

Configuração de redes metabólicas.

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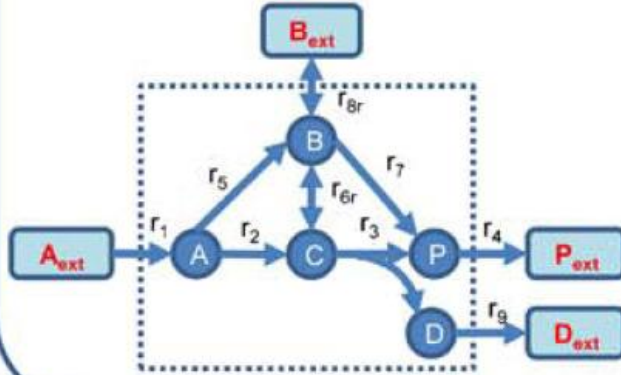
Departamento de Microbiologia

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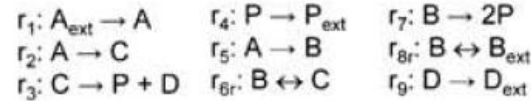
analysis of cellular metabolism

Problem statement

Network



Stoichiometric reactions



Stoichiometric matrix

	r ₁	r ₂	r ₃	r ₄	r ₅	r _{6r}	r ₇	r _{8r}	r ₉
A	1	-1	0	0	-1	0	0	0	0
B	0	0	0	0	1	-1	-1	-1	0
C	0	1	-1	0	0	1	0	0	0
D	0	0	1	0	0	0	0	0	-1
P	0	0	1	-1	0	0	2	0	0

$\underline{r} = [r_1 \ r_2 \ r_3 \ r_4 \ r_5 \ r_{6r} \ r_7 \ r_{8r} \ r_9]^T$

Equations to solve

A

$$\underline{S} \cdot \underline{r} = \underline{0}$$

Thermodynamic constraints:
r_{1,5,7,9} ≥ 0

$$\frac{d}{dt} \underline{C} = \underline{S} \times \underline{r} - \mu \times \underline{C},$$

μ · C (negligible)

$$S \cdot r = 0 \text{ (Eq 2)}$$

dC/dt = 0 (steady state)

$$r_i \geq 0 \text{ (Eq 3)}$$

Tools for analysis of cellular metabolism can be grouped into three categories, all of them developed from the same mathematical model:

- (1) Metabolic flux analysis,
- (2) Flux balance analysis and
- (3) Metabolic pathway analysis (Elementary mode analysis).

