

AB		CD		$\bar{C}$		C	
		00	01	11	10	00	01
A	00					00	$\leftrightarrow \bar{B}$
	01					01	$\leftrightarrow B$
	11					11	$\leftrightarrow \bar{D}$
	10					10	$\leftrightarrow \bar{B}$
		00	01	11	10	$\uparrow \bar{D}$	

Figura 3.76

### 3.10 Exercícios Propostos

3.10.1 - Simplifique cada expressão, utilizando a Álgebra de Boole.

a)  $S = ABC\bar{C} + \bar{A}\bar{B}C + ABC + \bar{A}\bar{B}C + \bar{A}BC\bar{C}$

b)  $S = ABCD + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}CD + \bar{A}BC\bar{D} + ABC\bar{D} + A\bar{B}CD + ABCD$

3.10.2 - Simplifique utilizando a Álgebra de Boole:

$$S = [(\overline{\overline{B}} + \overline{\overline{C}} + \overline{\overline{D}})(\overline{\overline{A}} + B + C) + C] + \overline{A}\overline{B}C + \overline{B}(\overline{A} + \overline{C})$$

3.10.3 - Idem, para a expressão:

$$S = A[\overline{\overline{B}}(\overline{\overline{C}} + \overline{\overline{D}}) + \overline{\overline{A}}(\overline{\overline{B}} + \overline{\overline{C}})] + \overline{C}\overline{D} + A\overline{B}C + AB$$

3.10.4 - Idem, para a expressão:

$$S = (\overline{\overline{A}} \oplus B + \overline{\overline{B}}\overline{\overline{C}}\overline{\overline{D}})[\overline{\overline{D}} + \overline{\overline{B}}C + D(\overline{\overline{A}} + B)] + \overline{A}\overline{D}$$

3.10.5 - Idem, para a expressão:

$$S = [(\overline{\overline{B}} + \overline{\overline{C}} + \overline{\overline{D}} + \overline{\overline{A}}\overline{\overline{C}})(A + \overline{\overline{B}} + \overline{\overline{C}}) + \overline{\overline{B}}(\overline{\overline{C}} + \overline{\overline{A}}\overline{\overline{B}} + \overline{\overline{A}}\overline{\overline{C}})](A + B)$$

3.10.6 - Desenhe o circuito que executa a expressão, simplificado.

$$S = (\overline{\overline{B}} + \overline{\overline{D}})\{\overline{\overline{B}} + C \odot D + \overline{\overline{A}}[\overline{\overline{B}}\overline{\overline{C}} + \overline{\overline{B}}C + A + B(\overline{\overline{C}} + \overline{\overline{D}})]\}$$

**3.10.7** - Simplifique através da Álgebra de Boole:

$$S = \overline{(AB + CD + AD)} \{ \overline{B} [C \oplus D + A(\overline{B} + \overline{C}) + A\overline{BC}] + \overline{A} \}$$

**3.10.8** - Demonstre que:

$$A \odot (B \oplus C) = A \oplus (B \odot C)$$

**3.10.9** - Através dos diagramas de Veitch-Karnaugh, determine a expressão simplificada de  $S_1$  e  $S_2$  da tabela 3.26.

A B	S <sub>1</sub>	S <sub>2</sub>
0 0	1	1
0 1	0	1
1 0	1	0
1 1	1	0

Tabela 3.26

**3.10.10** - Simplifique as expressões de  $S_1$ ,  $S_2$ ,  $S_3$  e  $S_4$  da tabela 3.27, utilizando os mapas de Veitch-Karnaugh.

A	B	C	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
0	0	0	1	1	0	0
0	0	1	0	1	1	1
0	1	0	1	1	0	1
0	1	1	1	0	0	0
1	0	0	1	1	1	1
1	0	1	1	1	1	0
1	1	0	0	1	1	1
1	1	1	1	0	0	1

Tabela 3.27

**3.10.11** - Idem ao anterior, para a tabela 3.28.

A	B	C	D	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
0	0	0	0	1	1	0	0
0	0	0	1	1	0	0	0
0	0	1	0	1	1	1	0
0	0	1	1	1	0	0	1
0	1	0	0	1	1	1	1
0	1	0	1	0	1	1	1
0	1	1	0	0	1	1	0
0	1	1	1	1	1	0	1
1	0	0	0	1	1	0	0
1	0	0	1	1	1	0	1
1	0	1	0	1	0	1	0
1	0	1	1	1	0	0	0
1	1	0	0	1	0	0	0
1	1	0	1	0	1	1	1
1	1	1	0	0	0	0	1
1	1	1	1	1	1	0	1

