

EXPERIMENTAL DESIGNS APPLIED TO HIGH-THROUGHPUT PHENOTYPING IN PLANT BREEDING

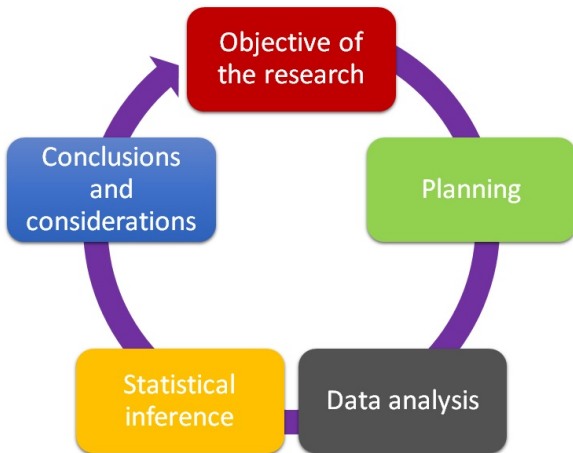
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Department of Genetics

September 12, 2017





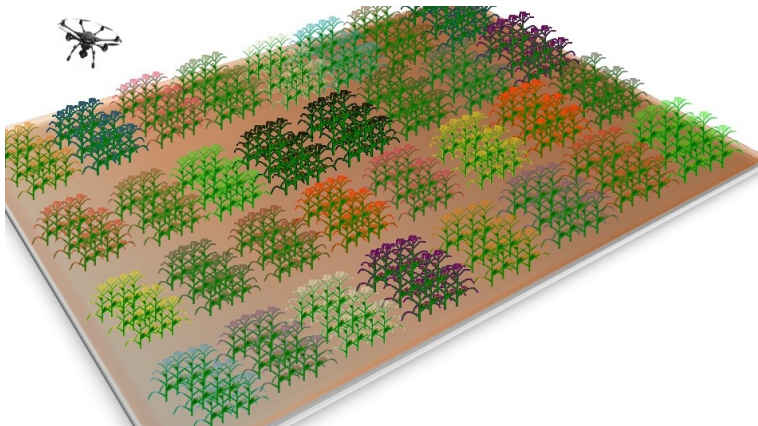
Experimental Designs

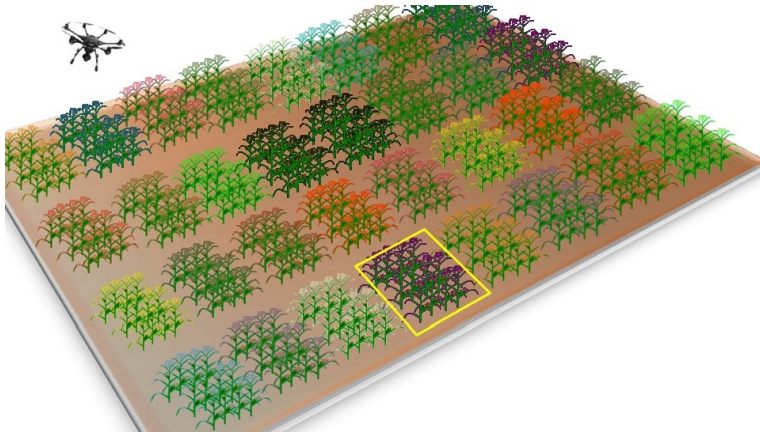
Experimental Structures

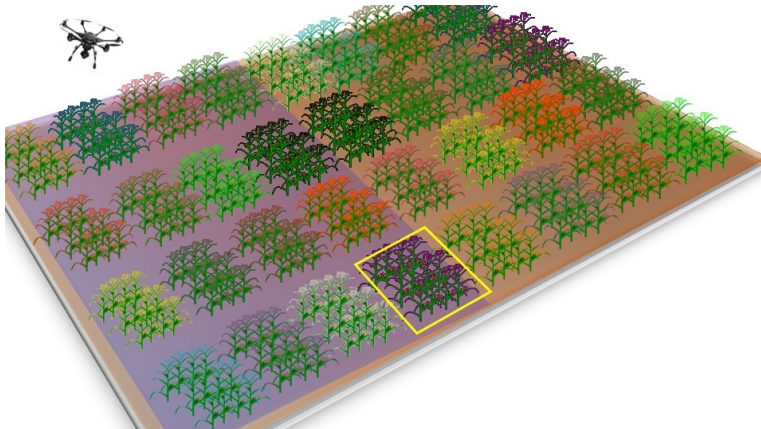
Data Collection

Statistical Issues



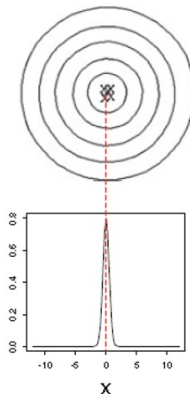






Accuracy

$$\hat{r}_{g\hat{g}} = \frac{\sigma_{g\hat{g}}^2}{\sqrt{\sigma_g^2 \cdot \sigma_{\hat{g}}^2}} = \sqrt{h^2}$$



(FRITSCH NETO & BORÉM, 2015)

Plot

Size and shape

- ✓ To reduce the experimental error
- ✓ Must be uniform
- ✓ Methods to estimate the optimal plot size
- ✓ Which is the best shape?
 - Environment effects
 - Image-based data collection