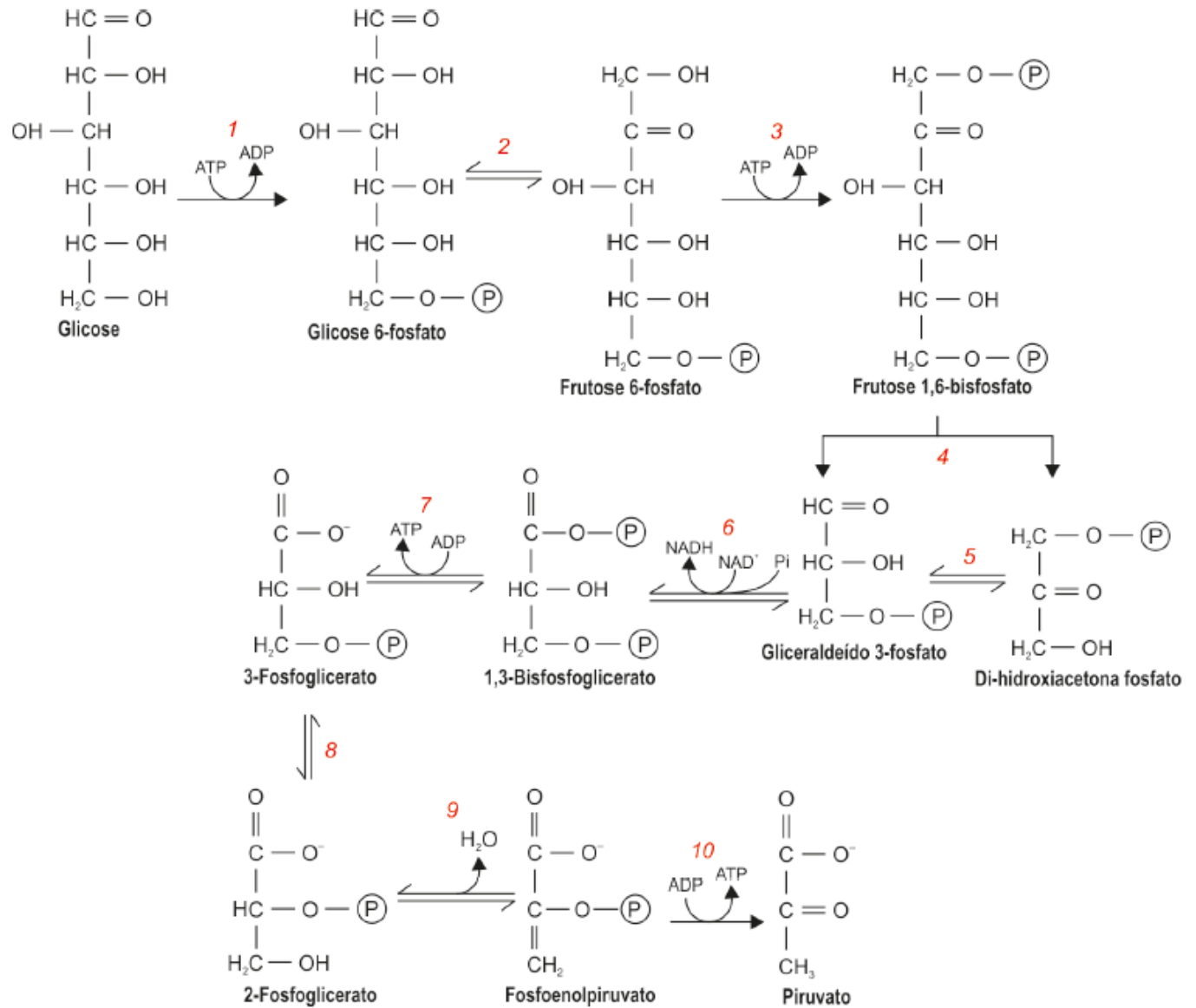
$$\begin{bmatrix} \mathbf{X.W} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{Z.Y} \end{bmatrix} = \begin{bmatrix} \mathbf{X.Y} \end{bmatrix}$$

$$\begin{bmatrix} \mathbf{a_1} & \mathbf{a_2} & \mathbf{a_3} & \mathbf{a_4} \\ \mathbf{b_1} & \mathbf{b_2} & \mathbf{b_3} & \mathbf{b_4} \\ \mathbf{c_1} & \mathbf{c_2} & \mathbf{c_3} & \mathbf{c_4} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{v_1} \\ \mathbf{v_2} \\ \mathbf{v_3} \\ \mathbf{v_4} \end{bmatrix} = \begin{bmatrix} \frac{\mathbf{da}}{\mathbf{dt}} \\ \frac{\mathbf{db}}{\mathbf{dt}} \\ \frac{\mathbf{dc}}{\mathbf{dt}} \end{bmatrix}$$

$$\frac{\mathbf{da}}{\mathbf{dt}} = \mathbf{a_1v_1} + \mathbf{a_2v_2} + \mathbf{a_3v_3} + \mathbf{a_4v_4}$$

$$\frac{\mathbf{db}}{\mathbf{dt}} = \mathbf{b_1v_1} + \mathbf{b_2v_2} + \mathbf{b_3v_3} + \mathbf{b_4v_4}$$

$$\frac{\mathbf{dc}}{\mathbf{dt}} = \mathbf{c_1v_1} + \mathbf{c_2v_2} + \mathbf{c_3v_3} + \mathbf{c_4v_4}$$



Embden
Meyerhoff
Parnas

Figura 3.4 Via de Embden-Meyerhoff-Parnas.

Embden-Meyerhoff-Parnas

EMP1 : Gliext + ATP = G6P + ADP .

EMP2 : G6P = F6P .

EMP3 : F6P + ATP = F16P + ADP .

EMP4 : F16P = G3P + DHP .

EMP5 : DHP = G3P .

EMP6 : G3P + NAD = BPG13 + NADH .

EMP7 : BPG13 + ADP = PG3 + ATP .

