



*EP-USP*

*PEF2602.  
Estruturas na Arquitetura I I - Sistemas Reticulados*



# *Tensoestruturas*

*Professores*

*Ruy Marcelo O. Pauletti , Leila Meneghetti Valverdes, Luís Bitencourt*

*1º Semestre 2019*



## ***Estrutura Retesadas ('Tensoestruturas'):***

“aquelas que requerem que seus elementos estejam rete **retesados**,  
Ao invés de **frouxos** ou **enrugados**, para funcionarem a contento”

## ***Estados de uma Tensoestrutura:***



***frouxo***

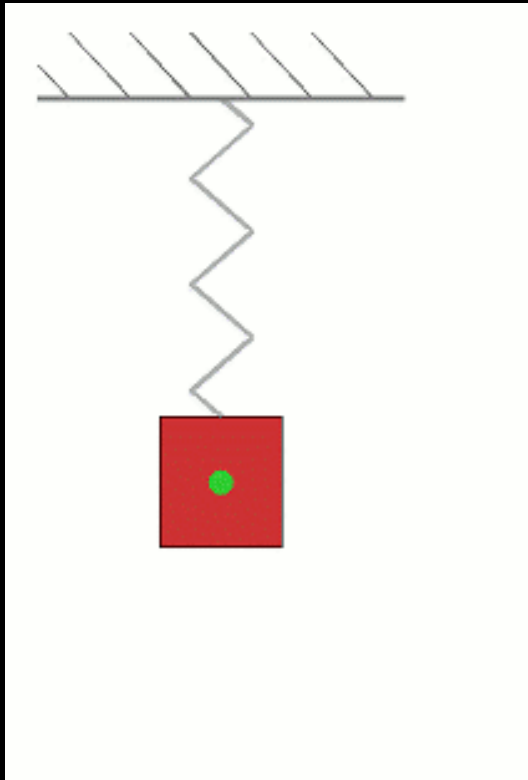


***enrugado***



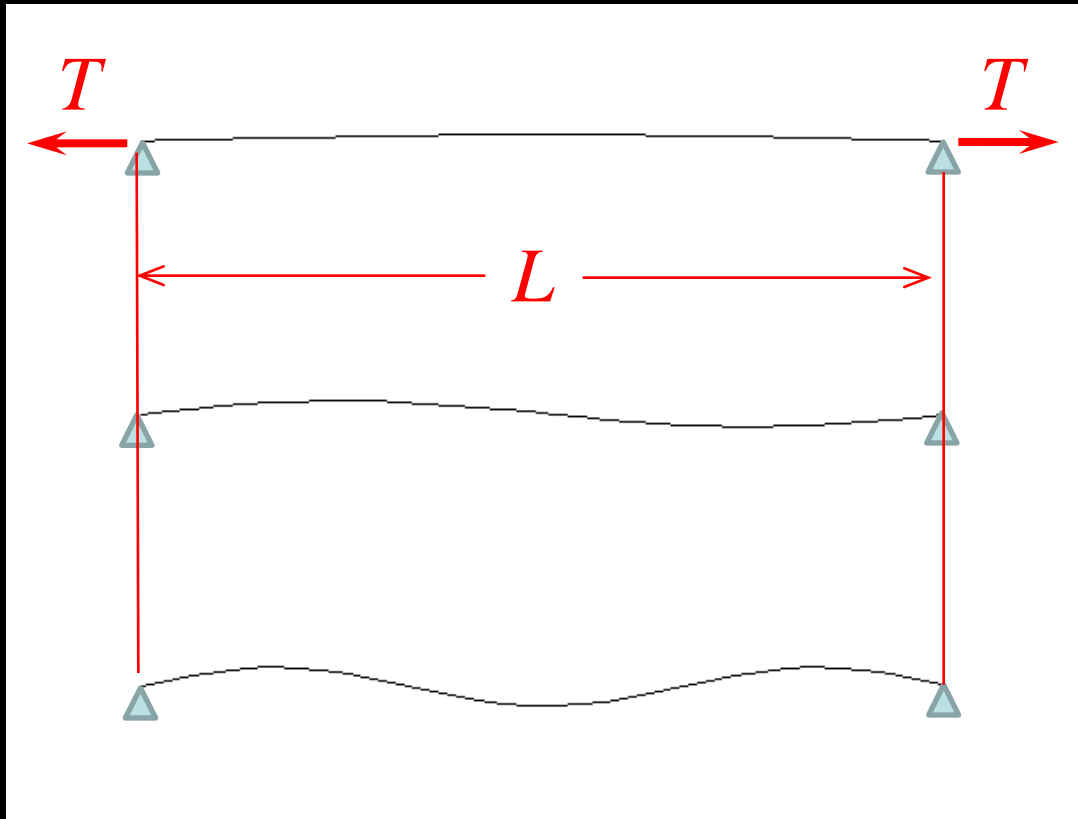
***retesado***

Um sistema massa-mola:



$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

Uma corda vibrando:

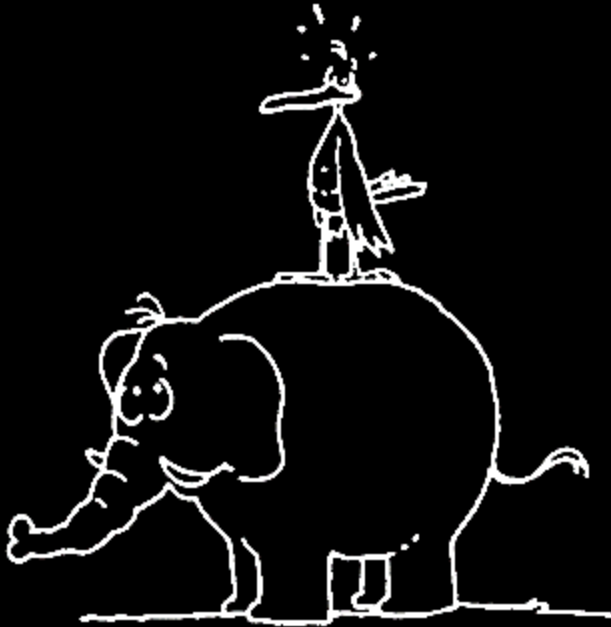


$$f = n\pi \sqrt{\frac{\left(\frac{T}{L}\right)}{m}}$$

'rigidez geométrica'

$$k_g \sim \frac{T}{L}$$

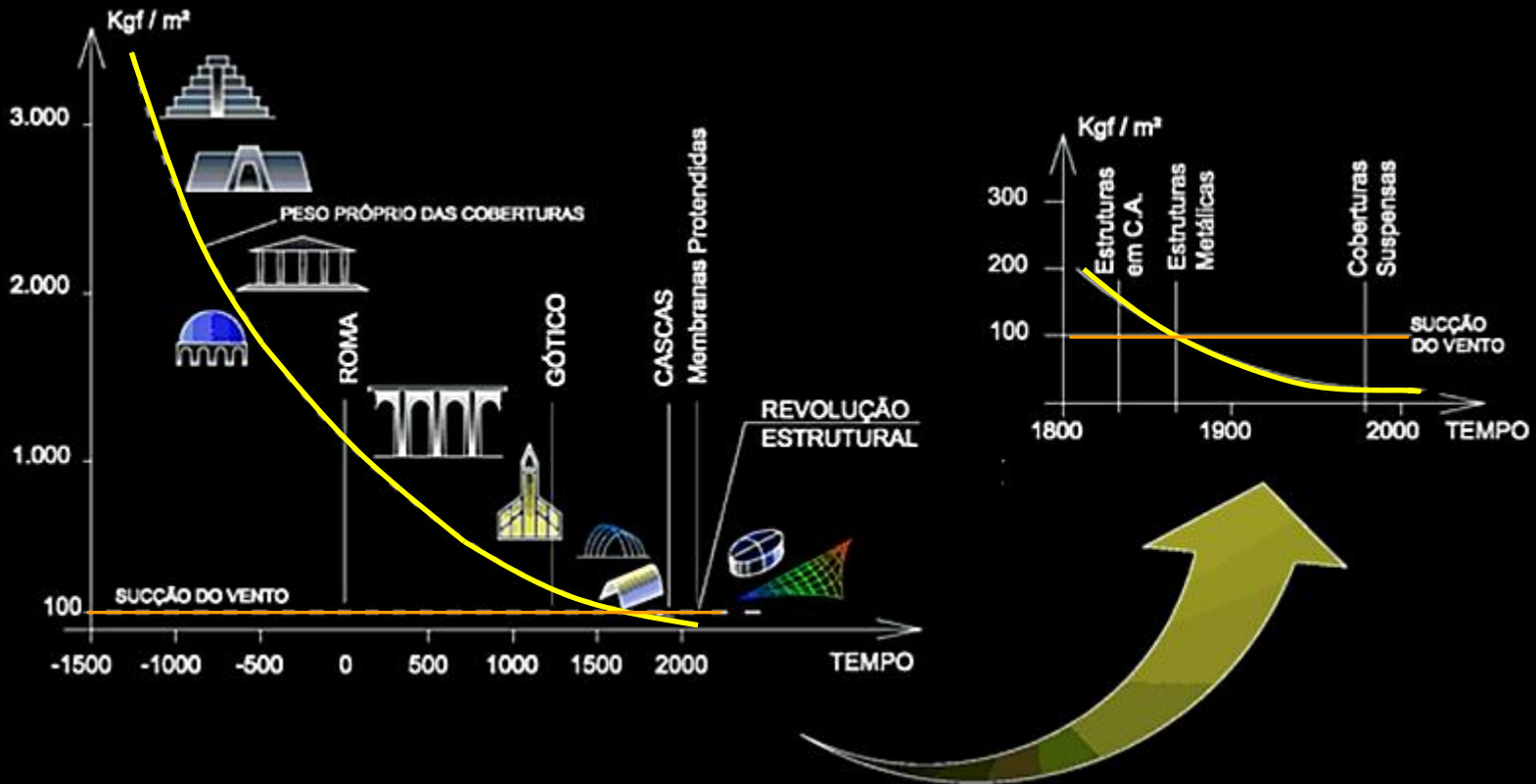
## *Estruturas Leves:*



'peso portante' << 'peso portado'

Desenho de Enzo Pinto, Nápoles, 1985.

# Estruturas Leves:



Adapted from R. Serger, "Structures nouvelles in architecture", in Cahiers du centre d'études architecturales, n. 1, 1967, p. 42.

***“Light structures, structures of light”***

***Horst Berger***





***“Light structures, structures of light”***

***Horst Berger***









Suvarnabhumi Airport,  
Bangkok, Thailand



Select Your Ultimate  
from

CIP

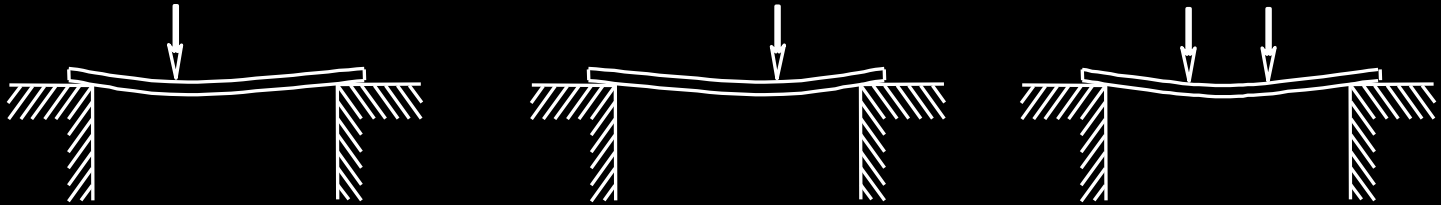




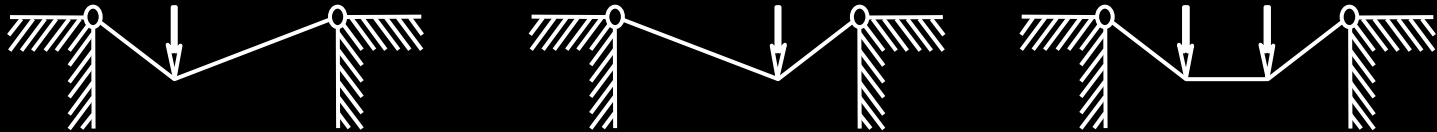
Photo by  
Tim Nugent, 2009



## ***Estruturas Flexíveis:***



*(a) Uma estrutura 'rígida', como uma viga, não muda drasticamente de forma, quando o carregamento varia*



*(b) Uma estrutura 'flexível', como um cabo, pode alterar drasticamente sua forma, quando o carregamento varia*



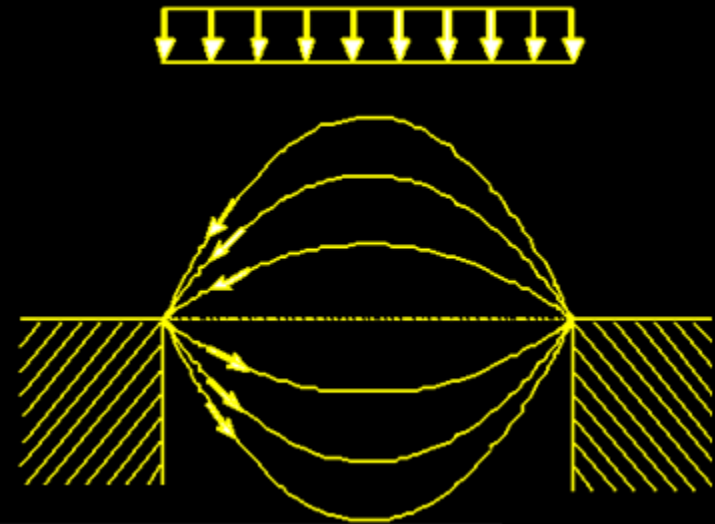
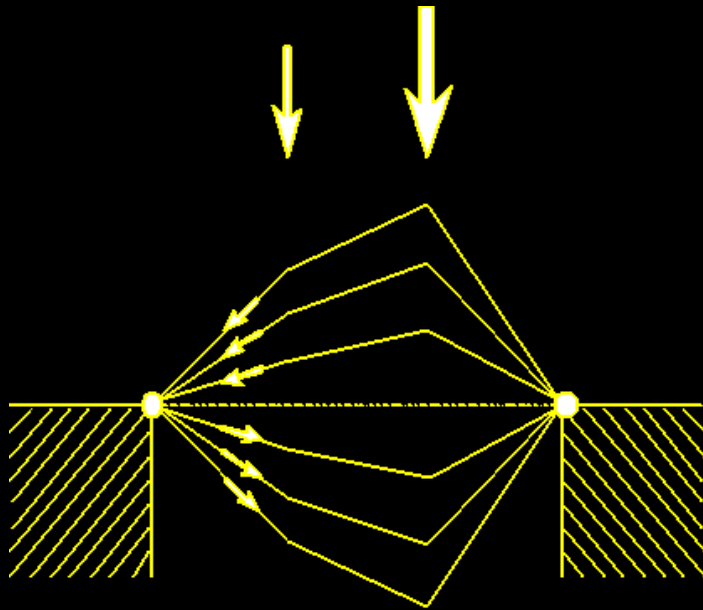
*Estruturas flexíveis deve se conformar às formas funiculares:  
'aquelas que equilibram um conjunto de carregamentos, sem desenvolver esforços de flexão*



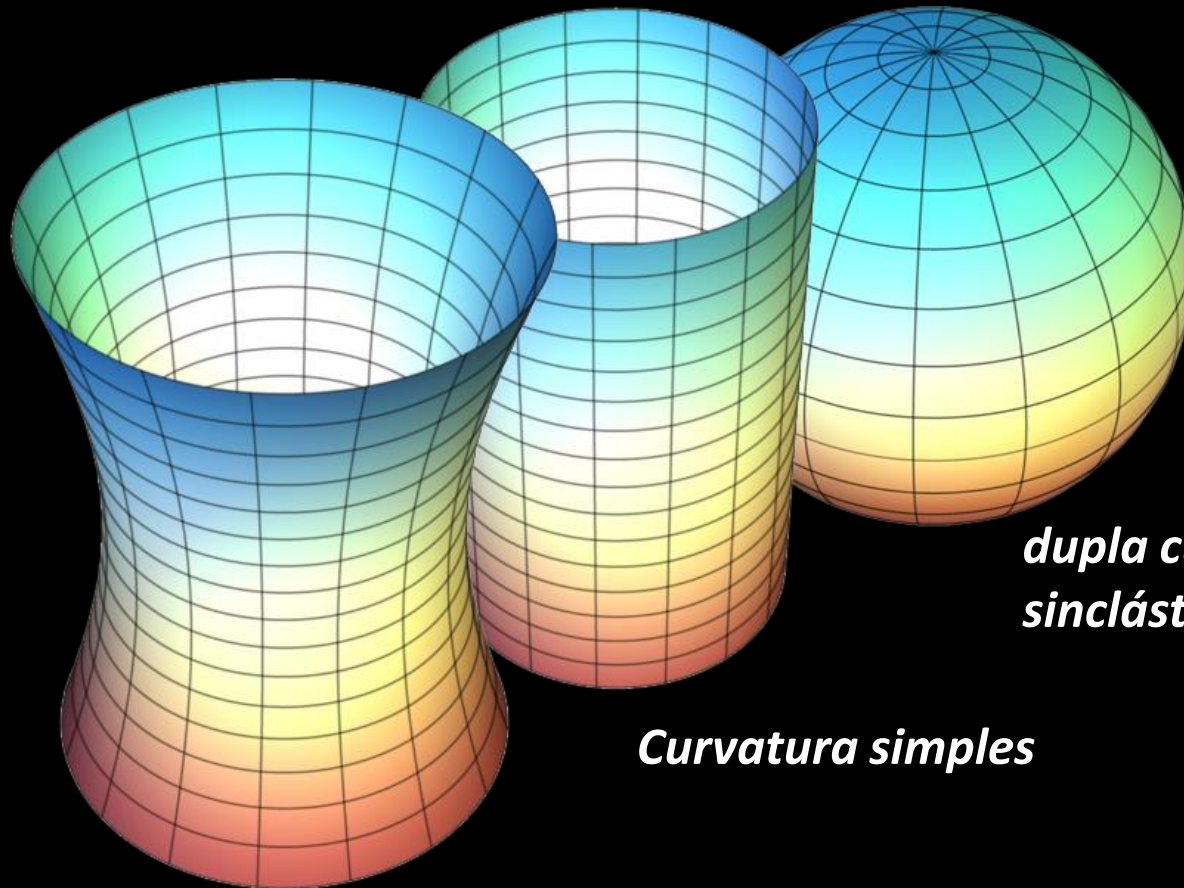




*Cada 'padrão de carregamento' tem associada a si uma 'família de formas funiculares':*



