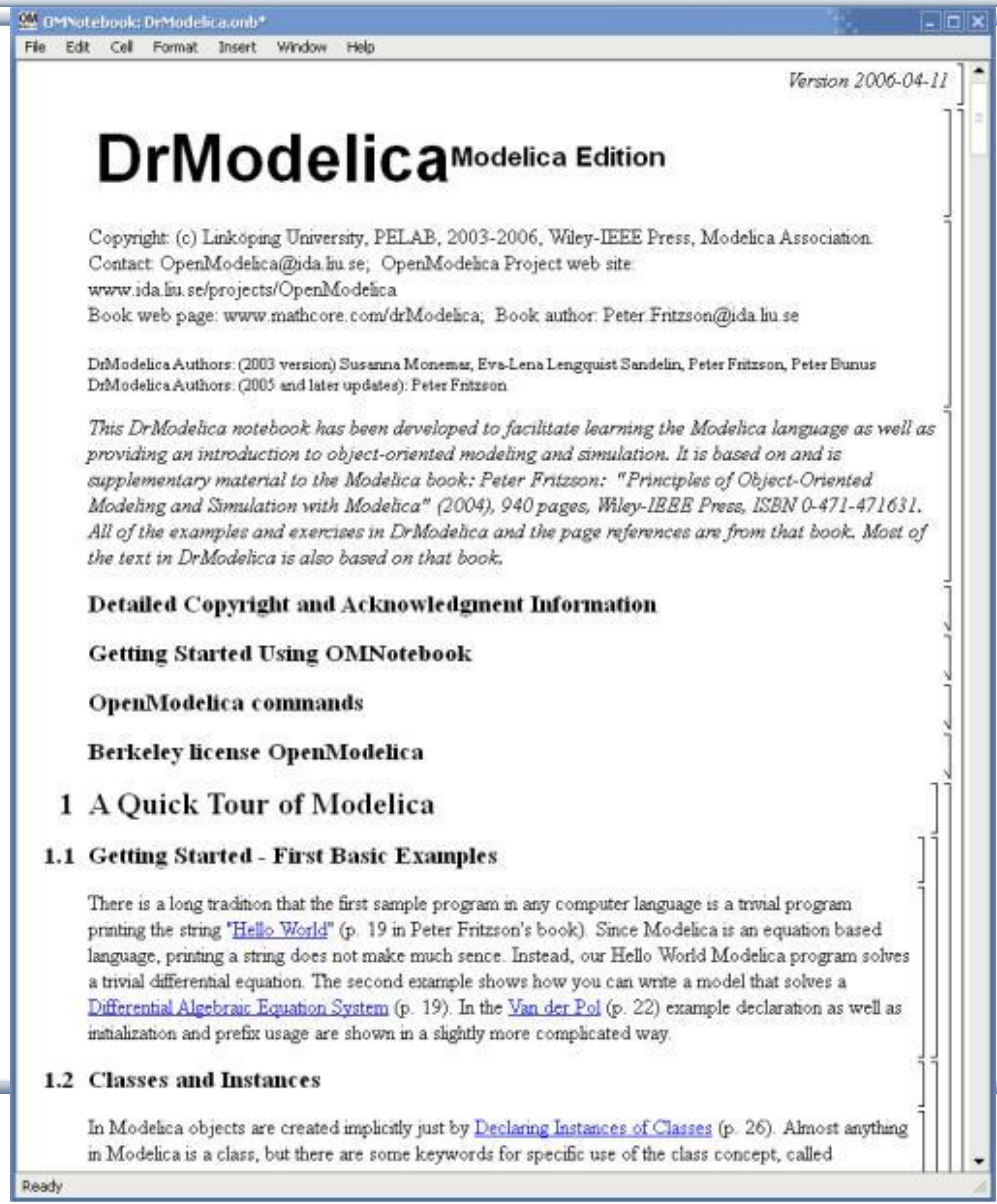


OMNotebook Electronic Notebook with DrModelica

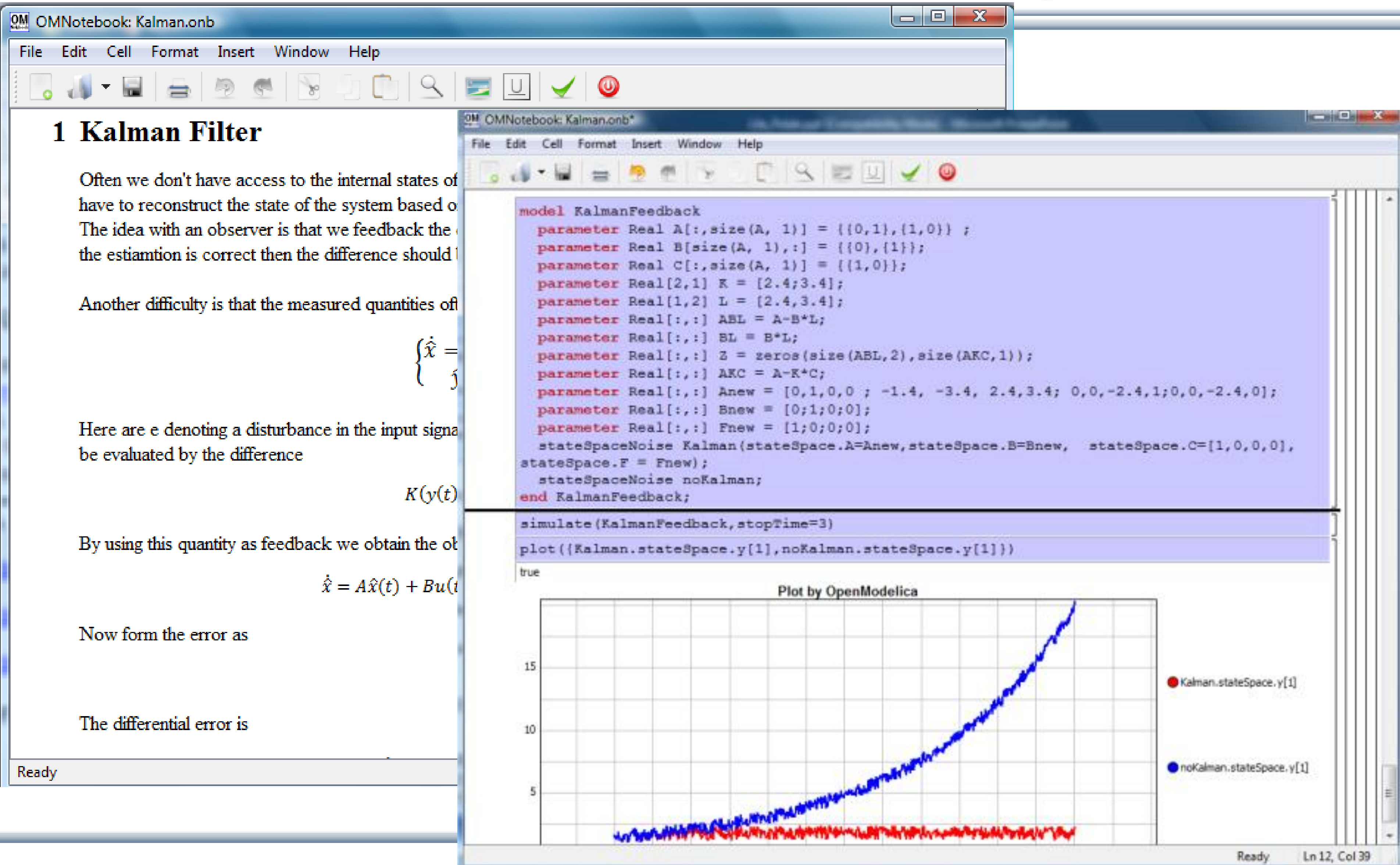
- Primarily for teaching
- Interactive electronic book
- Platform independent

Commands:

- *Shift-return (evaluates a cell)*
- File Menu (open, close, etc.)
- Text Cursor (vertical), Cell cursor (horizontal)
- Cell types: text cells & executable code cells
- Copy, paste, group cells
- Copy, paste, group text
- Command Completion (shift-tab)



OMnotebook Interactive Electronic Notebook Here Used for Teaching Control Theory



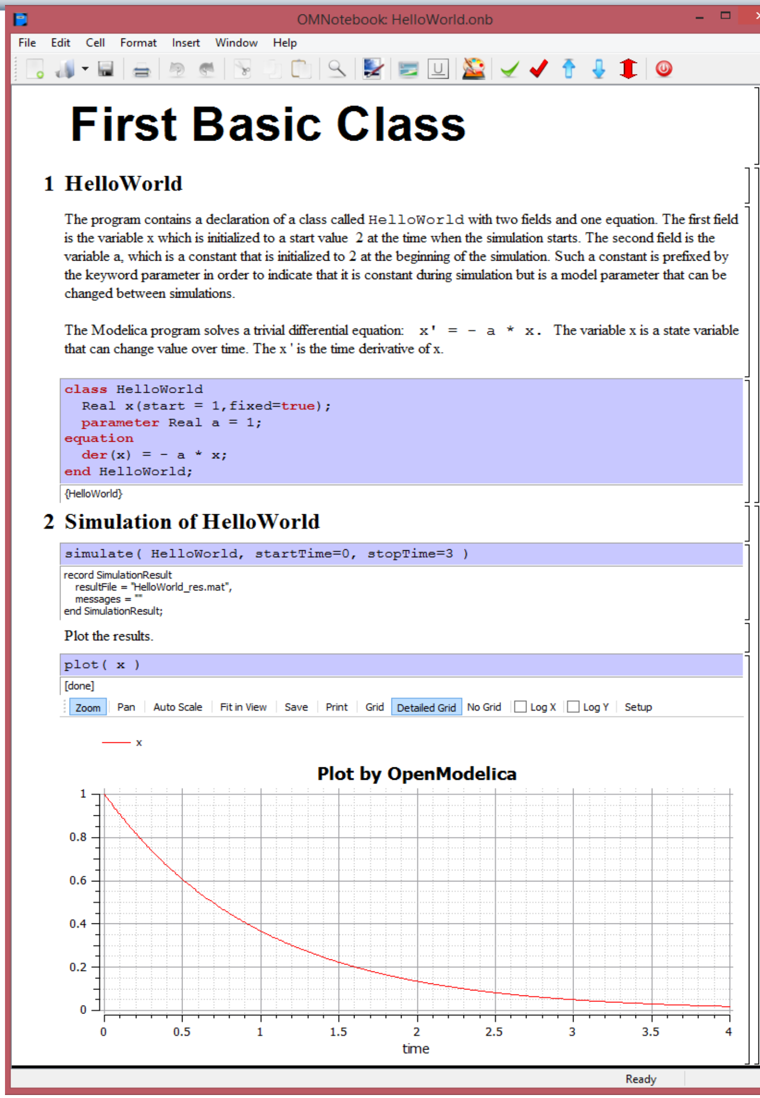
MODELICA

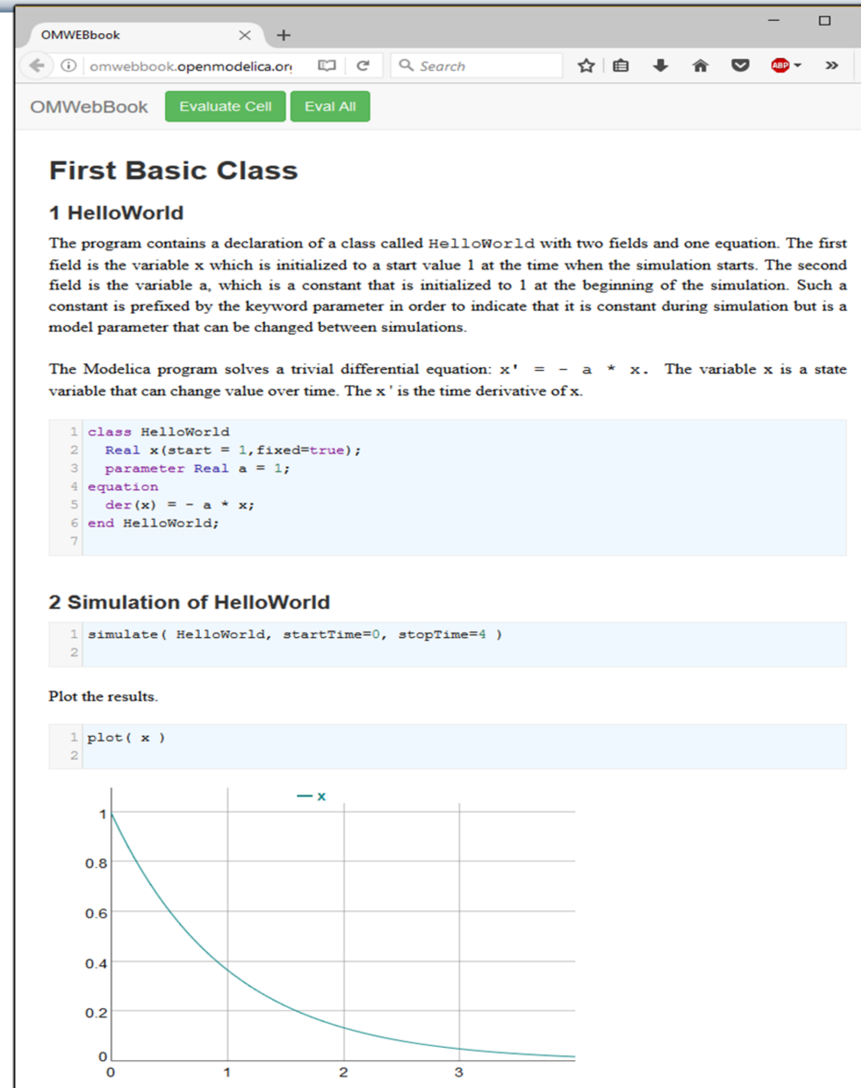
OM Web Notebook Generated from OMNotebook

Edit, Simulate, Plot Models on a Web Page

http://omwebbook.openmodelica.org/

OMNotebook





OMwebbook

BouncingBall Example of Using OMWebbook

Editing and Simulating the BouncingBall model

http://omwebbook.openmodelica.org/static/QuickTour/W

OMWEBbook

OMWebBook | Evaluate Cell | Eval All

```
model BouncingBall            "The bouncing ball model"
  constant Real g = 9.81;        // Gravitational acceleration
  parameter Real c = 0.9;        // Elasticity constant of ball
  parameter Real radius = 0.1;       // Radius of the ball
  Real height(start = 1,fixed=true); // height above ground of ball center
  Real velocity(start = 0,fixed=true);         // Velocity of the ball
equation
  der(height) = velocity;
  der(velocity) = -g;
  when height <= radius then
    reinit(velocity, -c*pre(velocity));
  end when;
end BouncingBall;
```

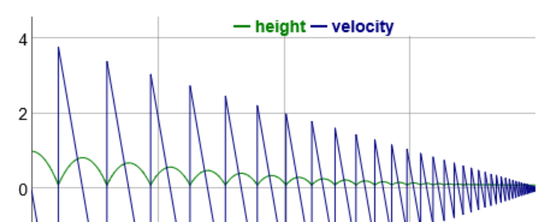
A bouncing ball

2 Simulation 1 of Bouncing Ball

When we simulate the BouncingBall model from 0 to 8 we see how it bounces

```
simulate( BouncingBall, stopTime=8 )
```

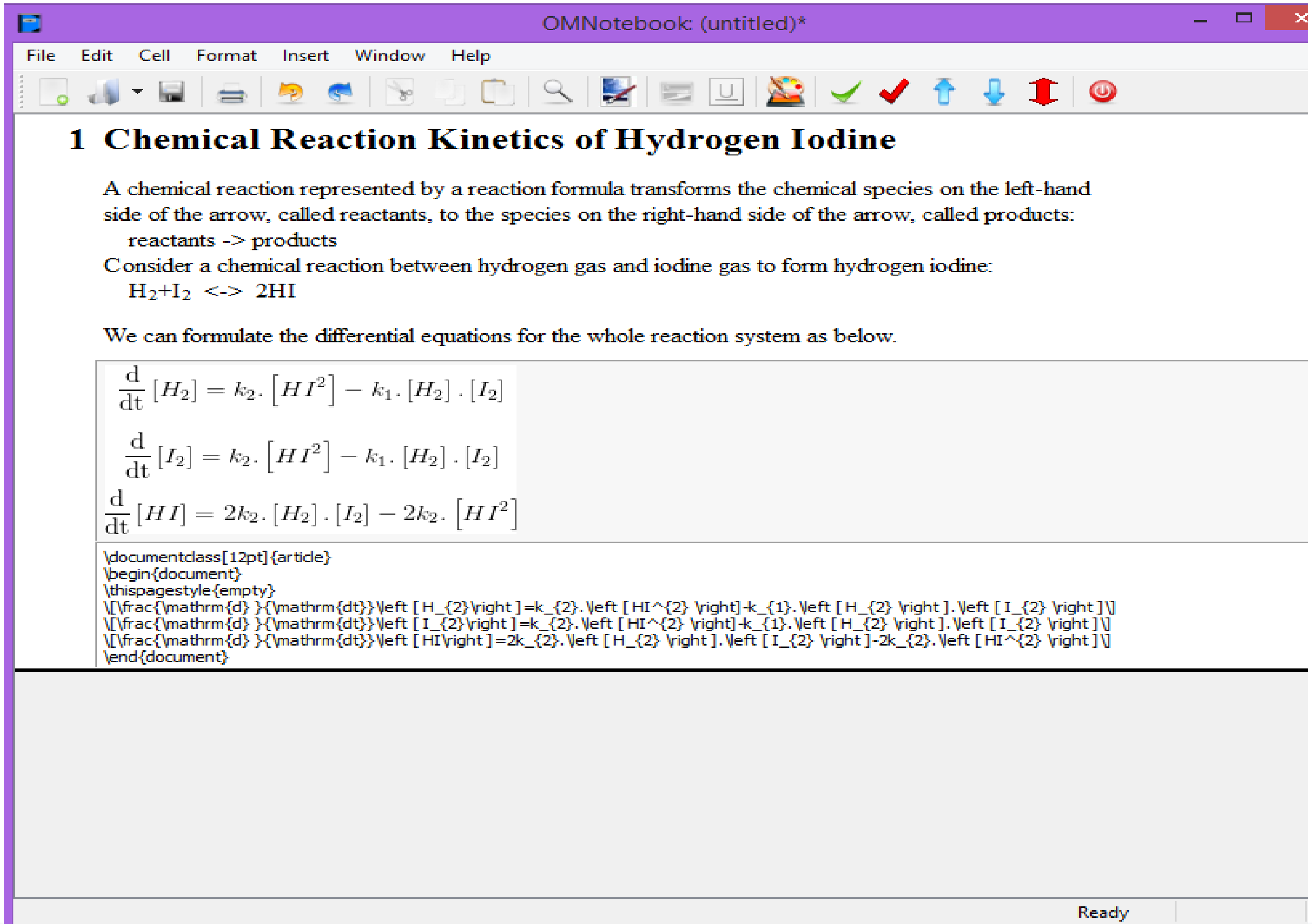
```
plot( { height, velocity } )
```



MODELICA

Mathematical Typesetting in OMNotebook and OMWebbook

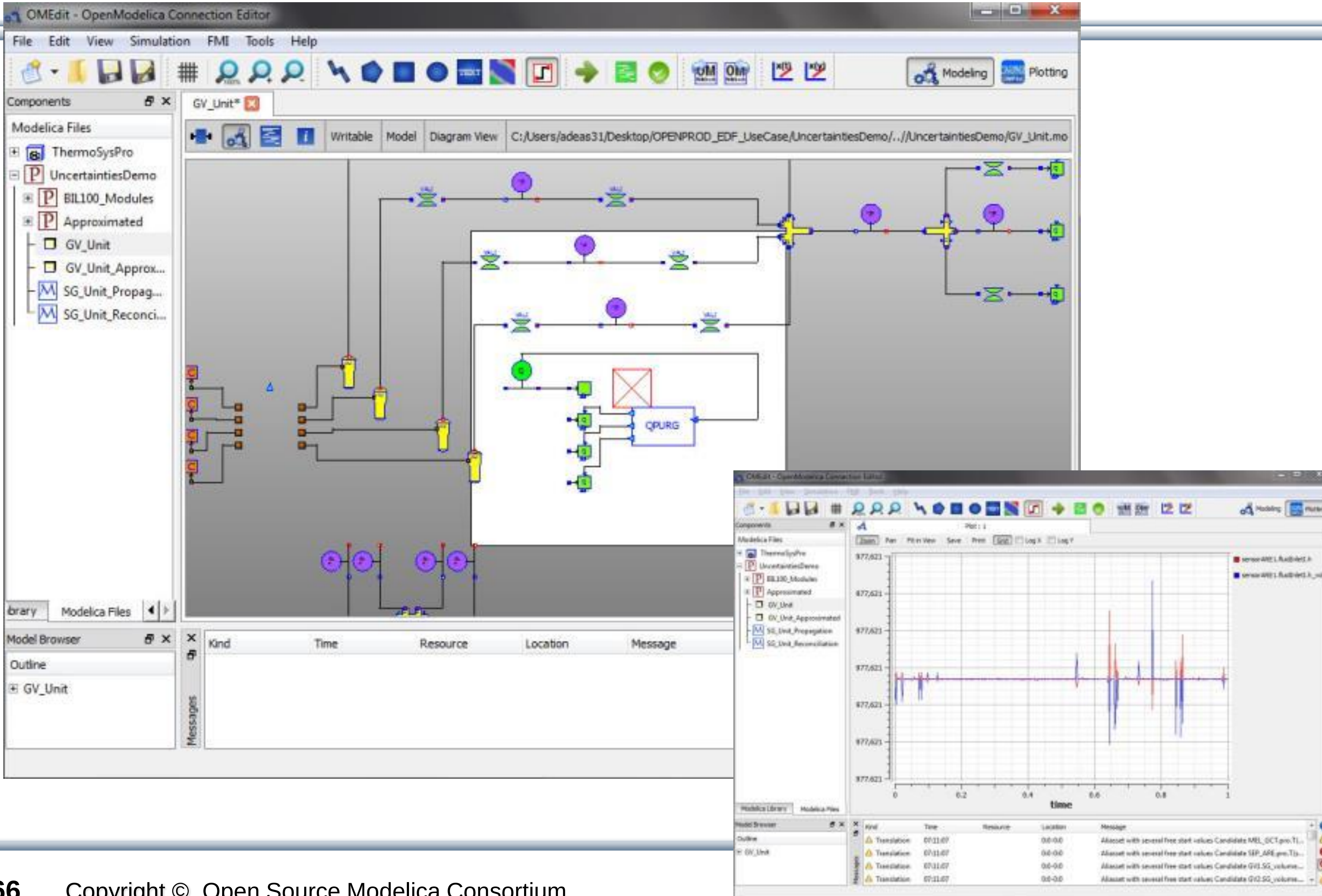
OMNotebook supports Latex formatting for mathematics



Contents in OMWebbook Generated from OMNotebook

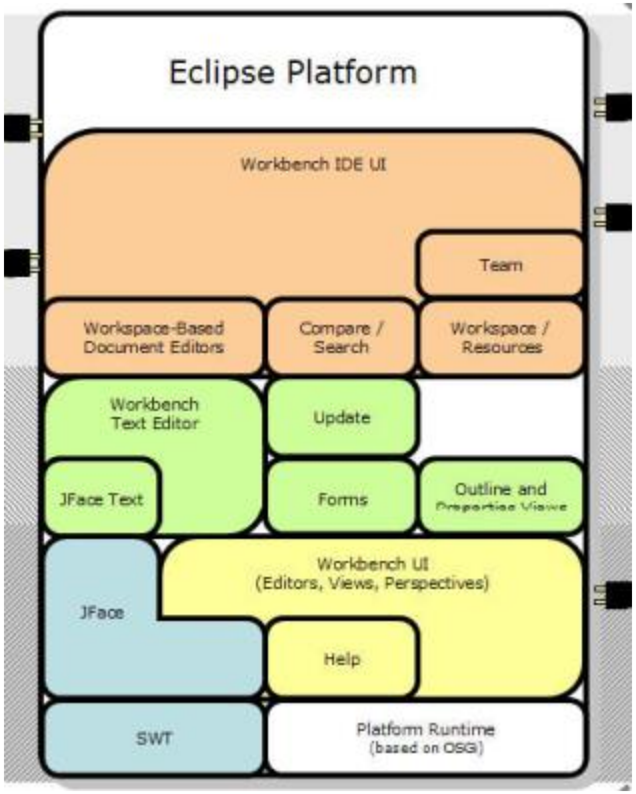
Latex instructions can be hidden by double clicking the Cell in tree view

OpenModelica Environment Demo

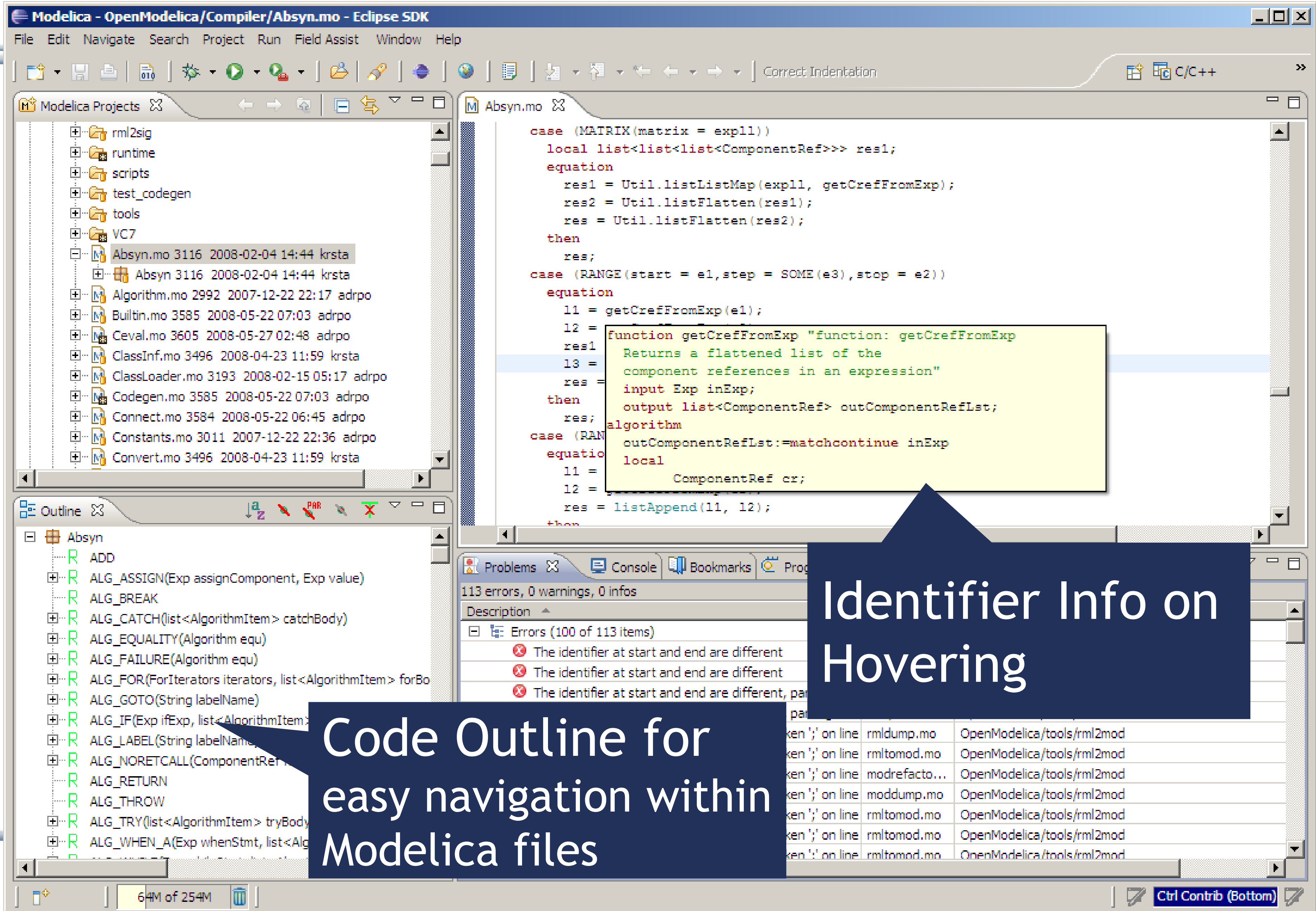


OpenModelica MDT – Eclipse Plugin

- Browsing of packages, classes, functions
- Automatic building of executables; separate compilation
- Syntax highlighting
- Code completion, Code query support for developers
- Automatic Indentation
- Debugger (Prel. version for algorithmic subset)



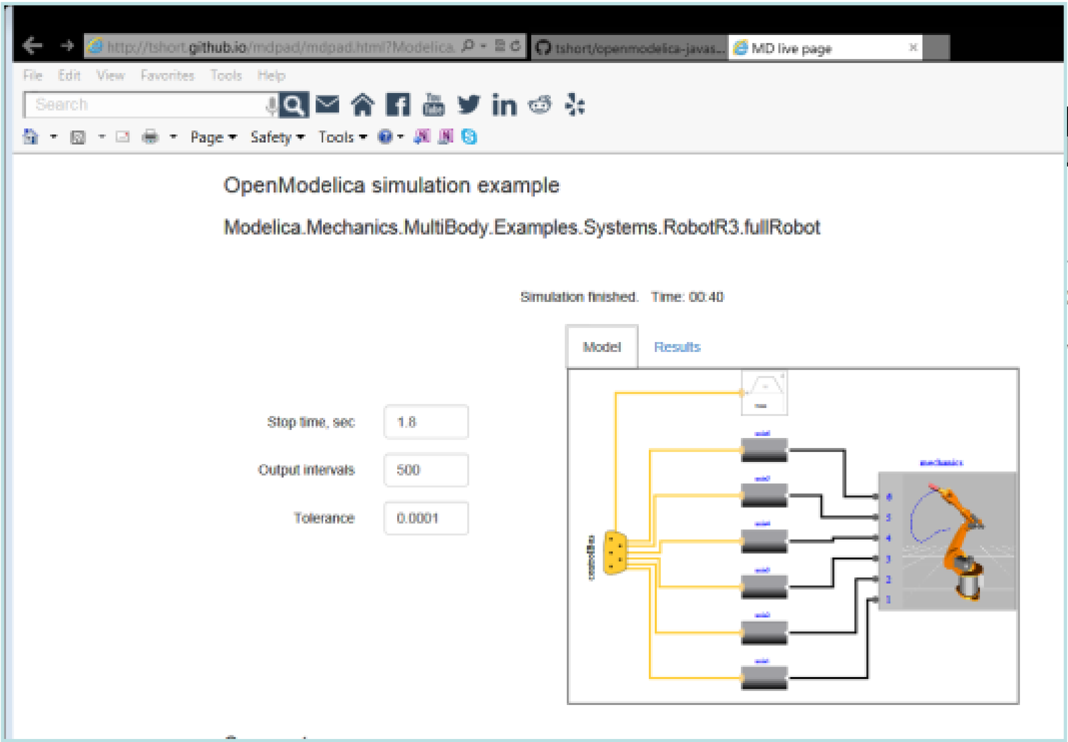
OpenModelica MDT: Code Outline and Hovering Info



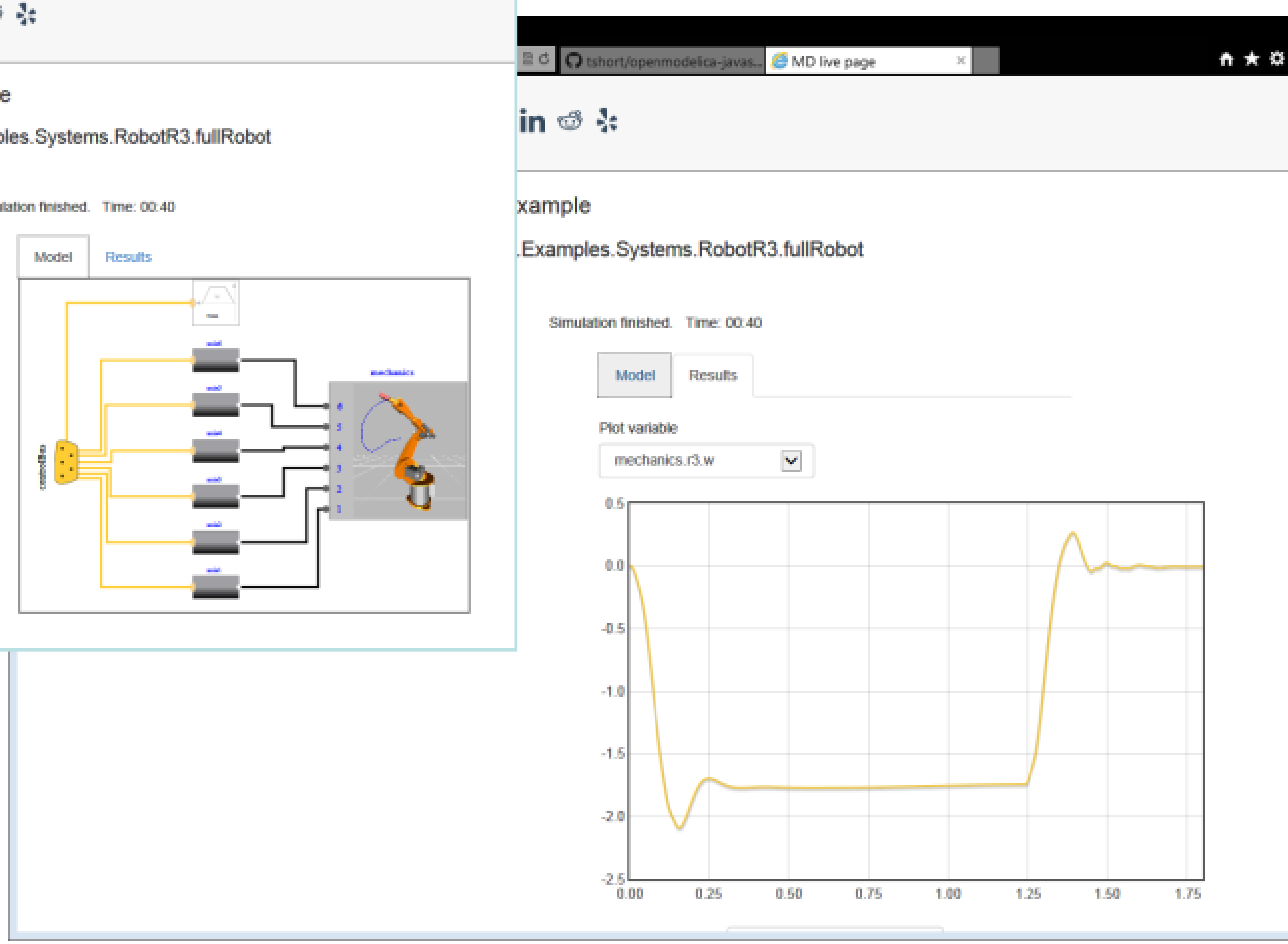
Identifier Info on Hovering

Code Outline for easy navigation within Modelica files

OpenModelica Simulation in Web Browser Client



MultiBody RobotR3.FullRobot

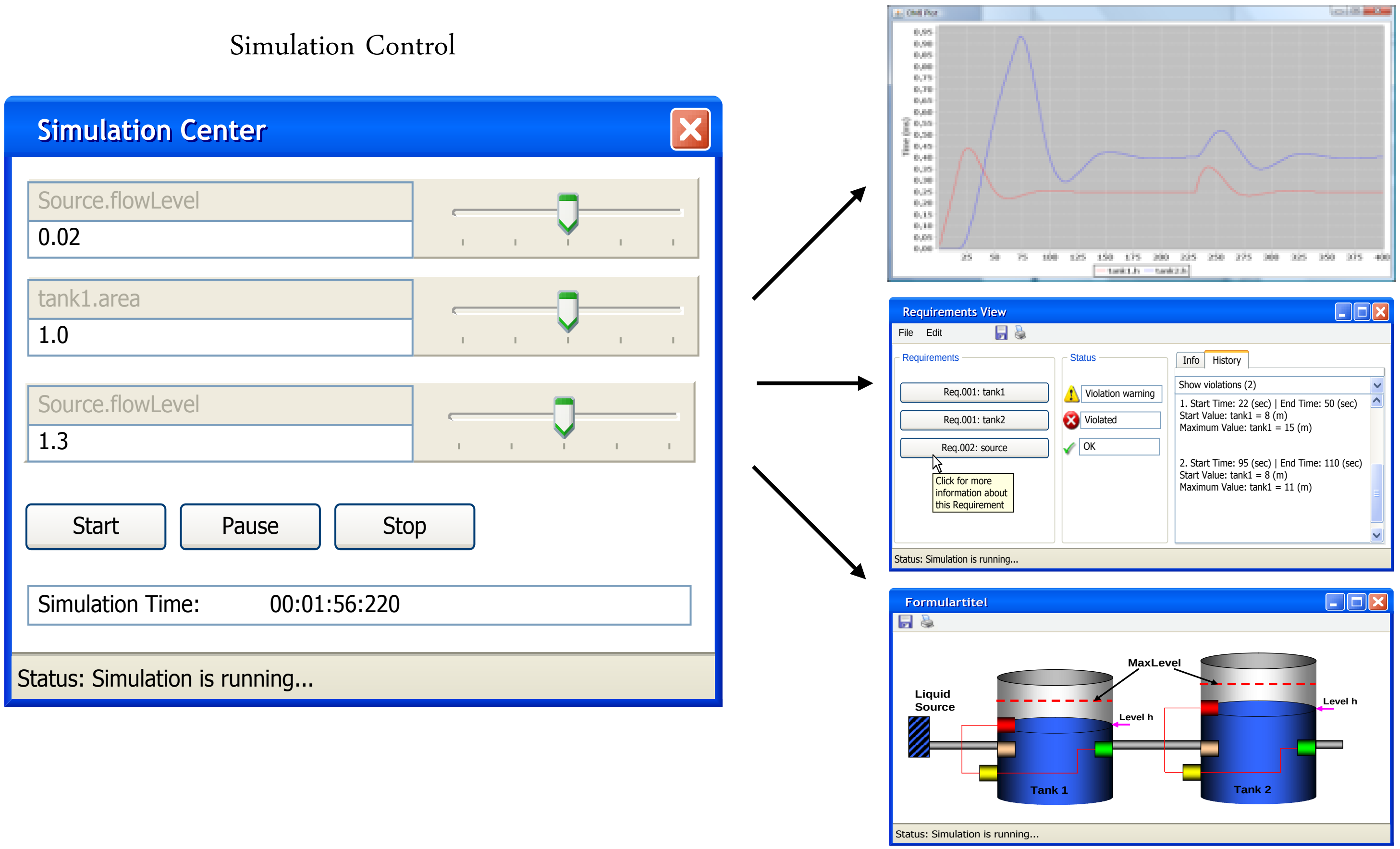


OpenModelica compiles to efficient Java Script code which is executed in web browser

