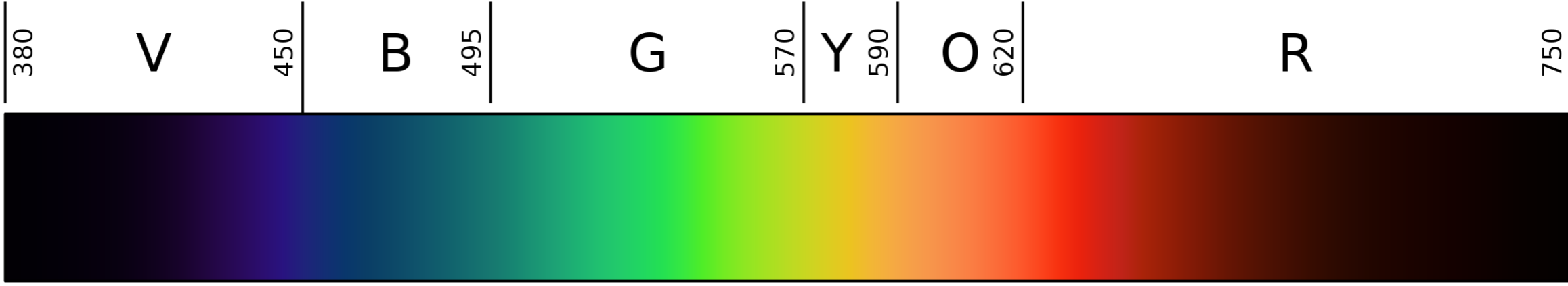


# Física IV

19 outubro 2020  
Ótica geométrica



1690

Huygens

1704

Newton

1802

Young

1864

Maxwell

1922

Compton

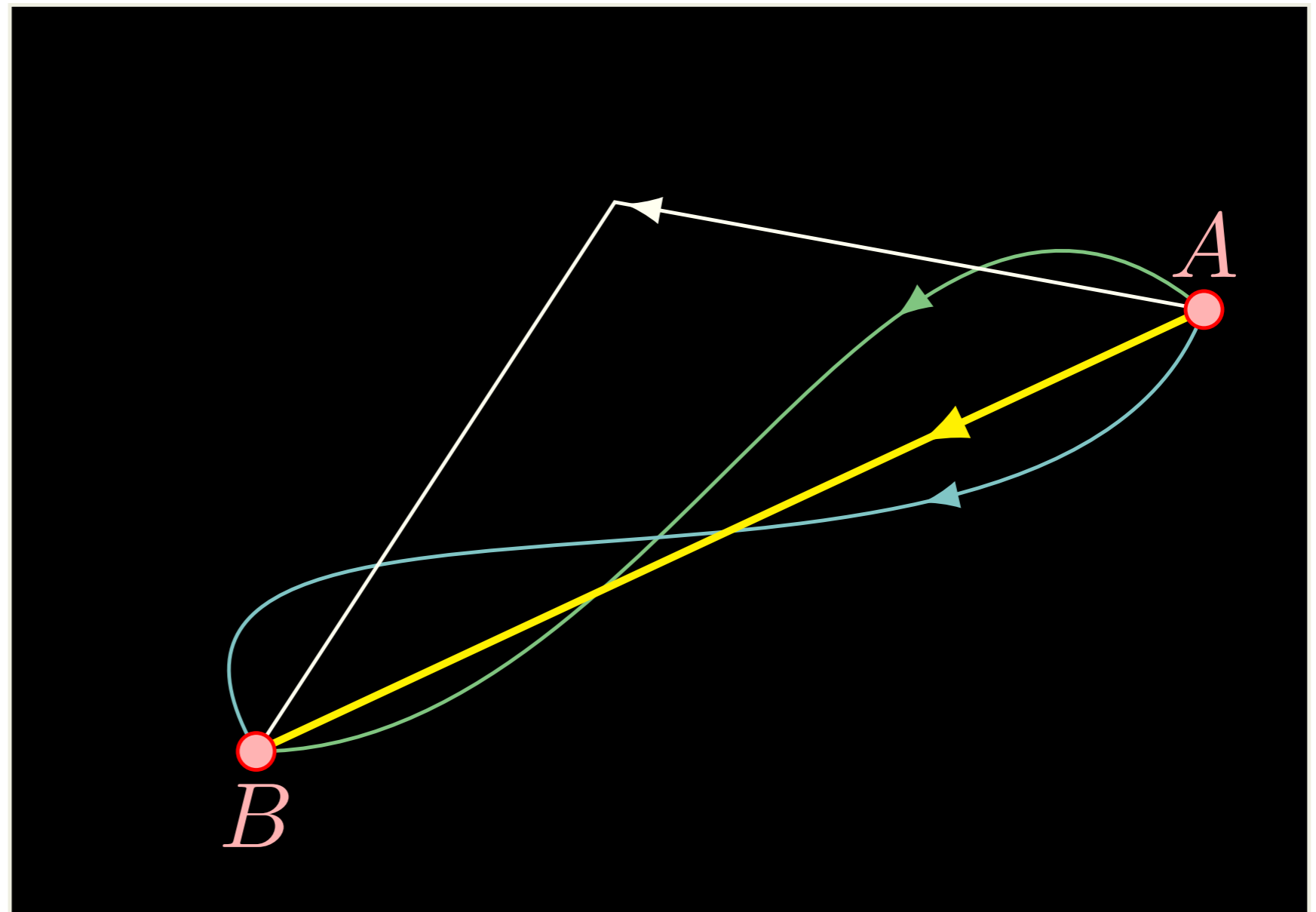
1925

Heisenberg

Luz



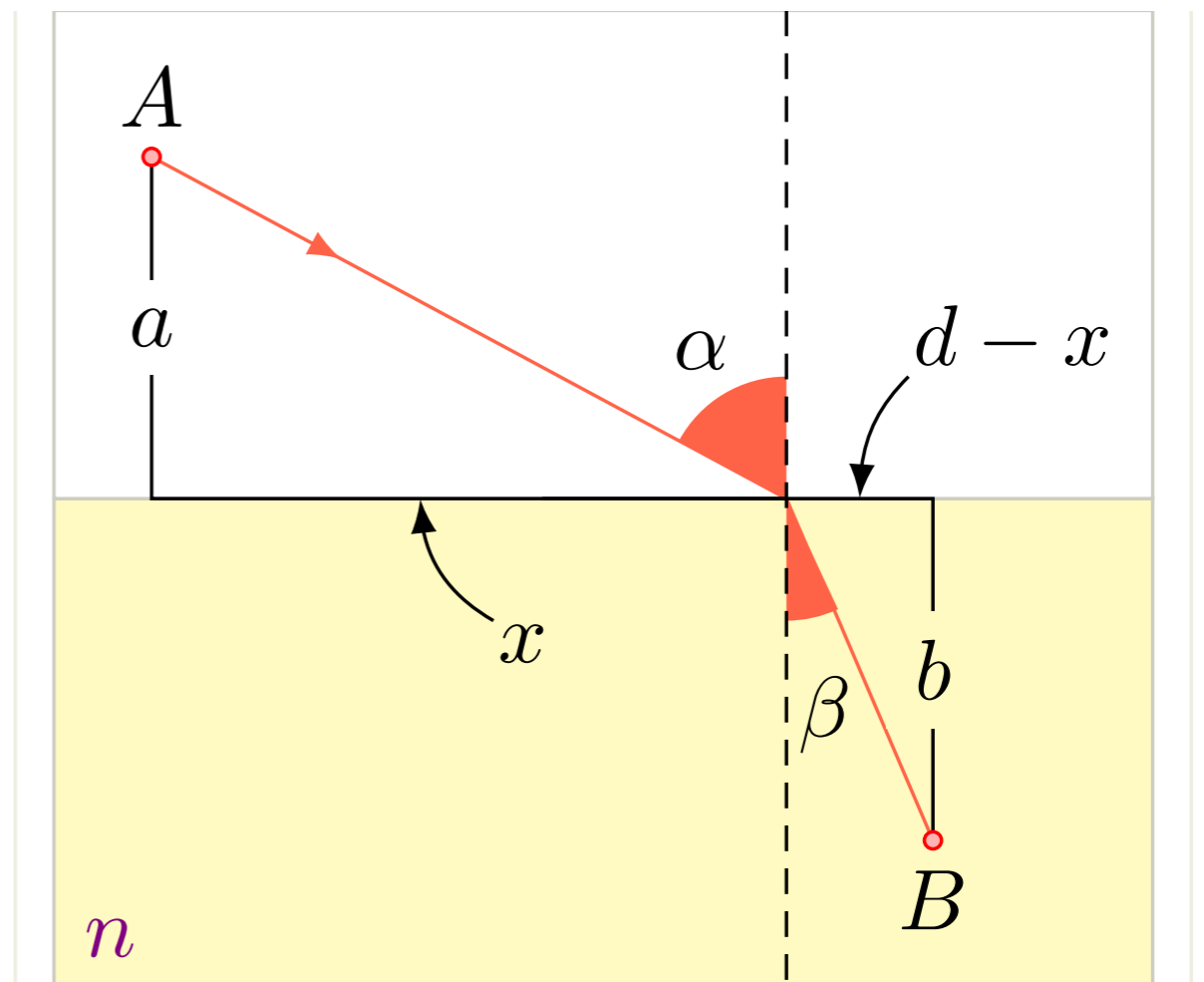
# Princípio de Fermat



Minimiza o tempo

# Princípio de Fermat

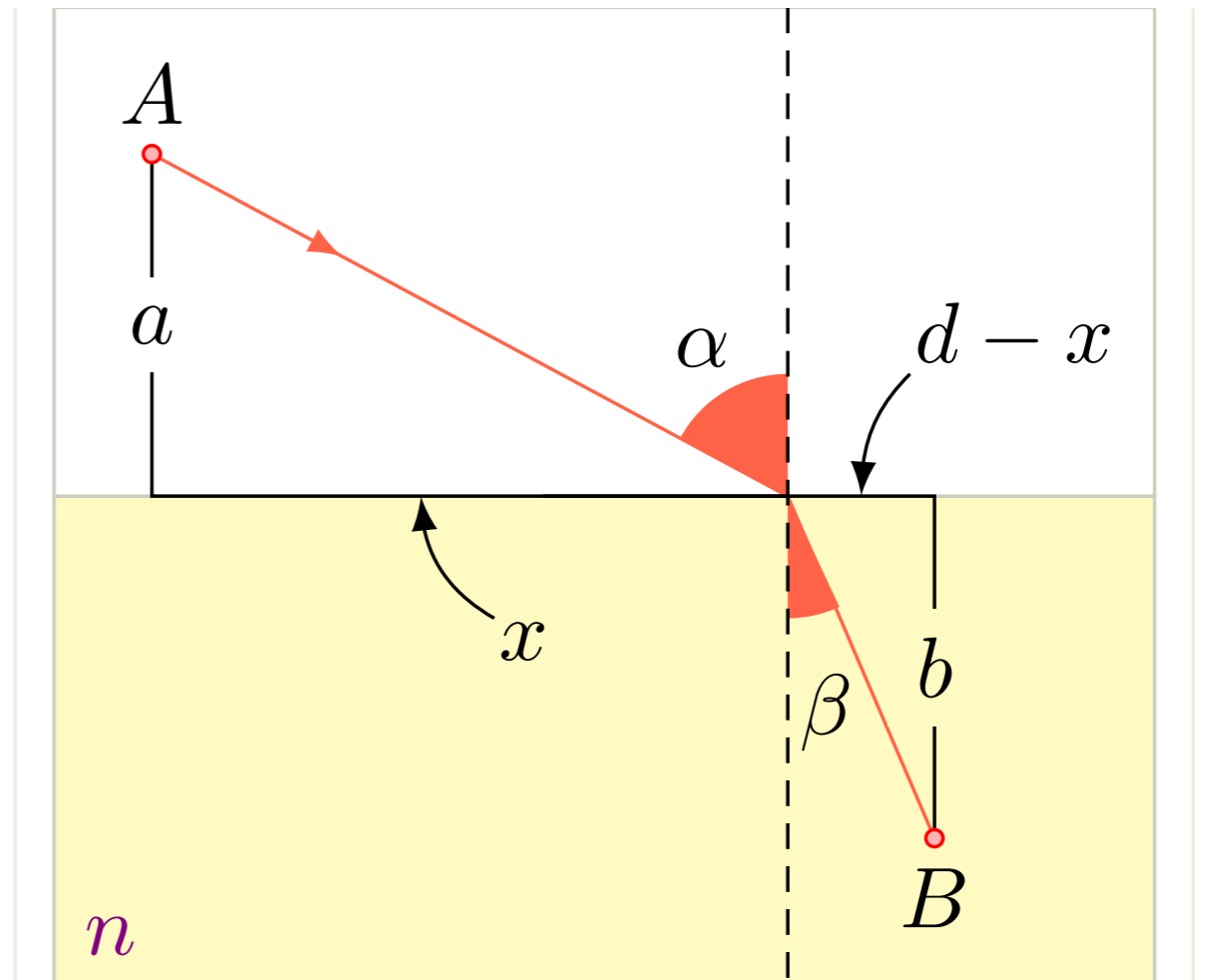
