

# **MAT 2020**

## MÉTODOS DE ANÁLISE TÉRMICA

DSC ... Metodologia e Aplicações

# PHASE EQUILIBRIA:

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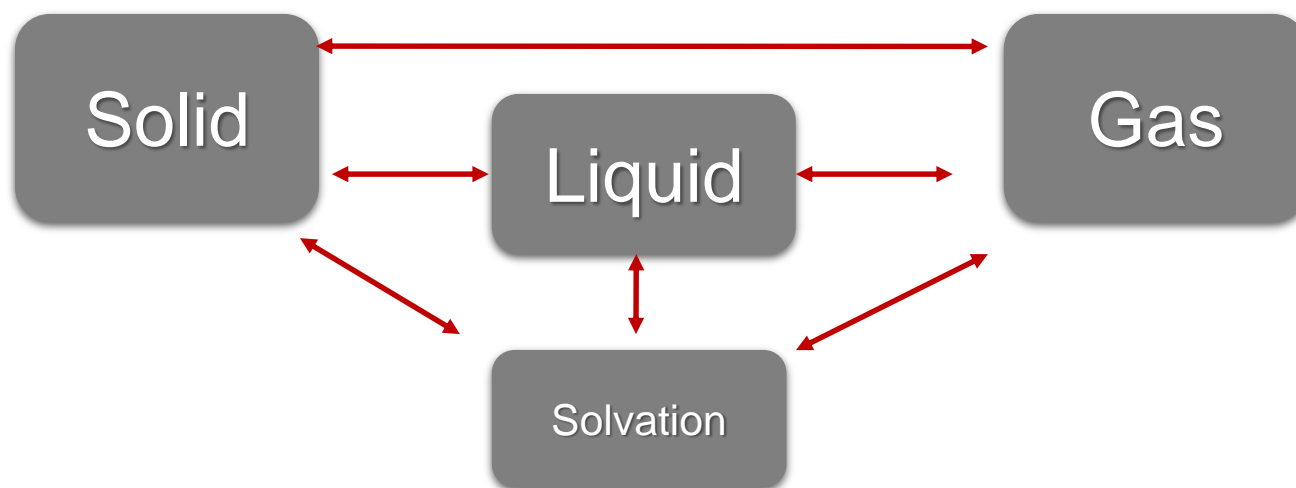
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## Overview

### - Understanding & Modeling



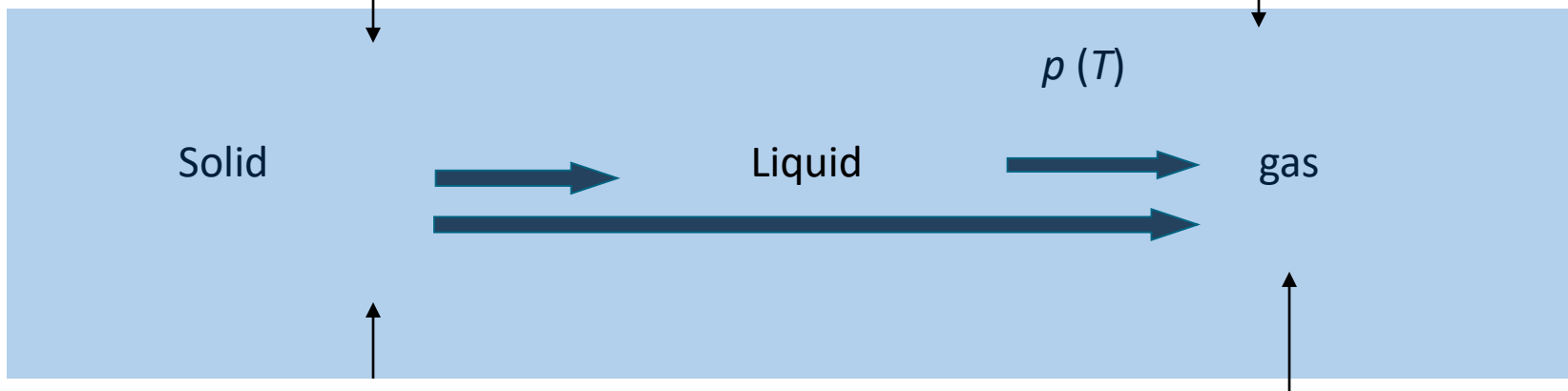
- Molecular **Symmetry**
- Molecular and Supramolecular **Structure**

- C-H- $\pi$  and  $\pi$ - $\pi$  .. interactions
- H-bond
- Electrostatic .. interactions

# Thermodynamics of solid / liquid / gas

**Enthalpies of formation (s/l)**  
(Combustion calorimetry)  
(high precision solution-reaction calorimetry)

**Entropies and Enthalpies of sub/vap (s/l)**  
(Knudsen effusion methods; static methods)  
(Micro calorimetry)

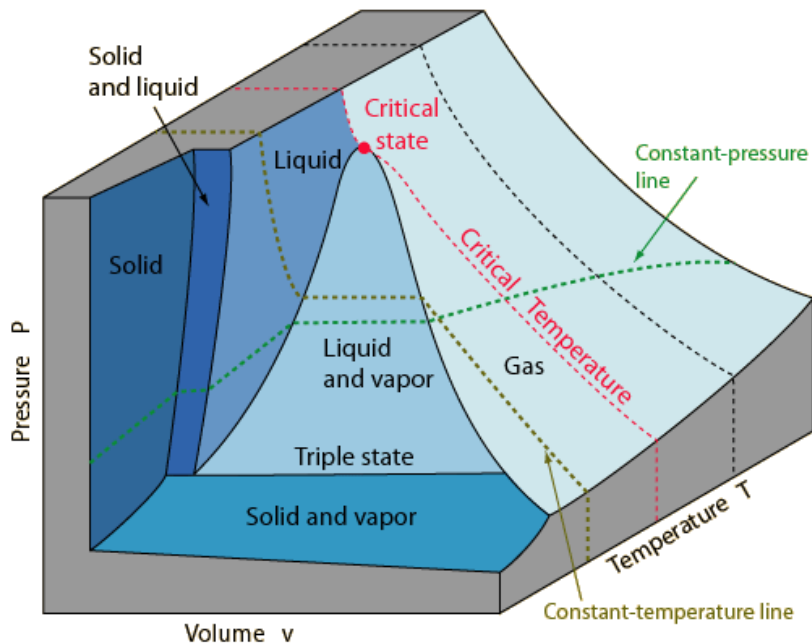


- Heat capacities; enthalpies and entropies of fusion;
- temperature of fusion  
(DSC, adiabatic calorimetry; drop calorimetry)

**Gas phase **ENERGETICS****  
(Computational thermochemistry)

# Pure substances

## *PVT diagram*

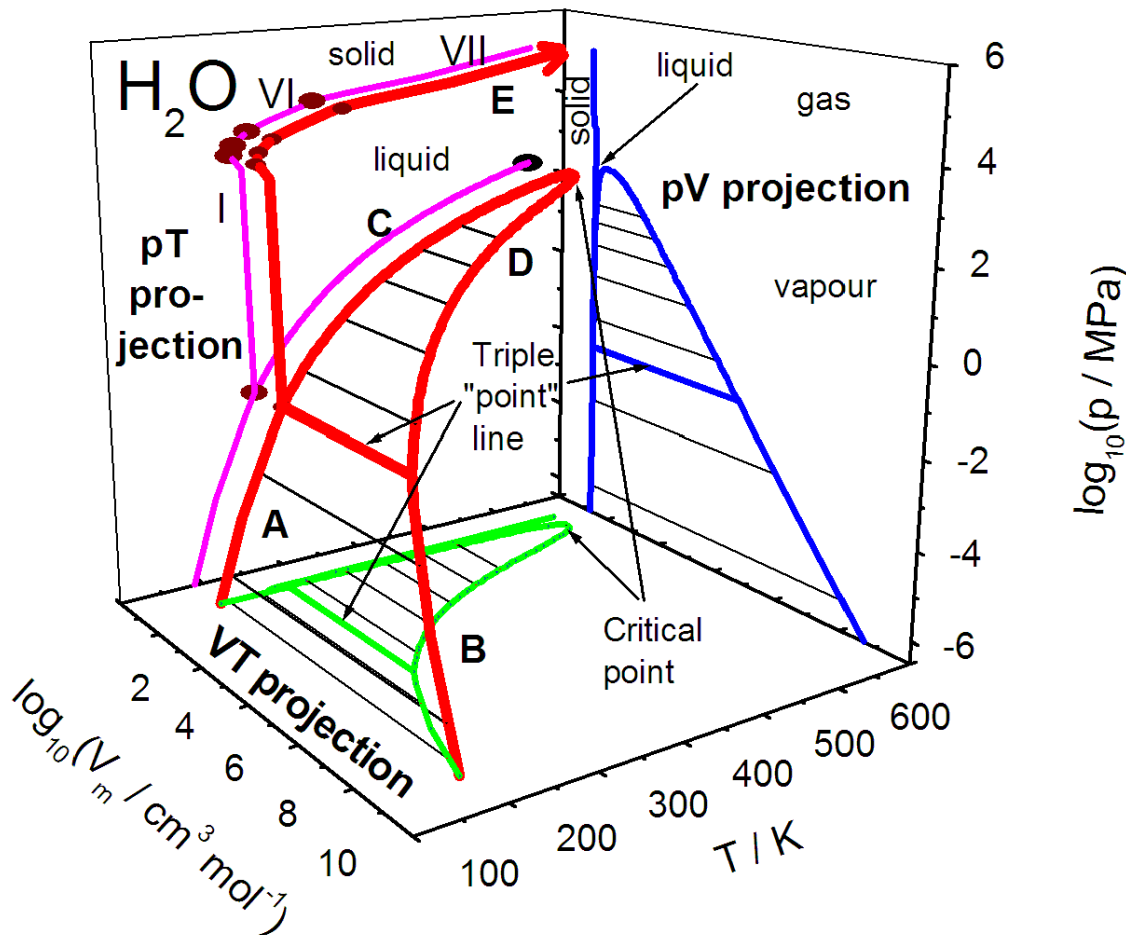


-Why each compound have a different PVT surface profile?

- C-H- $\pi$  and  $\pi$ - $\pi$  .. interactions
- H-bond
- Electrostatic .. interactions
- Molecular shape
- ...???