Interactive Simulation

Examples of Simulation Visualization

Simulation Control



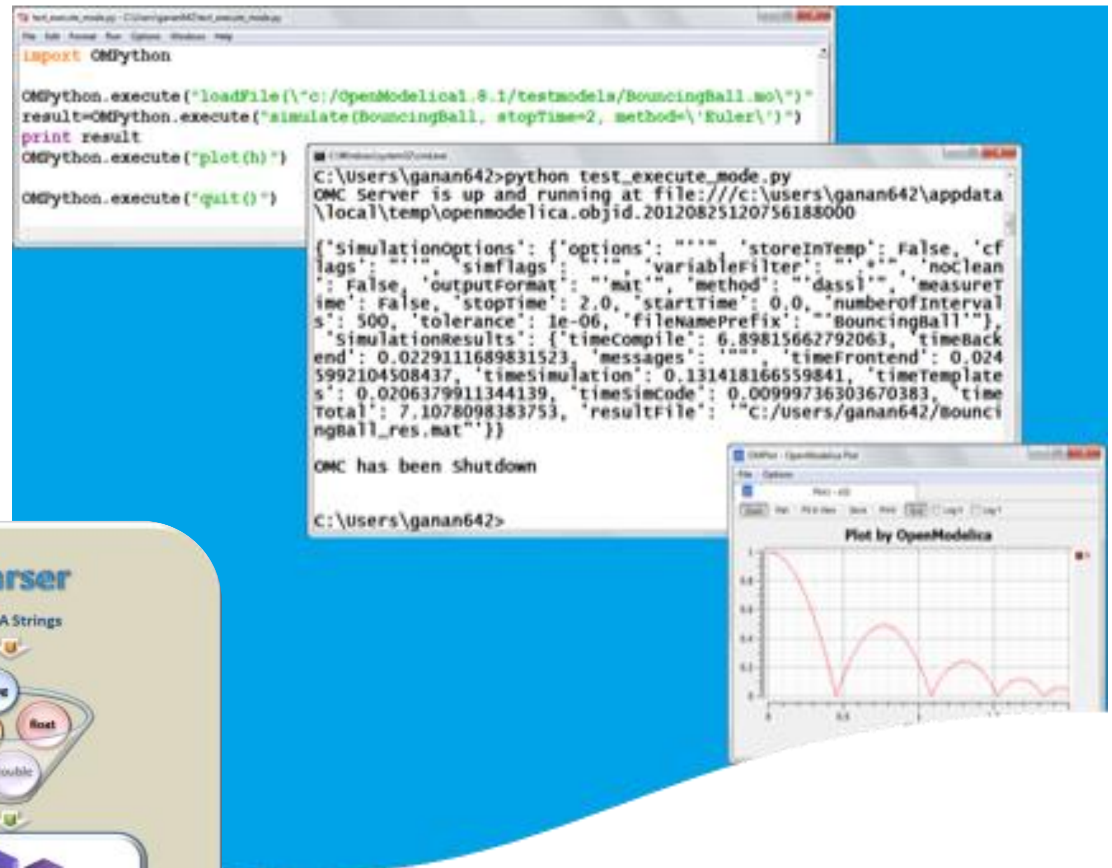
Plot View

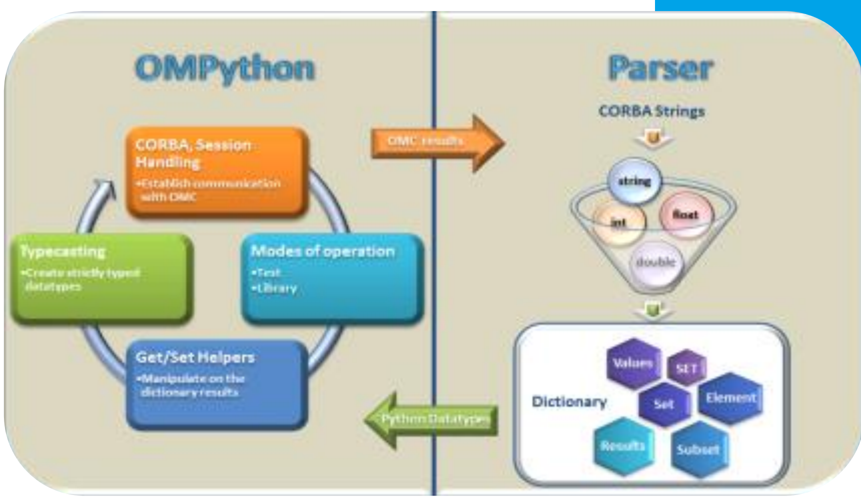
Requirements Evaluation View in ModelicaML

Domain-Specific Visualization View

OMPython – Python Scripting with OpenModelica

- Interpretation of Modelica commands and expressions
- Interactive Session handling
- Library / Tool
- Optimized Parser results
- Helper functions
- Deployable, Extensible and Distributable





MODELICA

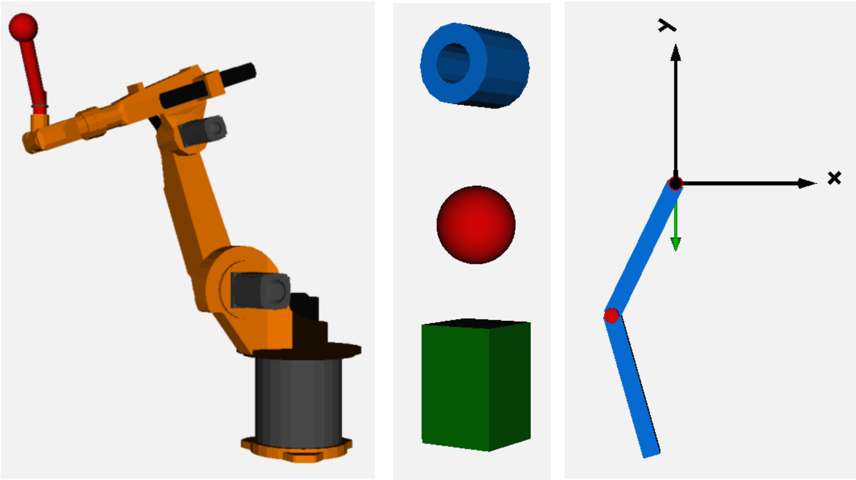
PySimulator Package

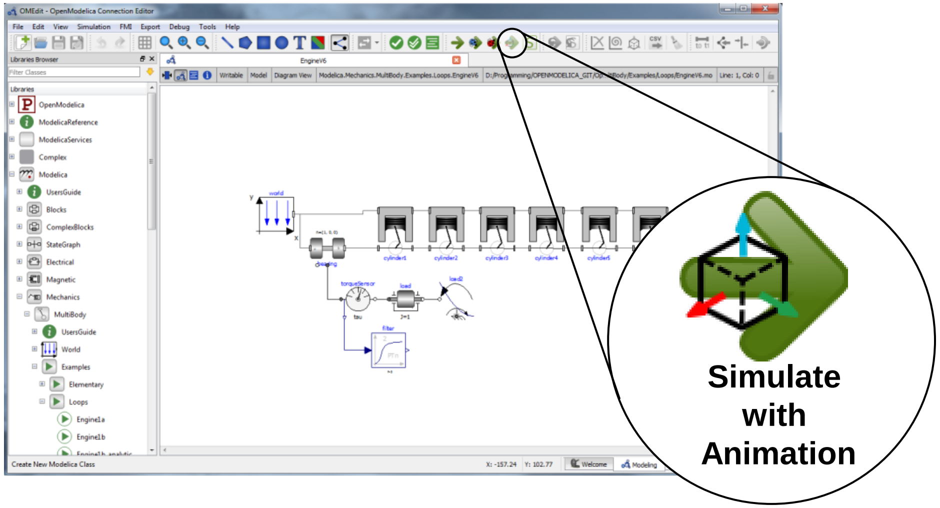
- PySimulator, a simulation and analysis package developed by DLR
- Free, downloadable
- Uses OMPython to simulate Modelica models by OpenModelica

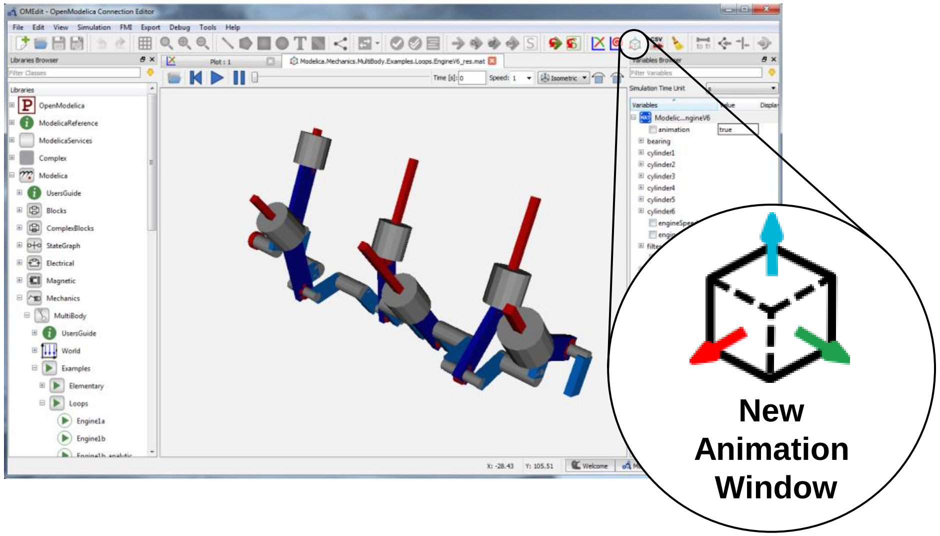
MODELICA

OMEdit 3D Visualization of Multi-Body Systems

- Built-in feature of OMEdit to animate MSL-Multi-Body shapes
- Visualization of simulation results
- Animation of geometric primitives and CAD-Files

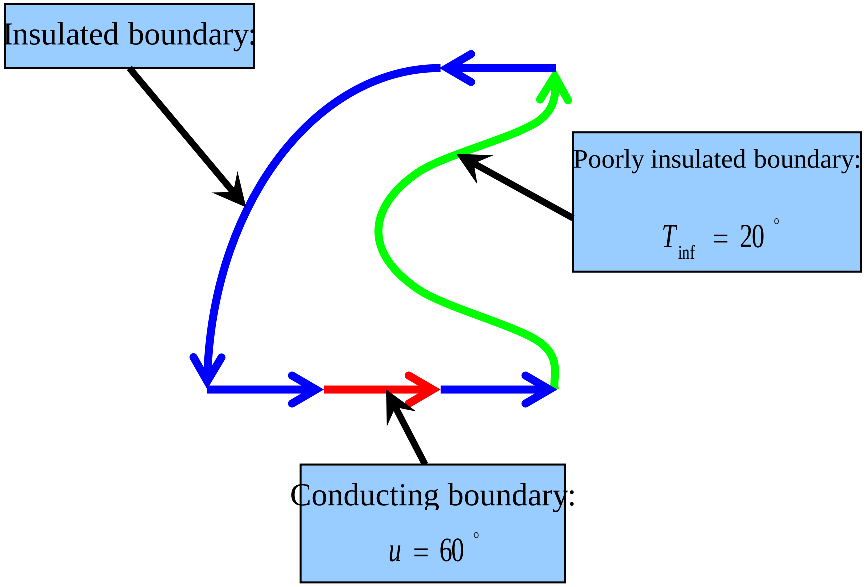


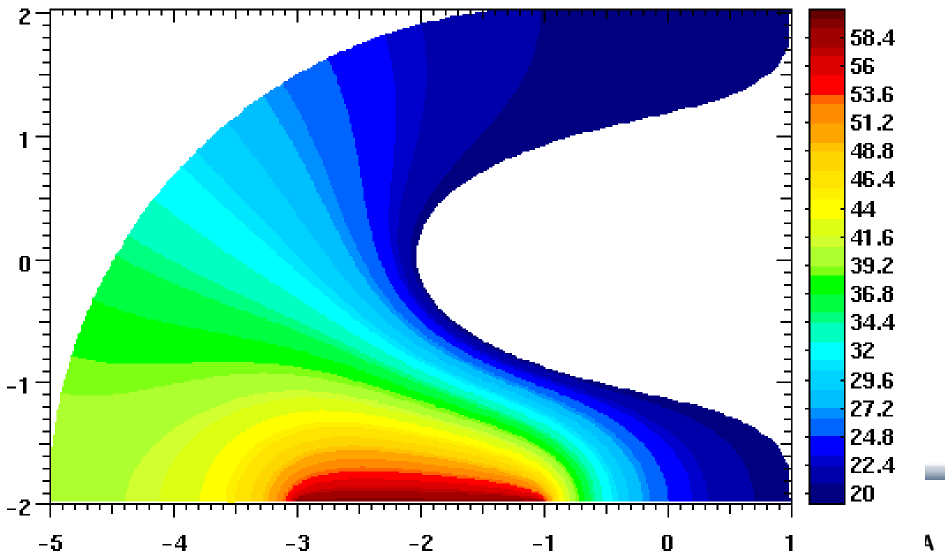




Extending Modelica with PDEs for 2D, 3D flow problems – Research

```
class PDEModel
   HeatNeumann h_iso;
   Dirichlet h_heated(g=50);
   HeatRobin h_glass(h_heat=30000);
   HeatTransfer ht;
   Rectangle2D dom;
equation
   dom.eq=ht;
   dom.left.bc=h_glass;
   dom.top.bc=h_iso;
   dom.right.bc=h_iso;
   dom.bottom.bc=h_heated;
end PDEModel;
```

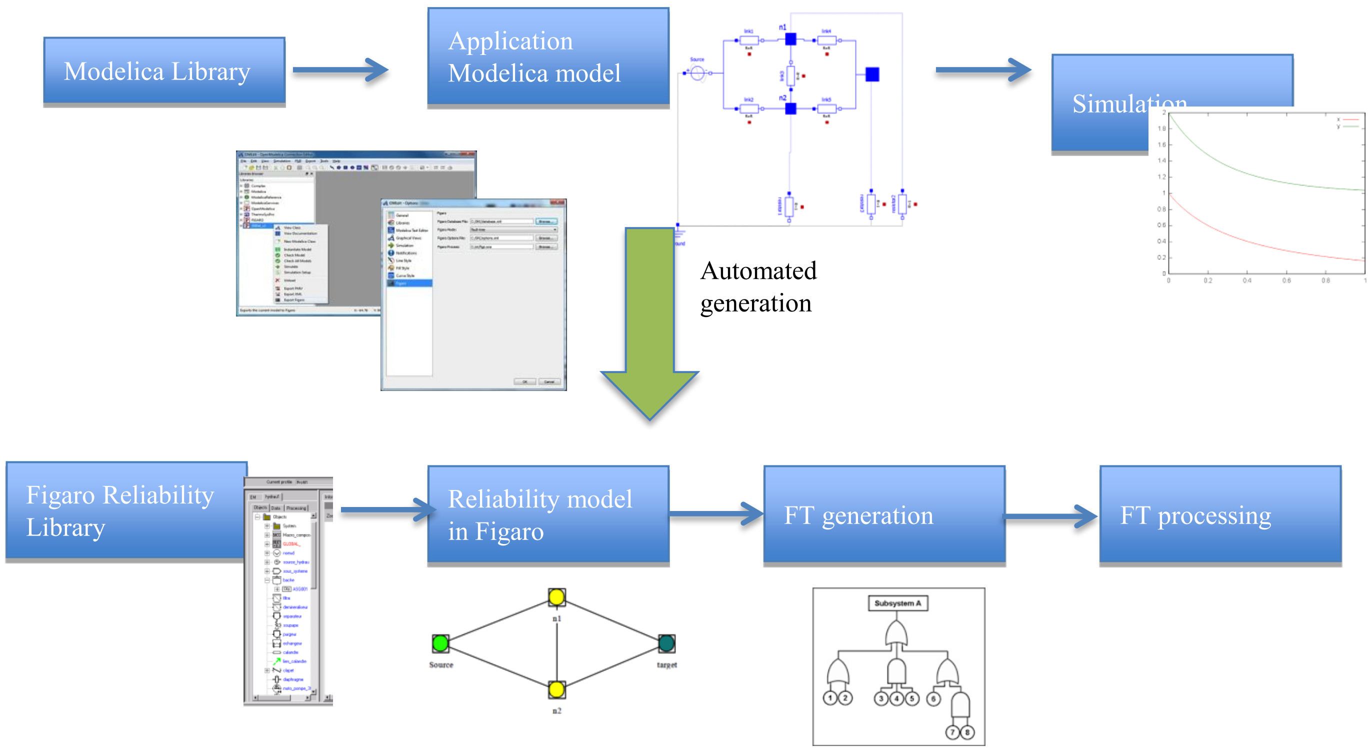




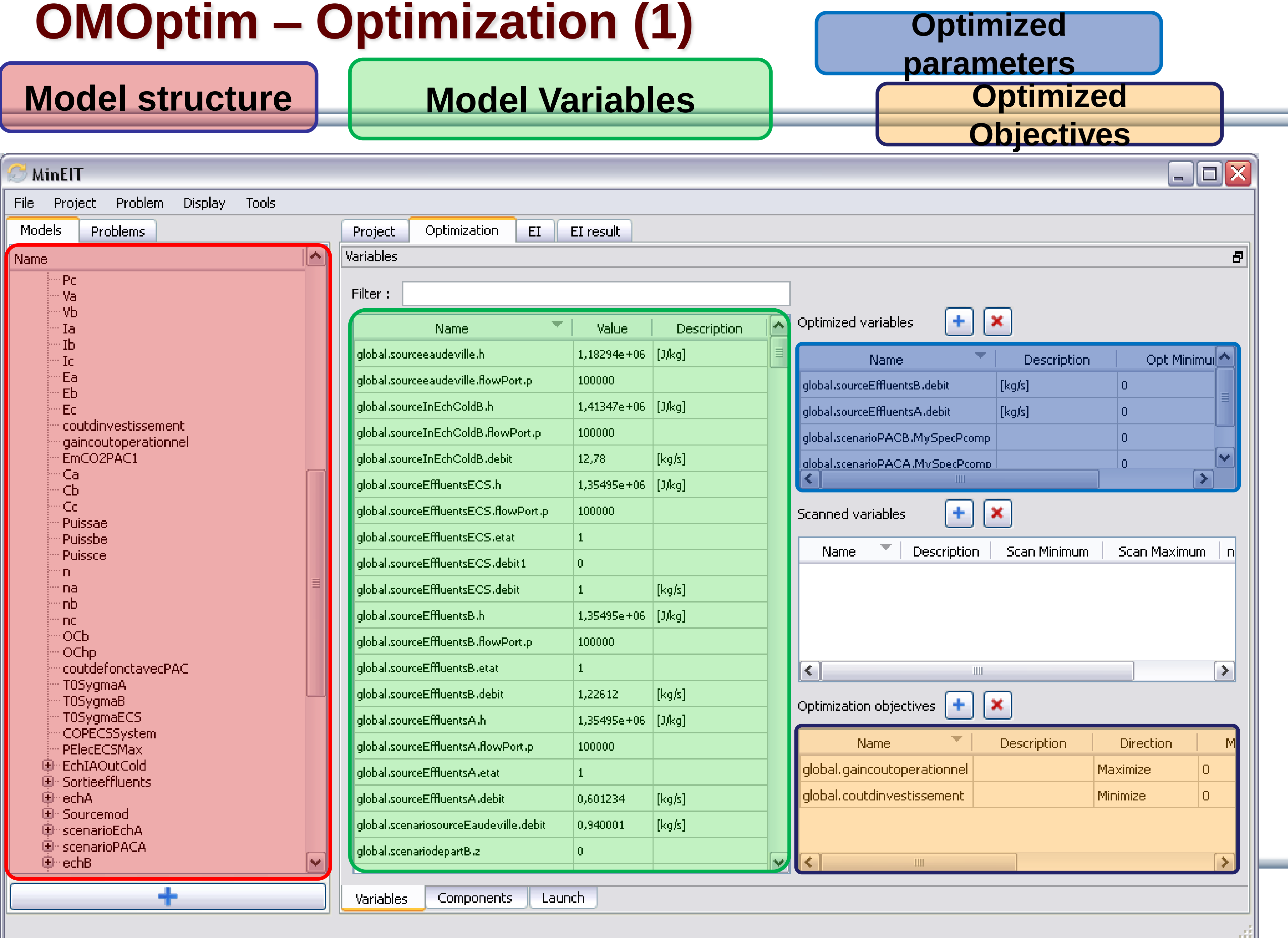
Prototype in OpenModelica 2005
PhD Thesis by Levon Saldamli
www.openmodelica.org
Currently not operational

Failure Mode and Effects Analysis (FMEA) in OM

- Modelica models augmented with reliability properties can be used to generate reliability models in Figaro, which in turn can be used for static reliability analysis
- Prototype in OpenModelica integrated with Figaro tool (which is becoming open-source)



OMOptim – Optimization (1)



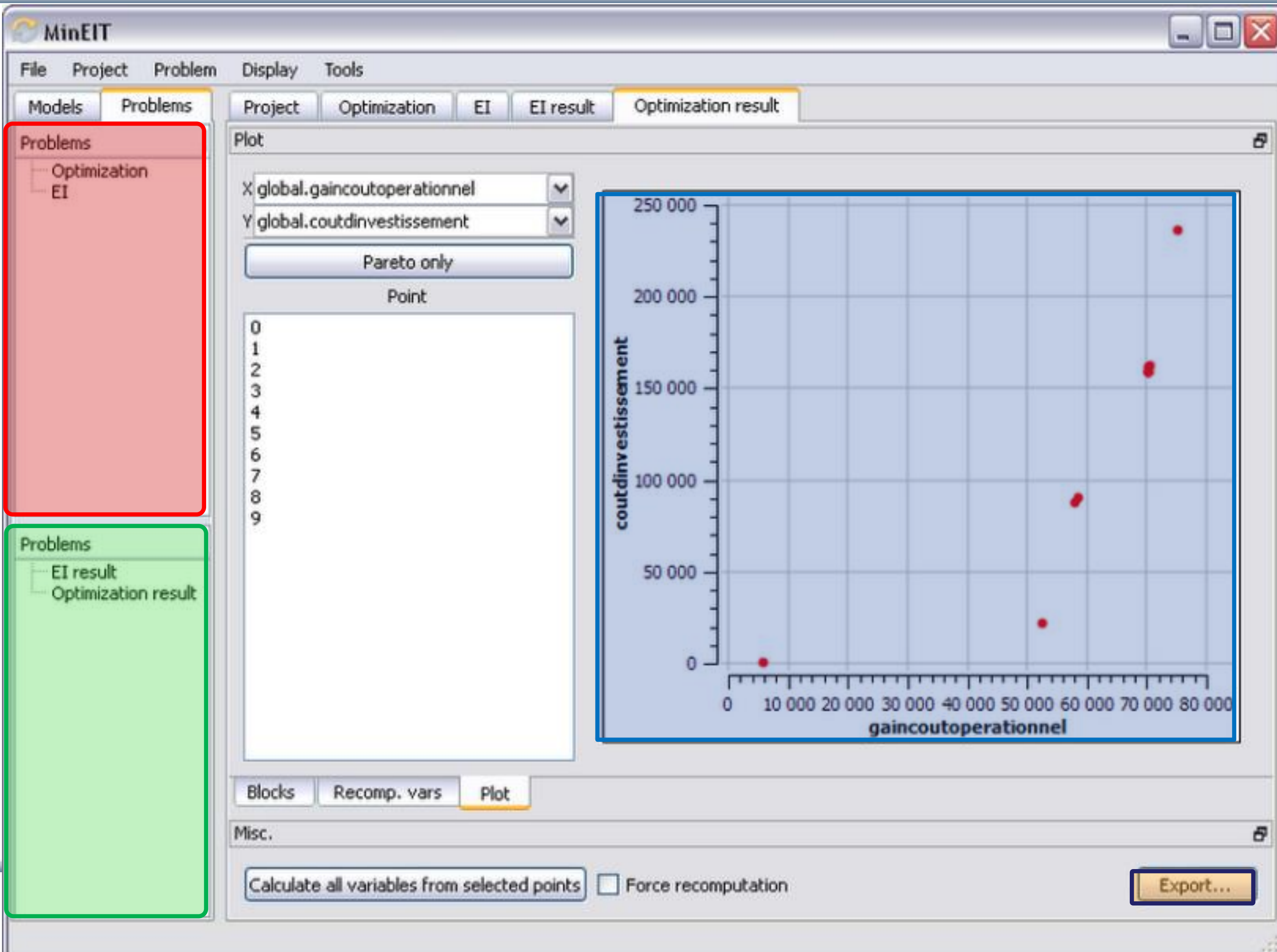
OMOptim – Optimization (2)

Problems

Solved problems

Result plot

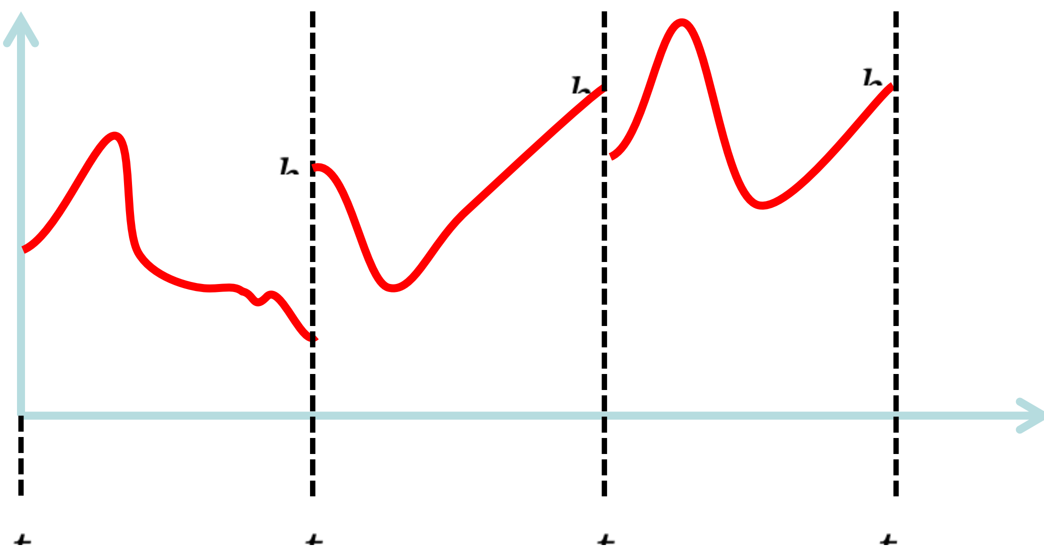
Export result data .csv



Multiple-Shooting and Collocation Dynamic Trajectory Optimization

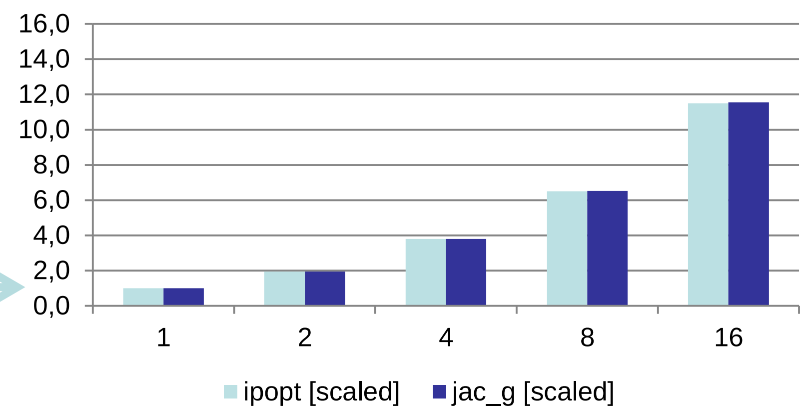
- Minimize a goal function subject to model equation constraints, useful e.g. for NMPC
- Multiple Shooting/Collocation
  - Solve sub-problem in each sub-interval

$$x_i(t_{i+1}) = h_i + \int_{t_i}^{t_{i+1}} f(x_i(t), u(t), t)\, dt \approx F(t_i, t_{i+1}, h_i, u_i), \qquad x_i(t_i) = h_i$$

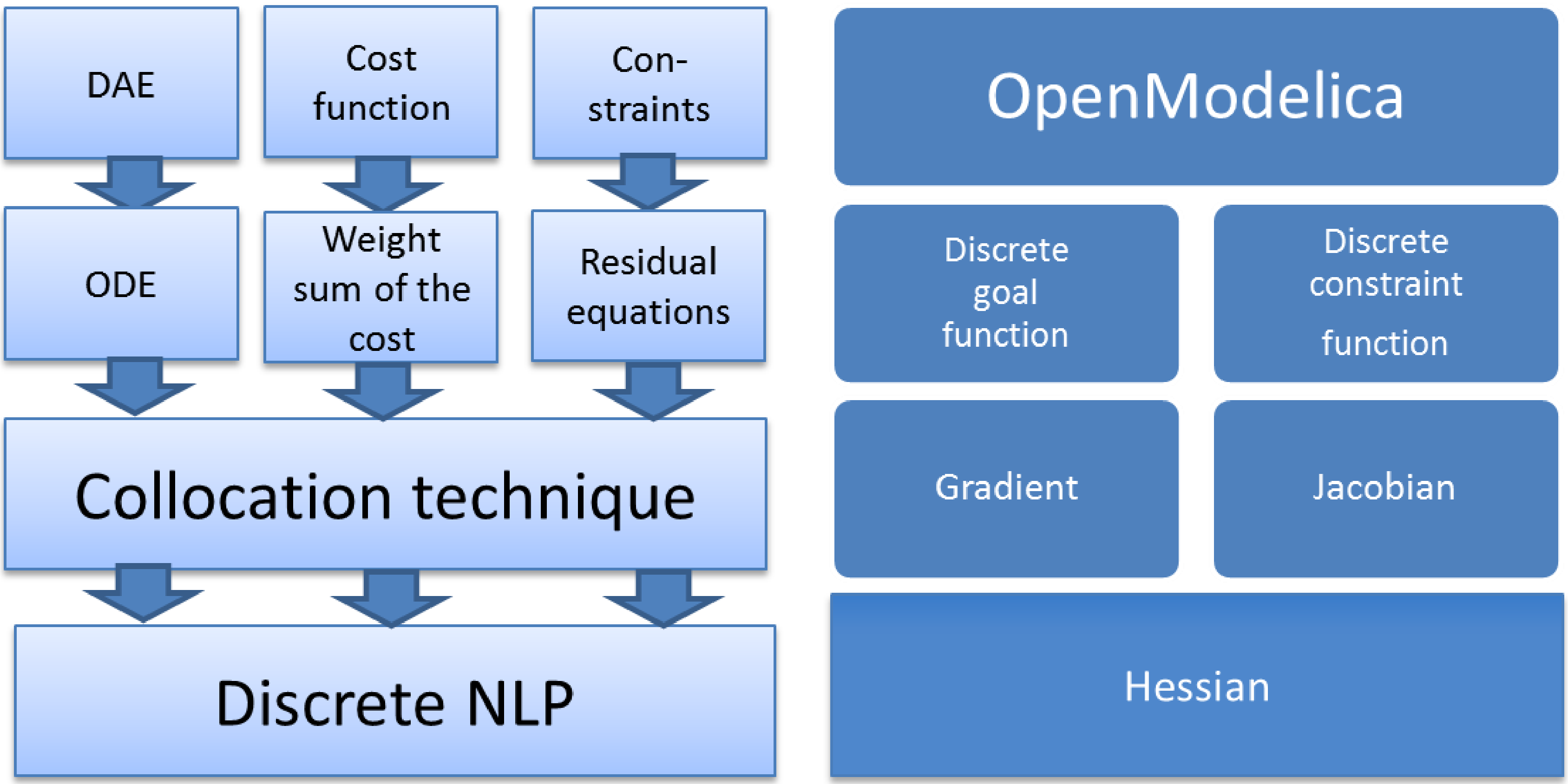


Example speedup, 16 cores:

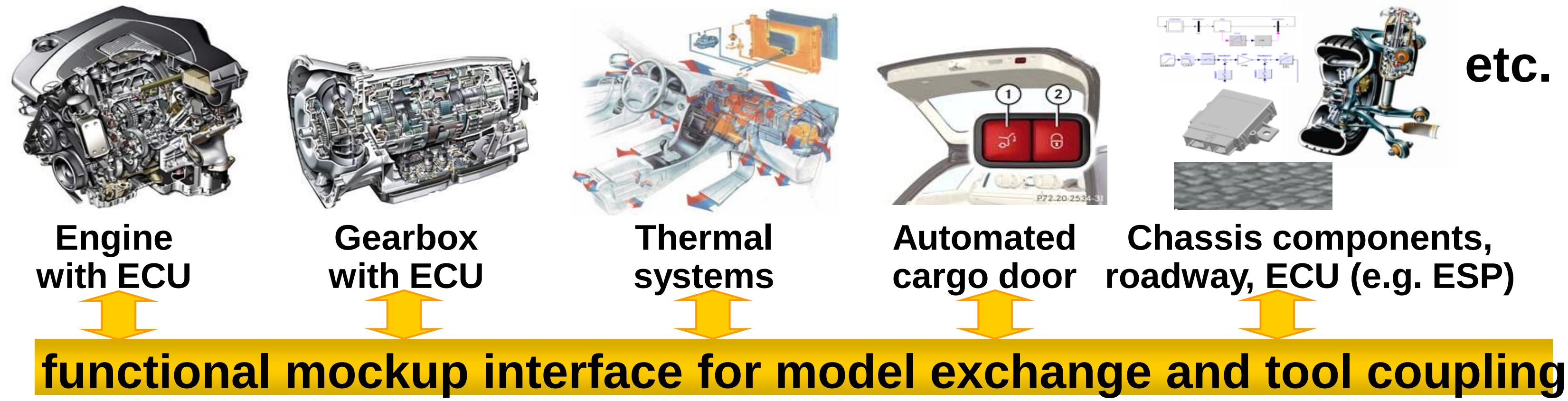
MULTIPLE_COLLOCATION



OpenModelica Dynamic Optimization Collocation



General Tool Interoperability & Model Exchange Functional Mock-up Interface (FMI)

