



4302212 – Física IV

## Ondas Eletromagnéticas – III

– Soluções independentes:

$$\frac{\partial E_y}{\partial z} = \frac{\partial B_x}{\partial t}$$

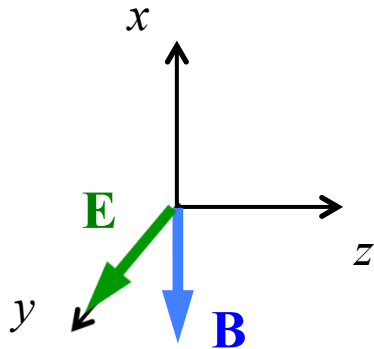
$$\frac{\partial B_x}{\partial z} = \frac{1}{c^2} \frac{\partial E_y}{\partial t}$$

$$\frac{\partial B_y}{\partial z} = -\frac{1}{c^2} \frac{\partial E_x}{\partial t}$$

$$\frac{\partial E_x}{\partial z} = -\frac{\partial B_y}{\partial t}$$

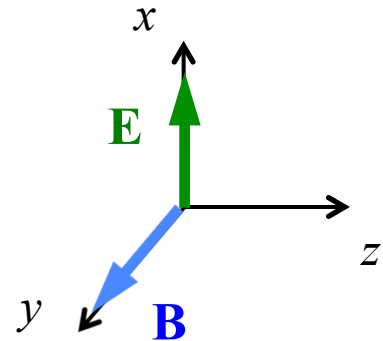
$$\mathbf{E} = E_y(z - ct) \hat{y}$$

$$\mathbf{B} = \frac{1}{c} \hat{z} \times \mathbf{E}$$



$$\mathbf{E} = E_x(z - ct) \hat{x}$$

$$\mathbf{B} = \frac{1}{c} \hat{z} \times \mathbf{E}$$



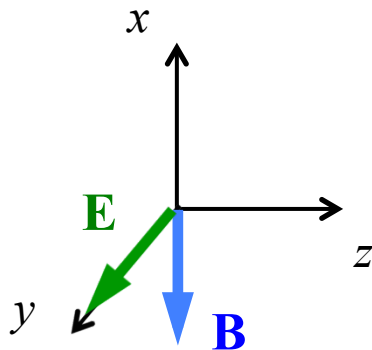
– **Polarização linear:** vetor  $\mathbf{E}(z,t)$  permanece no mesmo plano

– **Direção de Polarização:**  $\hat{\epsilon} = \hat{\mathbf{E}}$

– Diferentes polarizações lineares podem ser obtidas dos casos particulares discutidos:

