## PSI-3552 Fabricação e Caracterização de Dispositivos Nanoeletrônicos

Aula 03 - Dopagem Difusão Térmica

Laboratório de Microeletrônica Escola Politécnica Universidade de São Paulo

Prof. Roberto K. Onmori sala C2-70 (tel. 3091-5251)

email: RKONMORI@LME.USP.BR

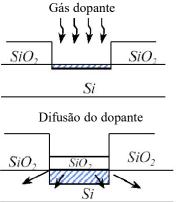
Prof. Fernando J. Fonseca sala C2-65 (tel. 3091-0730)

email: FERNANDO.EPUSP@GMAIL.COM

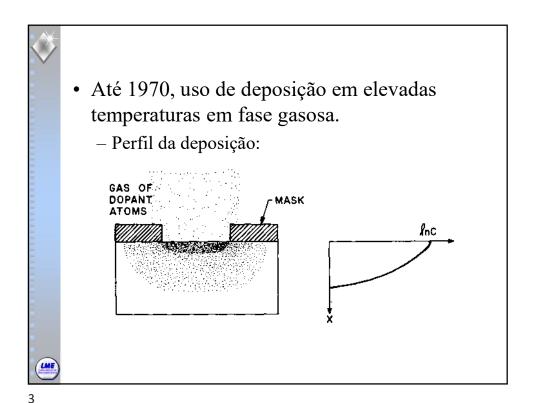
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## Introdução

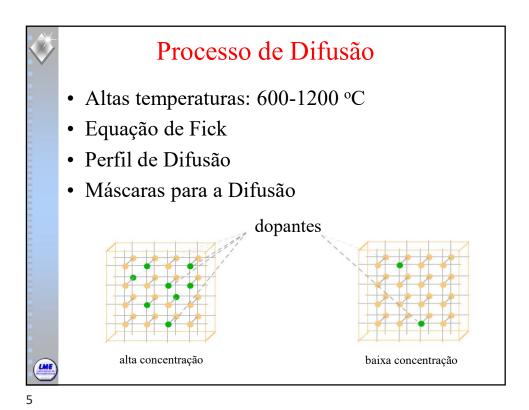
- Historicamente, necessidade de introduzir impurezas por difusão para obter regiões do tipo n (P, As) ou p (B) no silício.
- Dopagem é a exposição da lâmina de Si em uma fonte contendo P, As ou B (deposição) e
  - e a sua difusão em alta temperatura  $SiO_2 = SiO_2$

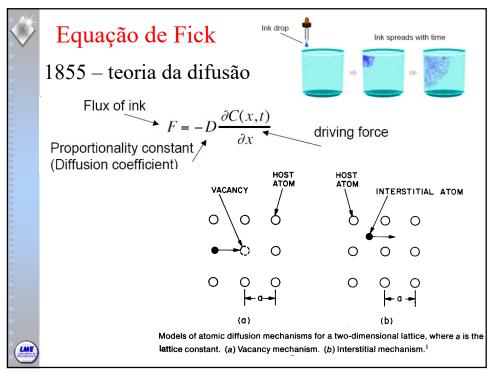


LME



• A partir de 1970, o processo de dopagem passou a ser via implantação iônica com o seguinte aspecto:







## Balanço de Massa

 ${Fica acumulado} = {entrada} - {saída}$ 

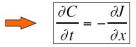
$$J_{x} \longrightarrow J_{x+\Delta x}$$

$$C = \begin{bmatrix} \frac{\#}{cm^{3}} \end{bmatrix}$$

$$C_{t+\Delta t} A \Delta x - C_{t} A \Delta x = J_{x} A \Delta t - J_{x+\Delta x} A \Delta t$$

$$J = \begin{bmatrix} \frac{\#}{cm^{2}s} \end{bmatrix}$$

$$\frac{C_{t+\Delta t} - C_t}{\Delta t} = -\frac{J_{x+\Delta x} - J_x}{\Delta x} \qquad \Longrightarrow \qquad \boxed{\frac{\partial C}{\partial t} = -\frac{\partial J}{\partial x}}$$







