



1) a) Problema do Consumidor: $\max_{c_t, \alpha_{t+1}, n_t} \sum_{t=0}^{\infty} \beta^t u(c_t, 1-n_t, g_t)$
 s.t.: $\sum_{t=0}^{\infty} q_t (c_t + \alpha_{t+1} - (1-\delta)\alpha_t) = \sum_{t=0}^{\infty} q_t ((1-\tau_{ur})u_r n_t + (1-\tau_{ar})r_t \alpha_t)$

C.P.O.: $[c_t] \beta^t u_{c_t} = \lambda q_t$ (1)

$[n_t] \beta^t u_{n_t} = \lambda q_t ((1-\tau_{ur})u_r)$ (2)

$[\alpha_{t+1}] \lambda q_{t+1} = \lambda q_{t+1} [(1-\delta) + (1-\tau_{ar})r_t]$ (3)

C.T.: $\lim_{t \rightarrow \infty} \beta^t u_{c_t} \alpha_{t+1} = 0$

Normalizações: $q_0 = 1$

$\stackrel{(1)}{\Rightarrow} \lambda = u_{c_0} \Rightarrow q_t = \beta^t \left(\frac{u_{c_t}}{u_{c_0}} \right)$ (4)

$\stackrel{(4) \cdot (2)}{\Rightarrow} \frac{u_{n_t}}{u_{c_t}} = (1-\tau_{ur})u_r$ (5)

$\stackrel{(4) \cdot (3)}{\Rightarrow} u_{\alpha_{t+1}} = \beta u_{\alpha_{t+1}} [(1-\delta) + (1-\tau_{ar})r_t]$ (6)

b) Problema da Firma: $\max_{\alpha_t, n_t} F(\alpha_t, n_t) - r_t \alpha_t - w_t n_t$

C.P.O.: $[\alpha_t] F_{\alpha_t} = r_t$

$[n_t] F_{n_t} = w_t$

c) O equilíbrio é uma sequência $\{c_t, \alpha_{t+1}, n_t, g_t\}_{t=0}^{\infty}$ tal que:

(i) O problema do consumidor é resolvido, i.e., a utilidade U é maximizada;

(ii) Ho' market clearing: $\begin{cases} n_t^s = n_t^d \\ c_t + \alpha_{t+1} - (1-\delta)\alpha_t + g_t = F(\alpha_t, n_t) \end{cases}$

Dados $\{g_t, w_t, r_t\}_{t=0}^{\infty}$ e α_0

$$d) \text{ Da R.O.: } \sum_{t=0}^{\infty} q_t (c_t + \kappa_{t+1} - (1-\delta)\kappa_t) = \sum_{t=0}^{\infty} q_t [(1-\tau_{nr})u_t n_t + (1-\tau_{ko})r_t \kappa_t]$$

$$\Rightarrow \sum_{t=0}^{\infty} q_t (c_t - (1-\tau_{nr})u_t n_t) = \sum_{t=0}^{\infty} q_t [(1-\tau_{nr})r_t \kappa_t + (1-\delta)\kappa_t - \kappa_{t+1}]$$

$$\Rightarrow \sum_{t=0}^{\infty} q_t (c_t - (1-\tau_{nr})u_t n_t) = q_0 [(1-\tau_{ko})r_0 + (1-\delta)] \kappa_0$$

$$- q_0 \kappa_1 + q_1 [(1-\tau_{ko})r_1 + (1-\delta)] \kappa_1$$

$$- q_1 \kappa_2 + q_2 [(1-\tau_{ko})r_2 + (1-\delta)] \kappa_2$$

$$+ \dots$$

$$+ \lim_{t \rightarrow \infty} q_t \kappa_{t+1} \xrightarrow{\text{c.f.}} 0$$

} Equações de Euler $\Rightarrow 0$

$$\Rightarrow \sum_{t=0}^{\infty} q_t (c_t - (1-\tau_{nr})u_t n_t) = q_0 [(1-\tau_{ko})r_0 + (1-\delta)] \kappa_0$$

