

# Eletrorromagnetismo

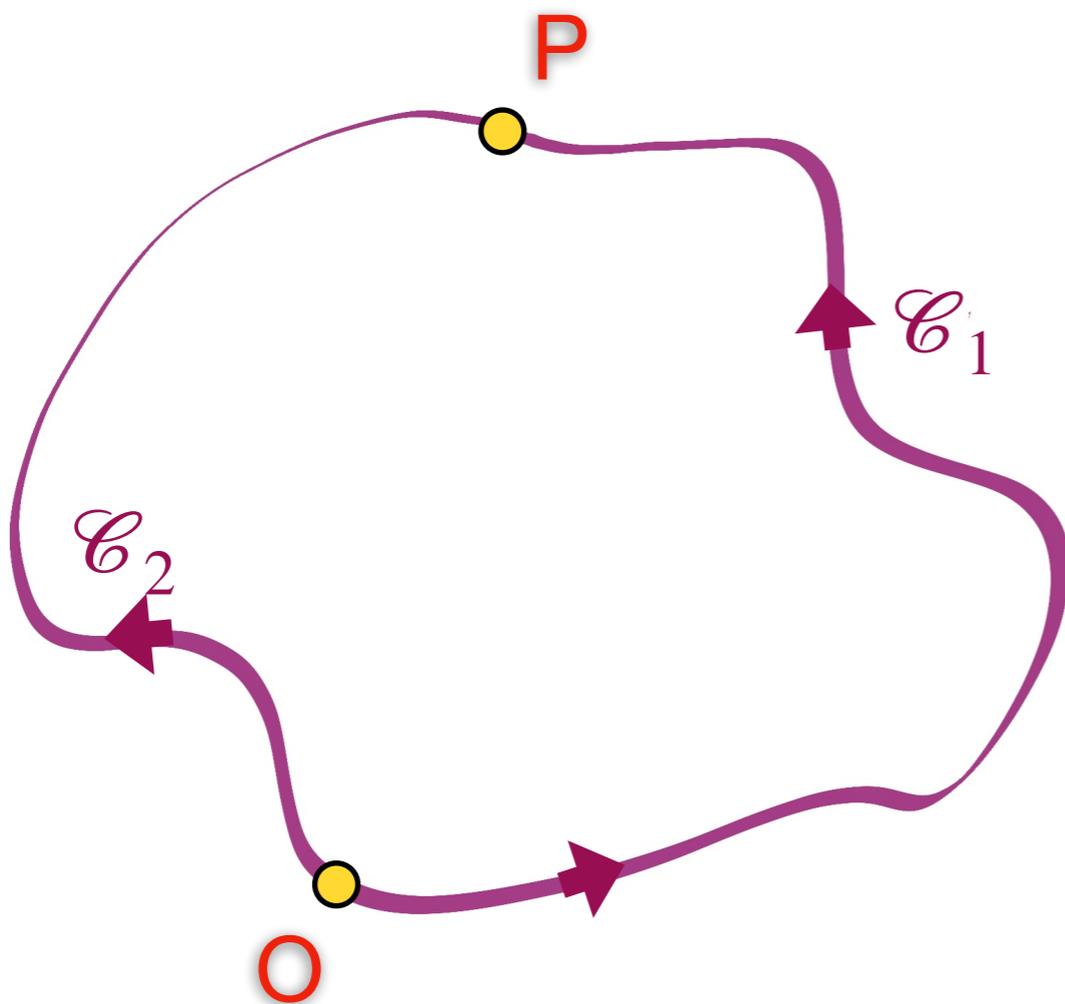
9 de abril  
Eletrostática

# Potencial eletrostático

$$\vec{\nabla} \times \vec{E} = 0$$

$$\int_{\mathcal{C}_1}^P \vec{E} \cdot d\vec{\ell} = \int_{\mathcal{C}_2}^P \vec{E} \cdot d\vec{\ell}$$

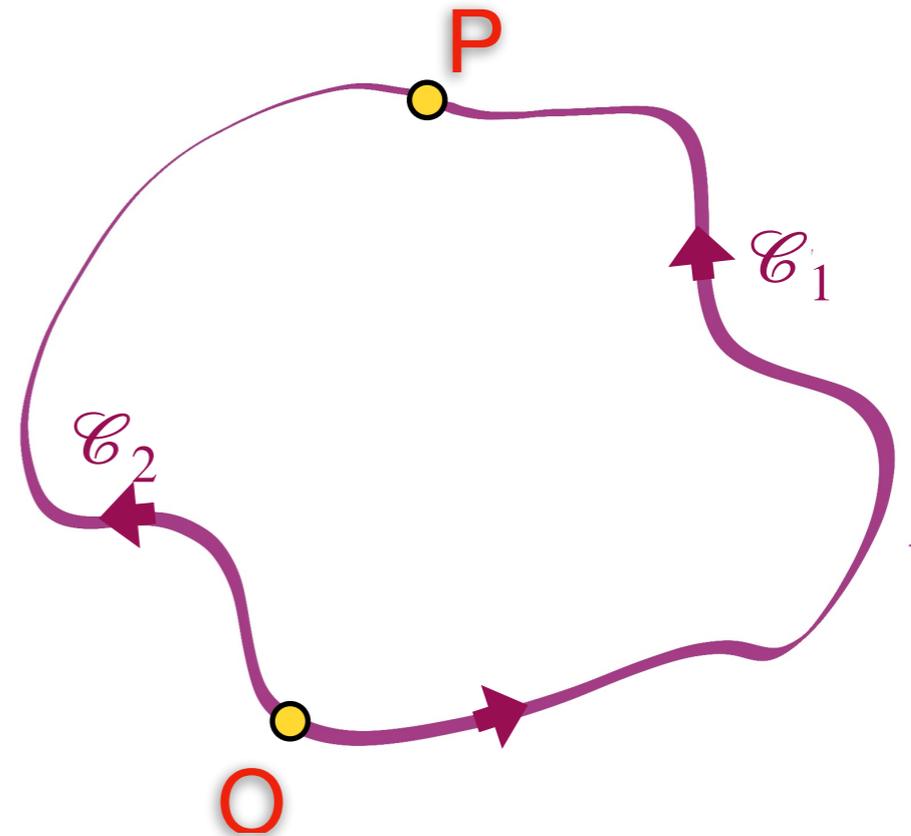
$$V(P) = - \int_O^P \vec{E} \cdot d\vec{\ell}$$