# Properties of pure substances

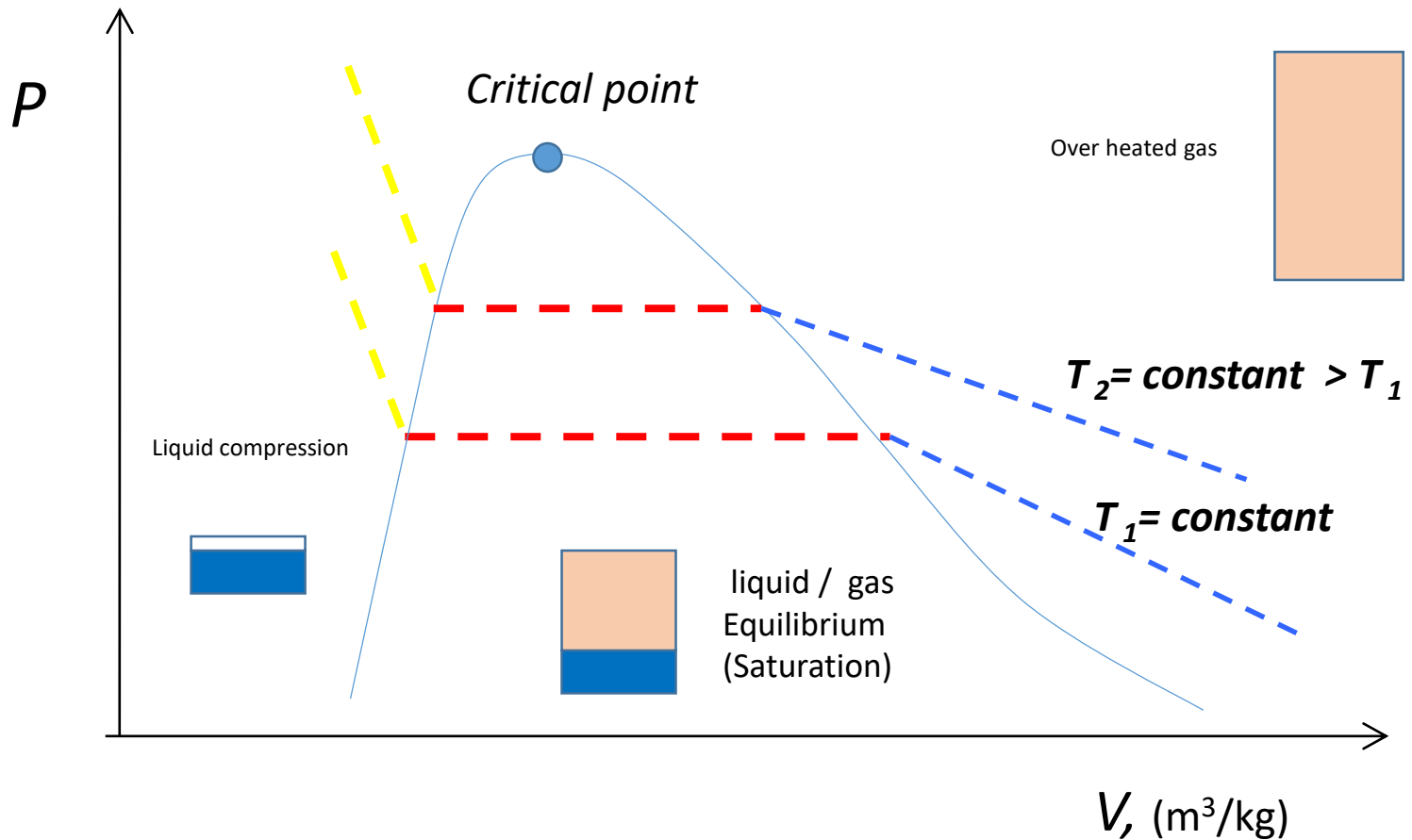
## PVT diagram



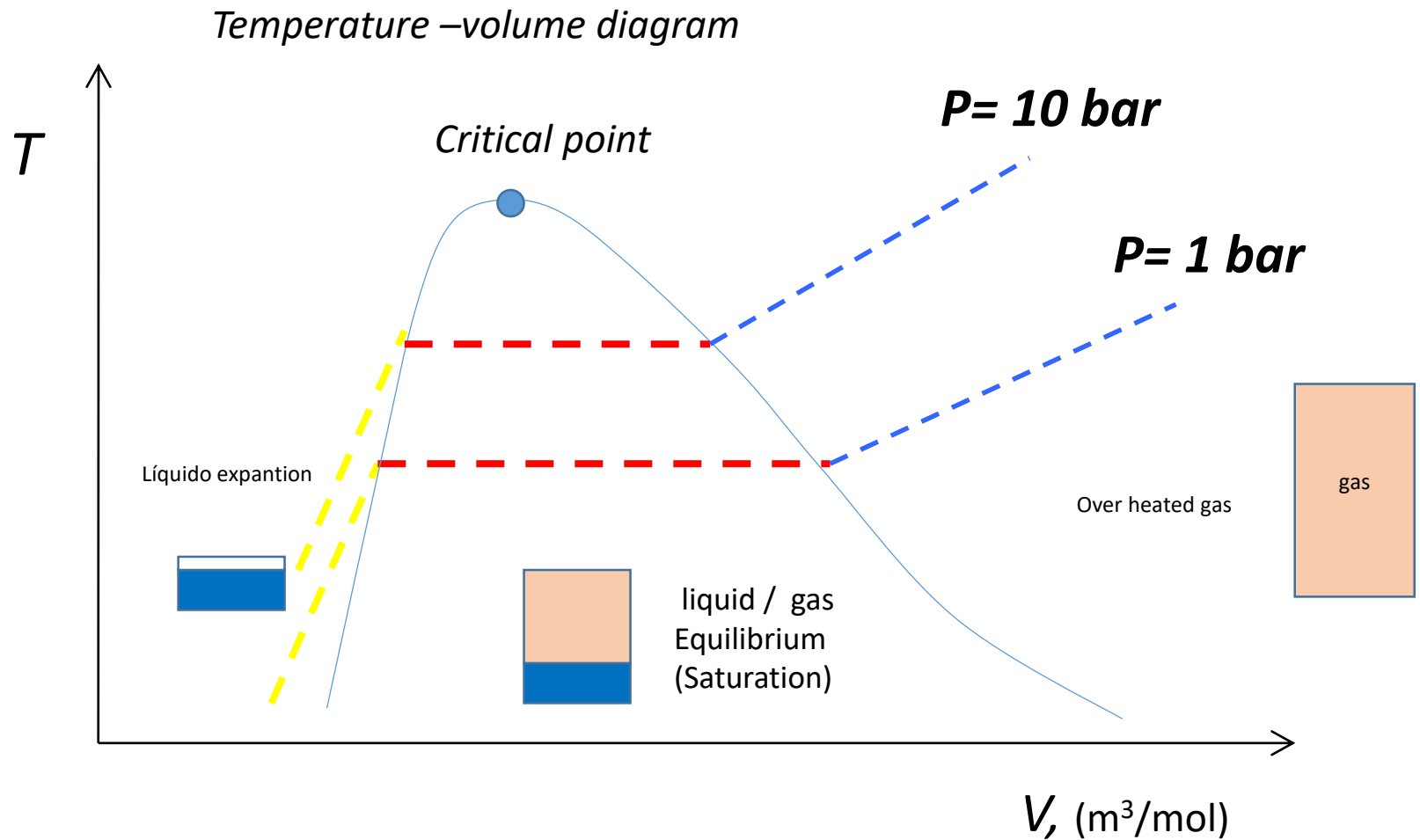
- PT projection :  
Complex and interesting profile!
- VT projection :  
Little dependence of the liquid / solid phases
- PV projection :  
Little dependence of the liquid / solid phases

# Properties of pure substances

Pressure–volume diagram

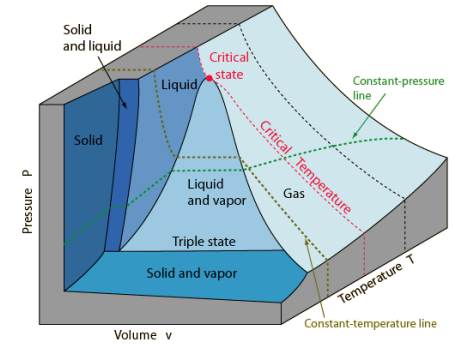
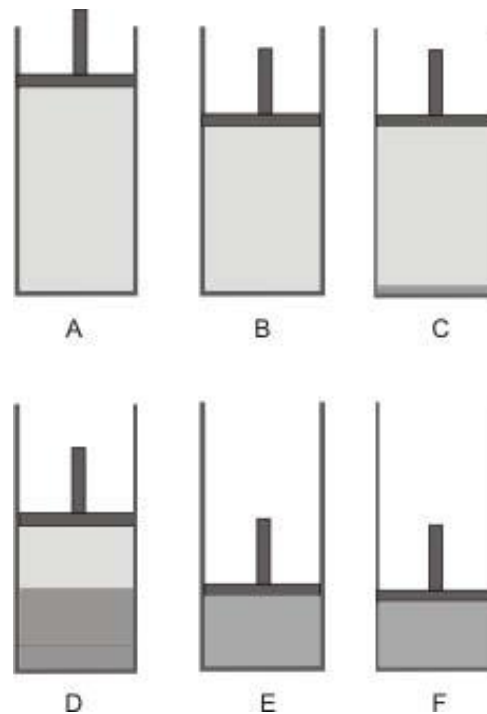
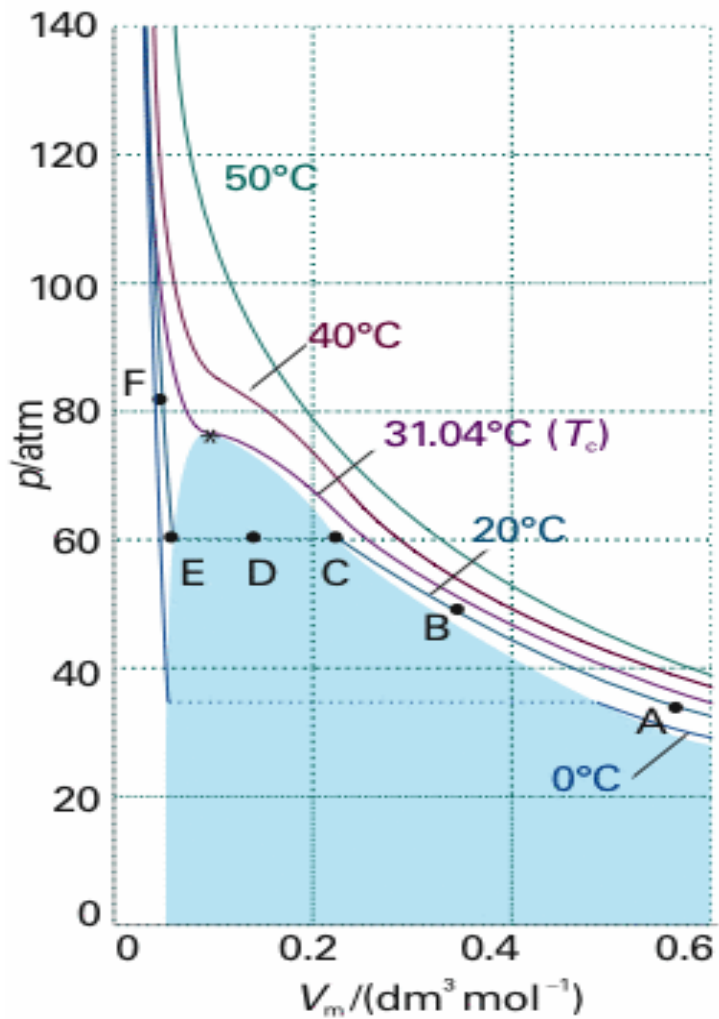