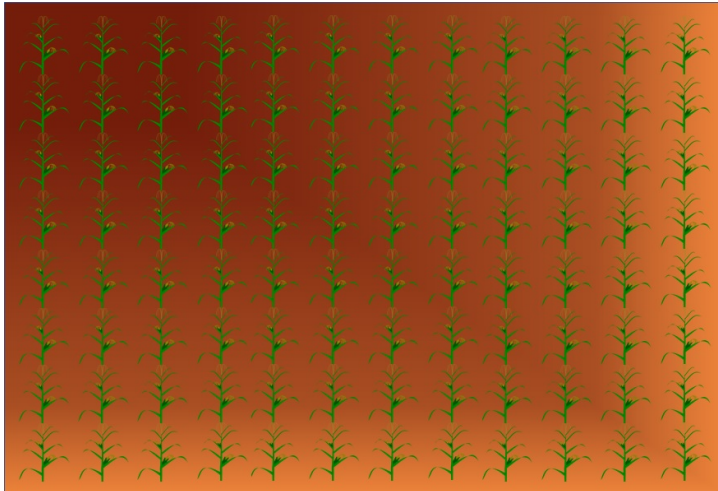


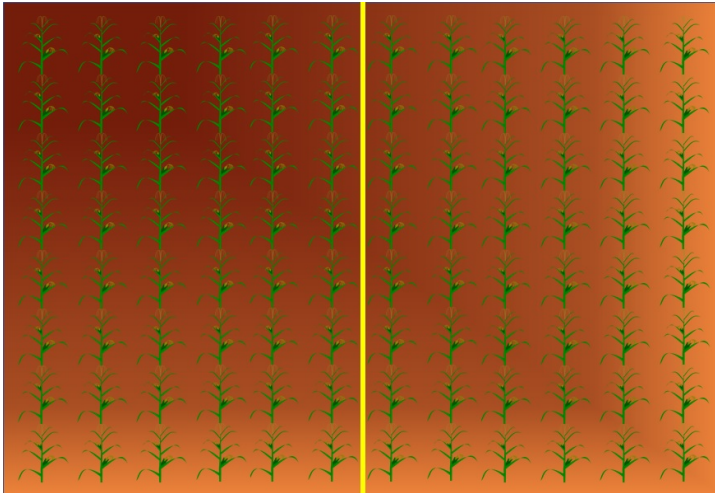
Plot

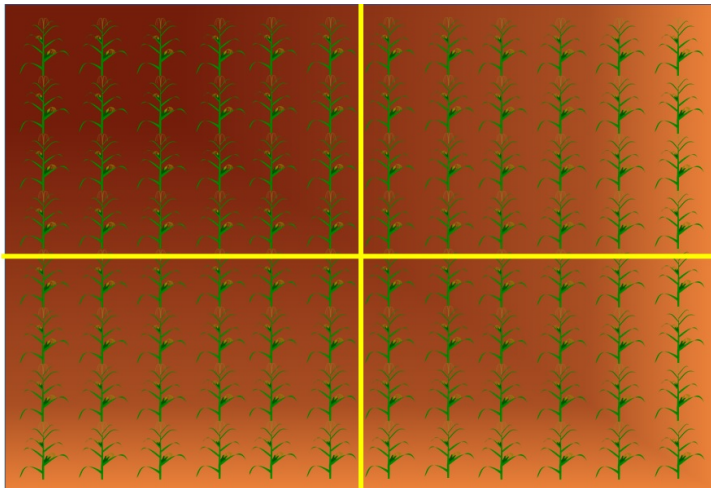
Size and shape

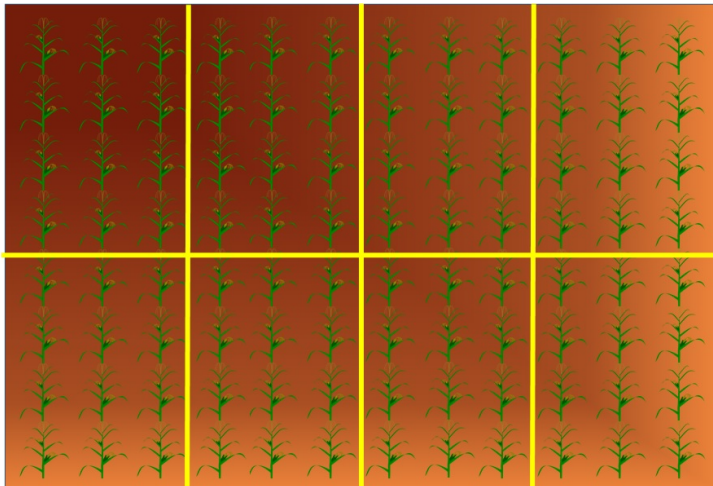
- ✓ To reduce the experimental error
- ✓ Must be uniform
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 - Environment effects
 - Image-based data collection

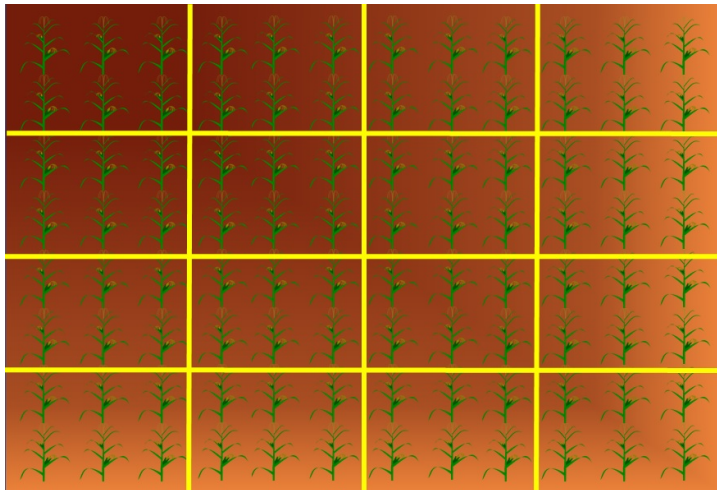


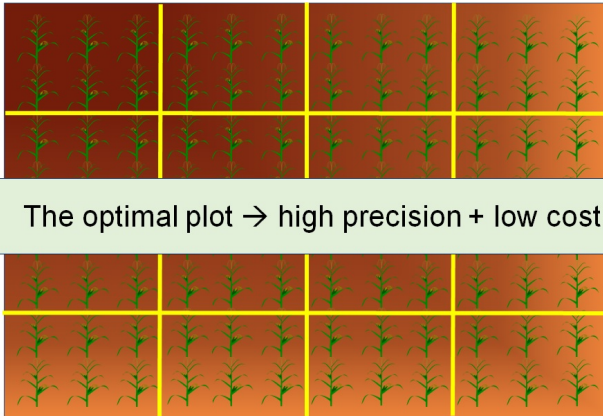










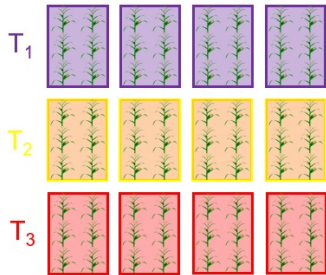




Basic principles of experimental design

1st: Replication

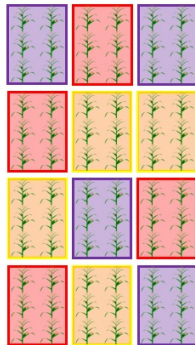
- ✓ To estimate the experimental variation
- ✓ How many replications are necessary?



Basic principles of experimental design

2nd: Randomization

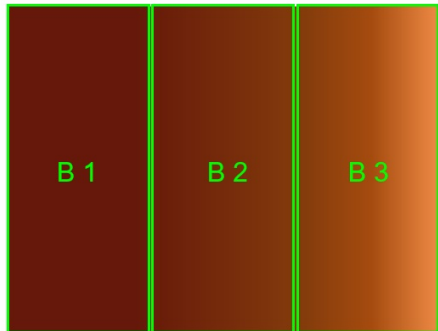
- ✓ All treatments have the same probability to be in any plot



Basic principles of experimental design

3rd: Local control

- ✓ Area is divided in homogenous blocks (*blocking*)

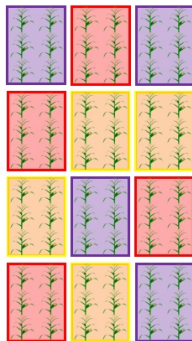


Completely Randomized Design

- ✓ Homogeneous experimental area
- ✓ Statistical model:

$$Y_{ij} = \mu + t_i + \varepsilon_{ij}$$

- ✓ Source of variation (S.V.) → treatments



Randomization



```
n <- 10 #number of Plots
Standard.Order <- factor(1:n)
Standard.Order
Variety <- factor(rep(c("A", "B", "C"), times = c(3, 4, 3)))
Variety
Plot <- order(r<-runif(n)) # generates 12 random numbers and use the order
# of them as the number for a Plot
r
Plot
CRDPotato.Design <- data.frame(Standard.Order,Plot,Variety)
CRDPotato.Design
remove("Standard.Order", "Plot", "Variety")
CRDPotato.Design[CRDPotato.Design$"Plot",] <- CRDPotato.Design #sort according to
CRDPotato.Design #use the last two columns to give to the scientist
```

| | Standard.Order | Plot | Variety |
|----|----------------|------|---------|
| 1 | 1 | 8 | A |
| 2 | 2 | 6 | A |
| 3 | 3 | 3 | A |
| 4 | 4 | 2 | B |
| 5 | 5 | 9 | B |
| 6 | 6 | 1 | B |
| 7 | 7 | 10 | B |
| 8 | 8 | 4 | C |
| 9 | 9 | 7 | C |
| 10 | 10 | 5 | C |