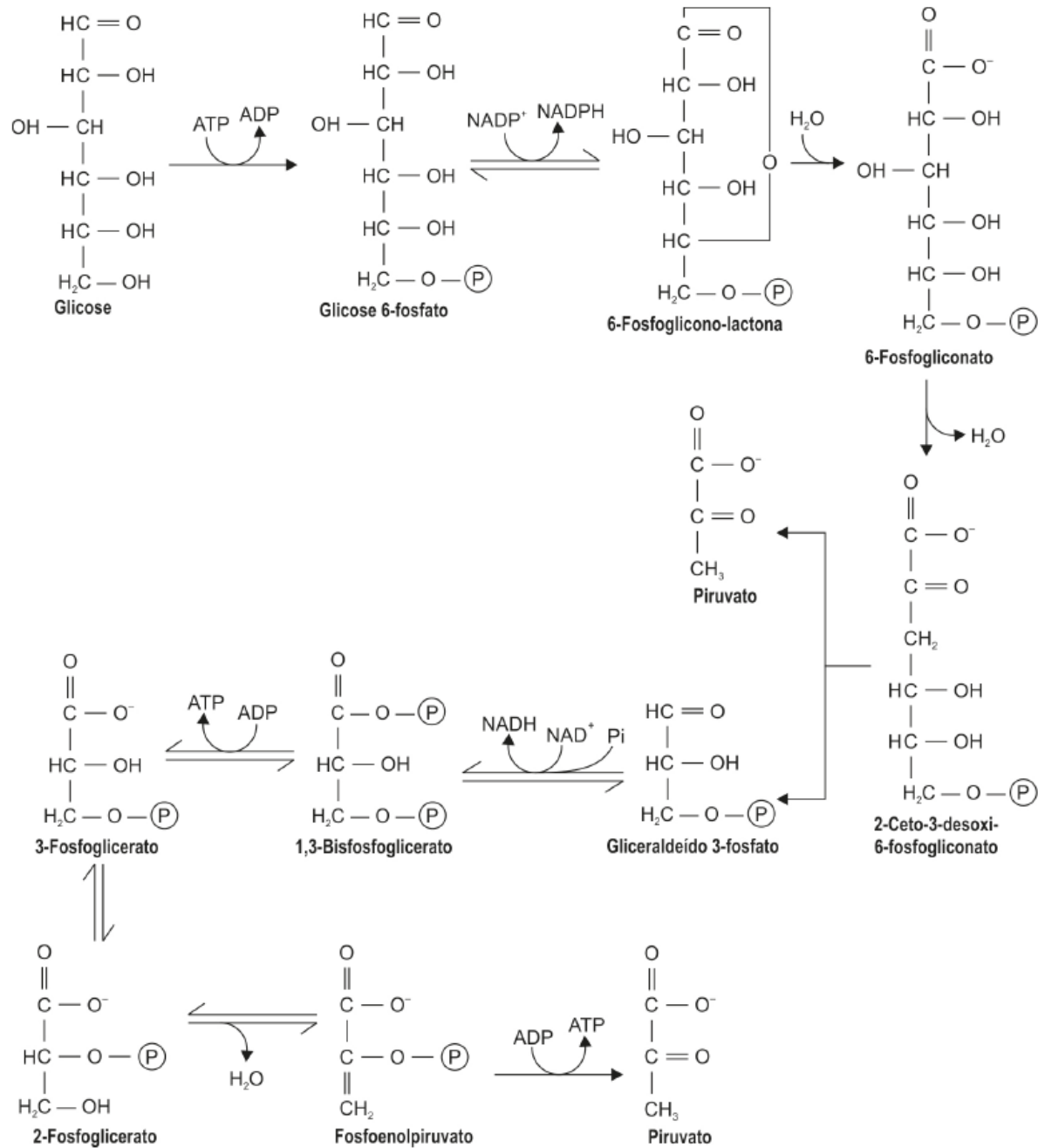
EMP8 : PG3 = PG2 .

EMP9 : PG2 = PEP .

EMP10 : PEP + ADP = PIR + ATP .

CPD : PIR + NAD + CoASH = AcCoA + NADH + CO₂ .

OXNAD : NADH + 3 ADP + O = NAD + 3 ATP .



Entner
Doudoroff

Figura 3.5 Via de Entner-Doudoroff.

Entner-Doudoroff

EMP1 : Gliext + ATP = G6P + ADP .

VP1 : G6P + NADP = PG6 + NADPH .

ED1 : PG6 = KDPG2 .

ED2 : KDPG2 = PIR + G3P .

EMP6 : G3P + NAD = BPG13 + NADH .

EMP7 : BPG13 + ADP = PG3 + ATP .