***Membranas e redes de cabos usualmente constituem superfícies de curvatura simples ou dupla:***

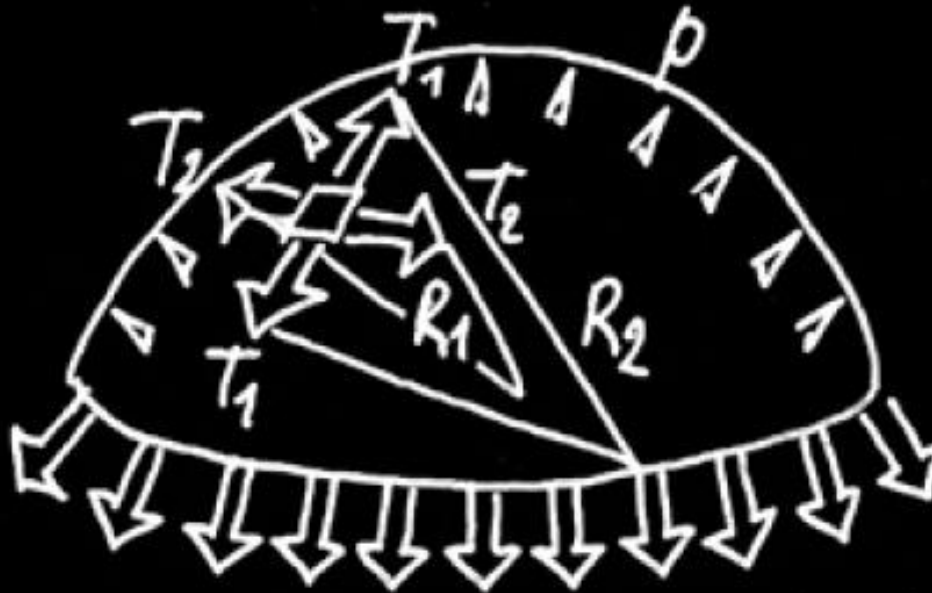


***dupla curvatura,  
anticlastica***

***Curvatura simples***

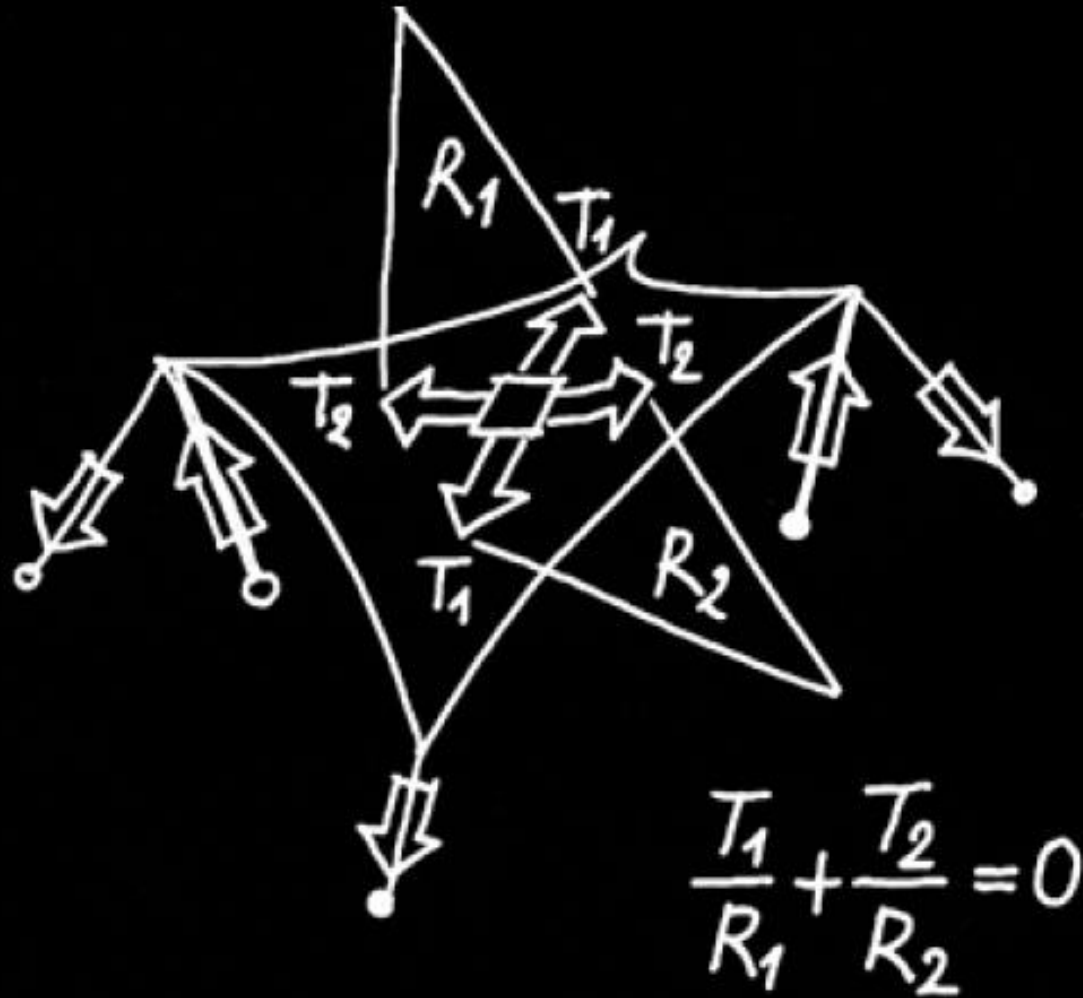
***dupla curvatura,  
sinclástica***

*Membranas pneumáticas em geral são sinclásticas:*

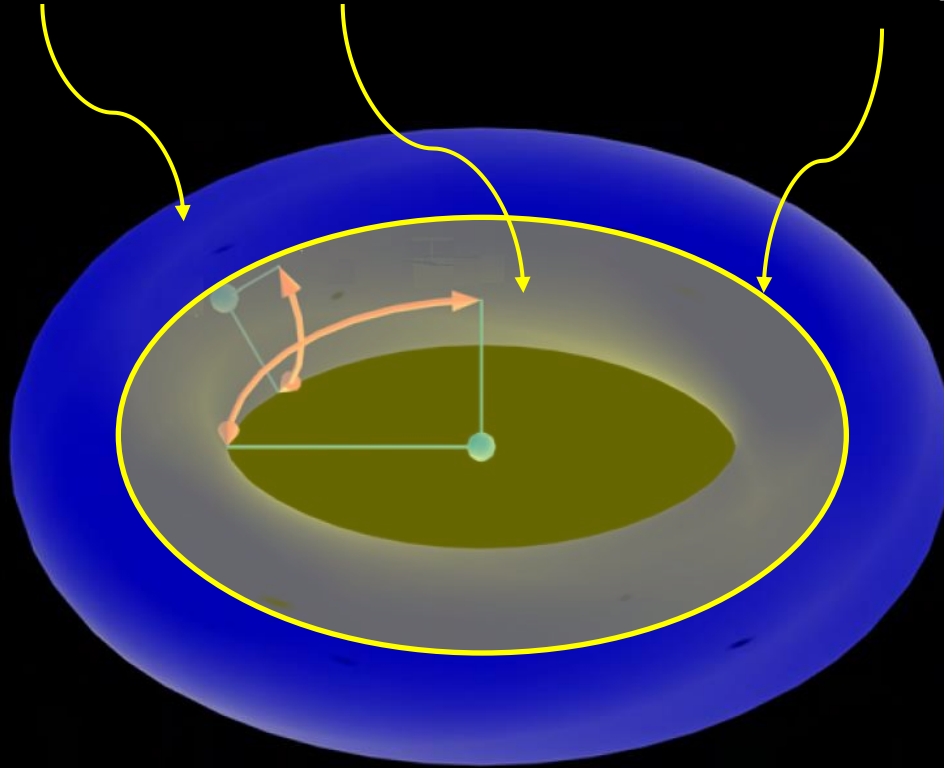


$$\frac{T_1}{R_1} + \frac{T_2}{R_2} = p$$

***Porém tendas são sempre anticlásticas or planas!***



***Estruturas pneumáticas podem apresentar zonas  
sinclásticas, anticlásticas e de curvature simples:***





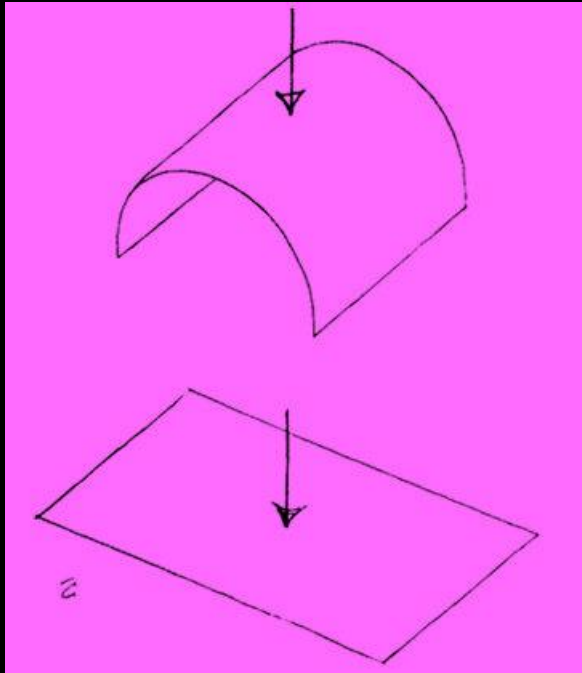


**SAVE  
THE  
CLIMATE**

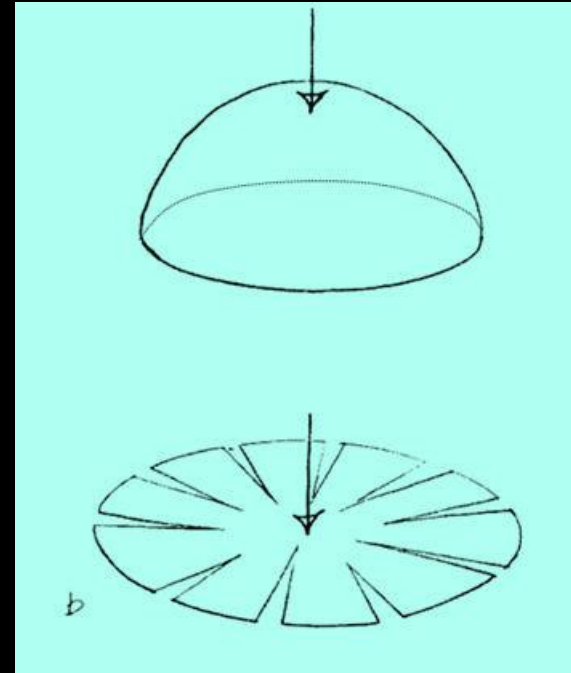
GREENPEACE



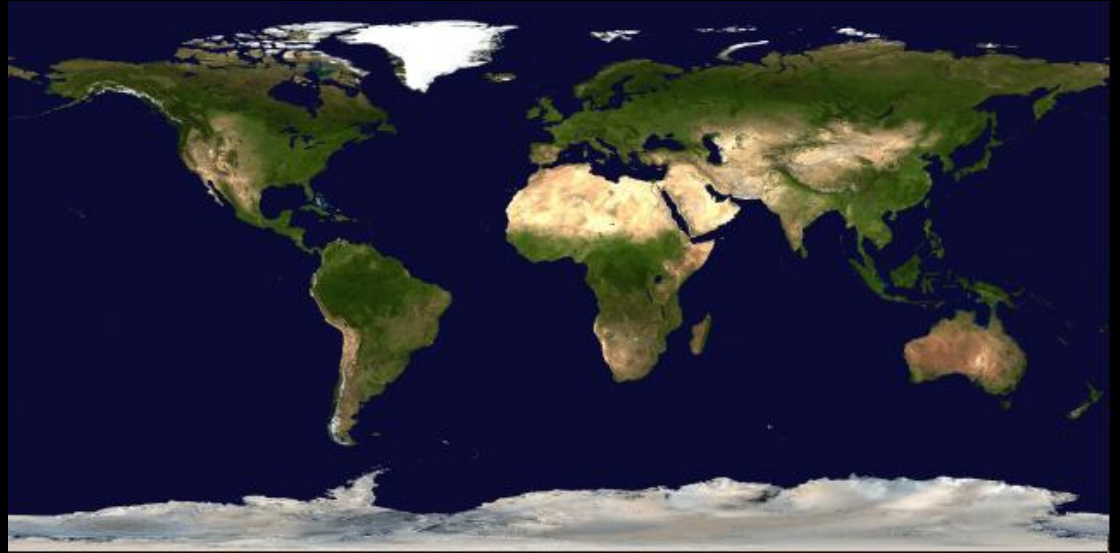
# Planificação



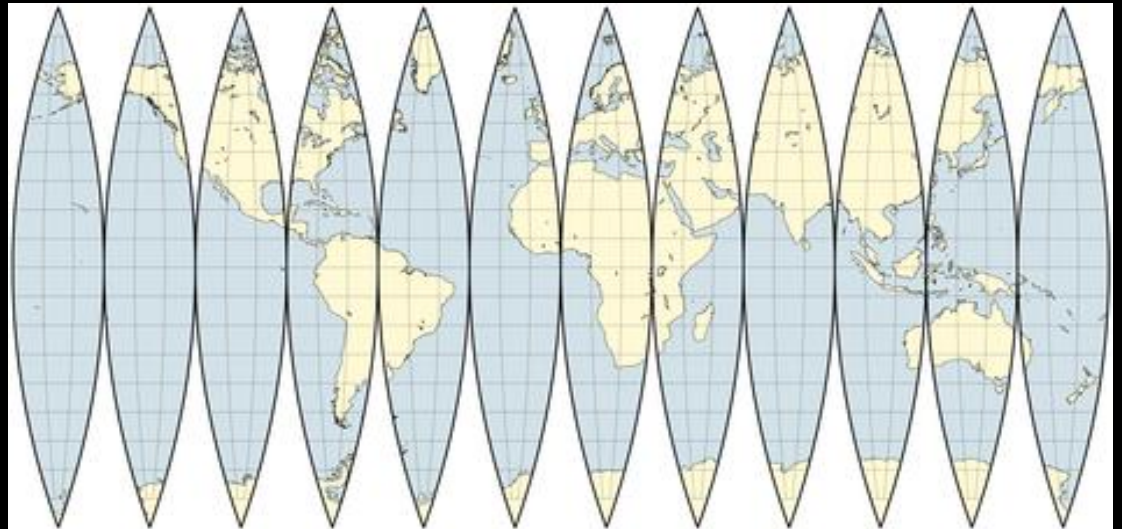
**Superfícies de curvatura simples  
podem ser planificadas sem distorção**



**Superfícies de dupla curvatura  
sofrem distorção quando planificadas**



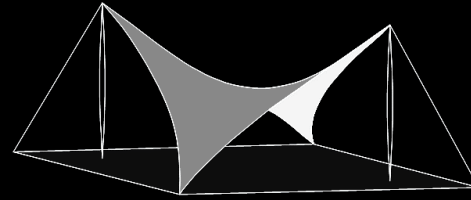
Mercator projection



A gore map using Apian's first projection.

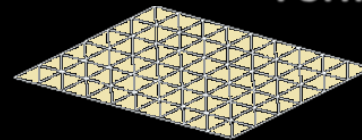
# O Processo de Projeto das Estruturas Retesadas

**INTENÇÃO ARQUITETÔNICA:**

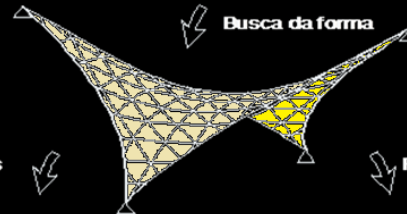


**PROJETO / ANÁLISE:**

**Forma inicial, não-viável**



**Busca de Forma**



**Forma final, viável**

Determinação dos padrões de corte

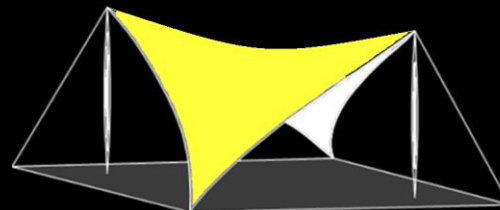
Resposta aos carregamentos

**Padronagem:**

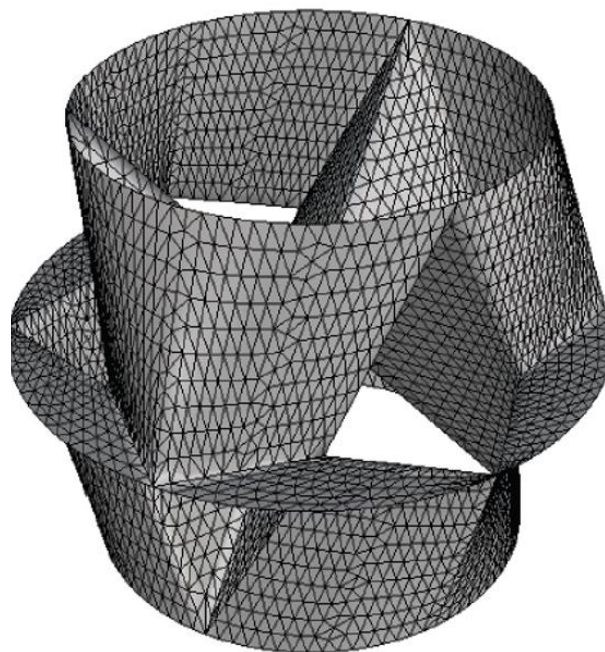
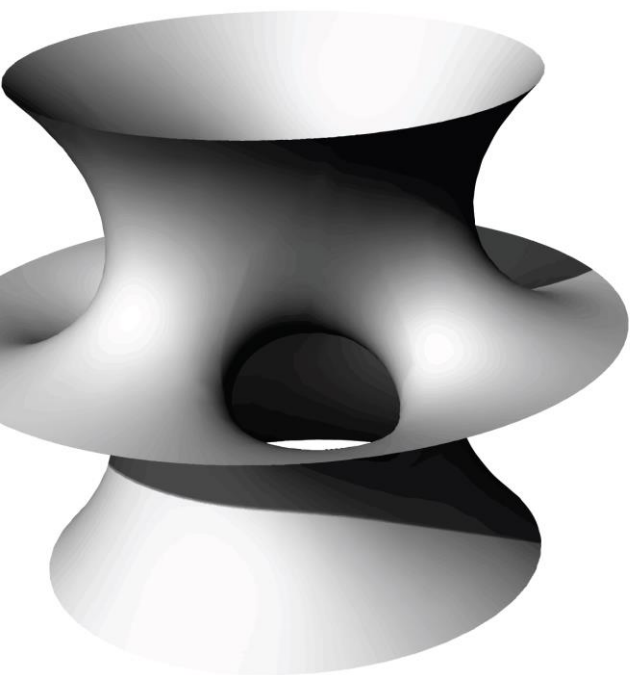


**Análise de Carregamentos**

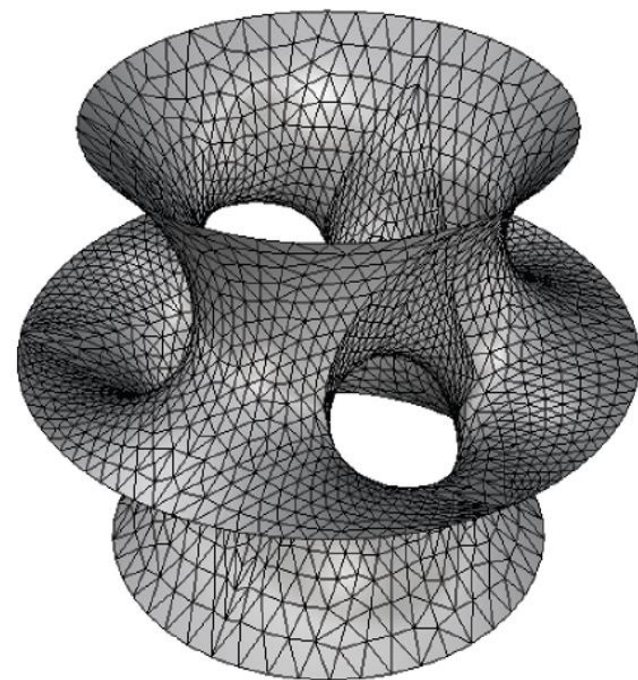
**SOLUÇÃO DE PROJETO:**



# Uma escultura de membrana (Princeton, 2017)

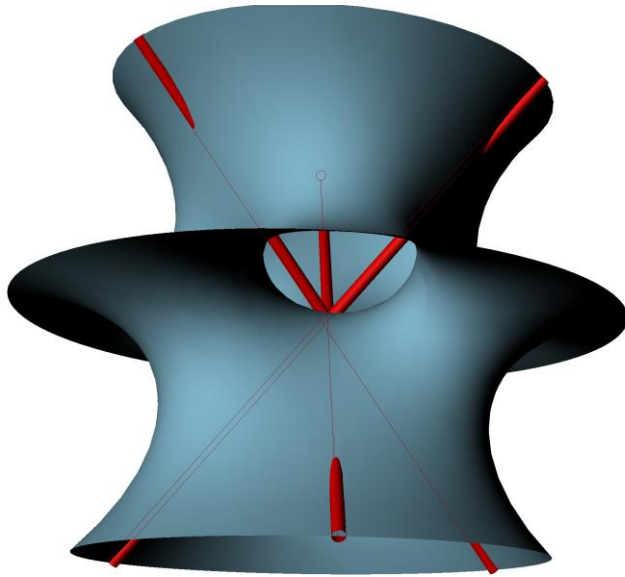


INITIAL MESH

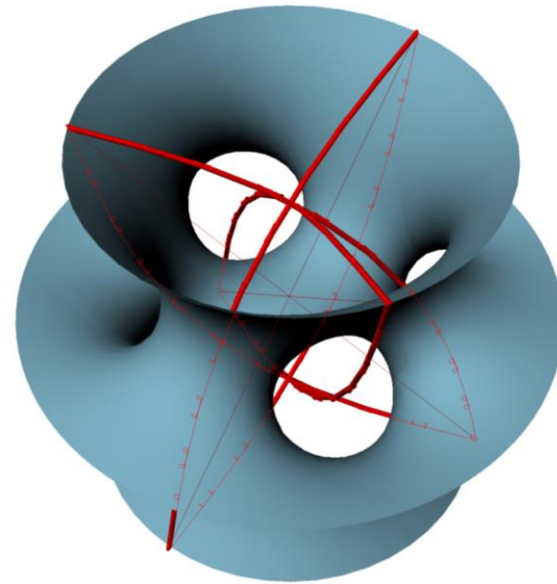


FINAL MESH

## Sistema de retesamento de flexão ativa

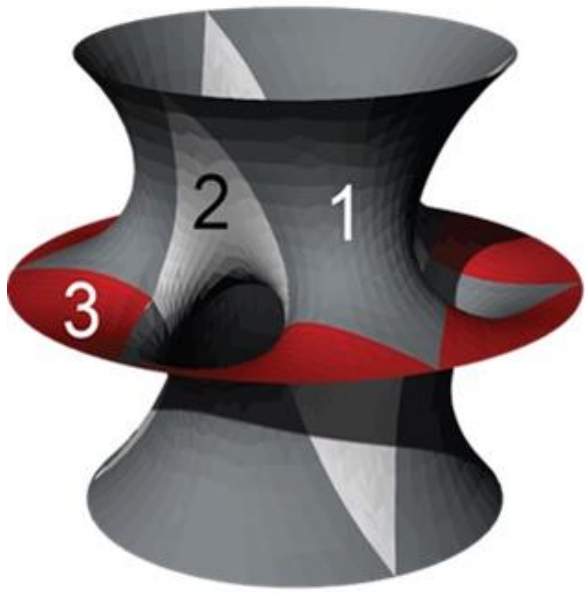


Barras retas interferem com a superfície da membrana

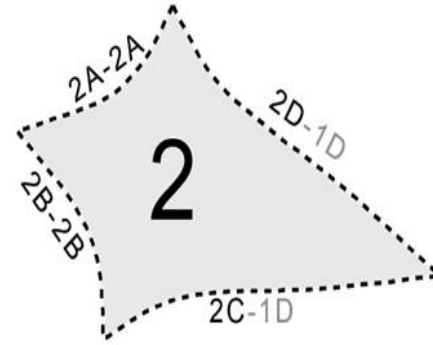
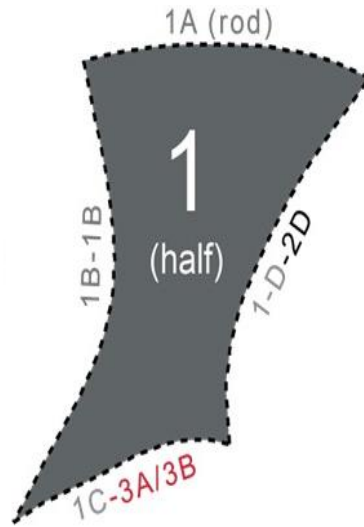


Barras fletidas podem ser acomodadas e provêm um Sistema de ativação (retesamento) muito conveniente

# PADRONAGEM



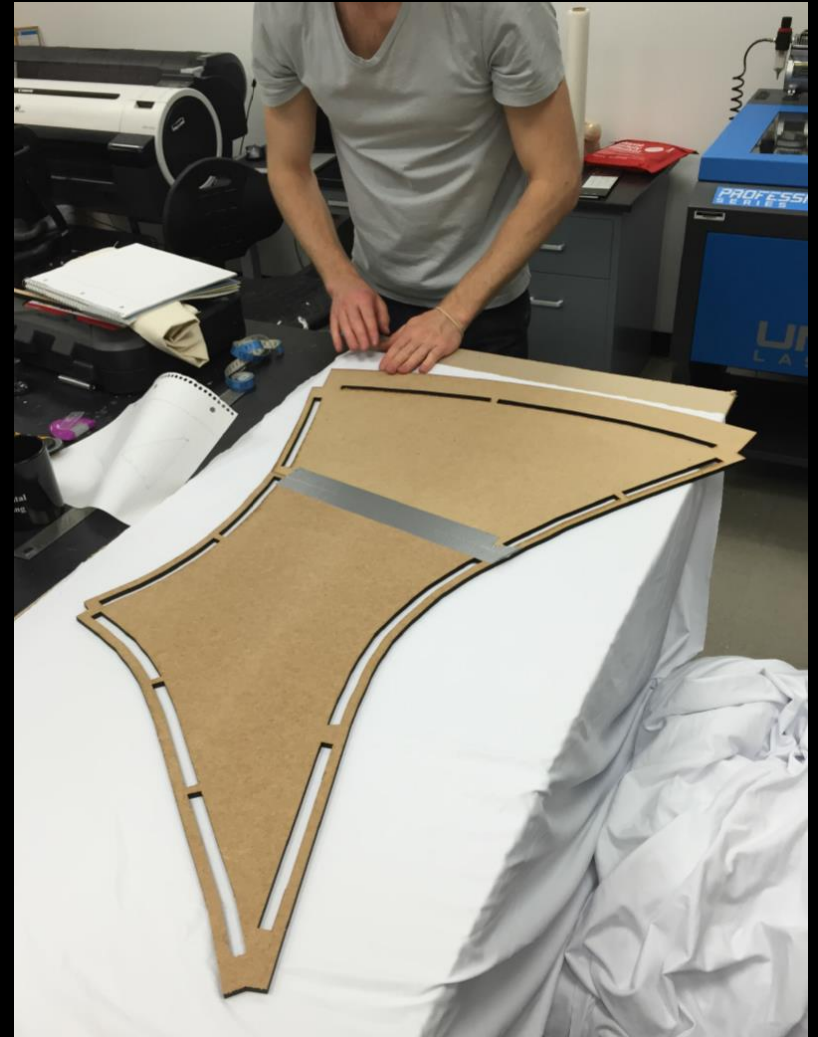
PERSPECTIVE VIEW

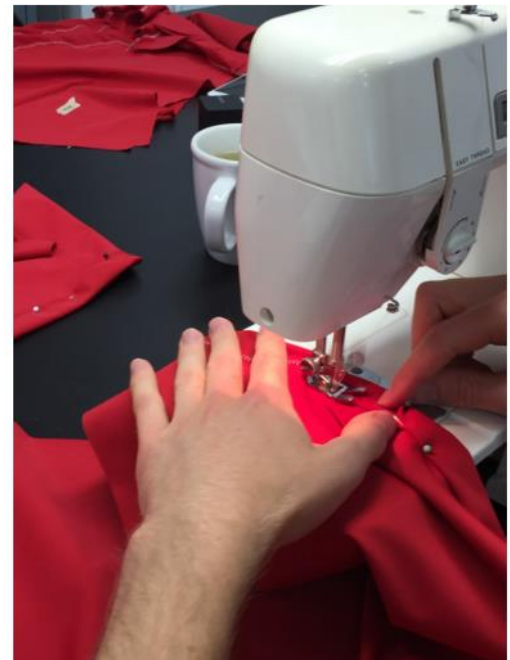
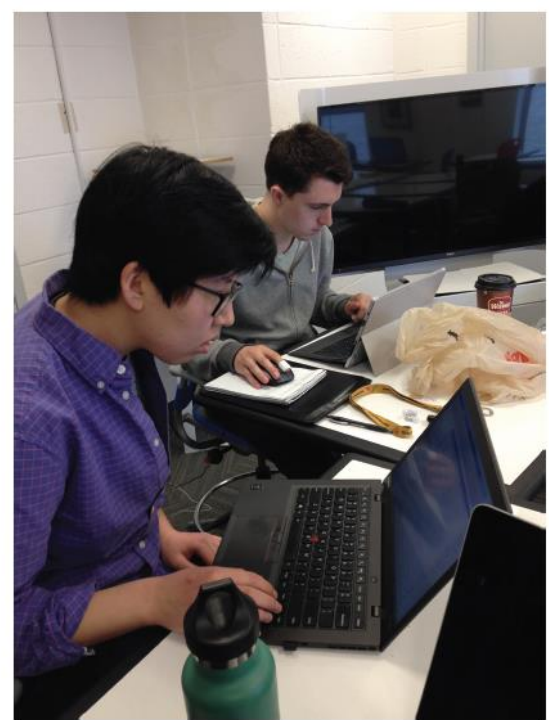
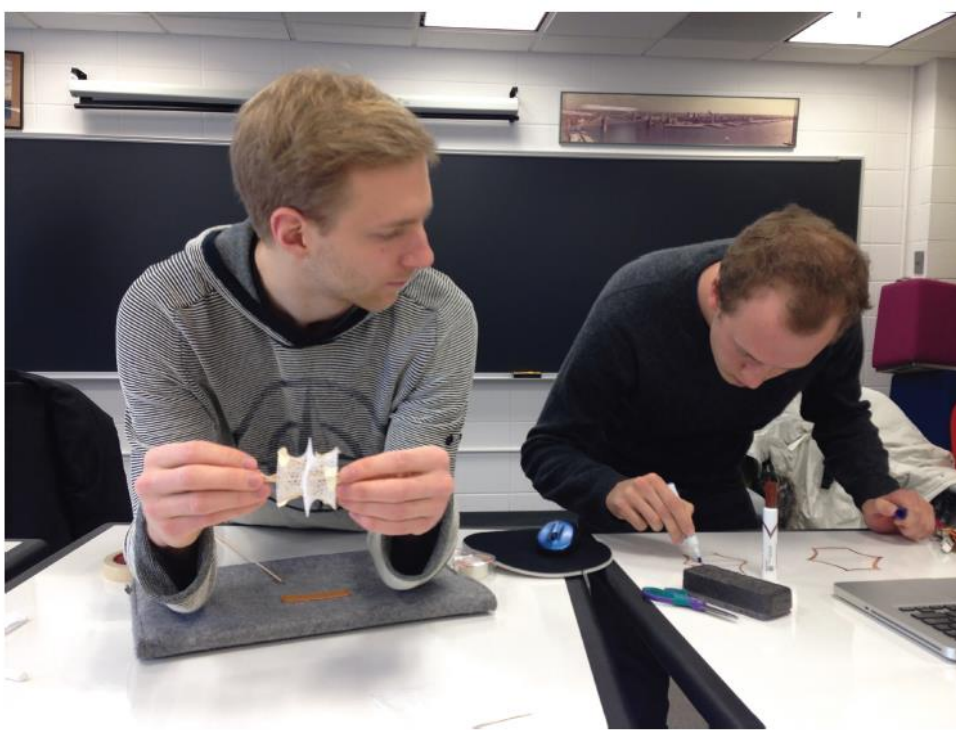


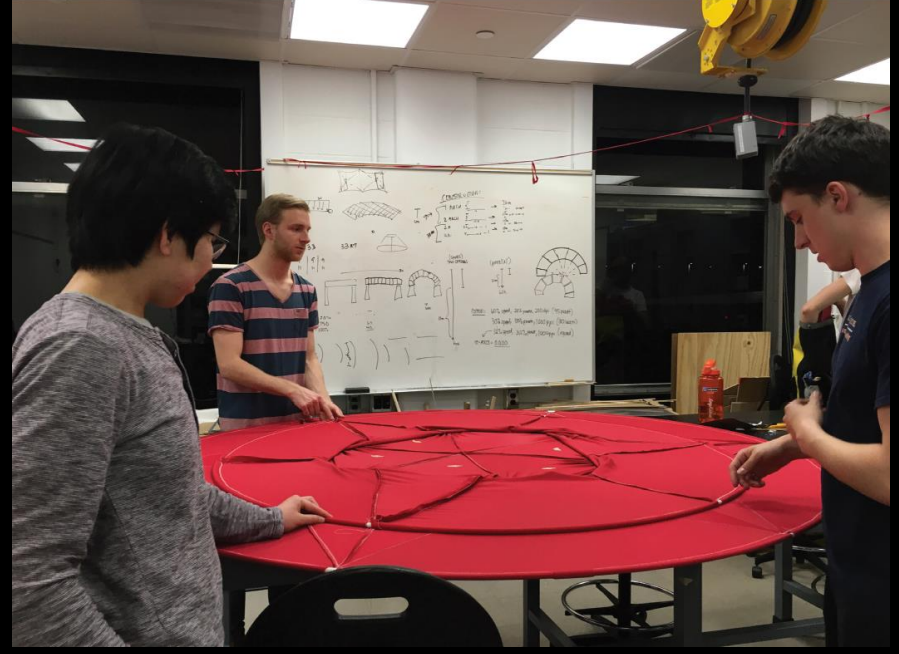
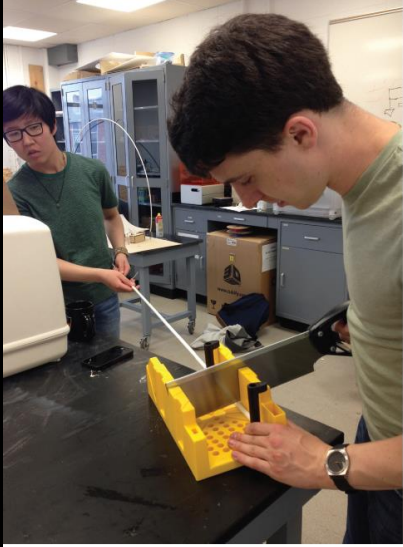
FLATTENED PATTERNS

