

INF3580/4580 – Semantic Technologies – Spring 2018

Lecture 11: OWL 2

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INFORMATICS



UNIVERSITY OF
OSLO

Outline

- 1 Reminder: *ALC*
- 2 Important assumptions
- 3 OWL 2
 - Axioms and assertions using individuals
 - Concept Restrictions
 - Modelling 'problems'
 - Roles
 - Datatypes

The \mathcal{ALC} Description Logic

Vocabulary

Fix a set of *atomic concepts* $\{A_1, A_2, \dots\}$, *roles* $\{R_1, R_2, \dots\}$ and *individuals* $\{a_1, a_2, \dots\}$.

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	$\exists R_i.C$		(existential restriction)

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Axioms

- $C \sqsubseteq D$ and $C \equiv D$ for concept descriptions D and C .
- $C(a)$ and $R(a, b)$ for concept description C , atomic role R and individuals a, b .

\mathcal{ALC} Semantics

Interpretation

An interpretation \mathcal{I} fixes a set $\Delta^{\mathcal{I}}$, the *domain*, $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ for each atomic concept A , $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ for each role R , and $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ for each individual a .

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Interpretation of Axioms

- $\mathcal{I} \models C \sqsubseteq D$ if $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ and $\mathcal{I} \models C \equiv D$ if $C^{\mathcal{I}} = D^{\mathcal{I}}$
- $\mathcal{I} \models C(a)$ if $a^{\mathcal{I}} \in C^{\mathcal{I}}$ and $\mathcal{I} \models R(a, b)$ if $\langle a^{\mathcal{I}}, b^{\mathcal{I}} \rangle \in R^{\mathcal{I}}$.

\mathcal{ALC} Examples

Let \mathcal{K} be the following set of axioms:

$$Penguin \sqsubseteq Animal \sqcap \forall eats.Fish$$

$$Penguin \sqcap Fish \sqsubseteq \perp$$

$$Penguin(a)$$

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Now $\mathcal{I} \models \mathcal{K}$.

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Now $\mathcal{J} \not\models \mathcal{K}$ since $\mathcal{J} \not\models Penguin \sqcap Fish \sqsubseteq \perp$.

Modelling patterns

So, what can we say with ACC ?

- ✓ Every person has a mother.
- ✓ Penguins eats only fish. Horses eats only chocolate.
- ✗ Every nuclear family has two parents, at least two children and a dog.
- ✓ No smoker is a non-smoker (and vice versa).
- ✗ Everybody loves Mary.
- ✗ Adam is not Eve (and vice versa).
- ✓ Everything is black or white.
- ✓ There is no such thing as a free lunch.
- ✗ Brothers of fathers are uncles.
- ✗ My friend's friends are also my friends.
- ✗ If Homer is married to Marge, then Marge is married to Homer.
- ✗ If Homer is a parent of Bart, then Bart is a child of Homer.

Today we'll learn how to say more.

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World assumptions

- Closed World Assumption (CWA)
- Open World Assumption (OWA)

CWA:

- Complete knowledge.
- Any statement that is not known to be true is false. (*)
- Typical semantics for database systems.

OWA:

- Potential incomplete knowledge.
- (*) does not hold.
- Typical semantics for logic-based systems.

Name assumptions

- Unique name assumption (UNA)
- Non-unique name assumption (NUNA)
- Under any assumption, equal names (read: individual URIs, DB constants) always denote the same “thing” (obviously).
 - E.g., cannot have $a^I \neq a^I$.
- Under UNA, different names *always* denote different things.
 - E.g., $a^I \neq b^I$.
 - common in relational databases.
- Under NUNA, different names *need not* denote different things.
 - Can have , $a^I = b^I$, or
 - $\text{dbpedia:0slo}^I = \text{geo:34521}^I$.

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$SROIQ(\mathcal{D})$ and OWL 2

- OWL 2 is based on the DL $SROIQ(\mathcal{D})$:
 - \mathcal{S} for \mathcal{ALC}^1 plus role transitivity,
 - \mathcal{R} for (complex) roles inclusions,
 - \mathcal{O} for closed classes,
 - \mathcal{I} for inverse roles,
 - \mathcal{Q} for qualified cardinality restrictions, and
 - \mathcal{D} for datatypes.