## Refração



# Princípio de Fermat

## Refração

$$\Delta t_A = \frac{\sqrt{a^2 + x^2}}{c}$$

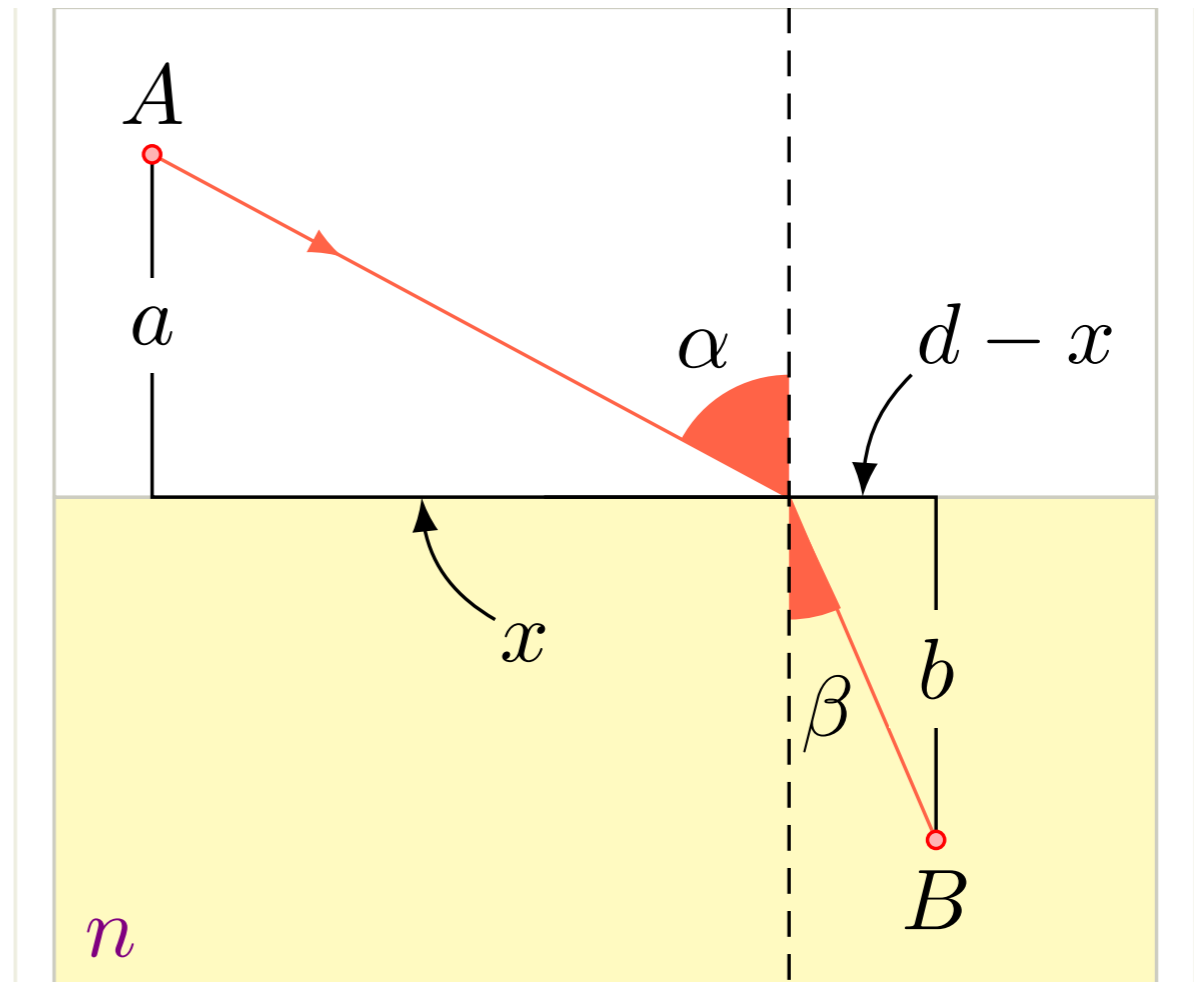


# Princípio de Fermat

## Refração

$$\Delta t_A = \frac{\sqrt{a^2 + x^2}}{c}$$

$$\Delta t_B = \frac{n\sqrt{b^2 + (d-x)^2}}{c}$$



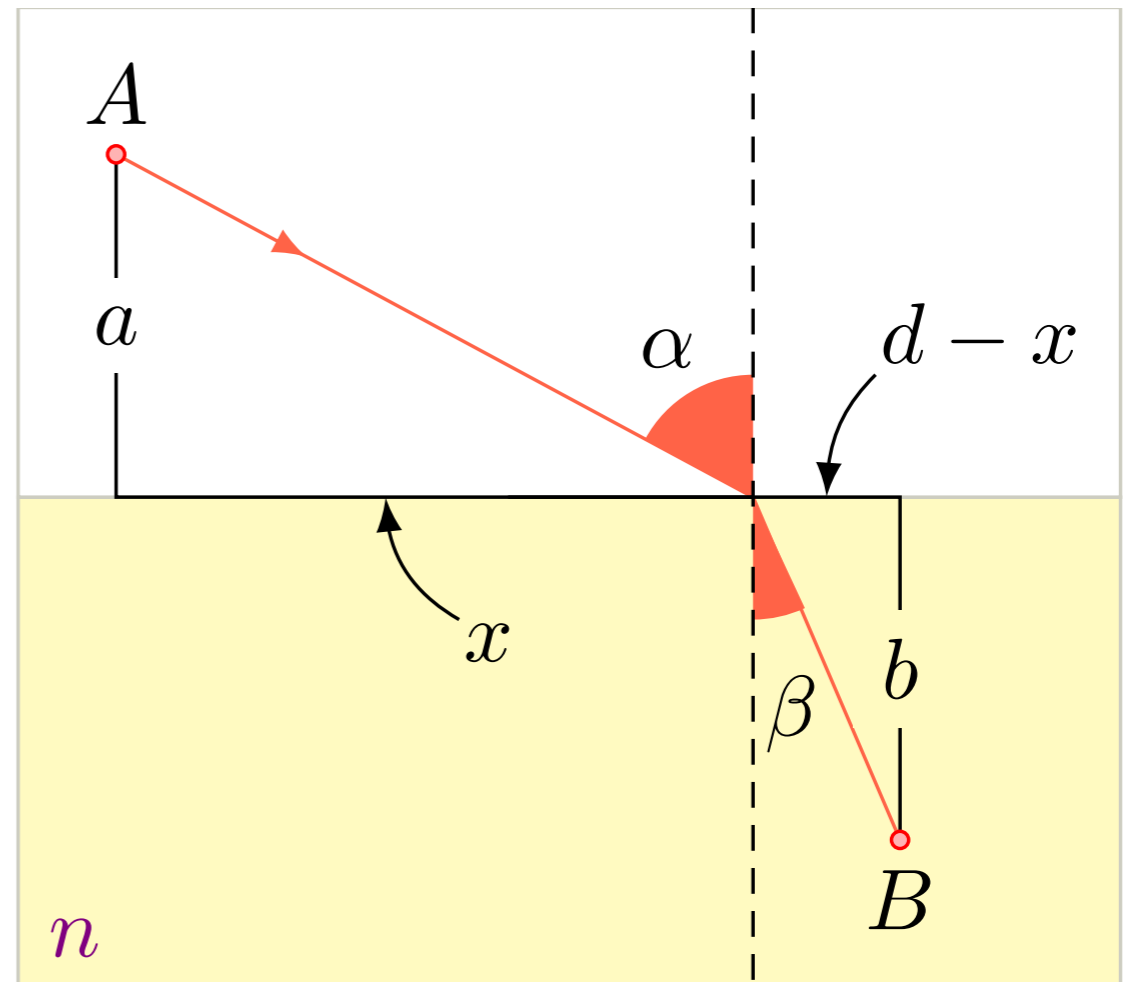
# Princípio de Fermat

## Refração

$$\Delta t_A = \frac{\sqrt{a^2 + x^2}}{c}$$

$$\Delta t_B = \frac{c}{n\sqrt{b^2 + (d-x)^2}}$$