(4) $q_t = \beta^t \left(\frac{u_{c_t}}{u_{c_0}} \right)$
(5) $\frac{u_{n_t}}{u_{c_t}} = (1-\tau_{nr})w_t$

$$\Rightarrow \sum_{t=0}^{\infty} \beta^t \frac{u_{c_t}}{u_{c_0}} \left(c_t - \left(\frac{u_{n_t}}{u_{c_t}} \right) n_t \right) = [(1-\tau_{ko})r_0 + (1-\delta)] \kappa_0$$

$$\Rightarrow \sum_{t=0}^{\infty} \beta^t [u_{c_t} c_t - u_{n_t} n_t] = u_{c_0} \kappa_0 [(1-\tau_{ko})r_0 + (1-\delta)]$$

e) Problema de Ramsey: $\max_{c_t, n_t, \kappa_{t+1}, g_t} \sum_{t=0}^{\infty} \beta^t u(c_t, l_t, g_t)$

s.t. $\begin{cases} c_t + \kappa_{t+1} - (1-\delta)\kappa_t + g_t = F(\kappa_t, n_t) \quad \forall t \\ \sum_{t=0}^{\infty} \beta^t [u_{c_t} c_t - u_{n_t} n_t] = u_{c_0} \kappa_0 [(1-\delta) + (1-\tau_{ko})r_0] \end{cases}$

$$\Leftrightarrow \max_{c_t, n_t, \kappa_{t+1}, g_t} \sum_{t=0}^{\infty} \left\{ \beta^t u(c_t, l_t, g_t) - \delta_t [c_t + \kappa_{t+1} - (1-\delta)\kappa_t + g_t - F(\kappa_t, n_t)] + \mu \sum_{t=0}^{\infty} \beta^t [u_{c_t} c_t - u_{n_t} n_t] - \mu u_{c_0} \kappa_0 [(1-\delta) + (1-\tau_{ko})r_0] \right\}$$

$$\Leftrightarrow \max_{c_t, n_t, \kappa_{t+1}, g_t} \sum_{t=0}^{\infty} \beta^t \left\{ [u(c_t, l_t, g_t) + \mu u_{c_t} c_t - \mu u_{n_t} n_t] - \delta_t [c_t + \kappa_{t+1} - (1-\delta)\kappa_t + g_t - F(\kappa_t, n_t)] - \mu u_{c_0} \kappa_0 [(1-\delta) + (1-\tau_{ko})r_0] \right\}$$

$$\Leftrightarrow \max_{c_t, n_t, \kappa_{t+1}, g_t} \sum_{t=0}^{\infty} \beta^t \left\{ W(c_t, l_t, g_t) - \delta_t [c_t + \kappa_{t+1} - (1-\delta)\kappa_t + g_t - F(\kappa_t, n_t)] - \mu u_{c_0} \kappa_0 [(1-\delta) + (1-\tau_{ko})r_0] \right\}$$

$$\begin{aligned} \text{C.P.O. : } & [c_t] W_{ct} = \delta_t \\ & [n_t] W_{nt} = \delta_t F_{nt} \\ & [g_t] W_{gt} = \delta_t \\ & [k_{t+1}] \delta_t = \beta \delta_{t+1} [(1-\delta) + F_{k,t+1}] \end{aligned}$$

$$\Rightarrow \begin{cases} F_{nt} = W_{ct}/W_{nt} \\ W_{gt} = W_{ct} \\ W_{ct} = \beta W_{c,t+1} [(1-\delta) + F_{k,t+1}] \end{cases}$$

$$p) x_t = x_{t+1} = x \quad \forall t \quad \forall x = c, n, k, g, \tau_n, \tau_k, v, r$$

$$\left. \begin{aligned} \text{Do problema de Ramsey: } & L = \beta [(1-\delta) + F_k] \\ \text{Do problema Decentralizado: } & L = \beta [(1-\delta) + (1-\tau_k) F_k] \end{aligned} \right\} \Rightarrow \tau_k = 0$$

$$\begin{aligned} g) W(c_t, l_t, g_t) &= u(c_t, l_t, g_t) + \mu u_{ct} c_t - \mu u_{nt} n_t \\ W(c_t, l_t, g_t) &= \frac{c_t^{1-\beta} - 1}{1-\beta} + v(l_t, g_t) + \mu c_t^{1-\beta} - \mu r_{ct} n_t \end{aligned}$$