# Potencial eletrostático

$$V(P) = - \int_O^P \vec{\mathbf{E}} \cdot d\vec{\ell}$$

$$V(P) - V(O) = \int_O^P \vec{\nabla} V \cdot d\vec{\ell}$$

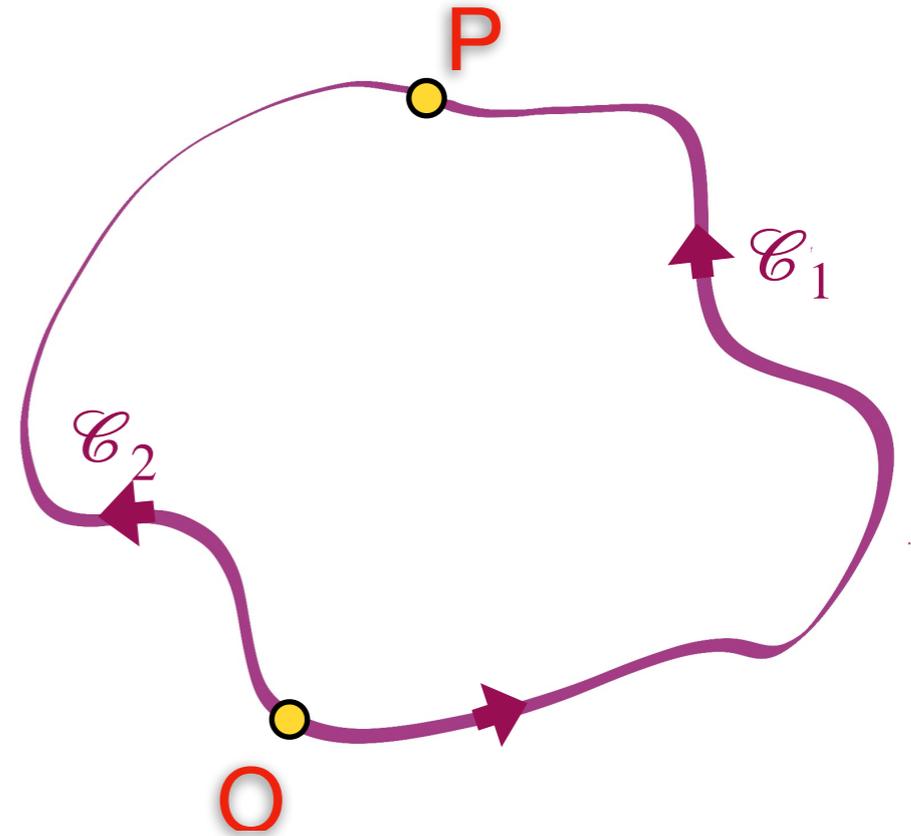


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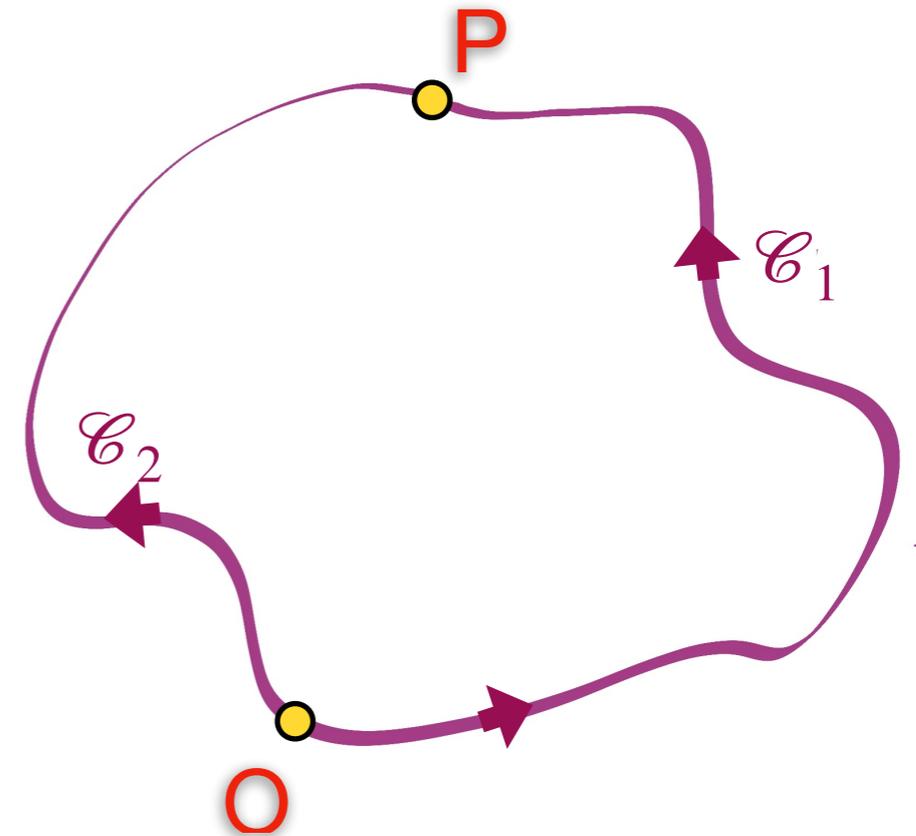
$$\vec{\mathbf{E}} = - \vec{\nabla} V$$