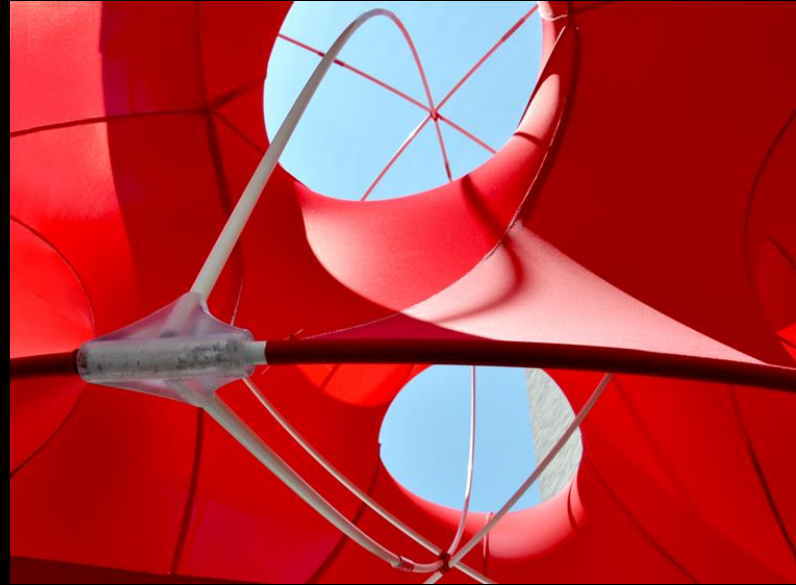


# PRODUÇÃO





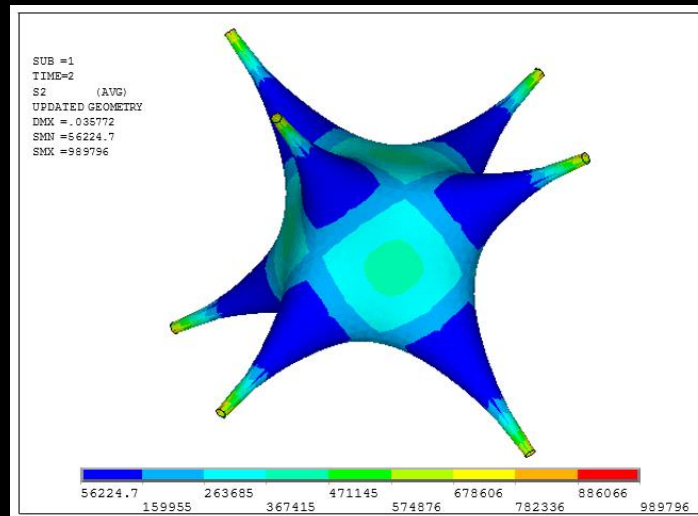
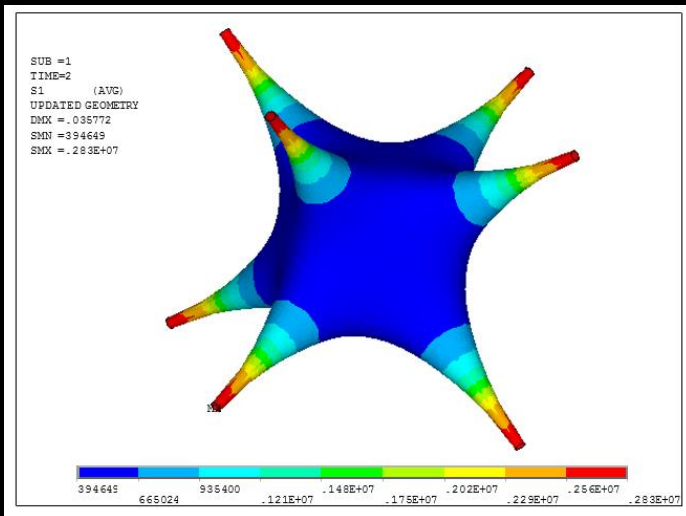
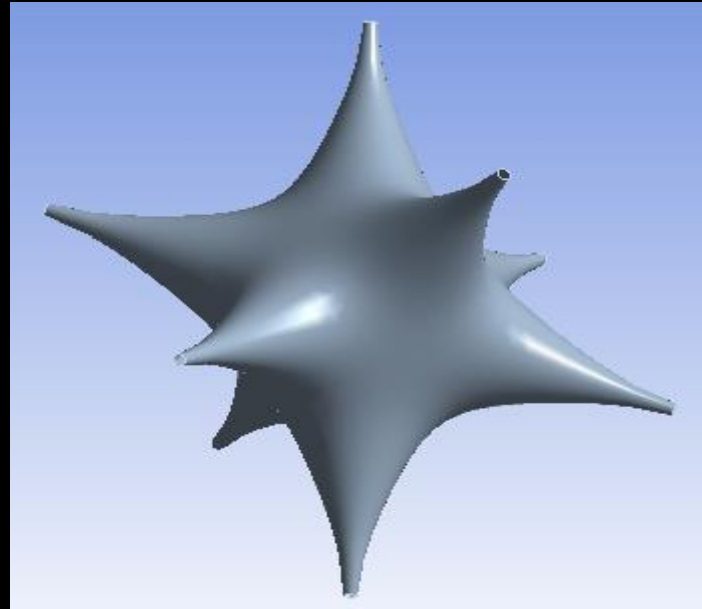
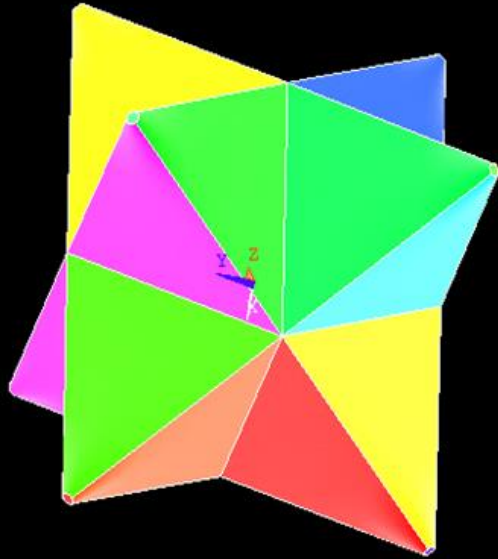




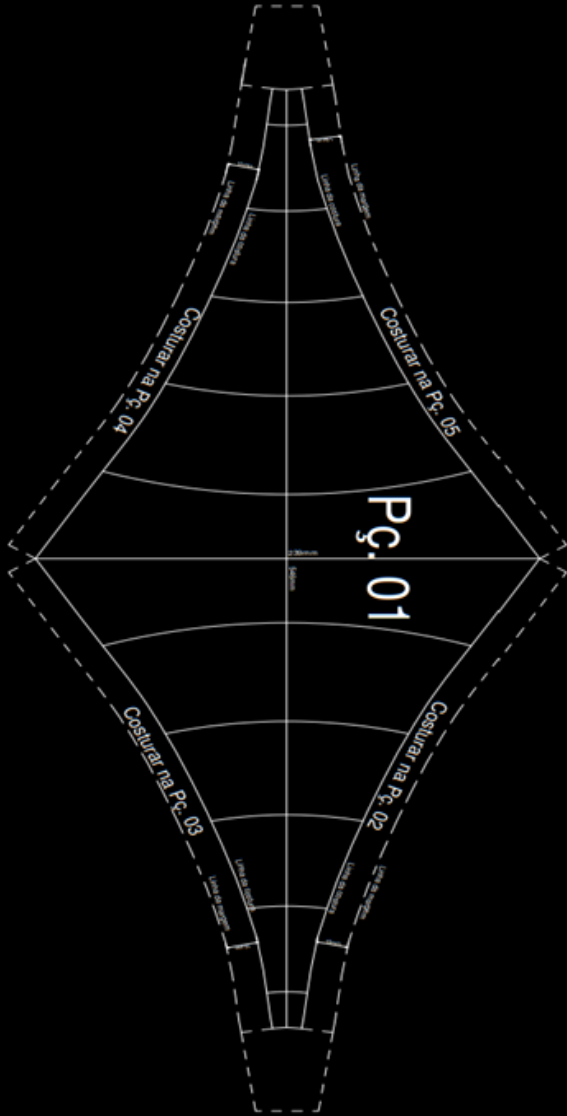
# A escultura exibida no hall of Universidade de Hamburgo (2017)



# The Octahedral cusped (São Paulo, 2017)







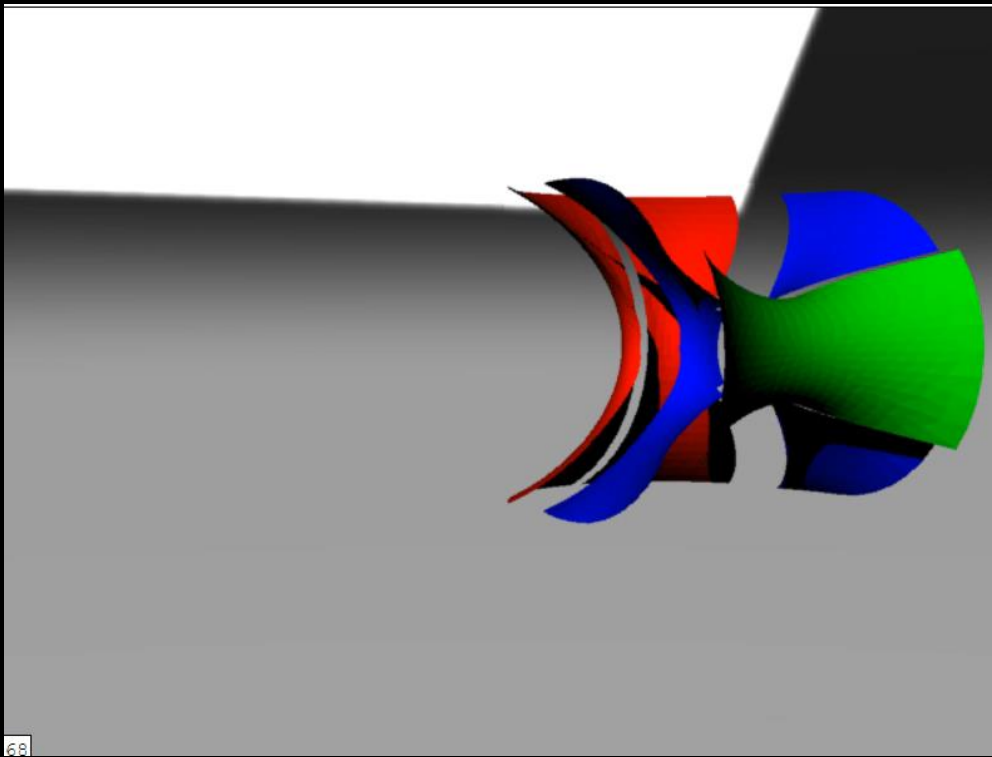




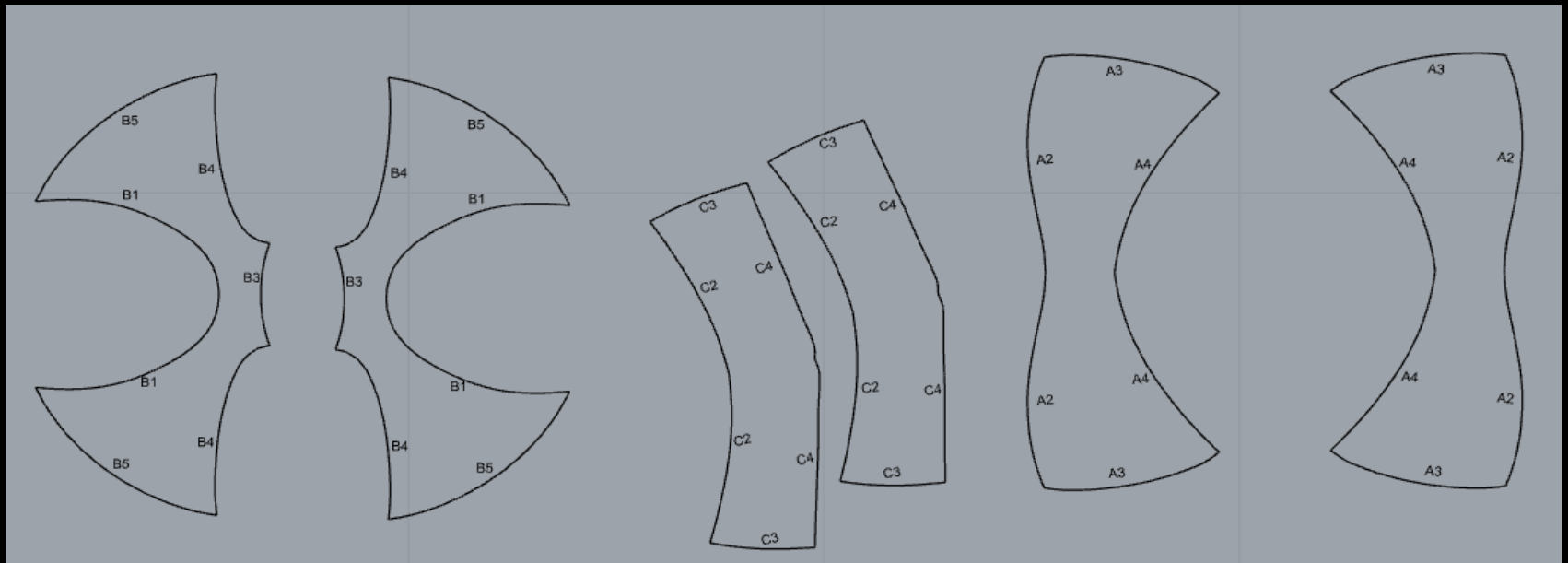


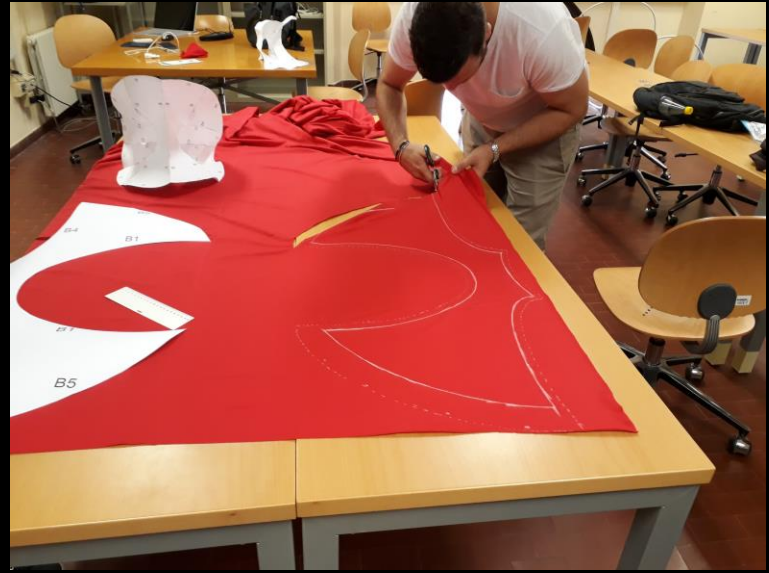
# An Enneper surface with a Handle (Padua, 2018)



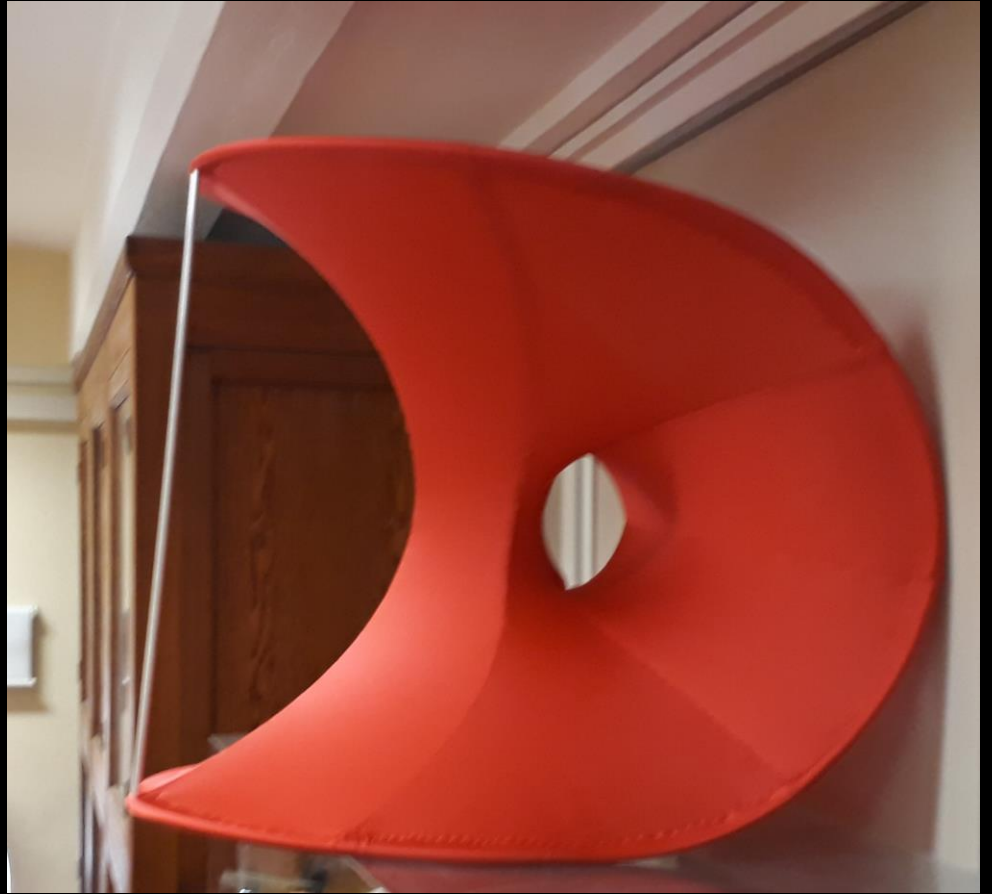


68









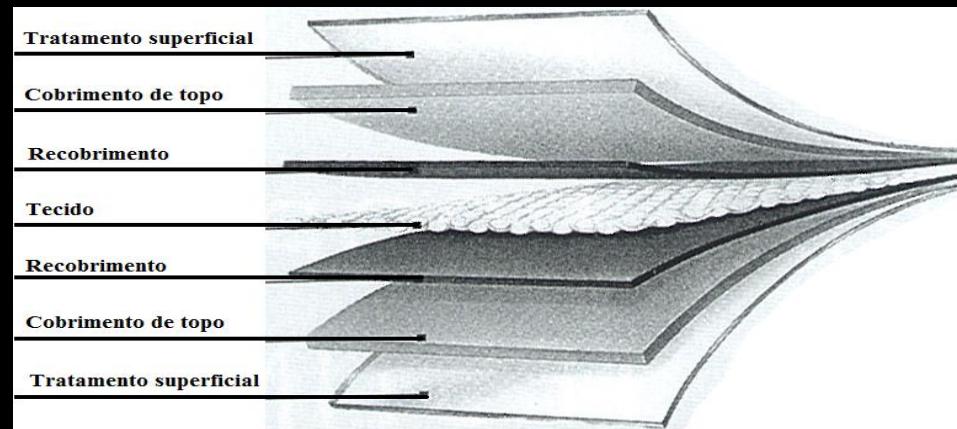
# Tecidos técnicos



Produção de um tecido de fibra de vidro (Pudenz, 2004)



Recobrimento com PTFE (Pudenz, 2004)

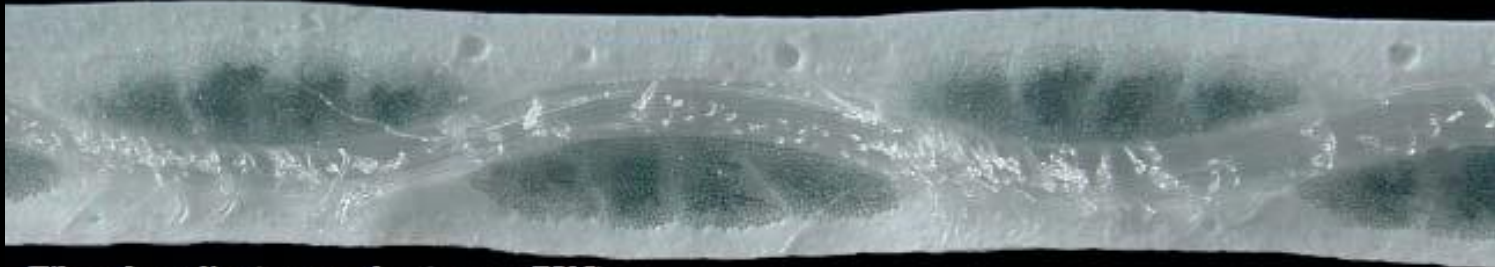


Diferentes camadas de um tecido técnico Blum *et al* (2004)





**Fibra de vidro recoberta com PTFE**



**Fibra de poliéster recoberta com PVC**

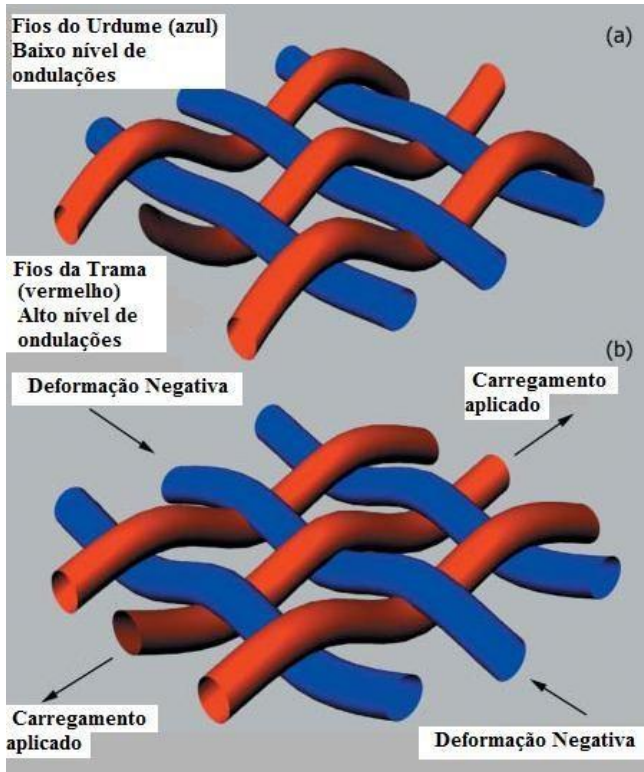
Seções transversais de tecidos de fibra de vidro e poliéster (BRIDGENS et al, 2004).

# PTFE-covered fiberglass fabric (1969)

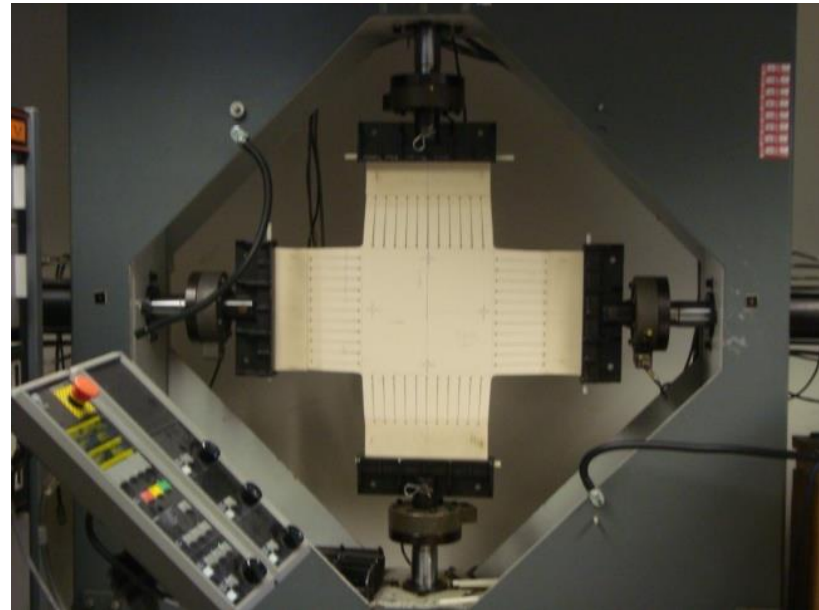
DuPont, Birdair, Chemfab & Owens-Corning



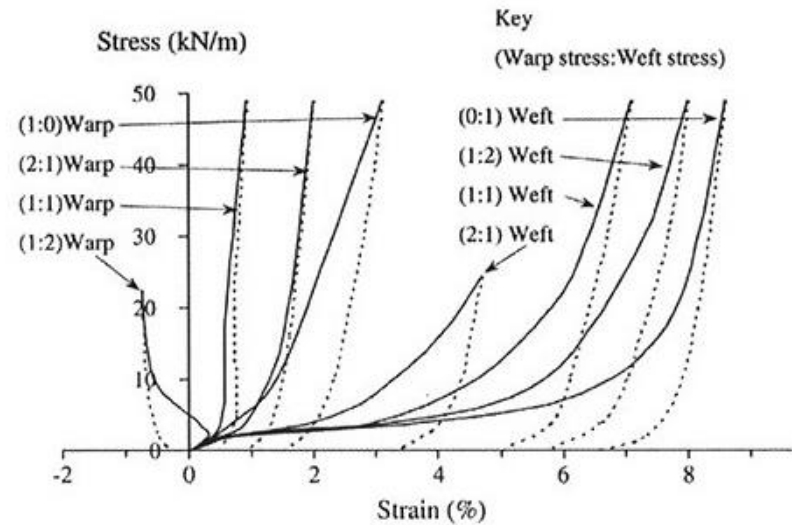
**Neil Armstrong's Suit  
Apollo 11 Project (1969)**



*Crimp Interchange*,  
Bridgens et al. (2004).