# Properties of pure substances



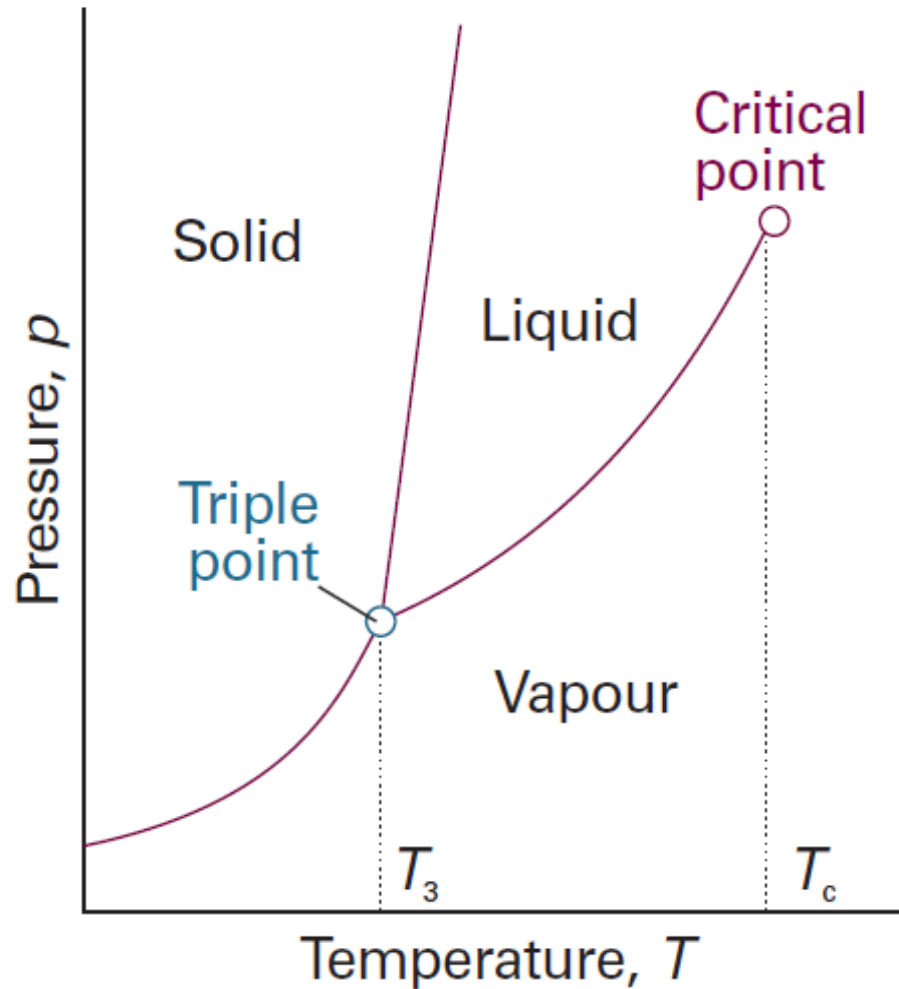


# P-V ...Isothermic lines

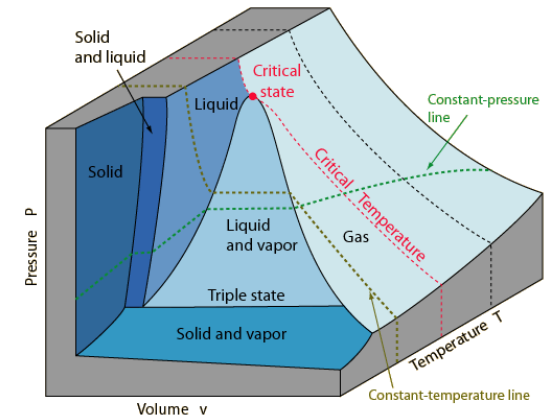


# Properties of pure substances

## PT diagram



- PT projection :  
Complex and interesting profile!



# Properties of pure substances

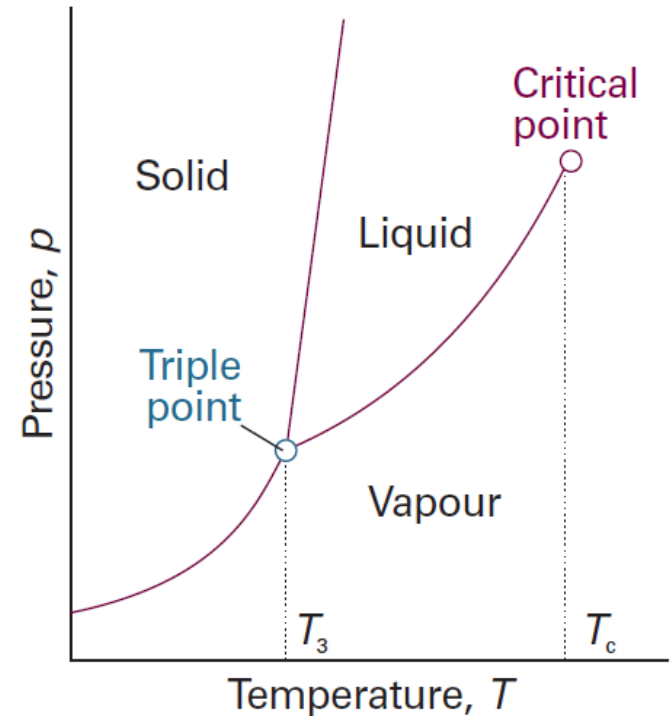
## *PT diagram*

### Phase

of a substance is a form of matter that is **uniform** throughout in **chemical composition** and **physical state**.

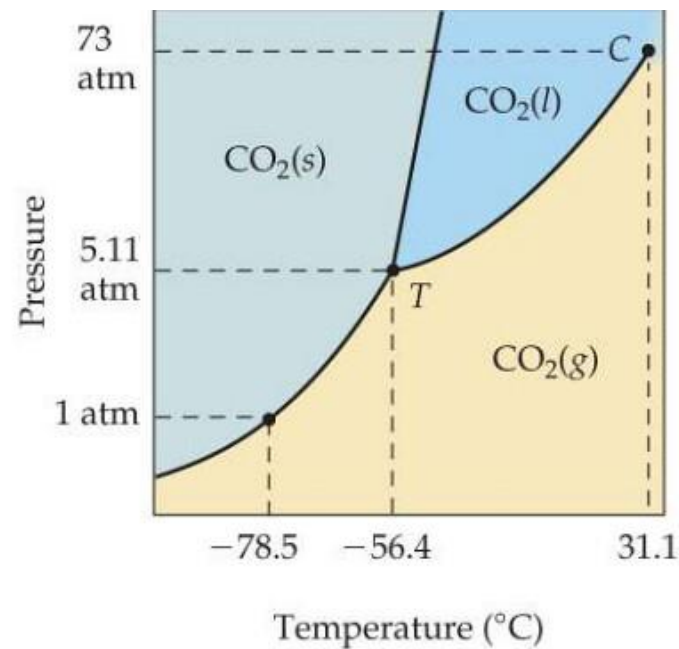
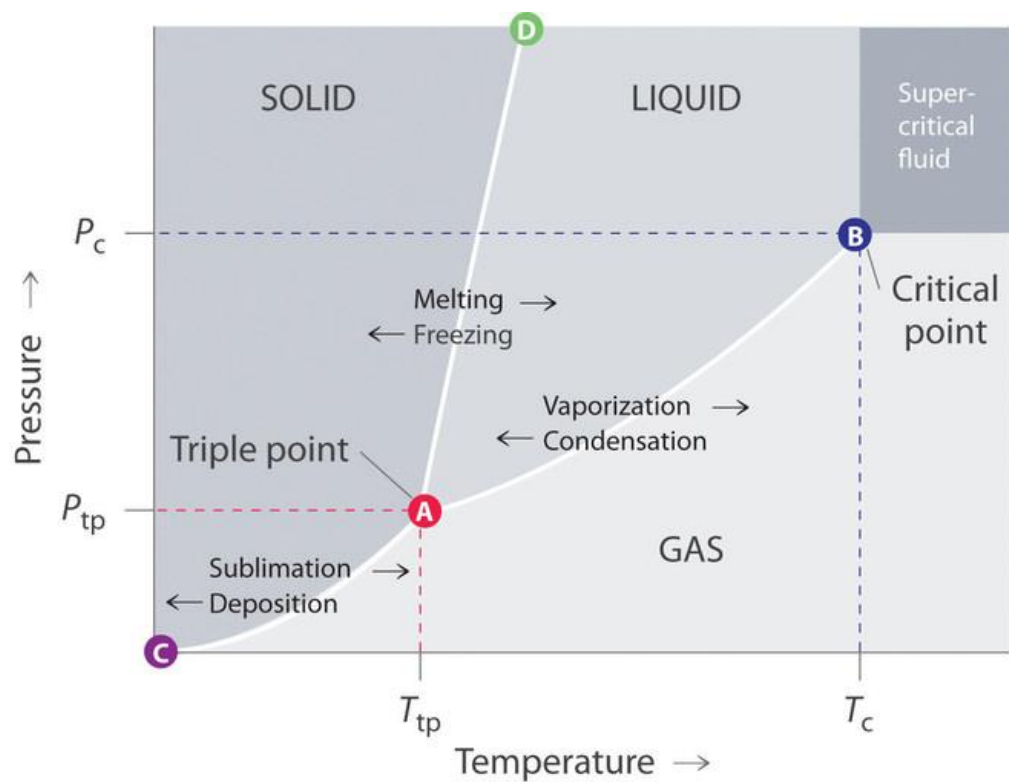
### Phase transition,

the spontaneous **conversion** of one **phase** into another phase, occurs at a characteristic  **$T$**  for a given  **$p$**