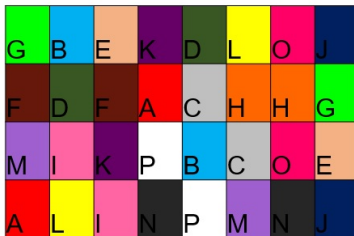
Figure 1: Before randomization.

| | Standard.Order | Plot | Variety |
|----|----------------|------|---------|
| 1 | 6 | 1 | B |
| 2 | 4 | 2 | B |
| 3 | 3 | 3 | A |
| 4 | 8 | 4 | C |
| 5 | 10 | 5 | C |
| 6 | 2 | 6 | A |
| 7 | 9 | 7 | C |
| 8 | 1 | 8 | A |
| 9 | 5 | 9 | B |
| 10 | 7 | 10 | B |

Figure 2: After randomization.

Table 1. Output from R (package *agricolae*) for a randomization of a completely randomized design experiment, with 16 treatments and two replications.

| plots | r | trat | plots | r | trat |
|-------|---|------|-------|---|------|
| 1 | 1 | G | 17 | 1 | M |
| 2 | 1 | B | 18 | 1 | I |
| 3 | 1 | E | 19 | 2 | K |
| 4 | 1 | K | 20 | 1 | P |
| 5 | 1 | D | 21 | 2 | B |
| 6 | 1 | L | 22 | 2 | C |
| 7 | 1 | O | 23 | 2 | O |
| 8 | 1 | J | 24 | 2 | E |
| 9 | 1 | F | 25 | 2 | A |
| 10 | 2 | D | 26 | 2 | L |
| 11 | 2 | F | 27 | 2 | I |
| 12 | 1 | A | 28 | 1 | N |
| 13 | 1 | C | 29 | 2 | P |
| 14 | 1 | H | 30 | 2 | M |
| 15 | 2 | H | 31 | 2 | N |
| 16 | 2 | G | 32 | 2 | J |



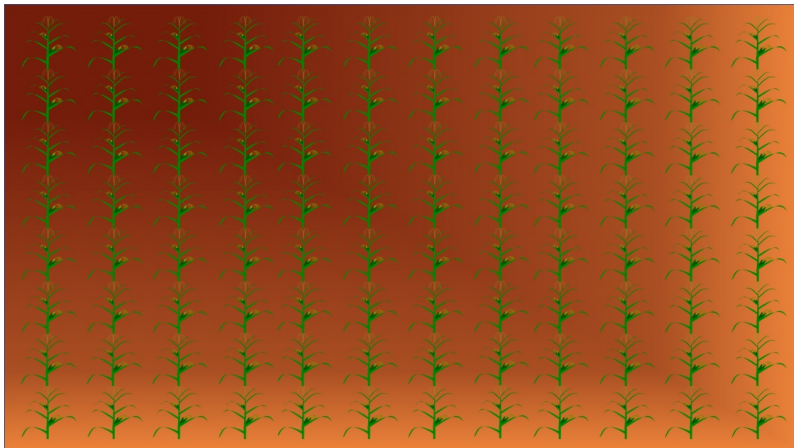
Randomized blocks design

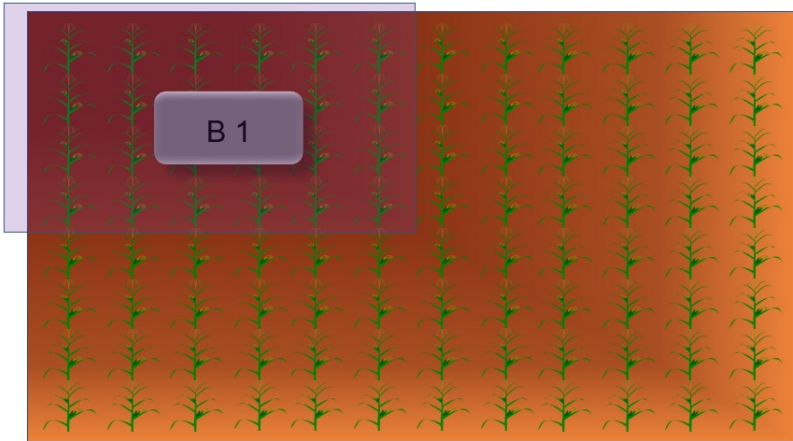
- ✓ Replication, randomization and local control are essential
- ✓ Blocks may contain the same replication of all treatments
- ✓ Randomization inside the blocks

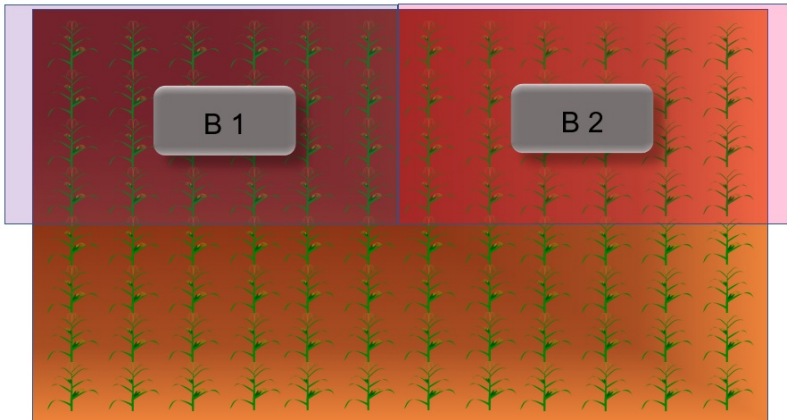
Statistical model:

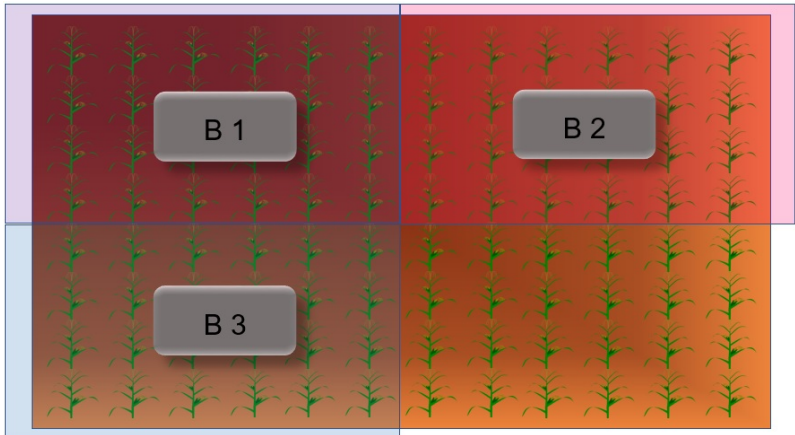
$$Y_{ij} = \mu + \underbrace{t_i + b_j}_{\text{S.V.}} + \varepsilon_{ij}$$