**Biaxial test (Chivante, 2009)**



$\sigma$ - $\epsilon$  curves for a PTFE-fiberglass fabric  
(warp = urdume; weft = trama), Kato *et al* (1999)

## Comparison between different types of structural fabrics

|                                   | PVC coated polyester fabrics     | PTFE coated glass fabrics           | Silicone coated glass fabrics           | PTFE coated PTFE fabrics |
|-----------------------------------|----------------------------------|-------------------------------------|---|--------------------------|
| Tensile strength warp/weft (kN/m) | 115/102                          | 124/100                             | 107/105                                 | 84/80                    |
| Fabric weight (g/m <sup>2</sup> ) | 1200 (type 3)                    | 1200 (type G5)                      | 1100                                    | 830                      |
| Trapezoidal tear warp/weft (N)    | 800/950                          | 400/400                             | 960/700                                 | 925/925                  |
| Visible light transmission (%)    | 10-15                            | 10-20                               | < 80                                    | 19-38                    |
| Flexibility/crease recovery       | high                             | low                                 | high                                    | high                     |
| Fire reaction                     | M2 (NFP 92 503)<br>B1 (DIN 4102) | M1 (NFP 92 503)<br>B1/A2 (DIN 4102) | A (ASTM E-108)<br>no toxicity of smokes |                          |
| Cleaning                          | easier with top coats            | self cleaning                       | self cleaning                           | self cleaning            |
| How to make the seams             | by high frequency                | thermally                           | vulcanisation                           | stitching                |
| Life span (years)                 | > 15-20                          | > 25                                | > 25                                    |                          |
| Cost                              | low                              | high                                | high                                    |                          |

## Comparação de usos e custos de diferentes tipos de tecido (incluindo elementos complementares)

| Fabric type  | Typical use  | Cost comparison*                 |
|--|--|----------------------------------|
| PTFE-coated fiberglass   | Large scale permanent structures Class A<br>ASTM E-108                         | \$75 – 100 per ft. <sup>2</sup>  |
| Silicone-coated fiberglass   | Large scale permanent structures Class A<br>ASTM E-108                         | \$75 – 100 per ft. <sup>2</sup>  |
| Vinyl-coated polyester   | Temporary and permanent structures   | \$50 – 75 per ft. <sup>2</sup>   |
| Woven PTFE   | (More pliable than standard PTFE) Retractable roofs, structures                | \$85 – 125 per ft. <sup>2</sup>  |
| ETFE   | High transparency (97%) Atria, indoor parks, biospheres, skylight applications | \$100 – 125 per ft. <sup>2</sup> |
| HDPE (High Density Polyethylene)   | Shade structures/systems   | \$25 – 50 per ft. <sup>2</sup>   |
| Laminates  | Tents, awnings & canopies  | \$35 – 50 per ft. <sup>2</sup>   |
| *2008 dollars. Surface area X cost per ft <sup>2</sup> = Budget Plan area (length X width) X Shape factor (H) = Surface area |  |                                  |

*Fabric Architecture 2009 Sourcebook*



## Tecidos de poliéster recobertos com PVC

| Type                                     | 1       | 2       | 3         | 4           | 5           |
|--|---------|---------|-----------|-------------|-------------|
| <b>Surface weight (g/m<sup>2</sup>)</b>  |         |         |           |             |             |
| French design guide                      | 720     | 1 000   | 1 200     | 1 400       | 2 000       |
| WG Messe Frankfurt                       | 800     | 900     | 1 050     | 1 300       | 1 450       |
| <b>Yarn linear density (dtex)</b>        |         |         |           |             |             |
| French design guide                      |         |         |           |             |             |
| WG Messe Frankfurt                       | 1 100   | 1 100   | 1 670     | 1 670       | 2 200       |
| <b>Tensile strength warp/weft (kN/m)</b> |         |         |           |             |             |
| French design guide                      | 60/60   | 84/80   | 110/104   | 120/130     | 160/170     |
| WG Messe Frankfurt                       | 60/60   | 88/79   | 115/102   | 149/128     | 196/166     |
| <b>Trapezoidal test warp/weft (N)</b>    |         |         |           |             |             |
| French design guide                      |         |         |           |             |             |
| WG Messe Frankfurt                       | 310/350 | 520/580 | 800/950   | 1 100/1 400 | 1 600/1 800 |
| <b>Yarn number per cm warp/weft</b>      |         |         |           |             |             |
| French design guide                      |         |         |           |             |             |
| WG Messe Frankfurt                       | 9/9     | 12/12   | 10.5/10.5 | 14/14       | 14/14       |

**Tecidos Poliéster / PVC Resistência ao fogo – Incêndio Shopping Nova América, RJ - 2015**



**Tecidos Poliéster / PVC Resistência ao fogo – Incêndio Shopping Nova América, RJ - 2015**



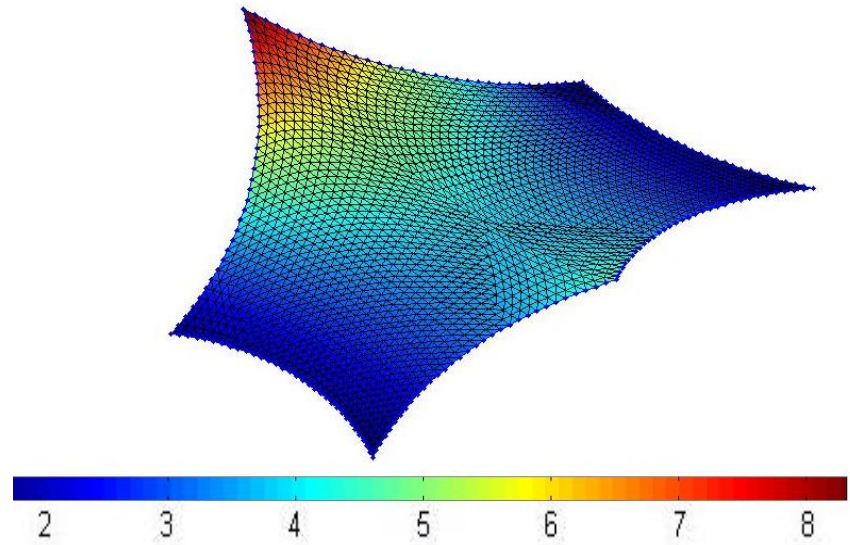
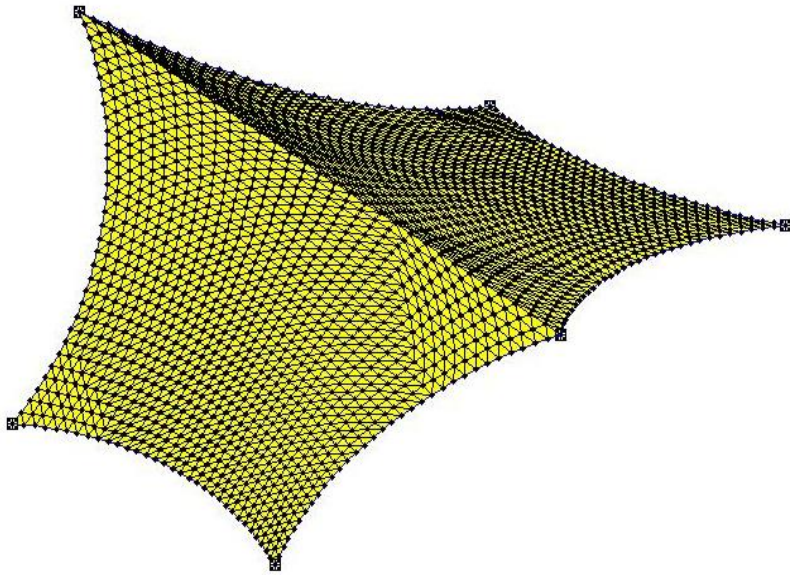


**Tecidos Poliéster / PVC Resistência ao fogo – Incêndio Shopping Nova América, RJ - 2015**

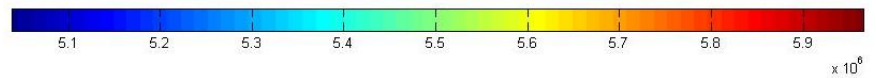
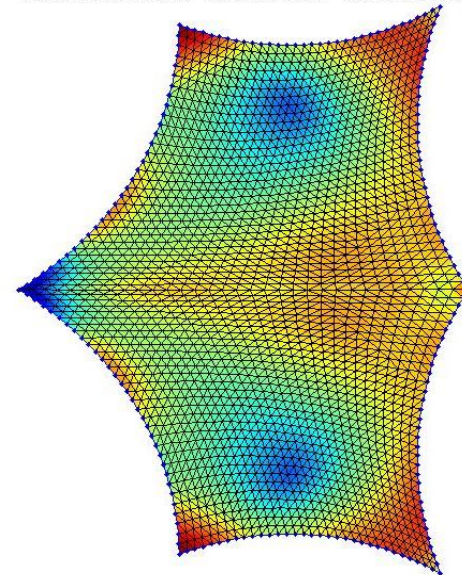
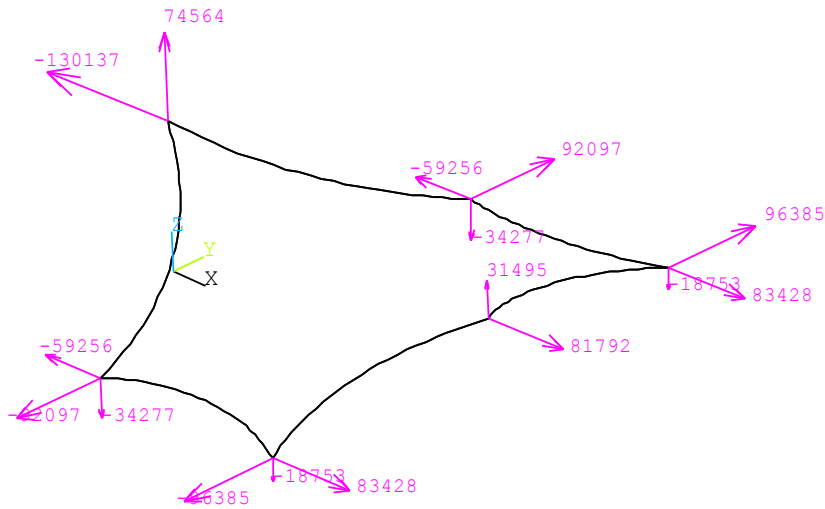


## Membrana de cobertura do Memorial dos Povos de Belém do Pará (2006)

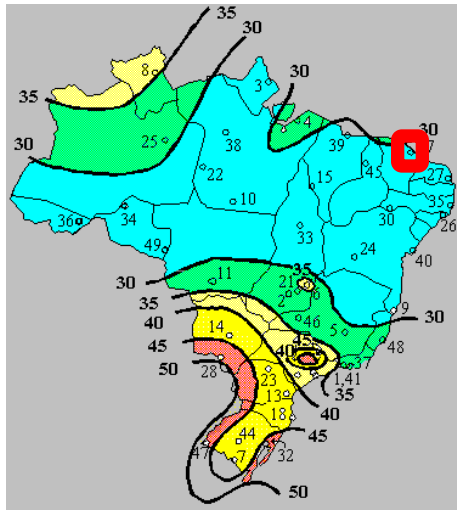




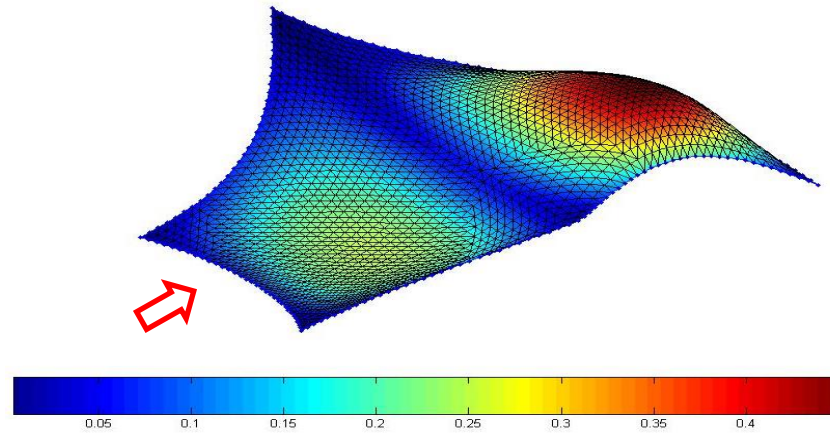
Primeira Tensão Principal : min 5030574.8403 max 5972740.9101



# Resposta às cargas de ventos

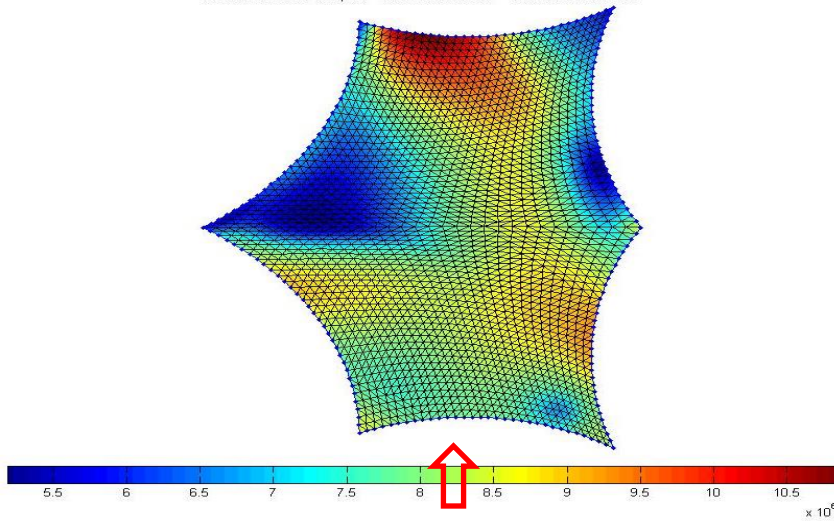


Deslocamentos USUM : min 0 max 0.45286

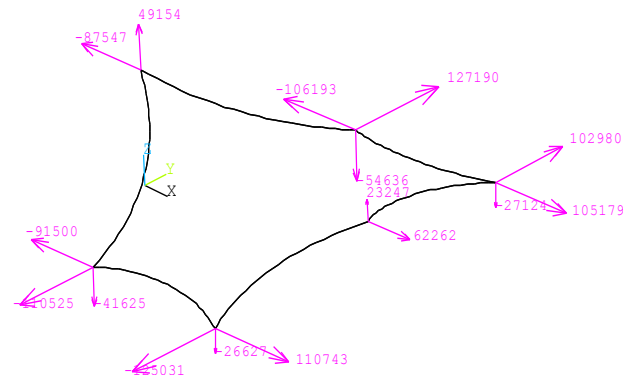


*displacement norms,  
for the Y-wind load case*

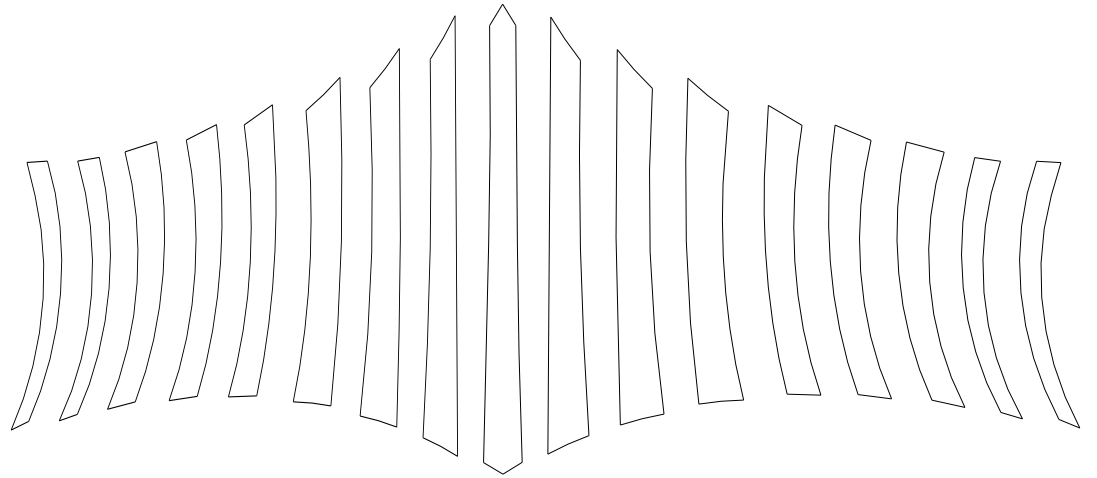
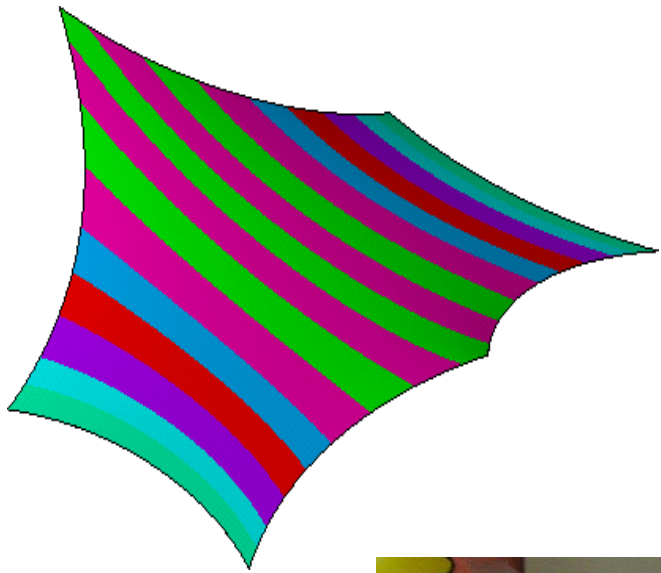
Primeira Tensão Principal : min 5141503.2016 max 10879346.2836



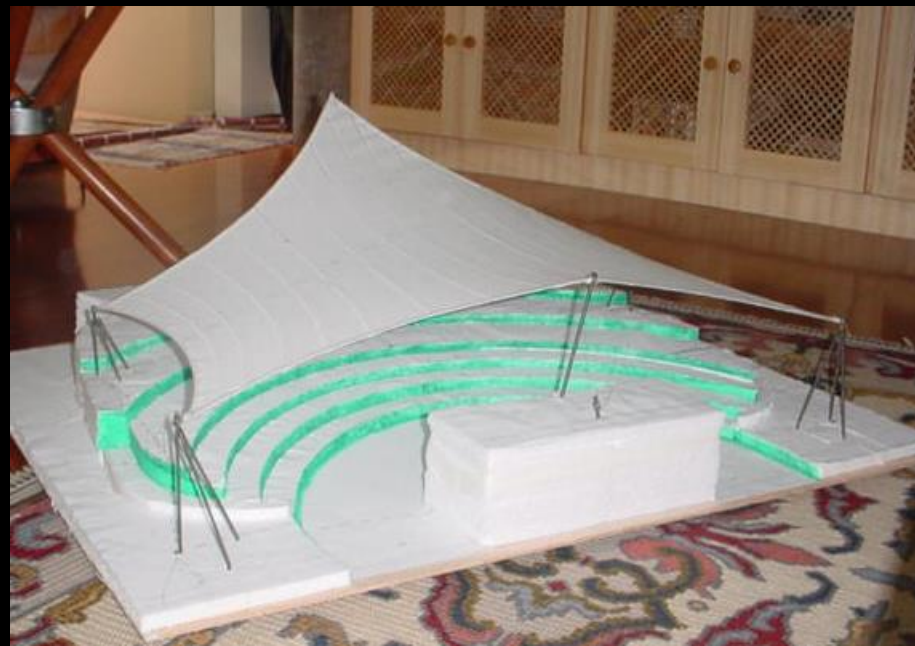
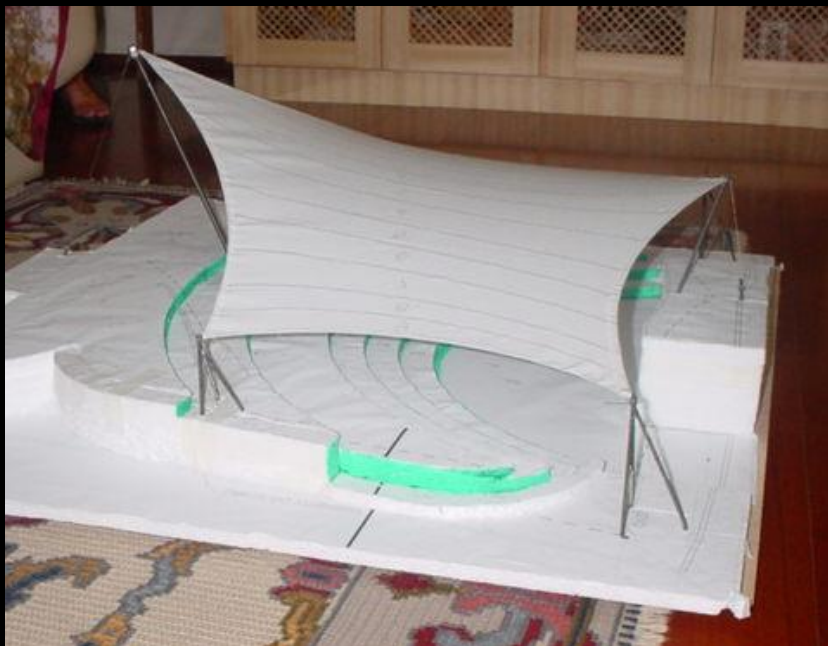
*Maximum 1<sup>st</sup> principal stresses  
(S1) for the Y-wind load case*



# Padrões de corte



# Maquete em tecido escala 1:50



# Modelo em tecido escala 1:10







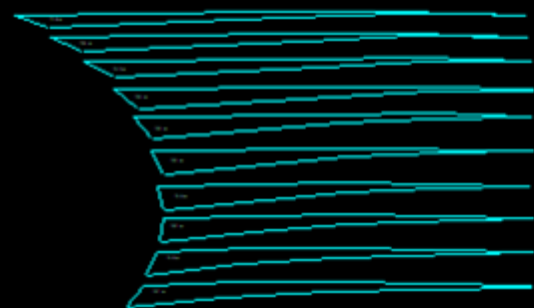
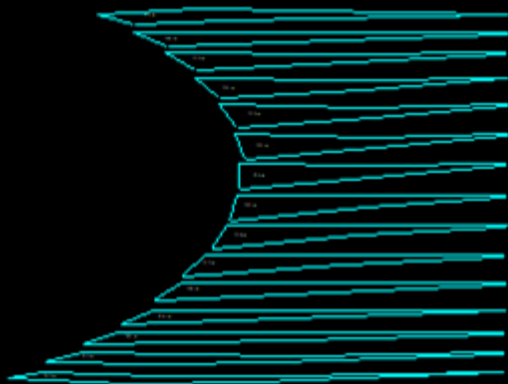
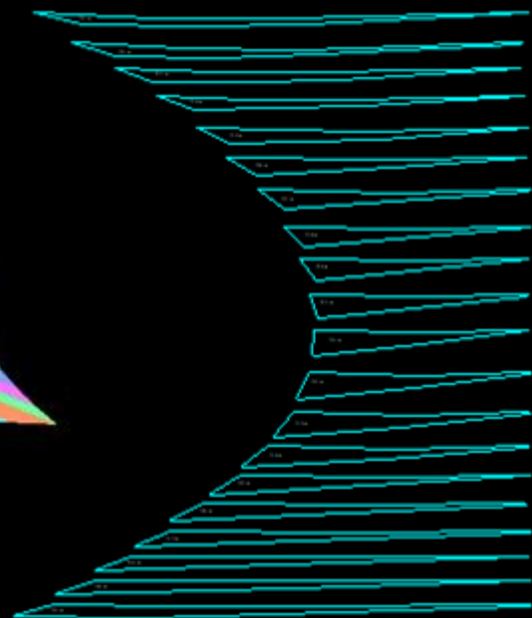
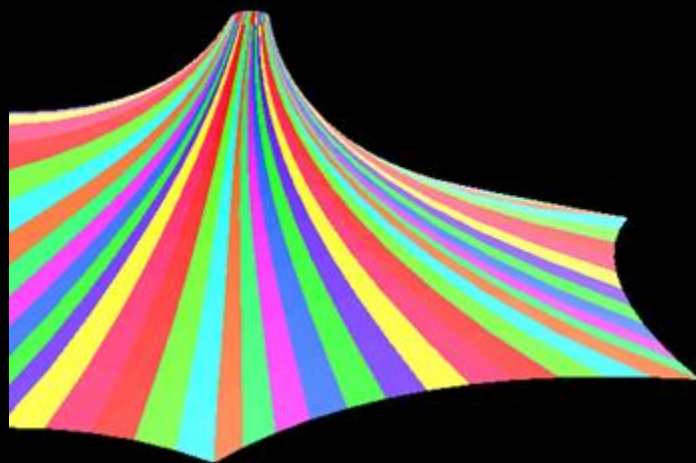
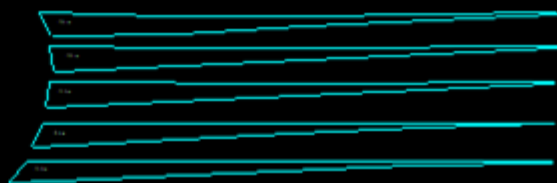
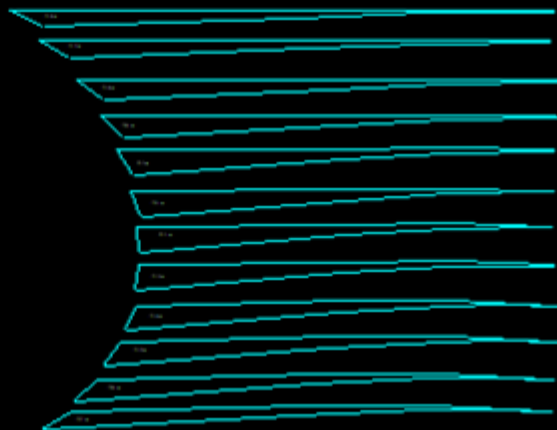