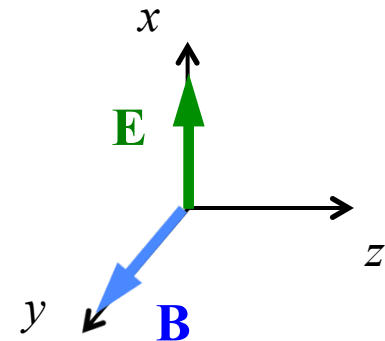
$$\hat{\epsilon} = \hat{y}$$

$$\mathbf{E} = E_y(z - ct) \hat{y}$$



$$\hat{\epsilon} = \hat{x}$$

$$\mathbf{E} = E_x(z - ct) \hat{x}$$



$$\mathbf{B} = \frac{1}{c} \hat{z} \times \mathbf{E}$$

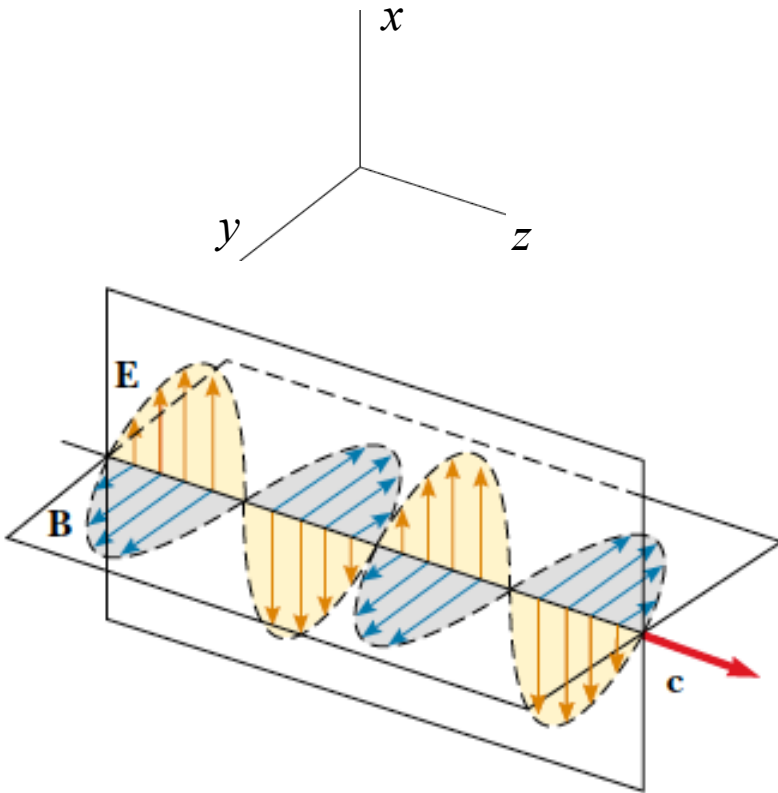
# Ondas EM Monocromáticas

$$E_x(z, t) = E_{\max} \cos[k(z - ct) + \phi] = E_{\max} \cos(kz - \omega t + \phi)$$

$$\omega = kc$$

$$B_y = \frac{1}{c} E_{\max} \cos(kz - \omega t + \phi)$$

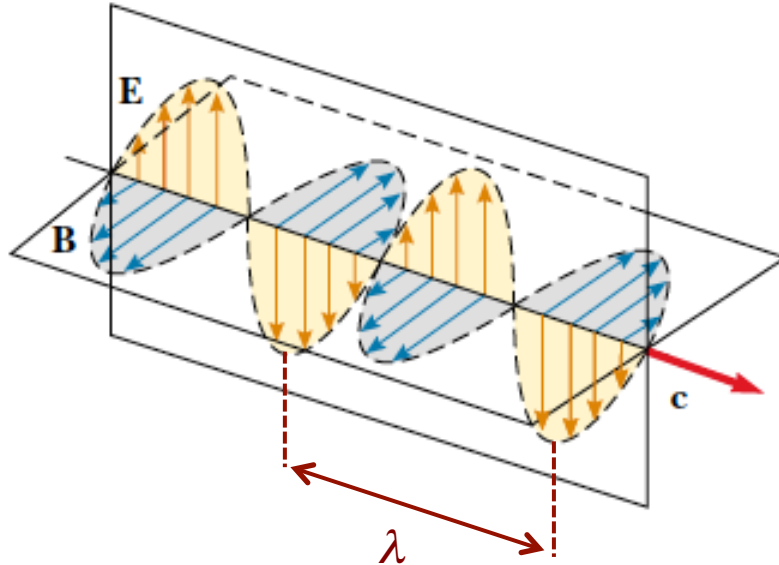
$$= B_{\max} \cos(kz - \omega t + \phi)$$



– Periodicidade espacial:

$$\mathbf{E} = E_{\max} \cos(kz - \omega t + \phi) \hat{\mathbf{x}}$$

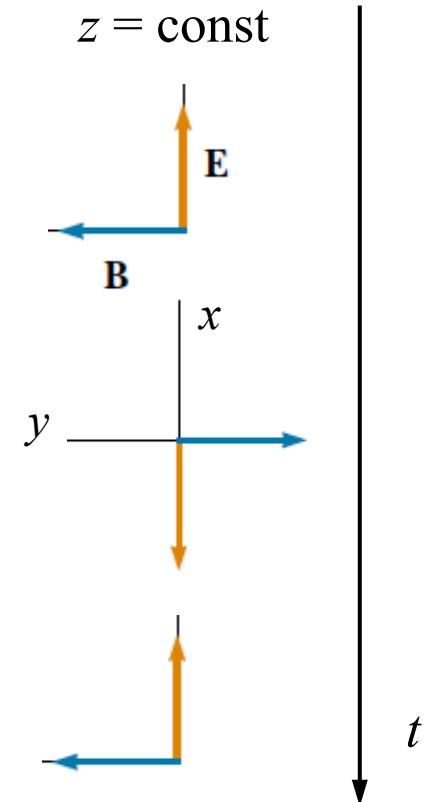
$$\lambda = \frac{2\pi}{k}$$



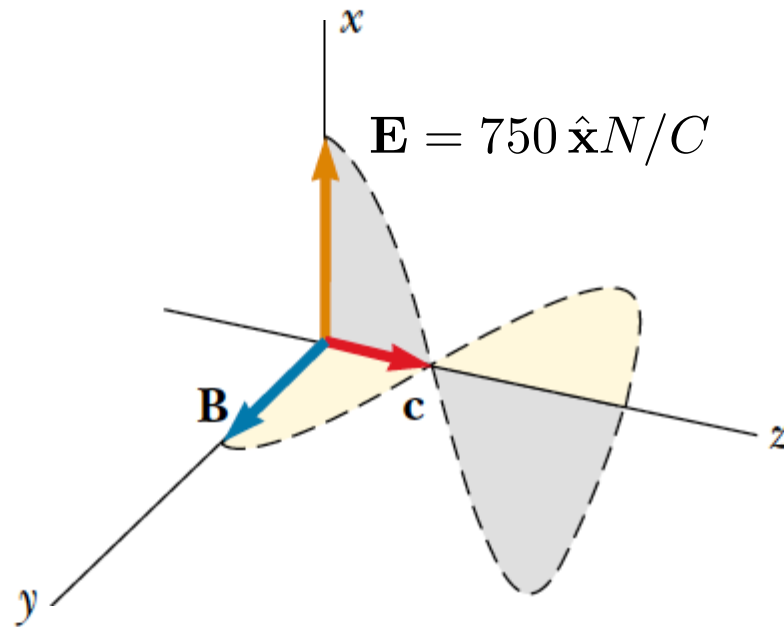
– Periodicidade temporal:

$$\mathbf{E} = E_{\max} \cos(kz - \omega t + \phi) \hat{\mathbf{x}}$$

$$T = \frac{2\pi}{\omega}$$



**Exercício:** Uma onda EM monocromática tem frequência de 40.0 MHz. (a) Determine seu período e comprimento de onda. (b) Em um dado instante e uma dada posição, o campo elétrico tem magnitude de 750 N/C ao longo da direção  $x$ . Determine a amplitude e direção do campo magnético nas mesmas condições.