# Properties of pure substances

## PT diagram



# Gibbs Phase Rule

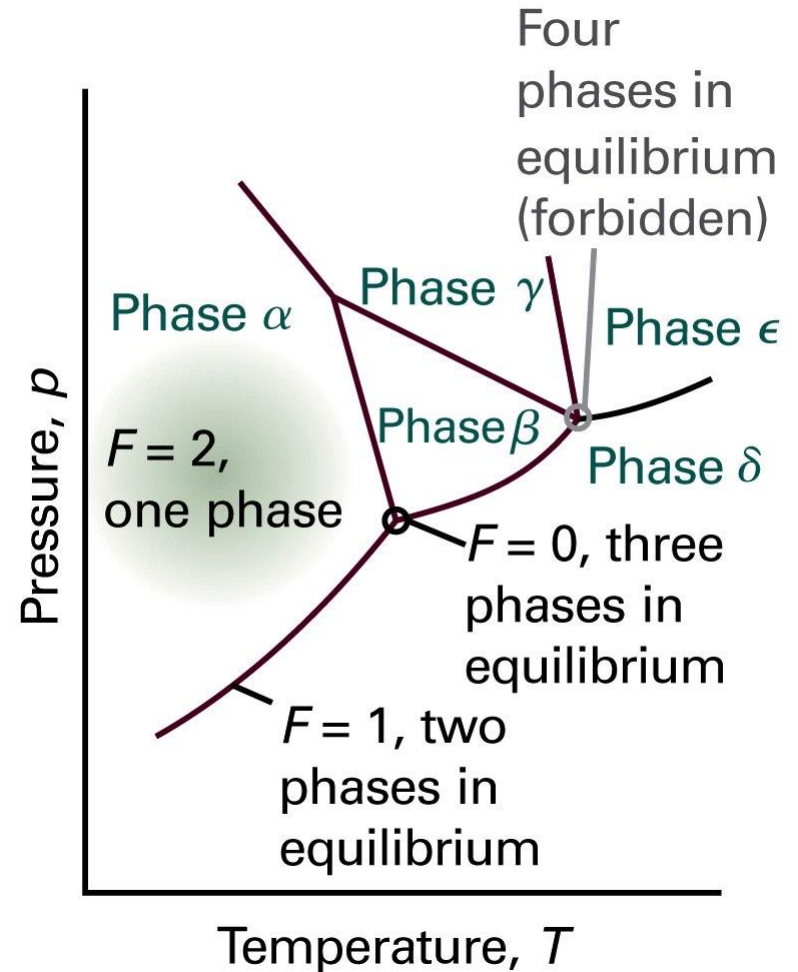
Gibbs Phase rule :  $v$  or  $F = C - P + 2$

$p, T$

for binary mixtures  $C = 2$

# Phases  $P$

Variance: Number of degrees of freedom

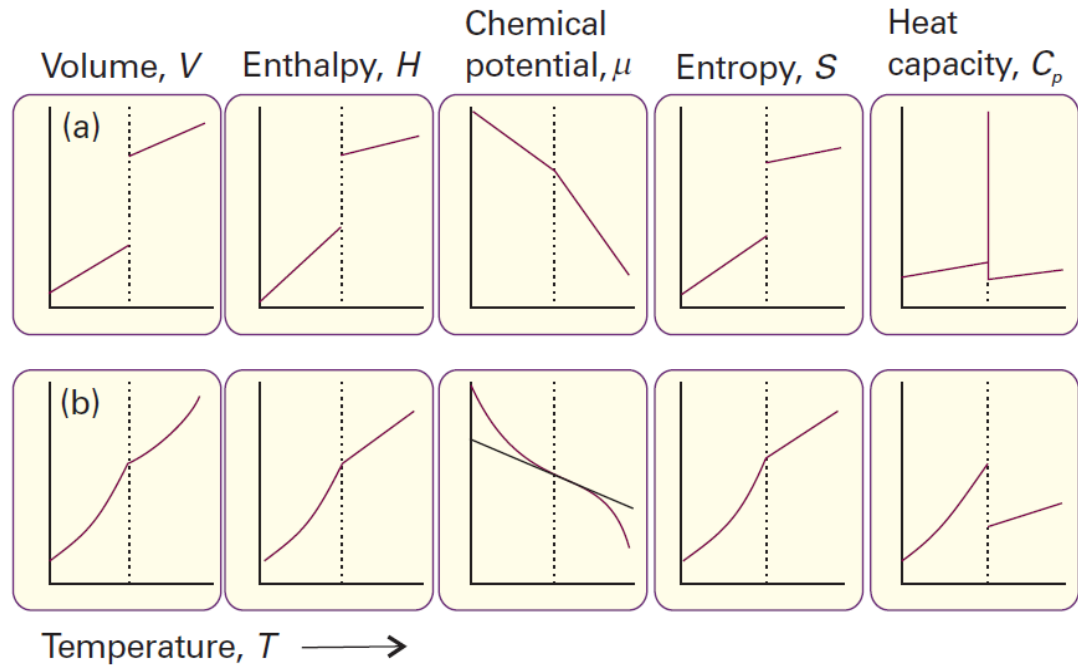


# Properties of pure substances

*PT diagram*

## First-order phase

e.g... fusion, vaporization ..etc



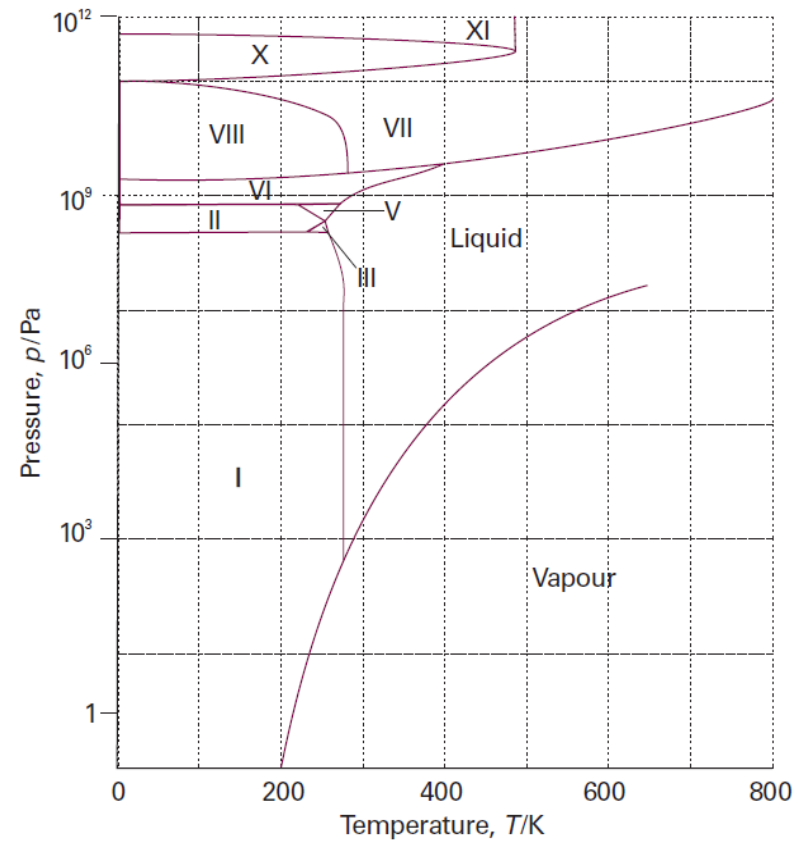
## Second-order

e.g... some ..... solid- solid ..etc

# Properties of pure substances

*PT diagram*

## Complex Phase diagram of $\text{H}_2\text{O}$



# Properties of pure substances

*PT diagram*

## Phase stability

$$\left(\frac{\partial G}{\partial T}\right)_p = -S$$

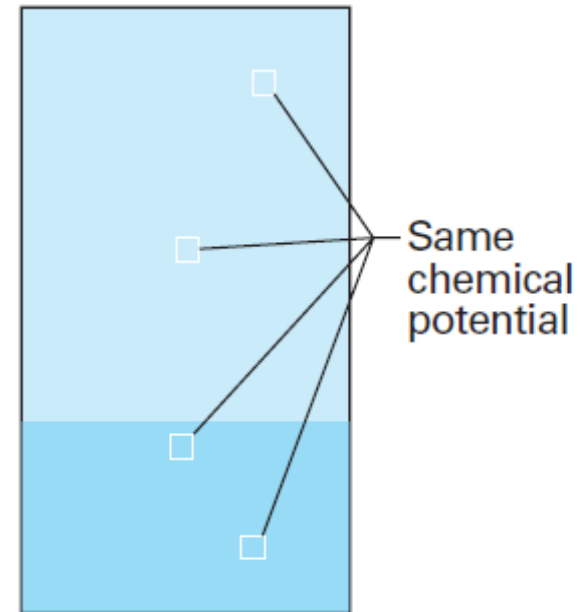
$$\left(\frac{\partial \mu}{\partial T}\right)_p = -S_m$$