## Membrana de cobertura do Memorial dos Povos de Belém do Pará (2006)



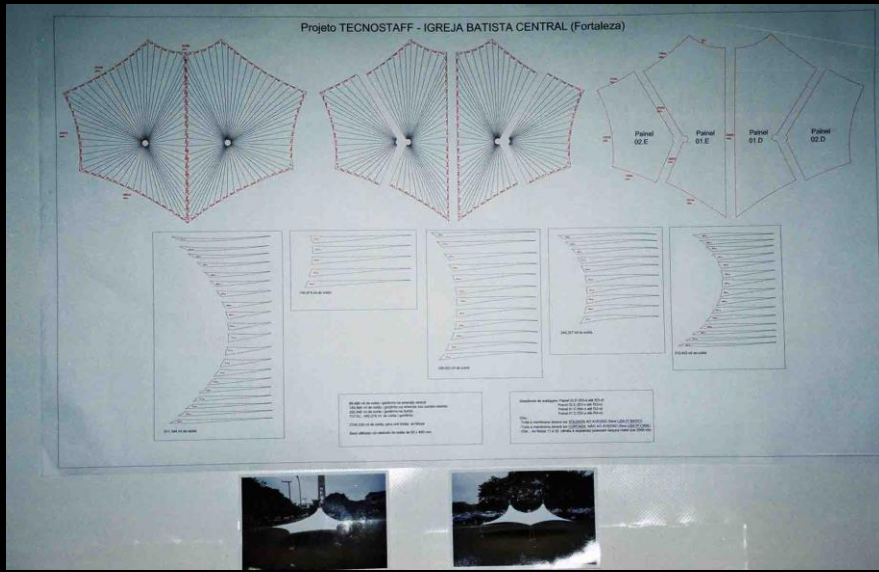
*Igreja Batista de Fortaleza  
durante a inauguração, 27 de Novembro, 2003*







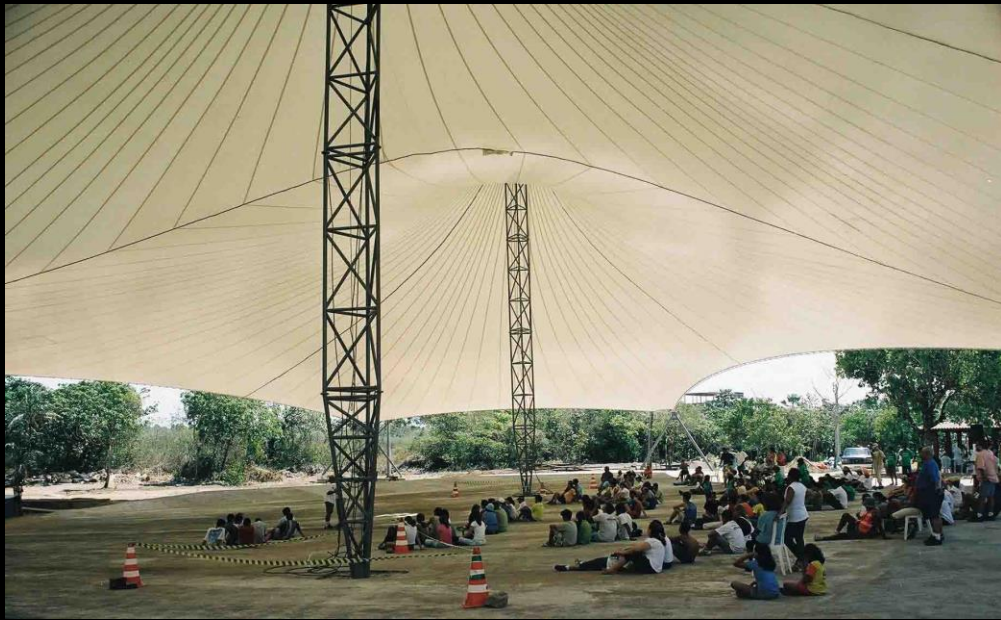
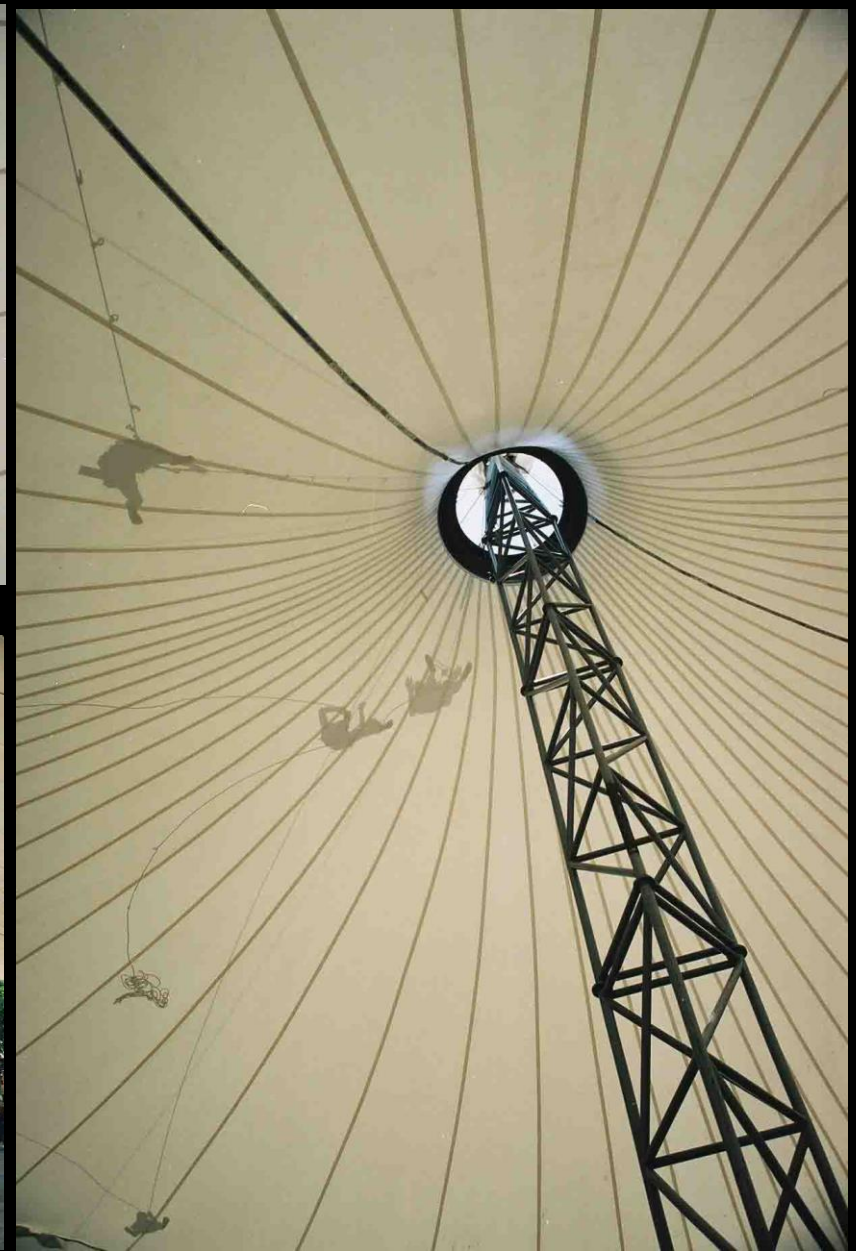


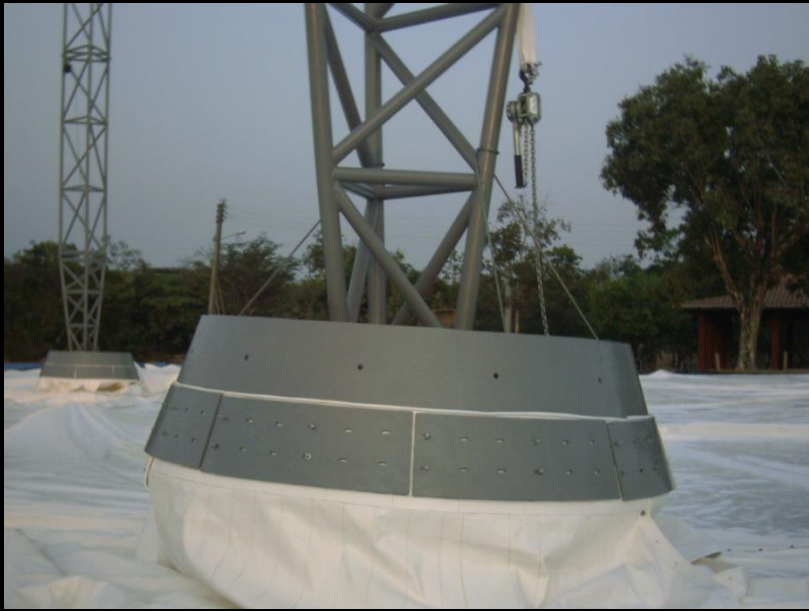












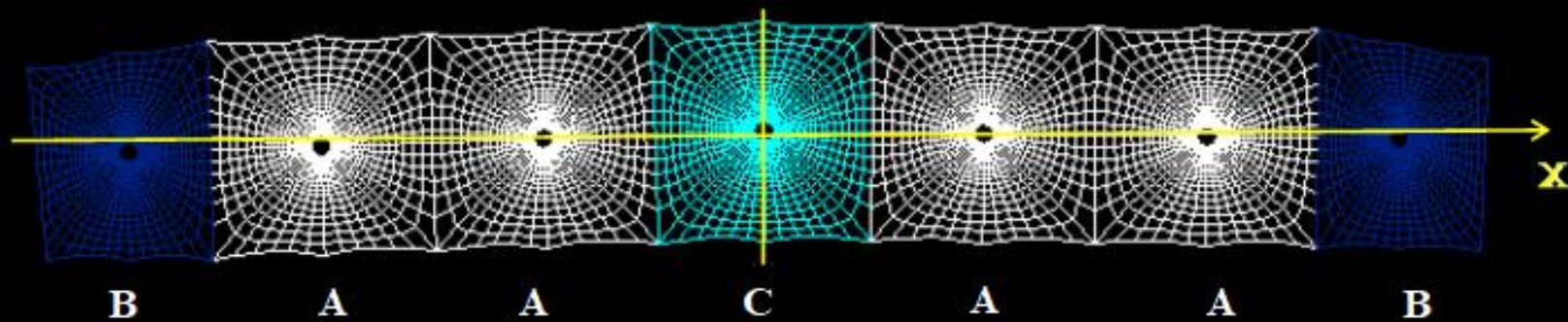
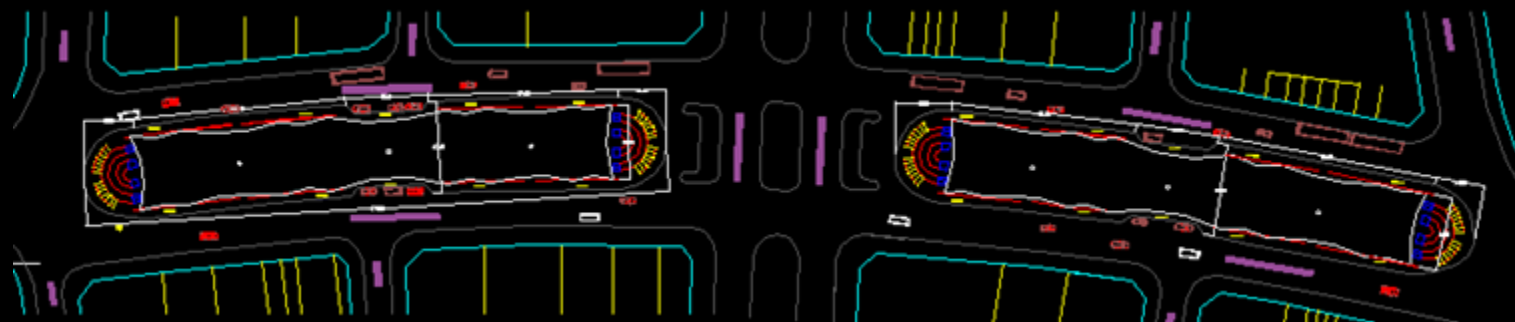




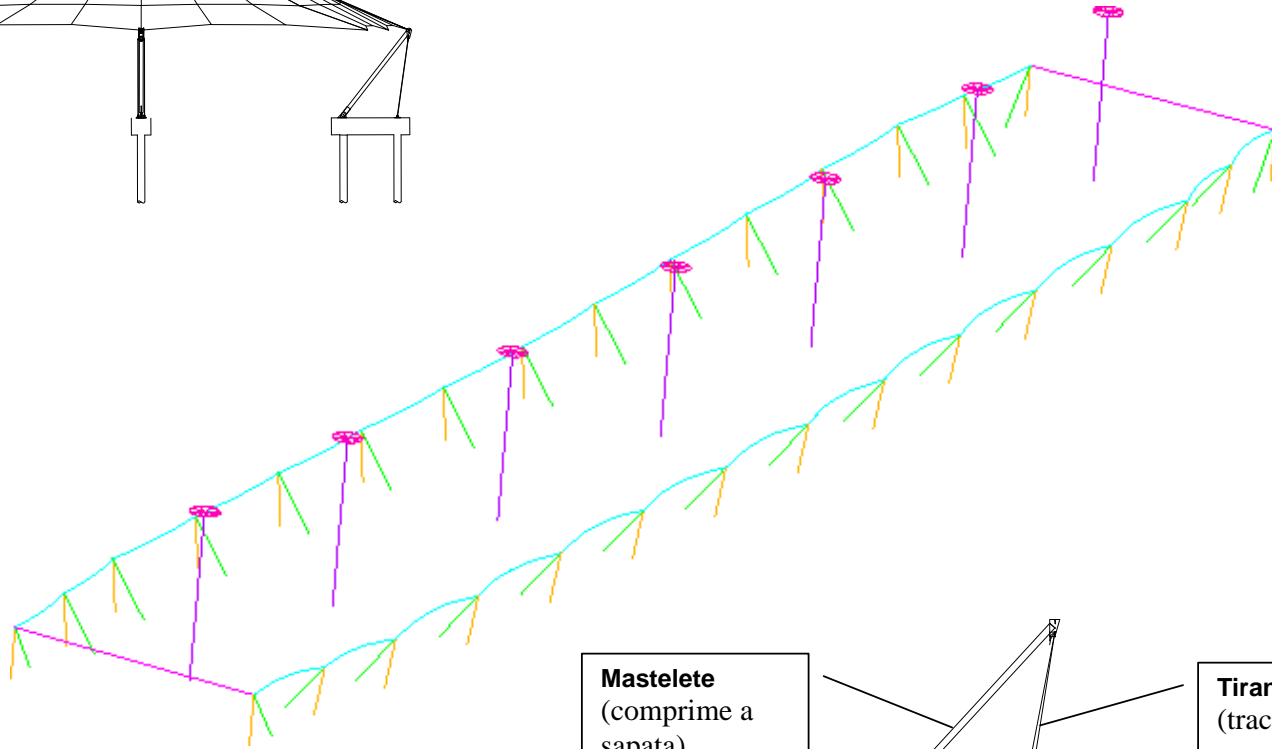
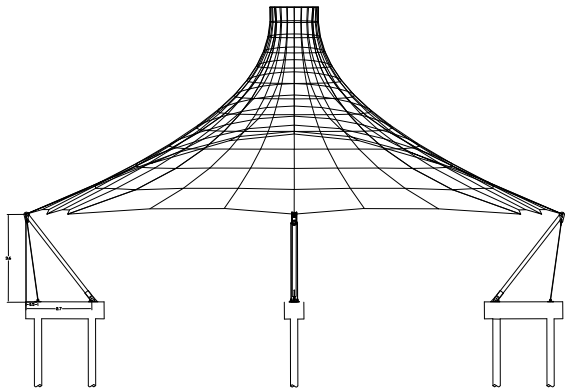
Goiania's Open Market (2006)





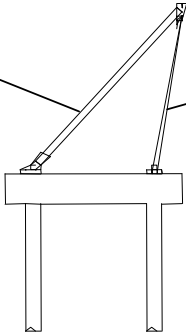


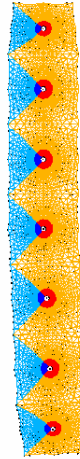
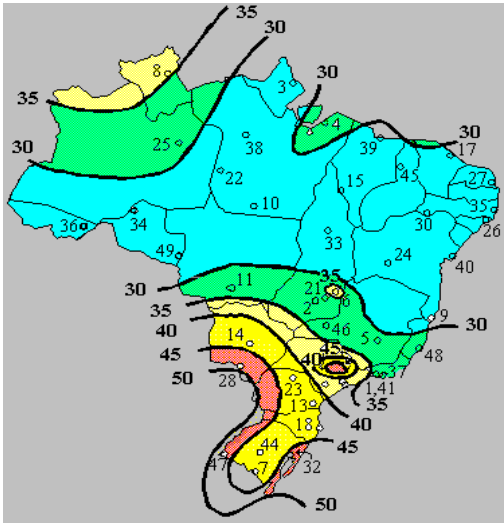




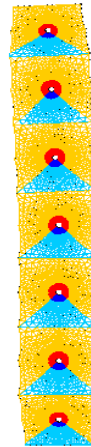
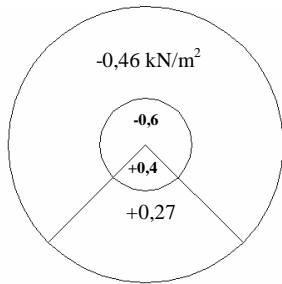
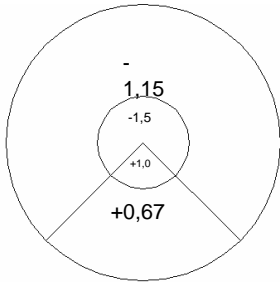
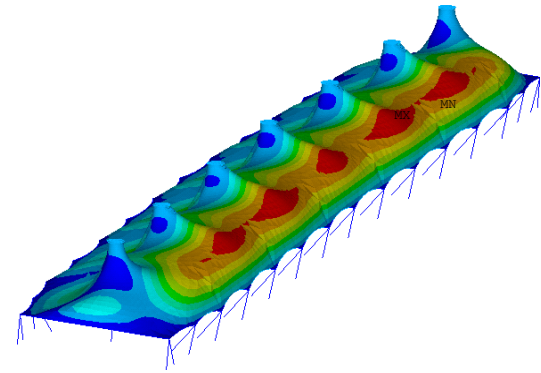
**Mastelete**  
(comprime a sapata)

**Tirante**  
(traciona a sapata)

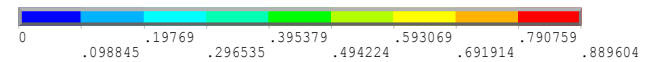
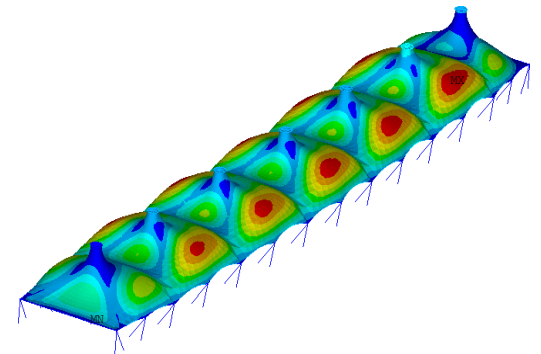




DMX = 1.089  
SMX = 1.089



DMX = .889604  
SMX = .889604











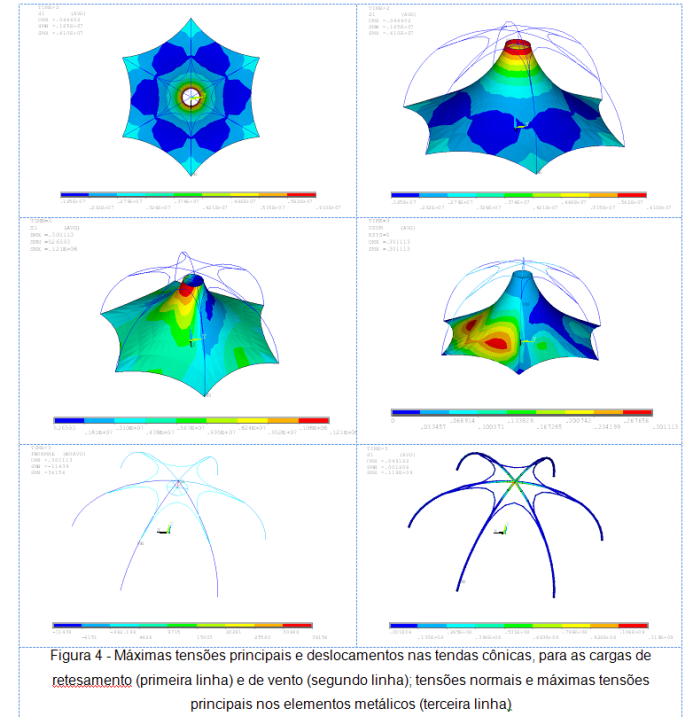


"Feira da Cidade de Ananindeua, PA (2006)  
Arch. José Maria Coelho Bassalo and Flávio Campos do Nascimento



"Feira da Cidade de Ananindeua, PA (2006)  
Arch. José Maria Coelho Bassalo and Flávio Campos do Nascimento



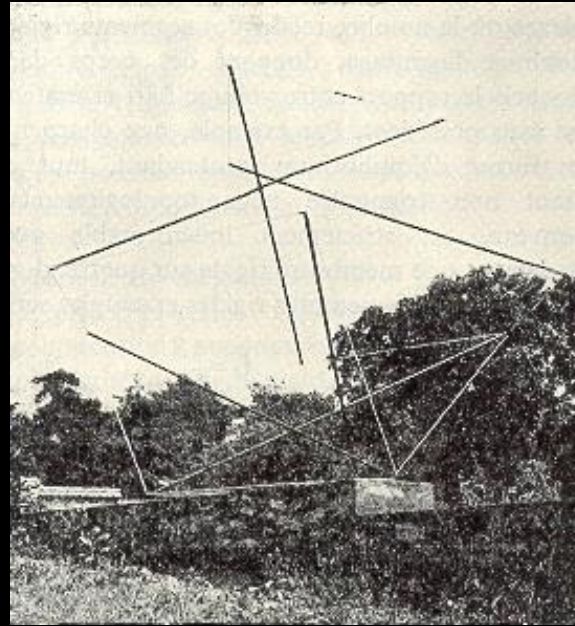


"Feira da Cidade de Ananindeua, PA (2006)  
Arch. José Maria Coelho Bassalo and Flávio Campos do Nascimento

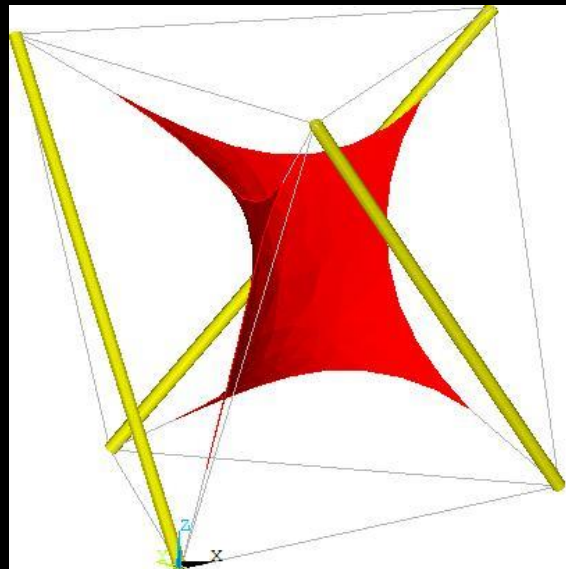
# Tensegrities



**Needle Tower,  
K. Snelson, 1948**



**The Monument to  
the Futile Form,  
D. Emmerich, 1966**

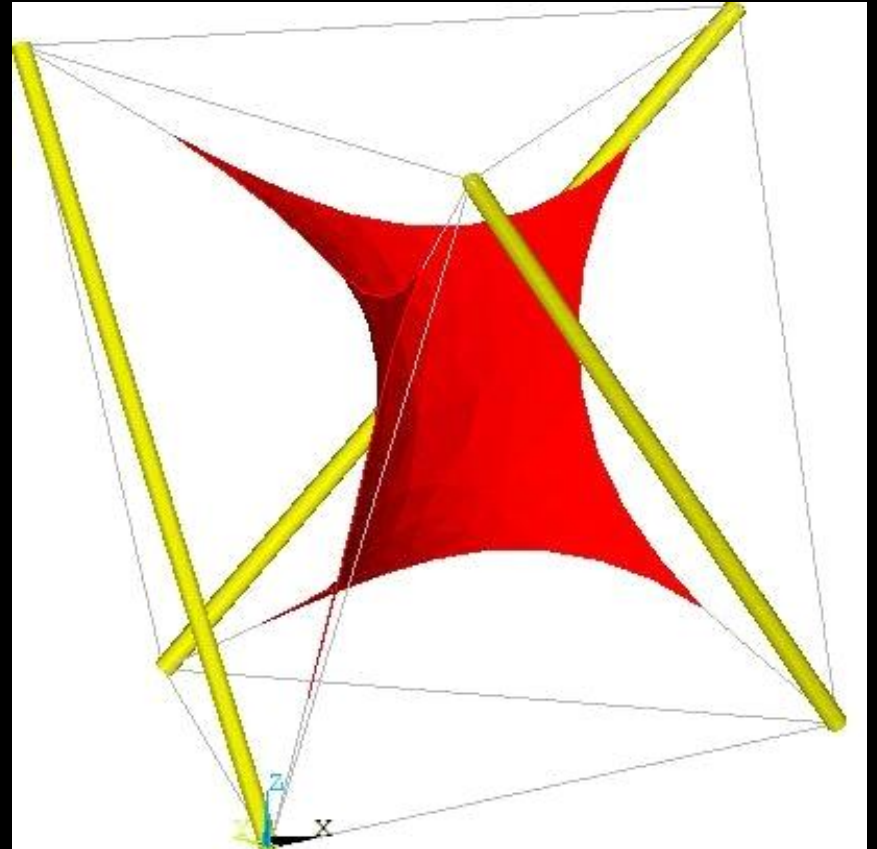


**The Monument to the  
Futile Form II  
Titotto, Deifeld, Pauletti,  
2003**

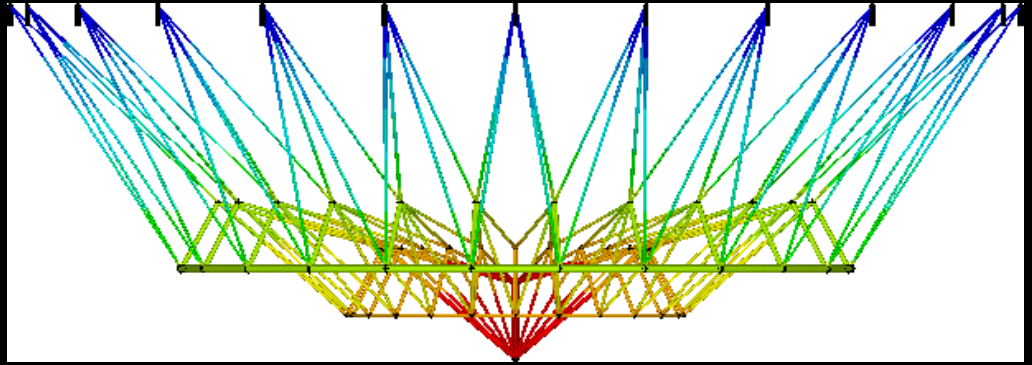
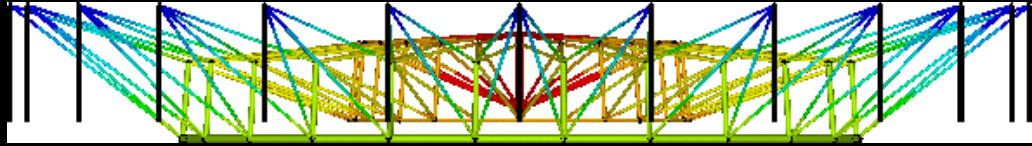
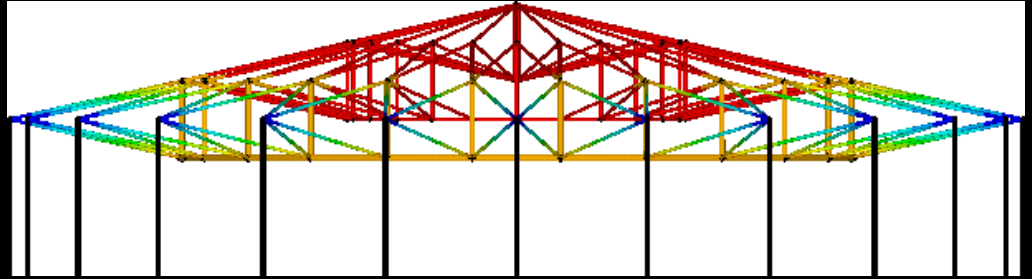
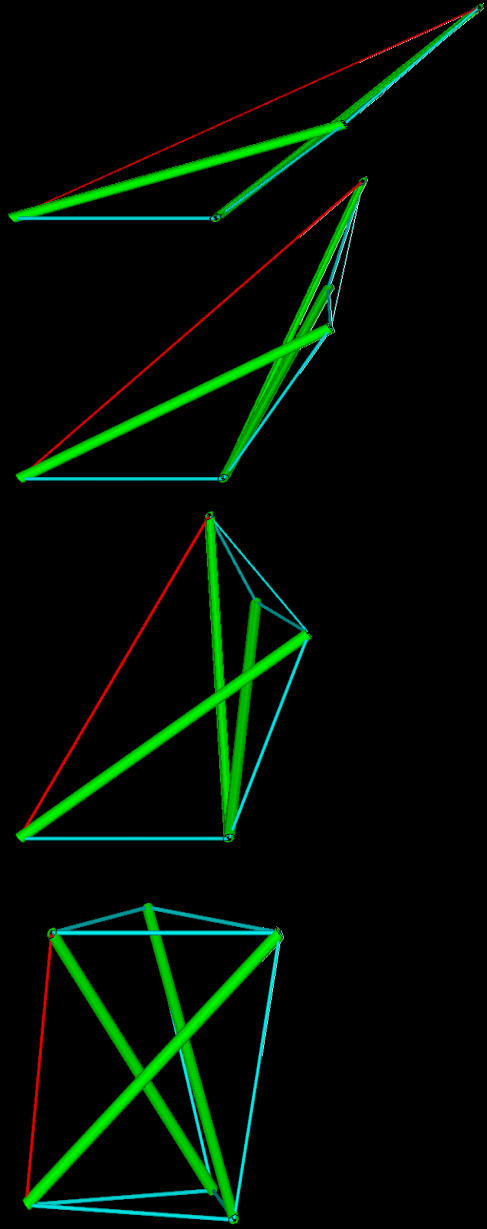