Tabela 3.28

**3.10.12**- Simplifique as expressões utilizando diagramas de Veitch-Karnaugh:

- a)  $S = A\bar{B}\bar{C} + A\bar{B}C + \bar{A}BC + \bar{A}B\bar{C} + ABC$
- b)  $S = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}CD + \bar{A}\bar{B}\bar{C}\bar{D} + AB\bar{C}D + \bar{A}BCD + A\bar{B}\bar{C}D$   
 $ABCD + A\bar{B}\bar{C}D$
- c)  $S = \bar{B}\bar{D} + \bar{A} + A\bar{B}\bar{C}D + A\bar{B}CD + \bar{A}\bar{C}$
- d)  $S = ABC + AB + \bar{A}BCD + BD + CD + \bar{B}CD + \bar{A}BC\bar{D}$

**3.10.13** - Determine as expressões simplificadas para  $S_1$  e  $S_2$  da tabela 3.29.

A	B	C	D	E	$S_1$	$S_2$
0	0	0	0	0	1	1
0	0	0	0	1	1	0
0	0	0	1	0	1	1
0	0	0	1	1	1	0
0	0	1	0	0	0	1
0	0	1	0	1	1	1
0	0	1	1	0	0	1
0	0	1	1	1	1	1
0	1	0	0	0	0	1
0	1	0	0	1	0	0
0	1	0	1	0	1	1
0	1	0	1	1	0	0
0	1	1	0	0	1	1
0	1	1	0	1	1	1
0	1	1	1	0	0	1
1	0	0	0	0	1	1
1	0	0	0	1	1	0
1	0	0	1	0	0	1
1	0	0	1	1	0	1
1	0	1	0	0	0	1
1	0	1	1	0	0	1
1	0	1	1	1	1	1
1	1	0	0	0	0	1

Tabela 3.29 (parte)

A	B	C	D	E	S <sub>1</sub>	S <sub>2</sub>
1	1	0	0	1	0	0
1	1	0	1	0	1	1
1	1	0	1	1	0	0
1	1	1	0	0	0	1
1	1	1	0	1	1	1
1	1	1	1	0	0	1
1	1	1	1	1	1	1

Tabela 3.29

**3.10.14** - Simplifique as expressões de S<sub>1</sub> e S<sub>2</sub> da tabela 3.30.

A	B	C	S <sub>1</sub>	S <sub>2</sub>
0	0	0	X	1
0	0	1	0	X
0	1	0	1	0
0	1	1	X	0
1	0	0	1	0
1	0	1	X	1
1	1	0	X	X
1	1	1	1	X

Tabela 3.30

**3.10.15** - Determine as expressões simplificadas de  $S_1$ ,  $S_2$ ,  $S_3$  e  $S_4$  da tabela 3.31.

A	B	C	D	$S_1$	$S_2$	$S_3$	$S_4$
0	0	0	0	1	X	0	X
0	0	0	1	X	X	0	0
0	0	1	0	X	1	0	X
0	0	1	1	X	0	1	1
0	1	0	0	1	X	X	1
0	1	0	1	0	1	X	X
0	1	1	0	X	0	1	0
0	1	1	1	X	1	0	1
1	0	0	0	X	1	X	0
1	0	0	1	1	0	1	1
1	0	1	0	X	X	0	0
1	0	1	1	1	1	0	X
1	1	0	0	X	0	1	1
1	1	0	1	X	1	0	1
1	1	1	0	1	1	X	1
1	1	1	1	0	X	1	X

Tabela 3.31

**3.10.16** - Desenhe os circuitos minimizados que executam as saídas  $S_1$  e  $S_2$  da tabela da verdade:

A	B	C	D	E	$S_1$	$S_2$
0	0	0	0	0	0	1
0	0	0	0	1	0	X
0	0	0	1	0	1	1
0	0	0	1	1	0	X
0	0	1	0	0	1	X
0	0	1	0	1	1	1
0	0	1	1	0	0	X
0	0	1	1	1	1	1
0	1	0	0	0	0	1
0	1	0	0	1	1	0
0	1	0	1	0	1	1
0	1	0	1	1	0	0
0	1	1	0	0	1	X
0	1	1	0	1	1	1
1	0	0	0	0	0	1
1	0	0	0	1	0	X
1	0	0	1	0	1	1
1	0	0	1	1	0	0
1	0	1	0	0	1	X
1	0	1	0	1	1	1
1	0	1	1	0	0	0
1	0	1	1	1	1	1
1	1	0	0	0	0	X
1	1	0	0	1	0	1
1	1	0	1	0	1	1
1	1	1	0	0	1	1
1	1	1	0	1	1	X
1	1	1	1	0	0	1
1	1	1	1	1	1	X

Tabela 3.32

**3.10.17** - Obtenha a expressão simplificada:

$$S = \overline{(\bar{A} + B)} \overline{\bar{B}} + (B \oplus C) [\overline{ABC} + B(\overline{A + \bar{D}}) + \overline{BC} + \overline{BD}] + ABD$$

**3.10.18** - Prove que:

$$\overline{A \oplus B \oplus C \oplus D} = A \odot B \odot C \odot D$$