$$\Rightarrow W_{ct} = c_t^{-\beta} + \mu (1-\beta) c_t^{-\beta} = c_t^{-\beta} (1 + \mu(1-\beta))$$

$$\begin{aligned} \text{Do Problema de Ramsey: } & c_t^{-\beta} (1 + \mu(1-\beta)) = \beta c_{t+1}^{-\beta} (1 + \mu(1-\beta)) [(1-\delta) + F_{k,t+1}] \\ & c_t^{-\beta} = \beta c_{t+1}^{-\beta} [(1-\delta) + F_{k,t+1}] \end{aligned}$$

$$\begin{aligned} \text{Do Problema Decentralizado: } & c_t^{-\beta} = \beta c_{t+1}^{-\beta} [(1-\delta) + (1-\tau_{k,t+1}) F_{k,t+1}] \end{aligned} \left. \right\} \begin{aligned} & \Rightarrow \tau_{k,t+1} = 0 \quad \forall t \geq 1 \\ & \Rightarrow \tau_{k,t} = 0 \quad \forall t \geq 2 \end{aligned}$$

$$h) \frac{\partial L}{\partial \tau_{k0}} = \mu u_{c0} k_0 r_0 > 0$$

$\begin{matrix} \vee & \vee & \vee & \vee \\ 0 & 0 & 0 & 0 \end{matrix}$
 RI
 Valor
 marginal

Ho' aumento de bem-estar com $\tau_{k0} > 0$. Para um governo limitado s'otimo taxar capital j' acumulados (k₀).

$$2) Y_t = Y_n + \alpha (\bar{\pi}_t + \bar{\pi}_t^e)$$

$$L = (1/2) \{ \lambda (Y_t - Y^*)^2 + (\bar{\pi}_t - \bar{\pi}^*)^2 \}$$

$$Y^* > Y_n, \quad \alpha > 0, \quad \lambda > 0$$

a) Comprometimento com credibilidade:

$$\min_{Y_t, \bar{\pi}_t} (1/2) \{ \lambda (Y_t - Y^*)^2 + (\bar{\pi}_t - \bar{\pi}^*)^2 \}$$

$$\text{s.t. } Y_t = Y_n + \alpha (\bar{\pi}_t - \bar{\pi}_t^e)$$

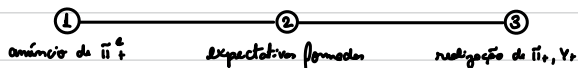
Por comprometimento $\bar{\pi}_t = \bar{\pi}_t^e \quad \forall t$ [governo ancore expectativas e não deriva]

Da restrição: $Y_t = Y_n \quad \forall t$

Dado o formato da função objetivo, não há nível de $\bar{\pi}_t$ que compense a diferença $(Y_n - Y^*)^2$. Logo, $\bar{\pi}_t = \bar{\pi}^* \quad \forall t$.

$$L^c = (1/2) \lambda (Y_n - Y^*)^2$$

b) Não Comprometimento:



$$\min_{Y_t, \bar{\pi}_t} (1/2) \{ \lambda (Y_t - Y^*)^2 + (\bar{\pi}_t - \bar{\pi}^*)^2 \}$$

$$\text{s.t. } Y_t = Y_n + \alpha (\bar{\pi}_t - \bar{\pi}_t^e)$$

$$\min_{\bar{\pi}_t} (1/2) \{ \lambda (Y_n - Y^* + \alpha (\bar{\pi}_t - \bar{\pi}_t^e))^2 + (\bar{\pi}_t - \bar{\pi}^*)^2 \}$$

$$\text{C.P.O.} : [\bar{\pi}_t] \alpha \lambda (Y_n - Y^* + \alpha (\bar{\pi}_t - \bar{\pi}_t^e)) + (\bar{\pi}_t - \bar{\pi}^*) = 0$$

$$\bar{\pi}_t = \frac{\lambda \alpha^2 \bar{\pi}_t^e + \bar{\pi}^* + \lambda \alpha (Y^* - Y_n)}{\lambda + \lambda \alpha^2}$$

$$\text{Público antecipa comportamento ótimo de regulador: } \bar{\pi}_t^e = \frac{\lambda \alpha^2 \bar{\pi}_t^e + \bar{\pi}^* + \lambda \alpha (Y^* - Y_n)}{\lambda + \lambda \alpha^2} \Rightarrow \bar{\pi}_t^e = \bar{\pi}^* + \lambda \alpha (Y^* - Y_n)$$