$$\Delta t = \Delta t_A + \Delta t_B$$



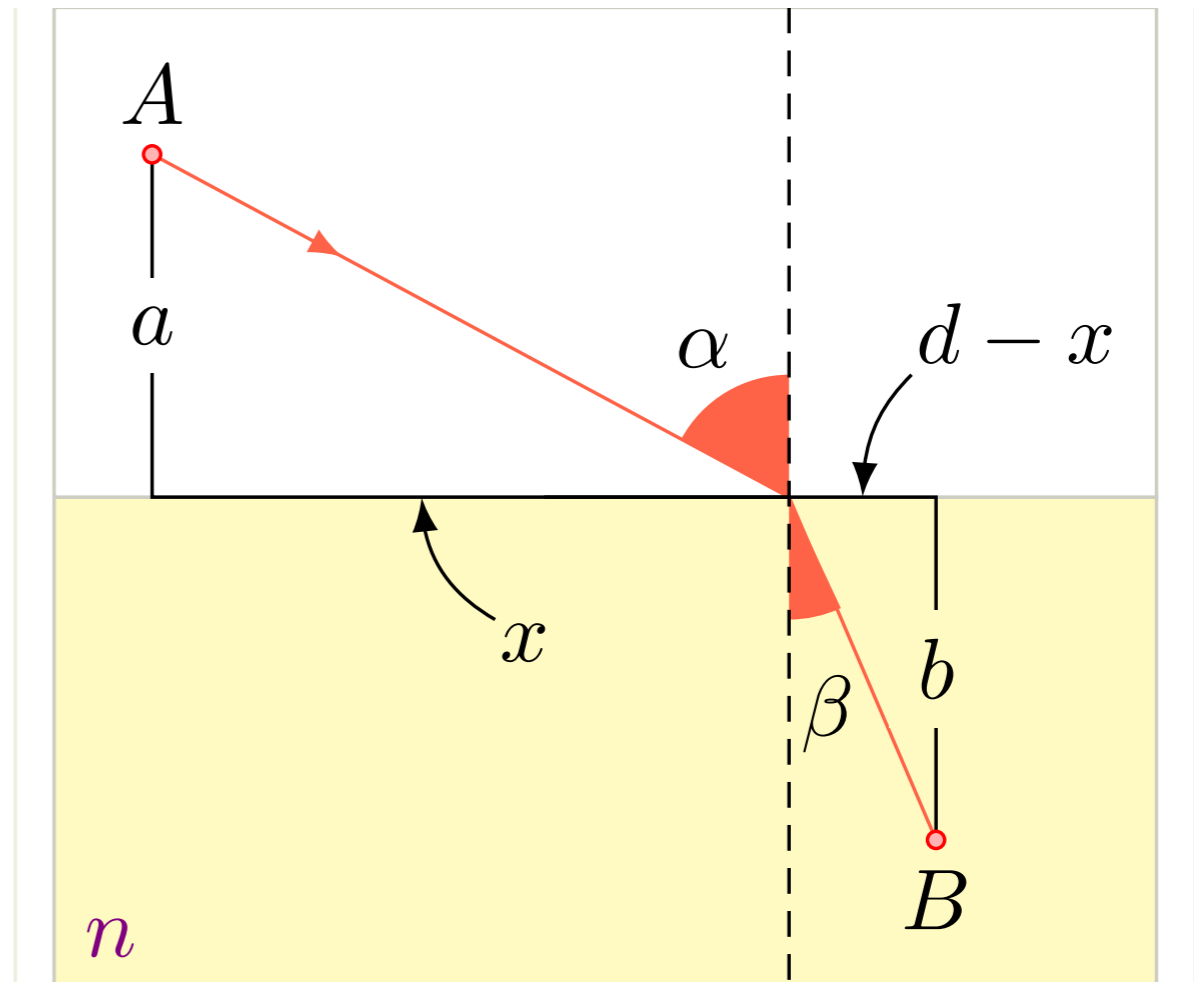
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$$\Delta t = \Delta t_A + \Delta t_B$$



$$\frac{d\Delta t}{dx} = 2c \left( \frac{x}{\sqrt{a^2 + x^2}} - n \frac{d-x}{\sqrt{b^2 + (d-x)^2}} \right)$$



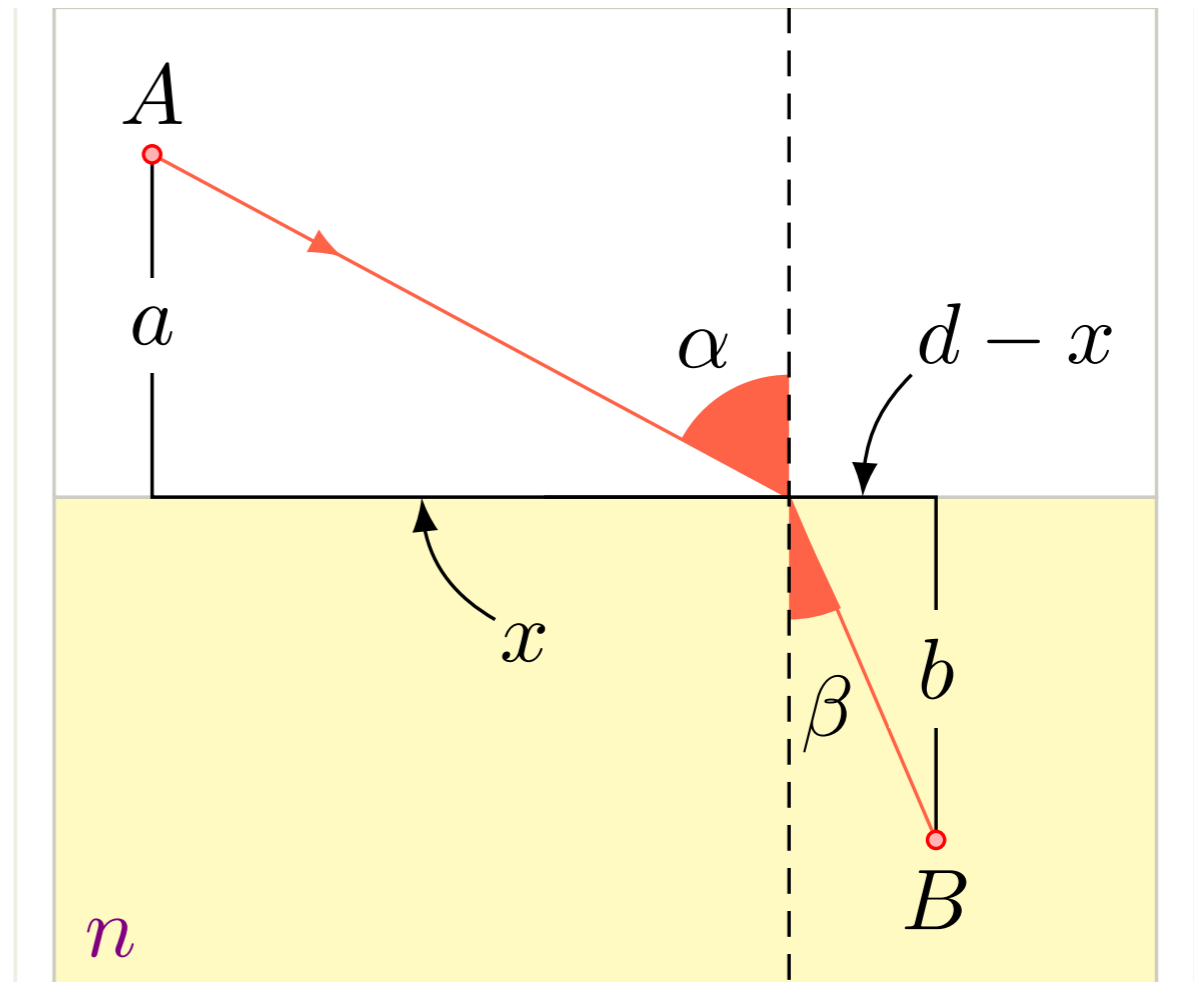
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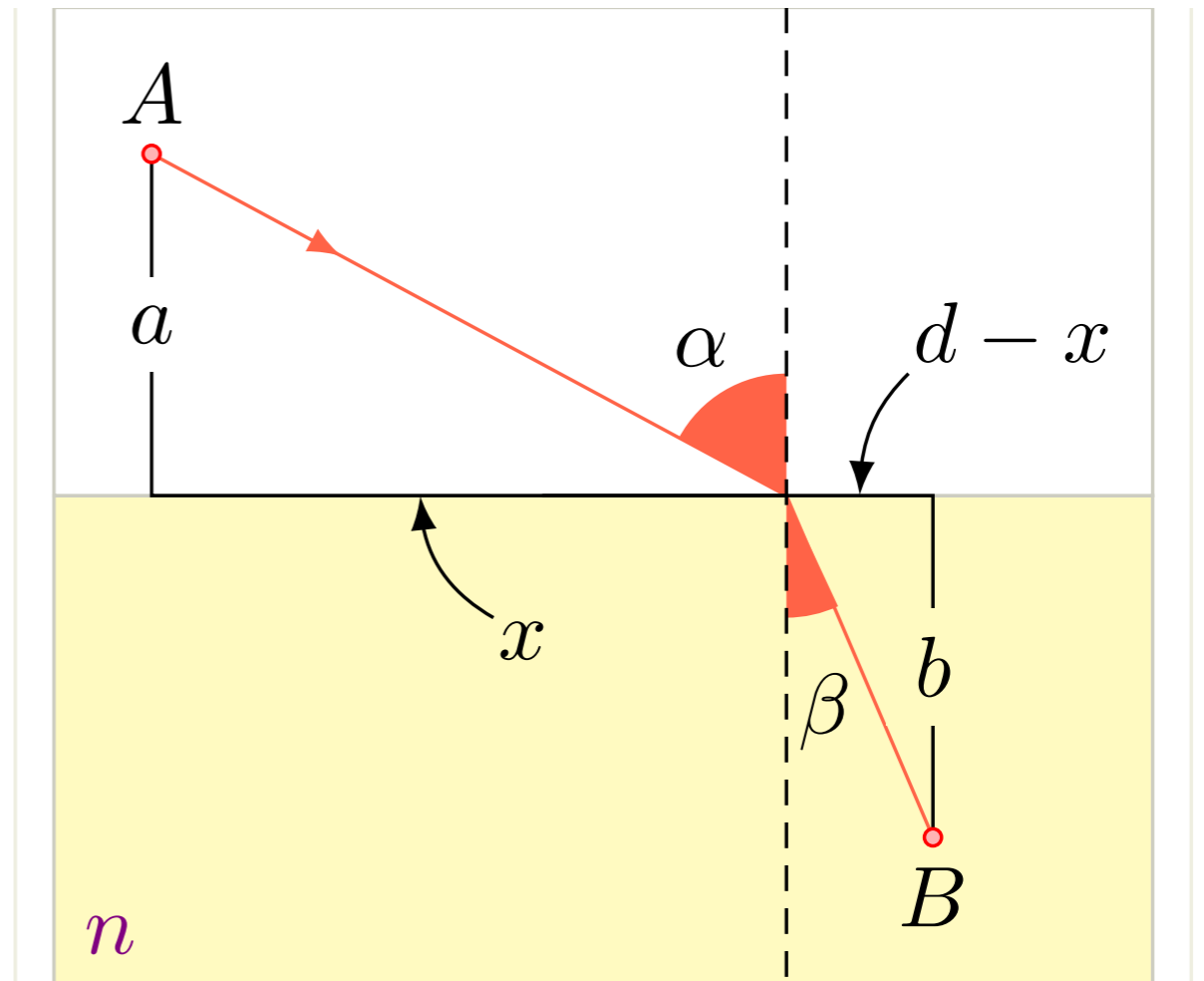