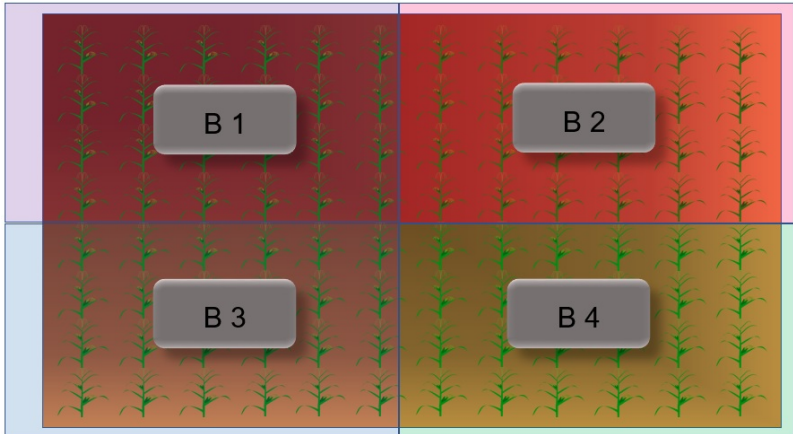
S.V.











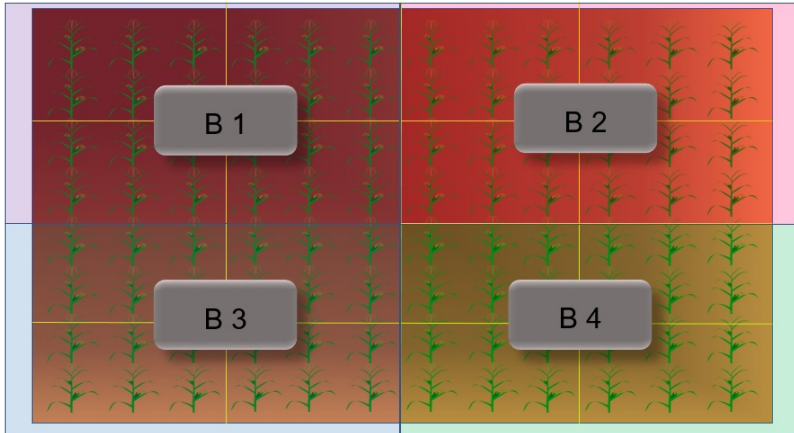


Table 2. Output from R (package *agricolae*) for a randomization of a RCBD, with 16 treatments and two replications.

| plots | block | trat | plots | block | trat |
|-------|-------|------|-------|-------|------|
| 101 | 1 | H | 201 | 2 | O |
| 102 | 1 | L | 202 | 2 | K |
| 103 | 1 | D | 203 | 2 | M |
| 104 | 1 | P | 204 | 2 | I |
| 105 | 1 | B | 205 | 2 | G |
| 106 | 1 | G | 206 | 2 | L |
| 107 | 1 | N | 207 | 2 | B |
| 108 | 1 | E | 208 | 2 | F |
| 109 | 1 | M | 209 | 2 | J |
| 110 | 1 | I | 210 | 2 | H |
| 111 | 1 | J | 211 | 2 | E |
| 112 | 1 | O | 212 | 2 | N |
| 113 | 1 | A | 213 | 2 | C |
| 114 | 1 | F | 214 | 2 | A |
| 115 | 1 | C | 215 | 2 | P |
| 116 | 1 | K | 216 | 2 | D |

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| 102 | 1 | L | 202 | 2 | K |
| 103 | 1 | D | 203 | 2 | M |
| 104 | 1 | P | 204 | 2 | I |
| 105 | 1 | B | 205 | 2 | G |
| 106 | 1 | G | 206 | 2 | L |
| 107 | 1 | N | 207 | 2 | B |
| 108 | 1 | E | 208 | 2 | F |
| 109 | 1 | M | 209 | 2 | J |
| 110 | 1 | I | 210 | 2 | H |
| 111 | 1 | J | 211 | 2 | E |
| 112 | 1 | O | 212 | 2 | N |
| 113 | 1 | A | 213 | 2 | C |
| 114 | 1 | F | 214 | 2 | A |
| 115 | 1 | C | 215 | 2 | P |
| 116 | 1 | K | 216 | 2 | D |

| Block 1 | | | | Block 2 | | | |
|------------|------------|------------|------------|------------|------------|------------|------------|
| H P_101 | B P_105 | M P_109 | A P_101 | O P_201 | G P_205 | J P_209 | C P_213 |
| L P_102 | G P_106 | I P_110 | F P_114 | K P_202 | L P_206 | H P_210 | A P_214 |
| D P_103 | N P_107 | J P_101 | C P_115 | M P_203 | B P_207 | E P_211 | P P_215 |
| P P_104 | E P_108 | O P_112 | K P_116 | I P_204 | F P_208 | N P_212 | D P_216 |

Table 2. Output from R (package *agricolae*) for a randomization of a RCBD, with 16 treatments and two replications.

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| 102 | 1 | L | 202 | 2 | K |
| 103 | 1 | D | 203 | 2 | M |
| 104 | 1 | P | 204 | 2 | I |
| 105 | 1 | B | 205 | 2 | G |
| 106 | 1 | G | 206 | 2 | L |
| 107 | 1 | N | 207 | 2 | B |
| 108 | 1 | E | 208 | 2 | F |
| 109 | 1 | M | 209 | 2 | J |
| 110 | 1 | I | 210 | 2 | H |
| 111 | 1 | J | 211 | 2 | E |
| 112 | 1 | O | 212 | 2 | N |
| 113 | 1 | A | 213 | 2 | C |
| 114 | 1 | F | 214 | 2 | A |
| 115 | 1 | C | 215 | 2 | P |
| 116 | 1 | K | 216 | 2 | D |

| Block 1 | | | | Block 2 | | | |
|---------|-------|-------|-------|---------|-------|-------|-------|
| H | B | M | A | O | G | J | C |
| P_101 | P_105 | P_109 | P_101 | P_201 | P_205 | P_209 | P_213 |
| L | G | I | F | K | L | H | A |
| P_102 | P_106 | P_110 | P_114 | P_202 | P_206 | P_210 | P_214 |
| D | N | J | C | M | B | E | P |
| P_103 | P_107 | P_101 | P_115 | P_203 | P_207 | P_211 | P_215 |
| P | E | O | K | I | F | N | D |
| P_104 | P_108 | P_112 | P_116 | P_204 | P_208 | P_212 | P_216 |