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 - \mathcal{D} for datatypes.
- So, today we'll see:
 - new concept and role builders,
 - new TBox axioms,
 - new ABox axioms,
 - new RBox axioms, and
 - datatypes.

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 - DL: $a = b$, $a \neq b$;
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- Remember:
 - Non unique name assumption (NUNA) in Sem. Web,
 - must sometimes use `=` and `≠` to get expected results.

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- Example:
 - $SimpsonFamily \equiv \{Homer, Marge, Bart, Lisa, Maggie\}$
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- Note:
 - The individuals does not necessarily represent different objects,
 - we still need $=$ and \neq to say that members are the same/different.
 - “Closed classes of data values” are *datatypes*.

Axioms involving individuals: Negative Property Assertions

- New ABox axiom.
- Syntax:
 - DL: $\neg R(a, b)$,
 - RDF/OWL: `owl:NegativePropertyAssertion` (Class of assertions/triples)
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 - Works both for object properties and datatype properties.
- Examples:
 - `:Bart not :hasFather :NedFlanders`
 - `:Bart not :hasAge "2"^^xsd:int`

Outline

- 1 Reminder: *ALC*
- 2 Important assumptions
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 - **Concept Restrictions**
 - Modelling 'problems'
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Recap of existential and universal restrictions

- Existential restrictions
 - have the form $\exists R.D$,
 - typically used to connect classes,
 - $C \sqsubseteq \exists R.D$: A C is R -related to (at least) *some* D :
 - Example: A person has a female parent: $Person \sqsubseteq \exists hasParent.Woman$.
 - Note that C -objects can be R -related to other things:
 - A person may have other parents who are not women—but there should be one who's a woman.

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- Universal restrictions

- have the form $\forall R.D$,
- restrict the things an object can be connected to,
- $C \sqsubseteq \forall R.D$: C is R -related to D 's *only*:
 - Example: A horse eats only chocolate: $Horse \sqsubseteq \forall eats.Chocolate$.
- Note that C -objects may not be R -related to anything at all:
 - A horse does not have to eat something—but if it does it must be chocolate.

Cardinality restrictions

- New concept builder.
- Syntax:
 - DL: $\leq_n R.D$ and $\geq_n R.D$ (and $=_n R.D$).
 - RDF/OWL: `owl:minCardinality`, `owl:maxCardinality`, `owl:cardinality`.
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- Semantics:
 - $(\leq_n R.D)^{\mathcal{I}} = \{a \in \Delta^{\mathcal{I}} : |\{b : \langle a, b \rangle \in R^{\mathcal{I}} \wedge b \in D^{\mathcal{I}}\}| \leq n\}$
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- Restricts the number of relations a type of object can/must have.
- TBox axioms read:
 - $C \sqsubseteq \square_n R.D$: "A C is R-related to n number of D's."
 - \leq : *at most*
 - \geq : *at least*
 - $=$: *exactly*

Example cardinality restriction

- $Car \sqsubseteq \leq_2 driveAxle.T$
 - “A car has at most two drive axles.”

Example cardinality restriction

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 - “A mammal has one parent that is a female and one parent that is a male.”
- $\geq_2 owns.Houses \sqcup \geq_5 own.Car \sqsubseteq Rich$
 - “Everyone who owns more than two houses or five cars is rich.”

One more value restriction

- Restrictions of the form $\forall R.D$, $\exists R.D$, $\leq_n R.D$, $\geq_n R.D$ are called *qualified* when D is not \top .
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- Example:
 - $Bieberette \equiv Girl \sqcap \exists loves.\{J.Bieber\}$
 - $\top \sqsubseteq \exists loves.\{Mary\}$
 - $Norwegian \equiv Person \sqcap \exists citizenOf.\{Norway\}$

Self restriction

- New construct builder.
- Local reflexivity restriction. Restricts to objects which are related to themselves.
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- Examples:
 - $AutoregulatingProcess \sqsubseteq \exists regulate.Self$
 - $\exists hasBoss.Self \sqsubseteq SelfEmployed$

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Restrictions, non-unique names and open worlds

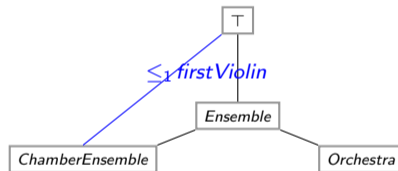
Restrictions + the OWA and the NUNA can be tricky, consider:

