

FORMULÁRIO – PSI3483 – ONDAS ELETROMAGNÉTICAS EM MEIOS GUIADOS

$\mu = \mu_r \mu_0$	$\varepsilon = \varepsilon_r \varepsilon_0$	$\mu_0 = 4\pi 10^{-7} (H/m)$
$\varepsilon_0 = 8,854 \cdot 10^{-12} (F/m)$		$tg \delta = \frac{\varepsilon'}{\varepsilon''} \quad \varepsilon' = \varepsilon_r$

Guias de ondas retangulares

Modos TE e TM			
$f_c = \frac{v}{2} \sqrt{\left(\frac{m}{a}\right)^2 + \left(\frac{n}{b}\right)^2}$		TE: $m, n = 0, 1, 2, \dots \quad m + n \neq 0$ TM: $m, n = 1, 2, 3, \dots$	
$\gamma = \sqrt{\left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 - \omega^2 \mu \varepsilon}$		$v = \frac{c}{\sqrt{\varepsilon_r}} \quad c = 3 \cdot 10^{11} \frac{mm}{s}$	
$\lambda_g = \lambda / \sqrt{1 - \left(\frac{f_c}{f}\right)^2}$	$\lambda = \frac{c}{f \cdot \sqrt{\varepsilon_r}}$	$Z_{TM} = \eta \sqrt{1 - \left(\frac{f_c}{f}\right)^2}$	$Z_{TE} = \eta / \sqrt{1 - \left(\frac{f_c}{f}\right)^2}$
Modos evanescentes $f < f_c$		Modos propagantes $f > f_c$	

Para o modo fundamental TE ₁₀	
Perda dielétrica	$\alpha_{d10} = 8,686 \cdot \frac{\omega \sqrt{\mu_0 \cdot \varepsilon'} \cdot (\varepsilon'' / \varepsilon')}{\eta \cdot b \cdot \sqrt{1 - (f_{c10} / f)^2}} \quad (dB / m)$
Perda condutiva	$\alpha_{c10} = 8,686 \cdot \frac{R_s [1 + (2b/a) \cdot (f_{c10} / f)^2]}{\eta \cdot b \cdot \sqrt{1 - (f_{c10} / f)^2}} \quad (dB / m)$
	$R_s = \sqrt{\frac{\omega \mu}{2\sigma}} \quad \eta = \frac{\eta_0}{\sqrt{\varepsilon_r}} = \frac{377}{\sqrt{\varepsilon_r}} \quad \Omega$
Perda total	$\alpha (dB / m) = \alpha_c (dB / m) + \alpha_d (dB / m)$

Guias de ondas cilíndricos

<p style="text-align: center;">Modos TM</p> $f_c = \frac{v}{2\pi \cdot a} \cdot p_{nm}$	<table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">n</th> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">p_{n1}</th> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">p_{n2}</th> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">p_{n3}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>2.405</td> <td>5.520</td> <td>8.654</td> </tr> <tr> <td>1</td> <td>3.832</td> <td>7.016</td> <td>10.174</td> </tr> <tr> <td style="border-bottom: 3px double black;">2</td> <td style="border-bottom: 3px double black;">5.135</td> <td style="border-bottom: 3px double black;">8.417</td> <td style="border-bottom: 3px double black;">11.620</td> </tr> </tbody> </table> <p>Zeros da função de Bessel de primeira ordem</p>	n	p_{n1}	p_{n2}	p_{n3}	0	2.405	5.520	8.654	1	3.832	7.016	10.174	2	5.135	8.417	11.620
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<p style="text-align: center;">Modos TE</p> $f_c = \frac{v}{2\pi \cdot a} \cdot p'_{nm}$	<table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">n</th> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">p'_{n1}</th> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">p'_{n2}</th> <th style="border-top: 1px solid black; border-bottom: 1px solid black;">p'_{n3}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>3.832</td> <td>7.016</td> <td>10.174</td> </tr> <tr> <td>1</td> <td>1.841</td> <td>5.331</td> <td>8.536</td> </tr> <tr> <td style="border-bottom: 3px double black;">2</td> <td style="border-bottom: 3px double black;">3.054</td> <td style="border-bottom: 3px double black;">6.706</td> <td style="border-bottom: 3px double black;">9.970</td> </tr> </tbody> </table> <p>Zeros da derivada da função de Bessel de primeira ordem</p>	n	p'_{n1}	p'_{n2}	p'_{n3}	0	3.832	7.016	10.174	1	1.841	5.331	8.536	2	3.054	6.706	9.970
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Parâmetro	Modos TE _{nm}	Modos TM _{nm}
λ_g	$\frac{2\pi}{\beta}$	$\frac{2\pi}{\beta}$
β	$\sqrt{k^2 - k_c^2}$	$\sqrt{k^2 - k_c^2}$
k	$\omega\sqrt{\mu\epsilon} = \frac{\omega}{v} = \frac{\omega}{c} \cdot \sqrt{\epsilon_r}$	$\omega\sqrt{\mu\epsilon} = \frac{\omega}{v} = \frac{\omega}{c} \cdot \sqrt{\epsilon_r}$
k_c	$\frac{p'_{nm}}{a}$	$\frac{p_{nm}}{a}$

Cabos coaxiais

$Z_c = \frac{60}{\sqrt{\epsilon_r}} \ln(b/a)$	$C = \frac{2\pi \cdot \epsilon_r \epsilon_0}{\ln(b/a)}$	$L = \frac{\mu}{2\pi} \ln \frac{b}{a}$
$G = \omega \cdot \text{tg} \delta \cdot C$	$f_c = \frac{c \cdot k_c}{2\pi \cdot \sqrt{\epsilon_r}}$	$k_c \approx \frac{2}{a+b}$
$\delta_s = \frac{1}{\sqrt{\pi f \mu \sigma}}$	$R_a = \frac{\rho_a}{A_a} \quad e \quad R_b = \frac{\rho_b}{A_b}$	$\sigma = \frac{1}{\rho}$
$\lambda = \frac{\lambda_0}{\sqrt{\epsilon_r}} \quad \lambda_0 = \frac{c}{f}$	$A_a = \delta_s \cdot 2\pi \cdot a$ $A_b = \delta_s \cdot 2\pi \cdot b$	$R = \frac{1}{2} \sqrt{\frac{f \cdot \mu}{\pi \cdot \sigma}} \left(\frac{1}{a} + \frac{1}{b} \right)$ <p style="text-align: center;">para $\rho_a = \rho_b$</p>