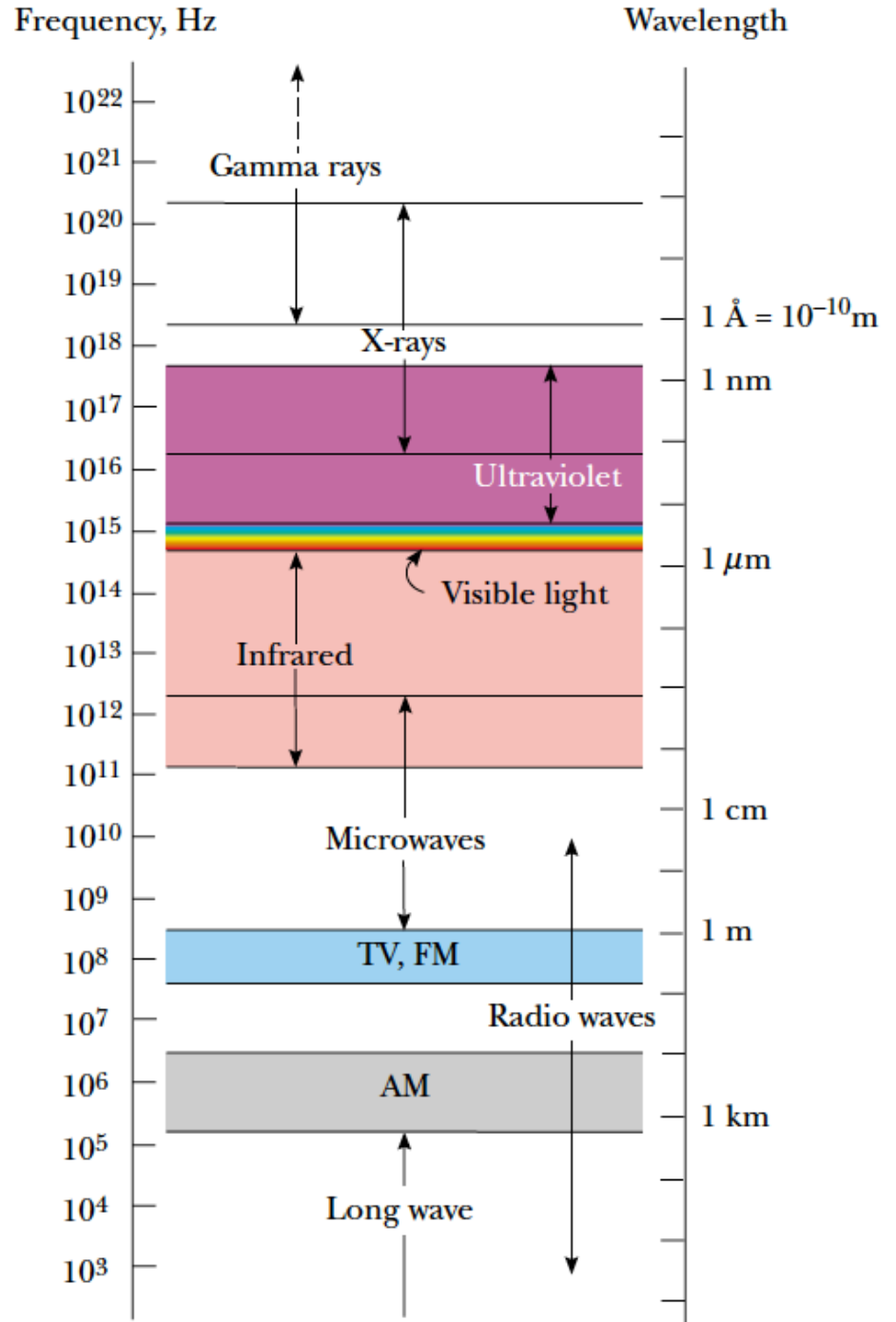
$$\lambda = \frac{c}{f} = \frac{3.00 \times 10^8 \text{ m/s}}{4.00 \times 10^7 \text{ s}^{-1}} = 7.50 \text{ m}$$

$$T = \frac{1}{f} = \frac{1}{4.00 \times 10^7 \text{ s}^{-1}} = 2.50 \times 10^{-8} \text{ s}$$

$$B_{\text{max}} = \frac{E_{\text{max}}}{c} = \frac{750 \text{ N/C}}{3.00 \times 10^8 \text{ m/s}} = 2.50 \times 10^{-6} \text{ T}$$