TBox:

$Orchestra \sqsubseteq Ensemble$

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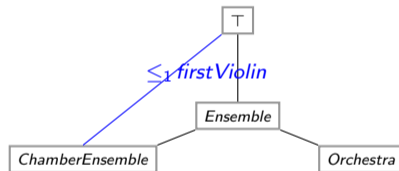
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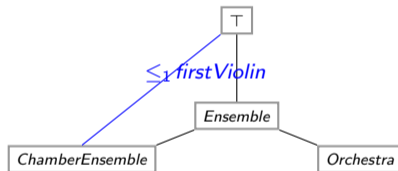
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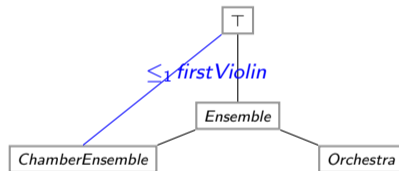
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- Orchestras and Chamber ensembles are Ensembles.
- Chamber ensembles have only one instrument on each voice,
- in particular, only one first violin.
- oslo has two first violins; is oslo an Orchestra?

Unexpected (non-)results

It does not follow from $TBox + ABox$ that $oslo$ is an *Orchestra*:

- An ensemble need neither be an orchestra nor a chamber ensemble, its “just” an ensemble.
- Add “covering axiom” $Ensemble \sqsubseteq Orchestra \sqcup ChamberEnsemble$:
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If we remove `firstViolin(oslo, lie)`, is oslo a *ChamberEnsemble*?

- it does not follow that oslo is a *ChamberEnsemble*.
- This is due to the OWA:
- oslo may have other first violinists.

Protégé demo of previous slide

- Make class Ensemble.
- Make subclass Orchestra.
- Make subclass ChamberEnsemble.
- Make object property firstViolin.
- Make `firstViolin` `max 1` superclass of ChamberEnsemble.
- Make an Ensemble `oslo`
- Make a Thing `skolem`
- Make a Thing `lie`
- Add `firstViolin` `skolem` to `oslo`
- Add `firstViolin` `lie` to `oslo`
- Classify! Nothing happens.
- Add covering axiom: `Orchestra` or `ChamberEnsemble` superclass of `Ensemble`.
- Classify! Nothing happens.
- `skolem` is different from `lie`
- Classify! Bingo! `oslo` is an `Orchestra`!

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Role characteristics and relationships (RBox)

Vocabulary

Given the *roles* $\{R_1, R_2, \dots\}$

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$R, S \rightarrow$	R_i		(atomic role)
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	$\neg R$		(complement role)
	R^-		(inverse role)
	$R \sqcap S$		(role intersection)
	$R \circ S$		(role chain)

Rbox (cont.)

- Role axioms: Let R and S be roles, then we can assert
 - subsumption: $R \sqsubseteq S$ $(R^{\mathcal{I}} \subseteq S^{\mathcal{I}})$,
 - equivalence: $R \equiv S$ $(R^{\mathcal{I}} = S^{\mathcal{I}})$,
 - disjointness: $R \sqcap S \sqsubseteq \perp_{\text{role}}$ $(R^{\mathcal{I}} \cap S^{\mathcal{I}} \subseteq \emptyset)$,
 - key: R is a key for concept C .

²Restrictions apply

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 - key: R is a key for concept C .
- A role can have the characteristics (axioms):
 - reflexive, irreflexive,
 - symmetric, asymmetric,
 - transitive, or/and²
 - functional, inverse functional.

²Restrictions apply

New roles

- The universal role, and the empty role—for both object roles and data roles.
- Syntax:
 - (DL: U (universal object role), D (universal data value role))
 - RDF/OWL, Manchester: `owl:topObjectProperty`, `owl:topDataProperty`,
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 - $U^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
 - $D^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Lambda$
- Reads:
 - all pairs of individuals are connected by `owl:topObjectProperty`,
 - no individuals are connected by `owl:bottomObjectProperty`.
 - all possible individuals are connected with all literals by `owl:topDataProperty`,
 - no individual is connected by `owl:bottomDataProperty` to a literal.