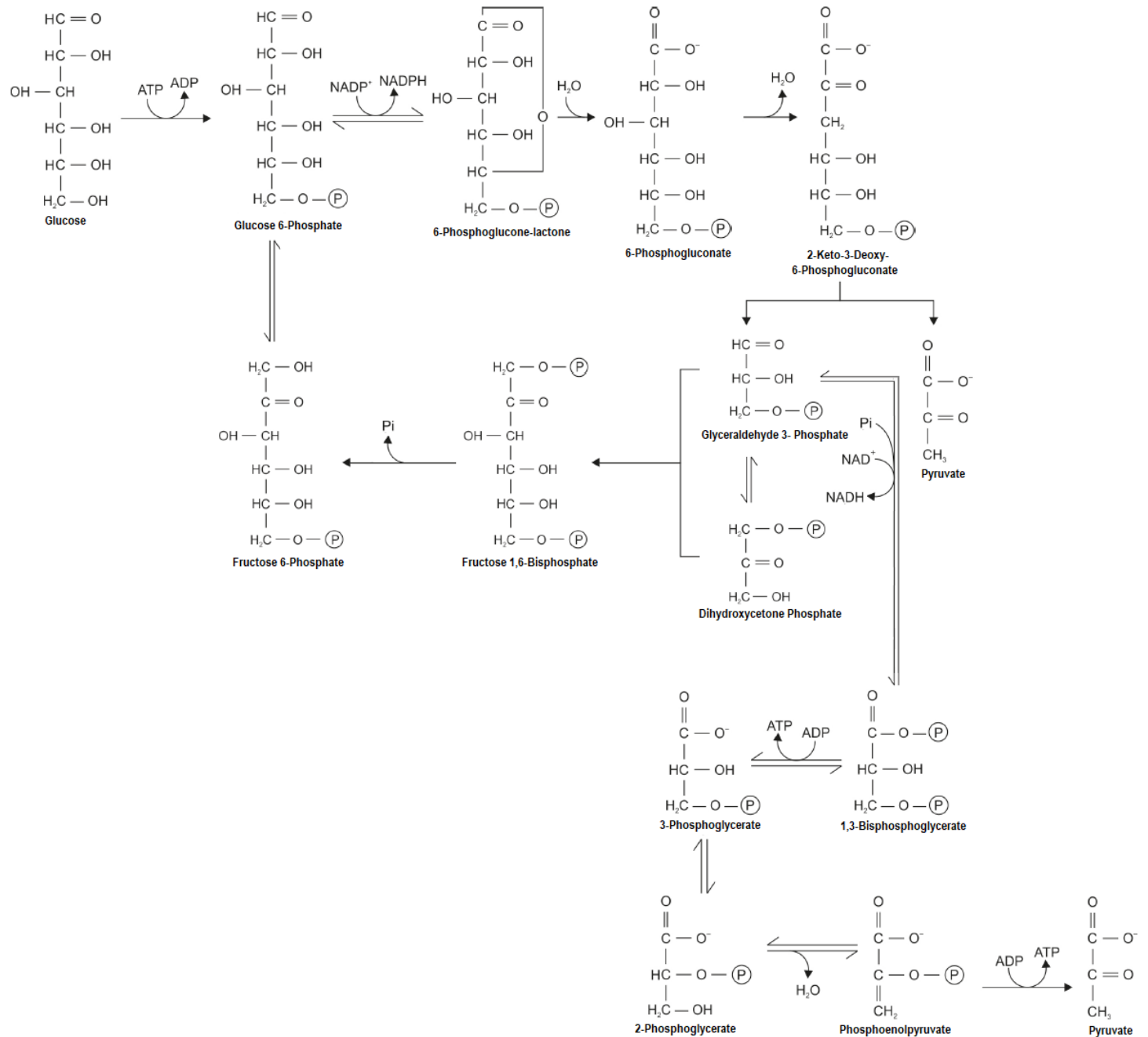
EMP8 : PG3 = PG2 .

EMP9 : PG2 = PEP .

EMP10 : PEP + ADP = PIR + ATP .

CPD : PIR + NAD + CoASH = AcCoA + NADH + CO2 .

OXNAD : NADH + 3 ADP + O = NAD + 3 ATP .



Entner
Doudoroff
cíclica

Entner-Doudoroff cíclica

EMP1 : Gliext + ATP = G6P + ADP .

VP1 : G6P + NADP = PG6 + NADPH .

ED1 : PG6 = KDPG2 .

ED2 : KDPG2 = PIR + G3P .

GLN1 : G3P = DHP .

GLN2 : G3P + DHP = F16P .

GLN3 : F16P = F6P + Pi .

GLN4 : F6P = G6P .