Por consequência:
$$\bar{r}_t = \frac{\lambda \alpha^2 [\bar{r}^* + \lambda \alpha (Y^* - Y_t)] + \bar{r}^* + \lambda \alpha (Y^* - Y_t)}{1 + \lambda \alpha^2}$$

$$\Rightarrow \bar{r}_t = \bar{r}^* + \lambda \alpha (Y^* - Y_t) \quad \forall t \quad \text{[Expectativa Racional]}$$

$$\Rightarrow Y_t = Y_t \quad \forall t$$

Nota que não há ganho sobre Y_t , mas há perda sobre \bar{r}_t .

$$L^{NC} = \left\{ (1/2) \lambda (1 + \lambda \alpha^2) (Y_t - Y^*)^2 \right\}$$

$$L^{NC} > L^C$$

c) Comprometimento por sempre:
$$W^C = \frac{L^C}{1 - \beta}$$

Devio:
$$W^D = 0$$

↳ Devio Y^*, \bar{r}^* . Vai determinar \bar{r}_t^e para depois decidir (por este momento, no nível)

$$Y_t = Y_t + \alpha (\bar{r}_t - \bar{r}_t^e) \Rightarrow \bar{r}_t^e = \bar{r}^* - \frac{(Y^* - Y_t)}{\alpha}$$

Uma vez que está além as expectativas, devio para $\bar{r}_t = \bar{r}^* \Rightarrow Y_t = Y_t + \alpha (\bar{r}^* - \bar{r}_t^e + \frac{(Y^* - Y_t)}{\alpha}) = Y^*$

Portanto, a partir do próximo período há punição eterna por perda de credibilidade. Logo,
$$W^R = 0 + \left(\frac{\beta}{1 - \beta} \right) L^{NC}$$

Para haver equilíbrio com comprometimento:
$$\frac{L^C}{1 - \beta} \leq \left(\frac{\beta}{1 - \beta} \right) L^{NC} \Leftrightarrow \beta \geq \frac{L^C}{L^{NC}}$$

Como $L^C < L^{NC}$, $\exists \sigma \in [L^C/L^{NC}, 1)$ tal que se $\beta \geq \sigma$, comprometimento eterno é equilíbrio.

$$3) a) \max_{c_t, k_{t+1}} \sum_{t=0}^{\infty} \beta^t \ln c_t$$

$$s.t. \quad c_t + k_{t+1} \leq (1-\tau) r_t k_t + \Pi_t$$

$$\left. \begin{array}{l} \text{C.P.O.: } [c_t] \quad \lambda_t = 1/c_t \\ [k_{t+1}] \quad \lambda_t = \beta \lambda_{t+1} (1-\tau) r_{t+1} \end{array} \right\} \quad 1/c_t = \beta E_t [(1/c_{t+1}) (1-\tau) r_{t+1}]$$

$$\text{C.T.: } \lim_{t \rightarrow \infty} \beta^t \lambda_t k_{t+1} = 0$$

$$b) \max_{k_t, h_t} \Pi_t = A k_t^\alpha h_t^{1-\alpha} - r_t k_t$$

$$\text{C.P.O.: } [k_t] \quad A \alpha (h_t / k_t)^{1-\alpha} = r_t$$

$$\frac{\partial \Pi_t}{\partial h_t} \quad A (1-\alpha) (k_t / h_t)^\alpha > 0 \quad \forall h_t \quad \Rightarrow h_t^* = h^{\max} \quad \forall t$$

c) O eq. competitivo é uma sequência de preços e dotações tais que tanto como dados, resolve o problema dos agentes e há market-clearing.