Corresponding mathematical properties and operations

If R and S are binary relations on X then

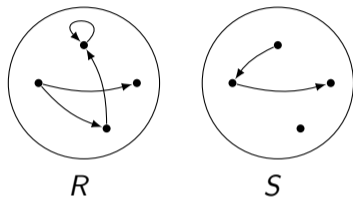
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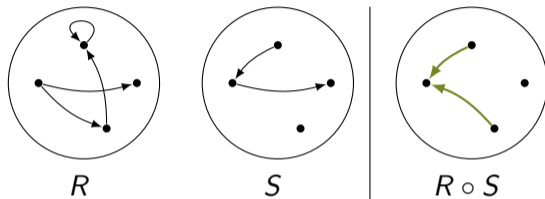
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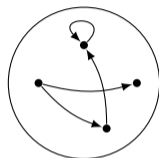
Role chaining and inverses illustrated



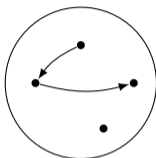
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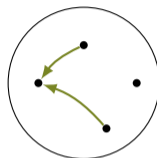
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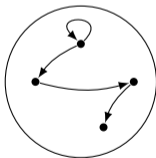
R



S

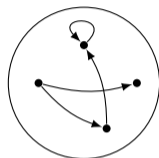
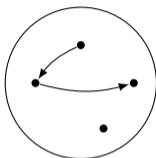
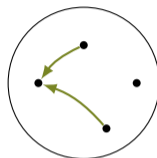
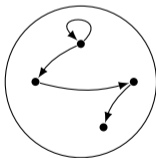
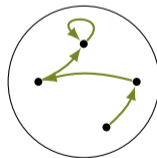


$R \circ S$



T

Role chaining and inverses illustrated

 R  S  $R \circ S$  T  T^{-}

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Functional:	if $\langle a, b \rangle, \langle a, c \rangle \in R$ implies $b = c$	$(\top \sqsubseteq \leq_1 R. \top)$

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Inverse functional:	if $\langle a, b \rangle, \langle c, b \rangle \in R$ implies $a = c$	$(\top \sqsubseteq \leq_1 R^- . \top)$

Properties in OWL

Remember: three kinds of *mutually disjoint* properties in OWL:

- ① `owl:DatatypeProperty`
 - link individuals to data values, e.g., `xsd:string`.
 - Examples: `:hasAge`, `:hasSurname`.
- ② `owl:ObjectProperty`
 - link individuals to individuals.
 - Example: `:hasFather`, `:driveAxle`.
- ③ `owl:AnnotationProperty`
 - has no logical implication, ignored by reasoners.
 - Examples: `rdfs:label`, `dc:creator`.

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- (Annotation properties have no logical implication, so nothing can be said about them.)

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Examples inverses and chains

Some inverses:

- $hasParent \equiv hasChild^{-}$
- $hasBiologicalMother \equiv gaveBirthTo^{-}$
- $olderThan \equiv youngerThan^{-}$



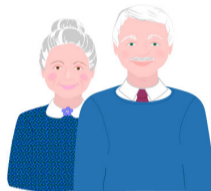
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- $hasParent \equiv hasChild^{-}$
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Some role chains:

- $hasParent \circ hasParent \sqsubseteq hasGrandParent$
- $hasAncestor \circ hasAncestor \sqsubseteq hasAncestor$
- $hasParent \circ hasBrother \sqsubseteq hasUncle$



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- Note:
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- Fortunately:
 - There are also *simple* patterns
 - that are quite useful.

Outline

- 1 Reminder: *ALC*
- 2 Important assumptions
- 3 OWL 2
 - Axioms and assertions using individuals
 - Concept Restrictions
 - Modelling 'problems'
 - Roles
 - Datatypes

Creating datatypes

- Many predefined datatypes are available in OWL:
 - all common XSD datatypes: `xsd:string`, `xsd:int`, ...
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- Example:
 - Teenager is equivalent to: (Manchester Person and (age some positiveInteger[\geq 13, \leq 19]))
 - “A teenager is a person of age 13 to 19.”

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So, what can we say now?

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... and more!

DL: Family of languages

`http://www.cs.man.ac.uk/~ezolin/dl/`

Next week

- More modelling with OWL/OWL 2.
- What cannot be expressed in OWL/OWL 2?