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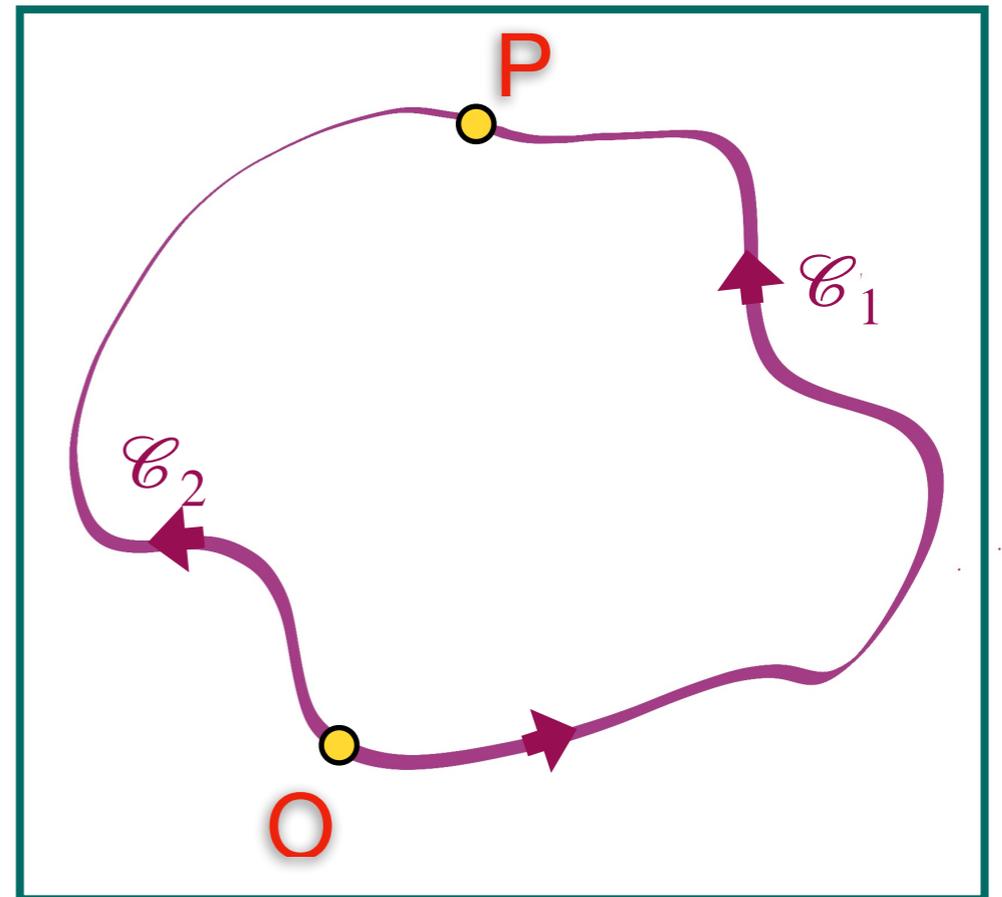