$$\mu_\alpha(p, T) = \mu_\beta(p, T)$$



$$S_m(\text{g}) > S_m(\text{l})$$

$$S_m(\text{l}) > S_m(\text{s})$$





# Properties of pure substances

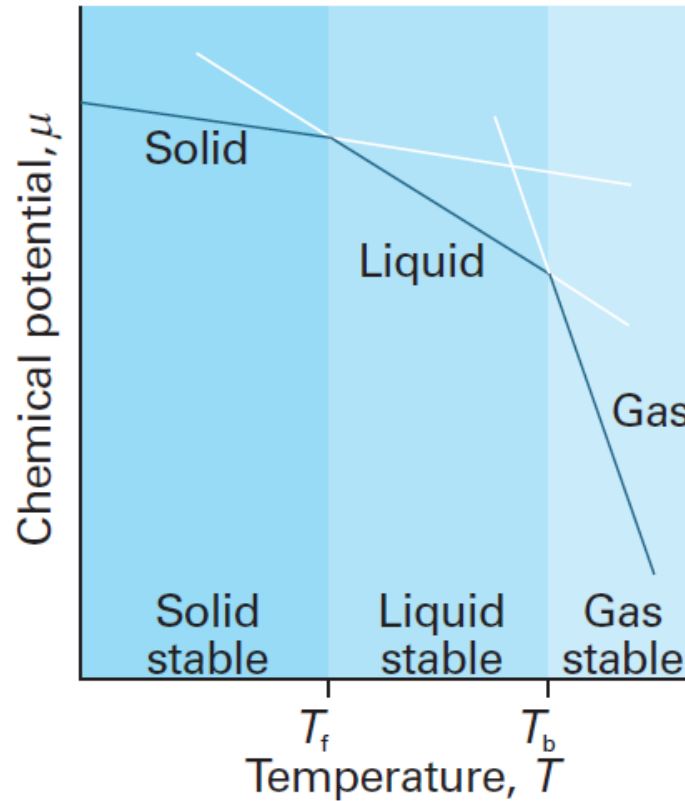
*PT diagram*

## Phase stability



$$\left(\frac{\partial G}{\partial T}\right)_p = -S$$

$$\left(\frac{\partial \mu}{\partial T}\right)_p = -S_m$$



$$S_m(g) > S_m(l)$$

$$S_m(l) > S_m(s)$$

# Properties of pure substances

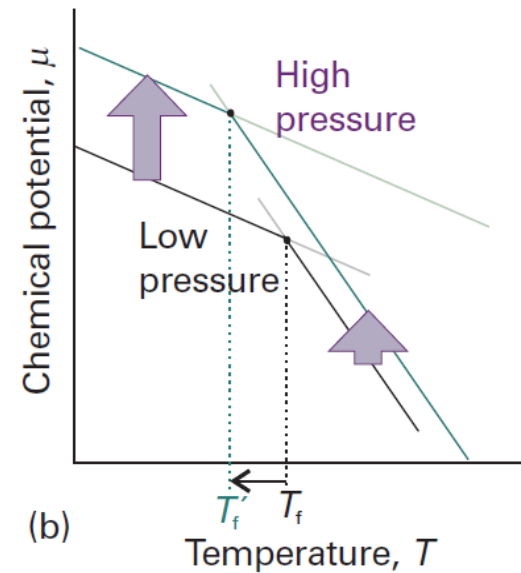
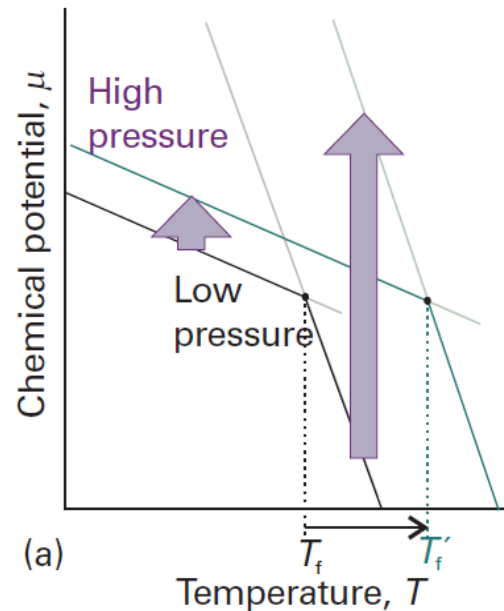
*PT diagram*

## Phase stability

$$\left(\frac{\partial \mu}{\partial p}\right)_T = V_m$$

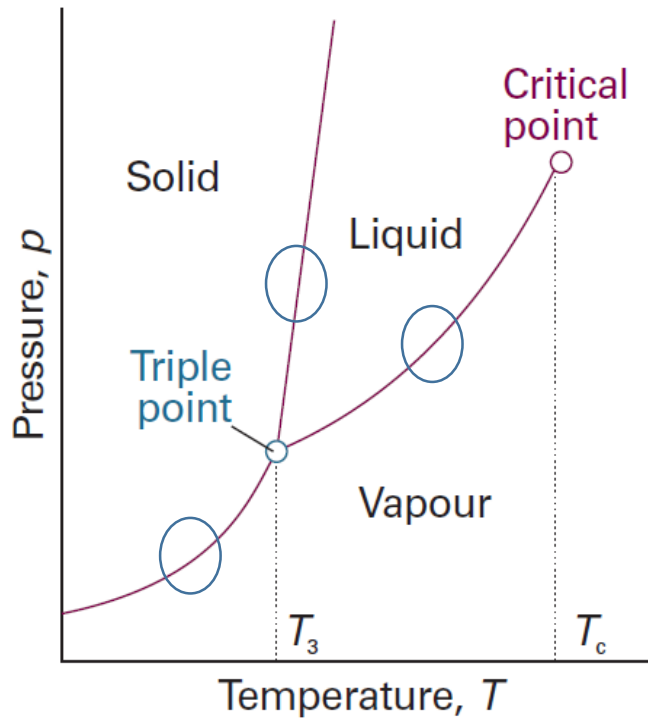
liq  $\rightleftharpoons$  Gas

Sol  $\rightleftharpoons$  Liq



# Properties of pure substances

*PT diagram*



**shape of the  
equilibrium lines**

○  $\frac{dp}{dT}$

# Properties of pure substances

*PT diagram*

$$\mu_{\alpha}(p, T) = \mu_{\beta}(p, T)$$

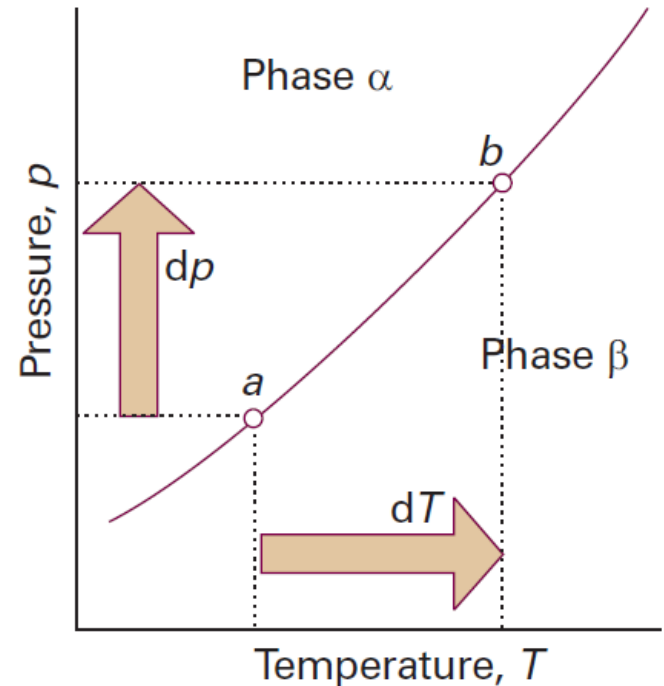


$$\left(\frac{\partial \mu}{\partial p}\right)_T = V_m$$

$$\left(\frac{\partial \mu}{\partial T}\right)_p = -S_m$$

$$\left(\frac{\partial \mu_{\beta}}{\partial p}\right)_T - \left(\frac{\partial \mu_{\alpha}}{\partial p}\right)_T = V_{\beta, m} - V_{\alpha, m} = \Delta_{\text{trs}} V$$

$$\left(\frac{\partial \mu_{\beta}}{\partial T}\right)_p - \left(\frac{\partial \mu_{\alpha}}{\partial T}\right)_p = -S_{\beta, m} + S_{\alpha, m} = \Delta_{\text{trs}} S = \frac{\Delta_{\text{trs}} H}{T_{\text{trs}}}$$



# Properties of pure substances

*PT diagram*

Phase<sub>α</sub>  $\rightleftharpoons$  Phase<sub>β</sub>

$$\mu_{\alpha}(p, T) = \mu_{\beta}(p, T)$$

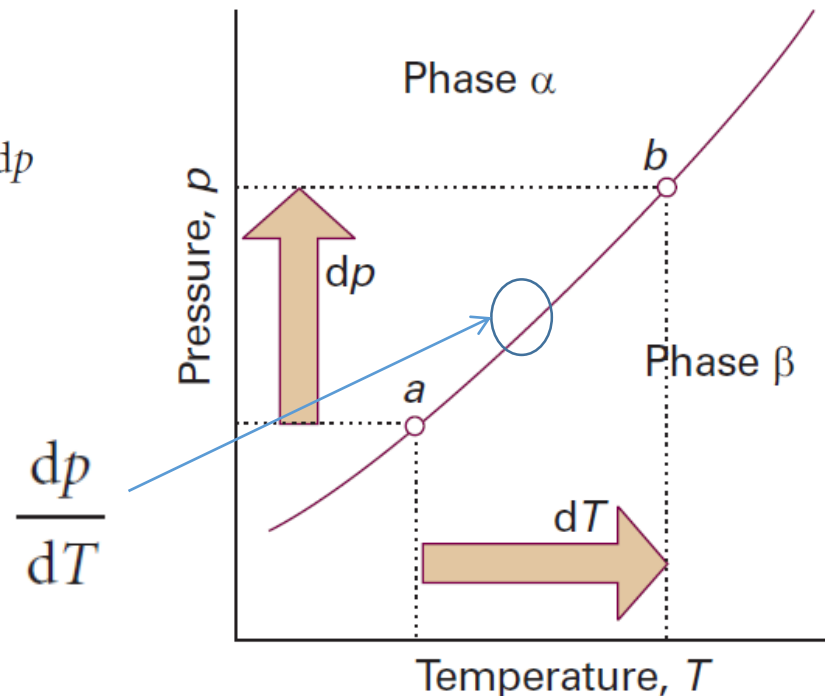
$$-S_{\alpha, m} dT + V_{\alpha, m} dp = -S_{\beta, m} dT + V_{\beta, m} dp$$