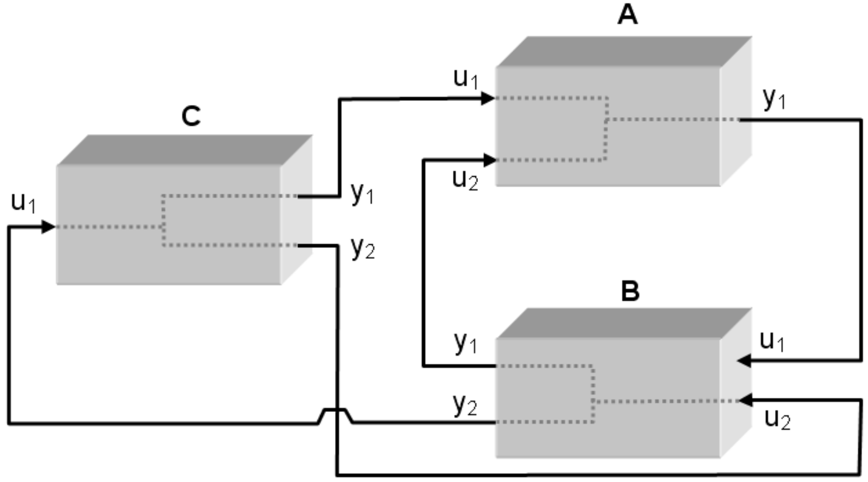


courtesy Daimler

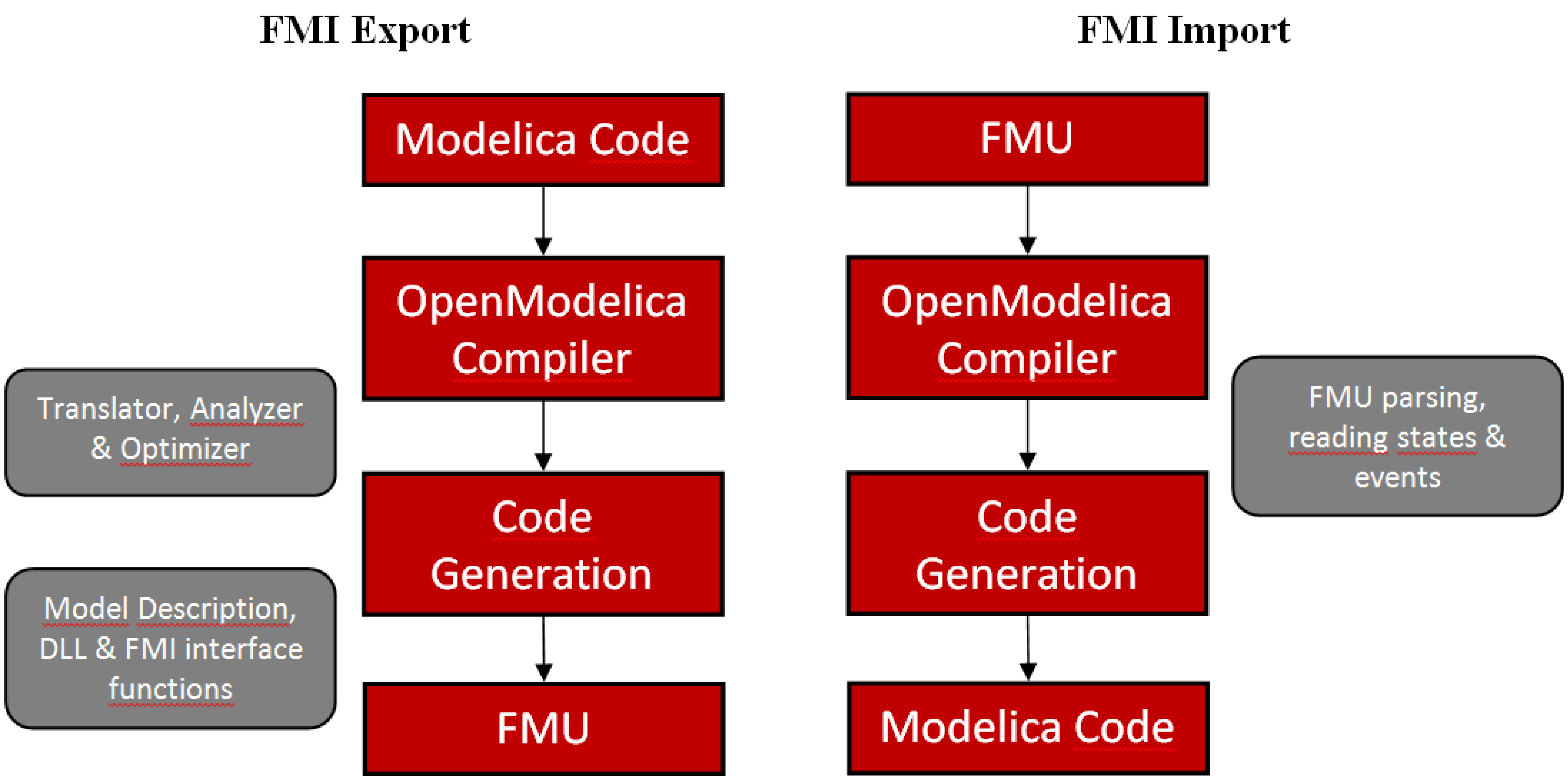
- FMI development was started by ITEA2 MODELISAR project. FMI is a Modelica Association Project now
- **Version 1.0**
- FMI for Model Exchange (released Jan 26,2010)
- FMI for Co-Simulation (released Oct 12,2010)
- **Version 2.0**
- FMI for Model Exchange and Co-Simulation (released July 25,2014)
- **> 60 tools** supporting it (https://www.fmi-standard.org/tools)

Functional Mockup Units

- Import and export of input/output blocks –
  Functional Mock-Up Units – FMUs, described by
  - differential-, algebraic-, discrete equations,
  - with time-, state, and step-events
- An FMU can be large (e.g. 100 000 variables)
- An FMU can be used in an embedded system (small overhead)
- FMUs can be connected together

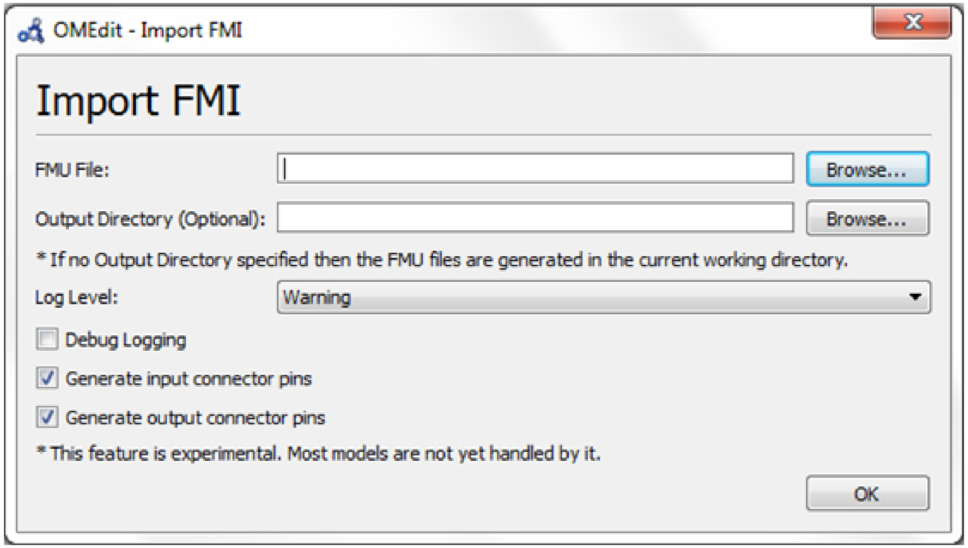


OpenModelica Functional Mockup Interface (FMI)



FMI in OpenModelica

- Model Exchange implemented (FMI 1.0 and FMI 2.0)
- FMI 2.0 Co-simulation available
- The FMI interface is accessible via the **OpenModelica scripting environment** and the **OpenModelica connection editor**



OpenModelica Code Generators for Embedded Real-time Code

- A **full-fledged** OpenModelica-generated source-code FMU (Functional Mockup Unit) code generator
  - Can be used to **cross-compile FMUs** for platforms with more available memory.
  - These platforms can **map** FMI inputs/outputs to analog/digital I/O in the importing FMI master.
- A very **simple code generator** generating a **small footprint** statically linked executable.
  - Not an FMU because there is no OS, filesystem, or shared objects in microcontrollers.

Code Generator Comparison, Full vs Simple

	Full Source-code FMU targeting 8-bit AVR proc	**Simple code generator targeting 8-bit AVR proc**
Hello World (0 equations)	43 kB flash memory 23 kB variables (RAM)	130 B flash memory 0 B variables (RAM)
SBHS Board (real-time PID controller, LCD, etc)	**68 kB** flash memory **25 kB** variables (RAM)	**4090 B** flash memory **151 B** variables (RAM)

The largest 8-bit AVR processor MCUs (Micro Controller Units) have 16 kB SRAM.

One of the more (ATmega328p; Arduino Uno) has 2 kB SRAM.

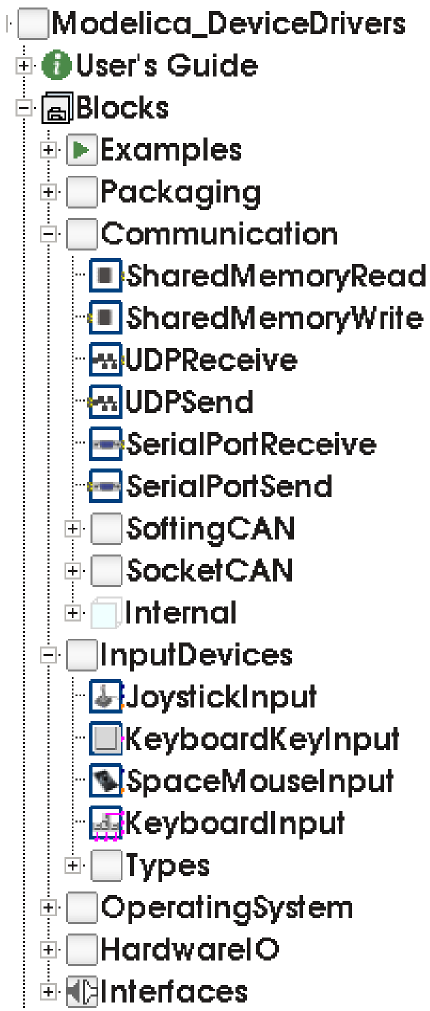
The ATmega16 we target has **1 kB SRAM available** (stack, heap, and global variables)

The Simple Code Generator

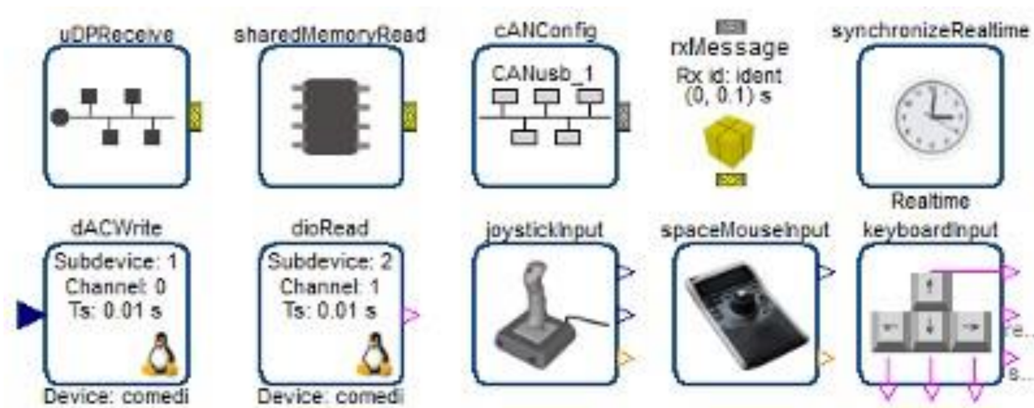
Supports only a limited Modelica subset

- No initialization (yet)
- No strongly connected components
- No events
- No functions (except external C and built-in)
- Only parts that OpenModelica can generate good and efficient code for right now (extensions might need changes in the intermediate code)
  - Unused variables are not accepted (OM usually duplicates all variables for pre() operators, non-linear system guesses, etc… but only a few of them are actually used)
- FMU-like interface (but statically linked)

Communication & I/O Devices: MODELICA_DEVICEDRIVERS Library



- **Free library** for interfacing hardware drivers
- **Cross-platform** (Windows and Linux)
- UDP, SharedMemory, CAN, Keyboard, Joystick/Gamepad
- DAQ cards for digital and analog IO (only Linux)
- Developed for **interactive real-time** simulations



MODELICA

OpenModelica and Device Drivers Library AVR Processor Support

- No direct Atmel AVR or Arduino support in the OpenModelica compiler
- **Everything is done by the Modelica DeviceDrivers library**
- All **I/O** is **modeled explicitly in Modelica**, which makes code generation very simple

Modelica Device Drivers Library - AVR processor sub-packages:

- IO.AVR.Analog (ADC – Analog Input)
- IO.AVR.PWM (PWM output)
- IO.AVR.Digital.LCD (HD44780 LCD driver on a single 8-pin digital port)
- OS.AVR.Timers (Hardware timer setup, used by real-time and PWM packages)
- OS.AVR.RealTime (very simple real-time synchronization; one interrupt per clock cycle; works for single-step solvers)

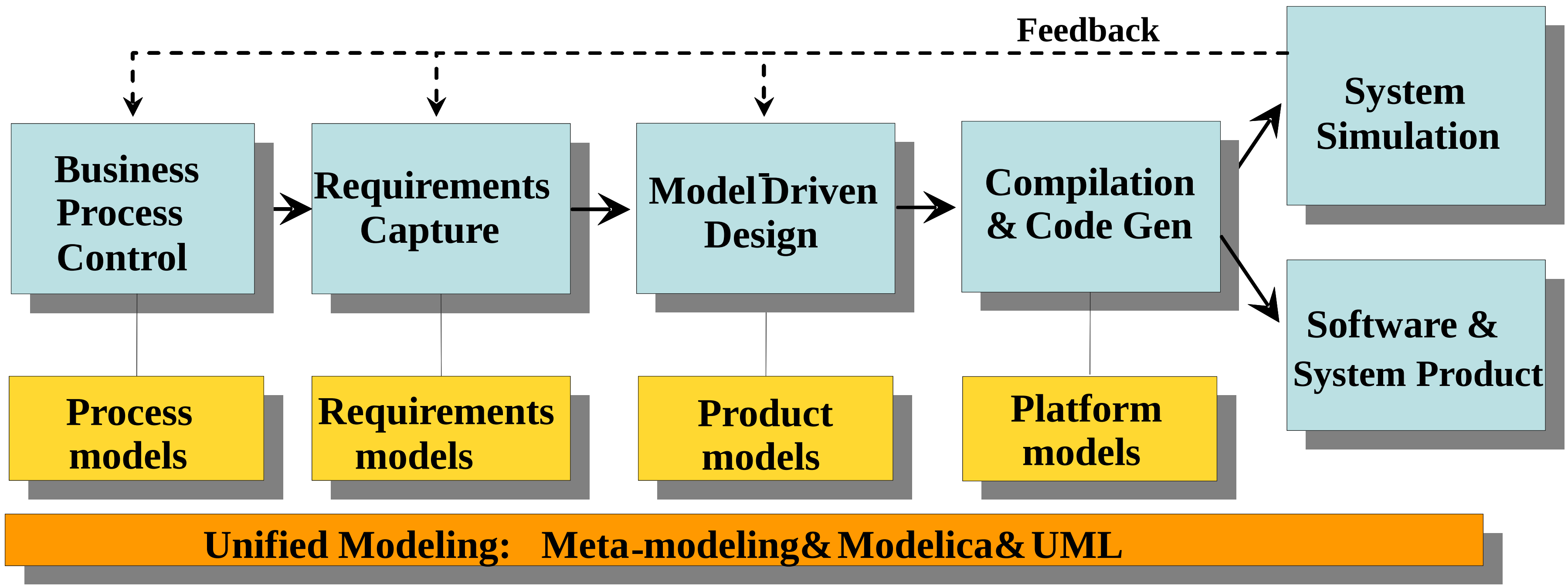
Use Case: SBHS (Single Board Heating System)

Single board heating system (IIT Bombay)

- Use for teaching basic control theory
- Usually controlled by serial port (set fan value, read temperature, etc)
- OpenModelica can generate code targeting the ATmega16 on the board (AVR-ISP programmer in the lower left).
  Program size is 4090 bytes including LCD driver and PID-controller (out of 16 kB flash memory available).

Movie Demo!

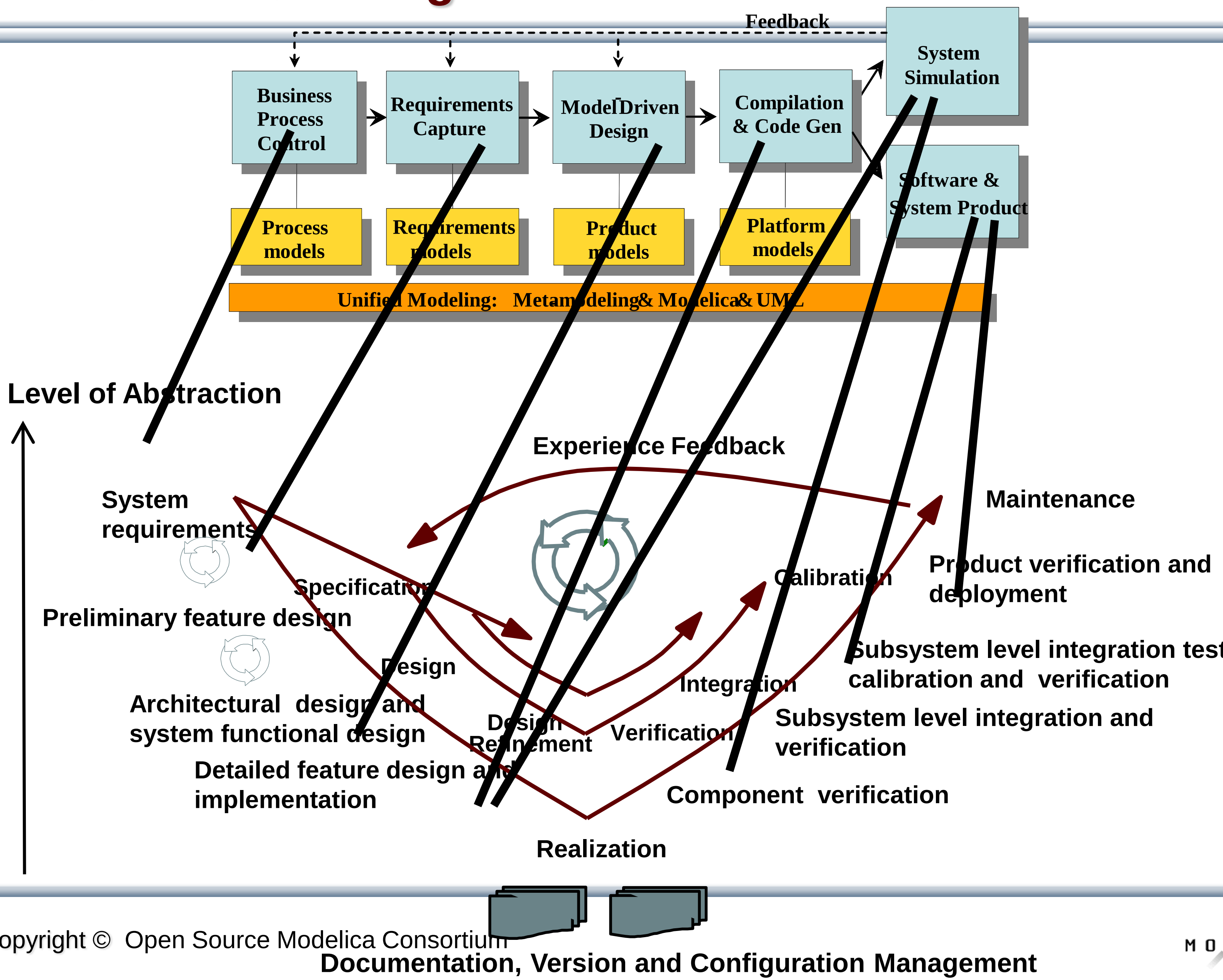
OPENPROD – Large 28-partner European Project, 2009-2012 Vision of Cyber-Physical Model-Based Product Development



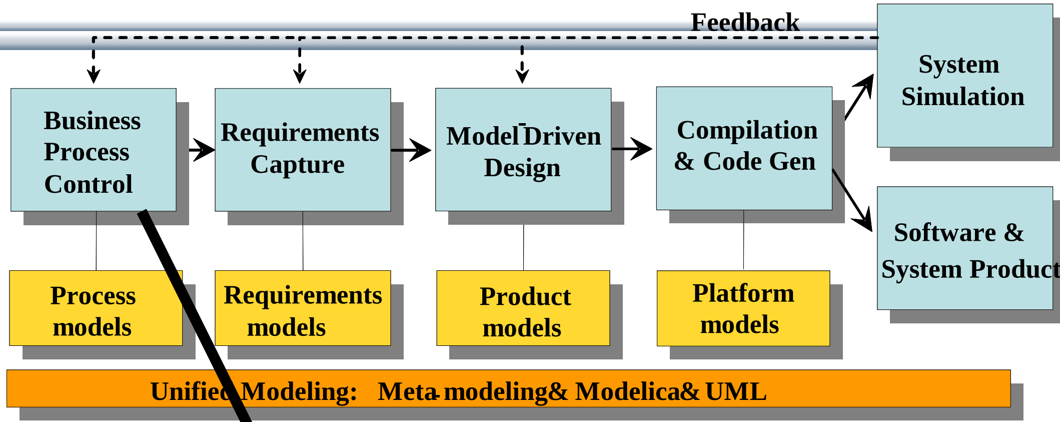
OPENPROD Vision of unified modeling framework for model-based product development.

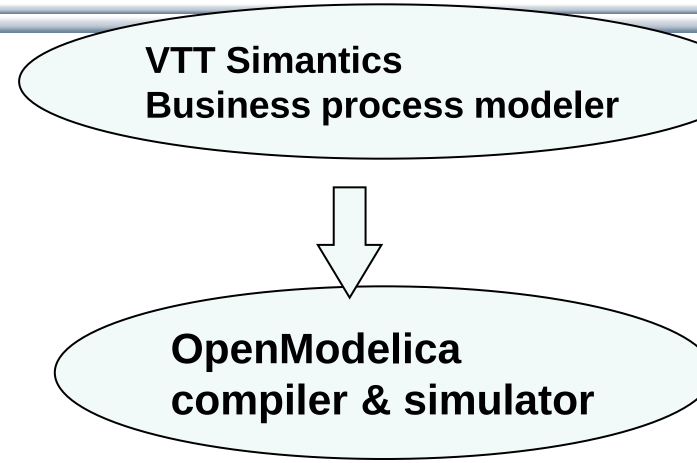
Open Standards – Modelica (HW, SW) and UML (SW)

OPENPROD Model-Based Development Environment Covers Product-Design V

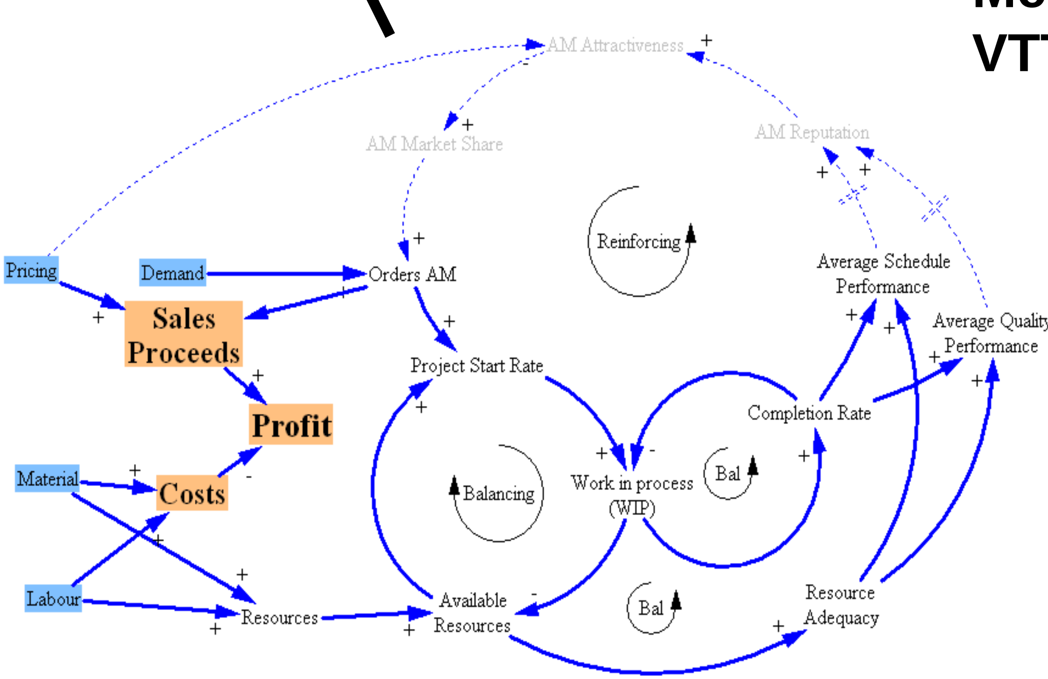


Business Process Control and Modeling



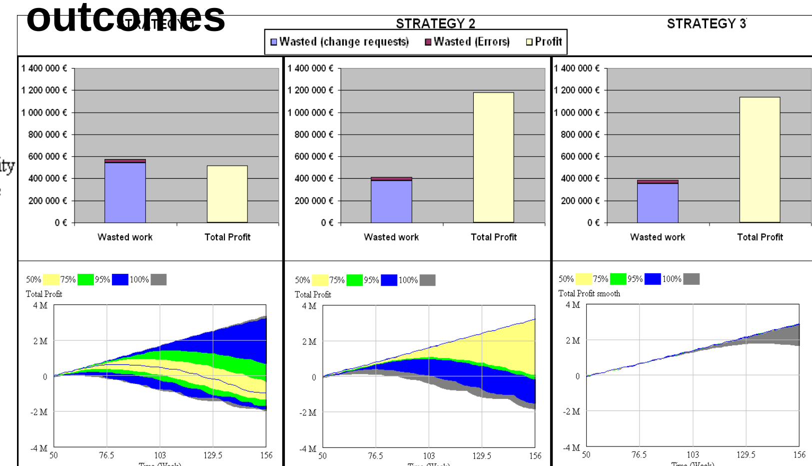


OpenModelica based simulation



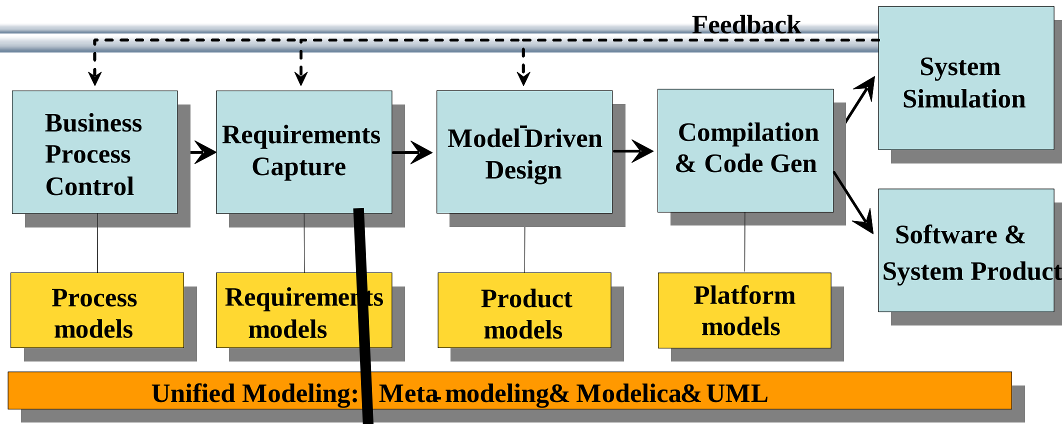
Metso Business model & simulation
VTT Simantics Graphic Modeling To

Simulation of 3 strategies with outcomes



MODELICA

Requirement Capture



vVDR (virtual Verification of Designs against Requirements)

in ModelicaML UML/Modelica Profile, part of OpenModelica

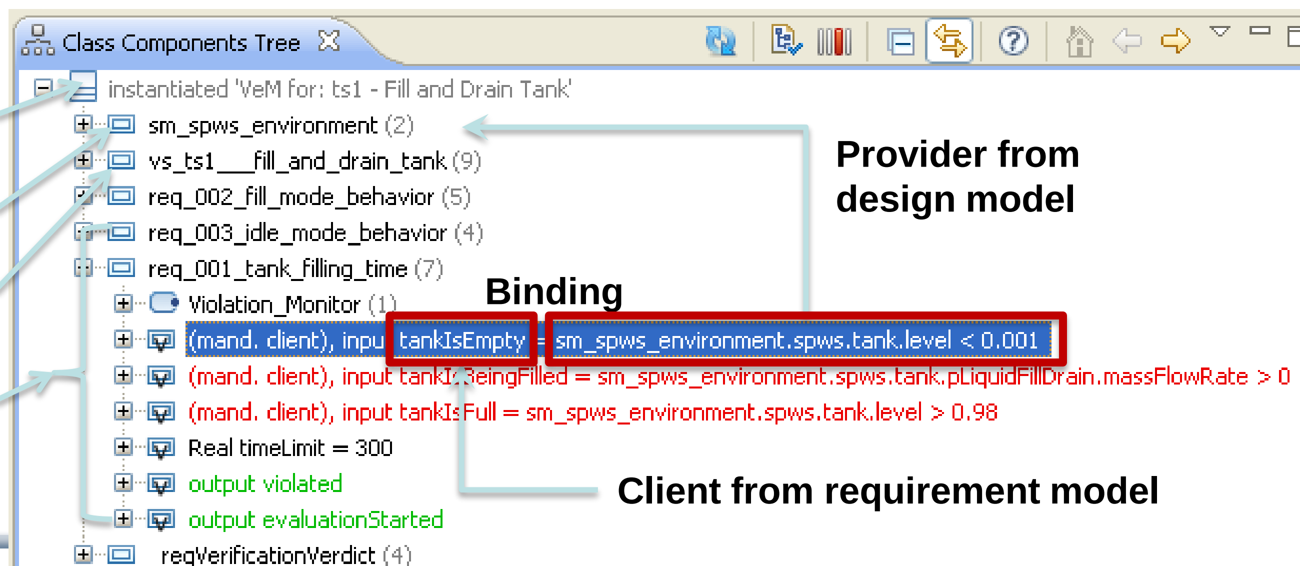
OpenModelica based simulation

Verification Model

Design Model

Scenario Model

Requirement Models



Binding

Provider from design model

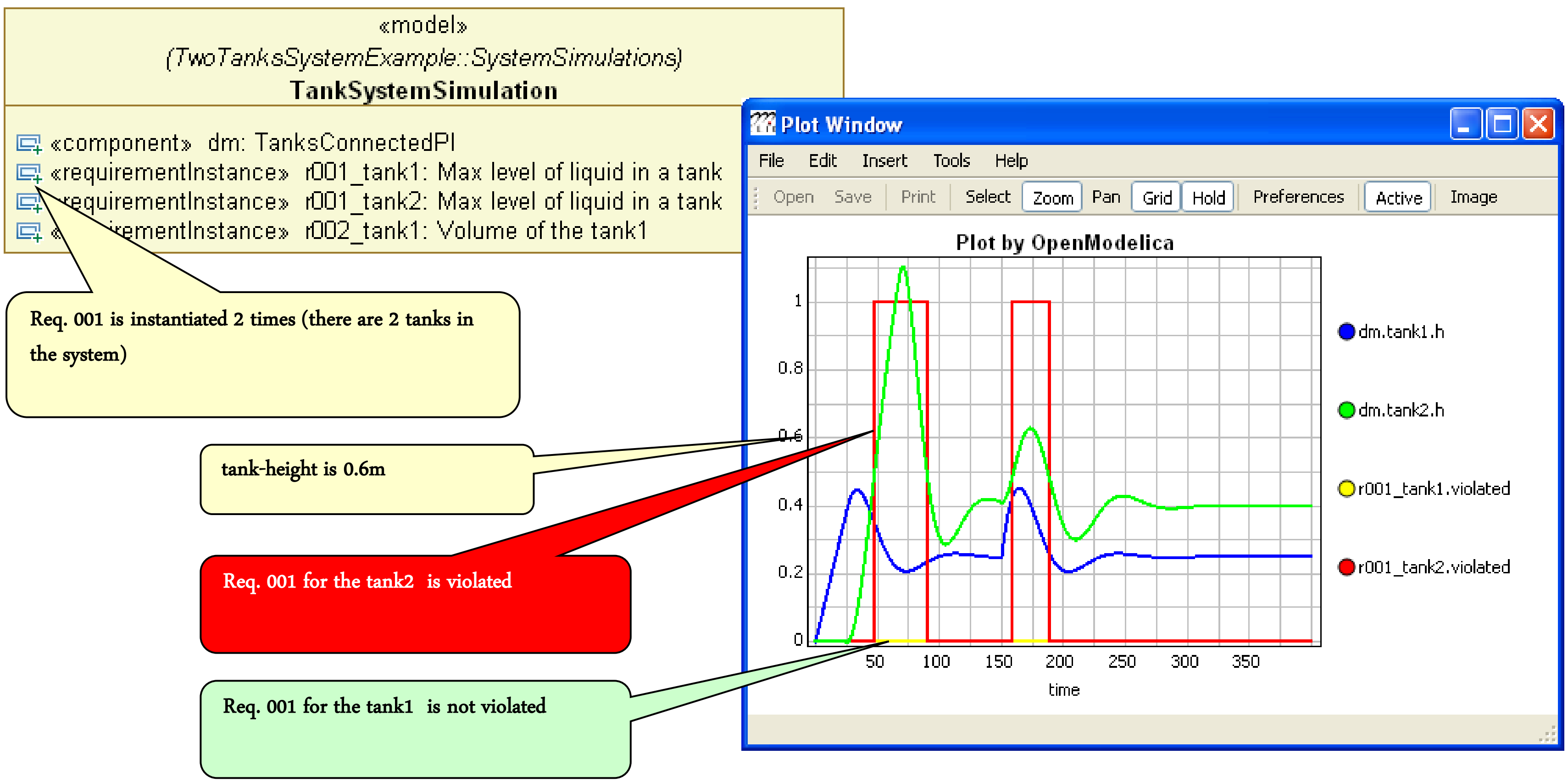
Client from requirement model

MODELICA

OpenModelica – ModelicaML UML Profile
SysML/UML to Modelica OMG Standardization

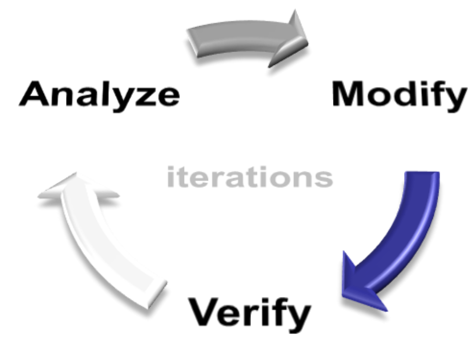
- ModelicaML is a UML Profile for SW/HW modeling
  - Applicable to "pure" UML or to other UML profiles, e.g. SysML
- Standardized Mapping UML/SysML to Modelica
  - Defines transformation/mapping for **executable** models
  - Being **standardized** by OMG
- ModelicaML
  - Defines graphical concrete syntax (graphical notation for diagram) for representing Modelica constructs integrated with UML
  - Includes graphical formalisms (e.g. State Machines, Activities, Requirements)
    - Which do not exist in Modelica language
    - Which are translated into executable Modelica code
  - Is defined towards generation of executable Modelica code
  - Current implementation based on the Papyrus UML tool + OpenModelica

Example: Simulation and Requirements Evaluation



vVDR Method – virtual Verification of Designs vs Requirements

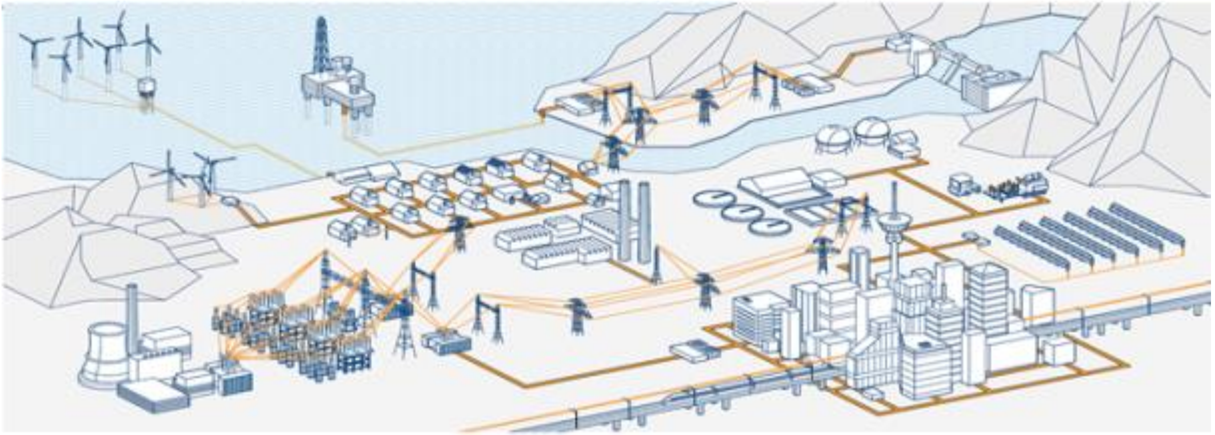
Actor	Task	Created Artifact
	Formalize Requirements	RMM Requirement Monitor Models
	Formalize Designs	DAM Designs Alternative Models
	Formalize Scenarios	SM Scenario Models
AUTOMATED	Create Verification Models *	VM Verification Models
AUTOMATED	Execute and Create Report	Reports
	Analyze Results	



Goal: Enable on-demand verification of designs against requirements using automated model composition at any time during development.