$$\frac{d\Delta t}{dx} = c \left( \frac{x}{\sqrt{a^2 + x^2}} - n \frac{(d-x)}{\sqrt{b^2 + (d-x)^2}} \right) = 0$$

# Princípio de Fermat

## Refração

$$\frac{x}{\sqrt{a^2 + x^2}} = n \frac{d - x}{\sqrt{b^2 + (d - x)^2}}$$



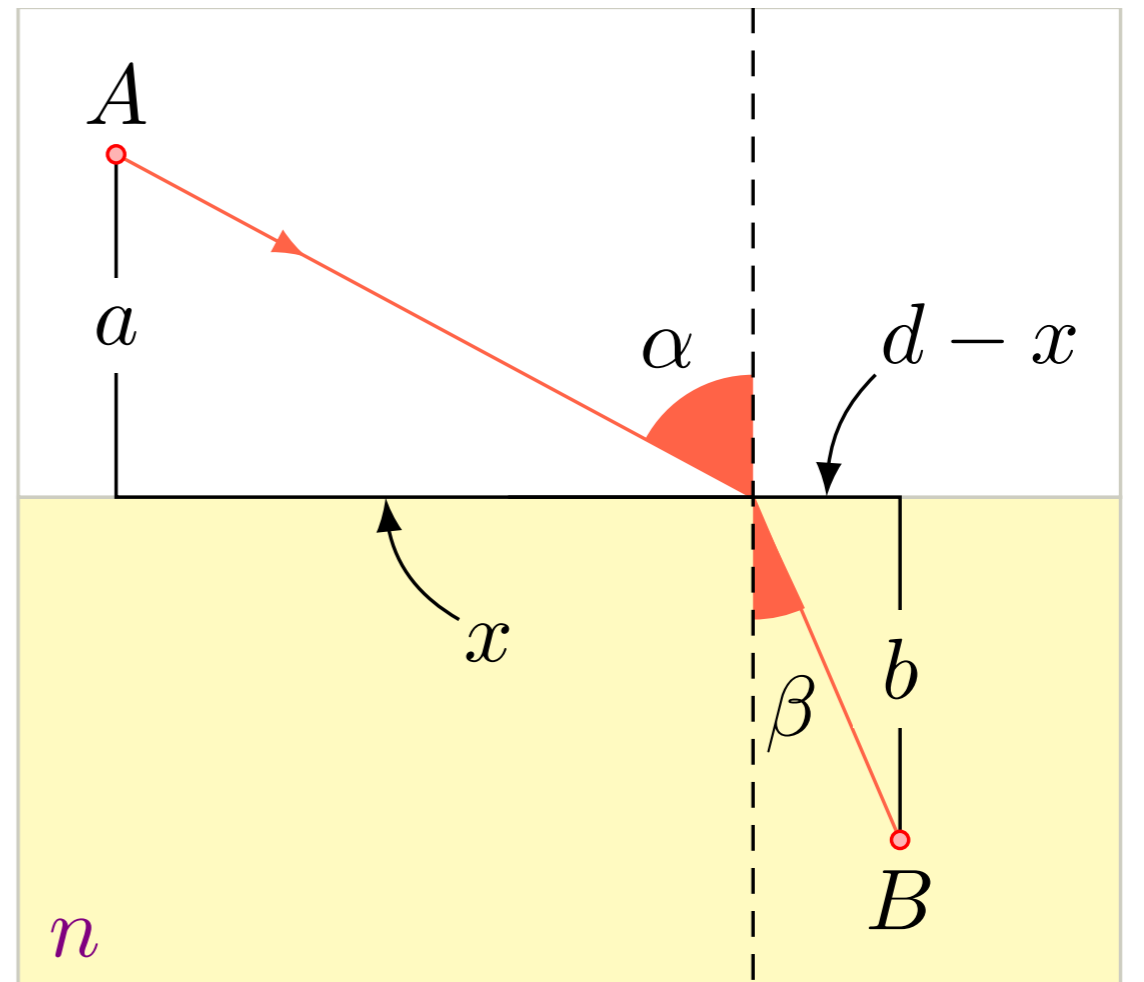
$$\frac{d\Delta t}{dx} = 2c \left( \frac{x}{\sqrt{a^2 + x^2}} - n \frac{d - x}{\sqrt{b^2 + (d - x)^2}} \right) = 0$$

