

Exercício 3 - Componente eletrônico detalhado

Importando as bibliotecas

```
from sympy import *  
import numpy as np  
from scipy.optimize import fsolve  
from numpy.linalg import solve  
  
init_printing(pretty_print=True)
```

Inserindo os dados do problema

```
Tar = 21  
Tp = 40  
kco = 350  
kce = 10  
kv = 8  
kaz = 0.03  
ksi = 146  
Lperna = 15/1000  
Lpl = 30/100  
Dperna = 1/1000  
Q = 2  
h = 80  
Nperna = 8
```

Dimensões do problema

```
m1 = 6.075/100  
m2 = 3.4/100
```

$$m_3 = 0.8/100$$

$$m_4 = 0.2/100$$

$$m_5 = 0.8/100$$

$$m_6 = 0.8/100$$

$$m_{chip} = 1.895/100$$

Definição das áreas

$$A_1 = m_1 * m_{chip} / 2$$

$$A_2 = m_2 * m_{chip} / 2$$

$$A_3 = m_3 * m_{chip} / 2$$

$$A_4 = m_4 * m_{chip} / 2$$

$$A_5 = m_5 * m_{chip} / 2$$

$$A_6 = m_6 * m_{chip} / 2$$

$$A_{perna} = (3.14 * D_{perna}^2) / 4$$

$$A_s = A_p = (m_1 + m_2) * m_{chip} / 2$$

Definição das distâncias

$$L_{12} = L_{21} = (m_1/2) + (m_2/2)$$

$$L_{34} = L_{43} = L_{56} = L_{65} = L_{78} = L_{87} = L_{12}$$

$$L_{13} = L_{31} = L_{24} = L_{42} = (m_3/2) + (m_4/2)$$

$$L_{35} = L_{53} = L_{46} = L_{64} = (m_4/2) + (m_5/2)$$

$$L_{57} = L_{75} = L_{68} = L_{86} = (m_5/2) + (m_6/2)$$

$$L_{1j} = L_{2j} = m_3/2$$

$$L_{3j} = L_{4j} = m_4/2$$

$$L_{5j} = L_{6j} = m_5/2$$

$$L_{7j} = L_{8j} = m_6/2$$

$$L_{3i} = L_{5i} = m_1/2$$

$$L_{4i} = L_{6i} = m_2/2$$

$$L_{1s} = L_{2s} = L_{1j}$$

$$L_{7p} = L_{8p} = L_{7j}$$

Definição das condutâncias

$$G_{12} = G_{21} = k_{ce} \cdot A_3 / L_{12}$$

$$G_{1j} = k_{ce} \cdot A_1 / L_{1j}$$

$$G_{3j} = k_v \cdot A_1 / L_{3j}$$

$$G_{13} = G_{31} = (G_{1j} \cdot G_{3j}) / (G_{1j} + G_{3j})$$

$$G_{2j} = k_{ce} \cdot A_2 / L_{2j}$$

$$G_{4j} = k_{az} \cdot A_2 / L_{4j}$$

$$G_{24} = G_{42} = (G_{2j} \cdot G_{4j}) / (G_{2j} + G_{4j})$$

$$G_{3i} = k_v \cdot A_4 / L_{3i}$$

$$G_{4i} = k_{az} \cdot A_4 / L_{4i}$$

$$G_{34} = G_{43} = (G_{3i} \cdot G_{4i}) / (G_{3i} + G_{4i})$$

$$G_{5i} = k_v \cdot A_5 / L_{5i}$$

$$G_{6i} = k_{si} \cdot A_5 / L_{6i}$$

$$G_{56} = G_{65} = (G_{5i} \cdot G_{6i}) / (G_{5i} + G_{6i})$$

$$G_{35} = G_{53} = k_v \cdot A_1 / L_{35}$$

$$G_{4j} = k_{az} \cdot A_2 / L_{4j}$$

$$G_{6j} = k_{si} \cdot A_2 / L_{6j}$$

$$G_{46} = G_{64} = (G_{4j} \cdot G_{6j}) / (G_{4j} + G_{6j})$$

$$G_{5j} = k_v \cdot A_1 / L_{5j}$$

$$G_{7j} = k_{ce} \cdot A_1 / L_{7j}$$

$$G_{57} = G_{75} = (G_{5j} \cdot G_{7j}) / (G_{5j} + G_{7j})$$

$$G_{78} = G_{87} = k_{ce} \cdot A_6 / L_{78}$$