ABB Industry Use of OpenModelica FMI 2.0 and Debugger

- ABB OPTIMAX® provides advanced model based control products for power generation and water utilities



- ABB: "*ABB uses several compatible Modelica tools, including OpenModelica, depending on specific application needs.*"
- ABB: "*OpenModelica provides outstanding debugging features that help to save a lot of time during model development.*"

Recent Large-scale ABB OpenModelica Application

Generate code for controlling 7.5 to 10% of German Power Production

ABB OPTIMAX PowerFit

- Real-time optimizing control of large-scale virtual power plant for system integration
- **Software including OpenModelica** now used in managing more than 2500 renewable plants, total up to 1.5 GW

High scalability supporting growth

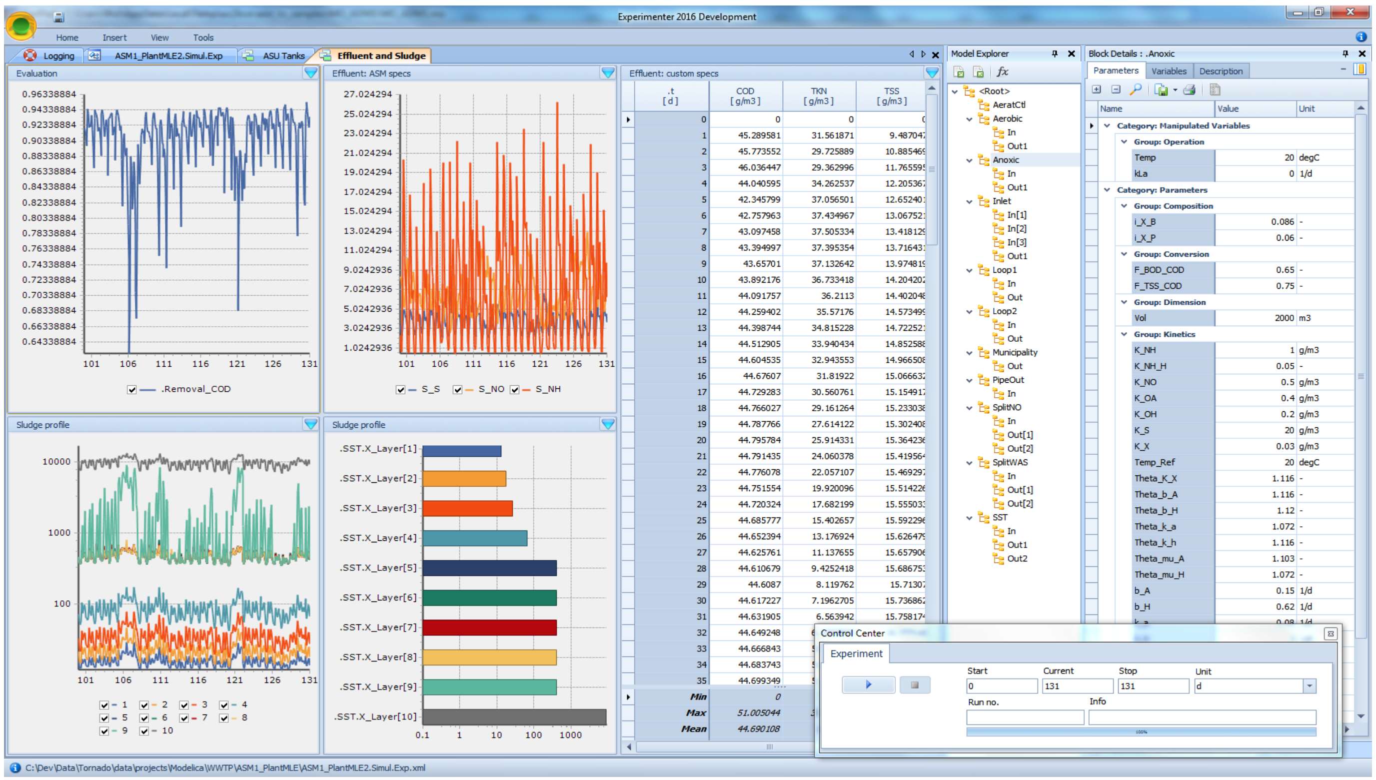
- 2012: initial delivery (for 50 plants)
- 2013: SW extension (500 plants)
- 2014: HW+SW extension (> 2000)
- 2015: HW+SW extension, incl. OpenModelica generating optimizing controller code in FMI 2.0 form

Manage 7.5% - 10% of German Power

- 2015, Aug: OpenModelica Exports FMUs for real-time optimizing control (seconds) of about **5.000 MW (7.5%) of power in Germany**

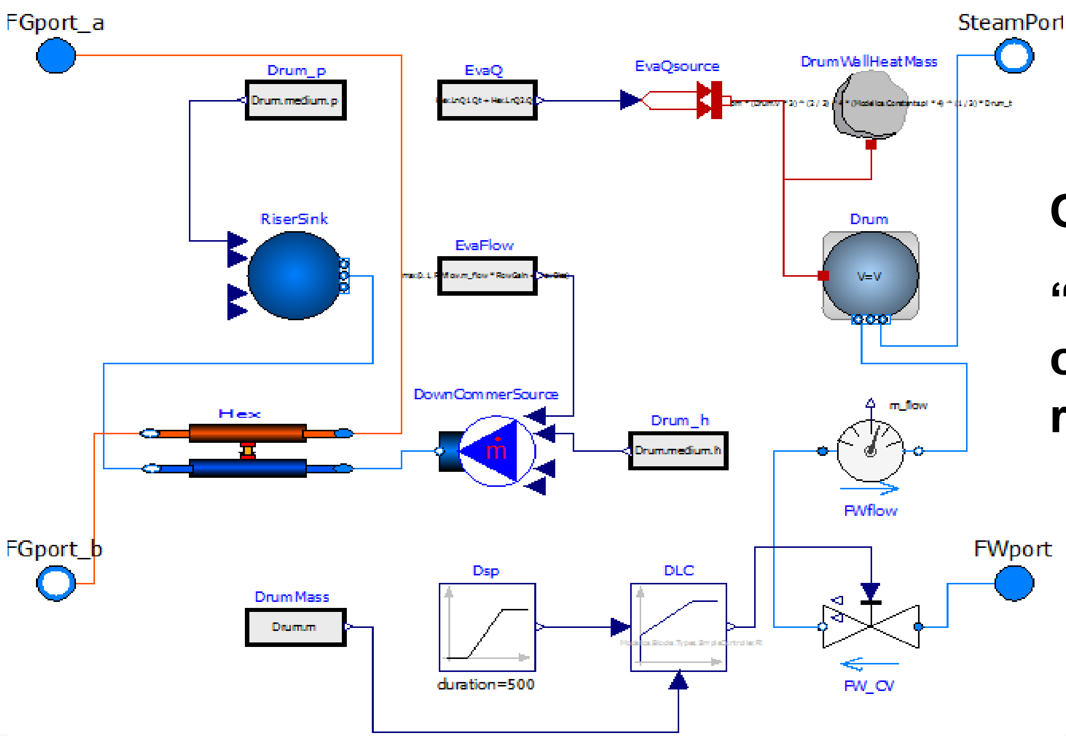
Industrial Product with OEM Usage of OpenModelica – MIKE by DHI, WEST Water Quality

- **MIKE by DHI**, www.mikebydhi.com, **WEST Water Quality** modeling and simulation environment
- Includes a large part of the OpenModelica compiler using the OEM license.
- Here a water treatment effluent and sludge simulation.



Performance Profiling for faster Simulation
(Here: Profiling equations of Siemens Drum boiler model with evaporator

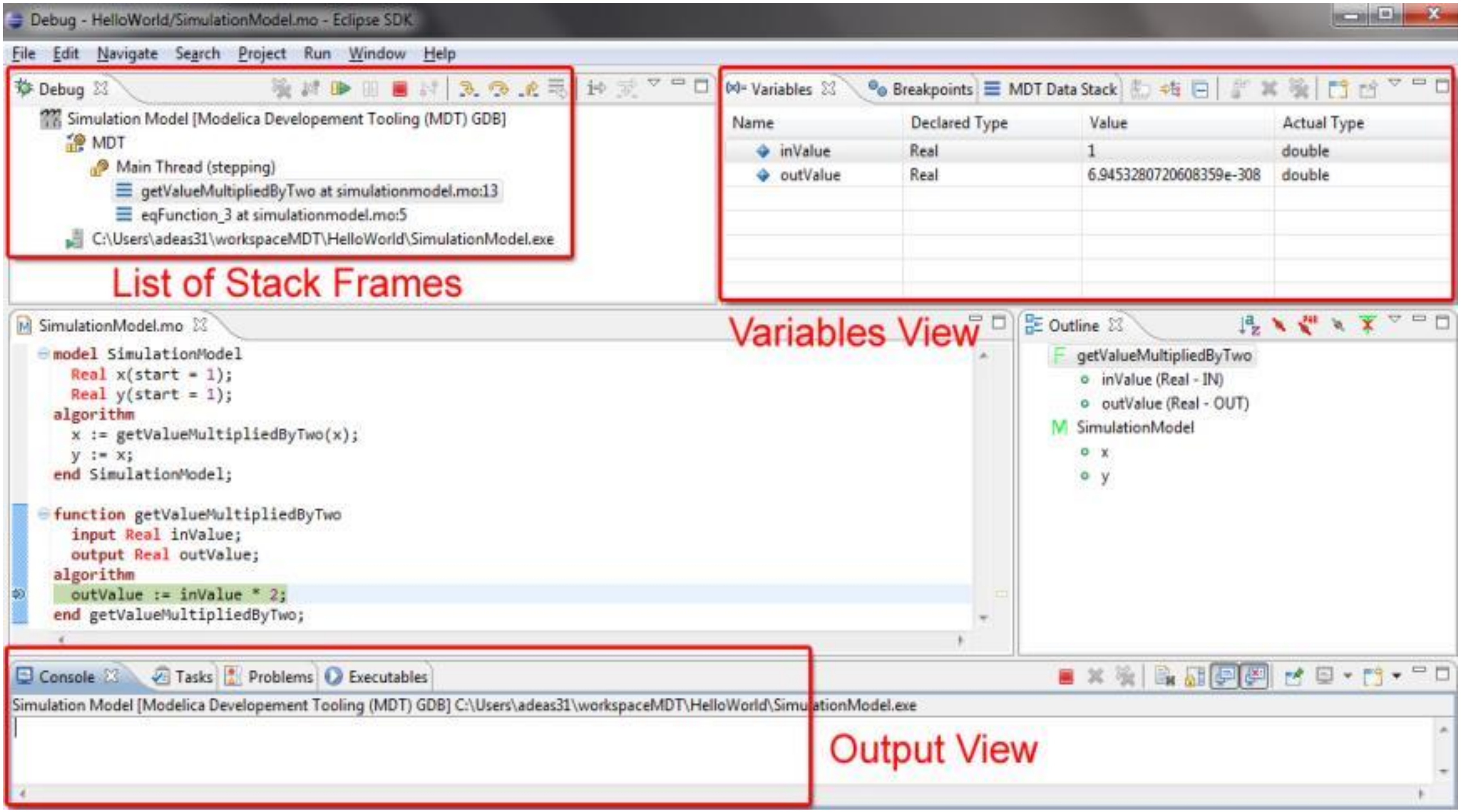
- Measuring **performance** of equation blocks to find bottlenecks
  - Useful as input before model simplification for real-time applications
- Integrated with the debugger to **point out the slow equations**
- Suitable **for real-time profiling** (collect less information), or a complete view of all equation blocks and function calls



Conclusion from the evaluation:

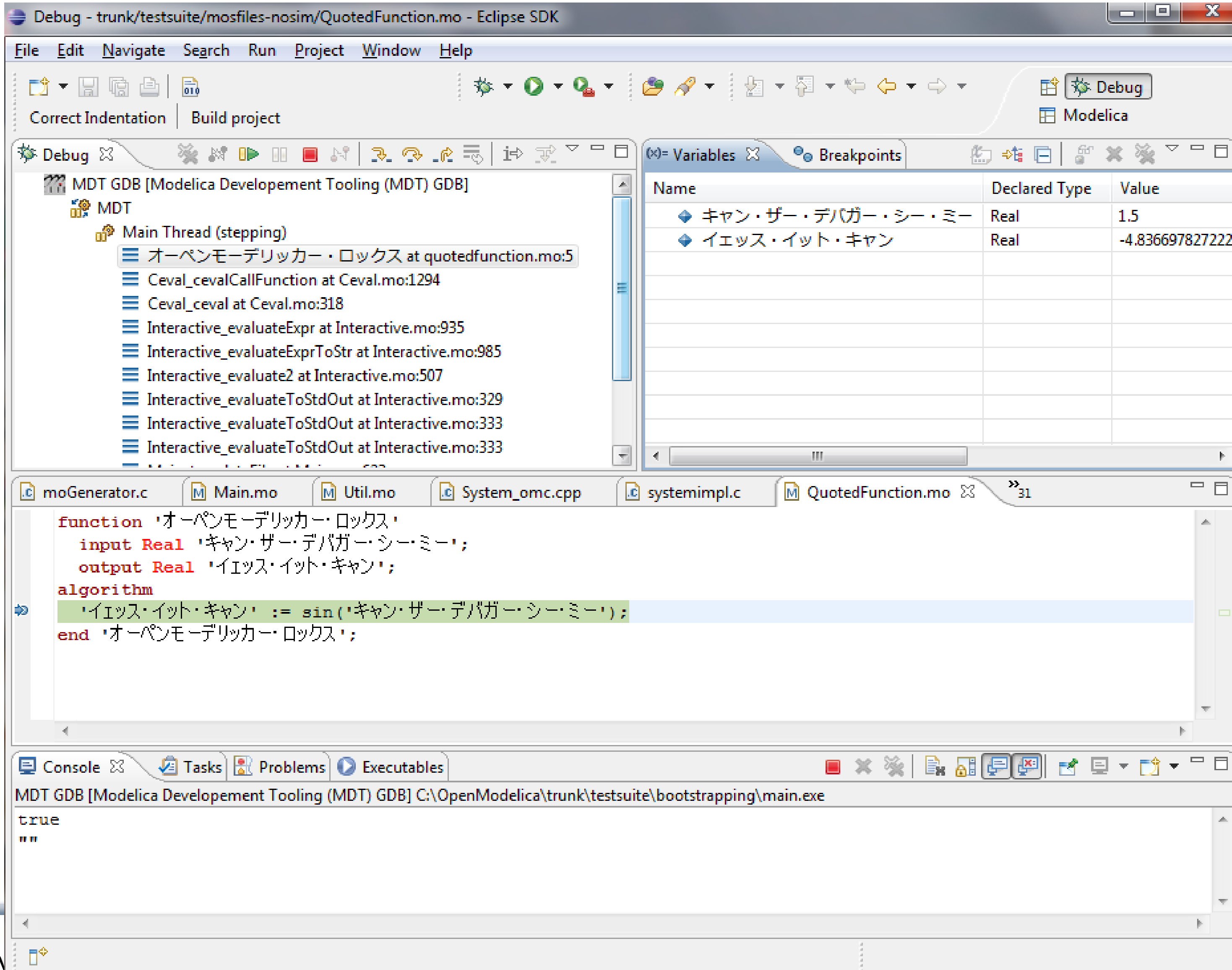
"…the profiler makes the process of performance optimization radically shorter."

OpenModelica MDT Algorithmic Code Debugger

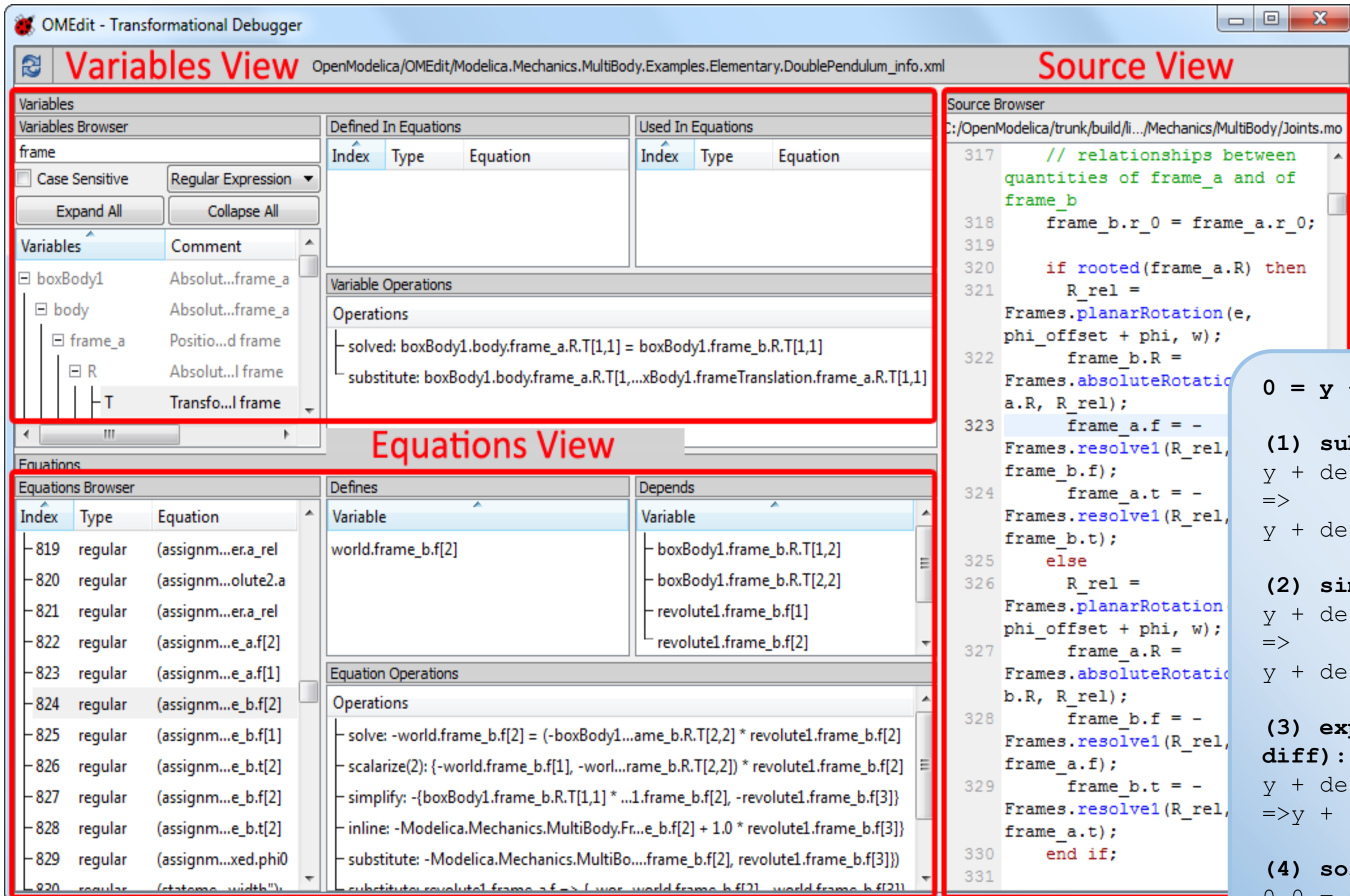


The OpenModelica MDT Debugger (Eclipse-based)

Using Japanese Characters



OpenModelica Equation Model Debugger

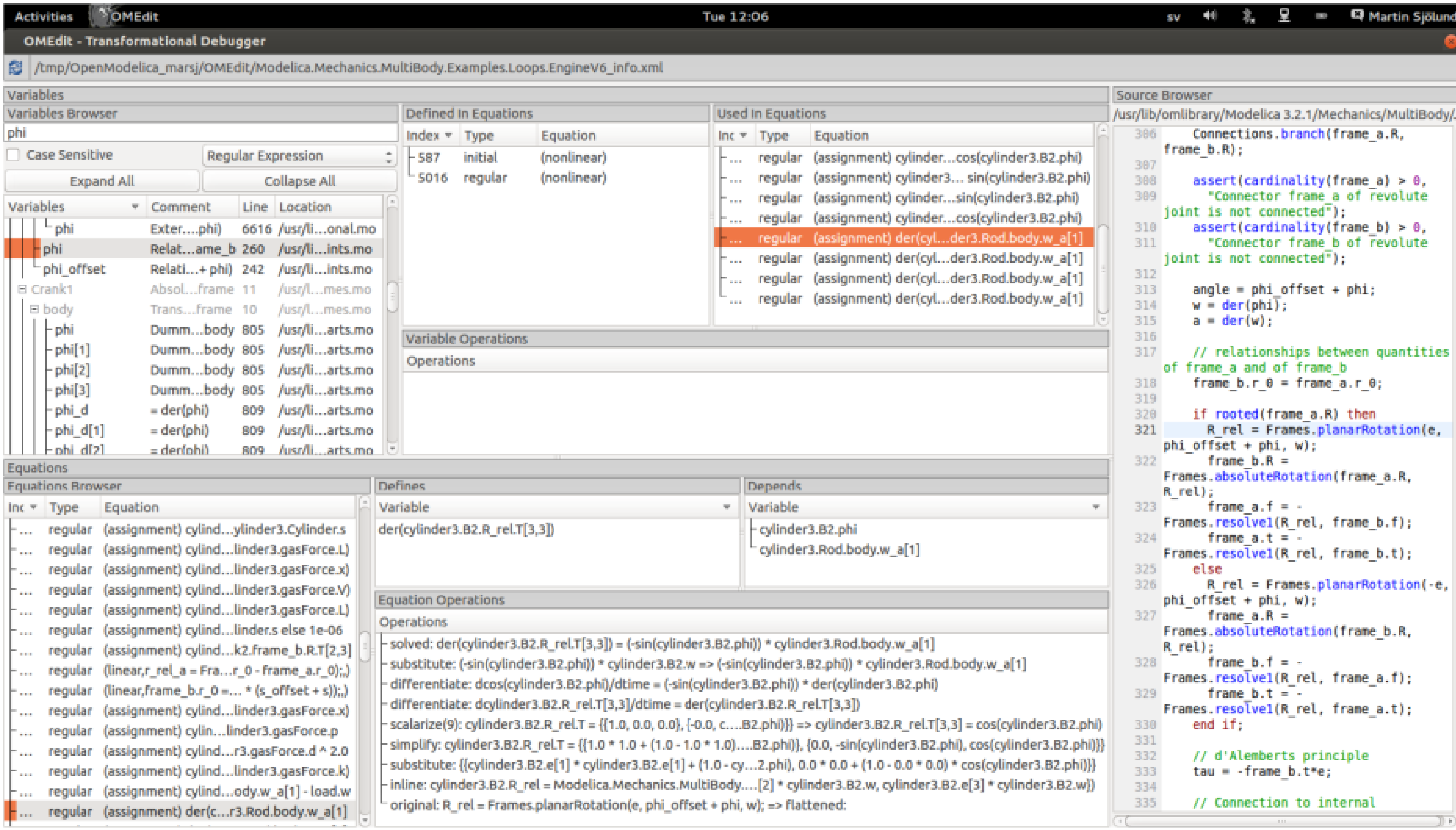


Showing equation transformations of a model:

```
0 = y + der(x * time * z); z = 1.0;

(1) substitution:
y + der(x * (time * z))
=>
y + der(x * (time * 1.0))

(2) simplify:
y + der(x * (time * 1.0))
=>
y + der(x * time)

(3) expand derivative (symbolic diff):
y + der(x * time)
=>y + (x + der(x) * time)

(4) solve:
0.0 = y + (x + der(x) * time)
=>
der(x) = ((-y) - x) / time
time <> 0
```

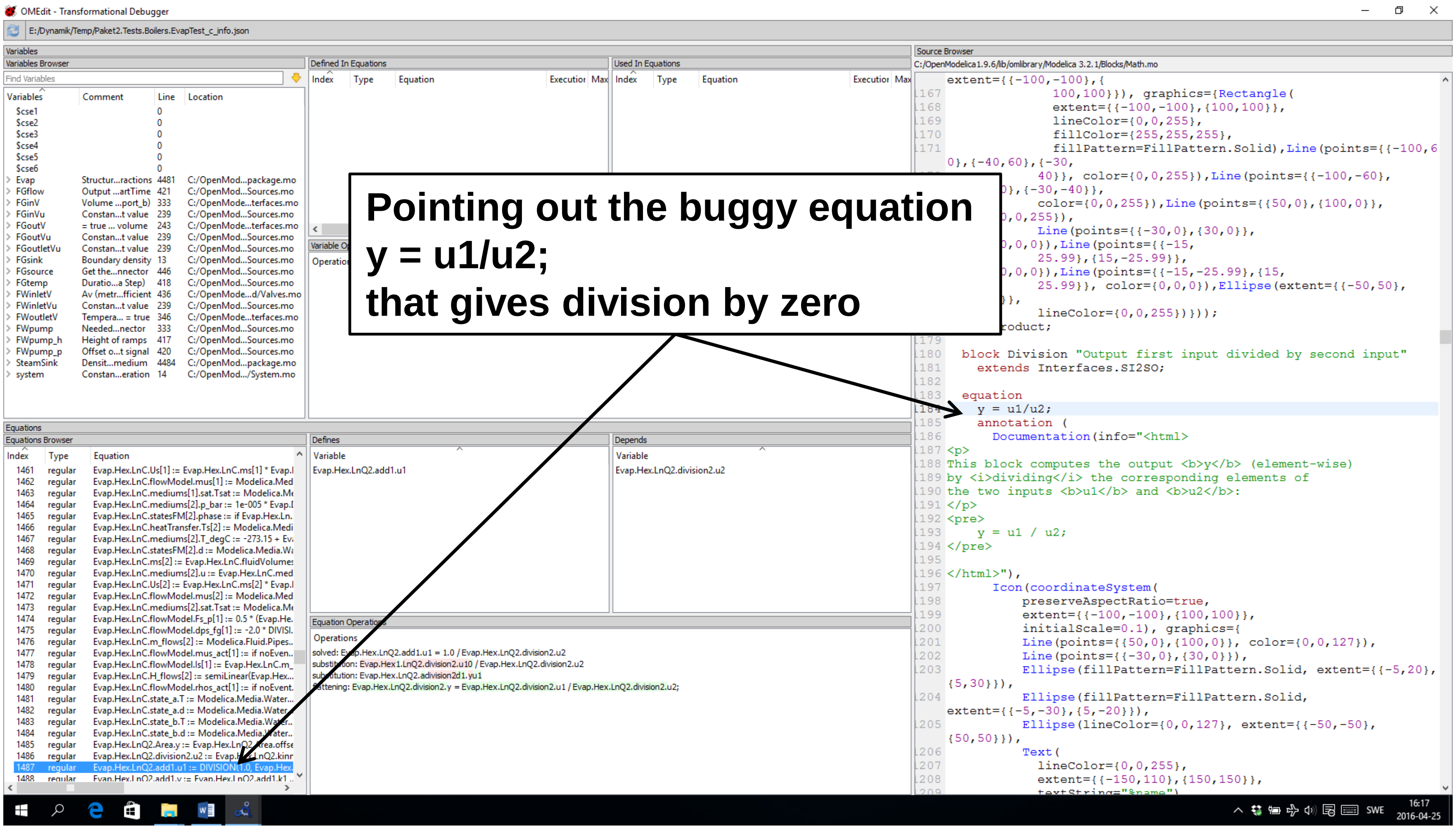
Mapping run-time error to source model position

Transformations Browser – EngineV6 Overview (11 116 equations in model)

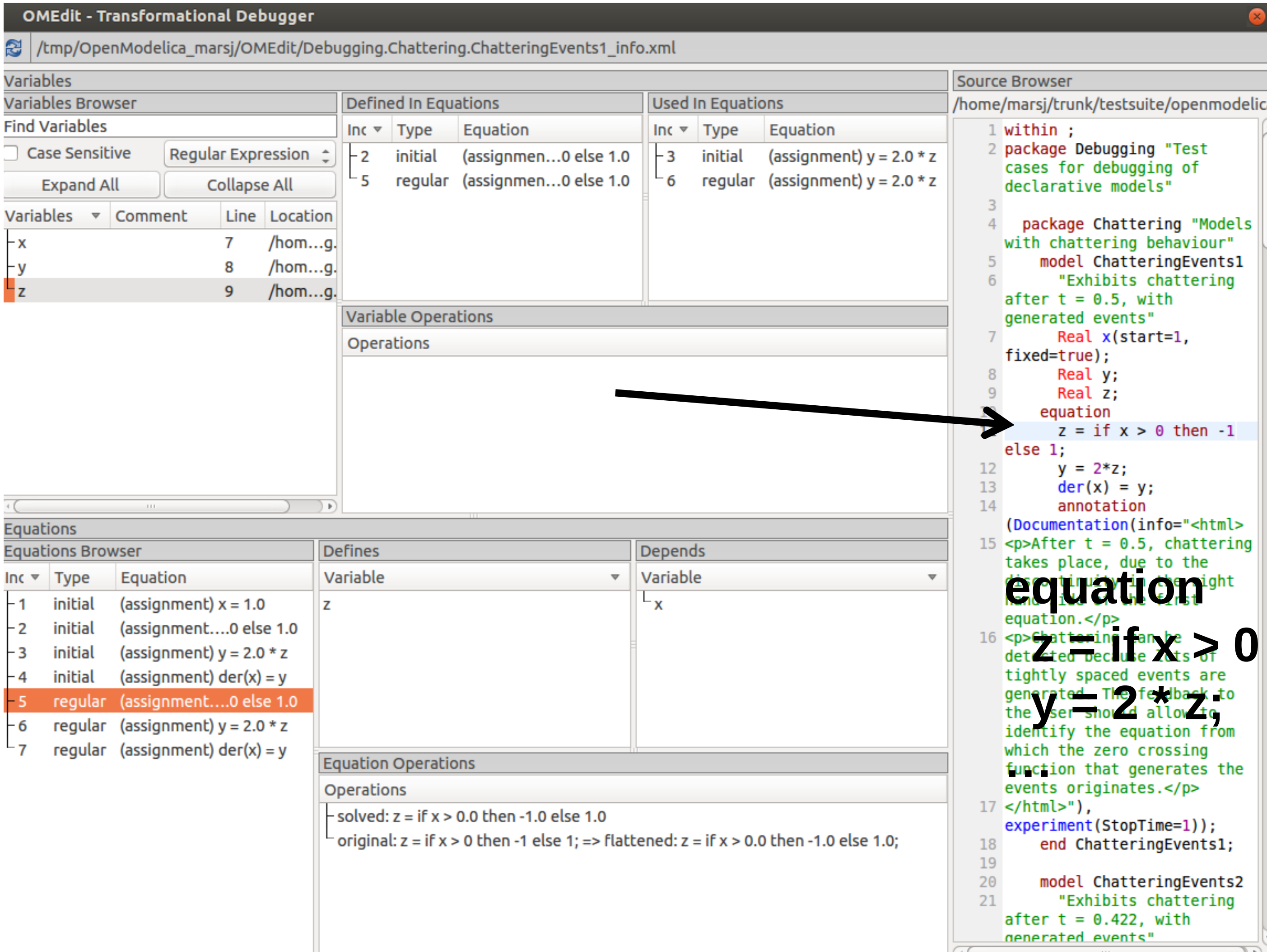


Equation Model Debugger on Siemens Model

(Siemens Evaporator test model, 1100 equations)



Debugging Example – Detecting Source of Chattering (excessive event switching) causing bad performance



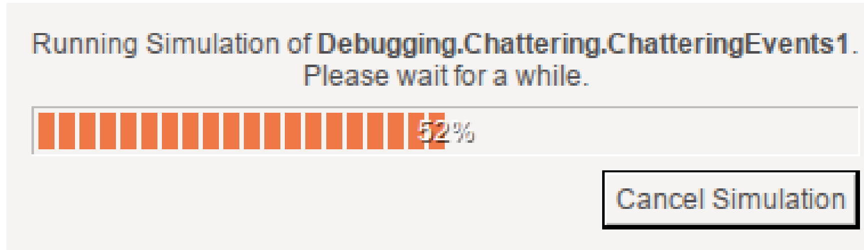
equation

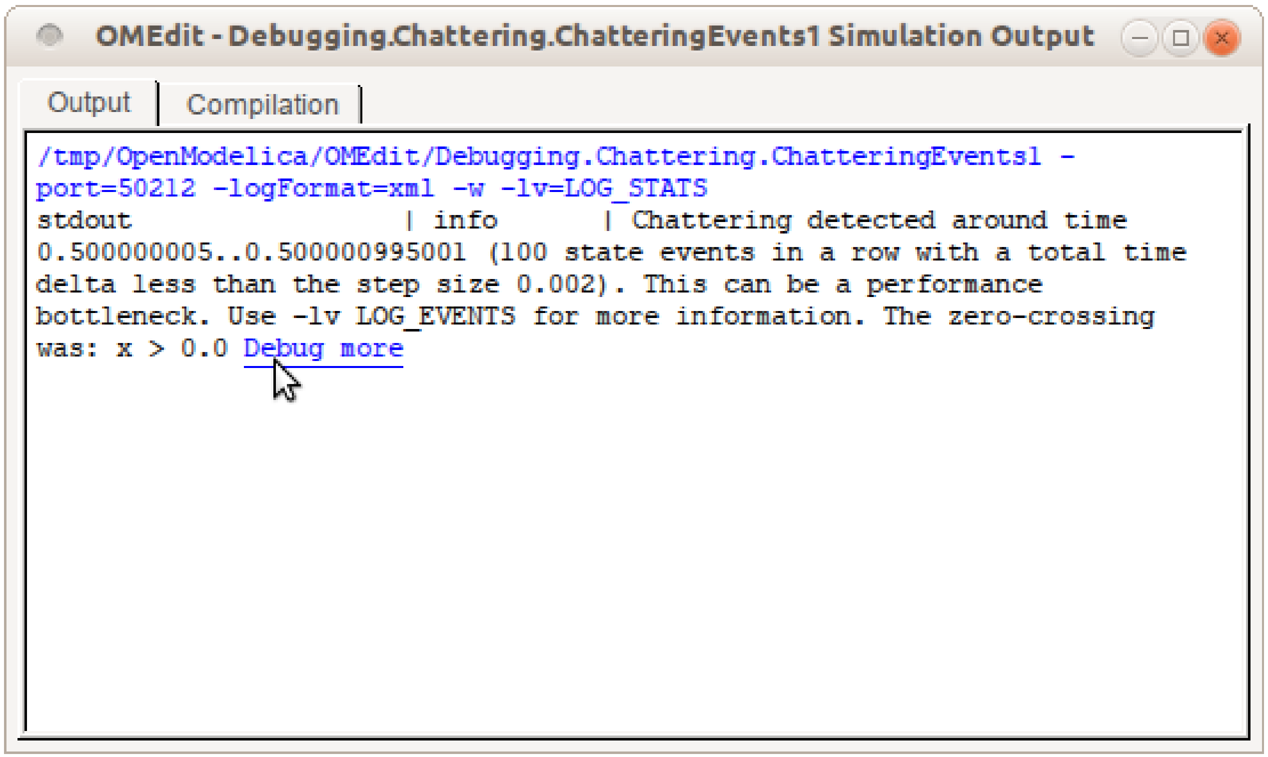
z = if x > 0 then -1 else 1;

y = 2 * z;

...

Error Indication – Simulation Slows Down

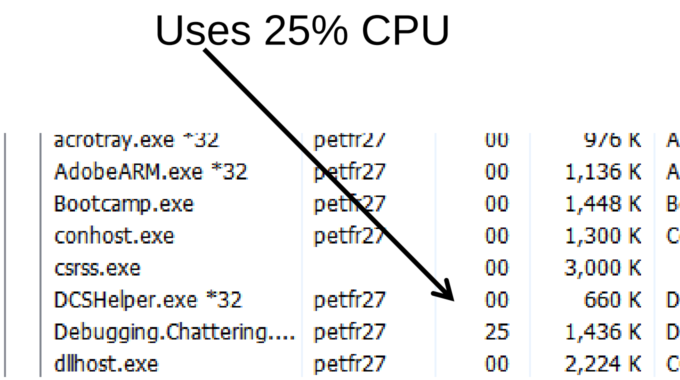




Exercise 1.2 – Equation-based Model Debugger

In the model ChatteringEvents1, chattering takes place after t = 0.5, due to the discontinuity in the right hand side of the first equation. Chattering can be detected because lots of tightly spaced events are generated. The debugger allows to identify the (faulty) equation that gives rise to all the zero crossing events.