# Princípio de Fermat

## Refração

$$\frac{x}{\sqrt{a^2 + x^2}} = n \frac{d - x}{\sqrt{b^2 + (d - x)^2}}$$

$$\sin \alpha = n \sin(\beta)$$



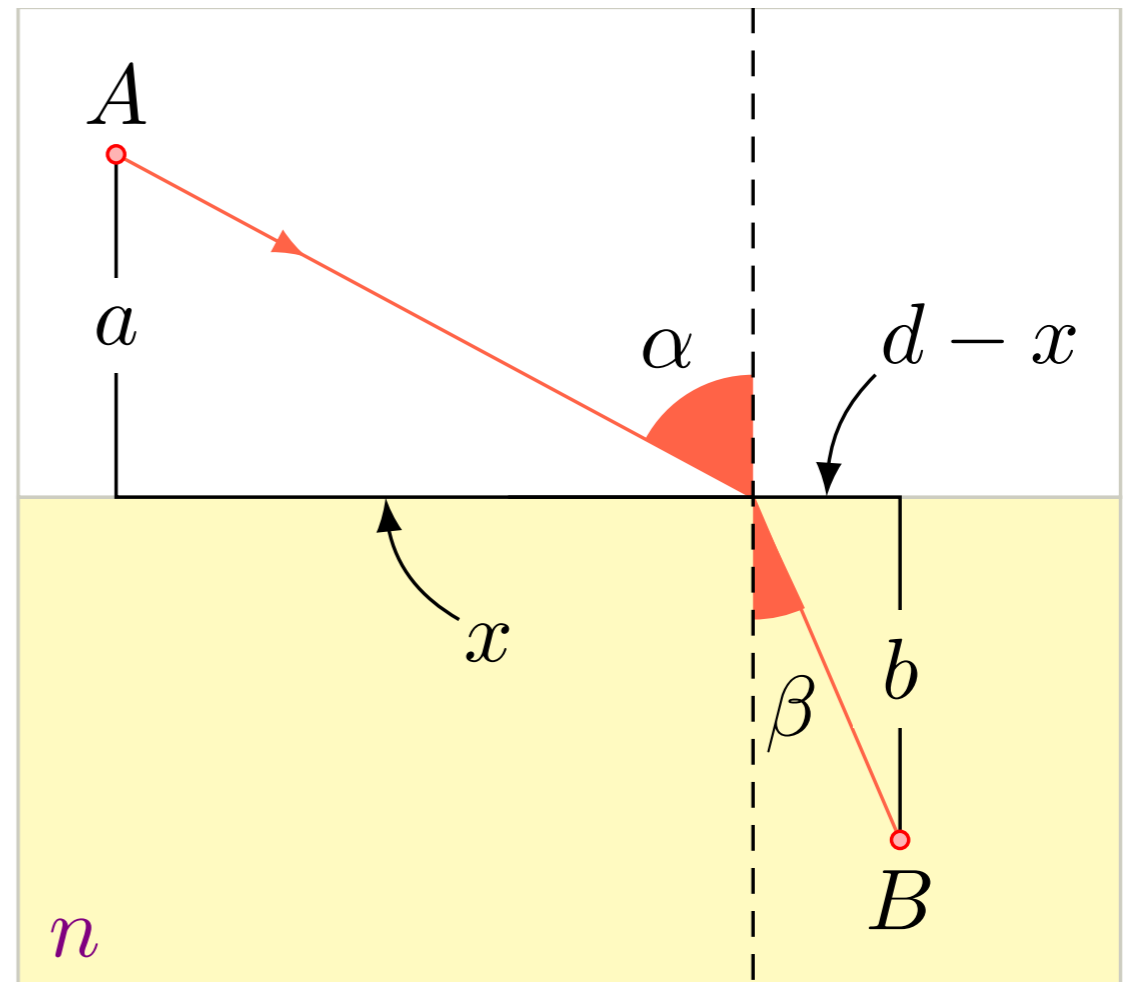
# Princípio de Fermat

## Refração

$$\frac{x}{\sqrt{a^2 + x^2}} = n \frac{d - x}{\sqrt{b^2 + (d - x)^2}}$$

$$\sin \alpha = n \sin(\beta)$$

Snell-Descartes



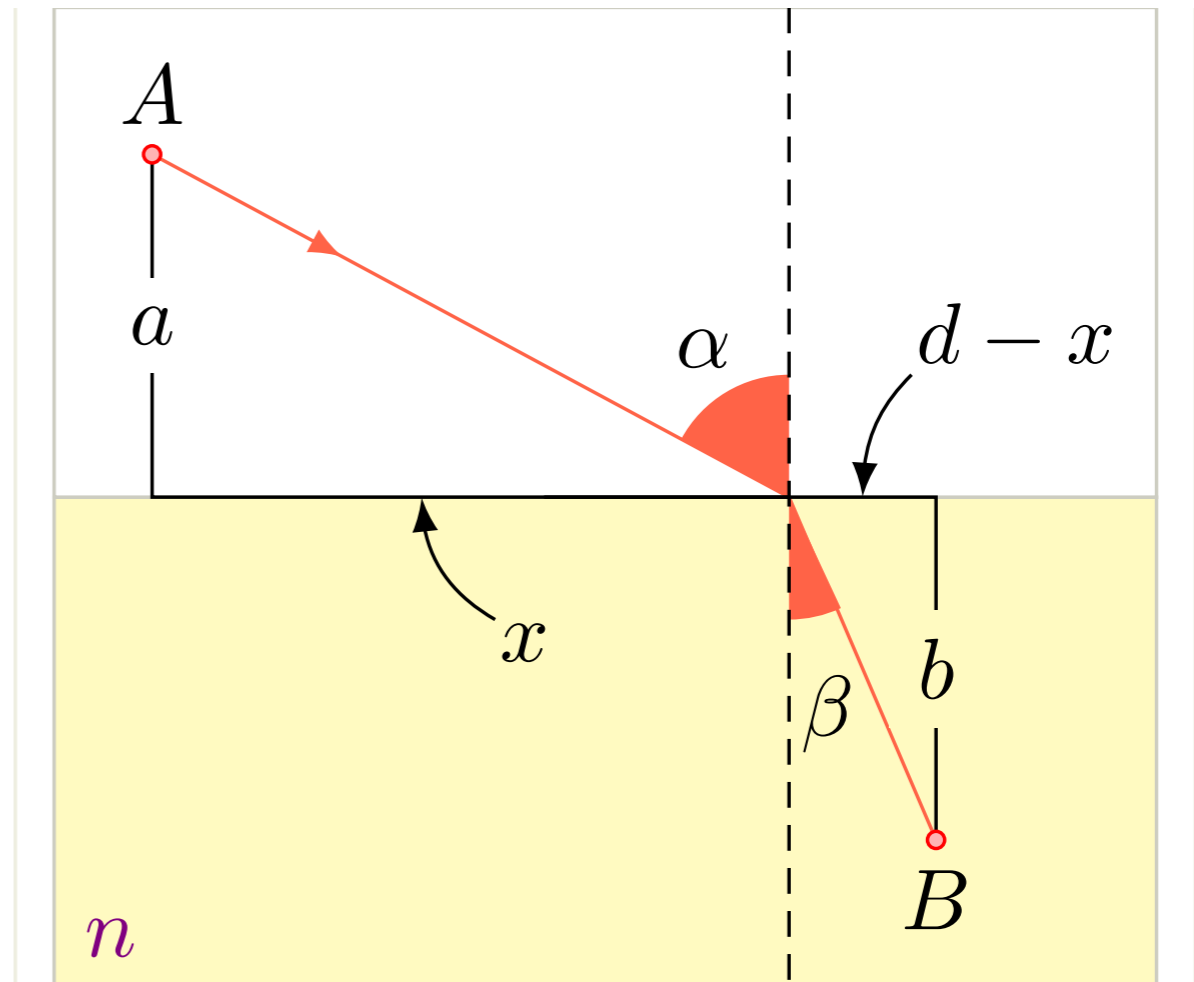
# Princípio de Fermat

## Refração

$$\Delta t_A = \frac{c}{\sqrt{a^2 + x^2}}$$

$$\Delta t_B = \frac{c}{n\sqrt{b^2 + (d-x)^2}}$$

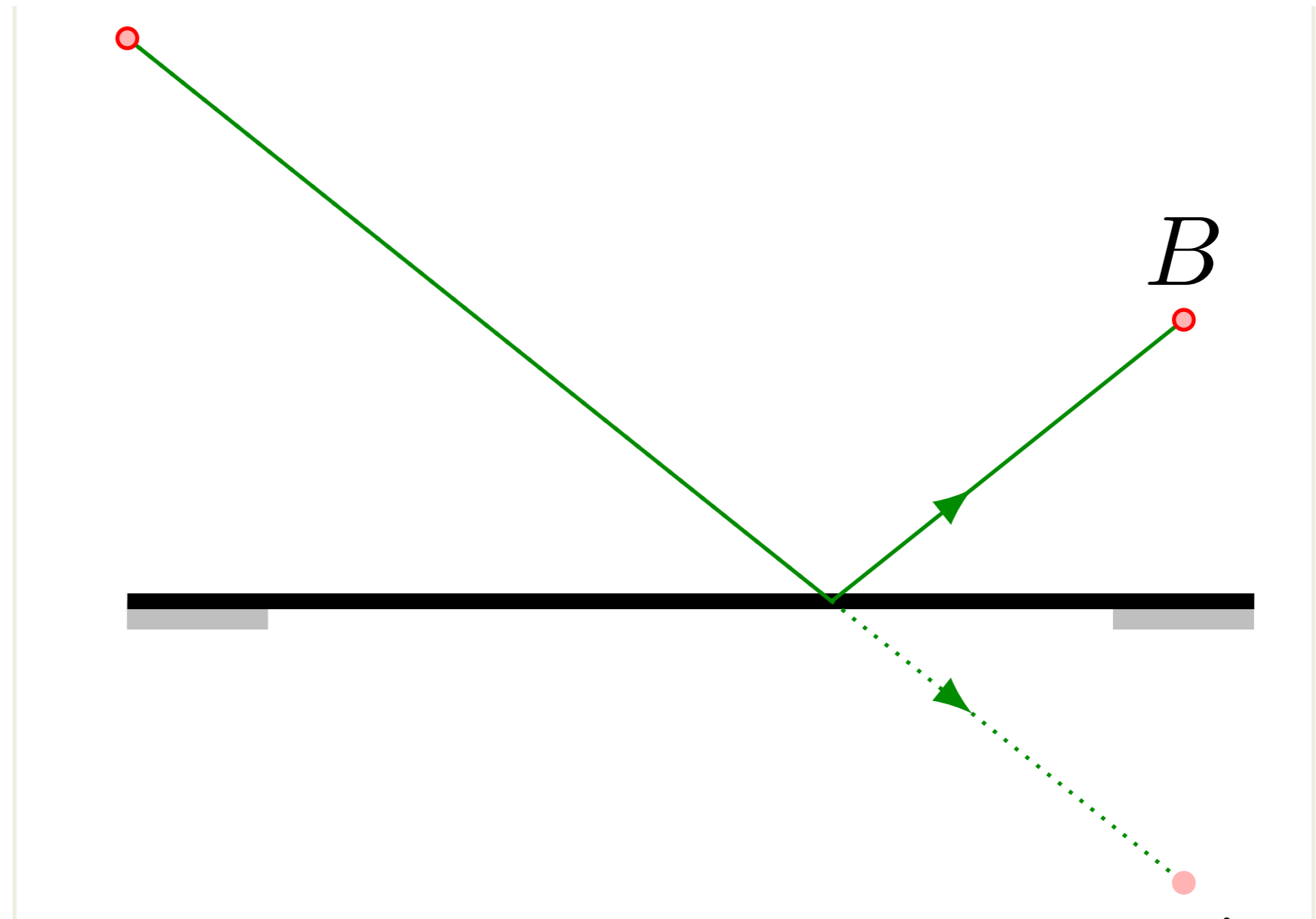
$$\Delta t = \Delta t_A + \Delta t_B$$



$$\frac{d\Delta t}{dx} = 2c \left( \frac{x}{\sqrt{a^2 + x^2}} - \frac{d-x}{n\sqrt{b^2 + (d-x)^2}} \right) = 0$$