$$\hat{\mathbf{B}} = \hat{\mathbf{z}} \times \hat{\mathbf{E}}$$

# Espectro das Ondas EM



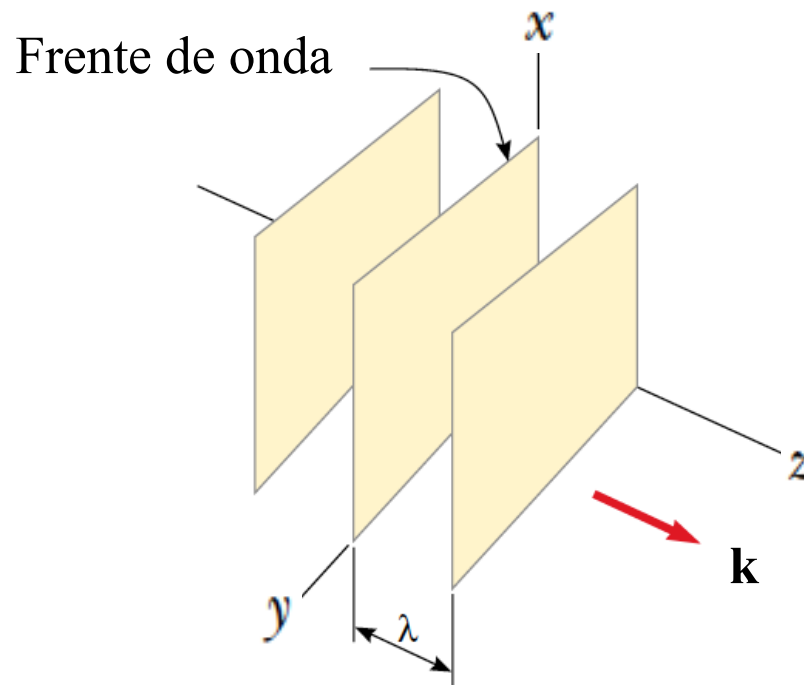


# Ondas EM Planas

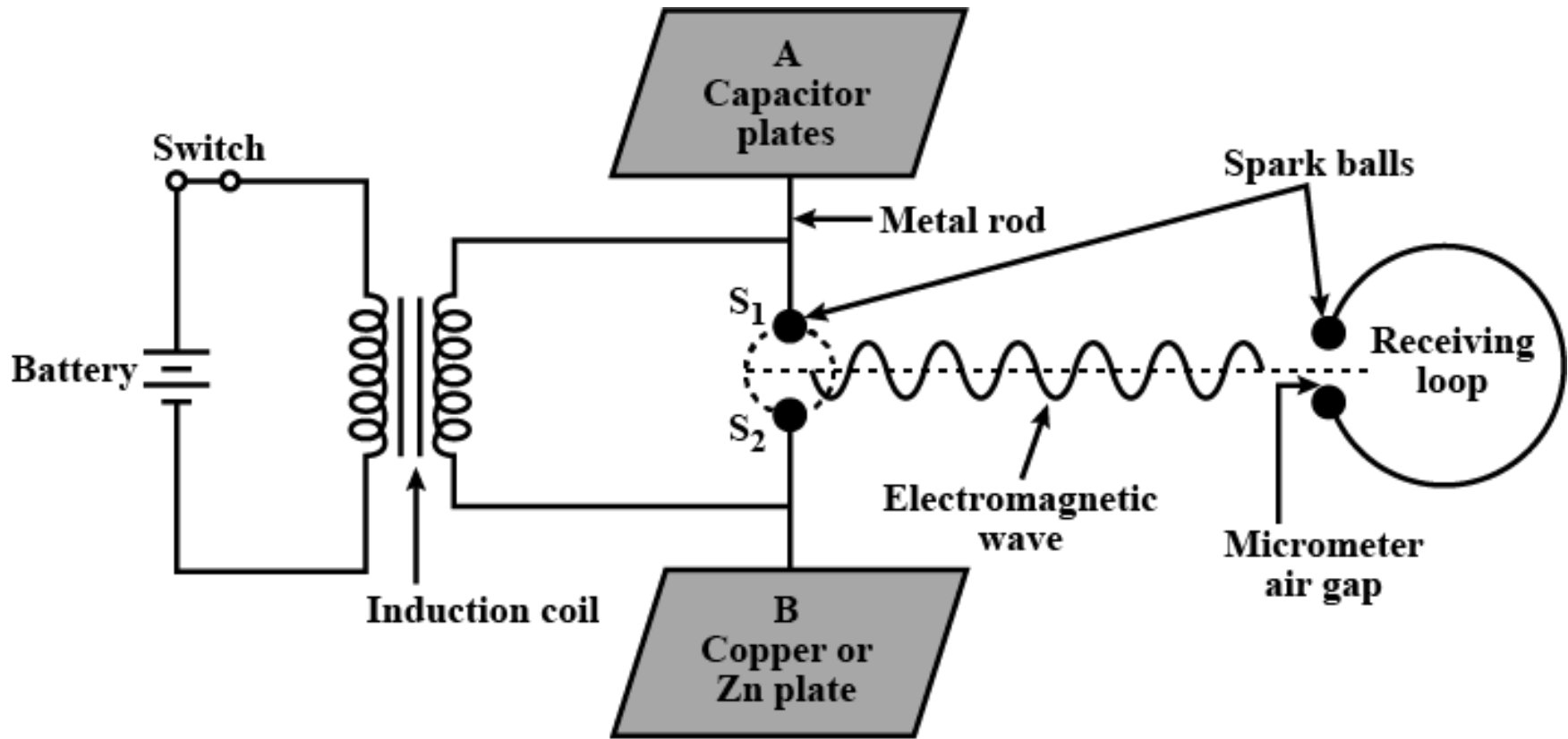
- As soluções discutidas constituem ondas EM linearmente polarizadas, monocromáticas e **planas**:

$$\mathbf{k} = k\hat{\mathbf{z}}$$

$$\mathbf{E} = E_{\max} \cos(\mathbf{k} \cdot \mathbf{r} - \omega t + \phi) \hat{\mathbf{x}}$$