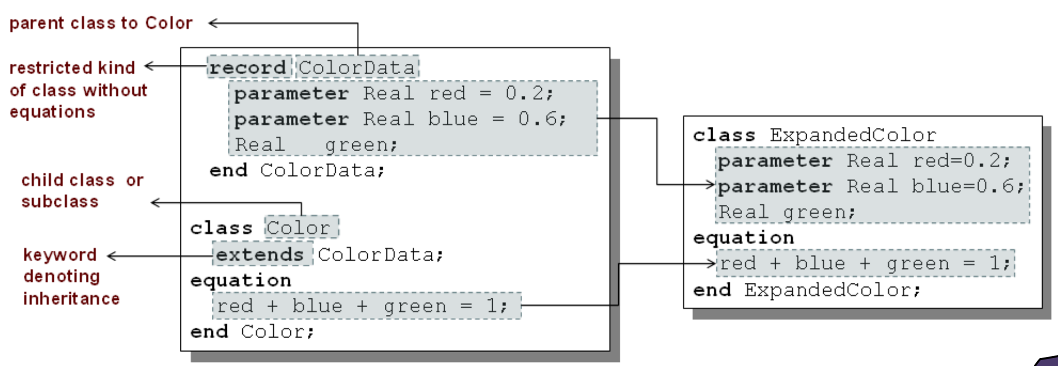
```
model ChatteringEvents1
  Real x(start=1, fixed=true);
  Real y;
  Real z;
equation
  z = noEvent(if x > 0 then -1 else 1);
  y = 2*z;
  der(x) = y;
end ChatteringNoEvents1;
```



- Switch to OMEdit text view (click on text button upper left)
- Open the Debugging.mo package file using OMEdit
- Open subpackage Chattering, then open model ChatteringEvents1
- Simulate in debug mode
- Click on the button Debug more (see prev. slide)
- Possibly start task manager and look at CPU. Then click stop simulation button

Part III

Modelica language concepts and textual modeling



Typed Declarative Equation-based Textual Language

Hybrid Modeling

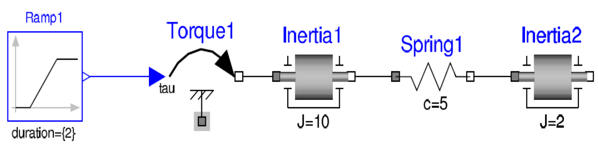
Acausal Modeling

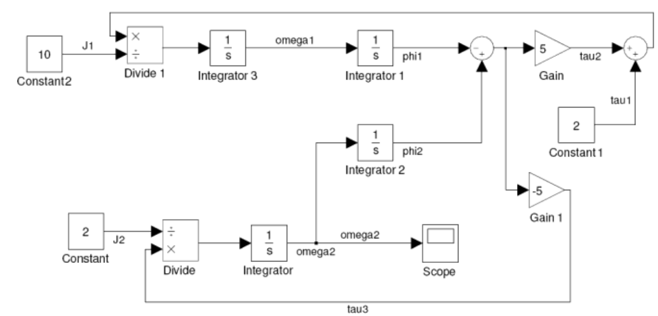
The order of computations is not decided at modeling time

Acausal

Causal

Visual Component Level





Equation Level

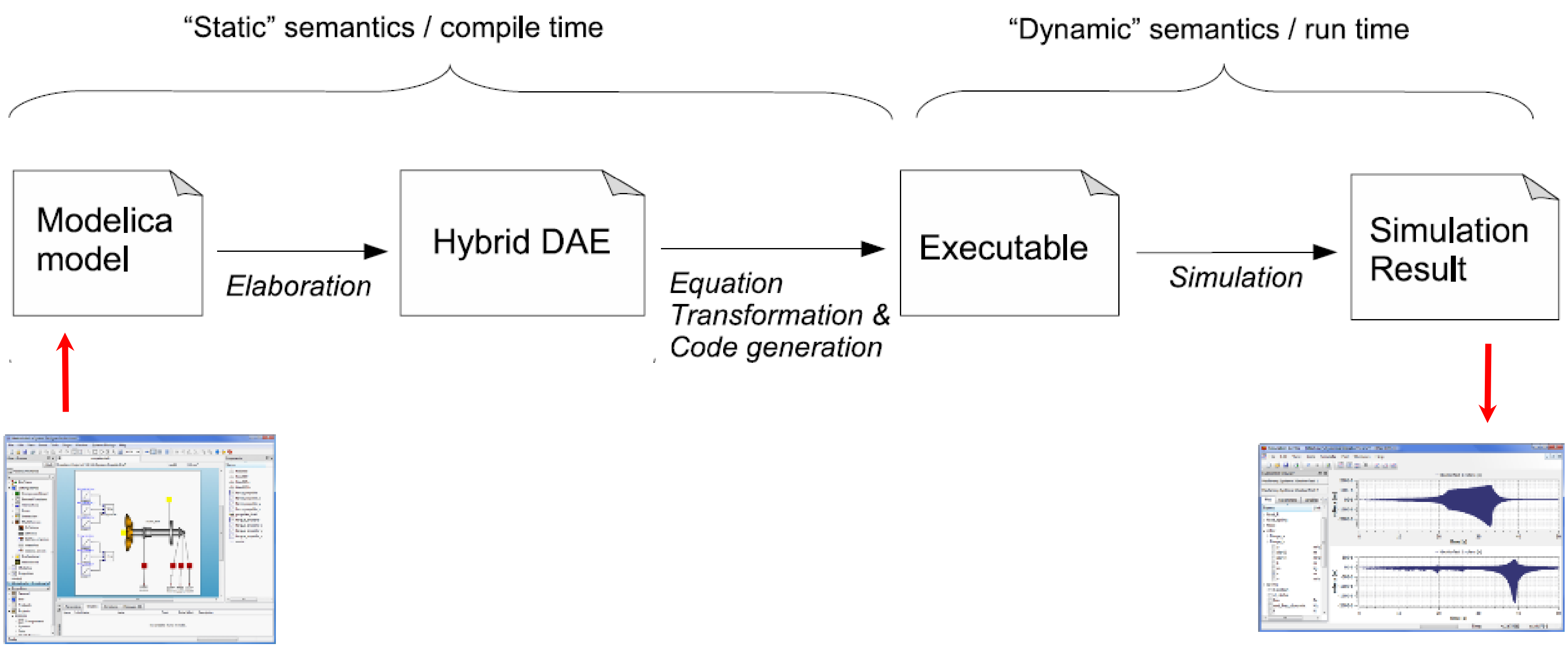
A resistor *equation*:

```
R*i = v;
```

Causal possibilities:

```
i := v/R;
v := R*i;
R := v/i;
```


Typical Simulation Process



Simple model - Hello World!

Equation: $x' = -x$
Initial condition: $x(0) = 1$

Name of model

Initial condition

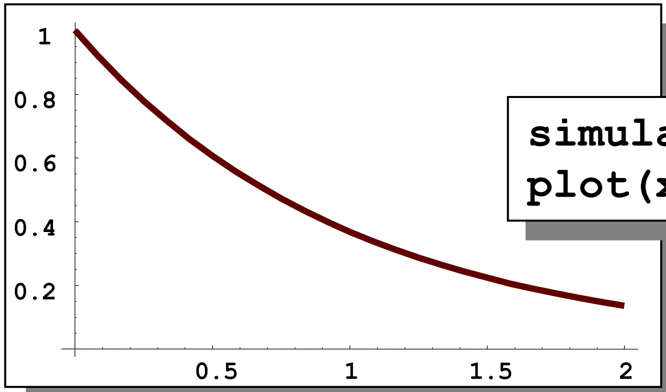
Continuous-time variable

Parameter, constant during simulation

```
model HelloWorld "A simple equation"
  Real x(start=1);
  parameter Real a = -1;
equation
  der(x)= a*x;
end HelloWorld;
```

Differential equation

Simulation in OpenModelica environment




```
simulate(HelloWorld, stopTime = 2)
plot(x)
```

Modelica Variables and Constants

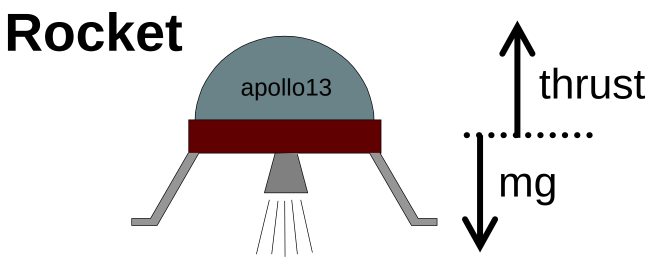
- Built-in primitive data types

Boolean	**true** or **false**
Integer	Integer value, e.g. **42** or **–3**
Real	Floating point value, e.g. **2.4e-6**
String	String, e.g. **“Hello world”**
Enumeration	Enumeration literal e.g. **ShirtSize.Medium**

- Parameters are constant during simulation
- Two types of constants in Modelica
  - **constant**
  - **parameter**

```
constant  Real    PI=3.141592653589793;
constant  String  redcolor = "red";
constant  Integer one = 1;
parameter Real    mass = 22.5;
```


A Simple Rocket Model



$$acceleration = \frac{thrust - mass \cdot gravity}{mass}$$

$$mass' = -massLossRate \cdot abs(thrust)$$

$$altitude' = velocity$$

$$velocity' = acceleration$$

```
class Rocket "rocket class"
  parameter String name;
  Real mass(start=1038.358);
  Real altitude(start= 59404);
  Real velocity(start= -2003);
  Real acceleration;
  Real thrust;  // Thrust force on rocket
  Real gravity; // Gravity forcefield
  parameter Real massLossRate=0.000277;
equation
  (thrust-mass*gravity)/mass = acceleration;
  der(mass)   = -massLossRate * abs(thrust);
  der(altitude) = velocity;
  der(velocity) = acceleration;
end Rocket;
```

new model (class Rocket)

parameters (changeable before the simulation) (parameter String)

floating point type (Real)

differentiation with regards to time (der(velocity))

declaration comment ("rocket class")

start value (start= -2003)

name + default value (massLossRate=0.000277;)

mathematical equation (acausal) ((thrust-mass*gravity)/mass = acceleration;)

Celestial Body Class

A class declaration creates a *type name* in Modelica

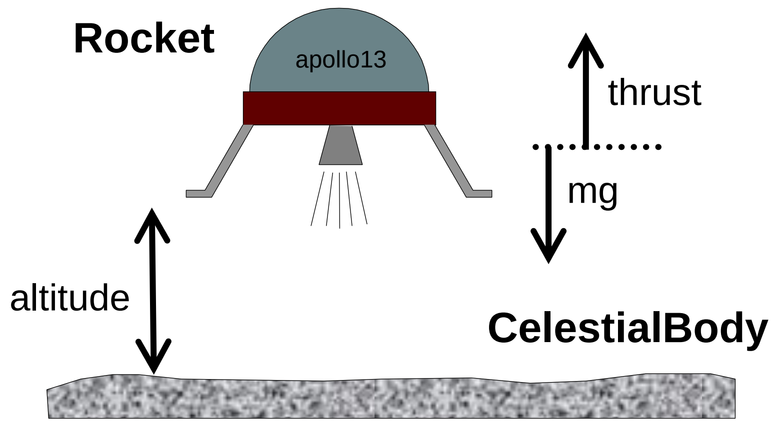
```
class CelestialBody
  constant  Real    g = 6.672e-11;
  parameter Real    radius;
  parameter String  name;
  parameter Real    mass;
end CelestialBody;
```

An *instance* of the class can be declared by *prefixing* the type name to a variable name

```
...
CelestialBody moon;
...
```

The declaration states that **moon** is a variable containing an object of type **CelestialBody**

Moon Landing



$$apollo.gravity = \frac{moon.g \cdot moon.mass}{(apollo.altitude + moon.radius)^2}$$

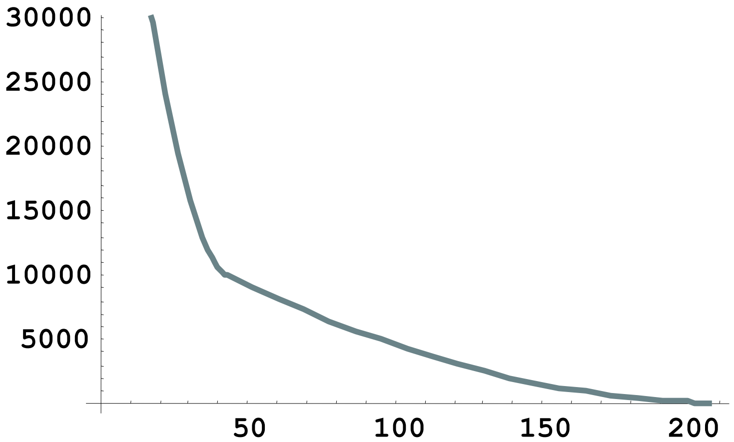
only access inside the class ← protected

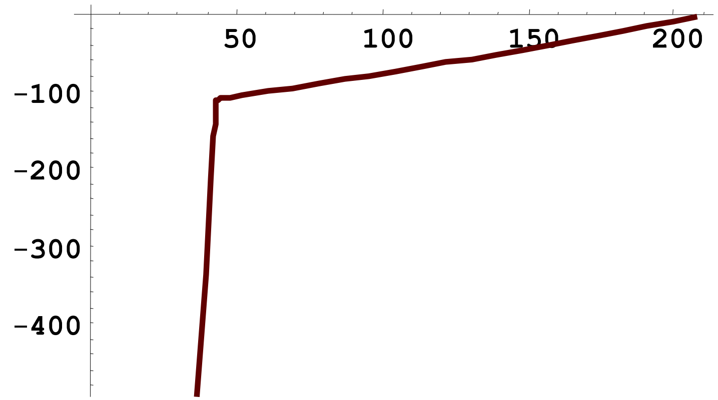
access by dot notation outside the class ← public

```
class MoonLanding
  parameter Real force1 = 36350;
  parameter Real force2 = 1308;
protected
  parameter Real thrustEndTime = 210;
  parameter Real thrustDecreaseTime = 43.2;
public
  Rocket        apollo(name="apollo13");
  CelestialBody   moon(name="moon",mass=7.382e22,radius=1.738e6);
equation
  apollo.thrust = if (time < thrustDecreaseTime) then force1
                  else if (time < thrustEndTime) then force2
                  else 0;
  apollo.gravity=moon.g*moon.mass/(apollo.altitude+moon.radius)^2;
end MoonLanding;
```


Simulation of Moon Landing

```
simulate(MoonLanding, stopTime=230)
plot(apollo.altitude, xrange={0,208})
plot(apollo.velocity, xrange={0,208})
```





It starts at an altitude of 59404 (not shown in the diagram) at time zero, gradually reducing it until touchdown at the lunar surface when the altitude is zero

The rocket initially has a high negative velocity when approaching the lunar surface. This is reduced to zero at touchdown, giving a smooth landing

Specialized Class Keywords

- Classes can also be declared with other keywords, e.g.: `model`, `record`, `block`, `connector`, `function`, ...
- Classes declared with such keywords have specialized properties
- Restrictions and enhancements apply to contents of specialized classes
- After Modelica 3.0 the `class` keyword means the same as `model`

- Example: (Modelica 2.2). A `model` is a class that cannot be used as a connector class
- Example: A `record` is a class that only contains data, with no equations
- Example: A `block` is a class with fixed input-output causality

```
model CelestialBody
  constant  Real    g = 6.672e-11;
  parameter Real    radius;
  parameter String  name;
  parameter Real    mass;
end CelestialBody;
```


Modelica Functions

- Modelica Functions can be viewed as a specialized class with some restrictions and extensions
- A function can be called with arguments, and is instantiated dynamically when called

```
function sum
  input  Real arg1;
  input  Real arg2;
  output Real result;
algorithm
  result := arg1+arg2;
end sum;
```


Function Call – Example Function with for-loop

Example Modelica function call:

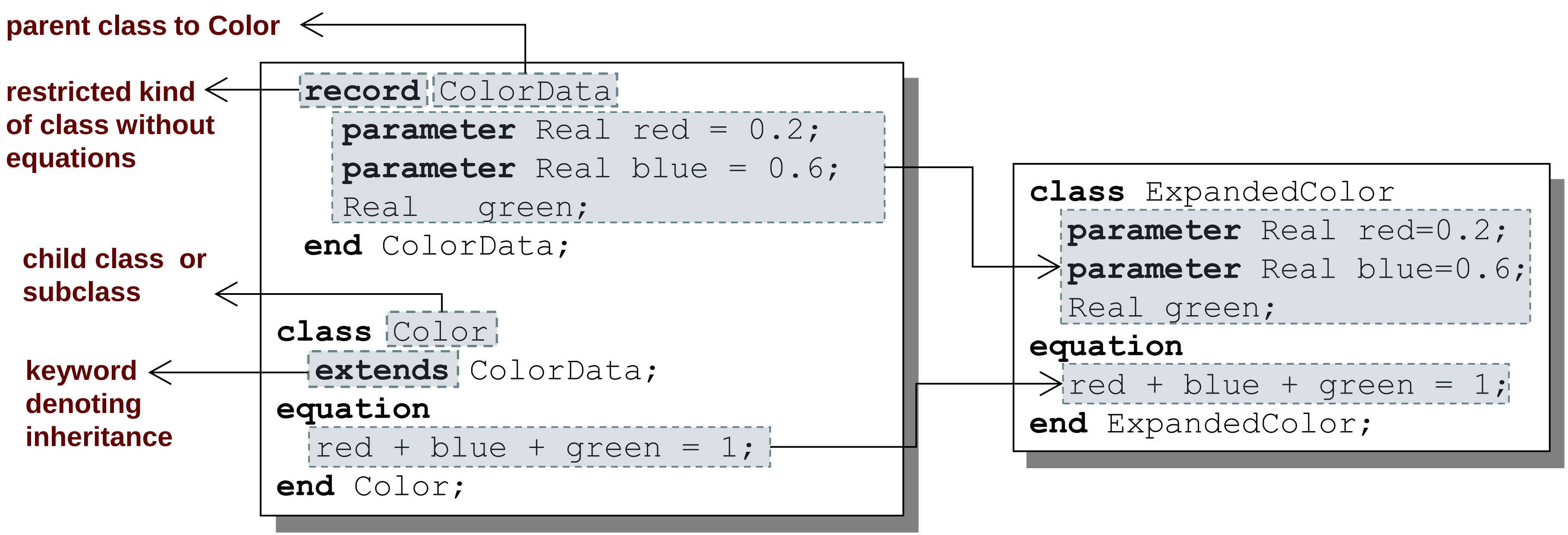
```
...
  p = polynomialEvaluator({1,2,3,4},21)
```

`{1,2,3,4}` becomes the value of the coefficient vector `A`, and `21` becomes the value of the formal parameter `x`.

```
function PolynomialEvaluator
  input  Real A[:];        // array, size defined
                           // at function call time
  input  Real x := 1.0;// default value 1.0 for x
  output Real sum;
protected
  Real   xpower;           // local variable xpower
algorithm
  sum := 0;
  xpower := 1;
  for i in 1:size(A,1) loop
    sum := sum + A[i]*xpower;
    xpower := xpower*x;
  end for;
end PolynomialEvaluator;
```

The function `PolynomialEvaluator` computes the value of a polynomial given two arguments:
a coefficient vector `A` and a value of `x`.

Inheritance



Data and behavior: field declarations, equations, and certain other contents are *copied* into the subclass

Multiple Inheritance

Multiple Inheritance is fine – inheriting both geometry and color

```
class Color
  parameter Real red=0.2;
  parameter Real blue=0.6;
  Real green;
equation
  red + blue + green = 1;
end Color;
```

```
class Point
  Real x;
  Real y,z;
end Point;
```

```
class ColoredPoint
  extends Point;
  extends Color;
end ColoredPoint;
```

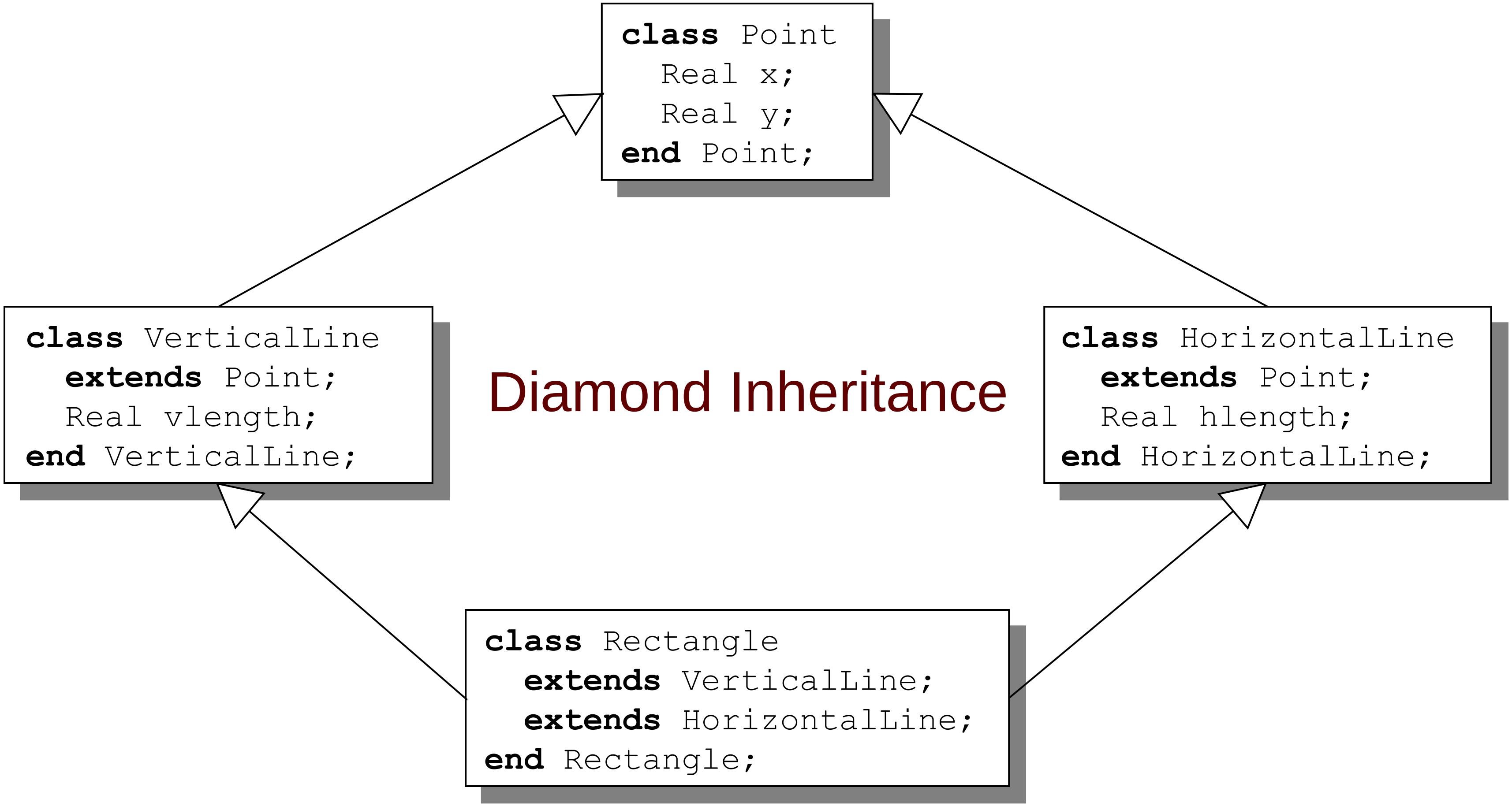
multiple inheritance

Equivalent to

```
class ColoredPointWithoutInheritance
  Real x;
  Real y, z;
  parameter Real red = 0.2;
  parameter Real blue = 0.6;
  Real green;
equation
  red + blue + green = 1;
end ColoredPointWithoutInheritance;
```

Multiple Inheritance cont'

Only one copy of multiply inherited class `Point` is kept



Simple Class Definition

- Simple Class Definition
  - Shorthand Case of Inheritance
- Example:

```
class SameColor = Color;
```

Equivalent to:

inheritance

```
class SameColor
  extends Color;
end SameColor;
```

- Often used for introducing new names of types:

```
type Resistor = Real;
```

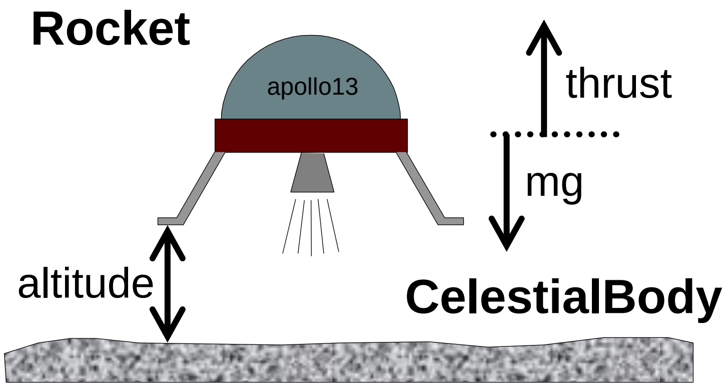
```
connector MyPin = Pin;
```


Inheritance Through Modification

- Modification is a concise way of combining inheritance with declaration of classes or instances
- A *modifier* modifies a declaration equation in the inherited class
- Example: The class `Real` is inherited, modified with a different `start` value equation, and instantiated as an `altitude` variable:

```
...
 Real altitude(start= 59404);
...
```


The Moon Landing - Example Using Inheritance (I)




```
model Rocket "generic rocket class"
  extends Body;
  parameter Real massLossRate=0.000277;
  Real altitude(start= 59404);
  Real velocity(start= -2003);
  Real acceleration;
  Real thrust;
  Real gravity;
equation
  thrust-mass*gravity= mass*acceleration;
  der(mass)= -massLossRate*abs(thrust);
  der(altitude)= velocity;
  der(velocity)= acceleration;
end Rocket;
```

```
model Body "generic body"
  Real   mass;
  String name;
end Body;
```

```
model CelestialBody
  extends Body;
  constant  Real g = 6.672e-11;
  parameter Real radius;
end CelestialBody;
```

Extra slide

The Moon Landing - Example using Inheritance (II)

inherited parameters

```
model MoonLanding
 parameter Real force1 = 36350;
 parameter Real force2 = 1308;
 parameter Real thrustEndTime = 210;
 parameter Real thrustDecreaseTime = 43.2;
 Rocket           apollo(name="apollo13", mass(start=1038.358) );
 CelestialBody    moon(mass=7.382e22,radius=1.738e6,name="moon");
equation
 apollo.thrust = if (time<thrustDecreaseTime) then force1
                 else if (time<thrustEndTime) then force2
                 else 0;
 apollo.gravity =moon.g*moon.mass/(apollo.altitude+moon.radius)^2;
end Landing;
```


Inheritance of Protected Elements

If an `extends`-clause is preceded by the `protected` keyword, all inherited elements from the superclass become protected elements of the subclass

```
class Color
  Real red;
  Real blue;
  Real green;
equation
  red + blue + green = 1;
end Color;
```

```
class Point
  Real x;
  Real y,z;
end Point;
```

```
class ColoredPoint
 protected
  extends Color;
 public
  extends Point;
end ColoredPoint;
```

Equivalent to

```
class ColoredPointWithoutInheritance
  Real x;
  Real y,z;
  protected Real red;
  protected Real blue;
  protected Real green;
equation
  red + blue + green = 1;
end ColoredPointWithoutInheritance;
```

The inherited fields from `Point` keep their protection status since that `extends`-clause is preceded by `public`

A protected element cannot be accessed via dot notation!

Exercises Part III a
(15 minutes)

Exercises Part III a

- Start OMNotebook (part of OpenModelica)
  - **Start-**>Programs->OpenModelica->OMNotebook
  - **Open File**: Exercises-ModelicaTutorial.onb from the directory you copied your tutorial files to.
  - **Note**: The DrModelica electronic book has been automatically opened when you started OMNotebook.
  - (**Alternatively**: Open the OMWeb notebook http://omwebbook.openmodelica.org/
- Open Exercises-ModelicaTutorial.pdf (also available in printed handouts)

Exercises 2.1 and 2.2 (See also next two pages)

- Open the **Exercises-ModelicaTutorial.onb** found in the Tutorial directory you copied at installation.
- **Exercise 2.1**. Simulate and plot the HelloWorld example. Do a slight change in the model, re-simulate and re-plot. Try command-completion, val( ), etc.

```
class HelloWorld "A simple equation"
  Real x(start=1);
equation
  der(x)= -x;
end HelloWorld;
```

```
simulate(HelloWorld, stopTime = 2)
plot(x)
```

- Locate the VanDerPol model in DrModelica (link from Section 2.1), using OMNotebook!
- **(extra) Exercise 2.2**: Simulate and plot VanDerPol. Do a slight change in the model, re-simulate and re-plot.

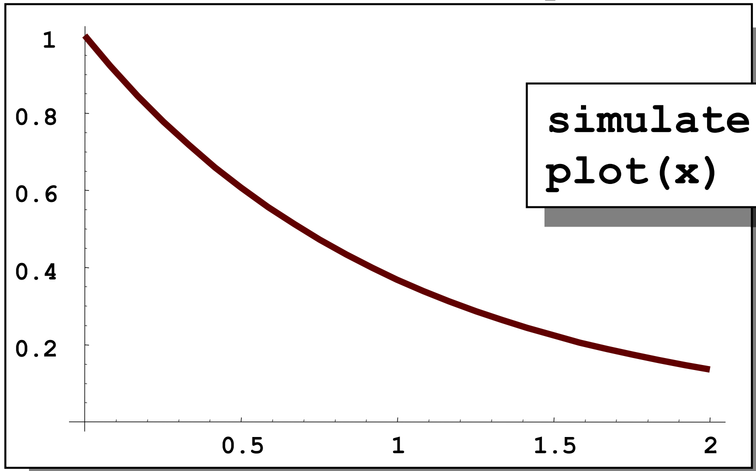
Exercise 2.1 – Hello World!

A Modelica "Hello World" model

Equation: x' = - x
Initial condition: x(0) = 1

```
class HelloWorld "A simple equation"
  parameter Real a=-1;
  Real x(start=1);
equation
  der(x)= a*x;
end HelloWorld;
```

Simulation in OpenModelica environment

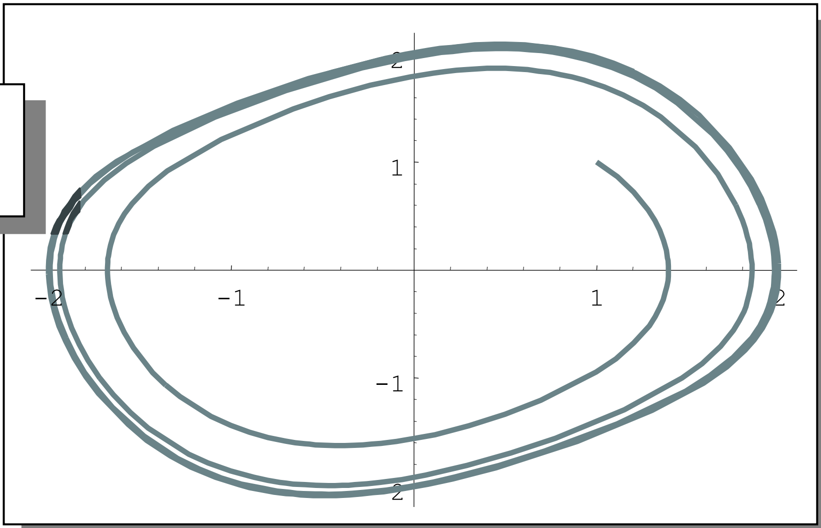



```
simulate(HelloWorld, stopTime = 2)
plot(x)
```

(extra) Exercise 2.2 – Van der Pol Oscillator

```
class VanDerPol  "Van der Pol oscillator model"
  Real x(start = 1)  "Descriptive string for x"; // x starts at 1
  Real y(start = 1)  "y coordinate";             // y starts at 1
  parameter Real lambda = 0.3;
equation
  der(x) = y;                          // This is the 1st diff equation //
  der(y) = -x + lambda*(1 - x*x)*y;   /* This is the 2nd diff equation */
end VanDerPol;
```

```
simulate(VanDerPol,stopTime = 25)
plotParametric(x,y)
```



(extra) Exercise 2.3 – DAE Example

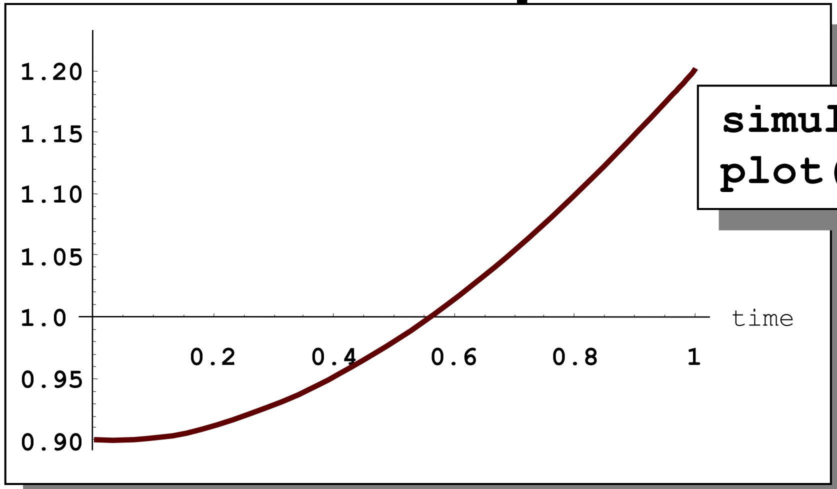
Include algebraic equation

Algebraic equations contain no derivatives

Exercise: Locate in DrModelica. Simulate and plot. Change the model, simulate+plot.

```
class DAEexample
  Real x(start=0.9);
  Real y;
equation
  der(y)+(1+0.5*sin(y))*der(x)
    = sin(time);
  x - y = exp(-0.9*x)*cos(y);
end DAEexample;
```

Simulation in OpenModelica environment




```
simulate(DAEexample, stopTime = 1)
plot(x)
```


Exercise 2.4 – Model the system below

- Model this Simple System of Equations in Modelica

$$\dot{x} = 2 * x * y - 3 * x$$

$$\dot{y} = 5 * y - 7 * x * y$$

$$x(0) = 2$$

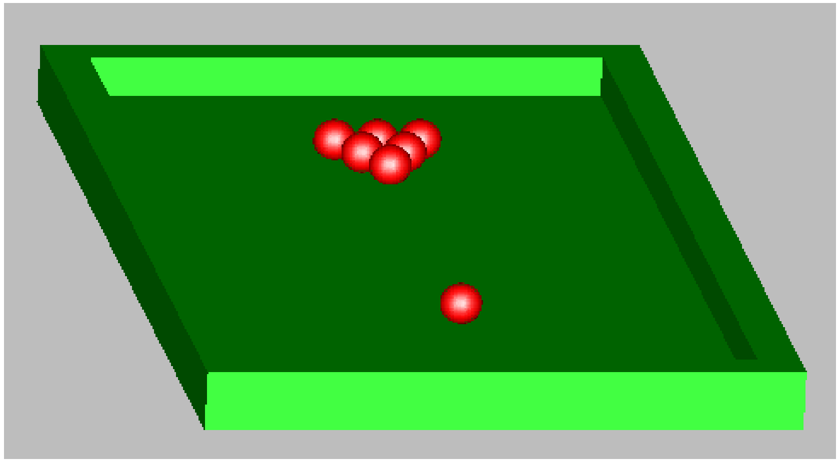
$$y(0) = 3$$

(extra) Exercise 2.5 – Functions

- a) Write a function, **`sum2`**, which calculates the sum of Real numbers, for a vector of arbitrary size.

- b) Write a function, **`average`**, which calculates the average of Real numbers, in a vector of arbitrary size. The function **`average`** should make use of a function call to **`sum2`**.

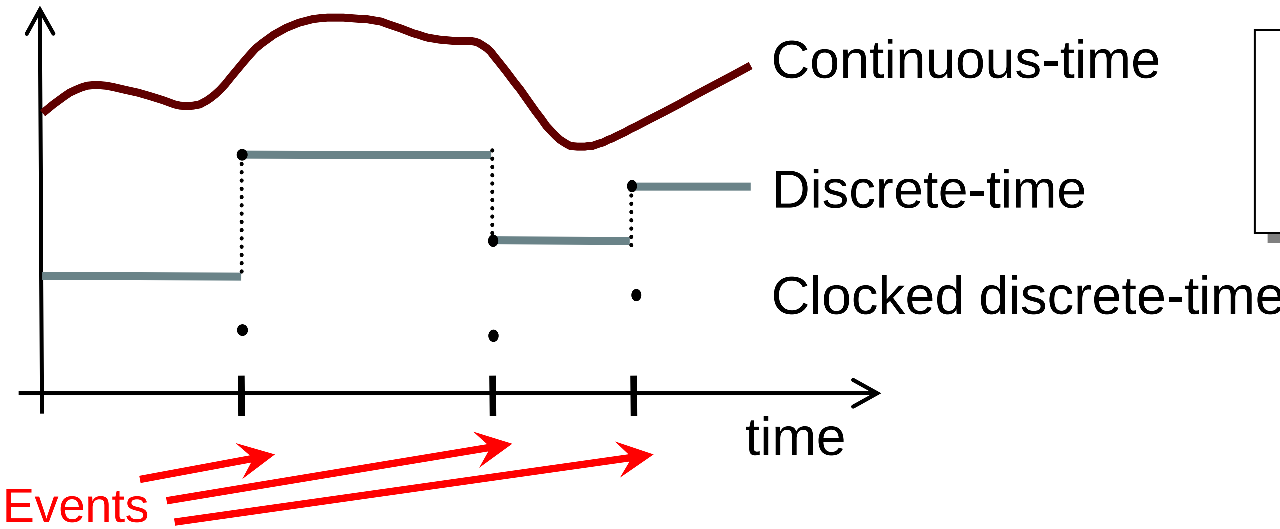
Part III b
Discrete Events and Hybrid Systems



Picture: Courtesy Hilding Elmqvist

Modelica Hybrid Modeling

Hybrid modeling = continuous-time + discrete-time modeling




```
Real x;
Voltage v;
Current i;
```

```
discrete Real x;
Integer i;
Boolean b;
```

- A *point* in time that is instantaneous, i.e., has zero duration
- An *event condition* or *clock tick* so that the event can take place
- A set of *variables* that are associated with the event
- Some *behavior* associated with the event,
  e.g. *conditional equations* that become active or are deactivated at the event

Event Creation – if

if-equations, if-statements, and if-expressions

```
if <condition> then
  <equations>
elseif <condition> then
  <equations>
else
  <equations>
end if;
```

```
model Diode "Ideal diode"
  extends TwoPin;
  Real s;
  Boolean off;
equation
  off = s < 0;
  if off then
    v=s
  else
    v=0;
  end if;
  i = if off then 0 else s;
end Diode;
```

false if `s<0`

If-equation choosing equation for `v`

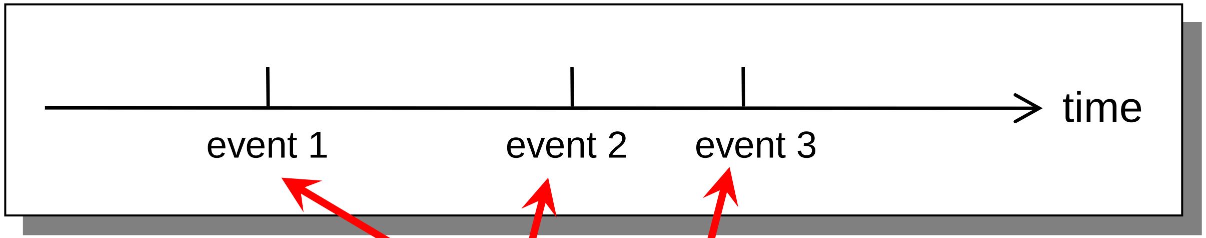
If-expression

Event Creation – when

when-equations *(two kinds: unclocked and clocked)*

when *<conditions>* **then**
  <equations>
end when; // un-clocked version

when *clock* **then**
  <equations>
end when;   // clocked version



Equations only active at event times

Time event

```
when time >= 10.0 then
   ...
end when;
```

Only dependent on time, can be scheduled in advance

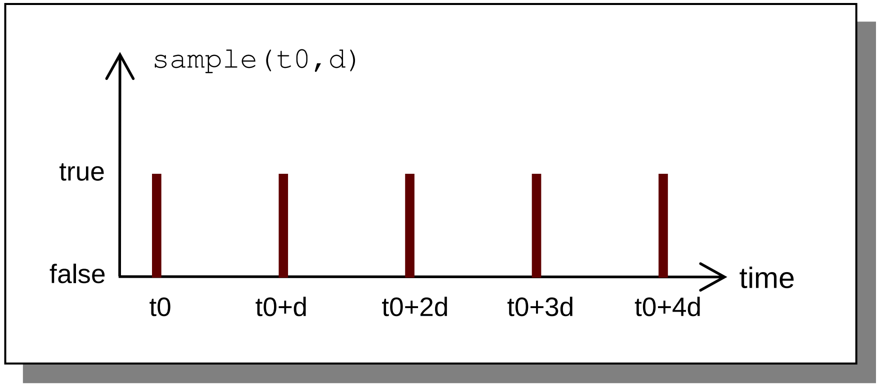
State event

```
when sin(x) > 0.5 then
   ...
end when;
```

Related to a state. Check for zero-crossing

Generating Repeated Events by unclocked sample

The call `sample(t0,d)` returns true and triggers events at times `t0+i*d`, where `i=0,1,` …

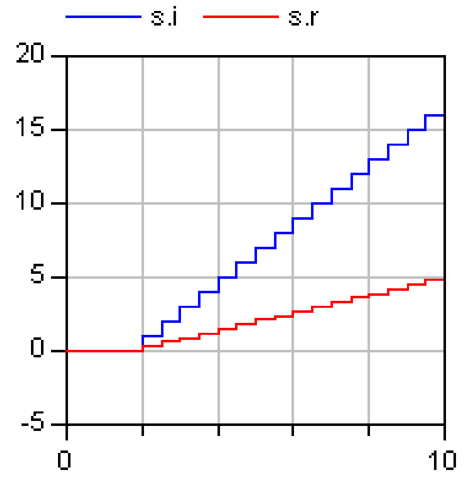


Variables need to be discrete

```
model SamplingClock
  Integer i;
  discrete Real r;
equation
  when sample(2,0.5) then
    i = pre(i)+1;
    r = pre(r)+0.3;
  end when;
end SamplingClock;
```

Creates an event after 2 s, then each 0.5 s

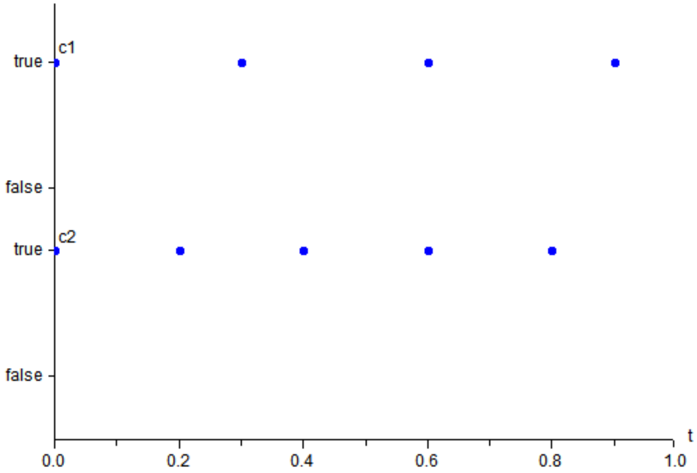
pre(...) takes the previous value before the event.