$$(V_{\beta, m} - V_{\alpha, m}) dp = (S_{\beta, m} - S_{\alpha, m}) dT$$

**Clapeyron equation**

$$\frac{dp}{dT} = \frac{\Delta_{\text{trs}} S}{\Delta_{\text{trs}} V}$$

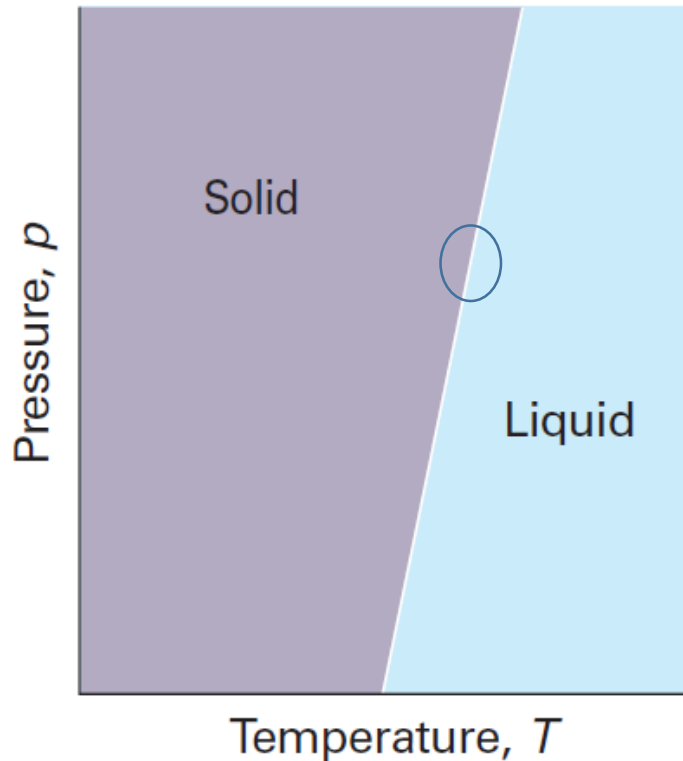
## Shape of the equilibria lines



# Properties of pure substances

## PT diagram

### Solid -Liquid ..condensed phases



$$\Delta_{fus} V = V_m(l) - V_m(s)$$

$$\Delta_{fus} S = S_m(l) - S_m(s)$$

$$\Delta_{fus} S = \Delta_{fus} H / T_{fus}$$

### Clapeyron equation

$$\frac{dp}{dT} = \frac{\Delta_{trs} S}{\Delta_{trs} V}$$

$$\frac{dp}{dT} = \frac{\Delta_{fus} H}{T \Delta_{fus} V}$$

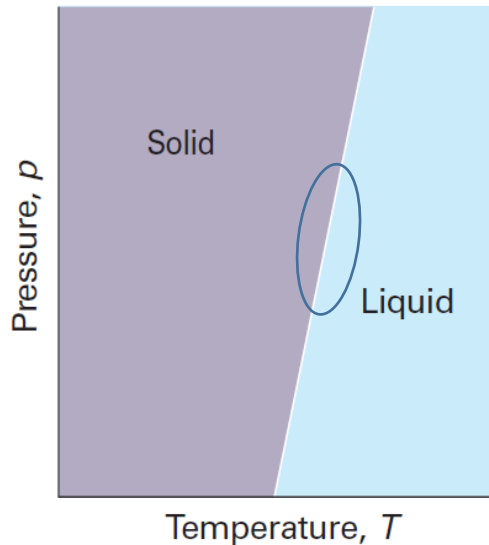
# Properties of pure substances

## PT diagram

### Solid -Liquid ..condensed phases

Clapeyron equation

$$\frac{dp}{dT} = \frac{\Delta_{\text{trs}}S}{\Delta_{\text{trs}}V}$$



$$\frac{dp}{dT} = \frac{\Delta_{\text{fus}}H}{T\Delta_{\text{fus}}V}$$

$$\int_{p^*}^p dp = \frac{\Delta_{\text{fus}}H}{\Delta_{\text{fus}}V} \int_{T^*}^T \frac{dT}{T}$$

$$p \approx p^* + \frac{\Delta_{\text{fus}}H}{\Delta_{\text{fus}}V} \ln \frac{T}{T^*}$$

$$\ln \frac{T}{T^*} = \ln \left( 1 + \frac{T - T^*}{T^*} \right) \approx \frac{T - T^*}{T^*}$$

therefore,

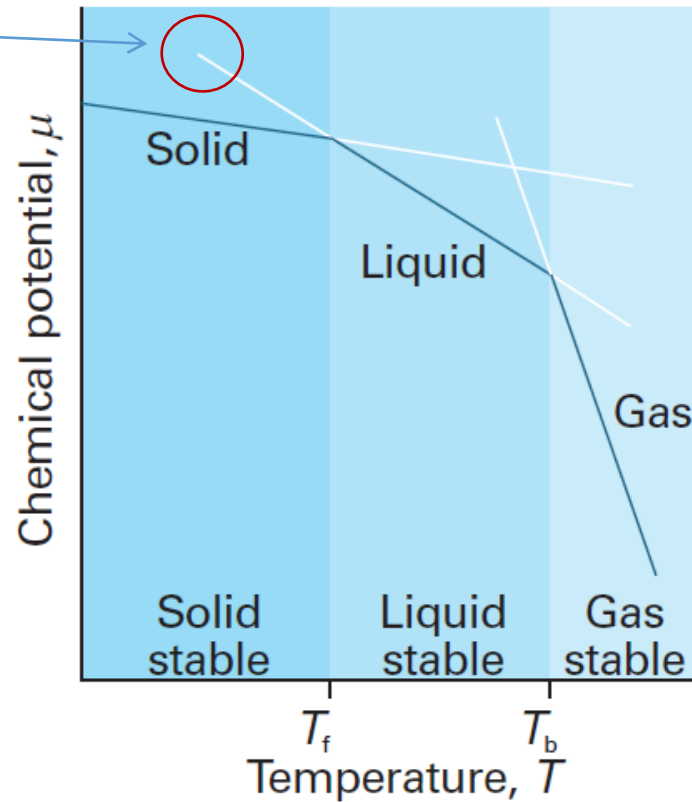
$$p \approx p^* + \frac{\Delta_{\text{fus}}H}{T^*\Delta_{\text{fus}}V} (T - T^*)$$