# Experimento de Hertz (1887)

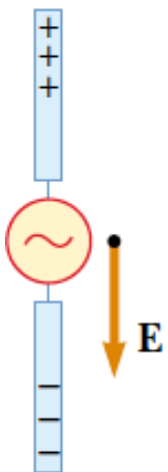
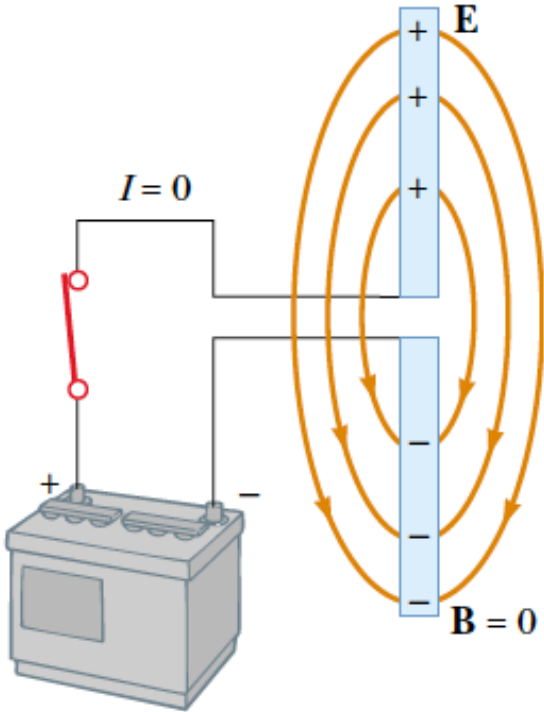


**Fig : Sketch of the apparatus used by Hertz for producing and detecting radiowaves**

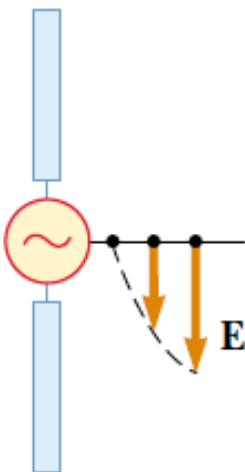
imagem: <https://www.toppr.com/ask/question/explain-the-hertzs-experiment-of-related-to-electromagnetic-wave/>