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Escolha do ponto  $O$



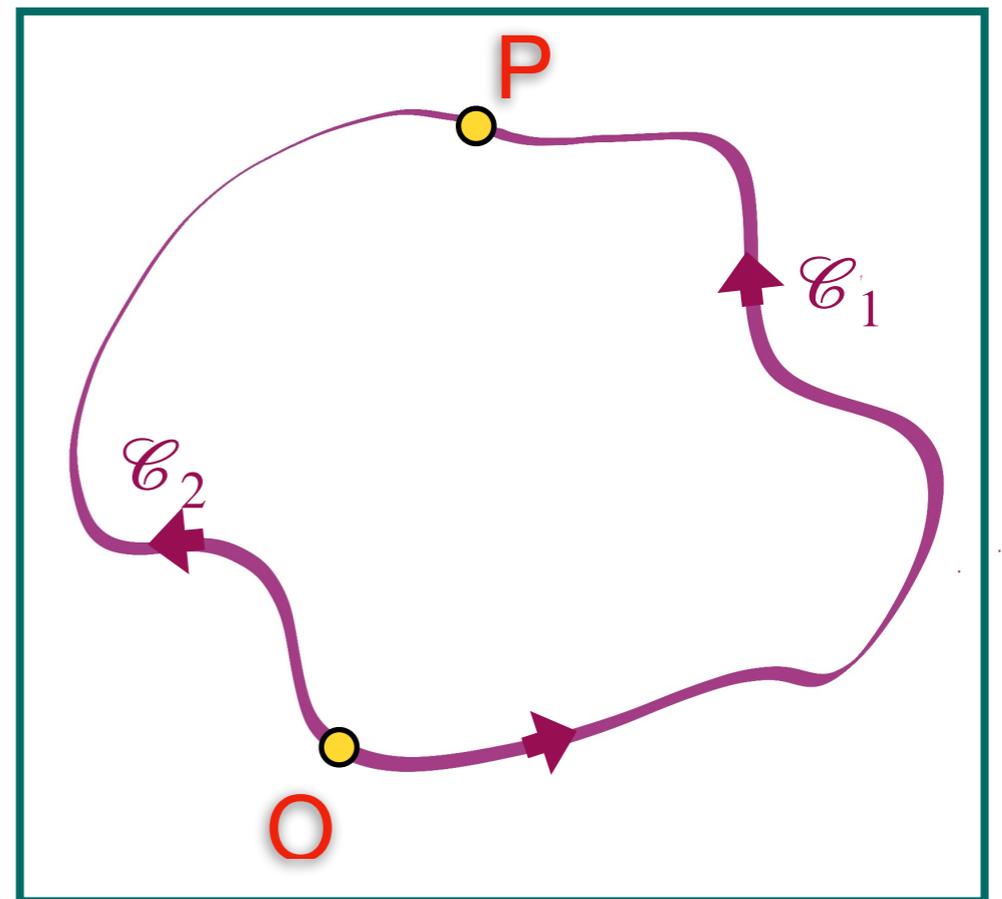
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• Via de regra,  $O \equiv \infty$



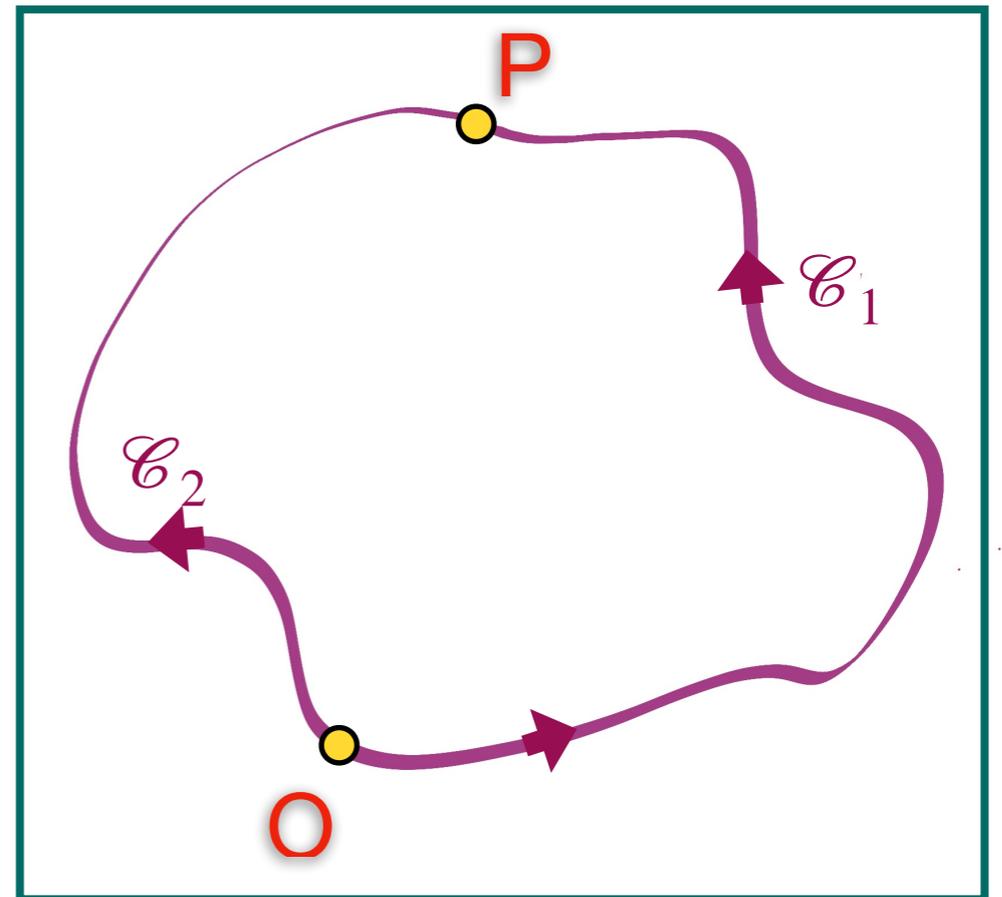
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Escolha do ponto  $O$

- Via de regra,  $O \equiv \infty$
- Exceção
  - Cargas que vão até  $\infty \Rightarrow$  escolher  $O$  conveniente