EMP6 : G3P + NAD = BPG13 + NADH .

EMP7 : BPG13 + ADP = PG3 + ATP .

EMP8 : PG3 = PG2 .

EMP9 : PG2 = PEP .

EMP10 : PEP + ADP = PIR + ATP .

CPD : PIR + NAD + CoASH = AcCoA + NADH + CO2 .

OXNAD : NADH + 3 ADP + O = NAD + 3 ATP .

Via das Pentoses

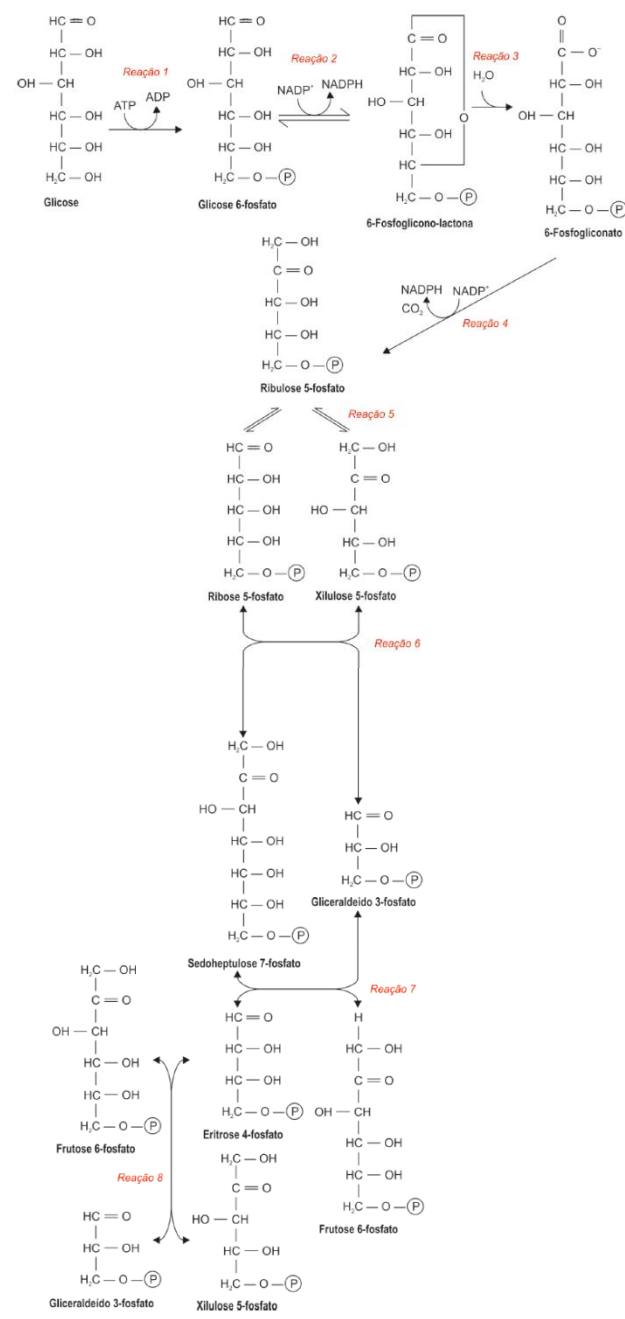


Figura 3.6 Via das pentoses.

Via das Pentoses

EMP1 : Gliext + ATP = G6P + ADP .

VP1 : G6P + NADP = PG6 + NADPH .

VP5 : PG6 + NADP = NADPH + RbI5P + CO2 .

VP6 : RbI5P = Rb5P .

VP7 : RbI5P = X5P .

VP8 : Rb5P + X5P = S7P + G3P .

VP9 : G3P + S7P = E4P + F6P .

VP10 : X5P + E4P = F6P + G3P .

EMP2 : G6P = F6P .

EMP6 : G3P + NAD = BPG13 + NADH .

EMP7 : BPG13 + ADP = PG3 + ATP .

EMP8 : PG3 = PG2 .

EMP9 : PG2 = PEP .