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| 105 | 1 | B | 205 | 2 | G |
| 106 | 1 | G | 206 | 2 | L |
| 107 | 1 | N | 207 | 2 | B |
| 108 | 1 | E | 208 | 2 | F |
| 109 | 1 | M | 209 | 2 | J |
| 110 | 1 | I | 210 | 2 | H |
| 111 | 1 | J | 211 | 2 | E |
| 112 | 1 | O | 212 | 2 | N |
| 113 | 1 | A | 213 | 2 | C |
| 114 | 1 | F | 214 | 2 | A |
| 115 | 1 | C | 215 | 2 | P |
| 116 | 1 | K | 216 | 2 | D |

| Block 1 | | | | Block 2 | | | |
|------------|------------|------------|------------|------------|------------|------------|------------|
| H P_101 | B P_105 | M P_109 | A P_101 | O P_201 | G P_205 | J P_209 | C P_213 |
| L P_102 | G P_106 | I P_110 | F P_114 | K P_202 | L P_206 | H P_210 | A P_214 |
| D P_103 | N P_107 | J P_101 | C P_115 | M P_203 | B P_207 | E P_211 | P P_215 |
| P P_104 | E P_108 | O P_112 | K P_116 | I P_204 | F P_208 | N P_212 | D P_216 |

Double local control designs - Latin Square Design (LSD)

- ✓ Blocks are build in rows and columns (complete blocks)
- ✓ Replication number = treatment number

$$Y_{ijk} = \mu + c_i + l_j + t_k + \varepsilon_{ij}$$

S.V.

- ✓ e.g.: t = 5 ; r = 5 (LSD) →

| | col_1 | col_2 | col_3 | col_4 | col_5 |
|------|-------|-------|-------|-------|-------|
| row1 | E | B | C | A | D |
| row2 | C | E | A | D | B |
| row3 | D | A | B | E | C |
| row4 | A | C | D | B | E |
| row5 | B | D | E | C | A |

| | CRD | RBD | LSD |
|----------------------|--|--|--|
| Main characteristics | <ul style="list-style-type: none"> - Replication - Randomization | <ul style="list-style-type: none"> - Replication - Randomization - Simple local control | <ul style="list-style-type: none"> - Replication - Randomization - Double local control |
| Utilization | Homogenous environment (ex.: green house) | Field experiments (heterogeneous area) | Very heterogeneous area |
| Causes of variation | Treatments | Treatments and blocks | Treatments, rows and columns |
| Advantages | Highest D.F. for residuals | Precise estimation of residual variation | Residuals are better estimated |
| Disadvantages | Requires homogeneous area | Plot homogeneity is required within each block | Number of plots increases exponentially as we increase number of treatments |
| Model | $Y_{ij} = \mu + t_i + \varepsilon_{ij}$ | $Y_{ij} = \mu + t_i + b_j + \varepsilon_{ij}$ | $Y_{ijk} = \mu + c_i + l_j + t_k + \varepsilon_{ij}$ |

Experimental Structures- Differences

Factorial Design in Blocks

| Block 1 | Block 2 | Block 3 | Block 4 | Block 5 |
|-----------|-----------|-----------|-----------|-----------|
| $S_1 V_3$ | $S_1 V_2$ | $A_0 V_3$ | $S_1 V_3$ | $A_0 V_2$ |
| $A_0 V_2$ | $A_0 V_1$ | $S_1 V_2$ | $A_0 V_3$ | $S_1 V_1$ |
| $A_0 V_1$ | $S_1 V_3$ | $A_0 V_2$ | $S_1 V_2$ | $S_1 V_3$ |
| $S_1 V_2$ | $S_1 V_1$ | $S_1 V_3$ | $A_0 V_1$ | $A_0 V_1$ |
| $A_0 V_3$ | $A_0 V_3$ | $S_1 V_2$ | $S_1 V_1$ | $A_0 V_3$ |
| $S_1 V_1$ | $A_0 V_2$ | $A_0 V_1$ | $A_0 V_2$ | $S_1 V_2$ |

Experimental Structures- Differences

Factorial Design in Blocks

| Block 1 | Block 2 | Block 3 | Block 4 | Block 5 |
|-----------|-----------|-----------|-----------|-----------|
| $A_1 V_3$ | $A_1 V_2$ | $A_0 V_3$ | $A_1 V_3$ | $A_0 V_2$ |
| $A_0 V_2$ | $A_0 V_1$ | $A_1 V_1$ | $A_0 V_3$ | $A_1 V_1$ |
| $A_0 V_1$ | $A_1 V_3$ | $A_0 V_2$ | $A_1 V_2$ | $A_1 V_3$ |
| $A_1 V_2$ | $A_1 V_1$ | $A_1 V_2$ | $A_0 V_1$ | $A_0 V_1$ |
| $A_0 V_3$ | $A_0 V_3$ | $A_1 V_3$ | $A_1 V_1$ | $A_0 V_3$ |
| $A_1 V_1$ | $A_0 V_2$ | $A_0 V_1$ | $A_0 V_2$ | $A_1 V_2$ |

Split Plots in Blocks

| Block 1 | Block 2 | Block 3 | Block 4 | Block 5 |
|-----------|-----------|-----------|-----------|-----------|
| $A_1 V_2$ | $A_1 V_1$ | $A_0 V_2$ | $A_1 V_1$ | $A_0 V_3$ |
| $A_1 V_1$ | $A_1 V_3$ | $A_0 V_3$ | $A_1 V_2$ | $A_0 V_1$ |
| $A_1 V_3$ | $A_1 V_2$ | $A_0 V_1$ | $A_1 V_3$ | $A_0 V_2$ |
| $A_0 V_2$ | $A_0 V_3$ | $A_1 V_3$ | $A_0 V_2$ | $A_1 V_2$ |
| $A_0 V_3$ | $A_0 V_1$ | $A_1 V_2$ | $A_0 V_3$ | $A_1 V_1$ |
| $A_0 V_1$ | $A_0 V_2$ | $A_1 V_1$ | $A_0 V_1$ | $A_1 V_3$ |

ANOVA

Table: Factorial Design in Blocks

| Source | df |
|----------------|---------------|
| Block | $r-1$ |
| Factor A | $a-1$ |
| Factor B | $b-1$ |
| $(A \times B)$ | $(a-1)(b-1)$ |
| Residual | $(ab-1)(r-1)$ |

ANOVA

Table: Factorial Design in Blocks

| Source | df |
|----------------|---------------|
| Block | $r-1$ |
| Factor A | $a-1$ |
| Factor B | $b-1$ |
| $(A \times B)$ | $(a-1)(b-1)$ |
| Residual | $(ab-1)(r-1)$ |

Table: Split Plots in Blocks

| Source | df |
|----------------|---------------|
| Block | $r-1$ |
| Factor A | $a-1$ |
| Residual (a) | $(r-1)(a-1)$ |
| Factor B | $b-1$ |
| $(A \times B)$ | $(a-1)(b-1)$ |
| Residual (b) | $a(b-1)(r-1)$ |