Generating Clock Tick Events using Clock()
(clocked models, Modelica 3.3)

- Clock( ) – inferred clock
- Clock(intervalCounter, resolution) – clock with Integer quotient (rational number) interval
- Clock(interval) – clock with a Real value interval
- Clock(condition, startInterval)
- Clock – solver clock

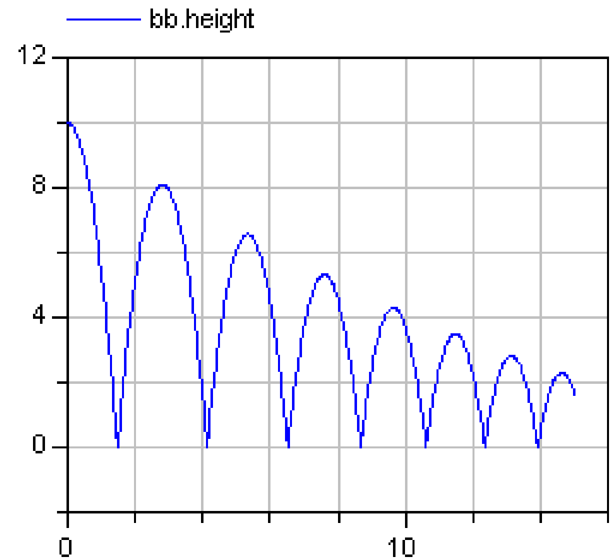
```
class ClockTicks
  // Integer quotient rational number interval clock
  Clock c1 = Clock(3,10);        // ticks: 0, 3/10, 6/10, ..
  // Clock with real value interval between ticks
  Clock c2 = Clock(0.2);         // ticks: 0.0, 0.2, 0.4, ...
end ClockTicks;
```



Reinit - Discontinuous Changes

The value of a *continuous-time* state variable can be instantaneously changed by a `reinit`-equation within a `when`-equation

```
model BouncingBall "the bouncing ball model"
  parameter Real g=9.81;   //gravitational acc.
  parameter Real c=0.90;   //elasticity constant
  Real height(start=10),velocity(start=0);
equation
  der(height) = velocity;
  der(velocity)=-g;
  when height<0 then
    reinit(velocity, -c*velocity);
  end when;
end BouncingBall;
```

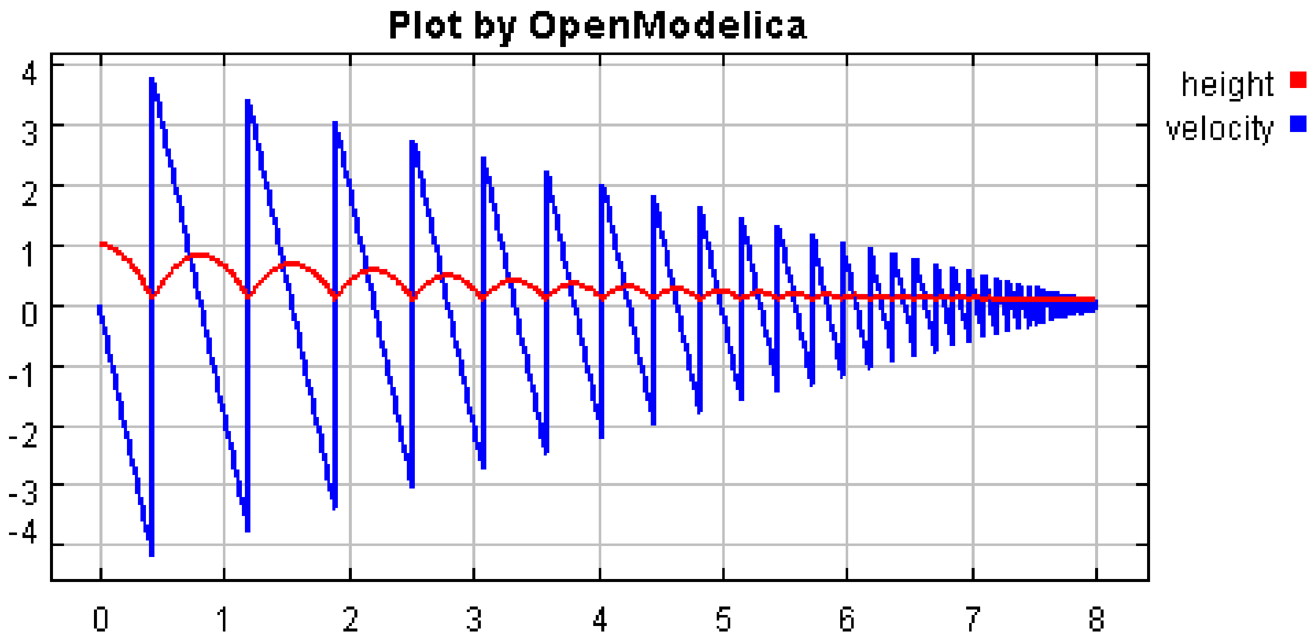


Initial conditions

Reinit "assigns" continuous-time variable `velocity` a new value

Exercise 2.6 – BouncingBall

- Locate the BouncingBall model in one of the hybrid modeling sections of DrModelica (the When-Equations link in Section 2.9), run it, change it slightly, and re-run it.



Part IIIc

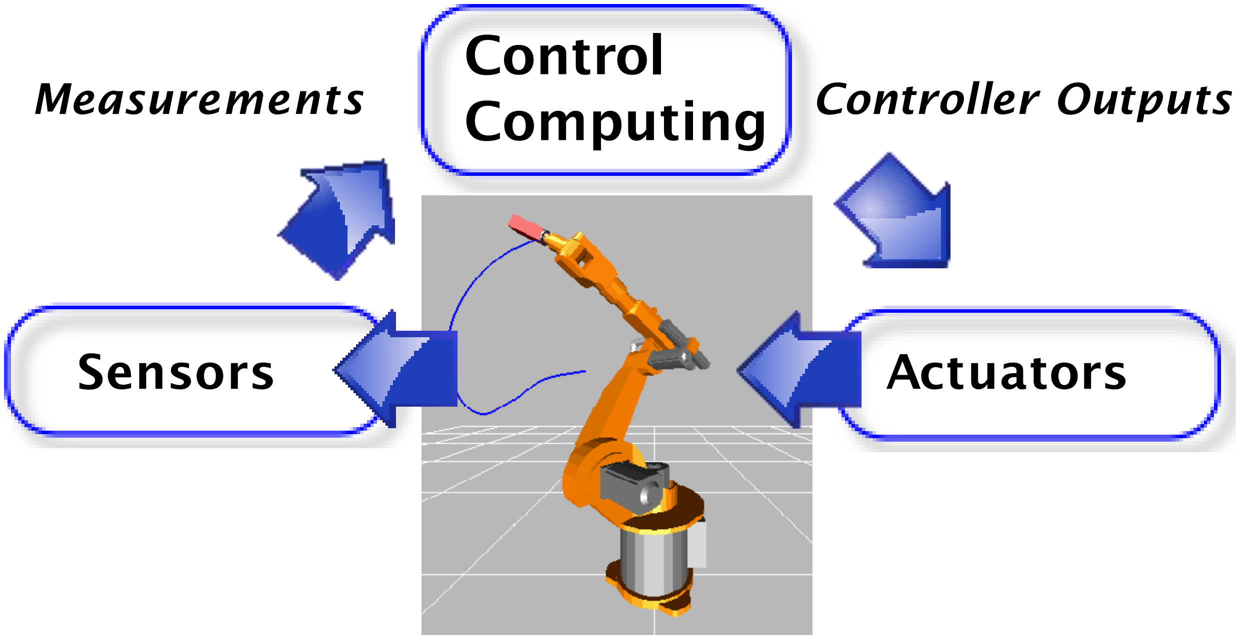
Clocked Synchronous Models and State Machines

and Applications for Digital Controllers

Control System Applications

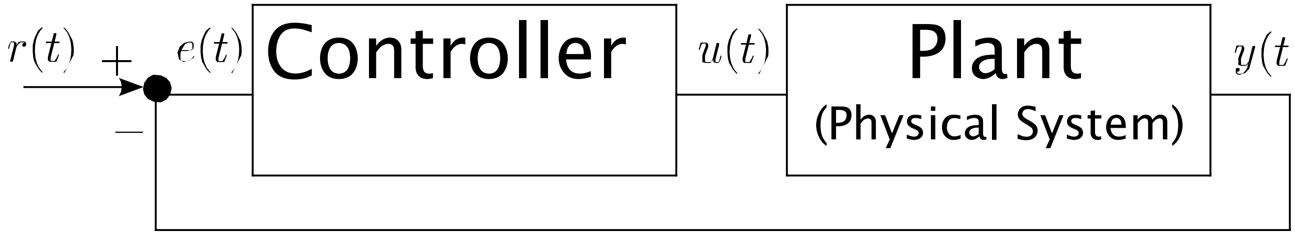
Control System

A control system is a device, or set of devices, that manages, commands, directs or regulates the behavior of other devices or systems (wikipedia).



MODELICA

Control Theory Perspective
Feedback Control System

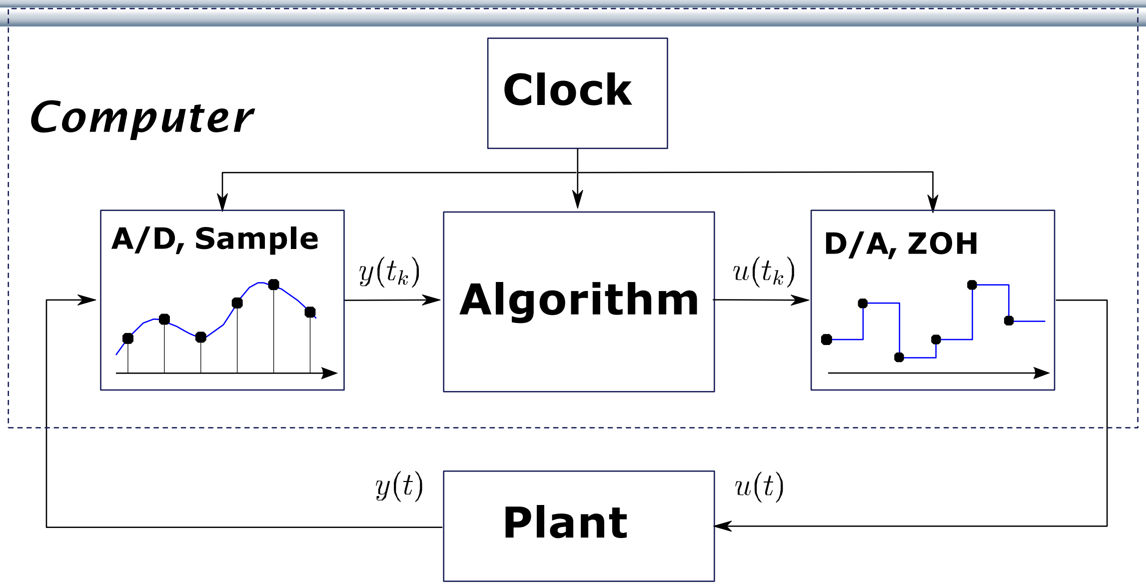


$r(t)$	**reference (setpoint)**
$e(t)$	**error**
$y(t)$	**measured process variable (plant output)**
$u(t)$	**control output variable (plant input)**

Usual Objective

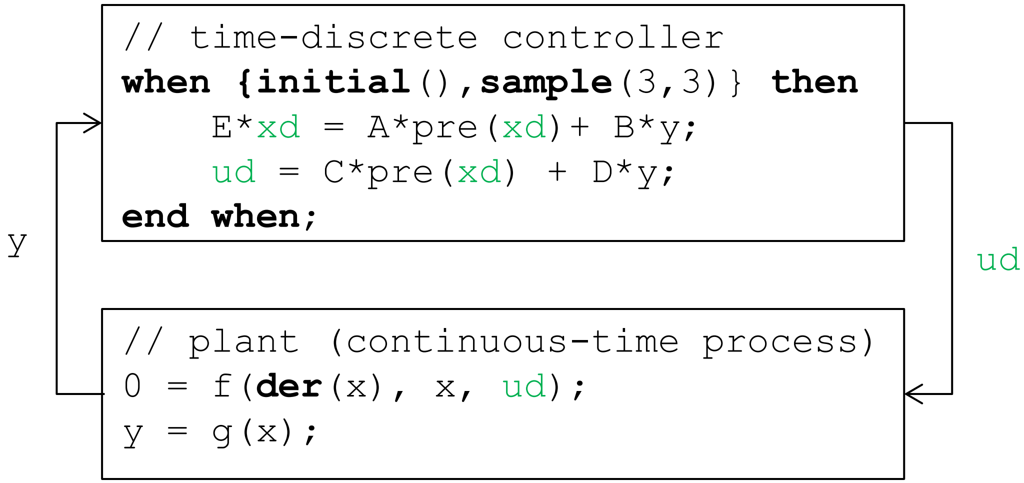
Plant output should follow the reference signal.

Embedded Real-Time Control System



1. ***Discrete-time*** controller + ***continuous-time*** plant ≡ *hybrid system* or *sampled-data system*
2. Interface between digital and analog world: Analog to Digital and Digital to Analog Converters (ADC and DAC).
3. ADC→Algorithm→DAC is synchronous (zero-delay model!)
4. A *clock* controls the *sampling instants*. Usually *periodic sampling*.

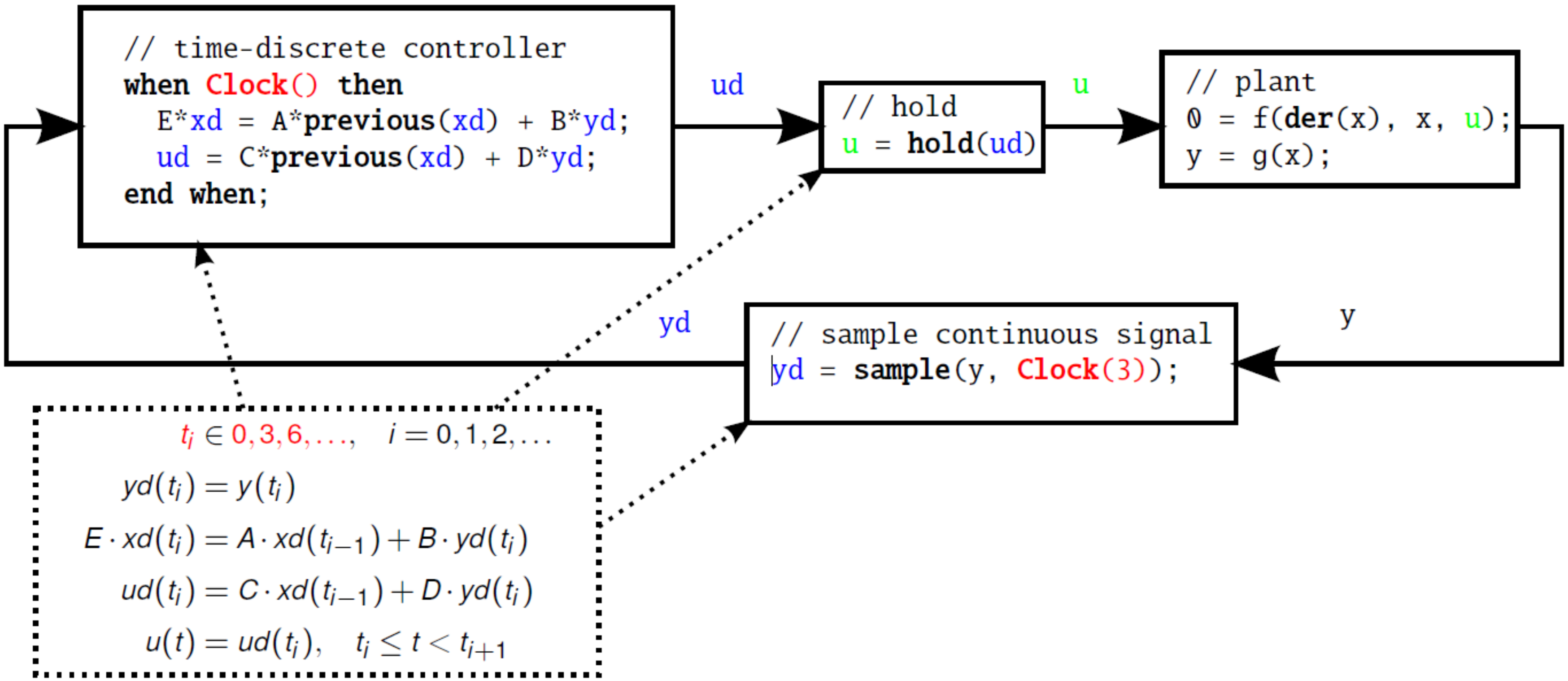
Controller with Sampled Data-Systems
(unclocked models, using pre() and sample())



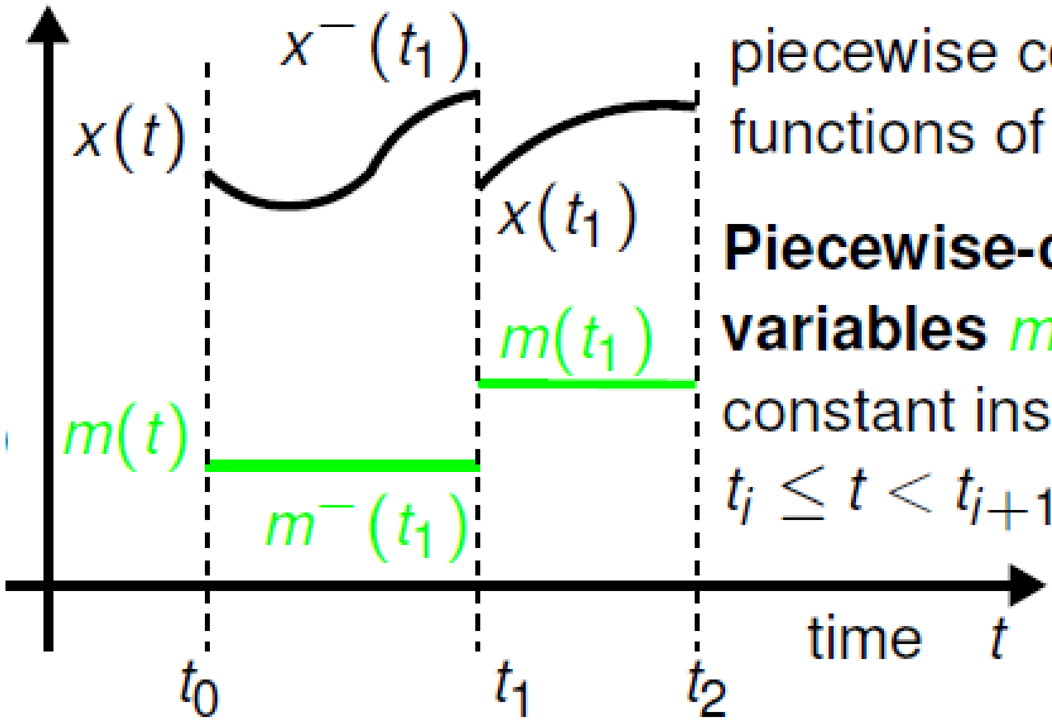
- y is automatically sampled at t = 3, 6, 9,…;
- xd, u are piecewise-constant variables that change values at sampling events (implicit zero-order hold)
- initial() triggers event at initialization (t=0)

Controller with Clocked Synchronous Constructs

clocked models using Clock(), previous(), hold() in Modelica 3.3



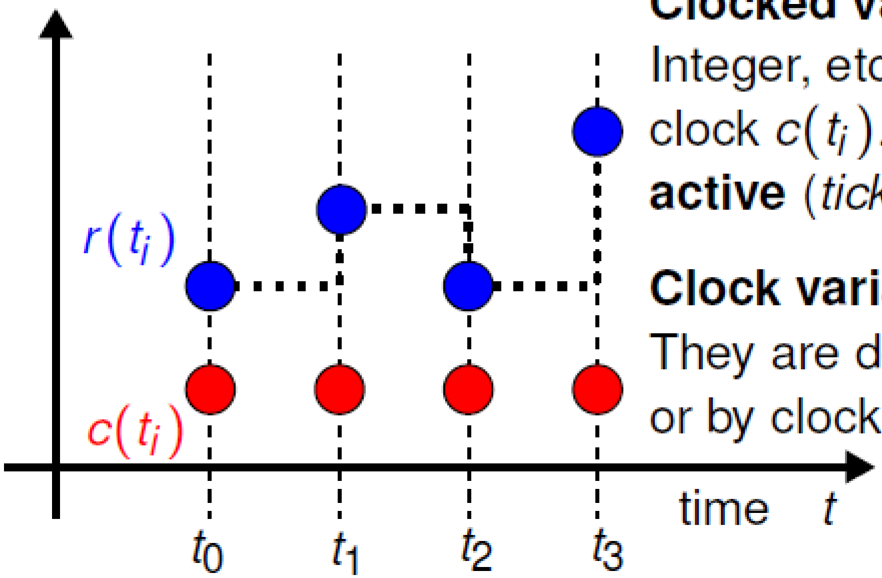
Unclocked Variables in Modelica 3.2



Continuous variables are Real numbers defined as piecewise continuous functions of time.

Piecewise-constant variables $m(t)$ are constant inside each $t_i \leq t < t_{i+1}$.

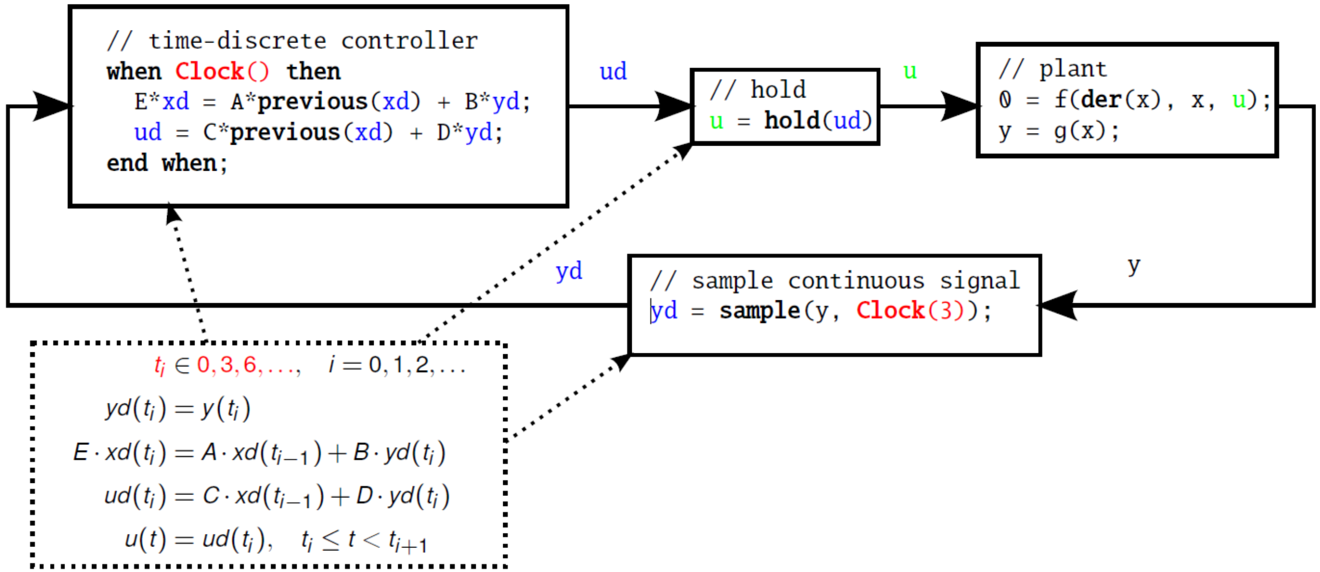
Clock variables (Clock) and Clocked Variables (Real)
(in Modelica 3.3)

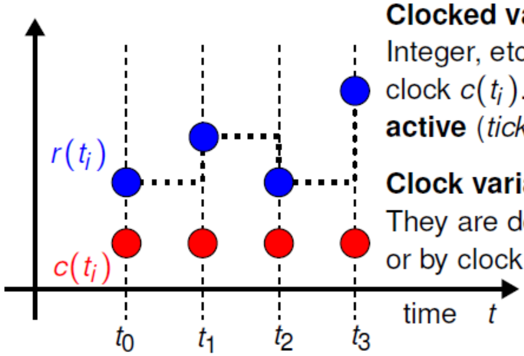


Clocked variables $r(t_i)$ are of base type Real, Integer, etc. They are uniquely associated with a clock $c(t_i)$. Can only be accessed when its clock is **active** (*ticks*).

Clock variables $c(t_i)$ are of base type **`Clock`**. They are defined by constructors such as **`Clock`**`(3)` or by clock operators relatively to other clocks.

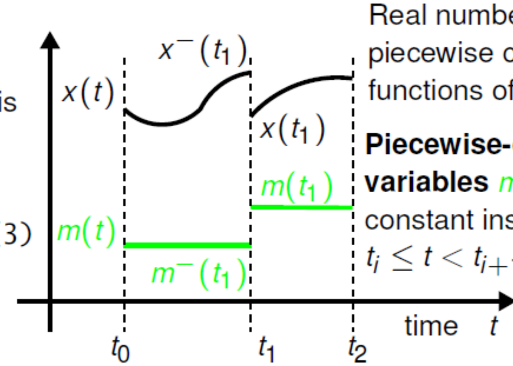
Clocked Synchronous Extension in Modelica 3.3





Clocked variables $r(t_i)$ are of base type Real, Integer, etc. They are uniquely associated with a clock $c(t_i)$. Can only be accessed when its clock is **active** (*ticks*).

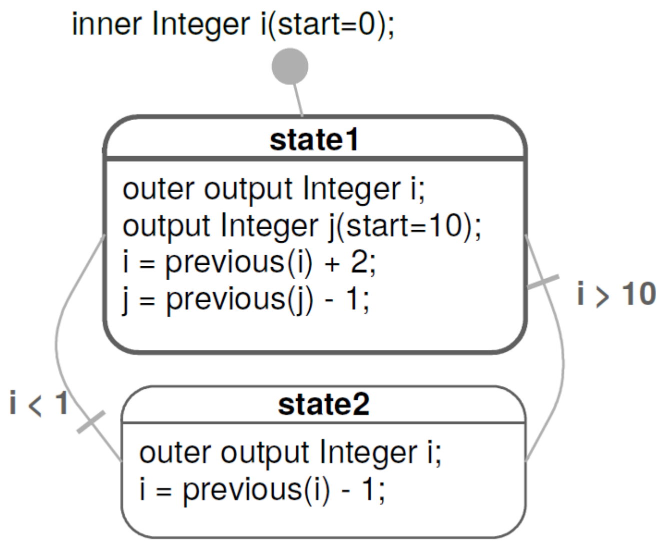
Clock variables $c(t_i)$ are of base type `Clock`. They are defined by constructors such as `Clock(3)` or by clock operators relatively to other clocks.

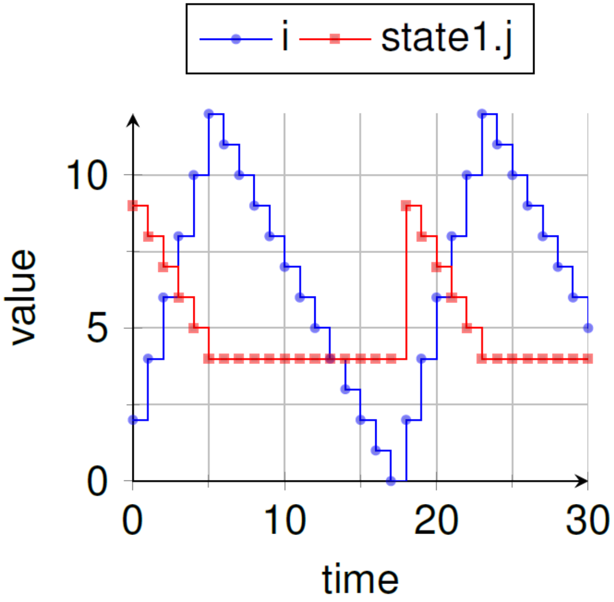


Continuous variables are Real numbers defined as piecewise continuous functions of time.

Piecewise-constant variables $m(t)$ are constant inside each $t_i \leq t < t_{i+1}$.

State Machines in Modelica 3.3: Simple Example



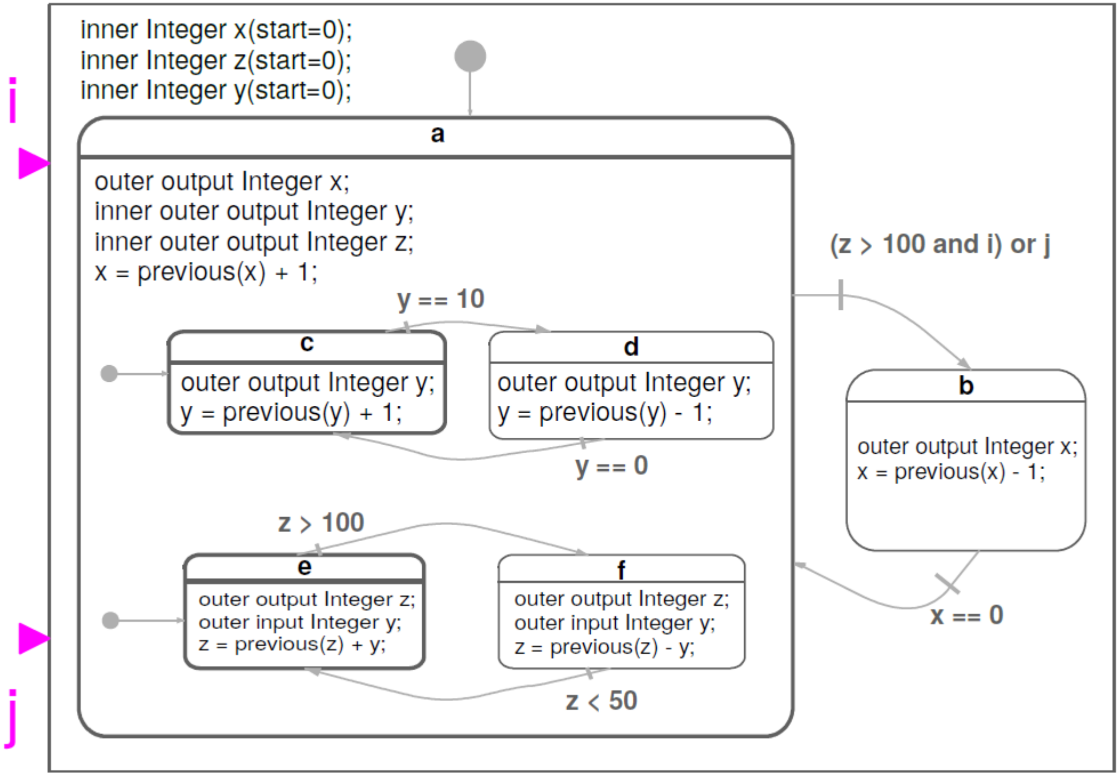


- Equations are active if corresponding *clock* ticks. Defaults to periodic clock with 1.0 s sampling period
- "i" is a shared variable, "j" is a local variable. Transitions are "*delayed*" and enter states by "*reset*"

Simple Example: Modelica Code

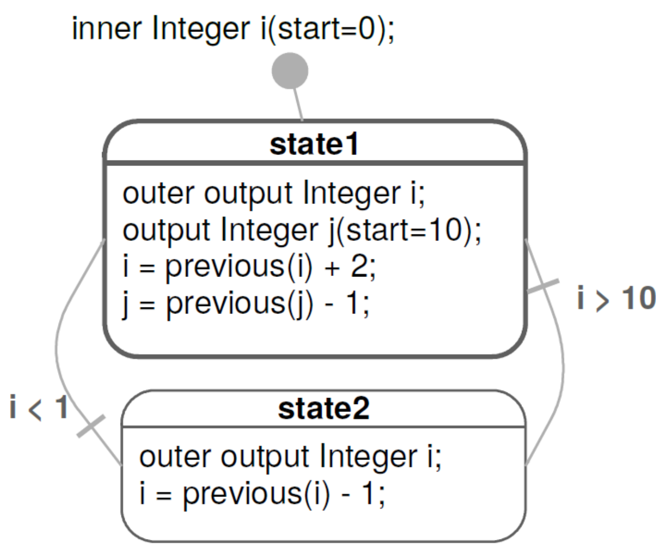
```
model Simple_NoAnnotations "Simple state machine"
  inner Integer i(start=0);
  block State1
    outer output Integer i;
    output Integer j(start=10);
  equation
    i =  previous(i) + 2;
    j =  previous(j) - 1;
  end State1;
  State1 state1;
  block State2
    outer output Integer i;
  equation
    i =  previous(i) - 1;
  end State2;
  State2 state2;
equation
  transition(state1,state2,i > 10,immediate=false);
  transition(state2,state1,i < 1,immediate=false);
  initialState(state1);
end Simple_NoAnnotations;
```

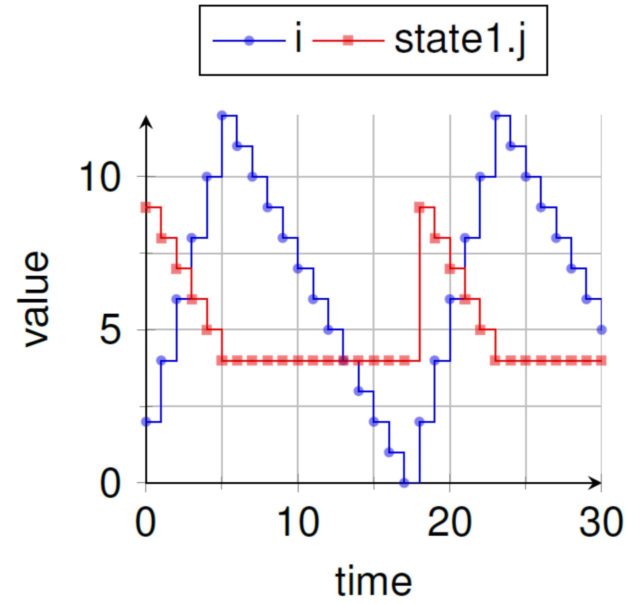

Hierarchical and Parallel Composition of Modelica State Machine Models



Semantics of Modelica state machines (and example above) inspired by Florence Maraninchi & Yann Rémond's "Mode-Automata" and by Marc Pouzet's Lucid Synchrone 3.0.