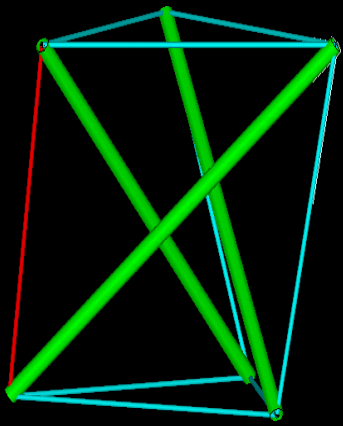


## Monument to the Futile Form II (2003)





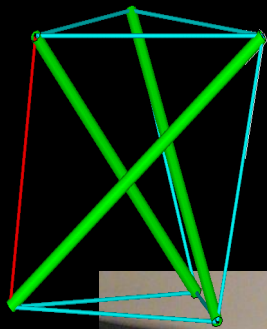




## 3 days workshop at Università delle Marche (Ancona) (2013)







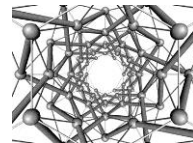
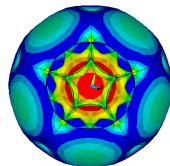
## 3 days workshop at Università delle Marche (Ancona) (2013)



*Ruy Marcelo de Oliveira Pauletti & Jung Yun Chi*  
*Polytechnic School - University of São Paulo*



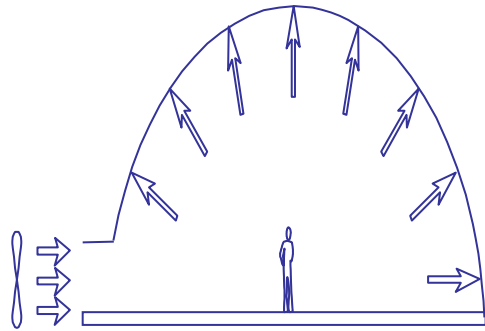
# *Modeling and Construction of the 'Dodecoid', an Inflated, Double-Skin Dodecahedron*



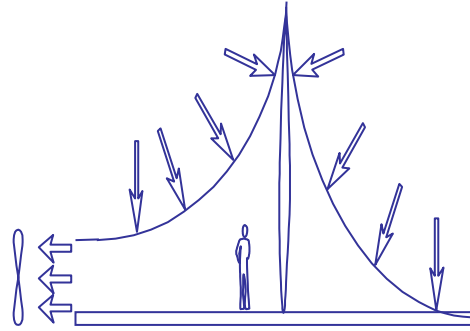
*IASS-2004*

*Shell and Spatial Structures: from Models to Realization*  
*Montpellier, 20-24/09/2004*

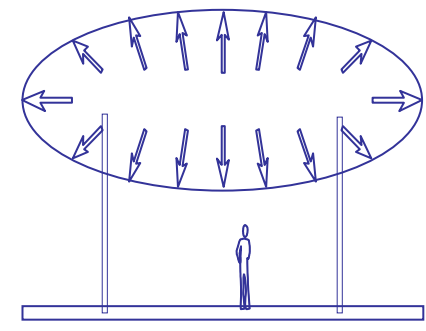
# Pneumatic Structures



(a) Insufflated;



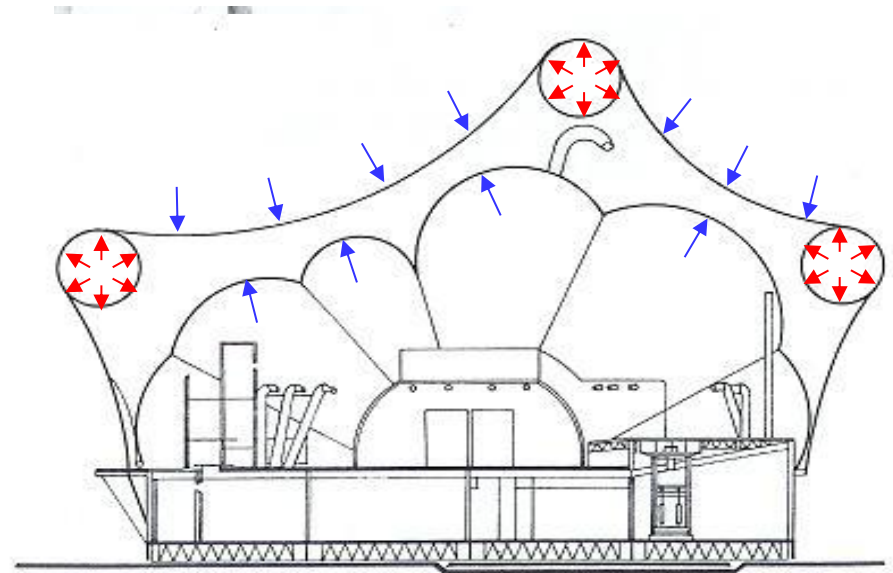
(b) Aspirated;



(c) Inflated



*Tokyo "Big-Egg" Dome (1988)*



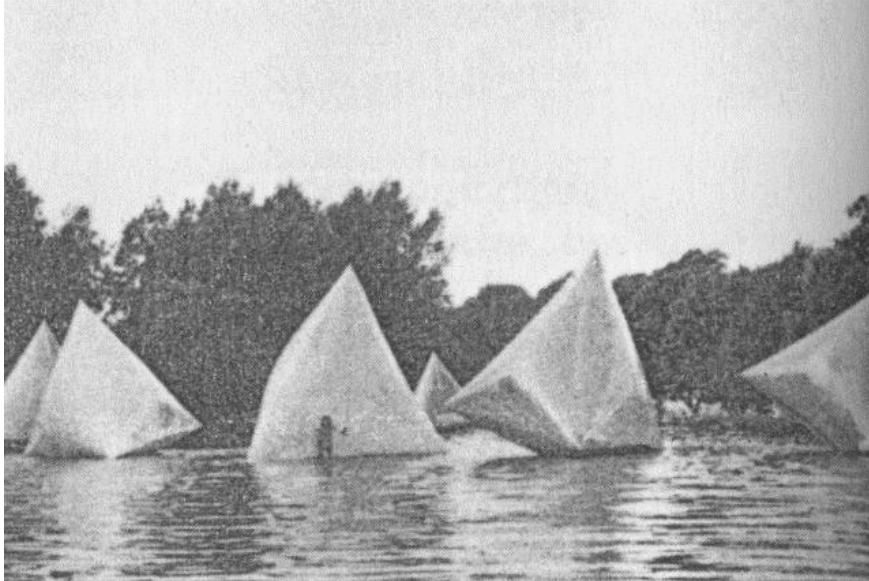
*Floating Pavilion (Osaka, 1970)*

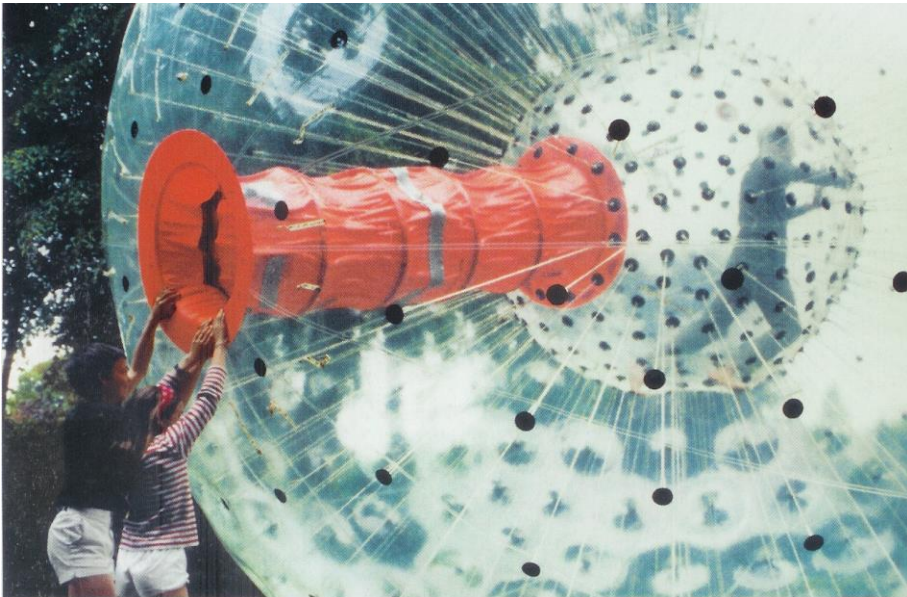
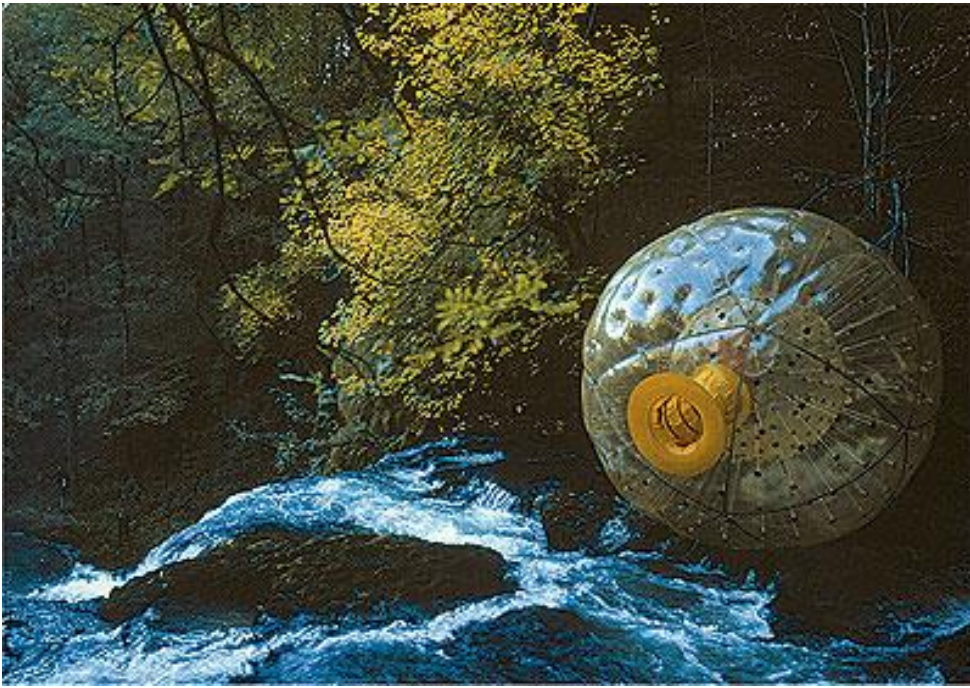


# *Inflated tetrahedron 'walking machine'*

*Eventstructure Research Group, 1968.*

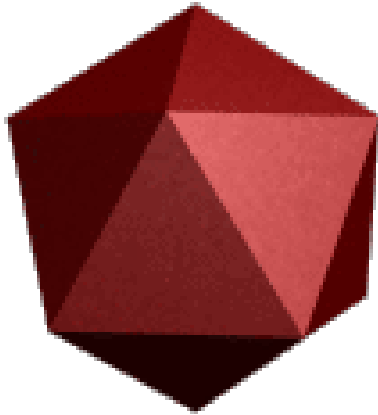
*0.5 mm thick transparent or translucent PVC foils;  
watertight zip fastened entrances.*





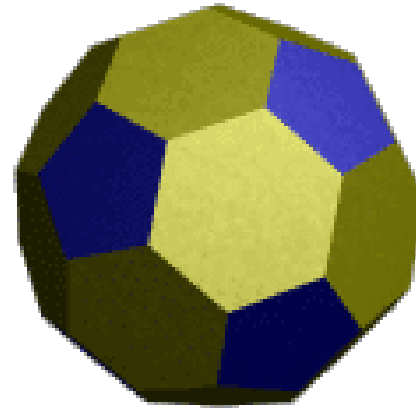
***La Balulle -  
Gilles Ebersolt, France  
(1973 – 1985)***





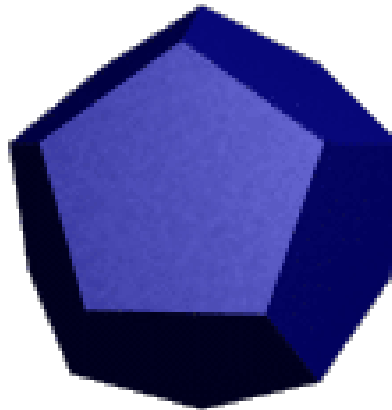
**Icosahedron**

Faces: 20  
Edges: 30  
Vertices: 12



**truncated  
icosahedron**

Faces: 32  
Edges: 90  
Vertices: 60



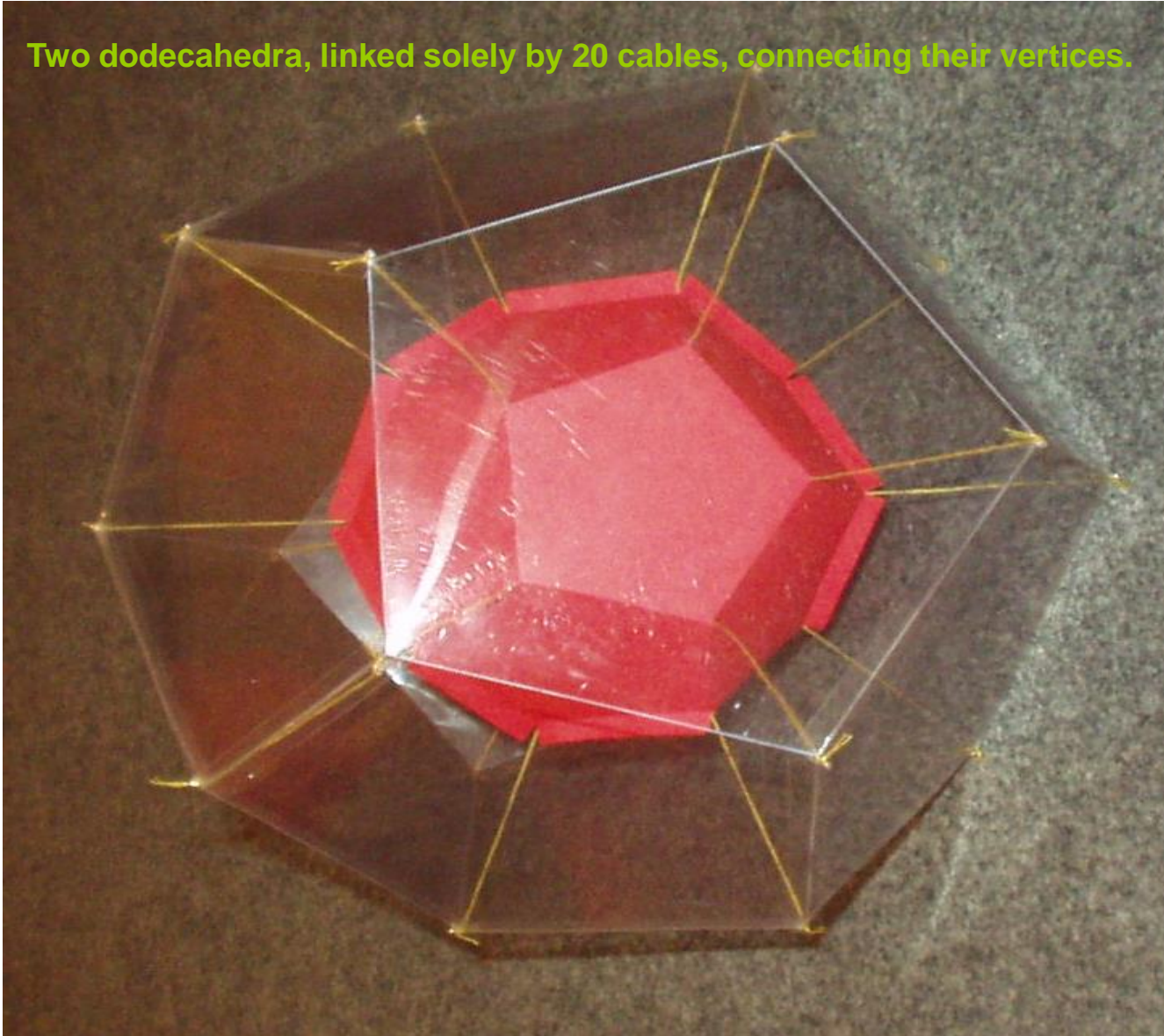
**Dodecahedron**

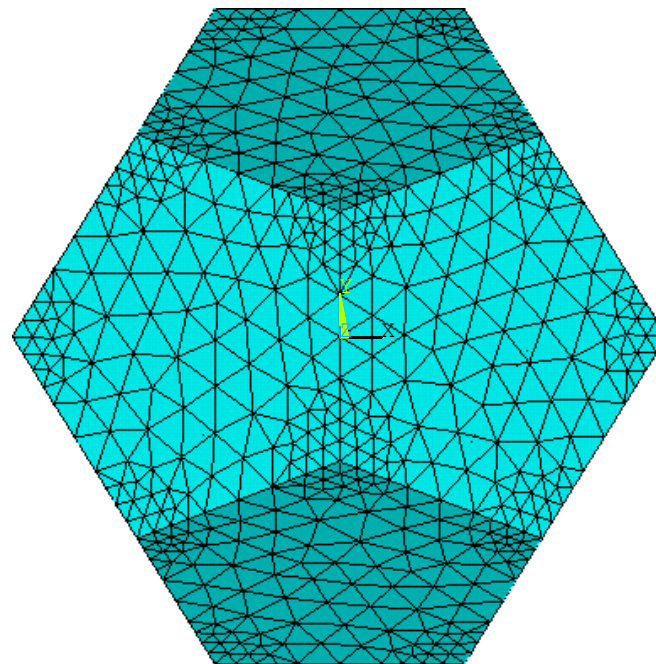
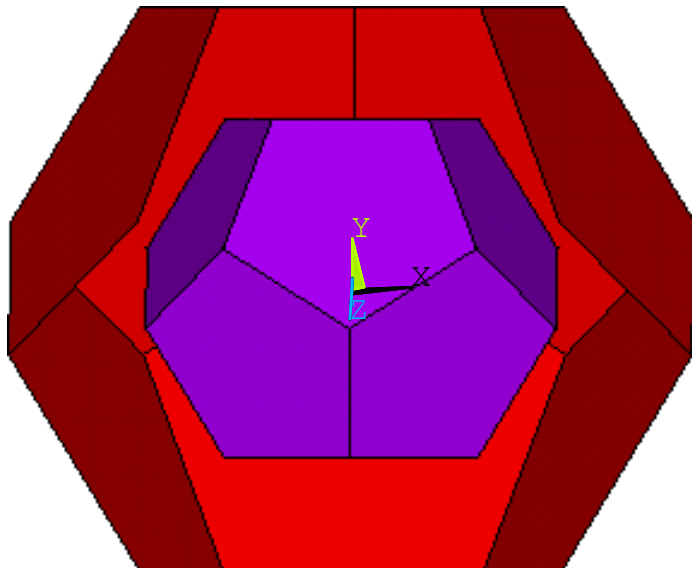
Faces: 12  
Edges: 30  
Vertices: 20



## The “Dodecoid”

Two dodecahedra, linked solely by 20 cables, connecting their vertices.