α – *Design*

Principles

- ✓ Randomization



α – *Design*

Principles

- ✓ Randomization
- ✓ Local control

α – *Design*

Principles

- ✓ Randomization
- ✓ Local control
- ✓ Replications

α – Design

Principles

- ✓ Randomization
- ✓ Local control
- ✓ Replications

Example

| Replication-I | | | | Replication-II | | | | Replication-III | | | |
|---------------|----|----|----|----------------|----|----|----|-----------------|-----|-----|-----|
| B1 | B2 | B3 | B4 | B5 | B6 | B7 | B8 | B9 | B10 | B11 | B12 |
| 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 |
| 5 | 6 | 7 | 8 | 7 | 8 | 5 | 6 | 8 | 5 | 6 | 7 |
| 9 | 10 | 11 | 12 | 12 | 9 | 10 | 11 | 10 | 11 | 12 | 9 |

Balanced incomplete block design (BIB)

where

$$\lambda(t - 1) = r(k - 1)$$

Balanced incomplete block design (BIB)

where

$$\lambda(t - 1) = r(k - 1)$$

✓ λ is pairs, k is plot, t is treatment, r is replication

Balanced incomplete block design (BIB)

where

$$\lambda(t - 1) = r(k - 1)$$

✓ λ is pairs, k is plot, t is treatment, r is replication

Example

| | | | |
|----|---|---|---|
| B1 | A | C | B |
| B2 | B | D | A |
| B3 | C | A | D |
| B4 | B | D | C |

Augmented Block Designs

| | |
|----------|----------|
| P_1 | T_1 |
| P_2 | T_2 |
| \vdots | \vdots |
| P_{k1} | T_c |

Block 1 = set 1 = small block 1

| | |
|----------|----------|
| P_{16} | T_1 |
| P_{17} | T_2 |
| \vdots | \vdots |
| P_{k2} | T_c |

Block 2 = set 2 = small block 2

\vdots

\vdots

| | |
|----------|----------|
| P_{41} | T_1 |
| P_{42} | T_2 |
| \vdots | \vdots |
| P_{kb} | T_c |

Block 3 = set 3 = small block 3

Augmented Block Designs

- ✓ Recommended number of controls: 3 - 4

Augmented Block Designs

✓ Recommended number of controls: 3 - 4

Example

| | | | | | | | | | |
|-----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| B1 | G2 | G3 | G1 | T2 | G7 | T1 | G6 | T3 | G4 |
| B2 | G12 | G10 | T2 | G11 | G8 | T1 | T3 | G13 | G9 |
| B3 | G18 | T3 | G16 | T1 | G14 | G19 | G17 | T2 | G15 |
| B4 | G23 | G25 | G20 | T1 | T2 | G24 | G22 | T3 | G21 |
| B5 | G27 | G26 | G31 | T2 | G28 | T3 | G30 | T1 | G29 |

Data collection tool - Drone

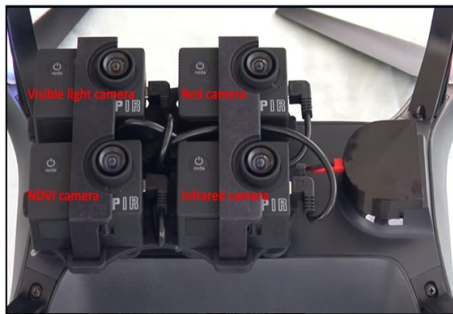


Figure: Drone and its main parts

Data collection tool - Drone

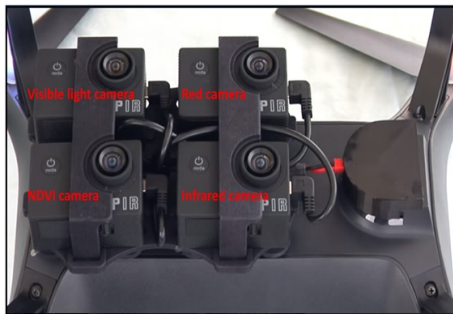
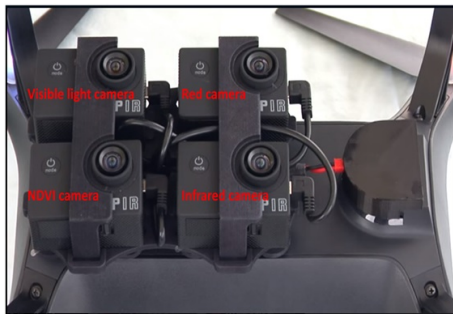


Figure: Drone and its main parts



Data collection tool - Drone



✓ Visible light camera: RGB

Figure: Drone and its main parts



Data collection tool - Drone

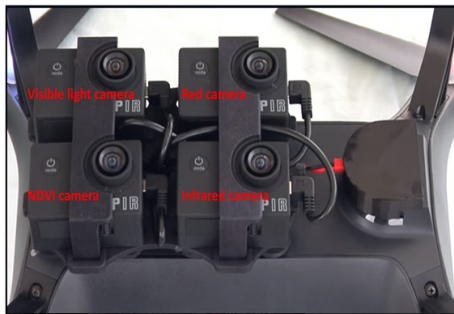


Figure: Drone and its main parts



- ✓ Visible light camera: RGB
- ✓ NDVI camera: difference between plants

Data collection tool - Drone

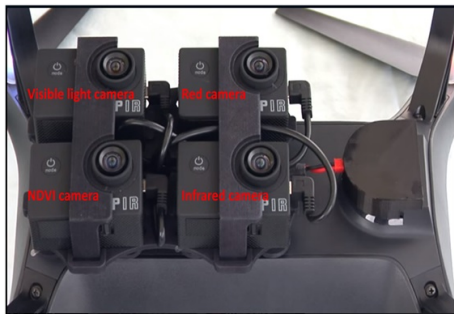


Figure: Drone and its main parts

- ✓ Visible light camera: RGB
- ✓ NDVI camera: difference between plants
- ✓ Infrared camera: adjustment of soil noise



Data collection tool - Drone

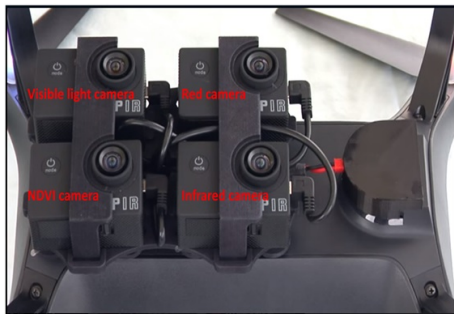


Figure: Drone and its main parts



- ✓ Visible light camera: RGB
- ✓ NDVI camera: difference between plants
- ✓ Infrared camera: adjustment of soil noise
- ✓ Red camera: infrared



Ground control points



Figure: reference point in the field



Ground control points

- ✓ Points of known coordinates in the area



Figure: reference point in the field



Ground control points

- ✓ Points of known coordinates in the area
- ✓ Helps the image assembly



Figure: reference point in the field



Ground control points



Figure: reference point in the field

- ✓ Points of known coordinates in the area
- ✓ Helps the image assembly
- ✓ Error correction (10 meters)

Ground control points



Figure: reference point in the field

- ✓ Points of known coordinates in the area
- ✓ Helps the image assembly
- ✓ Error correction (10 meters)
- ✓ 8 - 12 points