d) Apesar de haver retornos marginais decrescentes p/ cada insumo de maneira individual, temos retornos constantes de escala quando tratamos os insumos de maneira combinada ($\partial F / \partial (\alpha k_t^\alpha (1-\alpha) h_t^{1-\alpha}) = A > 0$). Essa é o misto de crescimento. O ponto principal é que estes insumos não acumulam. A infraestrutura vem à medida que o capital cresce. Assim, o modelo escapa do comodillo dos retornos marginais decrescentes (AK).

$$e) \text{ Equações de Euler: } 1+g = \beta(1-\tau) r_{t+1} \Rightarrow r_{t+1} = (1+g) / [\beta(1-\tau)] \quad \forall t \quad \left. \begin{array}{l} \\ \text{Regra de } h: \quad h_{t+1} = \tau r_t k_t \Rightarrow (h_{t+1} / k_{t+1}) = \tau r_t / (1+g) \end{array} \right\} \quad \begin{array}{l} (h_{t+1} / k_{t+1}) = \frac{\tau}{\beta(1-\tau)} \quad \forall t \\ \Rightarrow (k_t / h_t) = \beta / \tau - \beta \end{array}$$

$$\text{Demanda de } k_t: \quad r_t = A \alpha (h_t / k_t)^{1-\alpha}$$

$$\Rightarrow \frac{(1+g)}{\beta(1-\tau)} = A \alpha \left(\frac{\tau}{\beta(1-\tau)} \right)^{1-\alpha} \Rightarrow g = A \alpha \beta^\alpha \tau^{1-\alpha} (1-\tau)^\alpha - 1$$

$$p) \quad \frac{\partial g}{\partial \tau} = A \alpha \beta^\alpha \left[(1-\alpha) \left(\frac{1-\tau}{\tau} \right)^\alpha + \alpha \left(\frac{\tau}{1-\tau} \right)^{1-\alpha} \right] = A \alpha \beta^\alpha \left[\frac{(1-\alpha)(1-\tau) + \alpha \tau}{\tau^\alpha (1-\tau)^{1-\alpha}} \right]$$

$$\frac{\partial (k_t / h_t)}{\partial \tau} = -\beta / \tau^2 < 0$$

$$g) \max_{c_t, a_{t+1}, h_{t+1}} \sum_{t=0}^{\infty} \beta^t \ln c_t$$

$$\text{s.t.} \quad c_t + a_{t+1} + h_{t+1} = A a_t^\alpha h_t^{1-\alpha}$$

$$\text{C.P.O.: } [c_t] \quad \lambda_t = \lambda_{t+1}$$

$$[a_{t+1}] \quad \lambda_t = \beta \lambda_{t+1} A \alpha \left(\frac{h_{t+1}}{a_{t+1}} \right)^{1-\alpha}$$

$$[h_{t+1}] \quad \lambda_t = \beta \lambda_{t+1} A (1-\alpha) \left(\frac{a_{t+1}}{h_{t+1}} \right)^\alpha$$

$$\text{C.T.: } \begin{cases} \lim_{t \rightarrow \infty} \beta^t \lambda_t a_{t+1} = 0 \\ \lim_{t \rightarrow \infty} \beta^t \lambda_t h_{t+1} = 0 \end{cases}$$

$$h) \text{ Condensado Euler: } \frac{h_{t+1}}{a_{t+1}} = \frac{(1-\alpha)}{\alpha} \Rightarrow g = \beta A \alpha^\alpha (1-\alpha) - 1$$

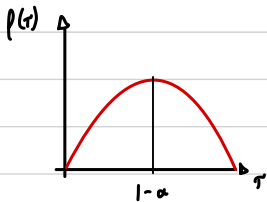
$$i) \text{ Descentralizado: } 1+g = A \alpha \beta^\alpha (1-\tau)^\alpha \tau^{1-\alpha}$$

$$\text{Eficiente: } 1+g = A \beta \alpha^\alpha (1-\alpha)^{1-\alpha}$$

$$(1-\tau)^\alpha \tau^{1-\alpha} = \left(\frac{\beta(1-\alpha)}{\alpha} \right)^{1-\alpha}$$

$$p(\tau) = (1-\tau)^\alpha \tau^{1-\alpha}$$

$$p'(\tau) = -\alpha \left(\frac{\tau}{1-\tau} \right)^{1-\alpha} + (1-\alpha) \left(\frac{\tau}{1-\tau} \right)^{-\alpha} = 0 \quad \Leftrightarrow \tau^* = 1-\alpha$$



$$p(\tau^*) = \alpha^\alpha (1-\alpha)^{1-\alpha}$$

$$p(\tau^{\text{ef}}) = \left(\frac{\beta^\alpha}{\alpha} \right) \alpha^\alpha (1-\alpha)^{1-\alpha}$$

Se $\beta = \alpha \left(\frac{\alpha}{1-\alpha} \right)$, τ^{ef} otimiza consumo.