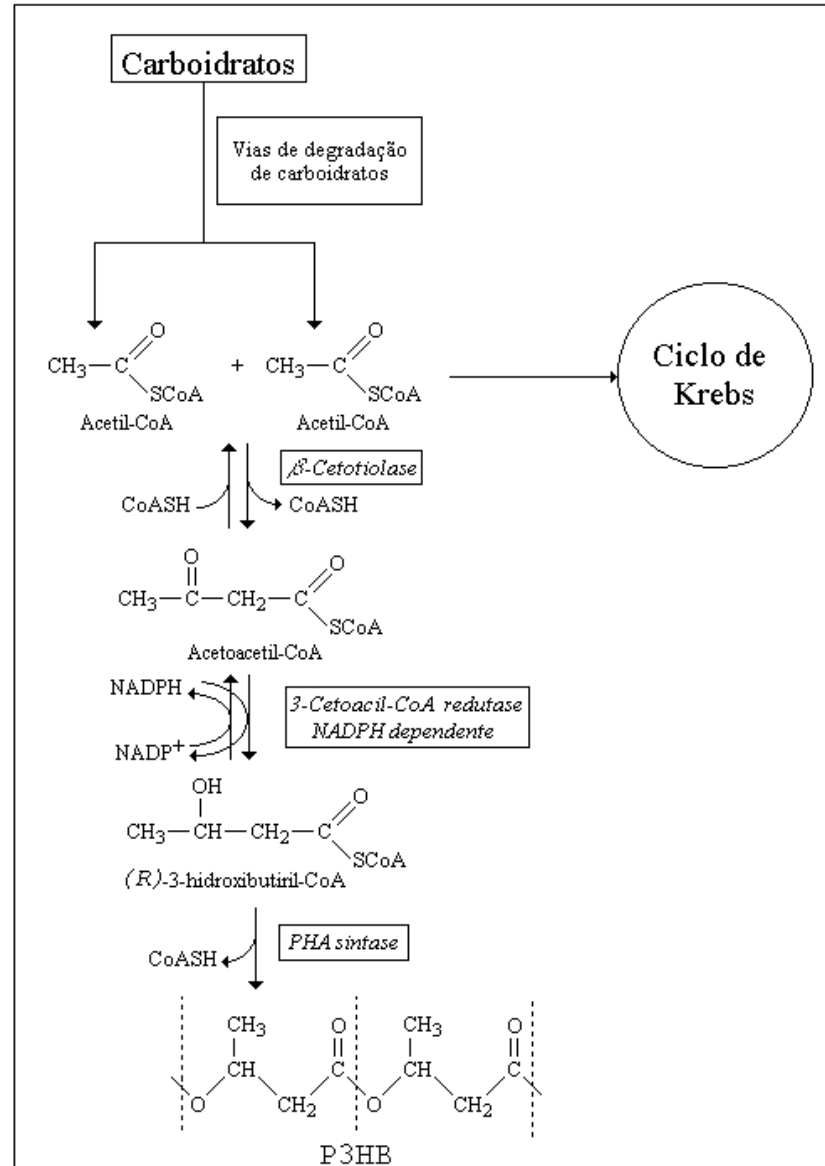
EMP10 : PEP + ADP = PIR + ATP .

CPD : PIR + NAD + CoASH = AcCoA + NADH + CO2 .

OXNAD : NADH + 3 ADP + O = NAD + 3 ATP .

BIOMASSA : 205 G6P + 71 F6P + 897 Rb5P + 361 E4P + 129 G3P + 1496 PG3 + 519 PEP + 2833 PIR + 3748 AcCoA + 1079 KG2 + 1787 OAA + 3547 NAD + 18225 NADPH + 18485 ATP = 1 g X_R + 18485 ADP + 3547 NADH + 18225 NADP + 3748 CoASH .