State Machines in Modelica 3.3: Simple Example





- Equations are active if corresponding *clock* ticks. Defaults to periodic clock with 1.0 s sampling period
- “i” is a shared variable, “j” is a local variable. Transitions are “*delayed*” and enter states by “*reset*”

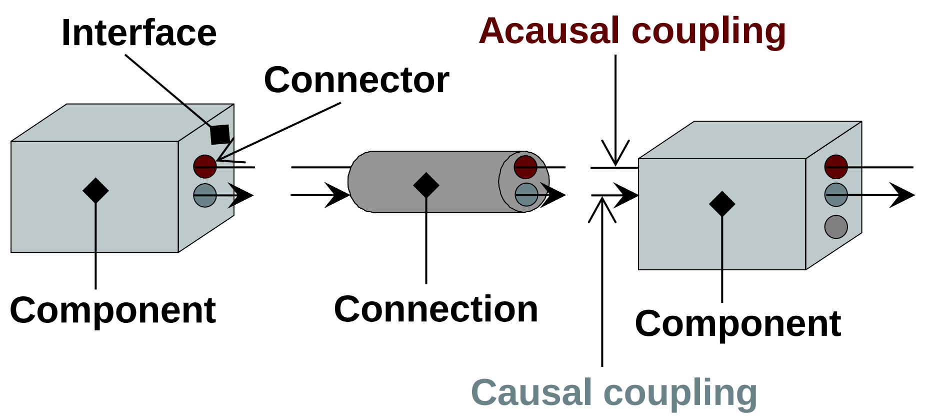
Simple Example: Modelica Code

```
model Simple_NoAnnotations "Simple state machine"
  inner Integer i(start=0);
  block State1
    outer output Integer i;
    output Integer j(start=10);
  equation
    i =  previous(i) + 2;
    j =  previous(j) - 1;
  end State1;
  State1 state1;
  block State2
    outer output Integer i;
  equation
    i =  previous(i) - 1;
  end State2;
  State2 state2;
equation
  transition(state1,state2,i > 10,immediate=false);
  transition(state2,state1,i < 1,immediate=false);
  initialState(state1);
end Simple_NoAnnotations;
```


Part IV

Components, Connectors and Connections – Modelica Libraries and Graphical Modeling

Software Component Model



A component class should be defined *independently of the environment,* very essential for *reusability*

A component may internally consist of other components, i.e. *hierarchical* modeling

Complex systems usually consist of large numbers of *connected* components

Connectors and Connector Classes

Connectors are instances of *connector classes*

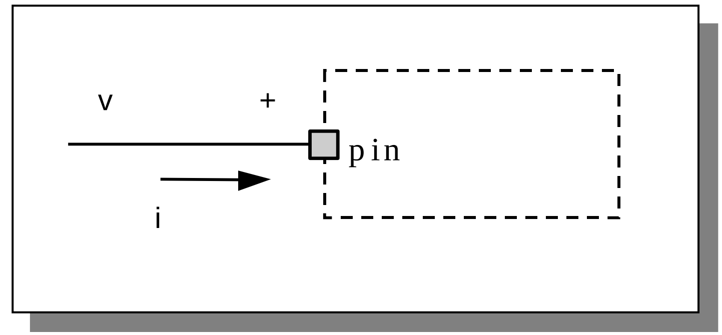
electrical connector

connector class

keyword `flow` indicates that currents of connected pins sum to zero.

an instance `pin` of class `Pin`

```
connector Pin
  Voltage      v;
  flow Current i;
end Pin;

Pin pin;
```

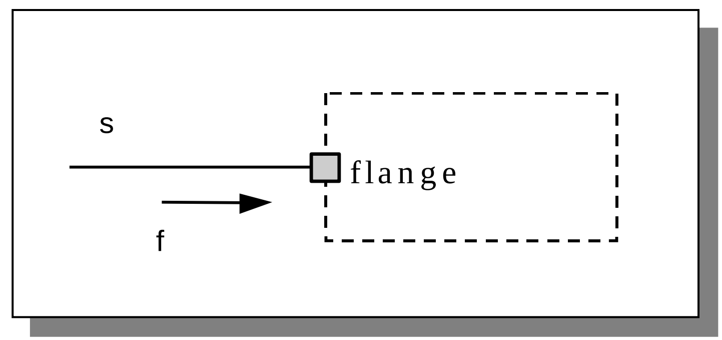


mechanical connector

connector class

an instance `flange` of class `Flange`

```
connector Flange
  Position    s;
  flow Force  f;
end Flange;

Flange flange;
```



The `flow` prefix

Three possible kinds of variables in connectors:

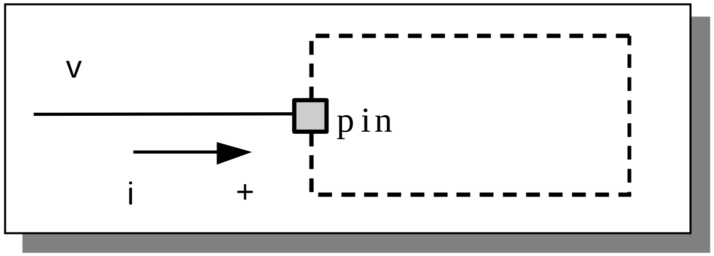
- *Potential variables potential* or energy level
- *Flow variables* represent some kind of flow
- *Stream variables* represent fluid flow in convective transport

Coupling

- *Equality coupling*, for potential variables
- *Sum-to-zero coupling*, for `flow` variables

The value of a `flow` variable is *positive* when the current or the flow is *into* the component

positive flow direction:



Physical Connector

- Classes Based on Energy Flow

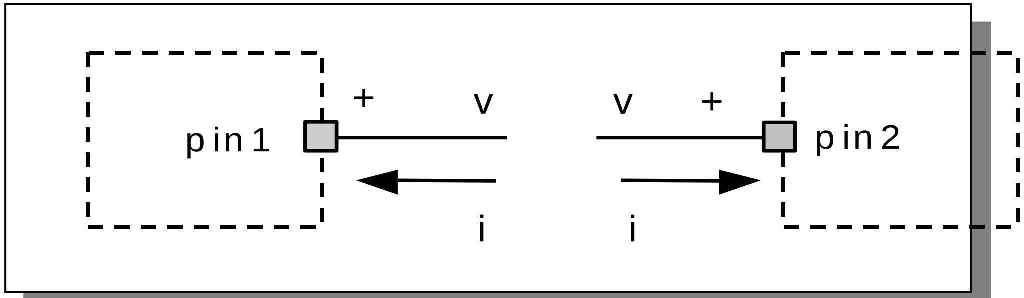
Domain Type	Potential	Flow	Carrier	Modelica Library
Electrical	Voltage	Current	Charge	`Electrical.Analog`
Translational	Position	Force	Linear momentum	`Mechanical.Translational`
Rotational	Angle	Torque	Angular momentum	`Mechanical.Rotational`
Magnetic	Magnetic potential	Magnetic flux rate	Magnetic flux	
Hydraulic	Pressure	Volume flow	Volume	`HyLibLight`
Heat	Temperature	Heat flow	Heat	`HeatFlow1D`
Chemical	Chemical potential	Particle flow	Particles	Under construction
Pneumatic	Pressure	Mass flow	Air	`PneuLibLight`

connect-equations

Connections between connectors are realized as *equations* in Modelica

```
connect(connector1,connector2)
```

The two arguments of a `connect`-equation must be references to *connectors*, either to be declared directly *within* the *same class* or be *members* of one of the declared variables in that class




```
Pin pin1,pin2;
//A connect equation
//in Modelica:
connect(pin1,pin2);
```

Corresponds to

```
pin1.v = pin2.v;
pin1.i + pin2.i =0;
```


Connection Equations

```
Pin pin1,pin2;
//A connect equation
//in Modelica
connect(pin1,pin2);
```

Corresponds to

```
pin1.v = pin2.v;
pin1.i + pin2.i =0;
```

Multiple connections are possible:

```
connect(pin1,pin2); connect(pin1,pin3); ... connect(pin1,pinN);
```

Each primitive connection set of potential variables is used to generate equations of the form:

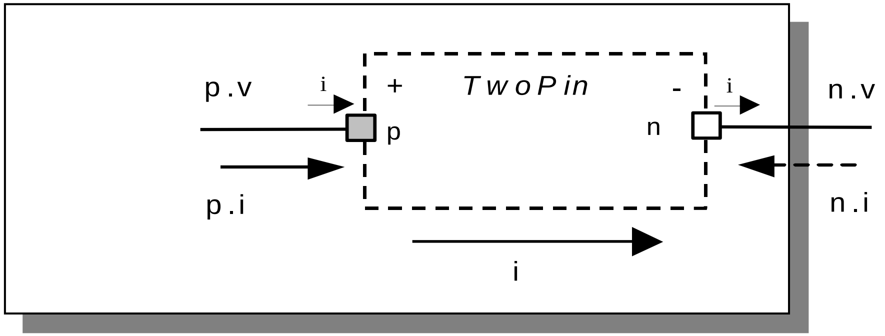
$$v_1 = v_2 = v_3 = \cdots v_n$$

Each primitive connection set of flow variables is used to generate *sum-to-zero* equations of the form:

$$i_1 + i_2 + \cdots (-i_k) + \cdots i_n = 0$$

Common Component Structure

The base class `TwoPin` has two connectors `p` and `n` for positive and negative pins respectively



partial class (cannot be instantiated)

positive pin

negative pin

```
partial model TwoPin
  Voltage     v
  Current     i
  Pin p;
  Pin n;
equation
  v = p.v - n.v;
  0 = p.i + n.i;
  i = p.i;
end TwoPin;
// TwoPin is same as OnePort in
// Modelica.Electrical.Analog.Interfaces
```

```
connector Pin
  Voltage       v;
  flow Current  i;
end Pin;
```

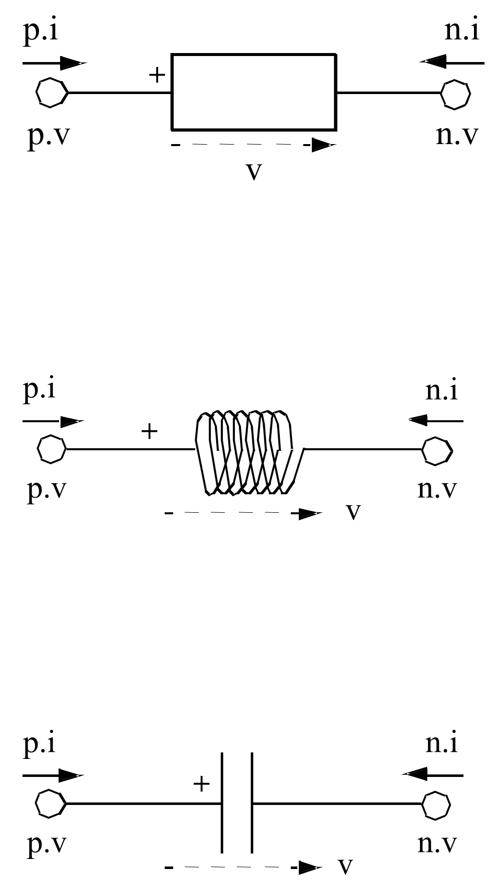
electrical connector class

Electrical Components

```
model Resistor "Ideal electrical resistor"
  extends TwoPin;
  parameter Real R;
equation
  R*i = v;
end Resistor;
```

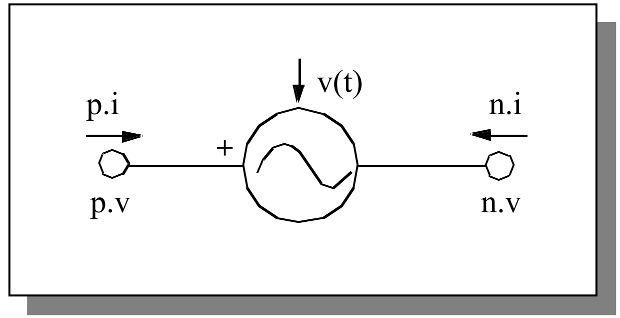
```
model Inductor "Ideal electrical inductor"
  extends TwoPin;
  parameter Real L "Inductance";
equation
  L*der(i) = v;
end Inductor;
```

```
model Capacitor "Ideal electrical capacitor"
  extends TwoPin;
  parameter Real C ;
equation
  i=C*der(v);
end Capacitor;
```

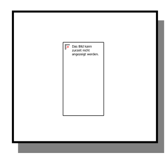


Electrical Components cont'

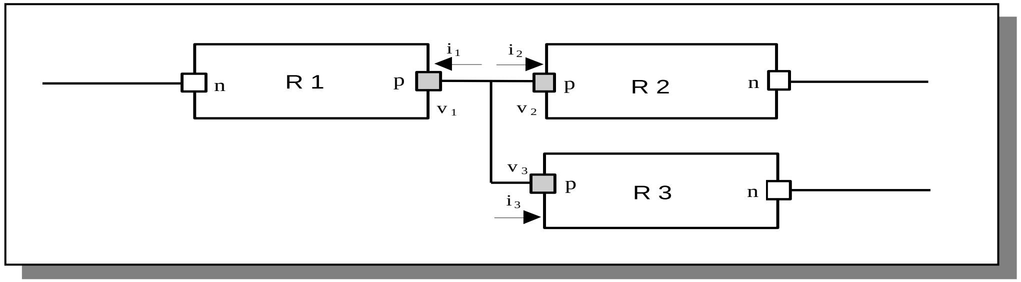
```
model Source
    extends TwoPin;
    parameter Real A,w;
equation
    v = A*sin(w*time);
end Resistor;
```




```
model Ground
    Pin p;
equation
    p.v = 0;
end Ground;
```



Resistor Circuit




```
model ResistorCircuit
  Resistor R1(R=100);
  Resistor R2(R=200);
  Resistor R3(R=300);
equation
  connect(R1.p, R2.p);
  connect(R1.p, R3.p);
end ResistorCircuit;
```

Corresponds to

```
R1.p.v = R2.p.v;
R1.p.v = R3.p.v;
R1.p.i + R2.p.i + R3.p.i = 0;
```


Modelica Standard Library - Graphical Modeling

- *Modelica Standard Library* (called Modelica) is a standardized predefined package developed by Modelica Association

- It can be used freely for both commercial and noncommercial purposes under the conditions of *The Modelica License*.

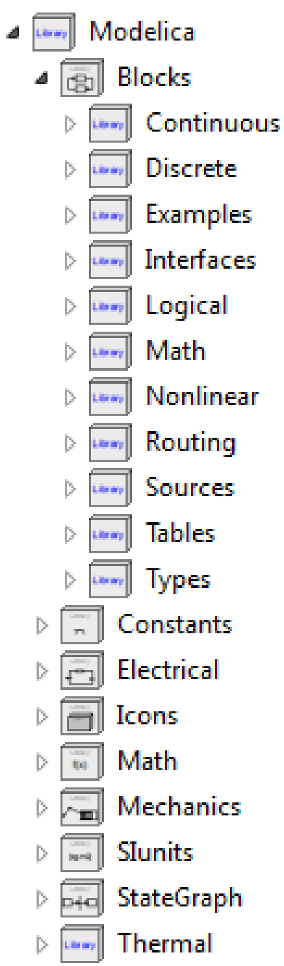
- Modelica libraries are available online including documentation and source code from http://www.modelica.org/library/library.html

Modelica Standard Library cont'

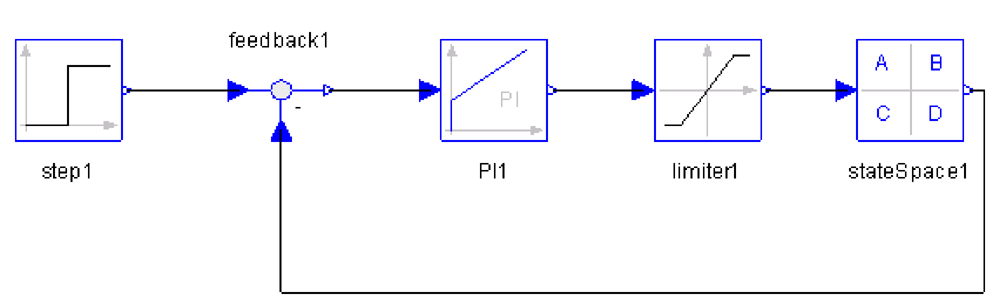
The Modelica Standard Library contains components from various application areas, including the following sublibraries:

- Blocks — Library for basic input/output control blocks
- Constants — Mathematical constants and constants of nature
- Electrical — Library for electrical models
- Icons — Icon definitions
- Fluid — 1-dim Flow in networks of vessels, pipes, fluid machines, valves, etc.
- Math — Mathematical functions
- Magnetic — Magnetic.Fluxtubes – for magnetic applications
- Mechanics — Library for mechanical systems
- Media — Media models for liquids and gases
- SIunits — Type definitions based on SI units according to ISO 31-1992
- Stategraph — Hierarchical state machines (analogous to Statecharts)
- Thermal — Components for thermal systems
- Utilities — Utility functions especially for scripting

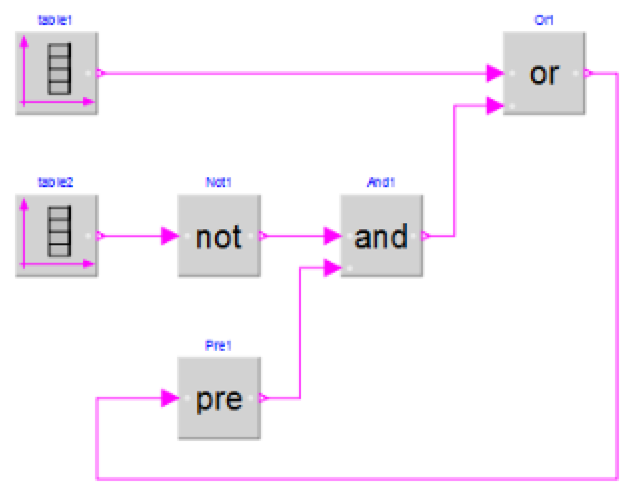
Modelica.Blocks



Continuous, discrete, and logical input/output blocks to build block diagrams.

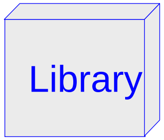


Examples:

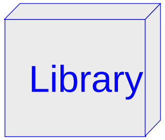


Modelica.Electrical

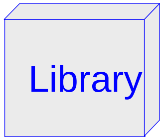
Electrical components for building analog, digital, and multiphase circuits



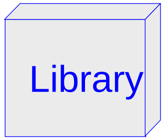
Analog



Digital

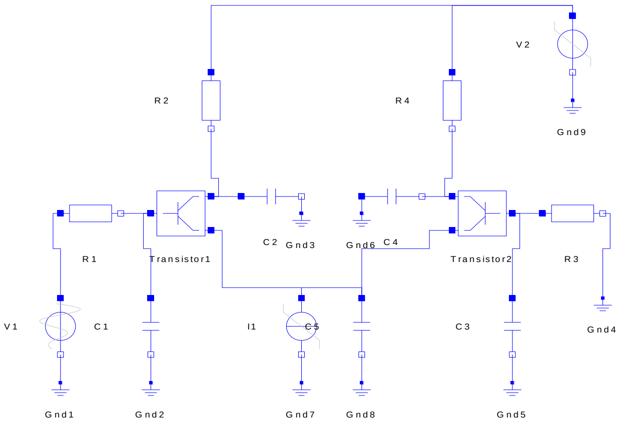


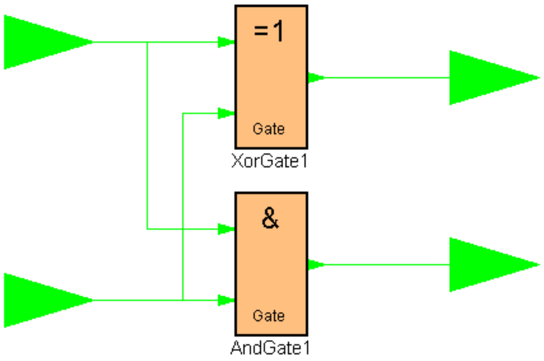
Machines

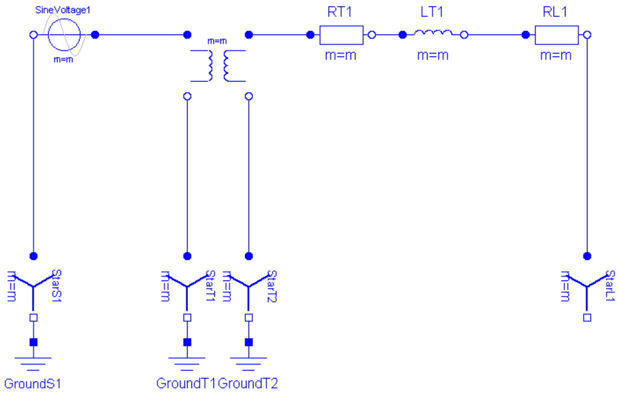


MultiPhase

Examples:





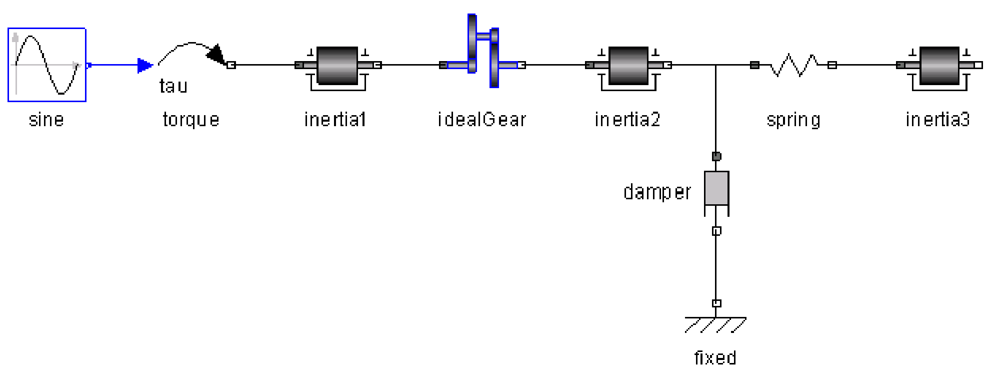


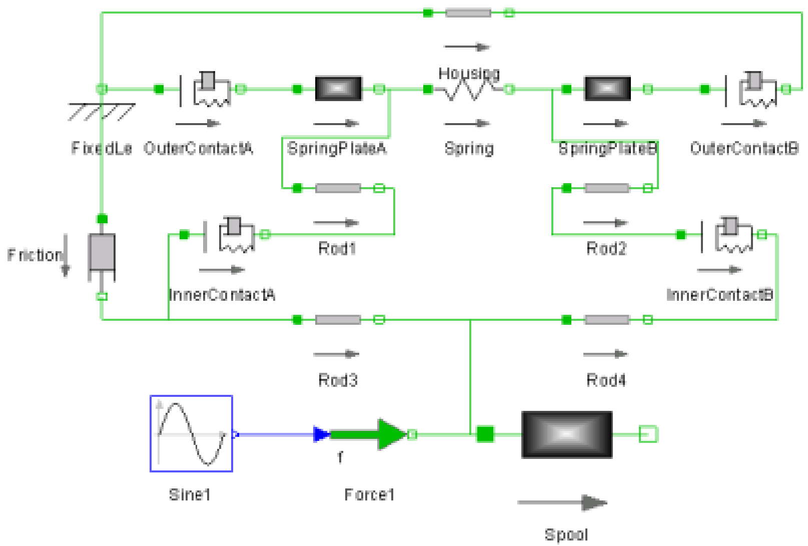
Modelica.Mechanics

Package containing components for mechanical systems

Subpackages:

- Rotational 1-dimensional rotational mechanical components
- Translational 1-dimensional translational mechanical components
- MultiBody 3-dimensional mechanical components





Other Free Libraries

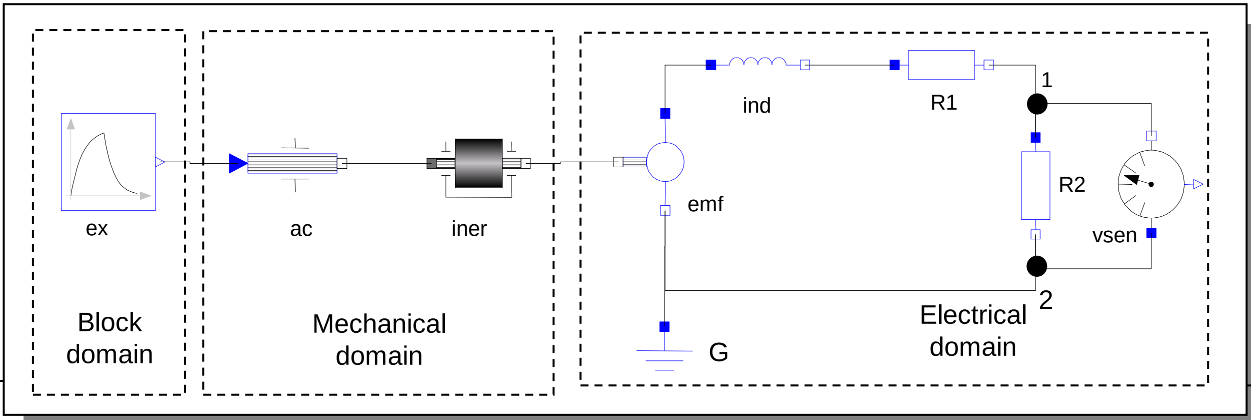
• WasteWater	Wastewater treatment plants, 2003
• ATPlus	Building simulation and control (fuzzy control included), 2005
• MotorCycleDymanics	Dynamics and control of motorcycles, 2009
• NeuralNetwork	Neural network mathematical models, 2006
• VehicleDynamics	Dynamics of vehicle chassis (obsolete), 2003
• SPICElib	Some capabilities of electric circuit simulator PSPICE, 2003
• SystemDynamics	System dynamics modeling a la J. Forrester, 2007
• BondLib	Bond graph modeling of physical systems, 2007
• MultiBondLib	Multi bond graph modeling of physical systems, 2007
• ModelicaDEVS	DEVS discrete event modeling, 2006
• ExtendedPetriNets	Petri net modeling, 2002
• External.Media Library	External fluid property computation, 2008
• VirtualLabBuilder	Implementation of virtual labs, 2007
• SPOT	Power systems in transient and steady-state mode, 2007
• ...	

Some Commercial Libraries

- Powertrain
- SmartElectricDrives
- VehicleDynamics
- AirConditioning
- HyLib
- PneuLib
- CombiPlant
- HydroPlant
- …

Connecting Components from Multiple Domains

- **Block domain**
- **Mechanical domain**
- **Electrical domain**

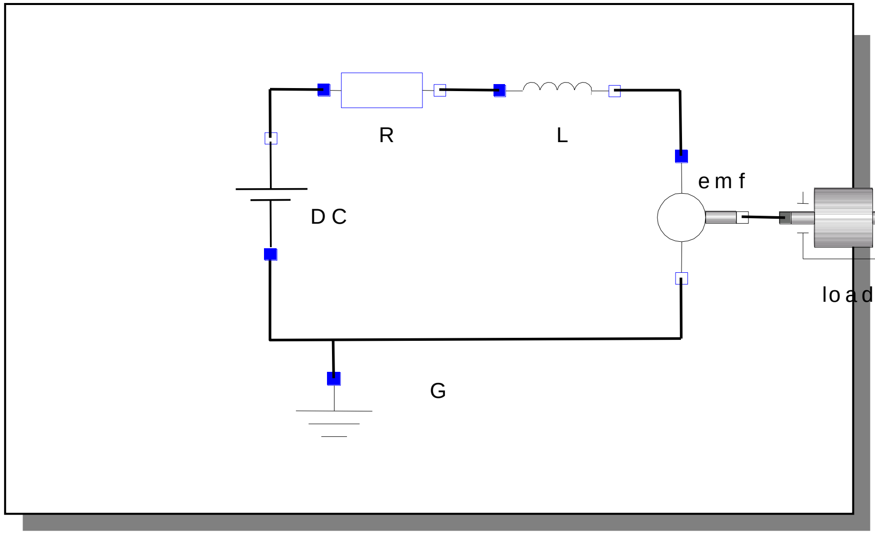



```
model Generator
  Modelica.Mechanics.Rotational.Accelerate ac;
  Modelica.Mechanics.Rotational.Inertia iner;
  Modelica.Electrical.Analog.Basic.EMF emf(k=-1);
  Modelica.Electrical.Analog.Basic.Inductor ind(L=0.1);
  Modelica.Electrical.Analog.Basic.Resistor R1,R2;
  Modelica.Electrical.Analog.Basic.Ground G;
  Modelica.Electrical.Analog.Sensors.VoltageSensor vsens;
  Modelica.Blocks.Sources.Exponentials ex(riseTime={2},riseTimeConst={1});
equation
  connect(ac.flange_b, iner.flange_a); connect(iner.flange_b, emf.flange_b);
  connect(emf.p, ind.p); connect(ind.n, R1.p); connect(emf.n, G.p);
  connect(emf.n, R2.n); connect(R1.n, R2.p); connect(R2.p, vsens.n);
  connect(R2.n, vsens.p); connect(ex.outPort, ac.inPort);
end Generator;
```

DCMotor Model Multi-Domain (Electro-Mechanical)

A DC motor can be thought of as an electrical circuit which also contains an electromechanical component.

```
model DCMotor
   Resistor R(R=100);
   Inductor L(L=100);
   VsourceDC DC(f=10);
   Ground G;
   EMF emf(k=10,J=10, b=2);
   Inertia load;
equation
   connect(DC.p,R.n);
   connect(R.p,L.n);
   connect(L.p, emf.n);
   connect(emf.p, DC.n);
   connect(DC.n,G.p);
   connect(emf.flange,load.flange);
end DCMotor;
```

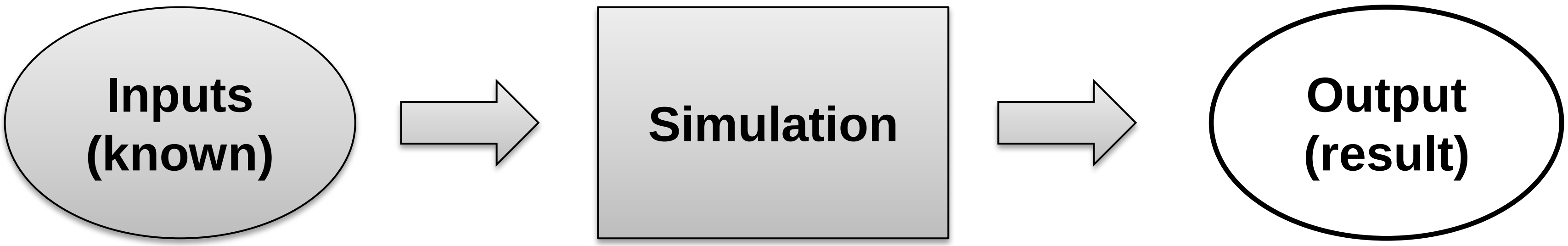


Part V
Dynamic Optimization Theory and Exercises

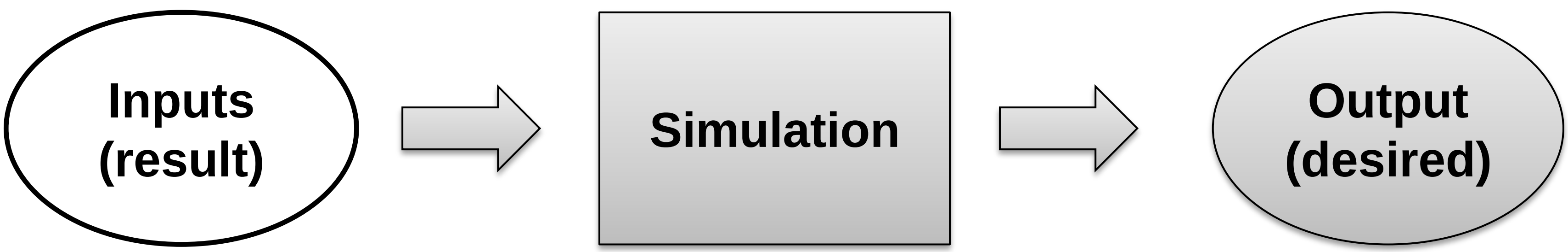
using OpenModelica

Built-in Dynamic Optimization - Motivation

Simulation



Optimization – Try to find the inputs that result in a desired output

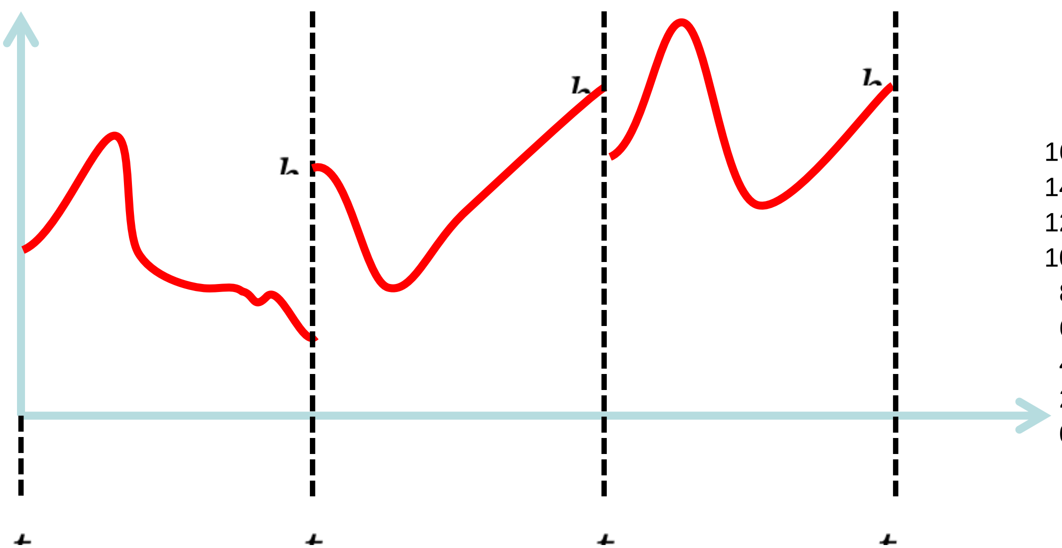


Optimization of Dynamic Trajectories Using Multiple-Shooting and Collocation

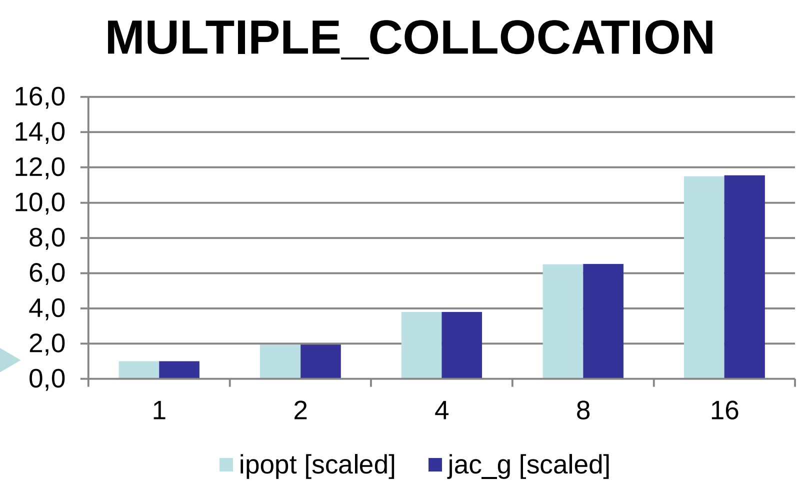
- Minimize a goal function subject to model equation constraints, useful e.g. for NMPC
- Multiple Shooting/Collocation
  - Solve sub-problem in each sub-interval

$$x_i(t_{i+1}) = h_i + \int_{t_i}^{t_{i+1}} f(x_i(t), u(t), t)\, dt \approx F(t_i, t_{i+1}, h_i, u_i), \qquad x_i\,(t_i) = h_i$$

This approach uses a single optimization run and is different from classical parameter sweep optimization typically using a large number of simulations



Example speedup, 16 cores:



Optimal Control Problem (OCP)

Cost function

$$\min_{u(t)} J(x(t),u(t),t) = \underbrace{E\left(x(t_f),u(t_f),t_f\right)}_{\text{Mayer-Term}} + \int_{t_0}^{t_f} \underbrace{L(x(t),u(t),t)}_{\text{Lagrange-Term}} \, dt \qquad (1)$$

Subject to

Initial conditions $$x(t_0) = x_0 \qquad (2)$$

Nonlinear dynamic model $$\dot{x} = f(x(t),u(t),t) \qquad (3)$$

Path constraints $$\hat{g}(x(t),u(t),t) \leq 0 \qquad (4)$$

Terminal constraints $$r\left(x(t_f)\right) = 0 \qquad (5)$$

where

$x(t) = [x^1(t), \dots, x^{n_x}]^T$ is the state vector and

$u(t) = [u^1(t), \dots, u^{n_u}(t)]^T$ is the control variable vector for

$t \in [t_0, t_f]$ respectively.