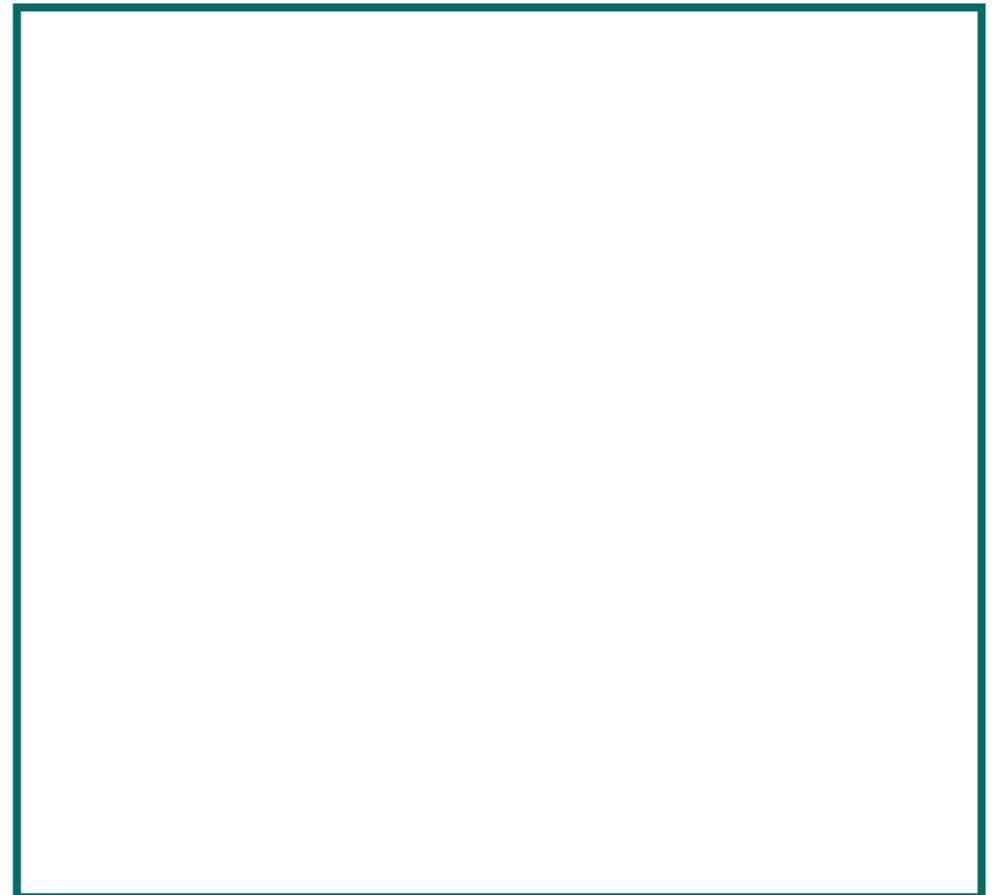


# Potencial de carga pontual

$$V(P) = - \int_O^P \vec{E} \cdot d\vec{\ell}$$

Escolha do ponto  $O$

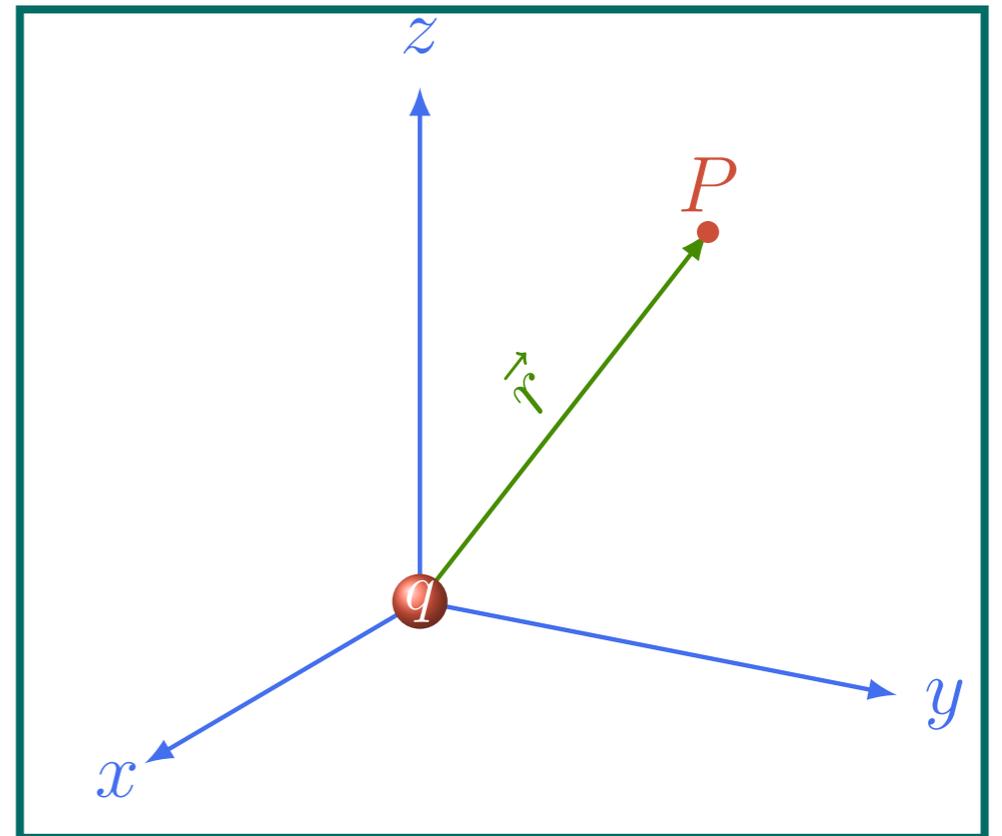
- Via de regra,  $O \equiv \infty$
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# Potencial de carga pontual