P3HB - biossíntese



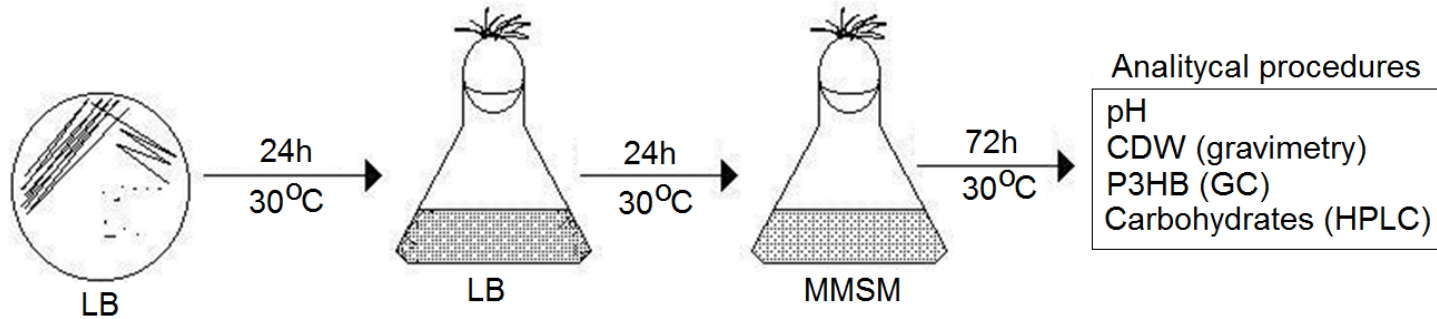
P3HB - biossíntese

PHB1 : $2 \text{ AcCoA} = \text{AcAcCoA} + \text{CoASH} .$

PHB2 : $\text{AcAcCoA} + \text{NADPH} = 3\text{HB-CoA} + \text{CoASH} + \text{NADP} .$

PHB3 : $3\text{HB-CoA} = 3\text{HB} + \text{CoASH} .$

P3HB production from sugarcane carbohydrates



$$Y_{P/C}^G = \frac{X_{HB}}{C_T}$$

$$C_T \begin{cases} \rightarrow C_C \rightarrow Y_{X_R/C_C} = \frac{X_R}{C_C} \\ \rightarrow C_{HA1} \rightarrow Y_{X_{HB}/C_{HB}} = \frac{X_{HB}}{C_{HB}} \end{cases}$$

$$Y_{P/C}^O = \frac{PHB}{PHB \left(\frac{1}{Y_{P/C}^T} - \frac{1}{Y_{X/C}} \right) + \frac{100}{Y_{X/C}}}$$

$$C_T = C_C + C_{HB}$$

$$\frac{X_{HB}}{Y_{P/C}^G} = \frac{X_R}{Y_{X_R/C_C}} + \frac{X_{HB}}{Y_{X_{HB}/C_{HB}}}$$

Dividir por X_T e multiplicar por 100

$$\frac{\%PHB}{Y_{P/C}^G} = \frac{\%CEL}{Y_{X_R/C_C}} + \frac{\%PHB}{Y_{X_{HB}/C_{HB}}}$$

$$Y_{P/C}^G = \frac{\%PHB}{\frac{100}{Y_{X_R/C_C}} - \frac{\%PHB}{Y_{X_R/C_C}} + \frac{\%PHB}{Y_{X_{HB}/C_{HB}}}}$$

$$Y_{P/C}^o = \frac{\text{PHB}}{\text{PHB} \left(\frac{1}{Y_{P/C}^T} - \frac{1}{Y_{X/C}} \right) + \frac{100}{Y_{X/C}}}$$