## Perfil de difusão para fonte infinita (C(0,t)=Cs)

$$C(x, 0) = 0$$
  $C(0, t) = C_s$   $C(\infty, t) = 0$ 

$$C(x, t) = C_s \operatorname{erfc}\left[\frac{x}{2\sqrt{Dt}}\right]$$
  $\operatorname{erf}(x) \equiv \frac{2}{\sqrt{\pi}} \int_0^x e^{-y^2} dy$   $\operatorname{erfc}(x) \equiv 1 - \operatorname{erf}(x)$   $\operatorname{erf}(0) = 0$ 

Table 1 Error Function Algebra

$$C(x, t) = 0 \quad C(0, t) = C_s \quad C(\infty, t) = 0$$

$$C(x, t) = C_s \text{ erfc} \left(\frac{x}{2\sqrt{Dt}}\right) \qquad \text{erf } (x) \equiv \frac{2}{\sqrt{\pi}} \int_0^x e^{-y^2} dy$$

$$\text{erfc } (x) \equiv 1 - \text{erf}(x)$$

$$\text{erf } (0) = 0$$

$$\text{erf } (\infty) = 1$$

$$\text{erf } (x) \cong \frac{2}{\sqrt{\pi}} x \text{ for } x << 1$$

$$\text{erfc } (x) \simeq \frac{1}{\sqrt{\pi}} \frac{e^{-x^2}}{x} \text{ for } x >> 1$$

$$\frac{d}{dx} \text{ erf } (x) = \frac{2}{\sqrt{\pi}} e^{-x^2}$$

$$\frac{d^2}{dx^2} \text{ erf } (x) = -\frac{4}{\sqrt{\pi}} x e^{-x^2}$$

$$\int_0^x \text{ erfc } (y') dy' = x \text{ erfc}(x) + \frac{1}{\sqrt{\pi}} (1 - e^{-x^2})$$

$$\int_0^\infty \text{ erfc } (x) dx = \frac{1}{\sqrt{\pi}}$$



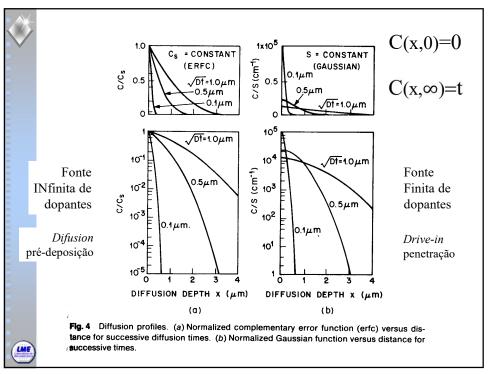


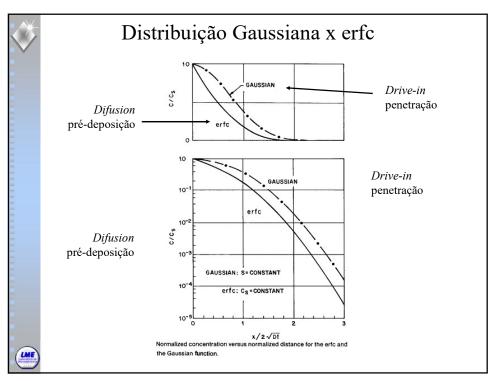
Donors (Electron-increasing Dopants)		Acceptors (Hole-increasing Dopants)	
P← As	Column V	B← Ga	Column III
Sb	elements	In Al	elements

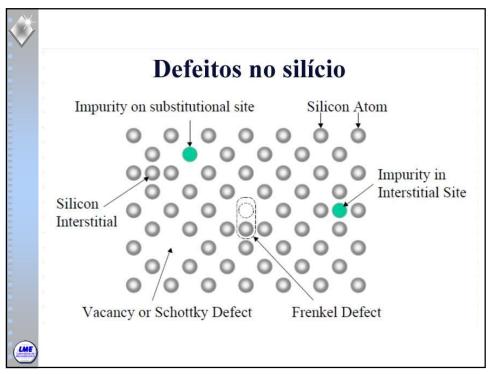
A difusão ocorre porque há um gradiente de concentração de dopante!