$$V(P) = - \int_O^P \vec{\mathbf{E}} \cdot d\vec{\ell}$$

$$O \rightarrow \infty$$

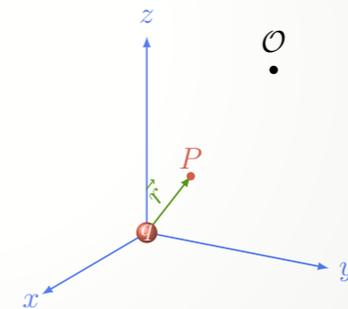


# Potencial de carga pontual

$$V(P) = - \int_O^P \vec{\mathbf{E}} \cdot d\vec{\ell}$$

$$\mathcal{O} \rightarrow \infty$$

$$V(\vec{\mathbf{r}}) = - \int_{\infty}^r \frac{1}{4\pi\epsilon_0} \frac{q}{r^3} \vec{\mathbf{r}} \cdot \hat{\mathbf{r}} dr$$



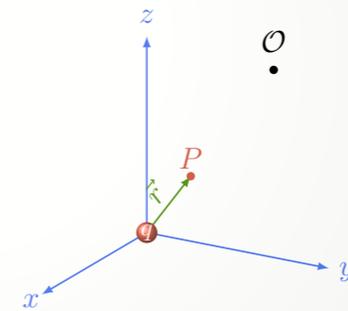
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# Potencial de carga pontual

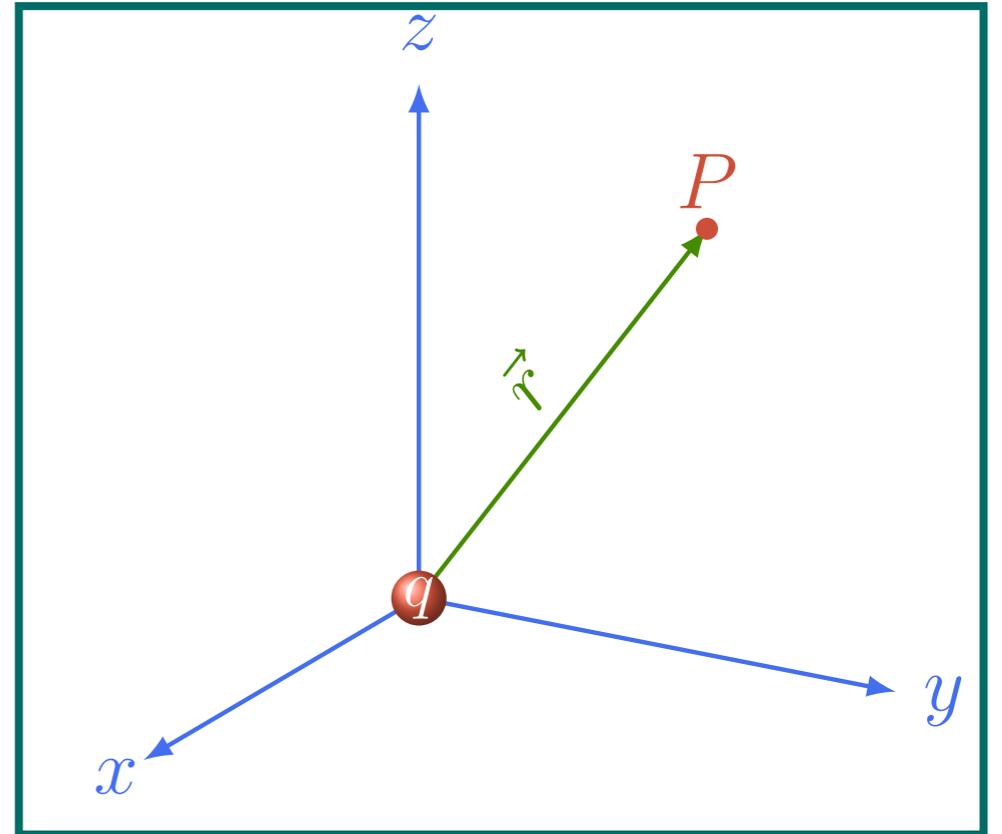
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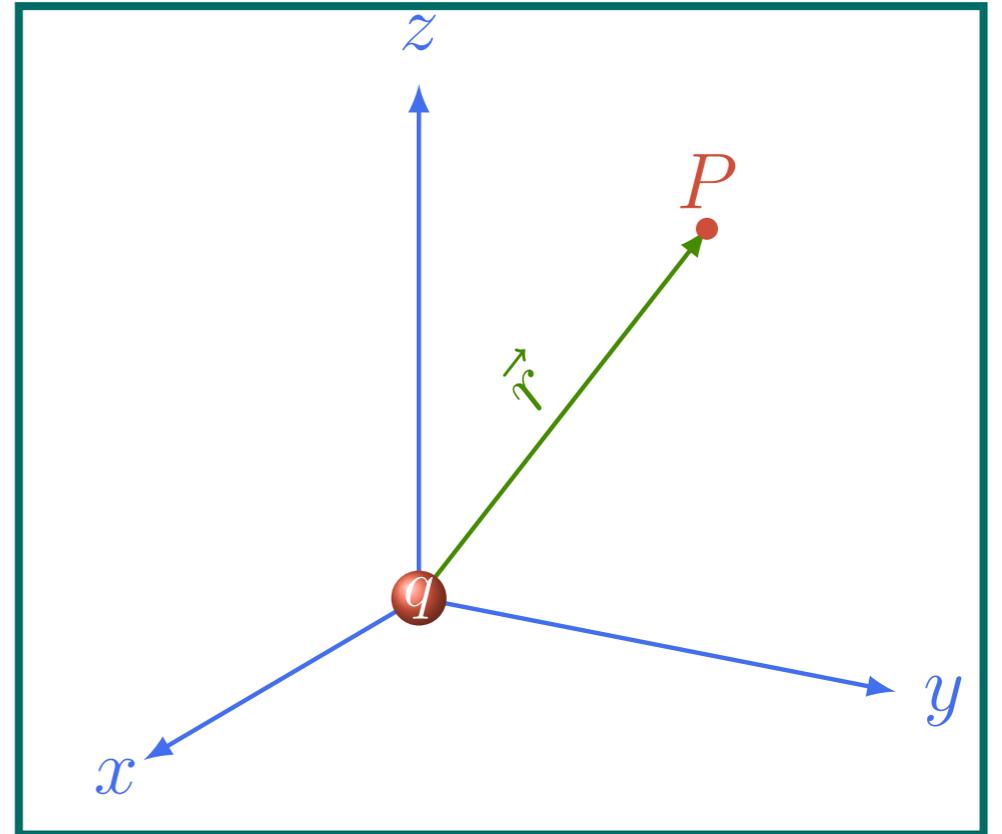
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# Potencial de carga pontual

