

1. *Ackley's Problem (ACK)* (Storn and Price, 1997)

$$\min_x f(x) = -20 \exp\left(-0.02 \sqrt{n^{-1} \sum_{i=1}^n x_i^2}\right) - \exp\left(n^{-1} \sum_{i=1}^n \cos(2\pi x_i)\right) + 20 + e$$

subject to  $-30 \leq x_i \leq 30$ ,  $i \in \{1, 2, \dots, n\}$ . The number of local minima is not known. The global minimum is located at the origin with  $f(x^*) = 0$ . Tests were performed for  $n = 10$ .

2. *Aluffi-Pentini's Problem (AP)* (Aluffi-Pentini et al., 1985)

$$\min_x f(x) = 0.25x_1^4 - 0.5x_1^2 + 0.1x_1 + 0.5x_2^2$$

subject to  $-10 \leq x_1, x_2 \leq 10$ . The function has two local minima, one of them is global with  $f(x^*) \approx -0.3523$  located at  $(-1.0465, 0)$ .

4. *Bohachevsky 1 Problem (BF1)* (Bohachevsky et al., 1986)

$$\min_x f(x) = x_1^2 + 2x_2^2 - 0.3 \cos(3\pi x_1) - 0.4 \cos(4\pi x_2) + 0.7$$

subject to  $-50 \leq x_1, x_2 \leq 50$ . The number of local minima is unknown but the global minimizer is located at  $x^* = (0, 0)$  with  $f(x^*) = 0$ .

5. *Bohachevsky 2 Problem (BF2)* (Bohachevsky et al., 1986)

$$\min_x f(x) = x_1^2 + 2x_2^2 - 0.3 \cos(3\pi x_1) \cos(4\pi x_2) + 0.3$$

subject to  $-50 \leq x_1, x_2 \leq 50$ . The number of local minima is unknown but the global minimizer is located at  $x^* = (0, 0)$  with  $f(x^*) = 0$ .

15. *Griewank Problem (GW)* (Griewank, 1981; Jansson and Knüppel, 1995)

$$\min_x f(x) = 1 + \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos\left(\frac{x_i}{\sqrt{i}}\right)$$

subject to  $-600 \leq x_i \leq 600$ ,  $i \in \{1, 2, \dots, n\}$ . The function has a global minimum located at  $x^* = (0, 0, \dots, 0)$  with  $f(x^*) = 0$ . Number of local minima for arbitrary  $n$  is unknown, but in the two dimensional case there are some 500 local minima. Tests were performed for  $n = 10$ .

7. *Camel Back - 3 Three Hump Problem (CB3)* (Dixon and Szegö, 1975)

$$\min_x f(x) = 2x_1^2 - 1.05x_1^4 + \frac{1}{6}x_1^6 + x_1x_2 + x_2^2$$

subject to  $-5 \leq x_1, x_2 \leq 5$ . The function has three local minima, one of them is global located at  $x^* = (0, 0)$  with  $f(x^*) = 0$ .

8. *Camel Back - 6 Six Hump Problem (CB6)* (Dixon and Szegö, 1978; Michalewicz, 1996)

$$\min_x f(x) = 4x_1^2 - 2.1x_1^4 + \frac{1}{3}x_1^6 + x_1x_2 - 4x_2^2 + 4x_2^4$$

subject to  $-5 \leq x_1, x_2 \leq 5$ . This function is symmetric about the origin and has three conjugate pairs of local minima with values  $f \approx -1.0316, -0.2154, 2.1042$ . The function has two global minima at  $x^* \approx (0.089842, -0.712656)$  and  $(-0.089842, 0.712656)$  with  $f(x^*) \approx -1.0316$ .

9. *Cosine Mixture Problem (CM)* (Breiman and Cutler, 1993)

$$\max_x f(x) = 0.1 \sum_{i=1}^n \cos(5\pi x_i) - \sum_{i=1}^n x_i^2$$

subject to  $-1 \leq x_i \leq 1, i \in \{1, 2, \dots, n\}$ . The global maxima are located at the origin with the function values 0.20 and 0.40 for  $n = 2$  and  $n = 4$ , respectively.

48. *Sinusoidal Problem (SIN)* (Zabinsky et al., 1992)

$$\min_x f(x) = - \left[ A \prod_{i=1}^n \sin(x_i - z) + \prod_{i=1}^n \sin(B(x_i - z)) \right]$$

subject to  $0 \leq x_i \leq 180, i \in \{1, 2, \dots, n\}$ . The variable  $x$  is in degrees. Parameter  $A$  affects the amplitude of the global optimum;  $B$  affects the periodicity and hence the number of local minima;  $z$  shifts the location of the global minimum; and  $n$  indicates the dimension. Our tests were performed with  $A = 2.5, B = 5, z = 30$ , and  $n = 10$ , and 20. The location of the global solution is at  $x^* = (90 + z, 90 + z, \dots, 90 + z)$  with the global optimum value of  $f(x^*) = -(A + 1)$ . The number of local minima increases dramatically in dimension, and when  $B = 5$  the number of local minima is equal to:

$$\sum_{i=0}^{\lfloor n/2 \rfloor} \left( \frac{n!}{(n-2i)!(2i)!} 3^{n-2i} 2^{2i} \right).$$