C.C., τ^{ef} não otimiza consumo.

$$4) \quad g = \frac{\lambda L \alpha}{\delta + \alpha}$$

$$a) \quad \frac{\partial g}{\partial \lambda} = \frac{L \alpha}{\delta + \alpha} > 0 \quad \uparrow \lambda \Rightarrow \text{aumento da eficiência de pesquisa} \Rightarrow \uparrow \text{progresso técnico} \Rightarrow g$$

$$\frac{\partial g}{\partial L} = \frac{\lambda \alpha}{\delta + \alpha} > 0 \quad \uparrow L \Rightarrow \uparrow L_A \Rightarrow \uparrow \text{progresso técnico} \Rightarrow \uparrow g$$

$$\frac{\partial g}{\partial \delta} = -\frac{g}{\delta + \alpha} < 0 \quad \uparrow \delta \Rightarrow \begin{cases} \uparrow \text{avaliação ao risco} \\ \uparrow \text{custos por substituição} \end{cases} \Rightarrow \downarrow K_A \Rightarrow \downarrow g$$

$$\frac{\partial g}{\partial \rho} = -\frac{1}{\delta + \alpha} < 0 \quad \uparrow \text{impaciência} \Rightarrow \downarrow \text{pesquisa} \Rightarrow \downarrow g$$

$$b) \quad \max \int_0^{\infty} e^{-\rho t} \left(\frac{C_t^{1-\alpha} - 1}{1-\alpha} \right) dt$$

$$\text{p.t.} \quad \begin{cases} \dot{K}_t = (L_{Y,t})^\alpha \int_0^{\hat{A}_t} x_t(i)^{1-\alpha} di - C_t \\ \dot{A}_t = \lambda A_t L_{A,t} \\ L_{A,t} + L_{Y,t} = L \end{cases}$$

$$x_t(i) = \bar{x}_t \quad \forall i \Rightarrow \dot{K}_t = (L_{Y,t})^\alpha A_t \bar{x}_t^{1-\alpha} - C_t$$

$$\Rightarrow \dot{K}_t = (L_{Y,t})^\alpha A_t \left(\frac{K_t}{A_t} \right)^{1-\alpha} - C_t$$

$$\Rightarrow \dot{K}_t = (A_t L_{Y,t})^\alpha K_t^{1-\alpha} - C_t \quad \rightarrow \text{nova versão da restrição.}$$

Hamiltoniano:

$$H = e^{-\rho t} \left(\frac{C_t^{1-\alpha} - 1}{1-\alpha} \right) + \mu_t \left[(A_t L_{Y,t})^\alpha K_t^{1-\alpha} - C_t \right] + \delta_t \left[\lambda A_t (L - L_{Y,t}) \right]$$

$$H_C = e^{-\rho t} C_t^{-\alpha} - \mu_t = 0 \Rightarrow \mu_t = e^{-\rho t} C_t^{-\alpha} \quad (0)$$

$$\frac{\partial H}{\partial \mu_t} = -\rho + \delta \mu_t = 0$$

$$\frac{\partial H}{\partial \mu_t} = -\rho + \delta \left(\frac{\dot{\mu}_t}{\mu_t} \right) = 0 \quad (1)$$

$$H_{L_Y} = 0 \Rightarrow \alpha \mu_t A_t^{1-\alpha} \left(\frac{K_t}{L_{Y,t}} \right)^{1-\alpha} = \delta_t \lambda A_t \quad (3)$$