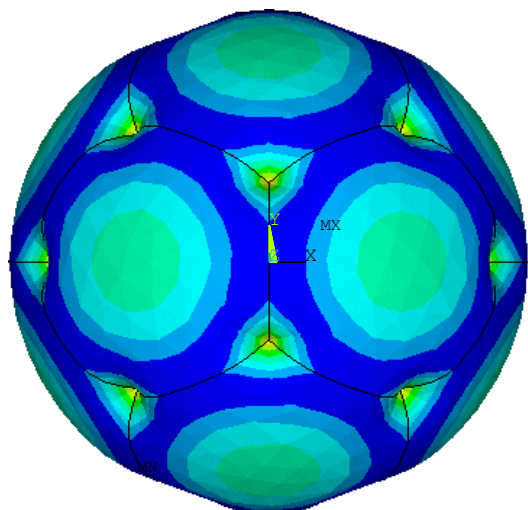




```

---
TIME=2
USUM      (AVG)
RSYS=0
DMX =.353357
SMN =.017586
SMX =.353357

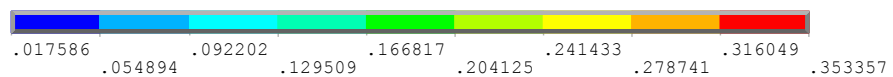
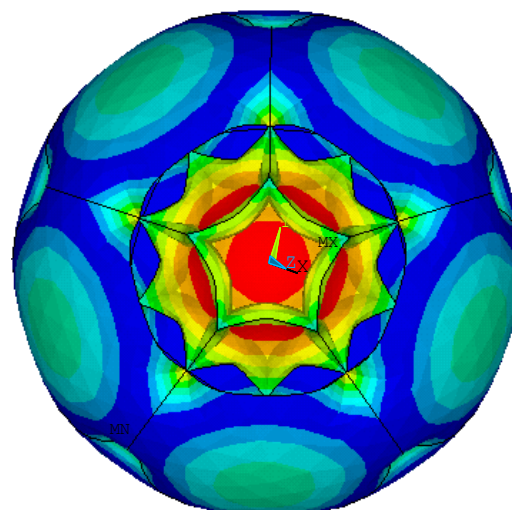
```



```

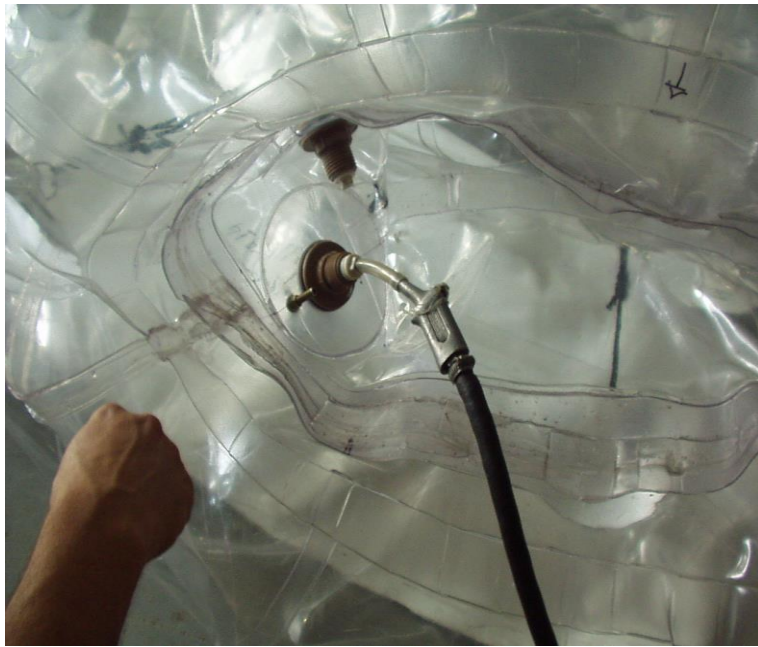
TIME=2
USUM      (AVG)
RSYS=0
DMX =.353357
SMN =.017586
SMX =.353357

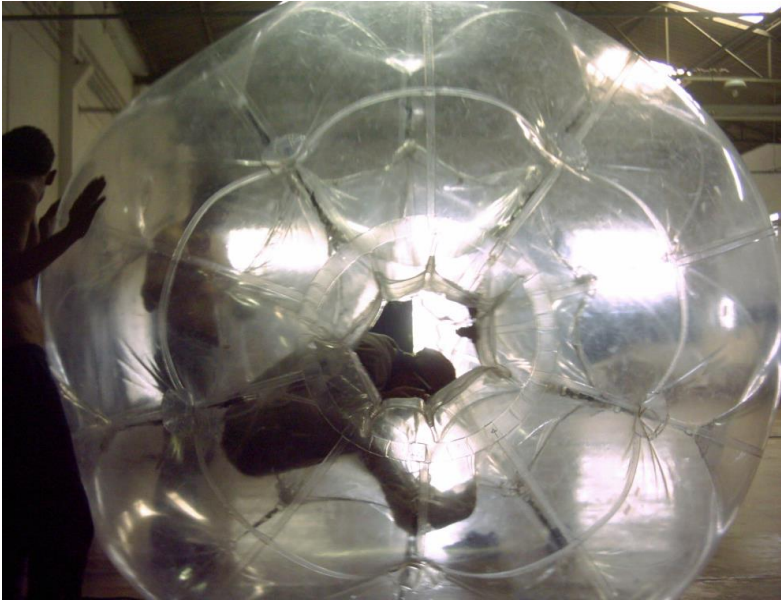
```





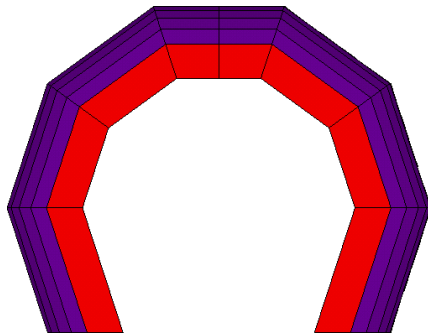
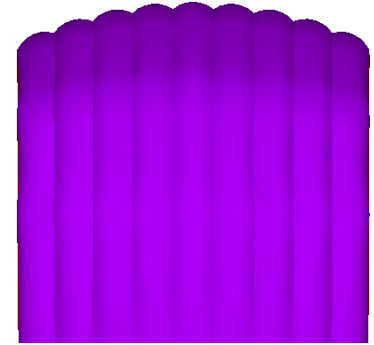
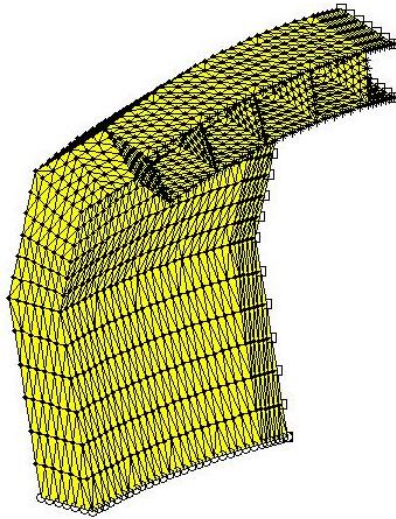
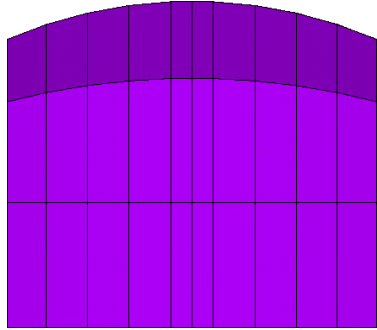




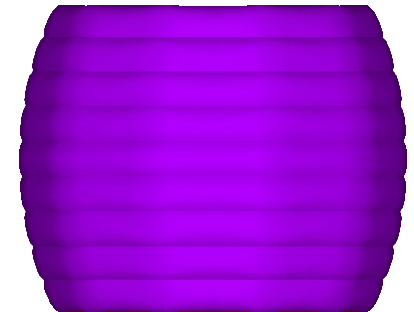
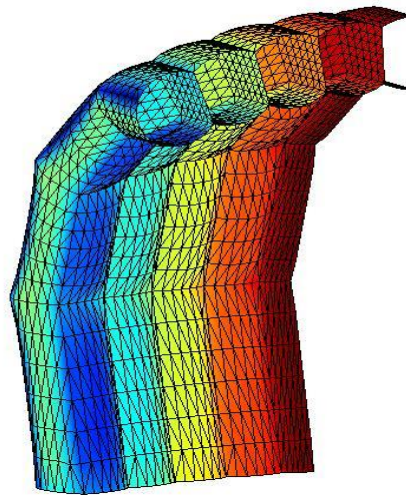
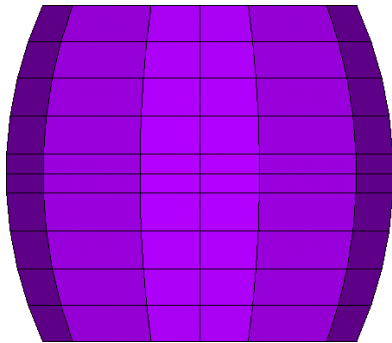
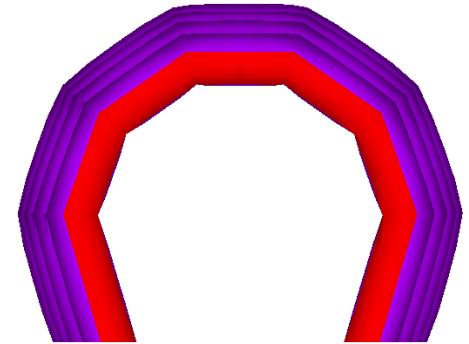




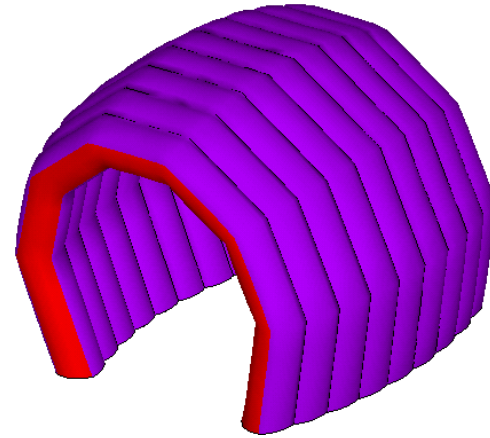
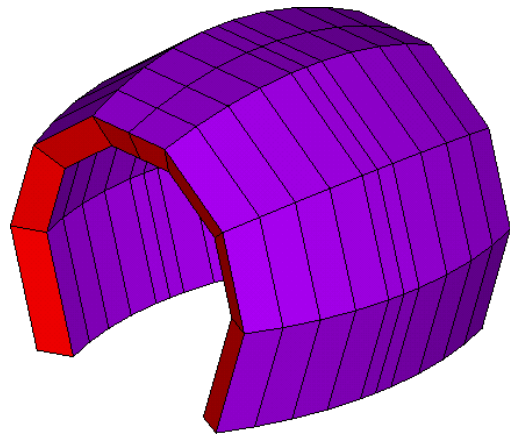
# A pneumatic dome (2005)



Desplacamientos UY : min -0.11962 max 0

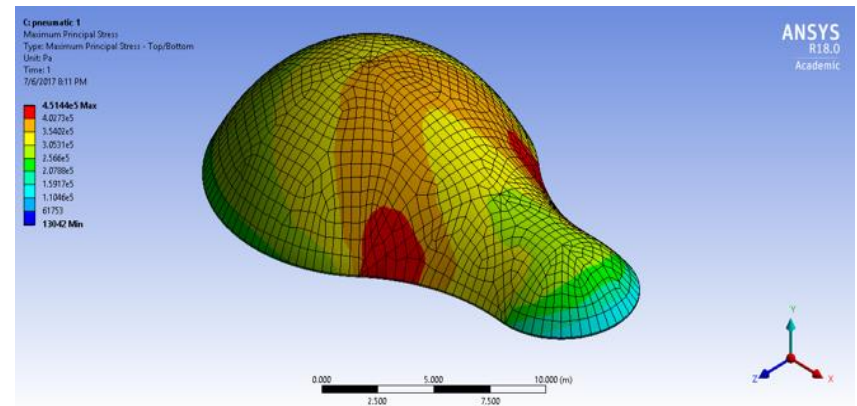
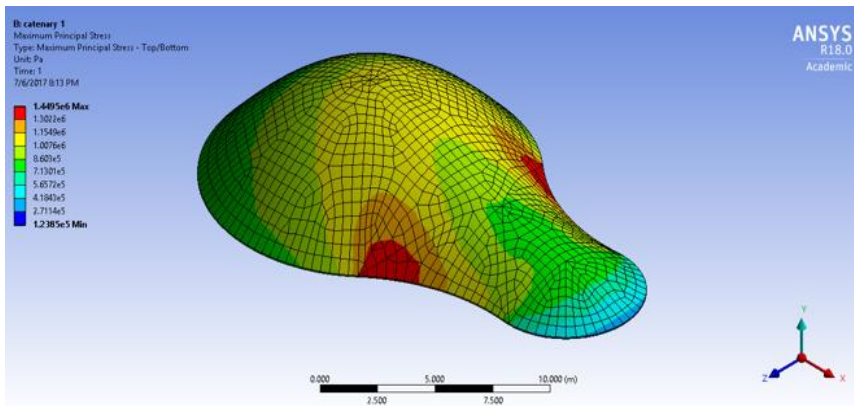
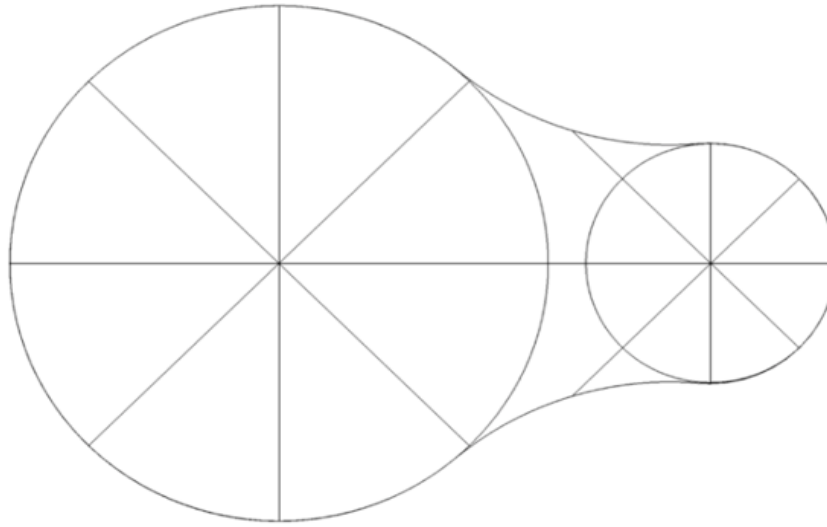






# Pneumatic Formworks: Formfinding with ANSYS

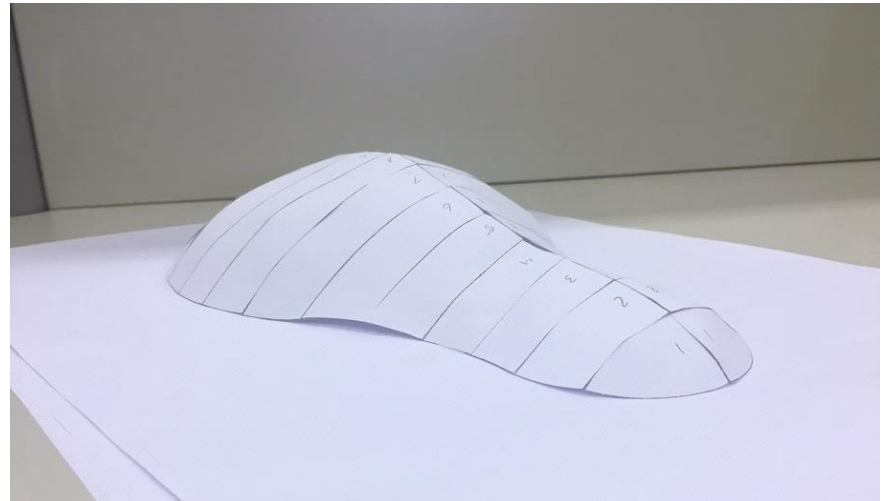
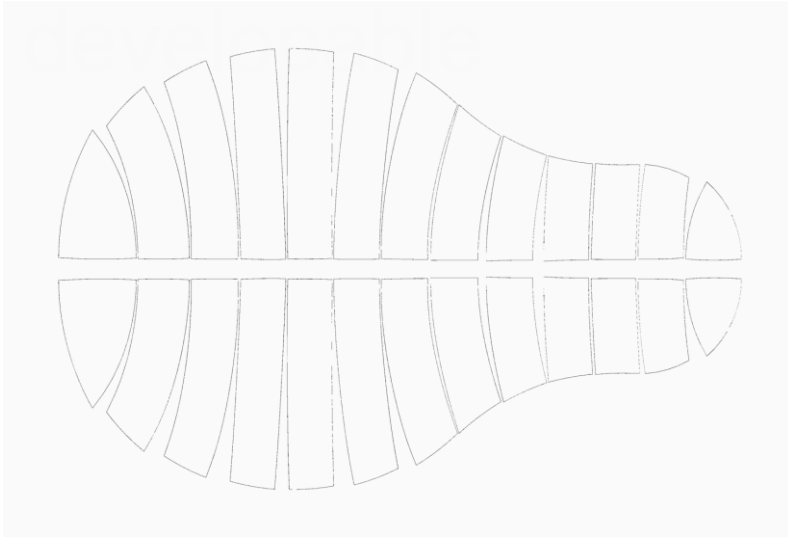
(Nyema Watson, 2017)



# Physical Model

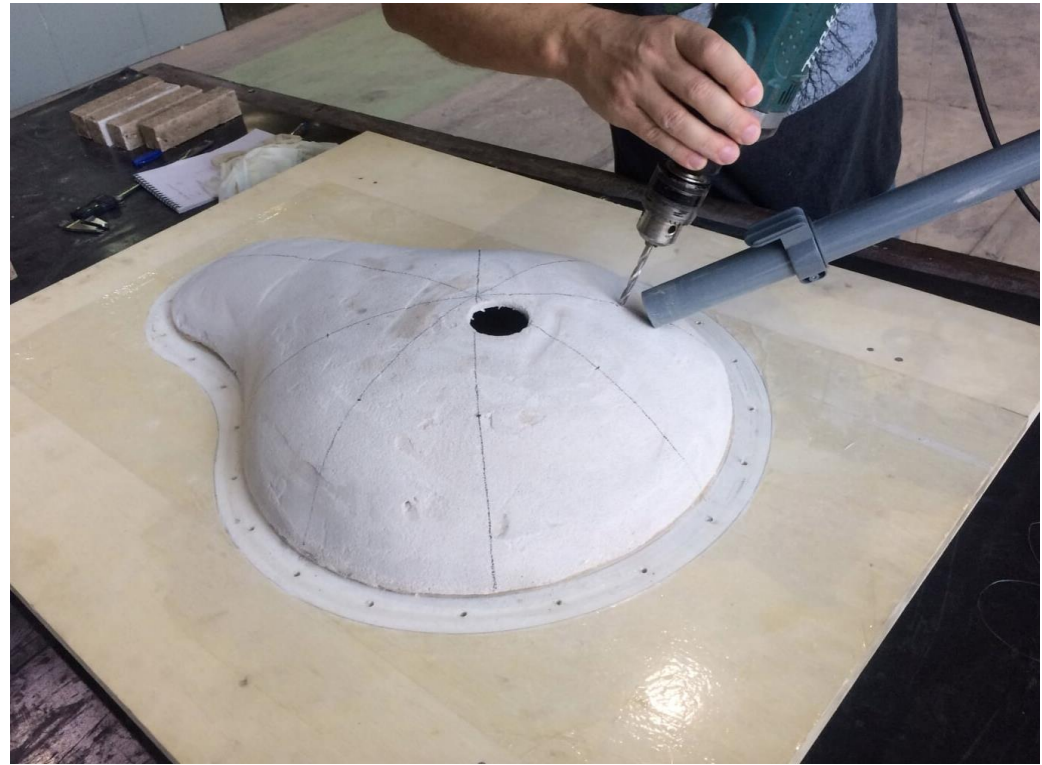
(Neyma Watson, Leila Meneghetti, Ruy Pauletti, 2017)

## Patterning: making a 3D surface



# Physical Model

(Neyma Watson, Leila Meneghetti, Ruy Pauletti, 2017)



# Sliding Cables and Wrinkling



**Pneumatic envelope for 'Angra III' ground preparation**

(September 2009)

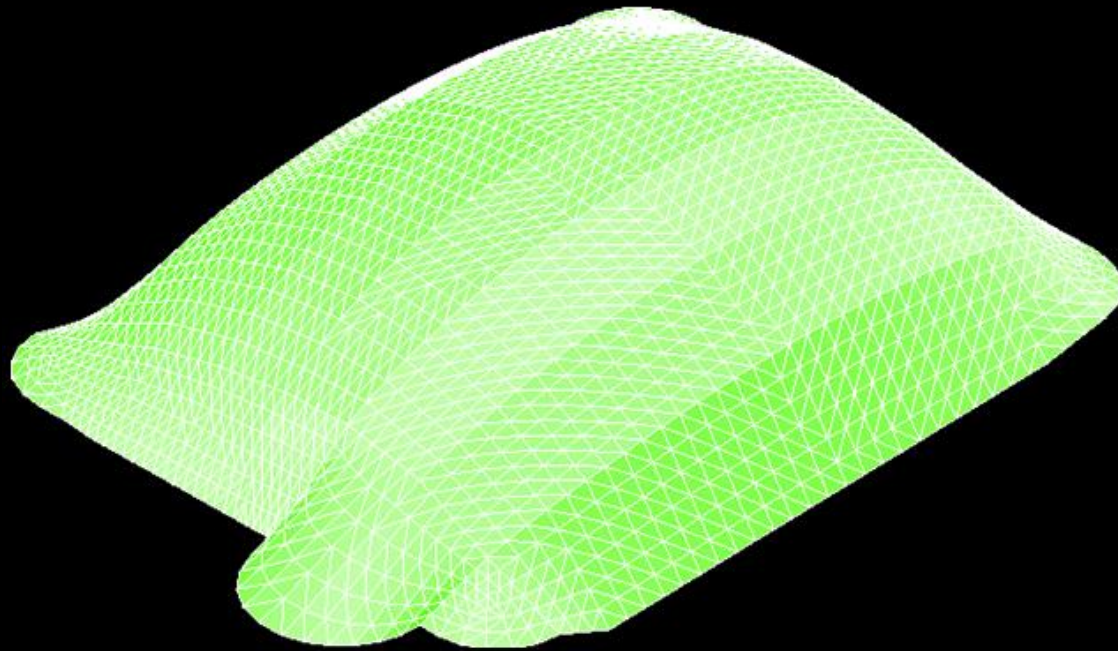
# Sliding Cables and Wrinkling



**Pneumatic envelope for 'Angra III' ground preparation**

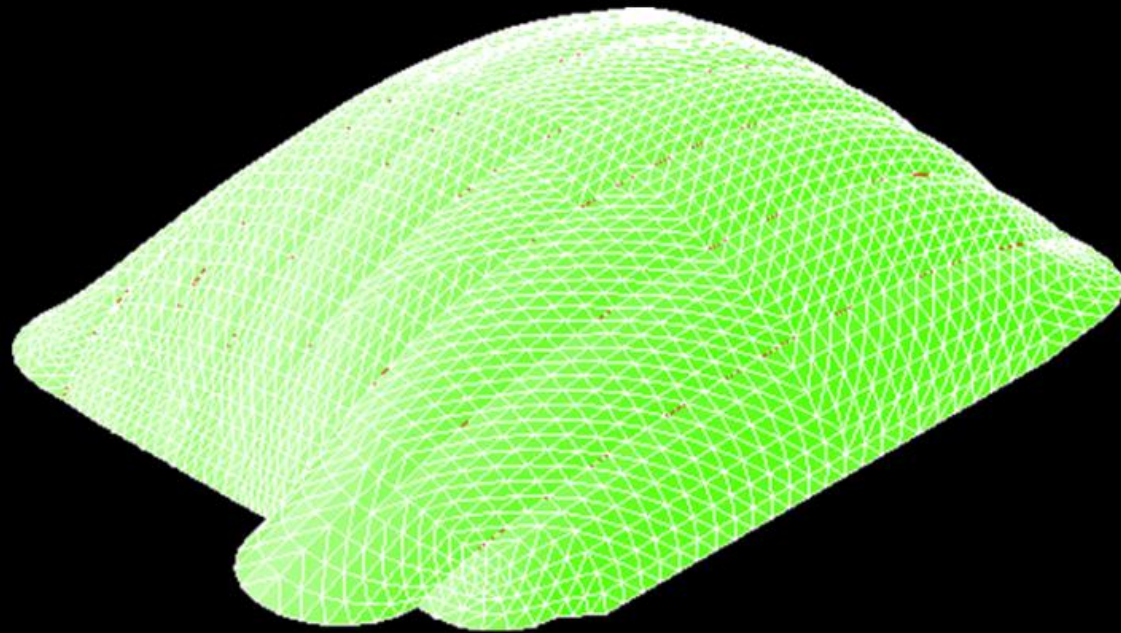
(September 2009)





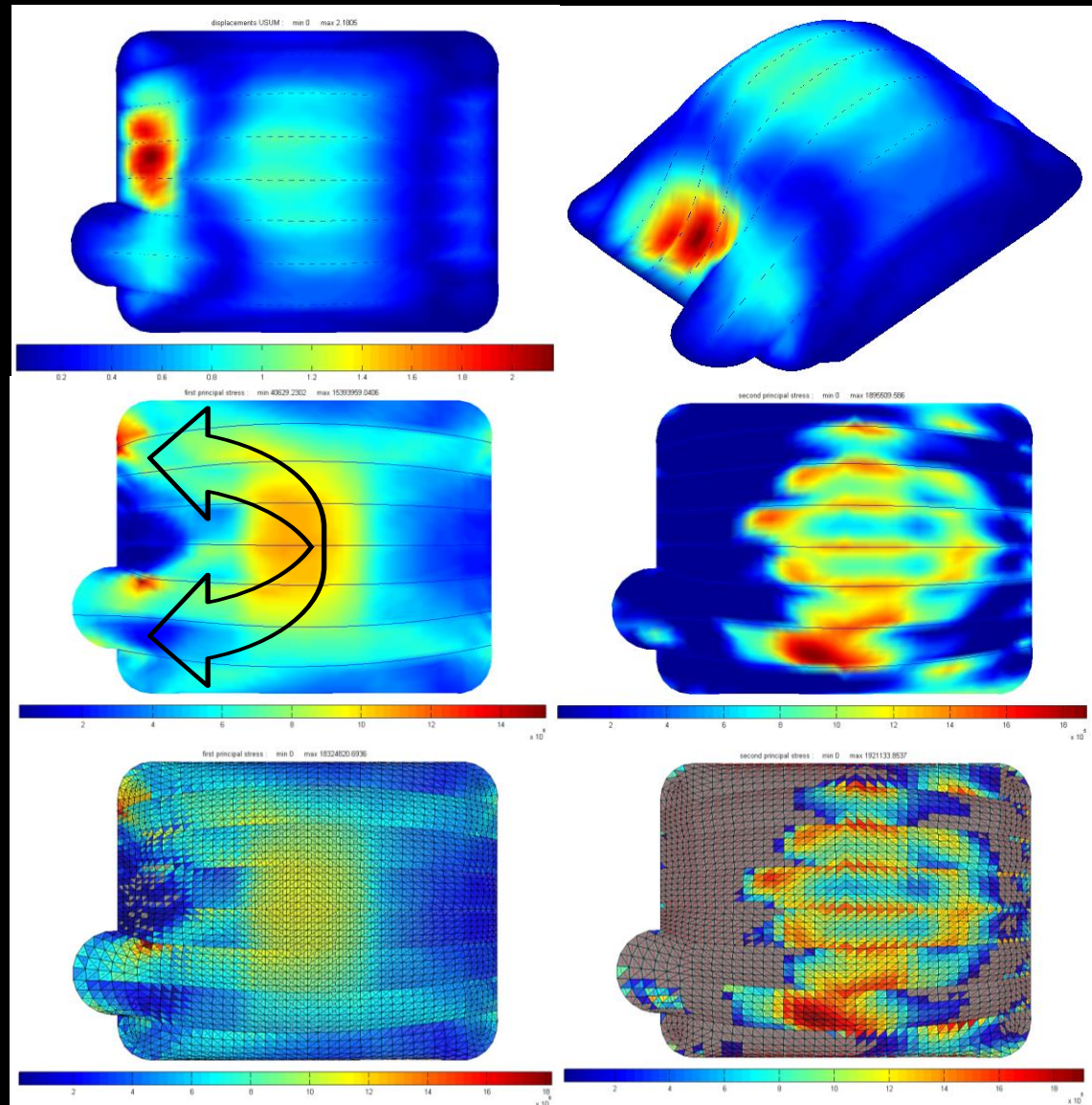
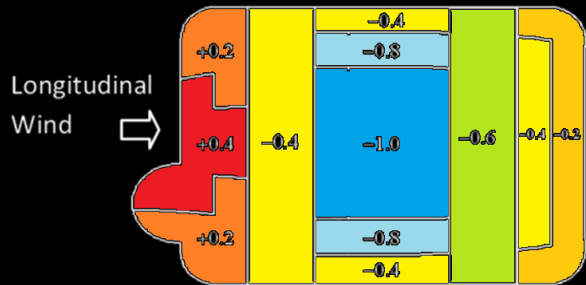
Initial mesh modeled in SATS