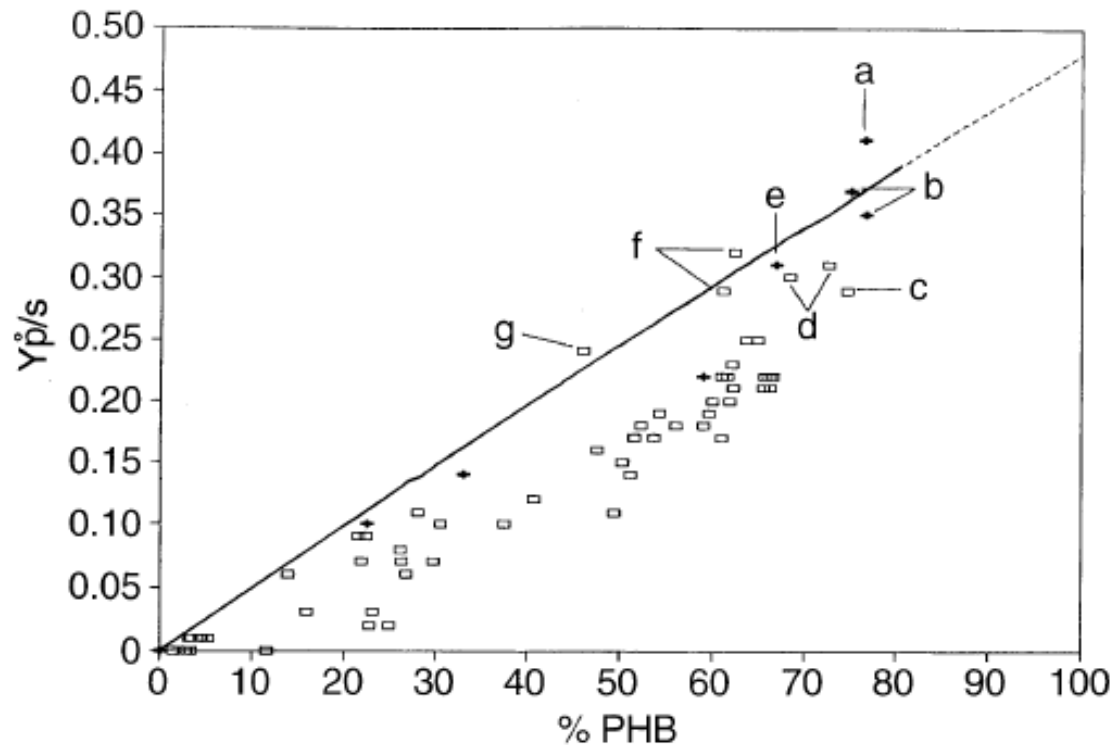


Fig. 1 Relation between $Y_{P/C}^o$ and poly-(3-hydroxybutyrate) (PHB) content for different strains isolated from soil (\square) or obtained from the culture collection ($+$) when glucose plus fructose was used as the carbon source. The line represents the values expected when $Y_{P/C}^T = 0.48$ g/g and $Y_{X/C} = 0.50$ g/g. Points related to strains *A. latus* DSM 1123 (a), *A. eutrophus* DSM 545 (b), IPT-101 (c), IPT-083 (d), *A. eutrophus* DSM 428 (e), IPT-086 (f), and IPT-055 (g) are indicated

$$Y_{P/C}^O = \frac{\text{PHB}}{\text{PHB} \left(\frac{1}{Y_{P/C}^T} - \frac{1}{Y_{X/C}} \right) + \frac{100}{Y_{X/C}}}$$

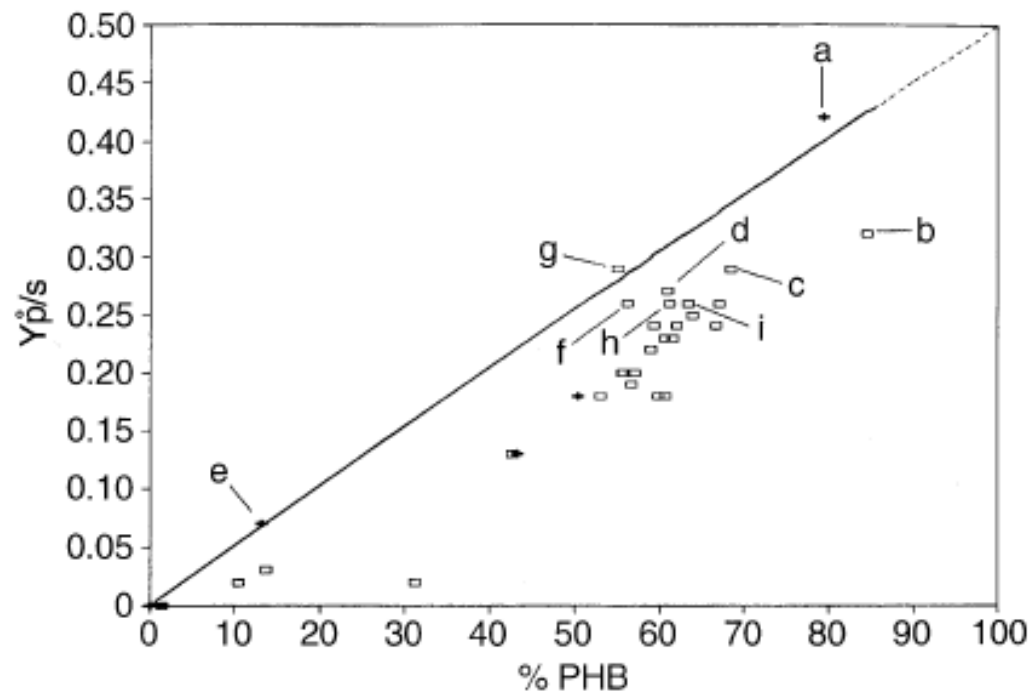


Fig. 2 Relation between $Y_{P/C}^O$ and PHB content for different strains isolated from soil (\square) or obtained from the culture collection ($+$) when sucrose was used as the carbon source. The line represents the expected values when $Y_{P/C}^T = 0.50$ g/g and $Y_{X/C} = 0.52$ g/g. Points related to strains *A. latus* DSM 1123 (a), IPT-044 (b), IPT-101 (c), IPT-083 (d), *A. latus* DSM 1122 (e), IPT-076 (f), IPT-055 (g), IPT-040 (h), and IPT-045 (i) are indicated