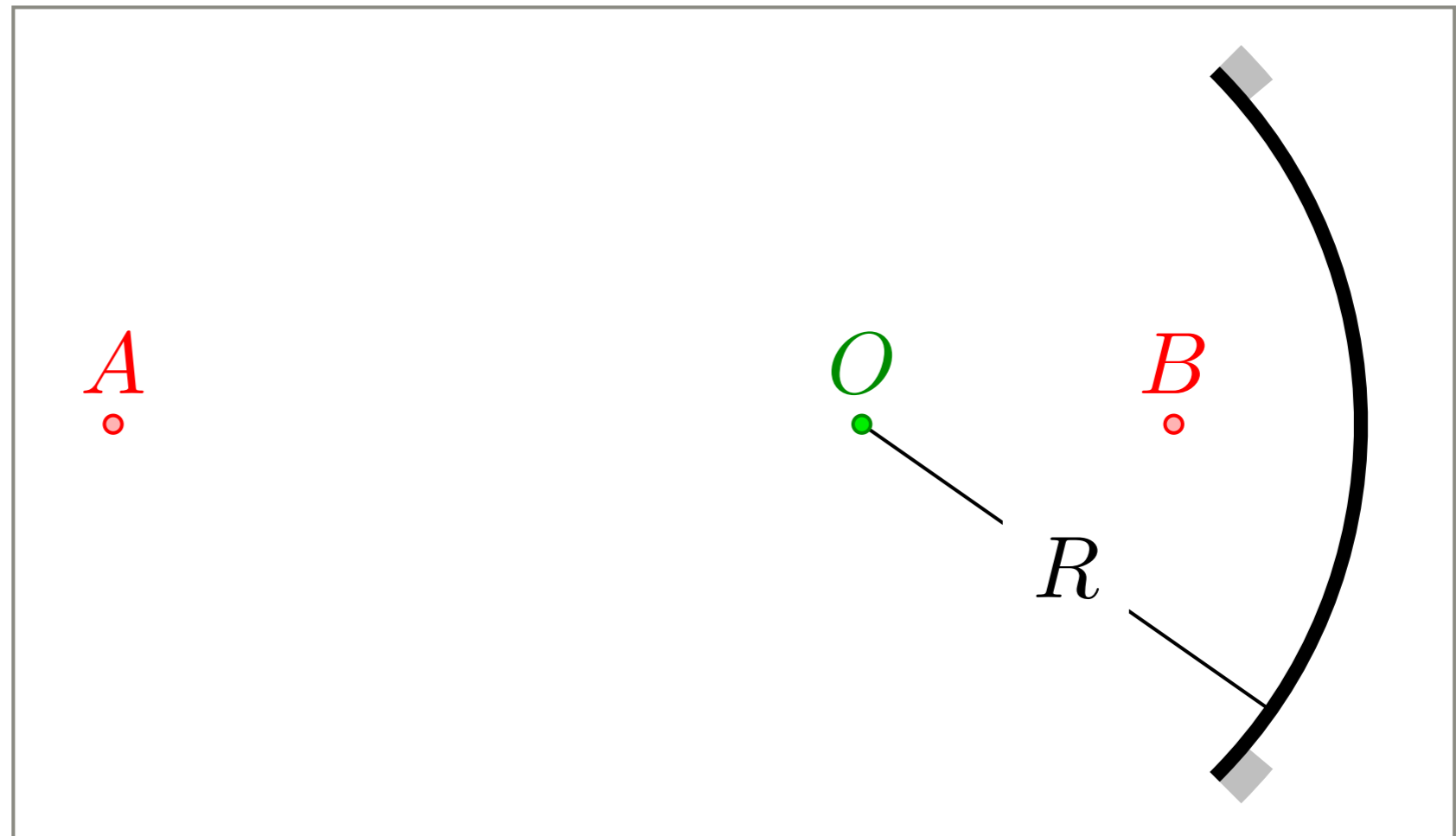
# Princípio de Fermat

## Espelho plano



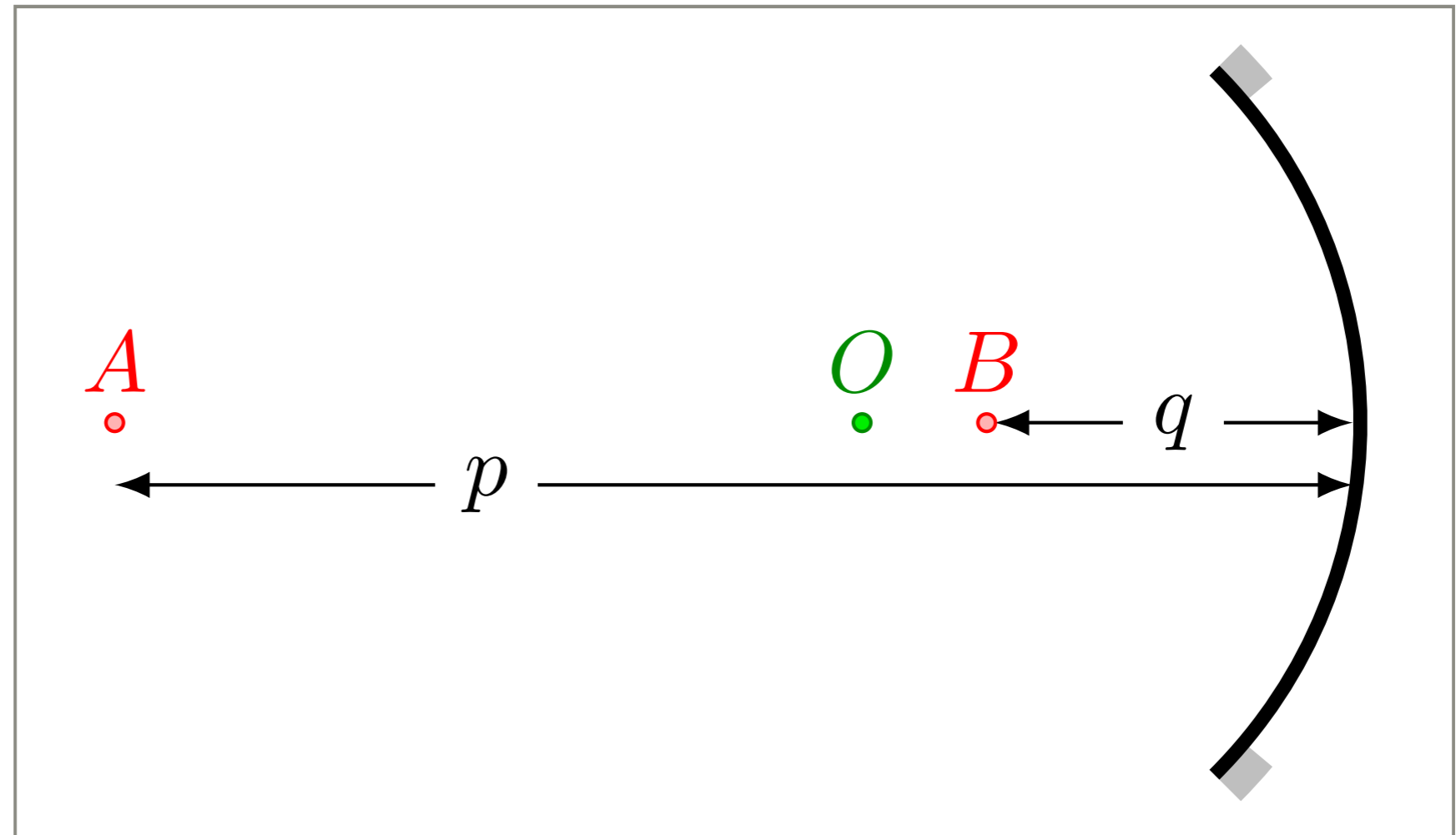
# Princípio de Fermat

## Espelho esférico



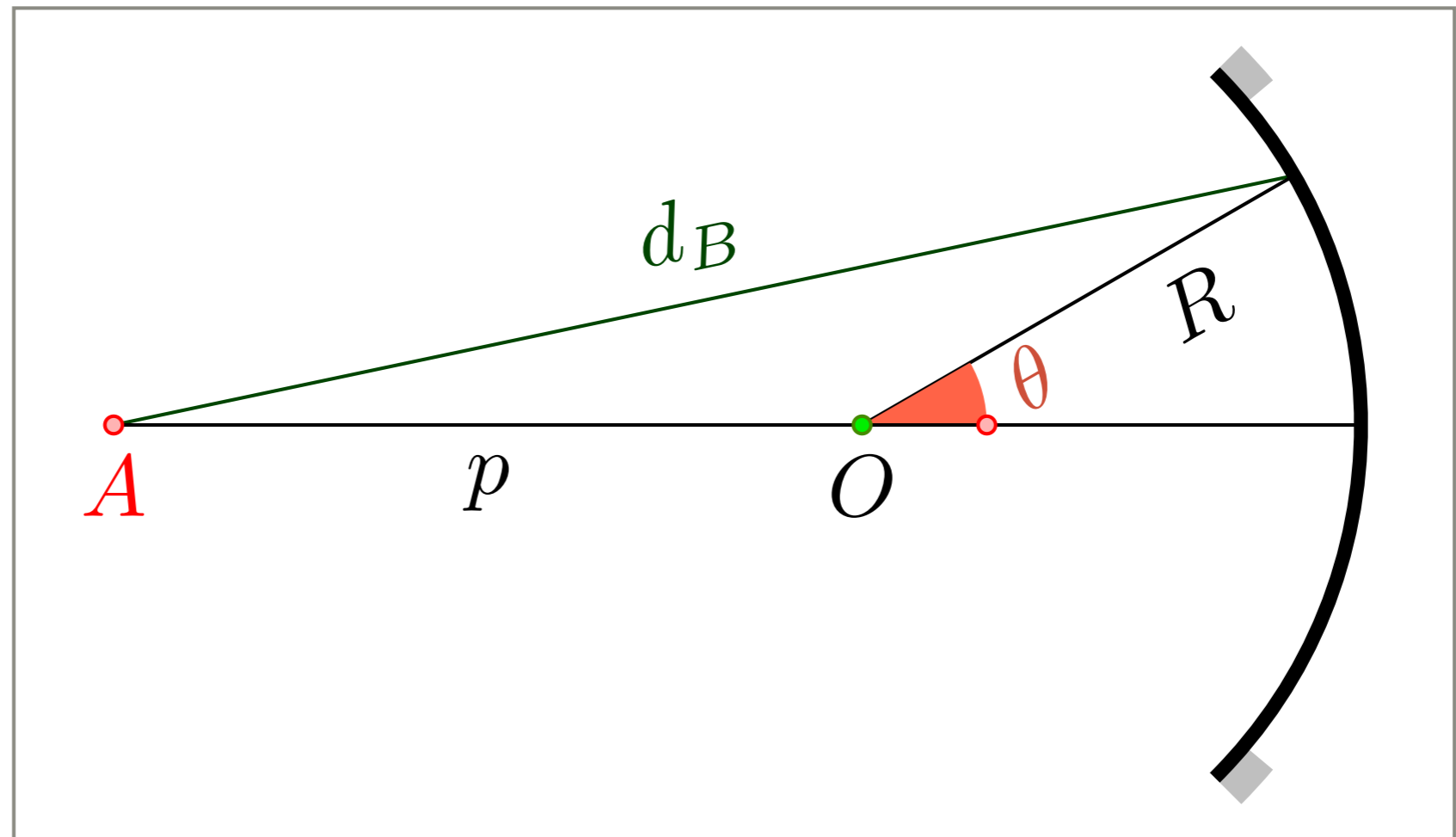
# Princípio de Fermat

## Espelho esférico



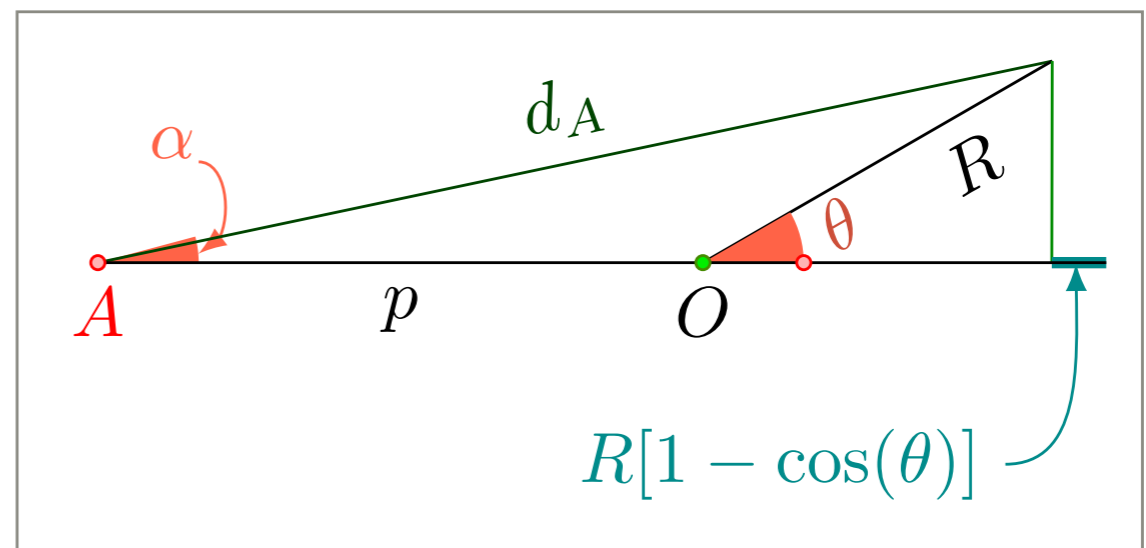
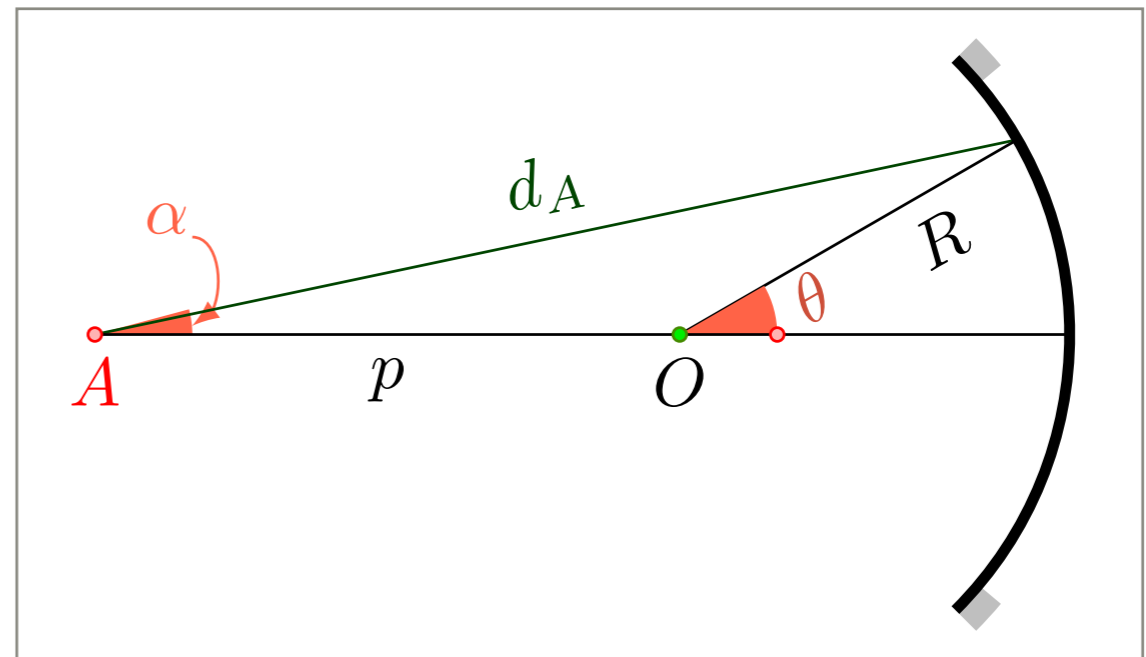


# Princípio de Fermat Espelho esférico



# Princípio de Fermat Espelho esférico

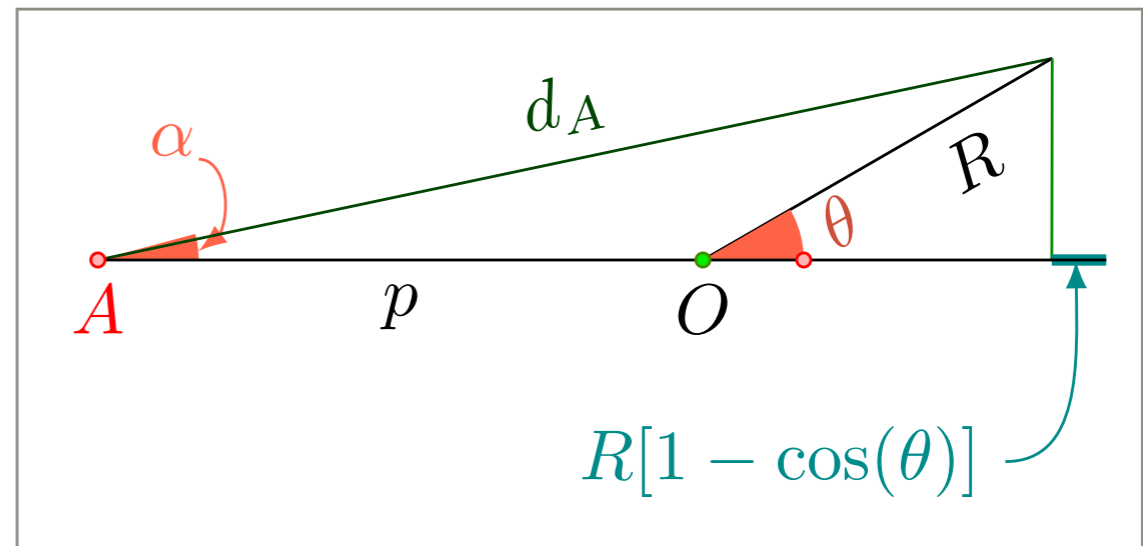