MODELICA

OCP Formulation in OpenModelica

The path constraints $\hat{g}(x(t), u(t), t) \leq 0$ can be split into box constraints

$$\begin{aligned} x_{\min} &\leq x(t) \leq x_{\max} \\ u_{\min} &\leq u(t) \leq u_{\max} \end{aligned}$$

Variable attributes `min` and `max` are reused for describing constraints, annotations are used for specifying the OCP

	Annotation
Mayer-Term	`Real costM annotation(isMayer=true);`
Lagrange-Term	`Real costL annotation(isLagrange=true);`
Constraints	`Real x(max=0) annotation(isConstraint=true);`
Final constraints	`Real y(min=0) annotation(isFinalConstraint=true);`

Predator-Prey Example – The Forest Model

Dynamic model of a forest with foxes x_f, rabbits x_r, fox hunters u_{hf} and rabbit hunters u_{hr} (adapted from Vitalij Ruge, “Native Optimization Features in OpenModelica”, part of the OpenModelica documentation)

$$\dot{x}_r = g_r \cdot x_r - d_{rf} \cdot x_r \cdot x_f - d_{rh} \cdot u_{hr}$$

$$\dot{x}_f = g_{fr} \cdot d_{\mathrm{rf}} \cdot x_r \cdot x_f - d_f \cdot x_f - d_{\mathrm{fh}} \cdot u_{hf}$$

IC: $x_r(t_0) = 700, \qquad x_f(t_0) = 10$

where

$g_r = 4 \cdot 10^{-2}$, Natural growth rate for rabbits

$g_{fr} = 1 \cdot 10^{-1}$, Efficiency in growing foxes from rabbits

$d_{rf} = 5 \cdot 10^{-3}$, Death rate of rabbits due to foxes

$d_{rh} = 5 \cdot 10^{-3}$, Death rate of rabbits due to hunters

$d_f = 9 \cdot 10^{-2}$, Natural death rate for foxes

$d_{fh} = 9 \cdot 10^{-2}$, Death rate of foxes due to hunters

Predator-Prey Example – Modelica model

```
model Forest "Predator-prey model"
  parameter Real g_r = 4e-2 "Natural growth rate for rabbits";
  parameter Real g_fr = 1e-1 "Efficiency in growing foxes from rabbits";
  parameter Real d_rf = 5e-3 "Death rate of rabbits due to foxes";
  parameter Real d_rh = 5e-2 "Death rate of rabbits due to hunters";
  parameter Real d_f = 9e-2 "Natural deathrate for foxes";
  parameter Real d_fh = 9e-2 "Death rate of foxes due to hunters";
  Real x_r(start=700,fixed=true) "Rabbits with start population of 700";
  Real x_f(start=10,fixed=true) "Foxes with start population of 10";
  input Real u_hr "Rabbit hunters";
  input Real u_hf "Fox hunters";
equation
  der(x_r) = g_r*x_r - d_rf*x_r*x_f - d_rh*u_hr;
  der(x_f) = g_fr*d_rf*x_r*x_f - d_f*x_f - d_fh*u_hf;
end Forest;
```

Control variables

Predator-Prey Example – Optimal Control Problem

Objective: Regulate the population in the forest to a desired level (5 foxes, 500 rabbits) at the end of the simulation ($t = t_f$)

$$J_{\text{Mayer}} = 0.1 \cdot \left(x_f(t_f) - 5\right)^2 + 0.01 \cdot \left(x_r(t_f) - 500\right)^2$$ (desired population at $t = t_f$)

Constraints: $u_{hf} \geq 0,\ u_{hf} \geq 0,\ x_r \geq 0,\ x_f \geq 0$

Modelica model:

Extension of the system model

constraint

Important for scaling, needs to be > 0 to make optimizer converge!

Cost function Mayer-term

```
model ForestOCP;
  extends Forest(
    u_hr(min=0, nominal=1e-4),u_hf(min=0, nominal=1e-4),
    x_r(min=0),x_f(min=0));
  Real J_Mayer =
    0.1*(x_r- 5)^2 + 0.01*(x_r - 500)^2 annotation(isMayer=true);
end ForestOCP;
```


Predator-Prey Example – Using OMNotebook

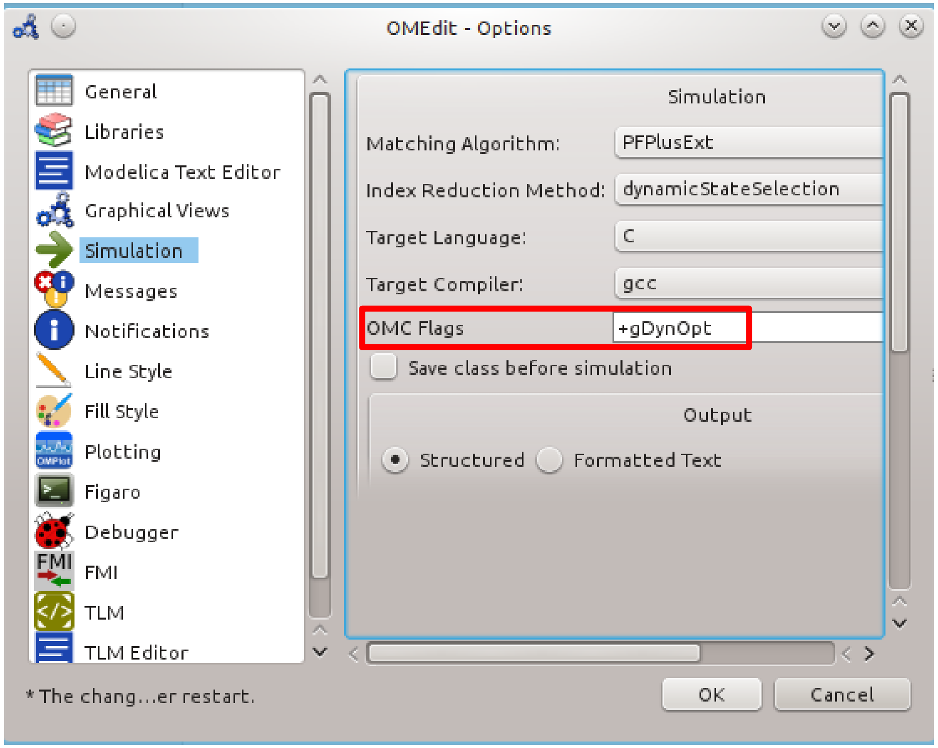
Start the optimization from OMNotebook using a time interval $[t_0, t_f] = [0{,}400]$seconds

```
setCommandLineOptions("+gDynOpt");
optimize(ForestOCP, stopTime=400, tolerance=1e-8, numberOfIntervals=50,
simflags="-s optimization");
```

Option	Example value	Description
numberOfIntervals	50	collocation intervals
startTime, stopTime	0, 400	time horizon in seconds
tolerance	1e-8	solver/optimizer tolerance
simflags	…	see documentation for details

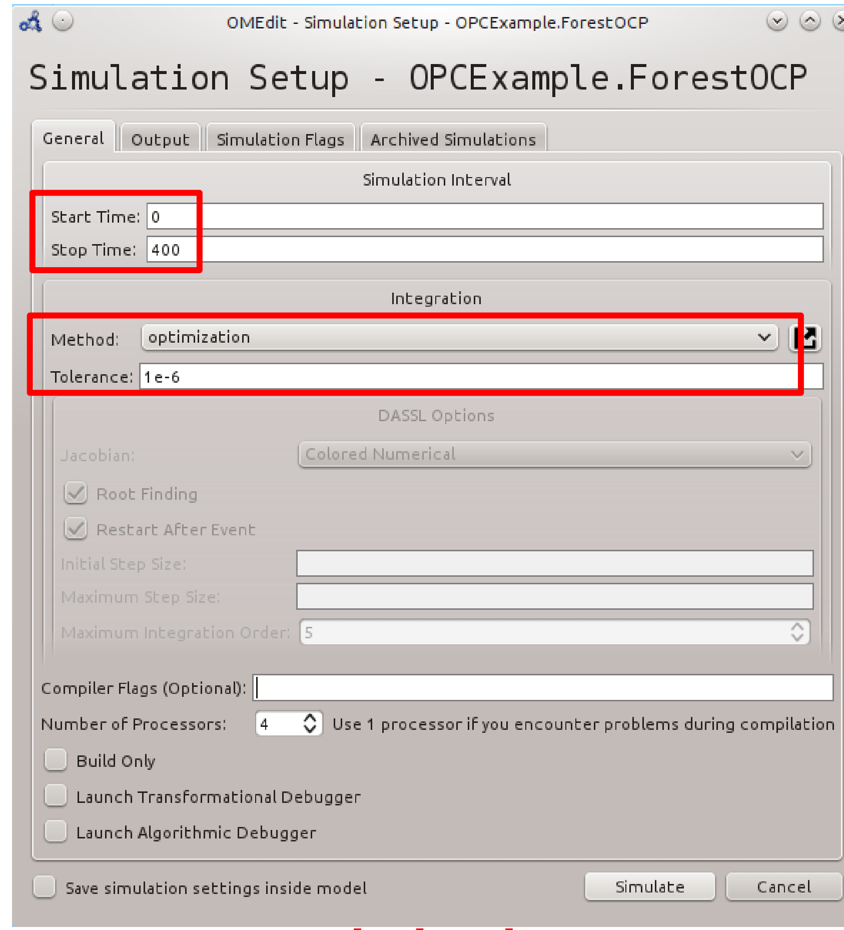
Predator-Prey Example – Using OMEdit

Tools→Options→Simulation



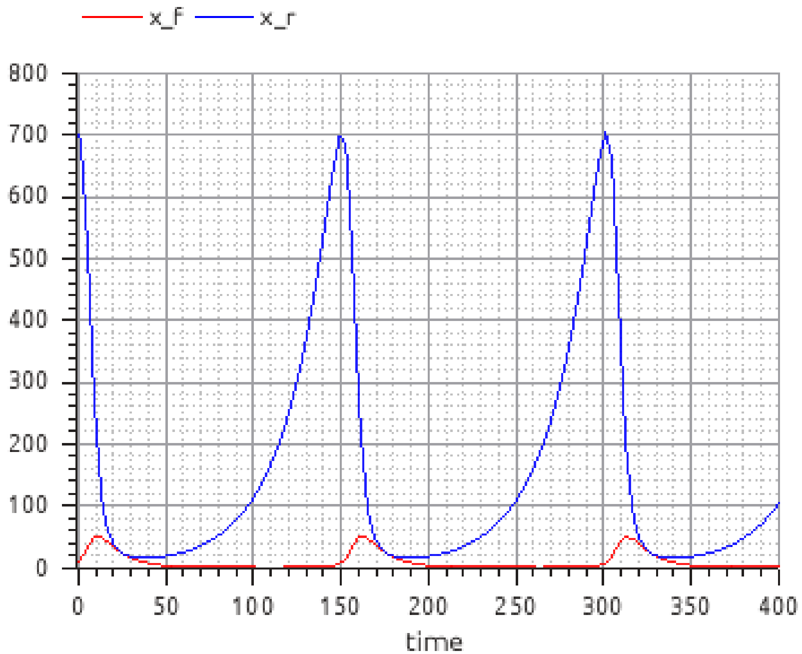
+gDynOpt

Simulation→Simulation Setup

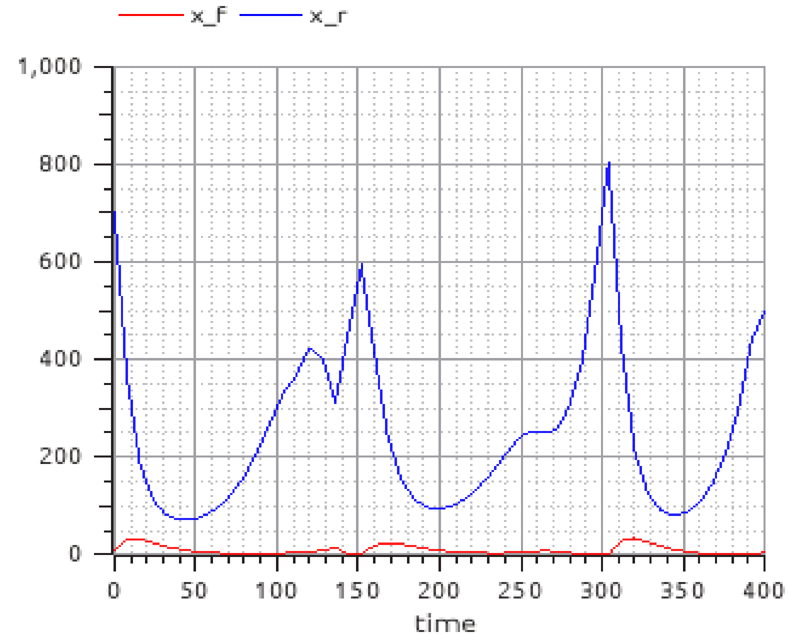


optimization

Predator-Prey Example – Plots



Simulation of the forest model with control variables $u_{hr} = u_{hf} = 0$



Simulation of the forest model using the control variables computed by the optimization. Notice (not well visible in the plot) that

$$x_r(t_f) = 500, x_f(t_f) = 5$$

Exercise – Optimal Control

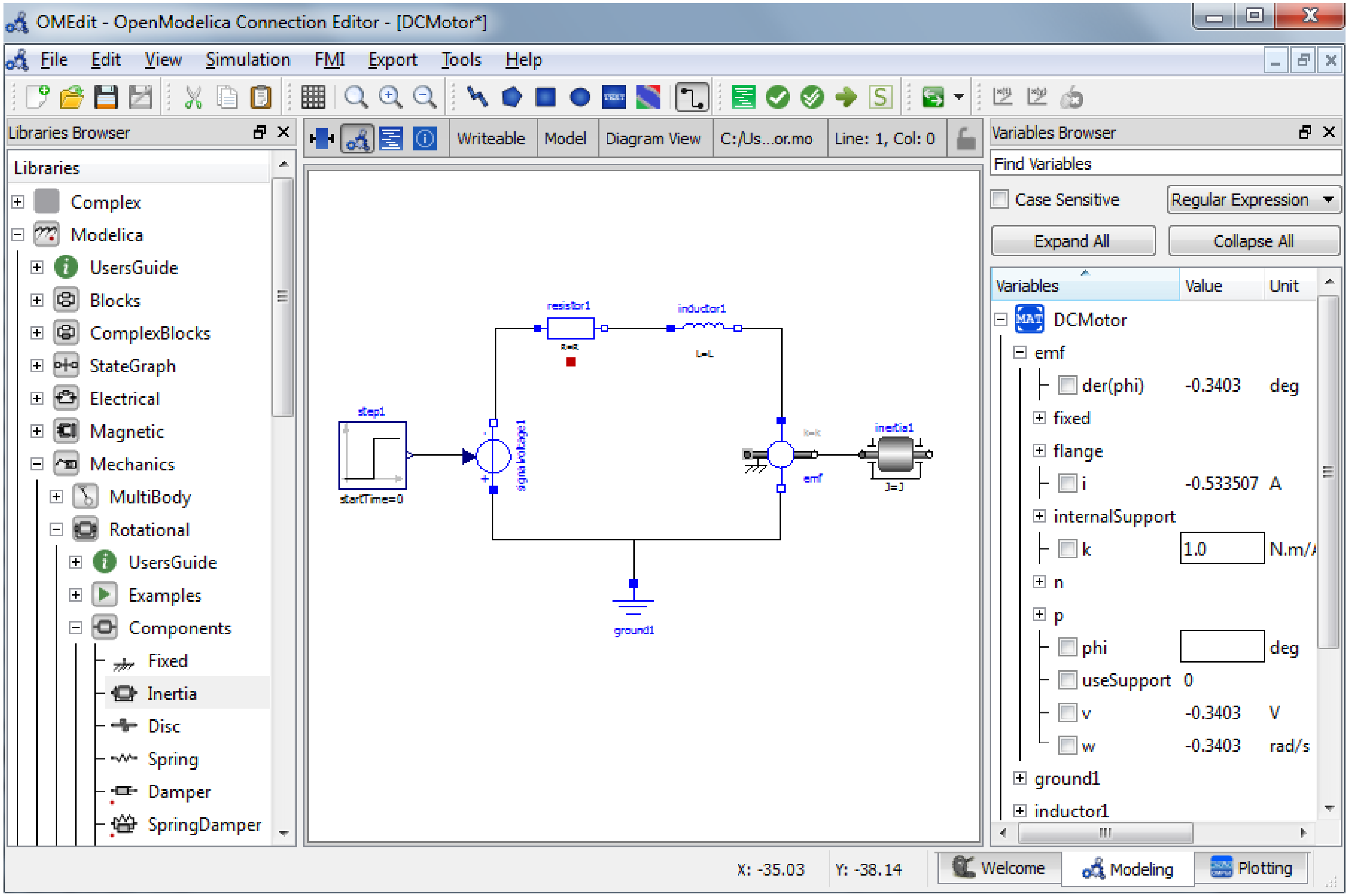
Load the `OPCExample.onb` ebook into OMNotebook and modify the optimization problem in the following ways:

1. Constrain the maximal number of rabbit hunters and fox hunters to five, respectively.
2. Change the Mayer-term of the cost function to a Lagrange-term.
3. Penalize the number of employed hunters by a suitable modification of the cost function and observe how the solution changes for different modifications.

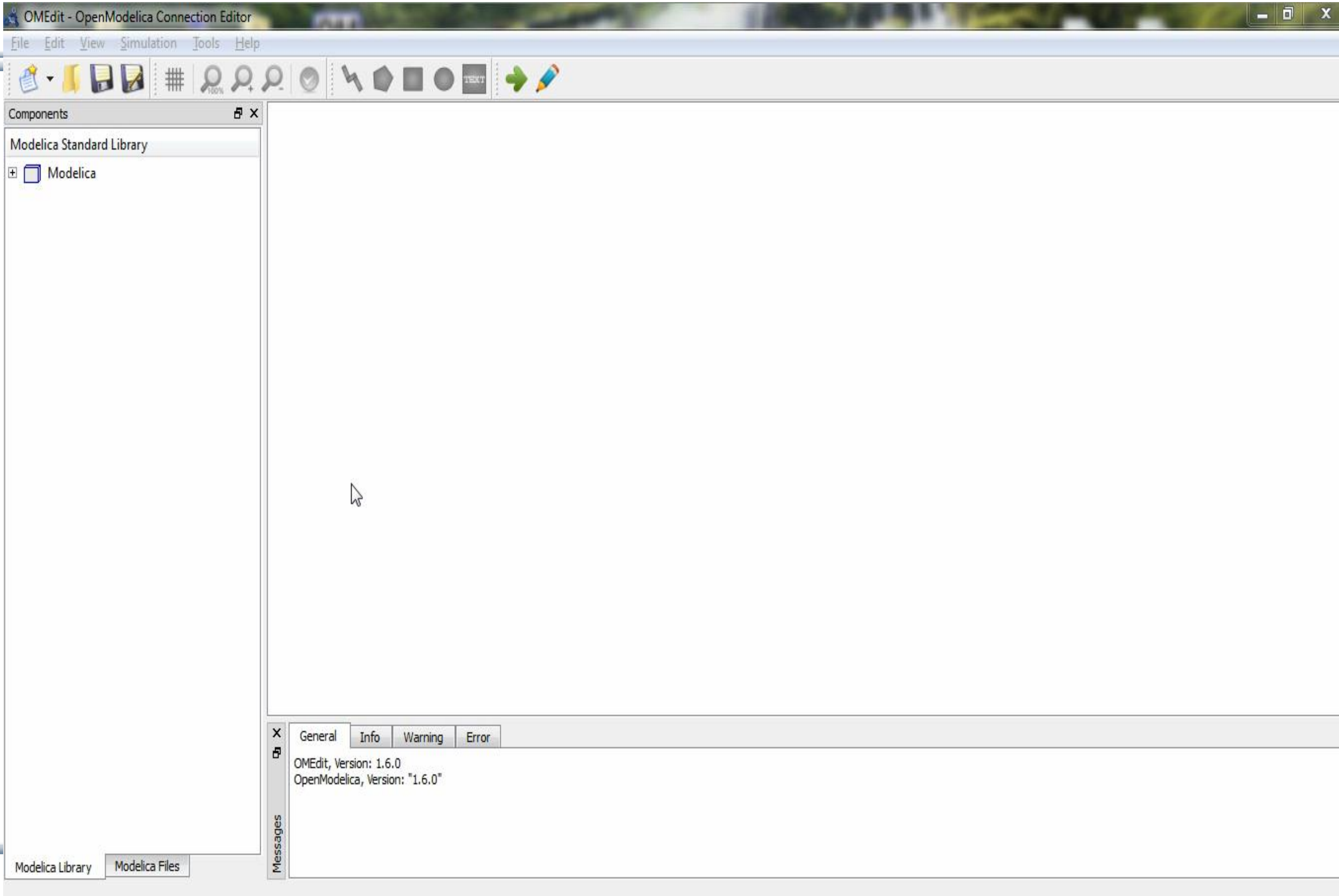
Part Vb
More
Graphical Modeling Exercises

using
OpenModelica

Graphical Modeling - Using Drag and Drop Composition



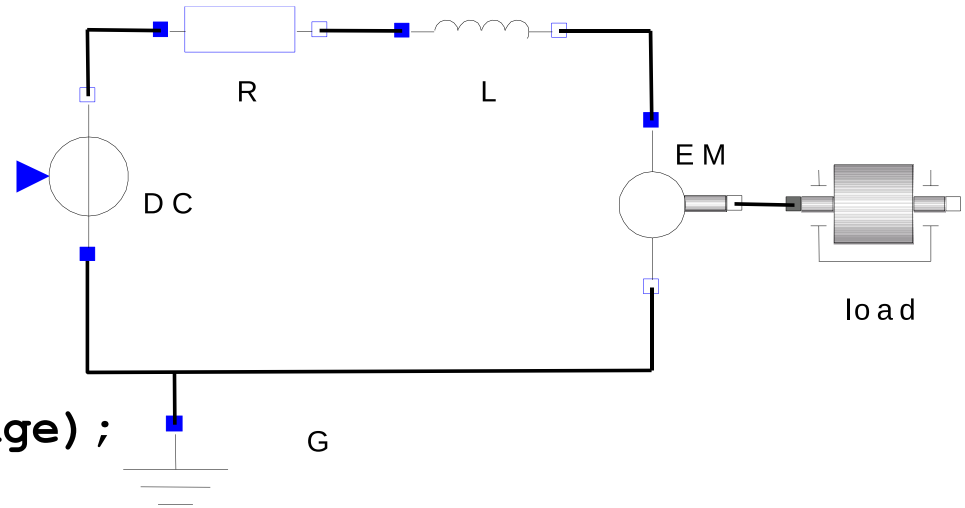
Graphical Modeling Animation – DCMotor



Multi-Domain (Electro-Mechanical) Modelica Model

- A DC motor can be thought of as an electrical circuit which also contains an electromechanical component

```
model DCMotor
   Resistor R(R=100);
   Inductor L(L=100);
   VsourceDC DC(f=10);
   Ground G;
   ElectroMechanicalElement EM(k=10,J=10, b=2);
   Inertia load;
equation
   connect(DC.p,R.n);
   connect(R.p,L.n);
   connect(L.p, EM.n);
   connect(EM.p, DC.n);
   connect(DC.n,G.p);
   connect(EM.flange,load.flange);
end DCMotor
```



Corresponding DCMotor Model Equations

The following equations are automatically derived from the Modelica model:

```
0 == DC.p.i + R.n.i          EM.u == EM.p.v - EM.n.v             R.u == R.p.v - R.n.v
DC.p.v == R.n.v              0 == EM.p.i + EM.n.i                0 == R.p.i + R.n.i
                             EM.i == EM.p.i                      R.i == R.p.i
0 == R.p.i + L.n.i           EM.u == EM.k * EM.ω                 R.u == R.R * R.i
R.p.v == L.n.v               EM.i == EM.M / EM.k
                             EM.J * EM.ω == EM.M - EM.b * EM.ω   L.u == L.p.v - L.n.v
0 == L.p.i + EM.n.i                                              0 == L.p.i + L.n.i
L.p.v == EM.n.v              DC.u == DC.p.v - DC.n.v             L.i == L.p.i
                             0 == DC.p.i + DC.n.i                L.u == L.L * L.i'
0 == EM.p.i + DC.n.i         DC.i == DC.p.i
EM.p.v == DC.n.v             DC.u == DC.Amp * Sin[2 π DC.f * t]

0 == DC.n.i + G.p.i
DC.n.v == G.p.v
```

(`load` component not included)

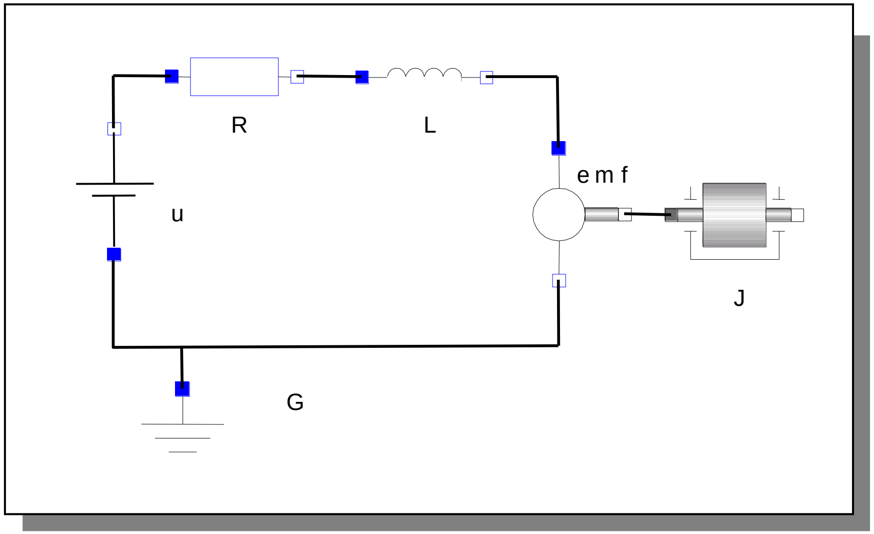
Automatic transformation to ODE or DAE for simulation:

$$\frac{dx}{dt} == f[x, u, t] \qquad g\left[\frac{dx}{dt}, x, u, t\right] == 0$$

Exercise 3.1

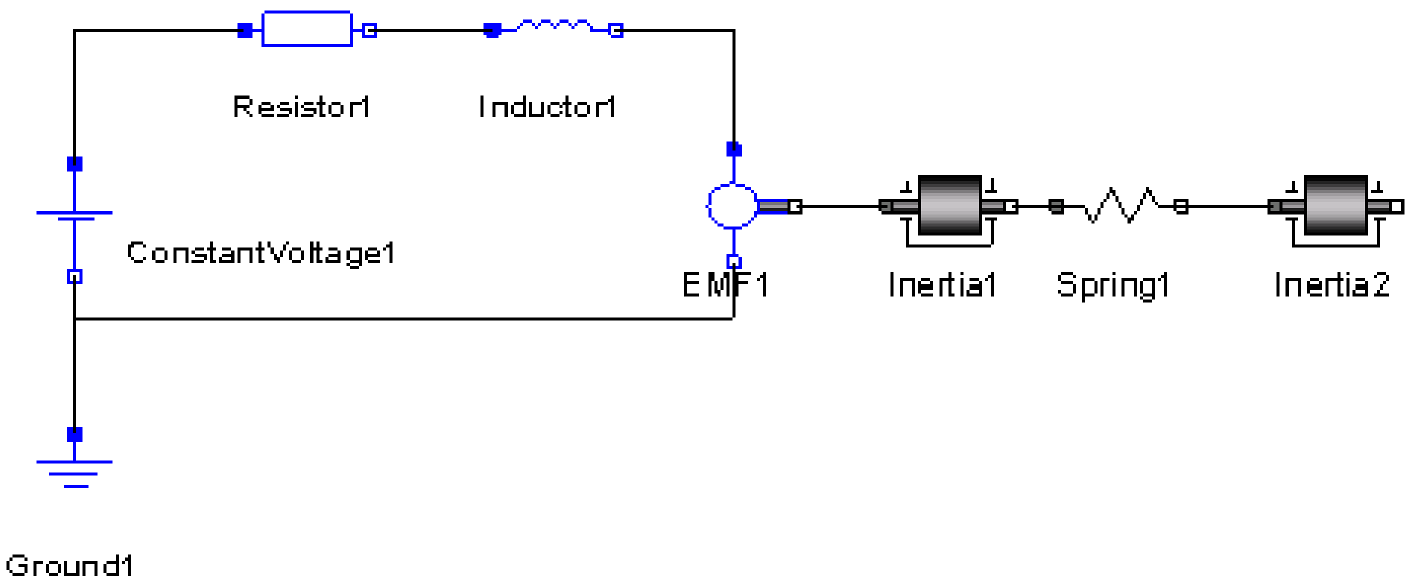
- Draw the `DCMotor` model using the graphic connection editor using models from the following Modelica libraries:
  `Mechanics.Rotational.Components`,
  `Electrical.Analog.Basic`,
  `Electrical.Analog.Sources`

- Simulate it for 15s and plot the variables for the outgoing rotational speed on the inertia axis and the voltage on the voltage source (denoted u in the figure) in the same plot.



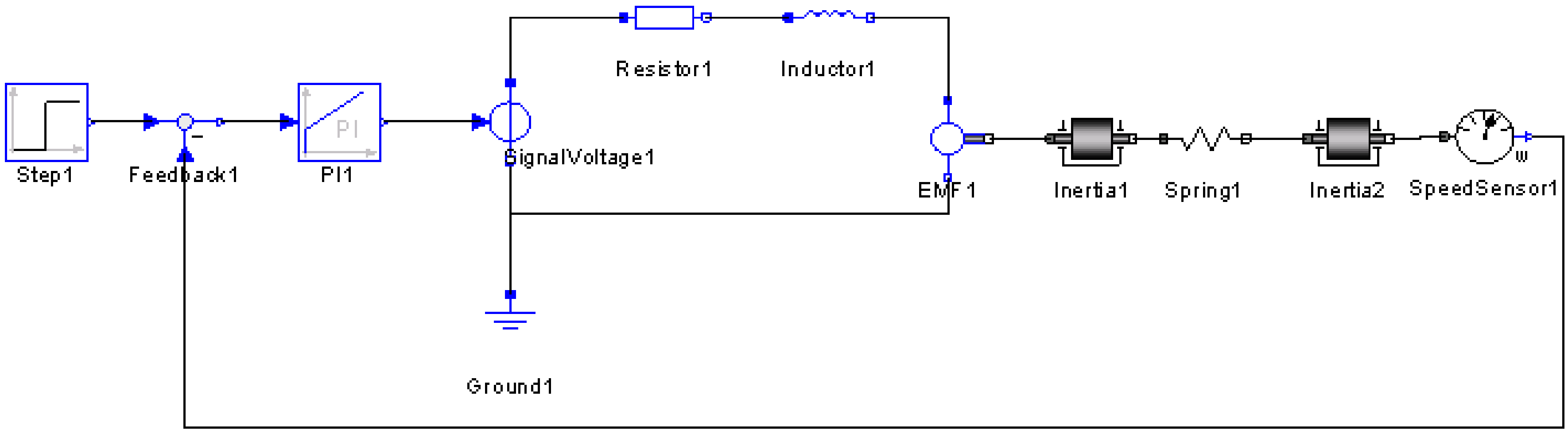
Exercise 3.2

- If there is enough time: Add a torsional spring to the outgoing shaft and another inertia element. Simulate again and see the results. Adjust some parameters to make a rather stiff spring.



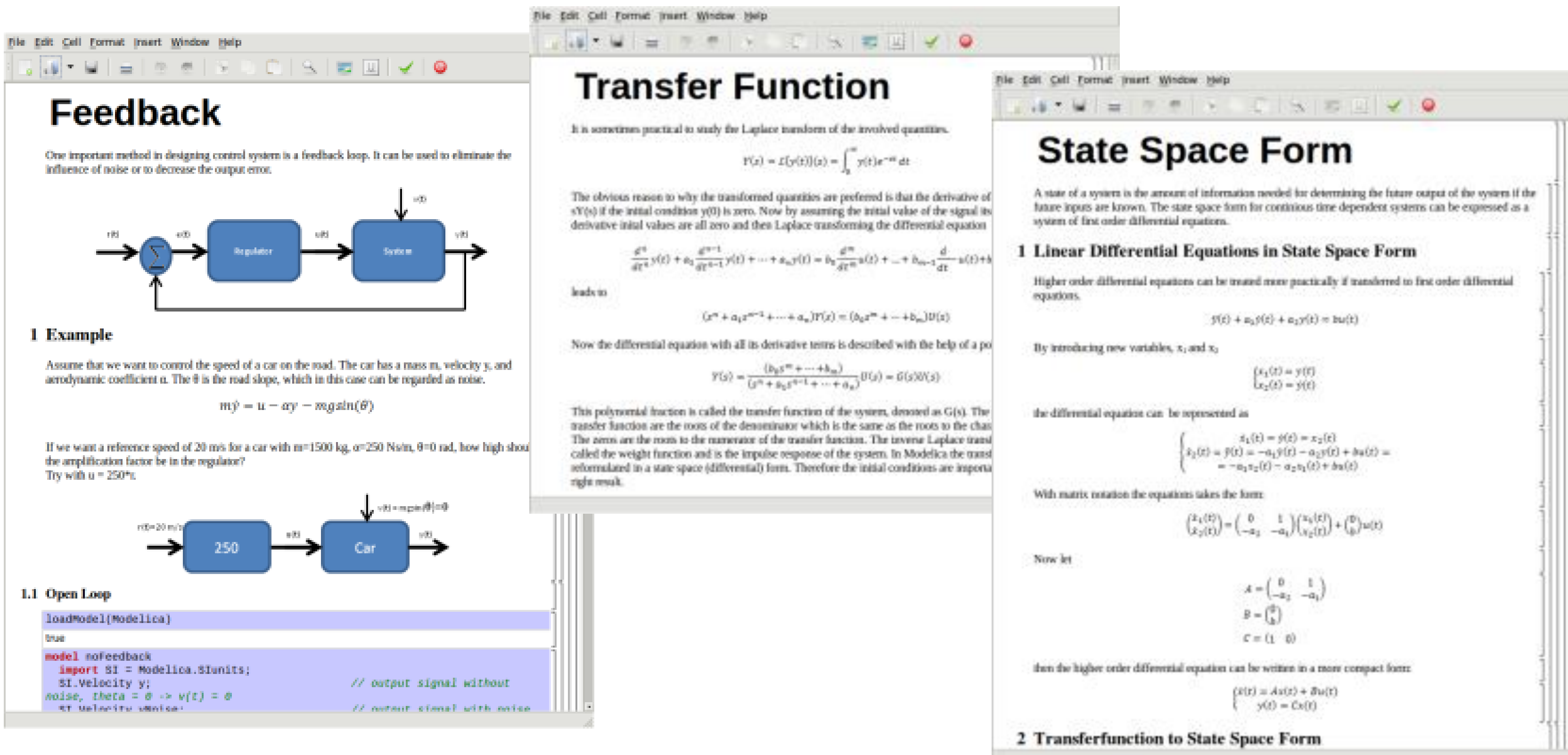
Exercise 3.3

- If there is enough time: Add a PI controller to the system and try to control the rotational speed of the outgoing shaft. Verify the result using a step signal for input. Tune the PI controller by changing its parameters in OMEdit.

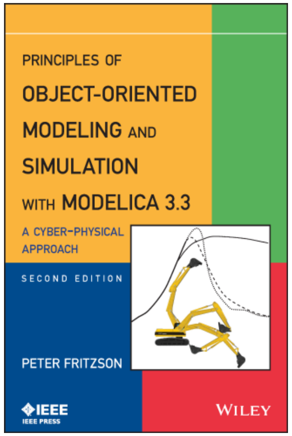


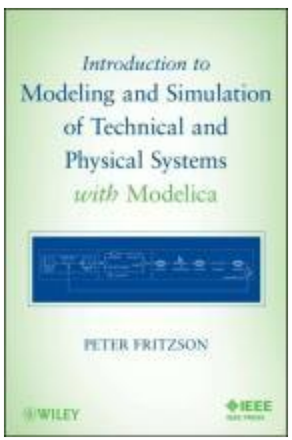
Exercise 3.4 – DrControl

- If there is enough time: Open the DrControl electronic book about control theory with Modelica and do some exercises.
  - **Open File**: C:OpenModelica1.9.3\share\omnotebook\drcontrol\DrControl.onb



Learn more…





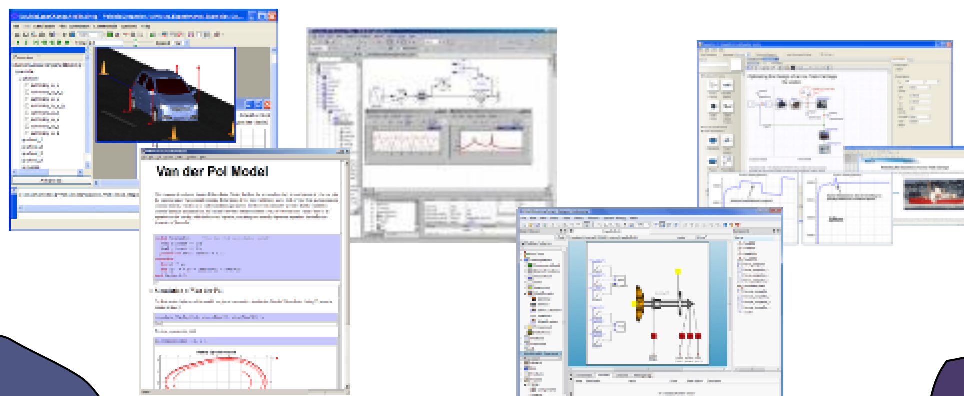
- OpenModelica
  - www.openmodelica.org
- Modelica Association
  - www.modelica.org
- Books
  - Principles of Object Oriented Modeling and Simulation with Modelica 3.3: A Cyber-Physical Approach, Peter Fritzson 2015.
  - Modeling and Simulation of Technical and Physical Systems with Modelica. Peter Fritzson., 2011 http://eu.wiley.com/WileyCDA/WileyTitle/productCd-111801068X.html
  - Introduction to Modelica, Michael Tiller

Summary

Multi-Domain Modeling

Visual Acausal Component Modeling

MODELICA



Typed Declarative Textual Language

Thanks for listening!

Hybrid Modeling