$$H_{A_t} = -\dot{\delta}_t \Rightarrow \frac{-\dot{\delta}_t}{\delta_t} = (1-\alpha) \left(\frac{A_t L_{Y,t}}{K_t} \right)^\alpha \quad (2) \quad H_{A_t} = -\dot{\delta}_t \Rightarrow \alpha \mu_t L_{Y,t}^\alpha \left(\frac{K_t}{A_t} \right)^{1-\alpha} + \delta_t \lambda (L - L_{Y,t}) = -\dot{\delta}_t \quad (4)$$

$$\text{C.T.A.:} \quad \begin{cases} \lim_{t \rightarrow \infty} \mu_t A_t = 0 & (5) \\ \lim_{t \rightarrow \infty} \delta_t A_t = 0 & (6) \end{cases}$$

$$c) (1) + (2) \Rightarrow \frac{\dot{C}_t}{C_t} = \left(\frac{1-\alpha}{\delta}\right) \left(\frac{A_t L_{vt}}{K_t}\right) - \rho \quad (7)$$

$$(3) \Rightarrow \frac{\mu_t}{\delta_t} = \left(\frac{\lambda}{\alpha}\right) \left(\frac{A_t L_{vt}}{K_t}\right)^{1-\alpha} \quad (8)$$

$$(8) \text{ em } (4) \Rightarrow -\frac{\dot{\delta}_t}{\delta_t} = \left(\frac{A_t L_{vt}}{K_t}\right)^{1-\alpha} \left(\frac{\lambda}{\alpha}\right) \left(\frac{K_t}{A_t}\right)^{\alpha} + \lambda(L - L_{vt})$$

$$\Rightarrow -\frac{\dot{\delta}_t}{\delta_t} = \lambda L \Rightarrow \delta_t = e^{-\lambda L t} \quad (9)$$

$$(9) \text{ em } (8) \Rightarrow \mu_t = \left(\frac{\lambda}{\alpha}\right) \left(\frac{A_t L_{vt}}{K_t}\right)^{1-\alpha} e^{-\lambda L t} \left\{ \left(\frac{\lambda}{\alpha}\right) \left(\frac{A_t L_{vt}}{K_t}\right)^{1-\alpha} = e^{-(\rho-\lambda L)t} C_t^{-\alpha} \Rightarrow \right.$$

$$(6) \Rightarrow \mu_t = e^{-\rho t} C_t^{-\alpha}$$

$$\frac{\partial}{\partial t} \left(\ln(\lambda/\alpha) + (1-\alpha) [\ln A_t + \ln L_{vt} - \ln K_t] - (\rho - \lambda L)t - \delta \ln C_t \right)$$

$$(1-\alpha) \left[\frac{\dot{A}_t}{A_t} + \frac{\dot{L}_{vt}}{L_{vt}} - \frac{\dot{K}_t}{K_t} \right] - (\rho - \lambda L) - \delta \frac{\dot{C}_t}{C_t}$$

$$L_{vt} = L_v \forall t \Rightarrow \dot{L}_{vt} = 0 \forall t \Rightarrow (1-\alpha) [\delta^* + 0 - \delta^*] = -(\rho - \lambda L) - \delta \delta^* \Rightarrow \delta^* = \frac{\lambda L - \rho}{\delta}$$

$$d) \delta = \frac{\lambda L \alpha - \rho}{\delta + \alpha} = \frac{\lambda L - \rho/\alpha}{1 + \delta/\alpha}$$

$$\delta^* = \frac{\lambda L - \rho}{\delta}$$

$$\delta^* - \delta = \frac{(\delta + \alpha)(\lambda L - \rho) - \delta(\lambda L \alpha - \rho)}{(\delta + \alpha)}$$

$$= \frac{\lambda L \delta - \rho \delta + \lambda L \alpha - \alpha \rho - \lambda L \alpha \delta + \delta \rho}{(\delta + \alpha)}$$

$$= \frac{\lambda L \delta (1-\alpha) + \alpha(\lambda L - \rho)}{(\delta + \alpha)} > 0$$

$$\Rightarrow \delta^* > \delta$$

Isso ocorre pois g está associado à economia desentralizada sem concorrência perfeita no mercado de bom intermediário. (Padrão de mercado).

5) A cenoura p. 465, seção 14.1.4