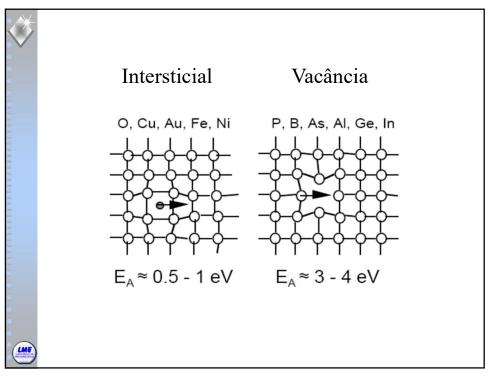


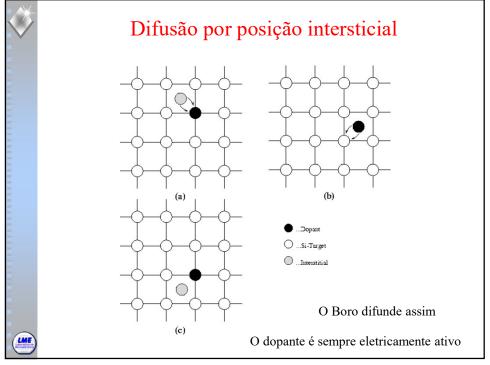
С

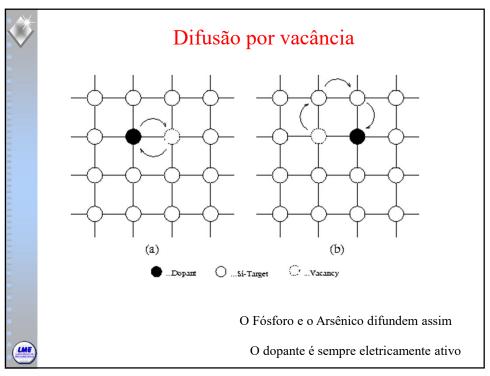


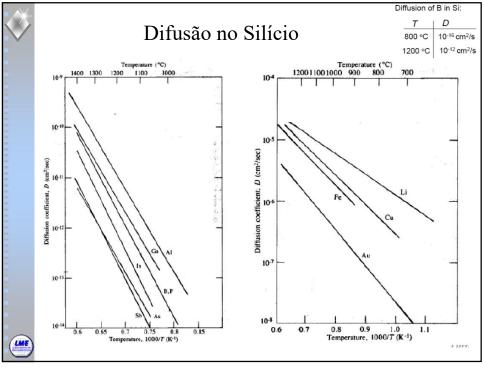


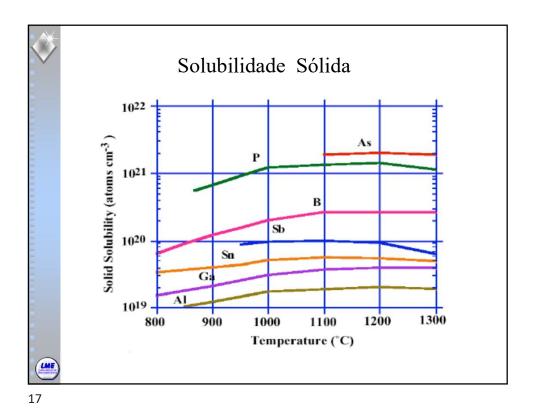












Difusion (Pré-Deposição) Fonte infinita de dopantes C(x,0) = 0IC Si concentration Dopant source  $C(0,t) = C_S$ **BCs** profiles (constantly  $C(\infty,t)=0$ replenished) time Solution:  $C(x,t) = C_S erfc \left[ x / 2 \sqrt{Dt} \right]$ Diffusion length complimentary error function