vídeo: <https://www.youtube.com/watch?v=9gDFll6Ge7g&t=173s>

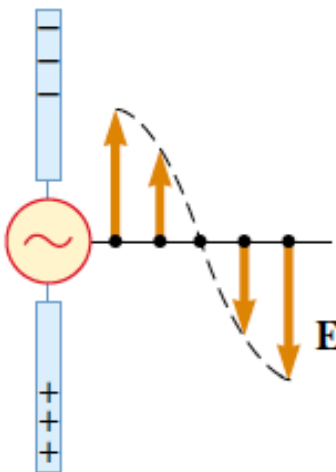
# Radiação de Dipolo



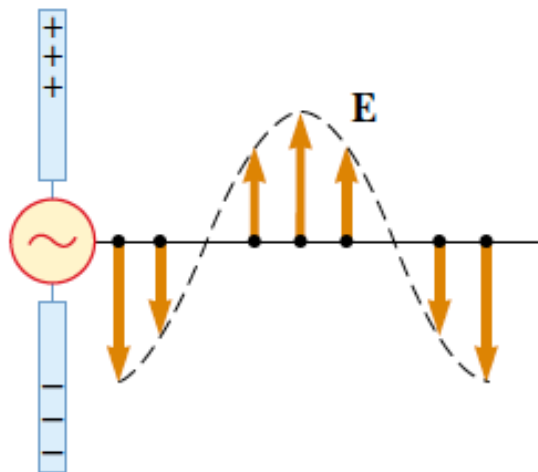
(a)  $t = 0$



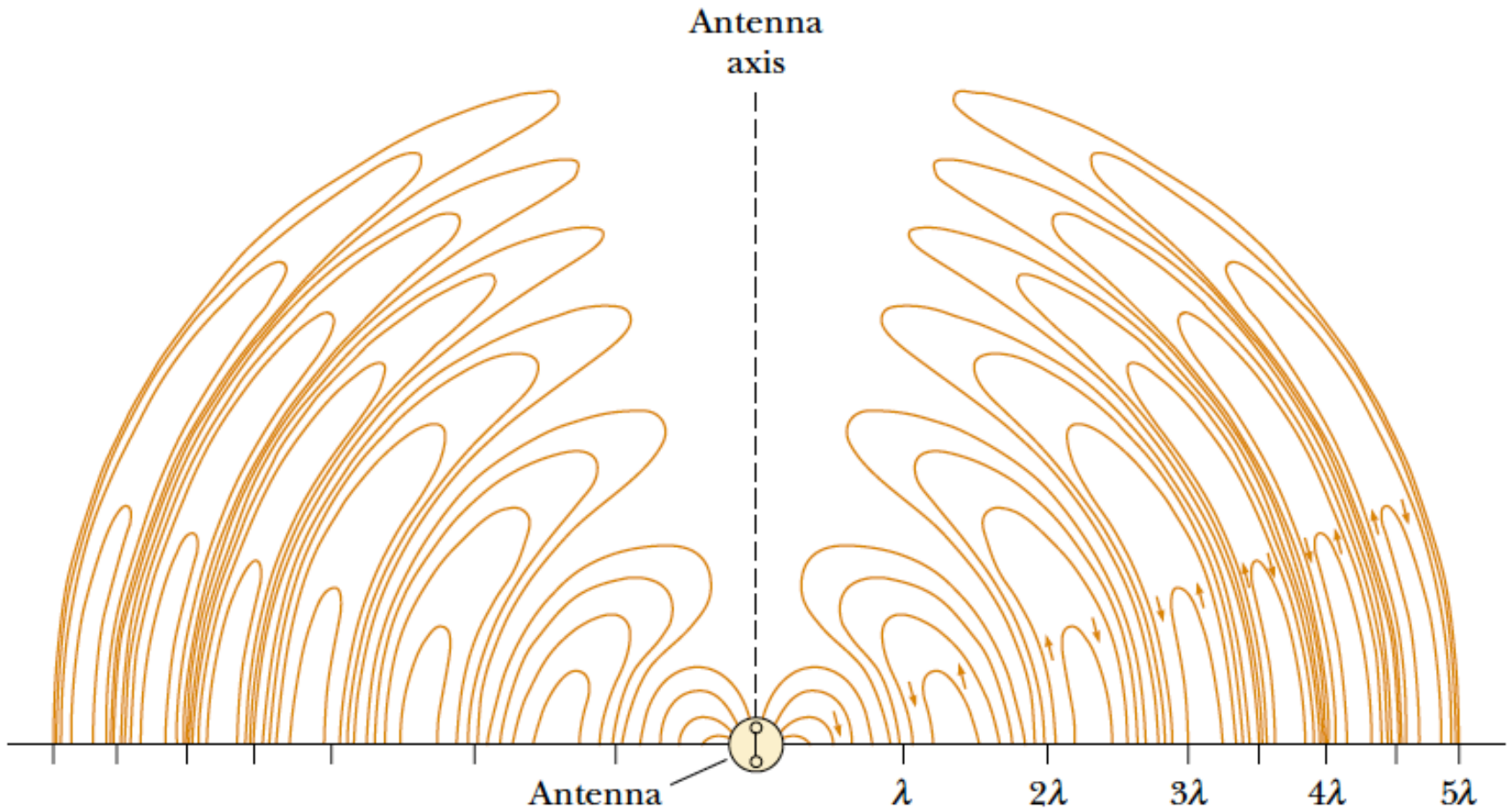
(b)  $t = \frac{T}{4}$



(c)  $t = \frac{T}{2}$



(d)  $t = T$



vídeo: [https://www.youtube.com/results?search\\_query=dipole+radiation+kink+generation](https://www.youtube.com/results?search_query=dipole+radiation+kink+generation)