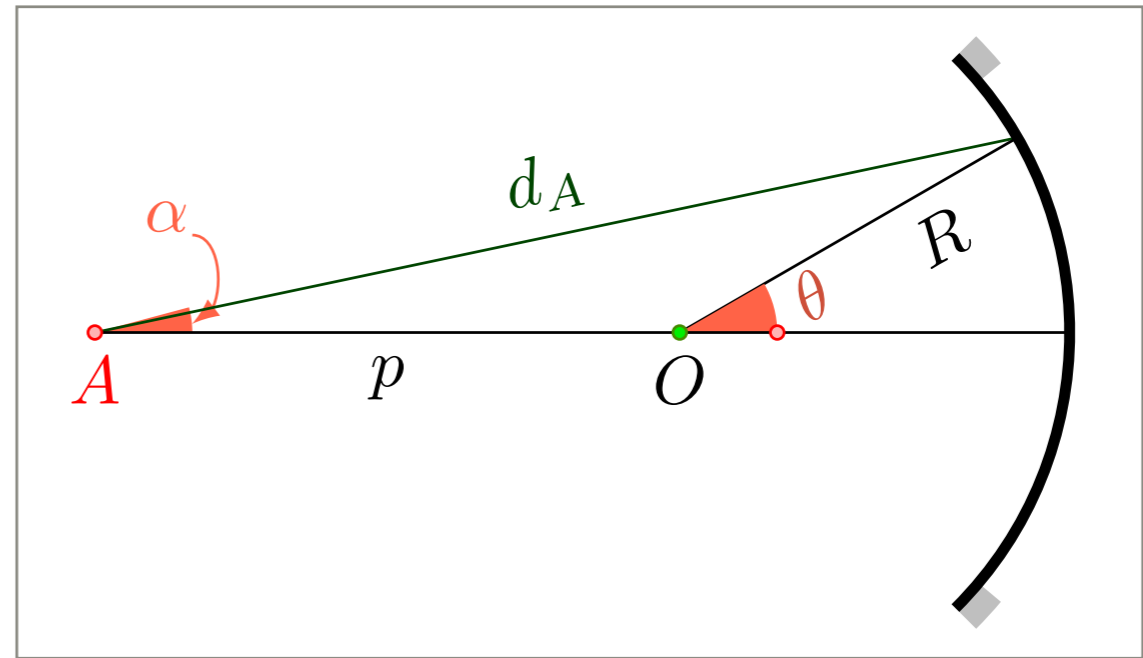
$$d_B^2 = R^2 \sin^2 \theta + \left( p - R(1 - \cos \theta) \right)^2$$



# Princípio de Fermat Espelho esférico

$$d_B^2 = R^2 \sin^2 \theta + \left( p - R(1 - \cos \theta) \right)^2$$

$$\Delta t_B = \frac{d_B}{c}$$

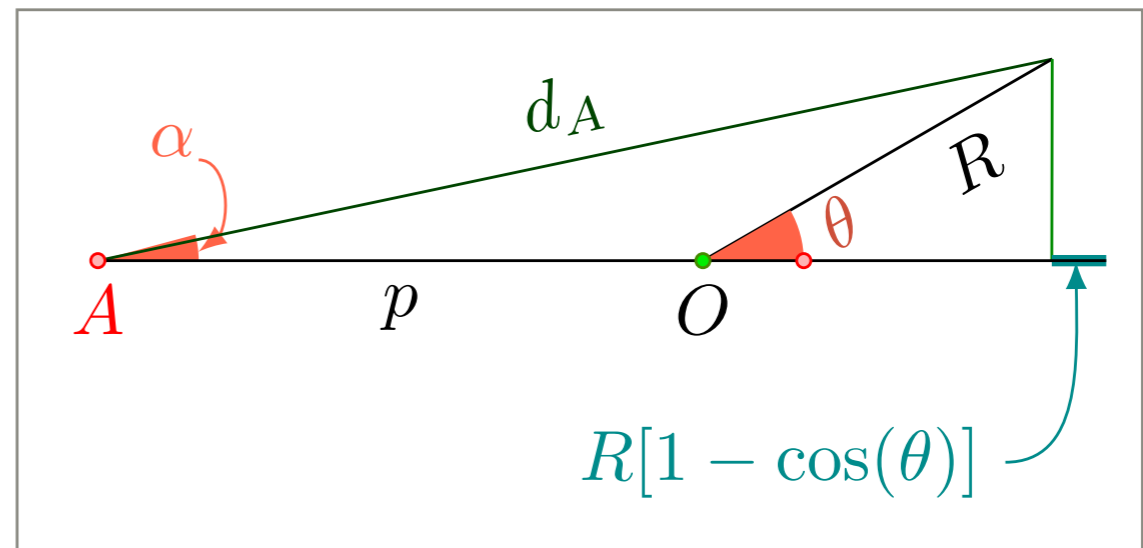
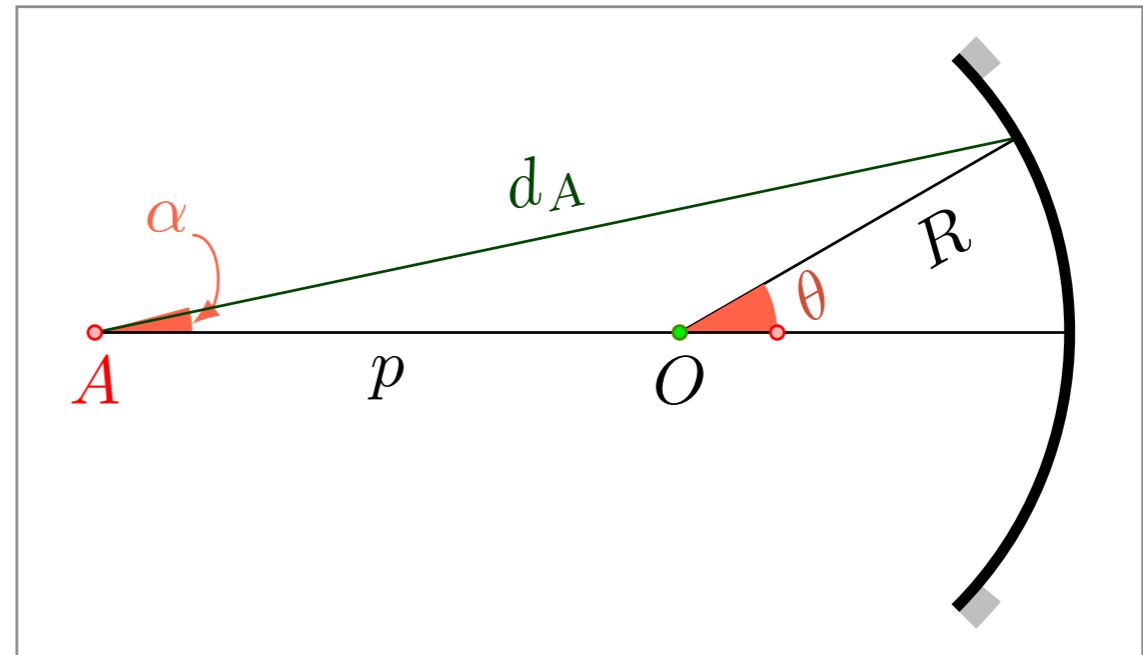