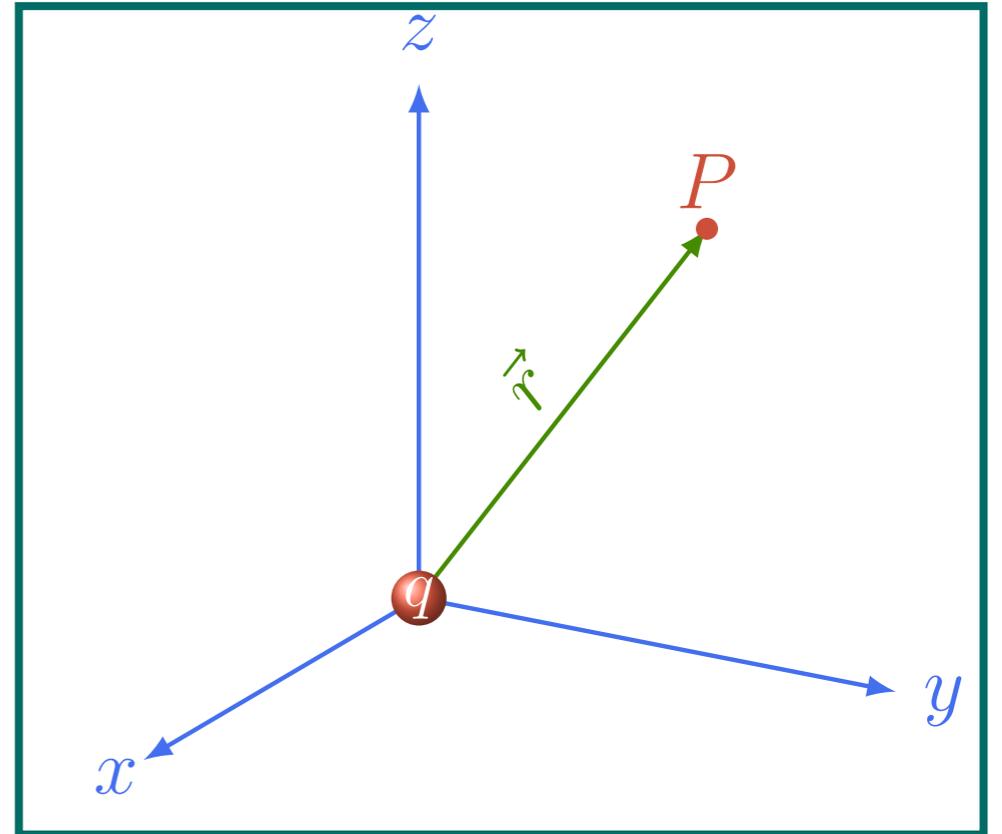
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$