### Linear approximation

# DSC: Supercooled Liquid

**Supercooled Liquid**

e.g. quenching the liquid

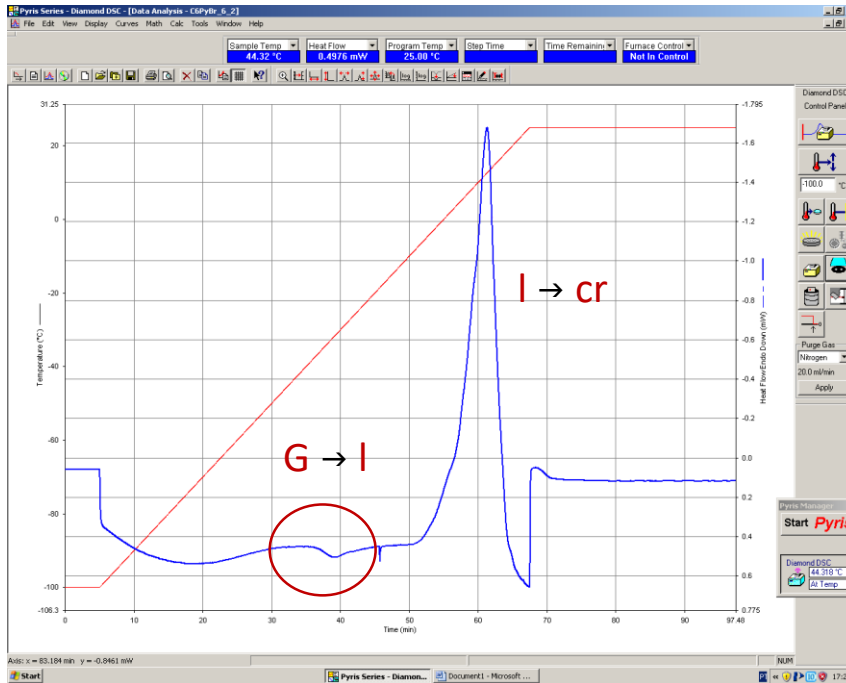




# DSC: Supercooled Liquid

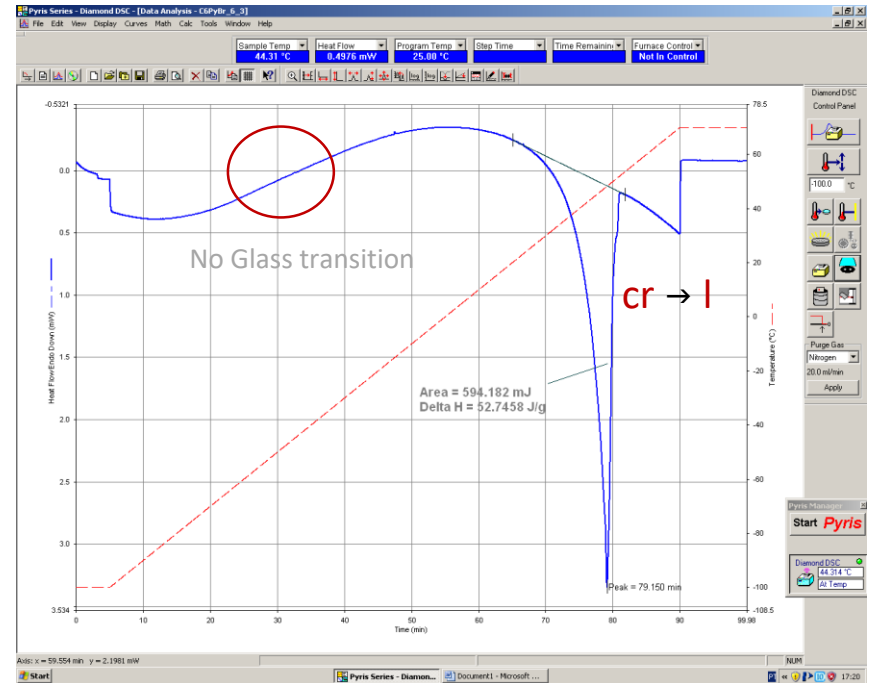
## Cold Crystallization

Glass to Liquid ..  $T_g$

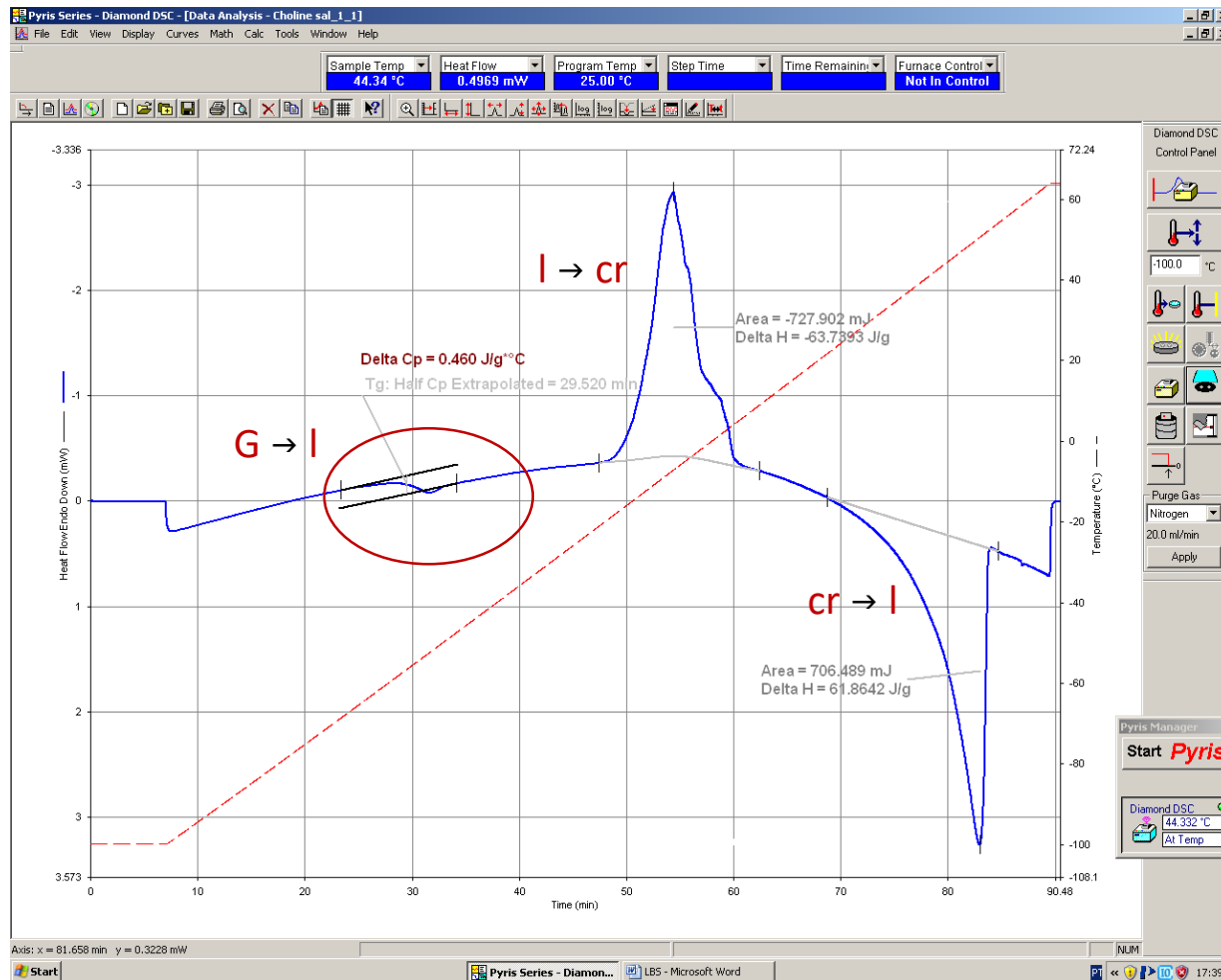


## Melting

No Glass transition found ..  $T_g$



# DSC: Supercooled Liquid



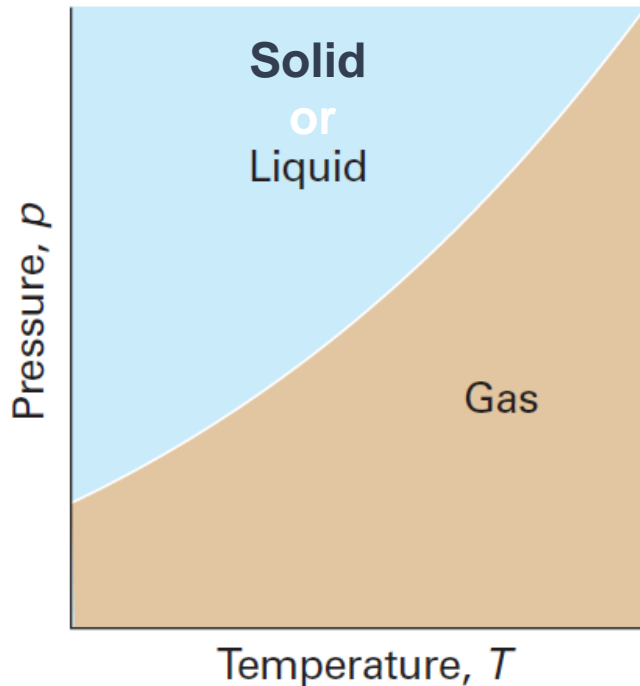
# Properties of pure substances

## PT diagram

liquid–vapour  
solid–vapour

Clapeyron equation

$$\frac{dp}{dT} = \frac{\Delta_{\text{trs}}S}{\Delta_{\text{trs}}V}$$



$$\frac{dp}{dT} = \frac{\Delta_{\text{vap}}H}{T\Delta_{\text{vap}}V}$$

$$\frac{dp}{dT} = \frac{\Delta_{\text{vap}}H}{T(RT/p)}$$

$$V_{\text{m}}(\text{g}) = RT/p$$

$$\Delta_{\text{vap}}V \approx V_{\text{m}}(\text{g})$$

$$\frac{d \ln p}{dT} = \frac{\Delta_{\text{vap}}H}{RT^2}$$

$$\ln \frac{p}{p^\circ} = -\frac{\Delta_{\text{cr/l}}^{\text{g}}H_{\text{m}}^\circ}{R} \cdot \frac{1}{T} + \frac{\Delta_{\text{cr/l}}^{\text{g}}S_{\text{m}}}{R}$$

Clausius–Clapeyron equation

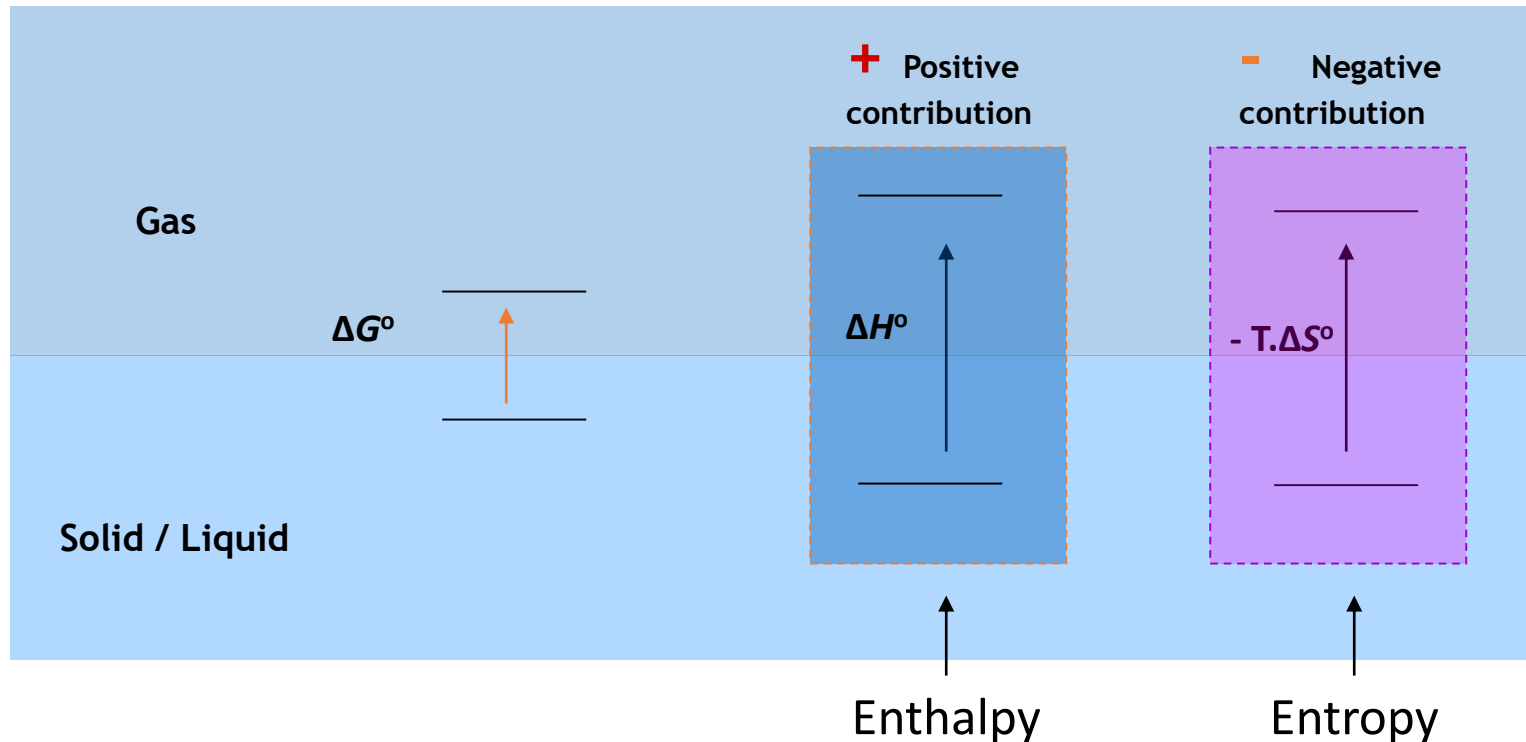
# Properties of pure substances

*PT diagram*

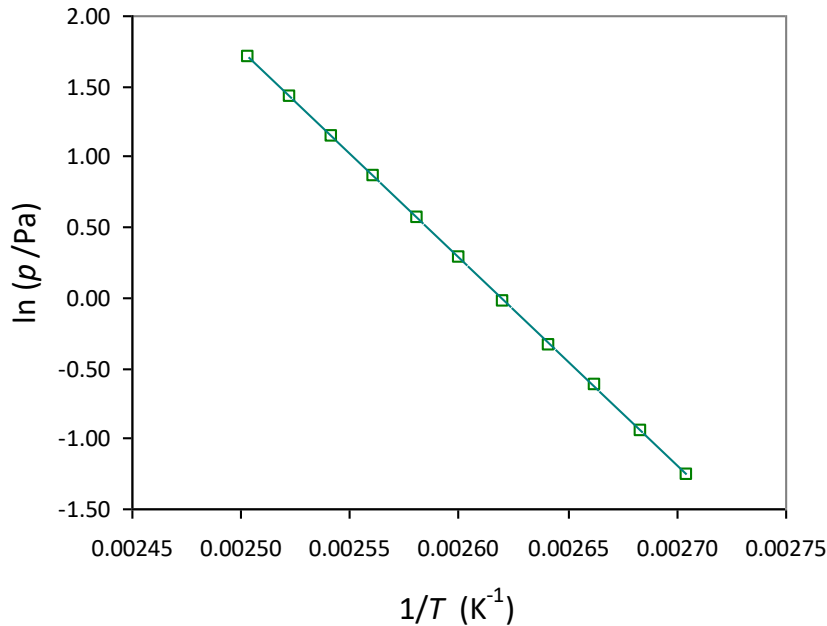
$P = f(T)$  ... vapor pressure Measurements