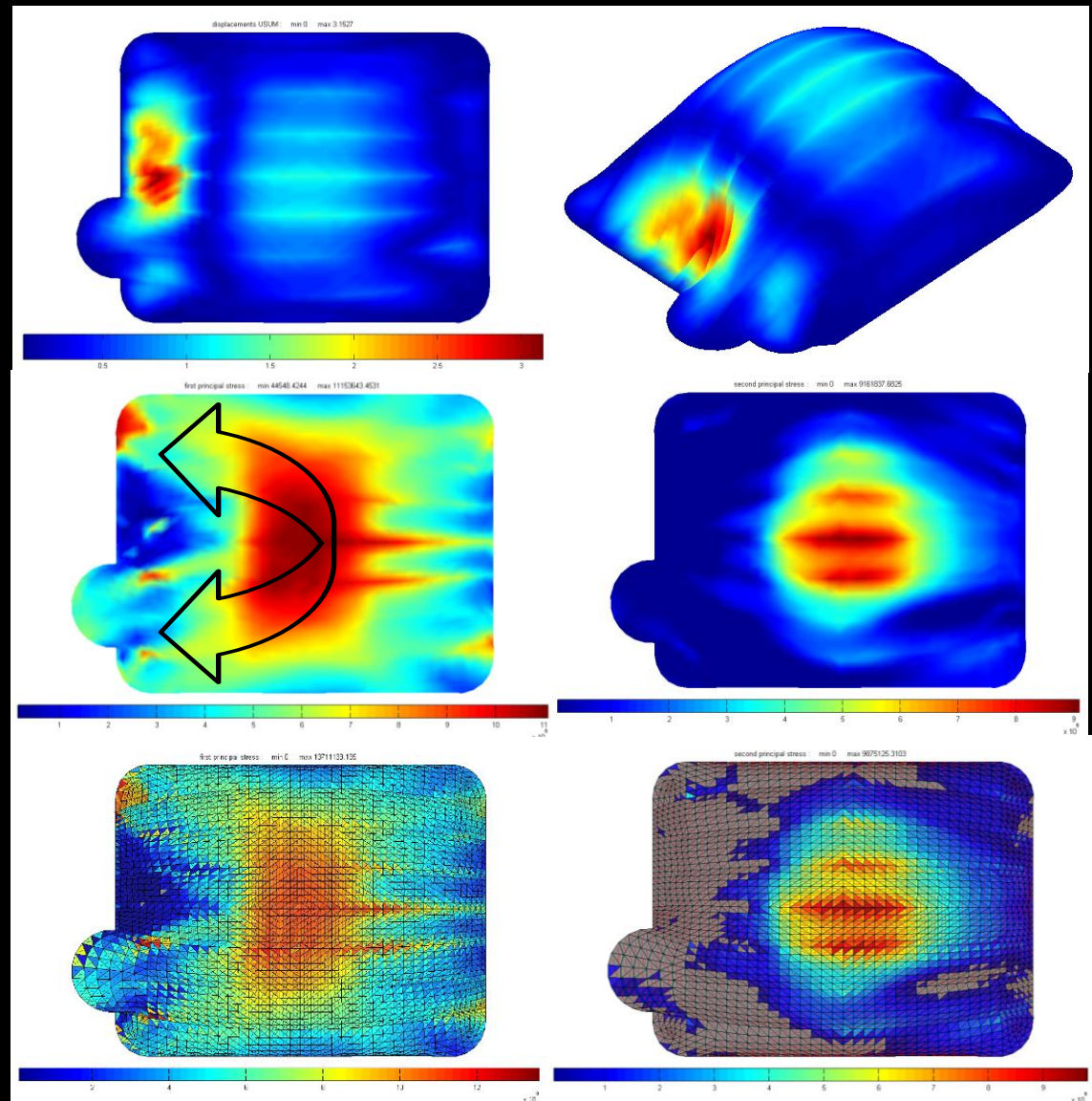
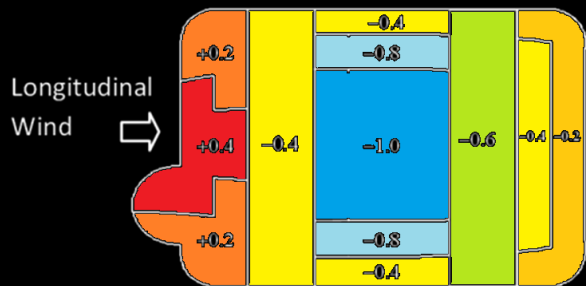
equilibrium geometry under internal pressure

# Longitudinal wind, adherent cables



(a) field of displacement norms; (b) *idem*, isometric view; (c) stress field; (d) stress field.

# Longitudinal wind, sliding cables



(a) field of displacement norms; (b) *idem*, isometric view; (c) stress field; (d) stress field.

# CENPES II – Rio de Janeiro, 2010

Archs. Ziegbert Zenettini, Wagner Garcia





# CENPES II

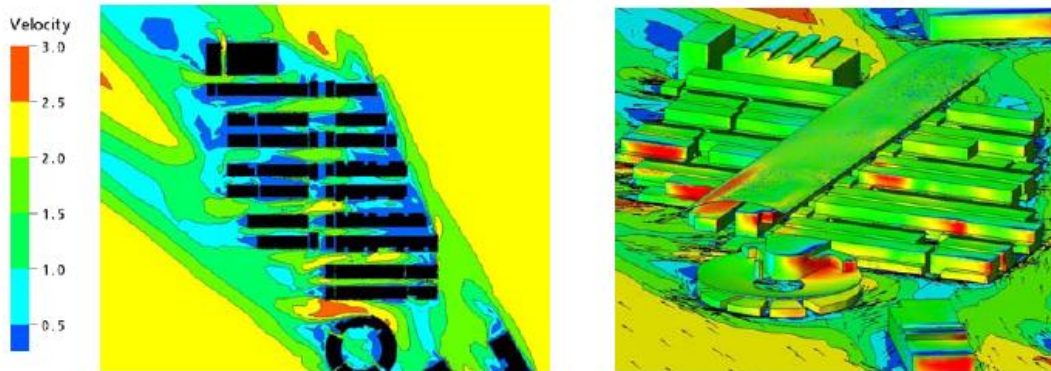
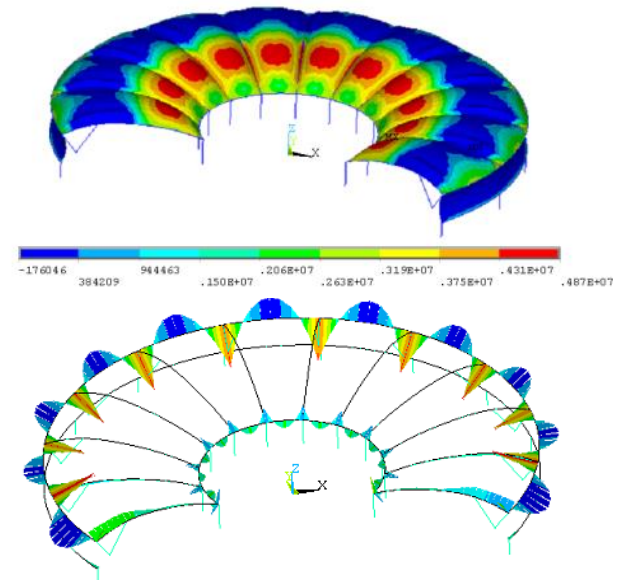
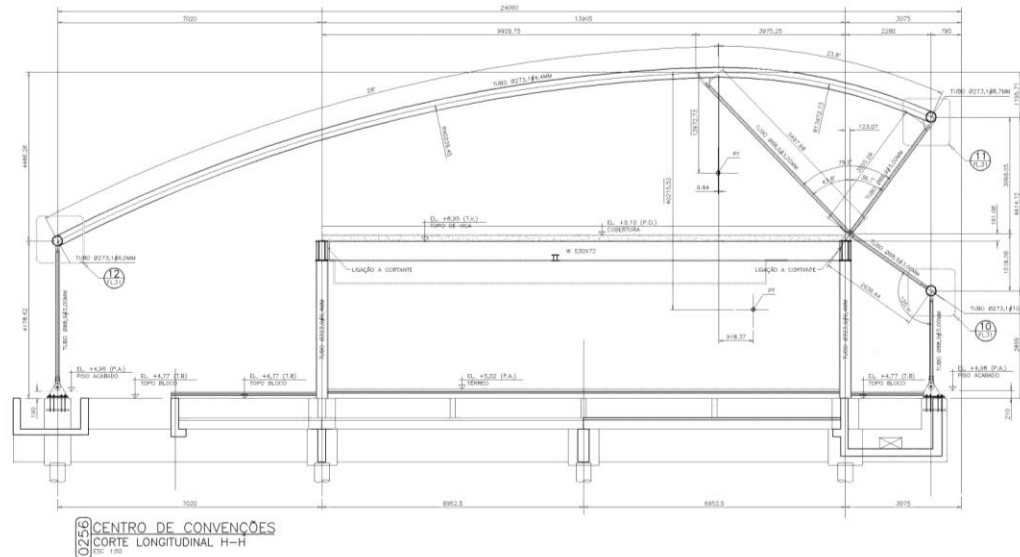
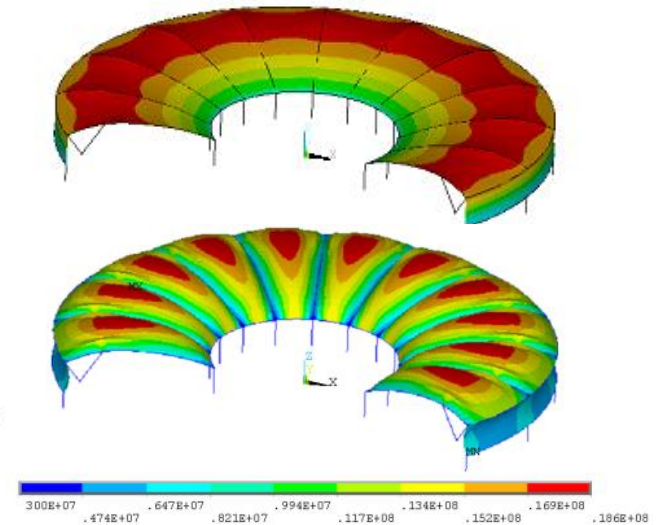
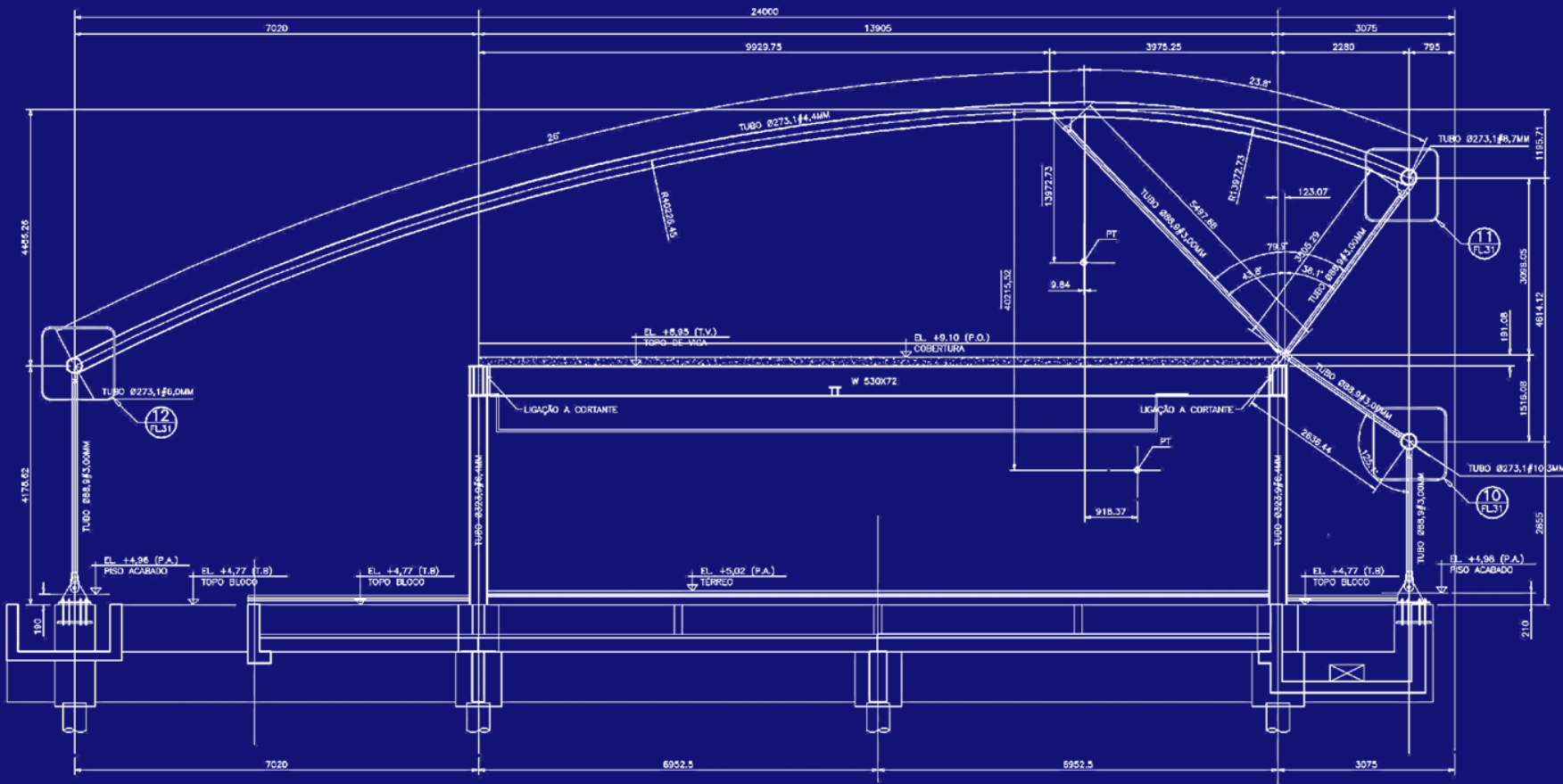


Figura 4 – À esquerda, distribuição da velocidade do vento no nível do pedestre, a 1,5m. Observar escala de velocidades de 0m/s a 3m/s. À direita, distribuição de pressões de vento sobre as envoltórias.






**CENTRO DE CONVENÇÕES**  
 CORTE LONGITUDINAL H-H  
 ESC. 1:50





# Membranes on top of 'Morro da Urca', Rio de Janeiro, 2014

Designers:

(1) Nelson Fielder

(2) Pedro Marcelo Pain de Santana







**Olympic Golf Field, Rio de Janeiro, 2016**



Olympic Golf Field, Rio de Janeiro, 2016



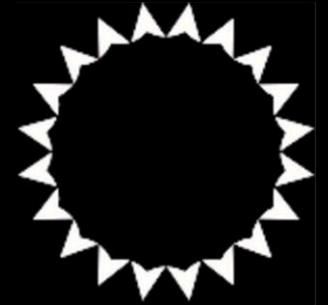
**Olympic Golf Field, Rio de Janeiro, 2016**



*EP-USP*

*PEF2602.*

*Estruturas na Arquitetura I I - Sistemas Reticulados*



*FAU-USP*

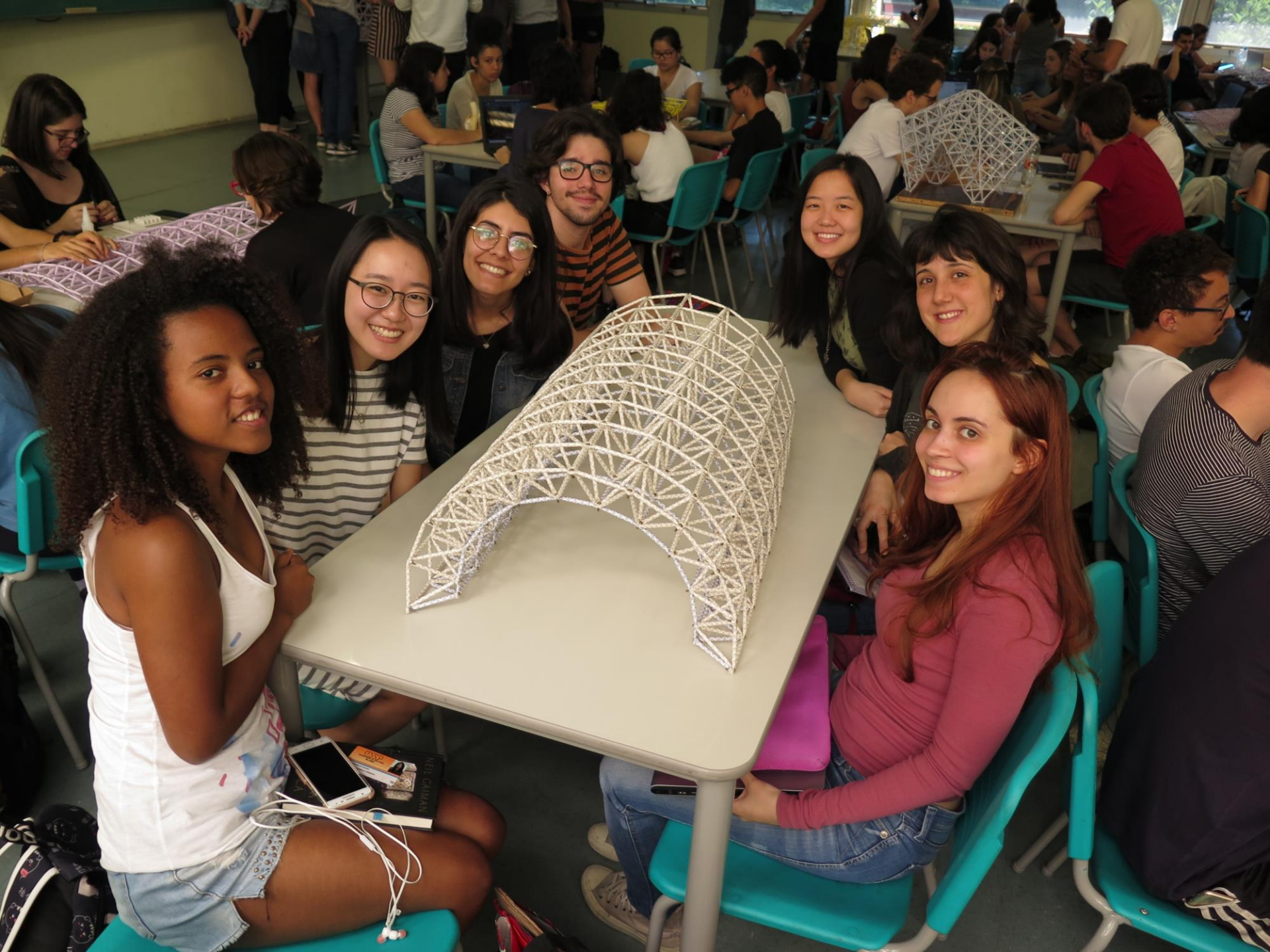
# *2º Trabalho em Grupo*

*Professores*

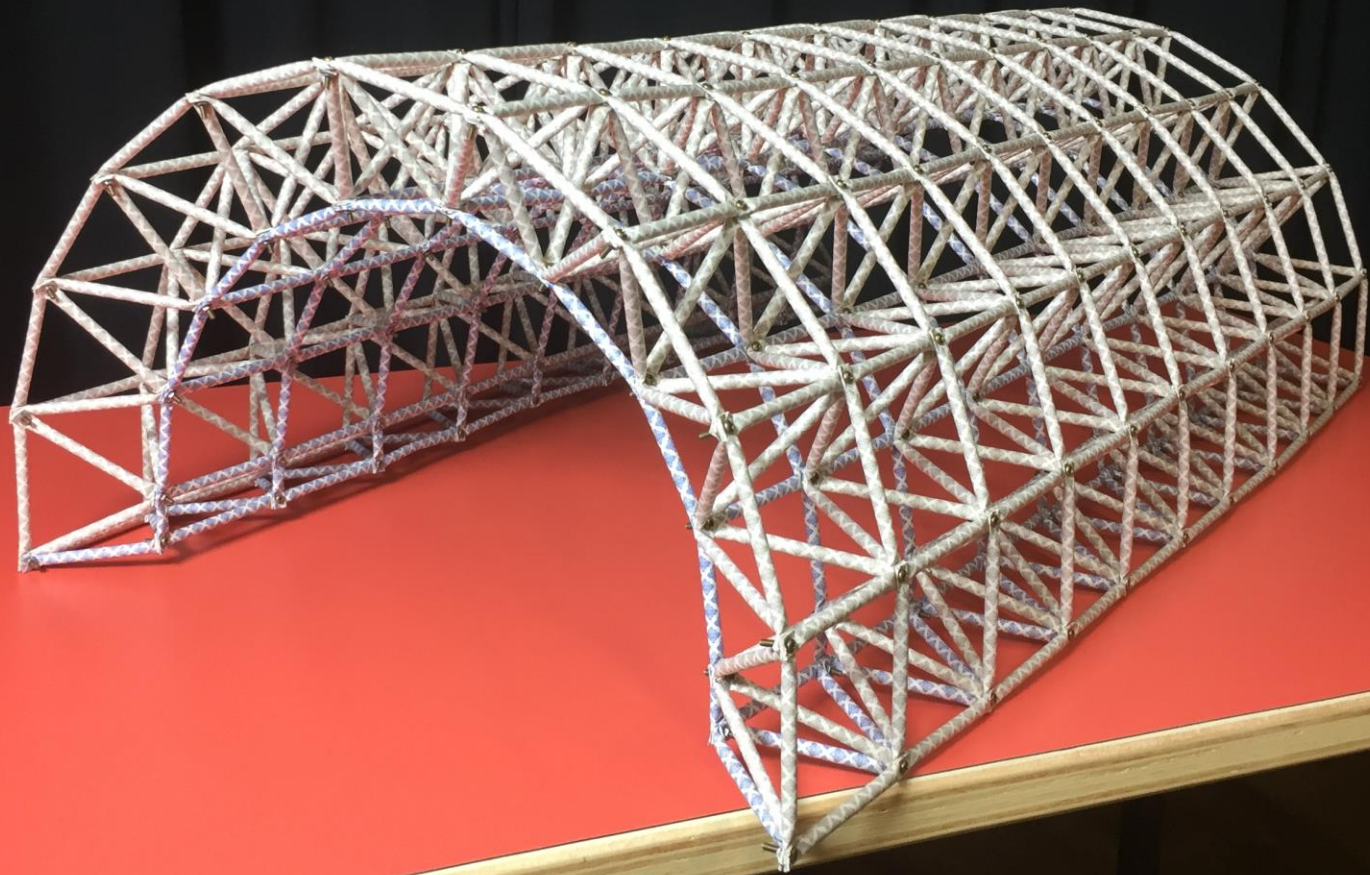
*Ruy Marcelo O. Pauletti , Leila Meneghetti Valverdes, Luís Bitencourt*

*1º Semestre 2019*







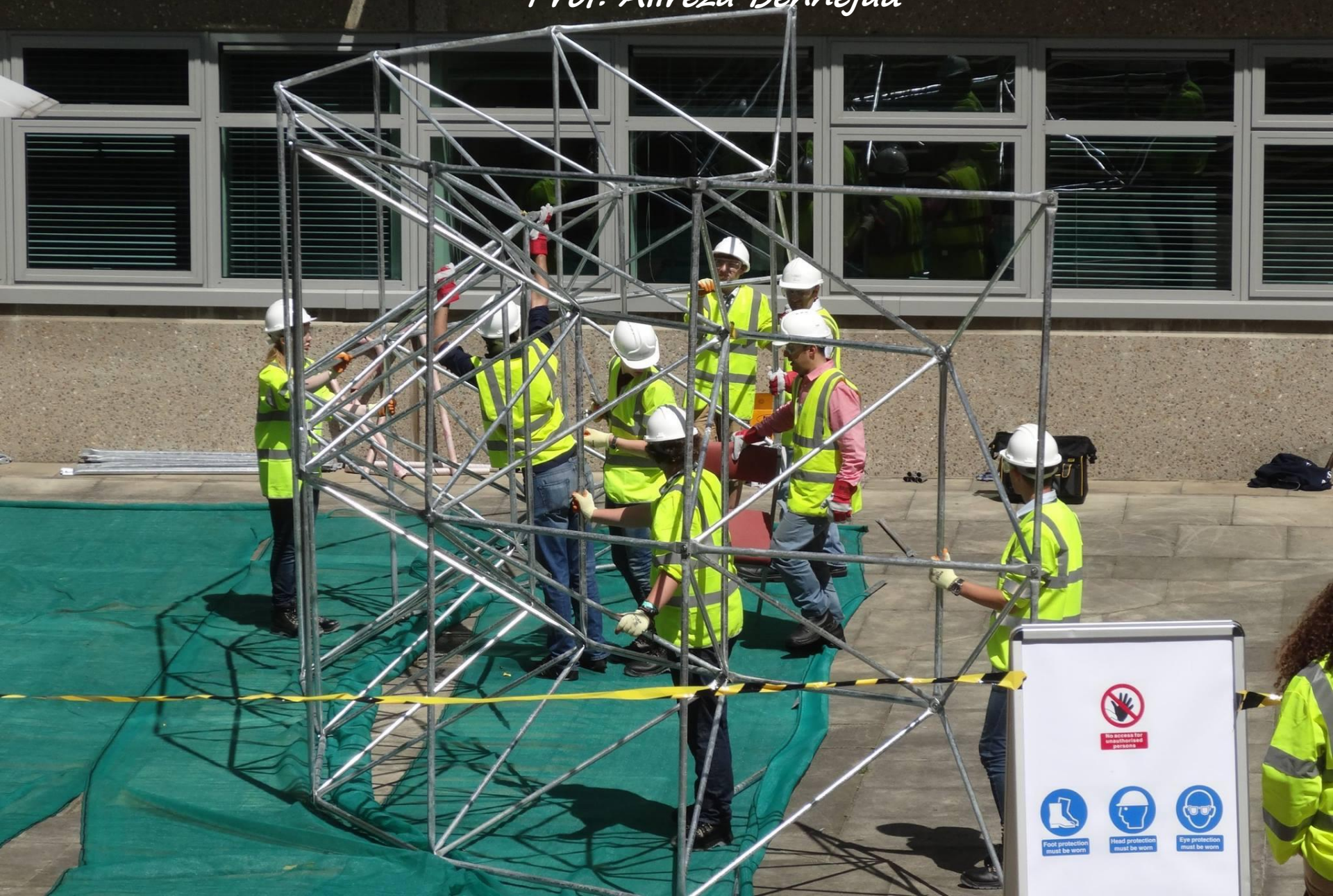


*DAD Project – University of Surrey, 2014*  
*Prof. Alireza Behnejad*



# DAD Project – University of Surrey, 2014

Prof. Alireza Behnejad



*DAD Project – University of Surrey, 2014*  
*Prof. Alireza Behnejad*