Ground control points

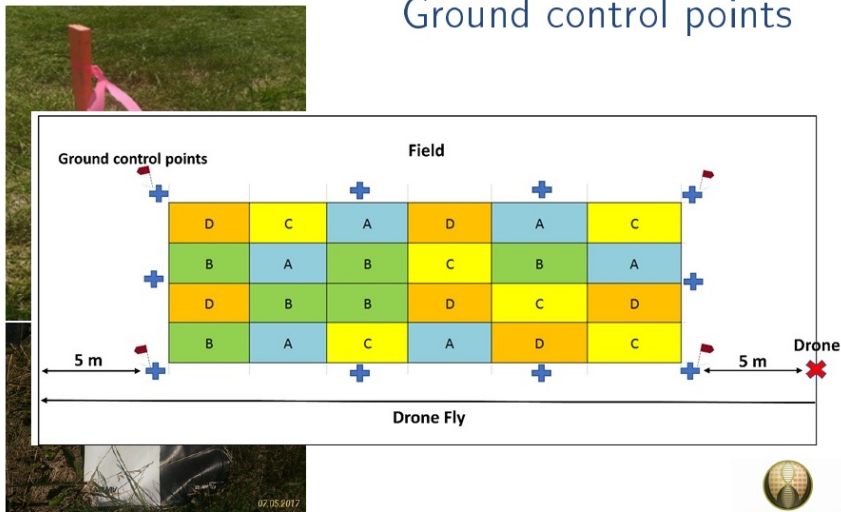


Figure: reference point in the field

Ground control points



Figure: reference point in the field

- ✓ Points of known coordinates in the area
- ✓ Helps the image assembly
- ✓ Error correction (10 meters)
- ✓ 8 - 12 points



Image sharpness





Image sharpness





Image sharpness

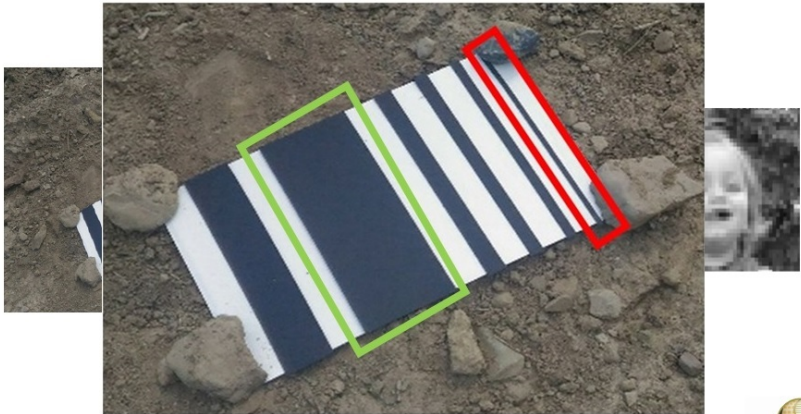
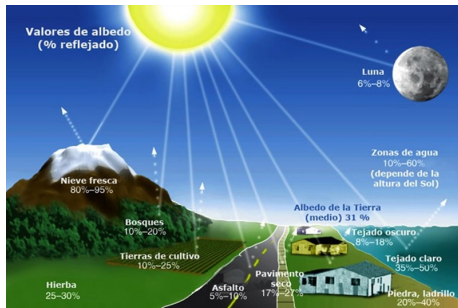




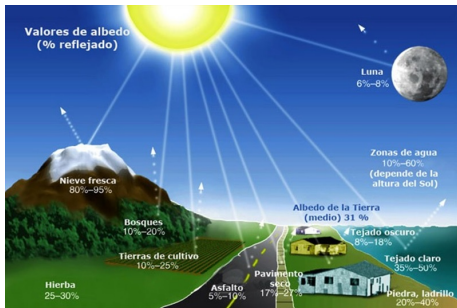
Image sharpness



Reflectance

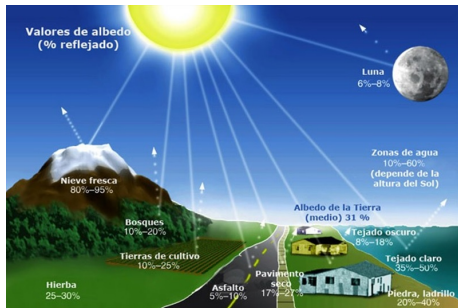


Reflectance



✓ Sun position must be 90 graus

Reflectance

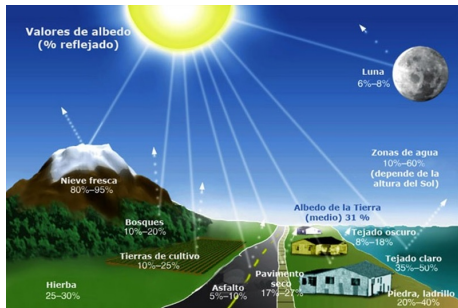


- ✓ Sun position must be 90 graus
- ✓ Albedo is the percentage of reflectance

Reflectance



Reflectance



- ✓ Sun position must be 90 graus
- ✓ Albedo is the percentage of reflectance

Weather station



Figure: Weather station

Weather station



Figure: Weather station

- ✓ Improves the acquisition of environmental variables

Weather station



Figure: Weather station

- ✓ Improves the acquisition of environmental variables
- ✓ Helpful to correct the environmental variables



Flight course start and path



→ Flight path

○ Start of the flight course

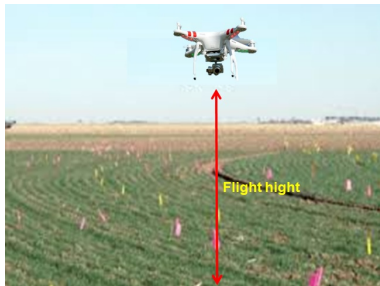


Flight height



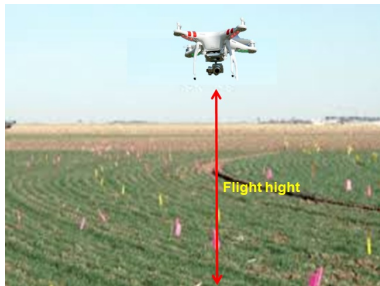
Flight hight

- ✓ Image quality and quantity are influenced by flight hight



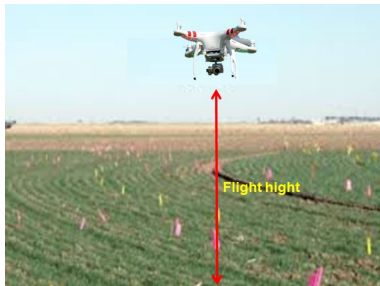
Flight hight

- ✓ Image quality and quantity are influenced by flight hight
- ✓ 10 - 12 meters: more accurate image



Flight height

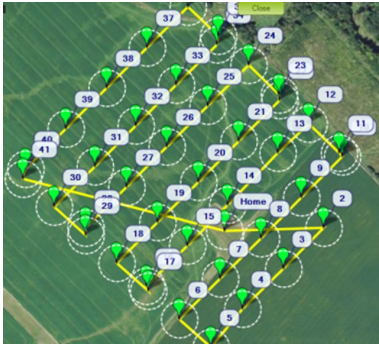
- ✓ Image quality and quantity are influenced by flight height
- ✓ 10 - 12 meters: more accurate image
- ✓ 12 - 20 meters: PLH, NDVI, CT