$$G_{8j} = k_{ce} \cdot A_2 / L_{8j}$$

$$G_{68} = G_{86} = (G_{6j} \cdot G_{8j}) / (G_{6j} + G_{8j})$$

$$G_{7p} = k_{ce} \cdot A_1 / L_{7p}$$

$$G_{8p} = k_{ce} \cdot A_2 / L_{8p}$$

$$G_{6p} = k_{co} \cdot A_{perna} / (4 \cdot L_{perna})$$

$$G_{1s} = k_{ce} \cdot A_1 / L_{1s}$$

$$G_{2s} = k_{ce} \cdot A_2 / L_{2s}$$

$$G_{sar} = h \cdot A_s$$

Equações de energia para regime permanente (escrevendo na forma de Eq(), simbólica)

$$\text{nos} = \text{Eq}(G_{1s}*(T_1-T_s) + G_{2s}*(T_2-T_s) + G_{sar}*(T_{ar}-T_s),0)$$

$$\text{no1} = \text{Eq}(G_{12}*(T_2-T_1) + G_{13}*(T_3-T_1) + G_{1s}*(T_s-T_1),0)$$

$$\text{no2} = \text{Eq}(G_{21}*(T_1-T_2) + G_{24}*(T_4-T_2) + G_{2s}*(T_s-T_2),0)$$

$$\text{no3} = \text{Eq}(G_{31}*(T_1-T_3) + G_{35}*(T_5-T_3) + G_{34}*(T_4-T_3),0)$$

$$\text{no4} = \text{Eq}(G_{42}*(T_2-T_4) + G_{43}*(T_3-T_4) + G_{46}*(T_6-T_4),0)$$

$$\text{no5} = \text{Eq}(G_{53}*(T_3-T_5) + G_{57}*(T_7-T_5) + G_{56}*(T_6-T_5),0)$$

$$\text{no6} = \text{Eq}(G_{64}*(T_4-T_6) + G_{65}*(T_5-T_6) + G_{68}*(T_8-T_6) + G_{6p}*(T_p-T_6) + Q/4,0)$$

$$\text{no7} = \text{Eq}(G_{75}*(T_5-T_7) + G_{78}*(T_8-T_7) + G_{7p}*(T_p-T_7),0)$$

$$\text{no8} = \text{Eq}(G_{86}*(T_6-T_8) + G_{87}*(T_7-T_8) + G_{8p}*(T_p-T_8),0)$$

Verificando como ficaram as equações

nos

no1

no2

no3

no4

no5

no6

no7

no8

Resolvendo o sistema de equações

```
def Temp1(z):
```

```
    T1 = z[0]
```

```
    T2 = z[1]
```

```
    T3 = z[2]
```

```
    T4 = z[3]
```

```
    T5 = z[4]
```

```
    T6 = z[5]
```

```
    T7 = z[6]
```

```
    T8 = z[7]
```

```
    Ts = z[8]
```

```
    F = np.empty((9))
```

```
    F[0] = G12*(T2-T1) + G13*(T3-T1) + G1s*(Ts-T1)
```

```
    F[1] = G21*(T1-T2) + G24*(T4-T2) + G2s*(Ts-T2)
```

```
    F[2] = G31*(T1-T3) + G35*(T5-T3) + G34*(T4-T3)
```

```
    F[3] = G42*(T2-T4) + G43*(T3-T4) + G46*(T6-T4)
```

```
    F[4] = G53*(T3-T5) + G57*(T7-T5) + G56*(T6-T5)
```

```
    F[5] = G64*(T4-T6) + G65*(T5-T6) + G68*(T8-T6) + G6p*(Tp-T6) + Q/4
```

```
    F[6] = G75*(T5-T7) + G78*(T8-T7) + G7p*(Tp-T7)
```

```
    F[7] = G86*(T6-T8) + G87*(T7-T8) + G8p*(Tp-T8)
```

```
    F[8] = G1s*(T1-Ts) + G2s*(T2-Ts) + Gsar*(Tar-Ts)
```

```
    return F
```

```
z0 = np.array([1,1,1,1,1,1,1,1,1])
```

```
z = fsolve(Temp1,z0)
```

Imprimindo os resultados

```
print('T1 =', z[0], 'T2=', z[1], 'T3=', z[2], 'T4=', z[3], 'T5=', z[4], 'T6=',  
z[5], 'T7=', z[6], 'T8=', z[7], 'Ts=', z[8])
```