$$\ln \frac{p}{p^0} = -\frac{\Delta_{cr/l}^g H_m^0}{R} \cdot \frac{1}{T} + \frac{\Delta_{cr/l}^g S_m}{R}$$

$$\Delta G^0 = \Delta H^0 - T \cdot \Delta S^0 = -RT \cdot \ln (p/p^0)$$



# $p=f(T)$ .....Phase diagrams

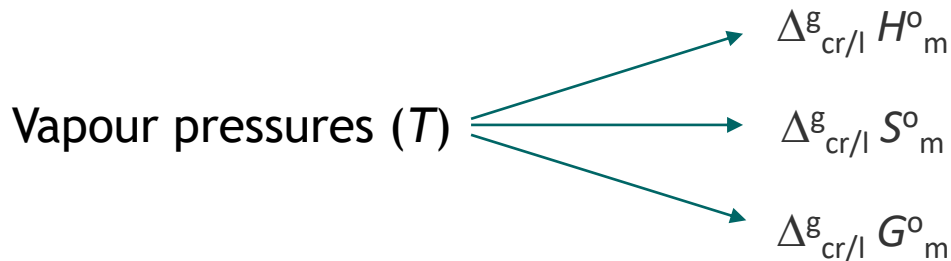


## Clausius-Clapeyron equation

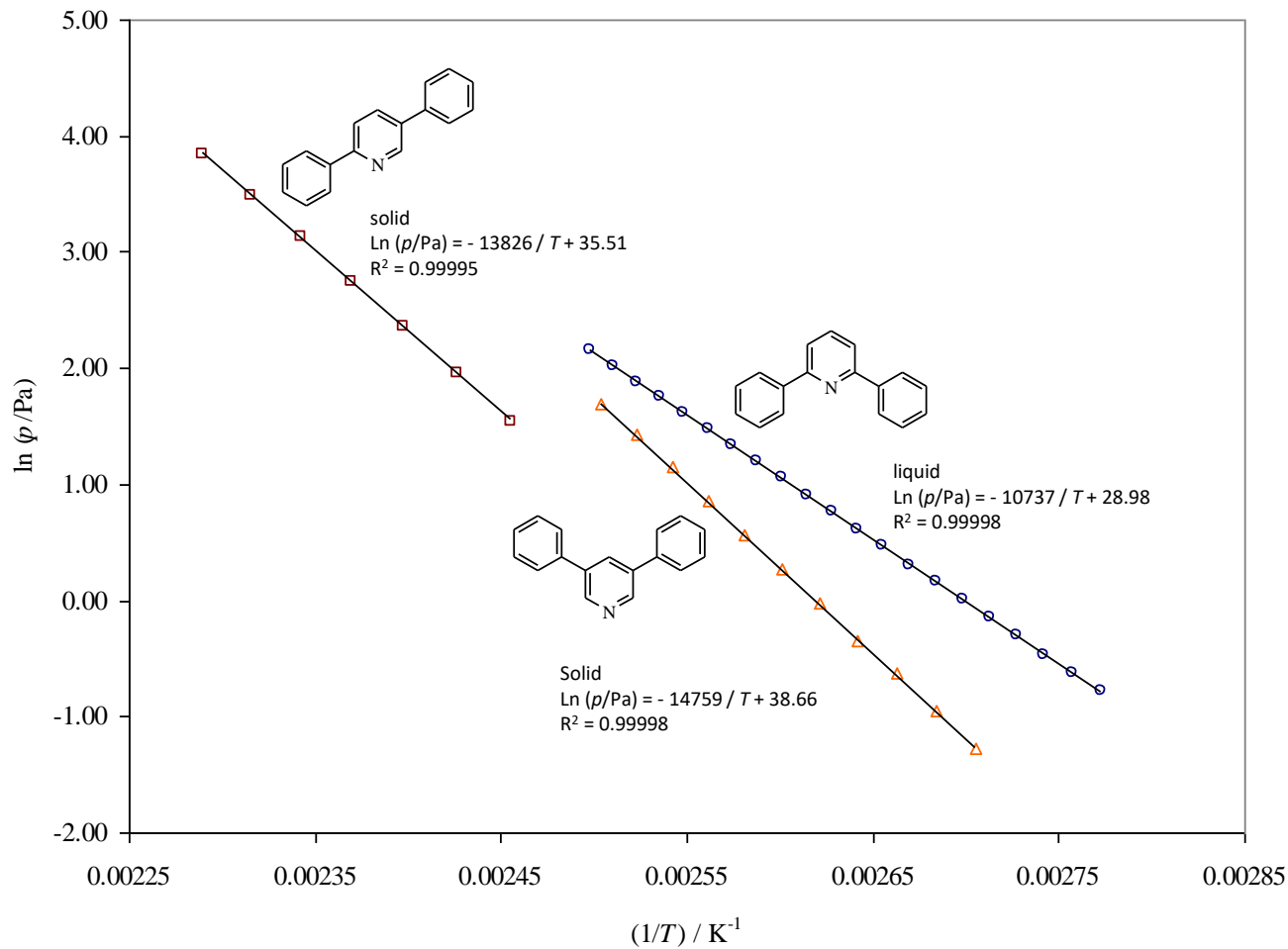
$$\ln \frac{p}{p^\circ} = -\frac{\Delta_{cr/l}^g H_m^\circ}{R} \cdot \frac{1}{T} + \frac{\Delta_{cr/l}^g S_m}{R}$$

## Clarke & Glew equation

Cp ..correction



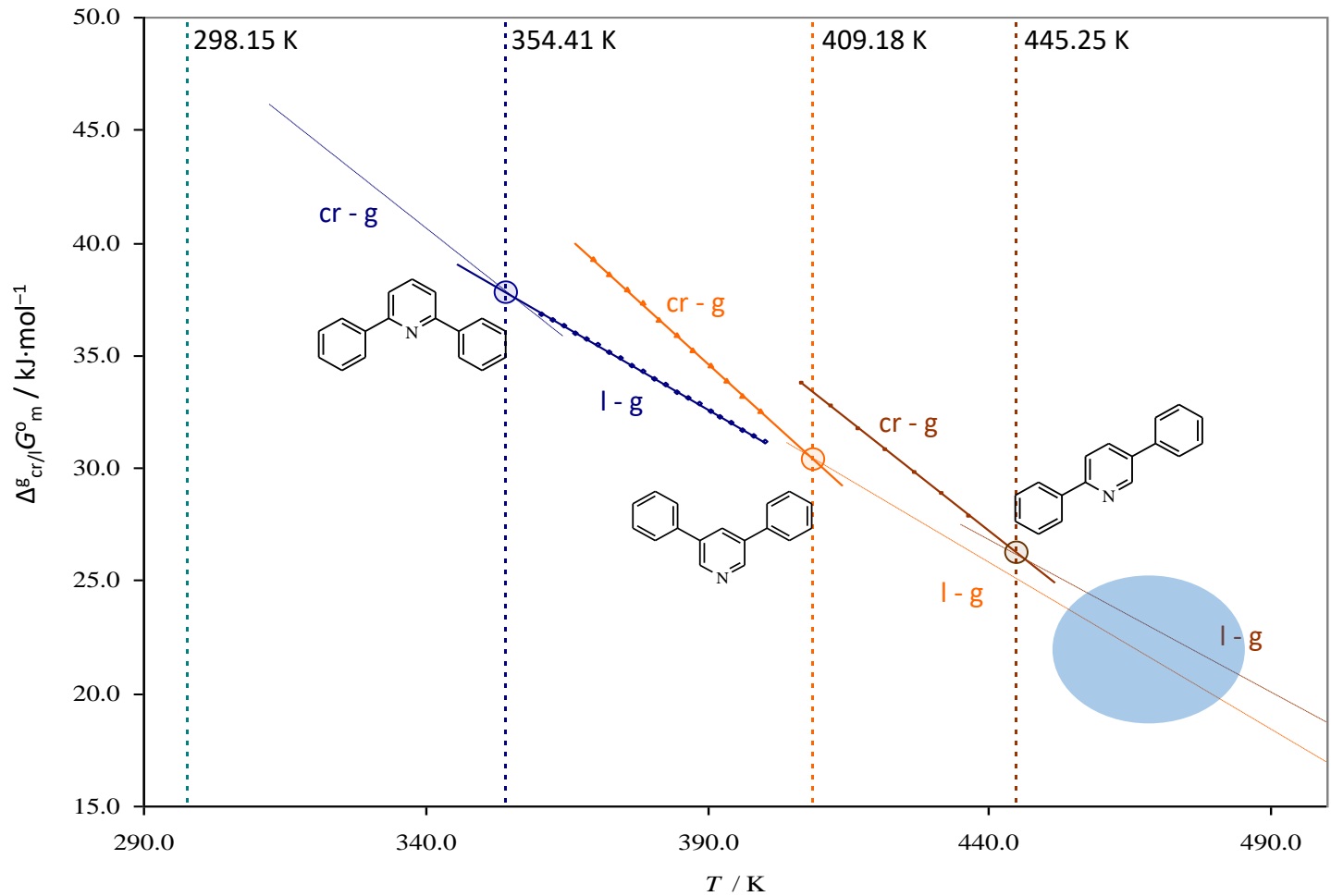
# $p=f(T)$ .....Phase diagrams



MKS (0-1333 Pa)

MKS (0-133 Pa)

# $\rho=f(T)$ .....Phase diagrams



- C-H- $\pi$  and  $\pi$ - $\pi$  .. interactions
- H-bond
- Electrostatic .. interactions
- Molecular shape
- ...???

# $p=f(T)$ .....Phase diagrams