Factors that influence flight range

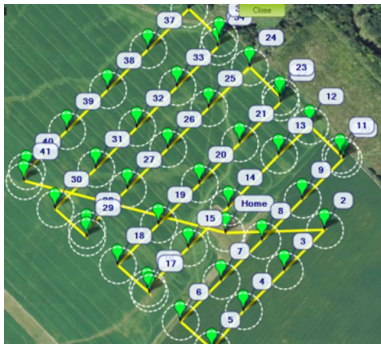


Factors that influence flight range



✓ Flight hight

Factors that influence flight range



- ✓ Flight hight
- ✓ Bateria charge (15 - 20 minutes)

Factors that influence flight range



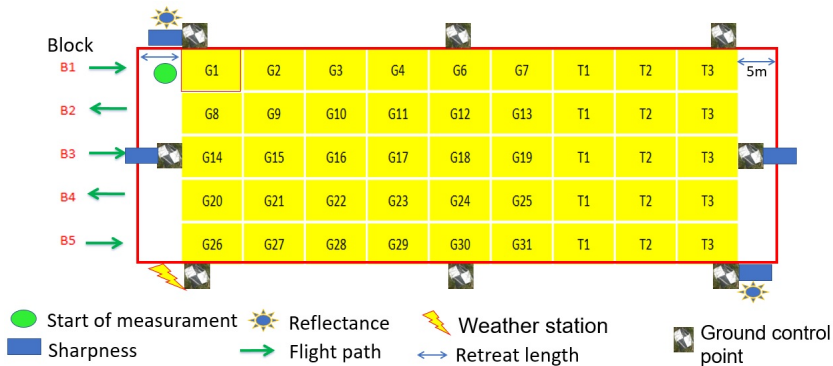
- ✓ Flight hight
- ✓ Battery charge (15 - 20 minutes)
- ✓ 70 - 75% of image overlap

Factors that influence flight range



- ✓ Flight hight
- ✓ Battery charge (15 - 20 minutes)
- ✓ 70 - 75% of image overlap
- ✓ 1 - 3 seconds per image

Augmented Blocks



Statistical Model

$$Y = \mu + \text{Block} + \text{Treat} + \text{■} + \text{☀} + \text{⚡} + \varepsilon$$

- ✓ μ : constant
- ✓ Block: effect inside the statistical model
- ✓ Treat: treatment effect ($G_i + T_i$) inside the statistical model
- ✓ ■: Sharpness covariable (gradient information)
- ✓ ☀: Reflectance covariable (environment information)
- ✓ ⚡: Weather station covariable (soil and climate information)

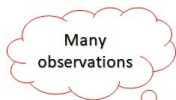
Statistical Model

Decrease
the residual

$$Y = \mu + \text{Block} + \text{Treat} + \boxed{\text{■} + \text{☀} + \text{⚡}} + \varepsilon$$

- ✓ μ : constant
- ✓ Block: effect inside the statistical model
- ✓ Treat: treatment effect ($G_i + T_i$) inside the statistical model
- ✓ ■: Sharpness covariable (gradient information)
- ✓ ☀: Reflectance covariable (environment information)
- ✓ ⚡: Weather station covariable (soil and climate information)

Statistical Model



$$\boxed{Y} = \mu + \text{Block} + \text{Treat} + \text{■} + \text{☀} + \text{⚡} + \varepsilon$$

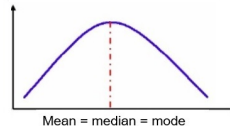
- ✓ μ : constant
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- ✓ ■: Sharpness covariable (gradient information)
- ✓ ☀: Reflectance covariable (environment information)
- ✓ ⚡: Weather station covariable (soil and climate information)

Position measures

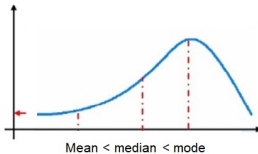
- ☐ Mean
- ☐ Median
- ☐ Mode

- Normal
- t-Student

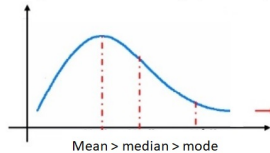
Symetric distribution



Asymmetric left-skewed distribution (or negative asymmetry)



Asymmetric right-skewed distribution (or positive asymmetry)



- Asymmetric distributions: Qui-quadrado; F-Snedecor; Weibull; Poisson; Lognormal

What happens when we have an experiment with distilliers values?

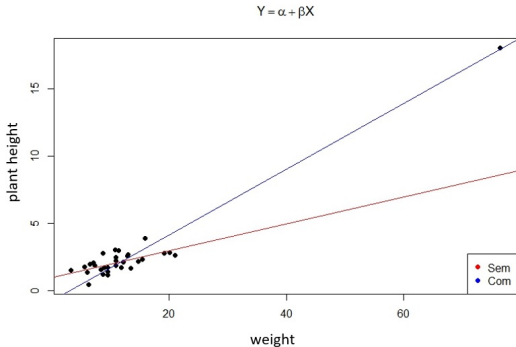


```
$media_x_sem  
[1] 10.985
```

```
$media_x_com  
[1] 13.69097
```

```
$media_y_sem  
[1] 2.066333
```

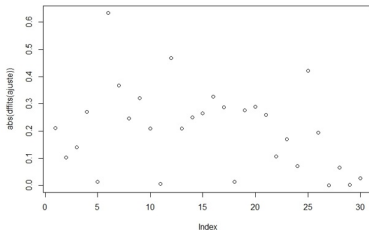
```
$media_y_com  
[1] 2.580323
```



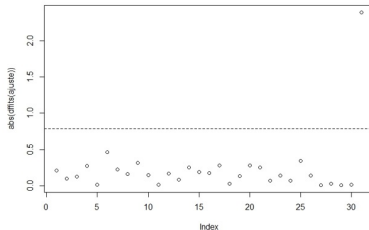
What are the outliers effects in true value?

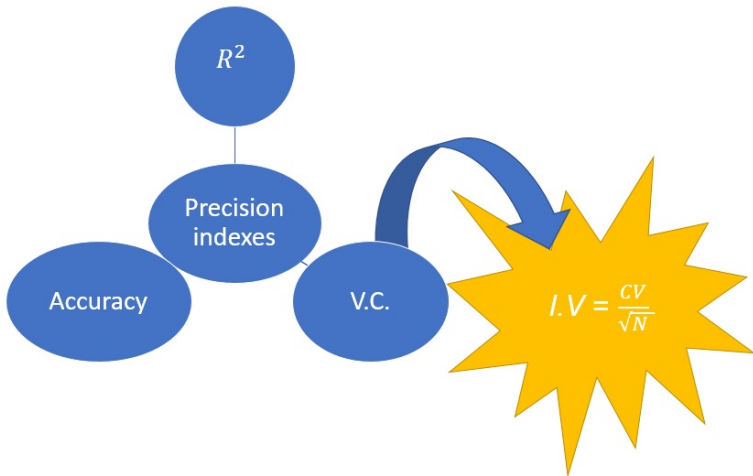
DFFits

Without outliers



With outliers







ESCOLA SUPERIOR DE AGRICULTURA "LUIZ DE QUEIROZ"

The End

THANK YOU FOR YOUR ATTENTION!