# Princípio de Fermat Espelho esférico

$$d_B^2 = R^2 \sin^2 \theta + \left( p - R(1 - \cos \theta) \right)^2$$

$$\Delta t_B = \frac{d_B}{c}$$

$$\frac{d\Delta t_B}{d\theta} = \frac{-2R(p - R)\sin \theta}{cp}$$



# Princípio de Fermat

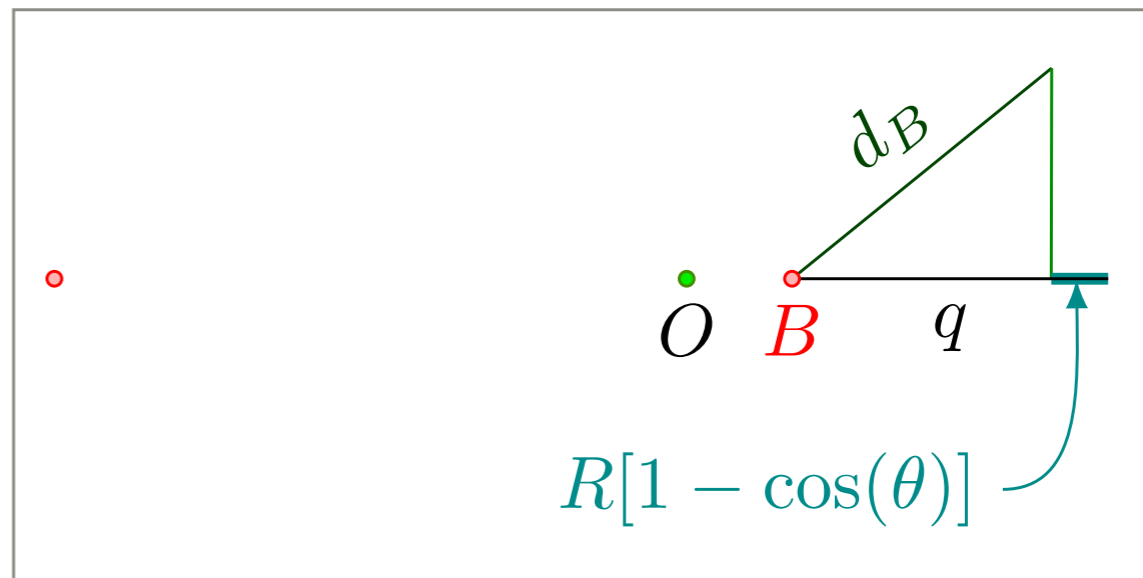
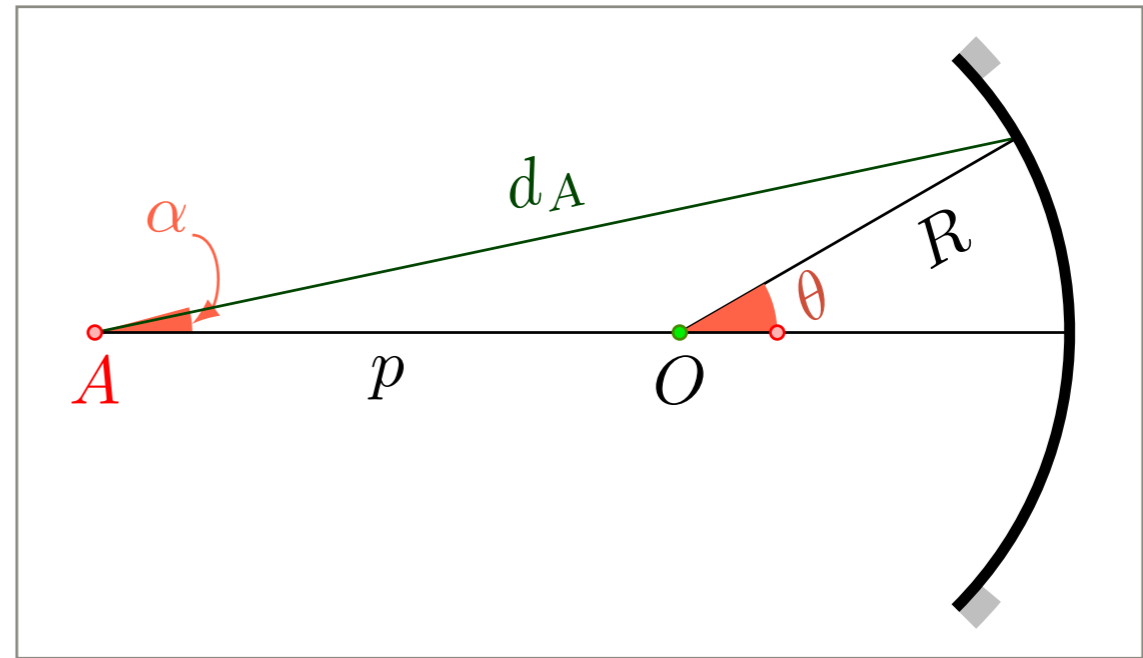
## Espelho esférico

$$d_B^2 = R^2 \sin^2 \theta + \left( p - R(1 - \cos \theta) \right)^2$$

$$\Delta t_B = \frac{d_B}{c}$$

$$\frac{d\Delta t_B}{d\theta} = \frac{-2R(p - R)\sin \theta}{cp}$$

$$\frac{d\Delta t_A}{d\theta} = \frac{-2R(q - R)\sin \theta}{cq}$$



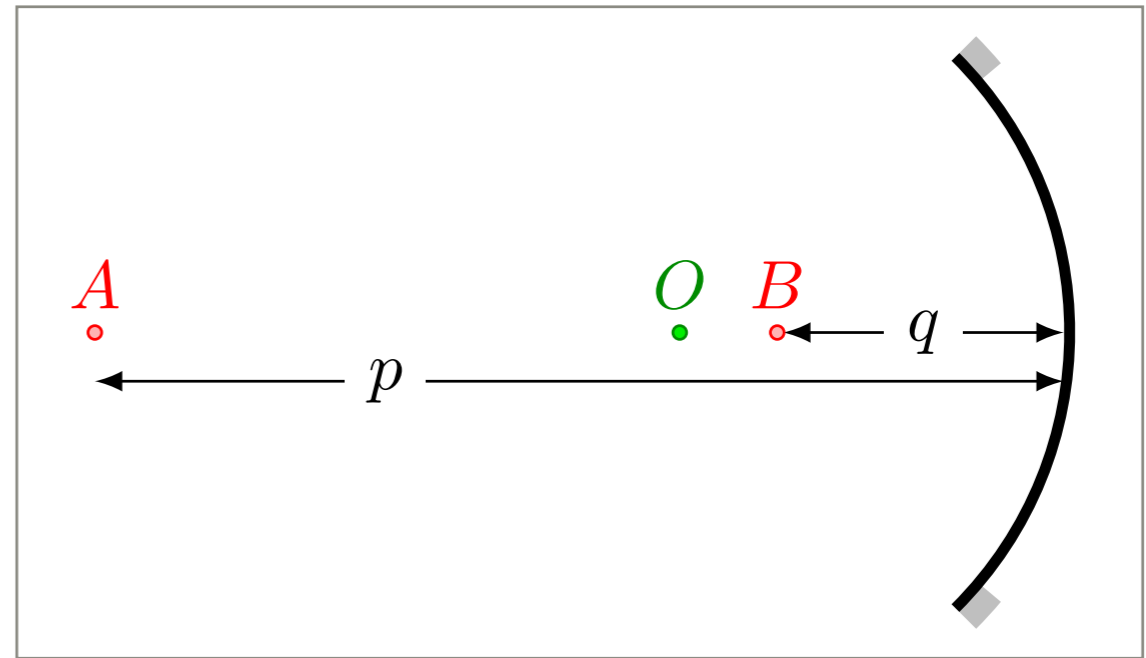
# Princípio de Fermat

## Espelho esférico

$$\frac{d\Delta t_B}{d\theta} = \frac{-2R(p - R)\sin\theta}{cp}$$

$$\frac{d\Delta t_A}{d\theta} = \frac{-2R(q - R)\sin\theta}{cq}$$

$$-2R \sin\theta \left( \frac{q - R}{q} + \frac{p - R}{p} \right) = 0$$



$$\frac{d\Delta t_B}{d\theta} = \frac{-2R(p - R)\sin\theta}{cp}$$

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$$-2R \sin\theta \left( \frac{q - R}{q} + \frac{p - R}{p} \right) = 0$$

$$\frac{q - R}{q} + \frac{p - R}{p} = 0$$



$$\frac{1}{p} + \frac{1}{q} = \frac{2}{R}$$