# Potencial de carga pontual

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

$$\vec{E} = -\vec{\nabla}V$$

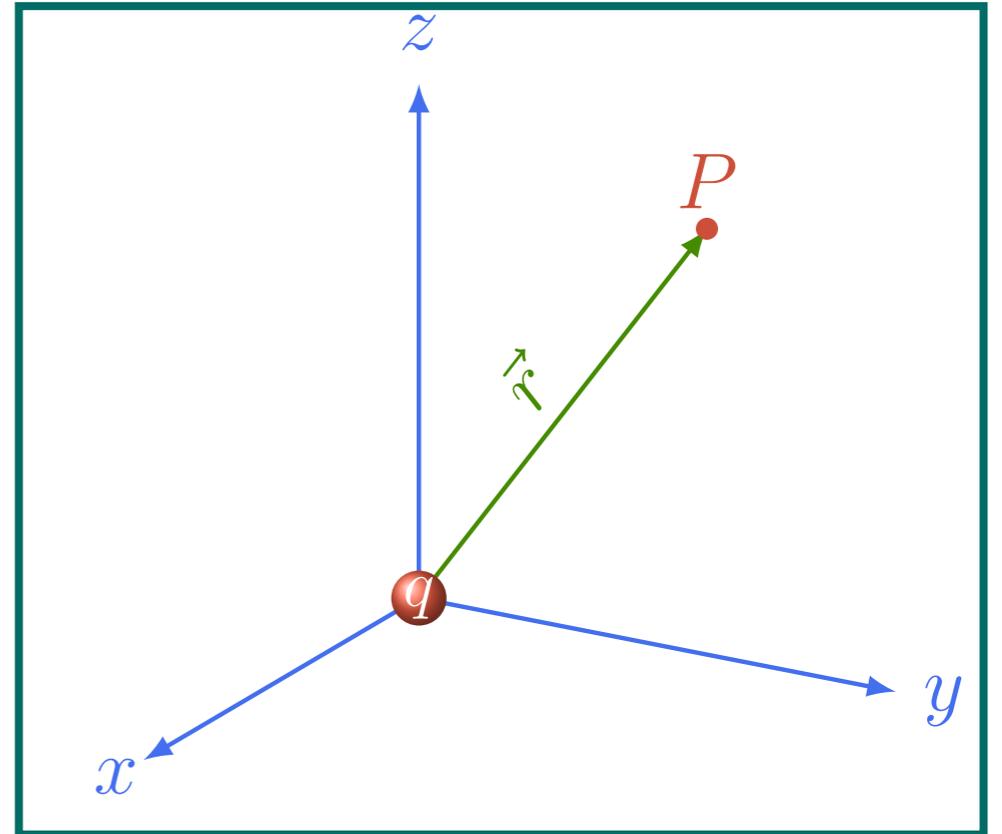


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$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

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$$\vec{E}(\vec{r}) = -\frac{\partial V}{\partial r} \hat{r}$$



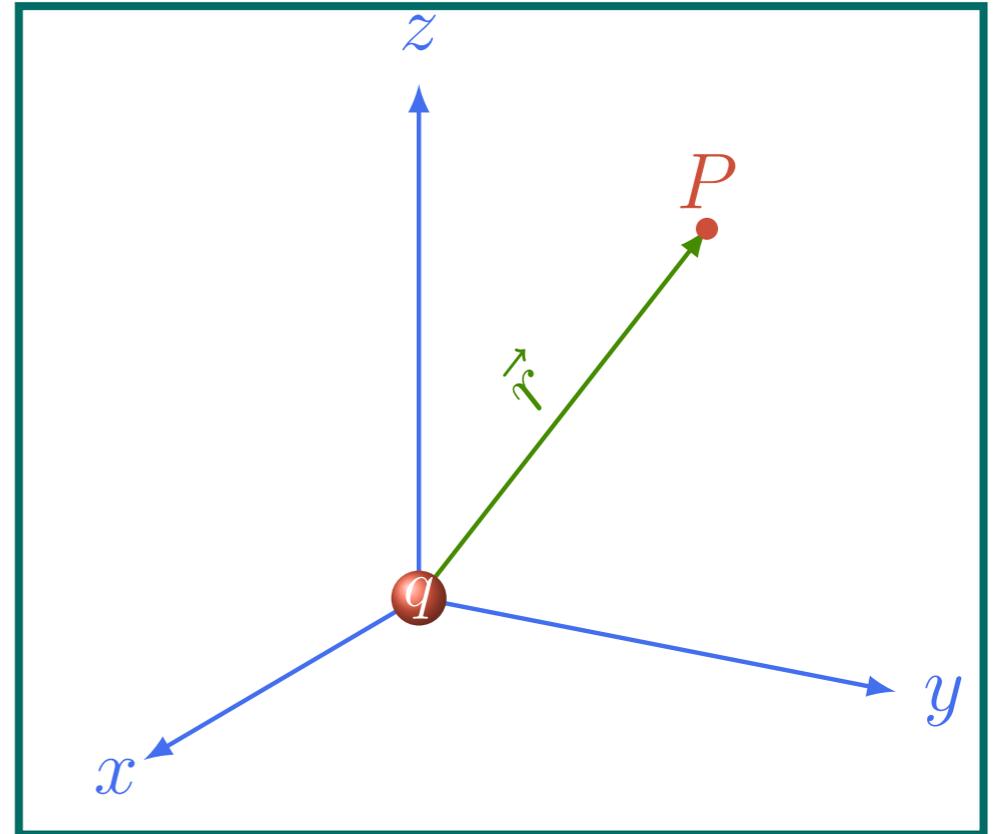
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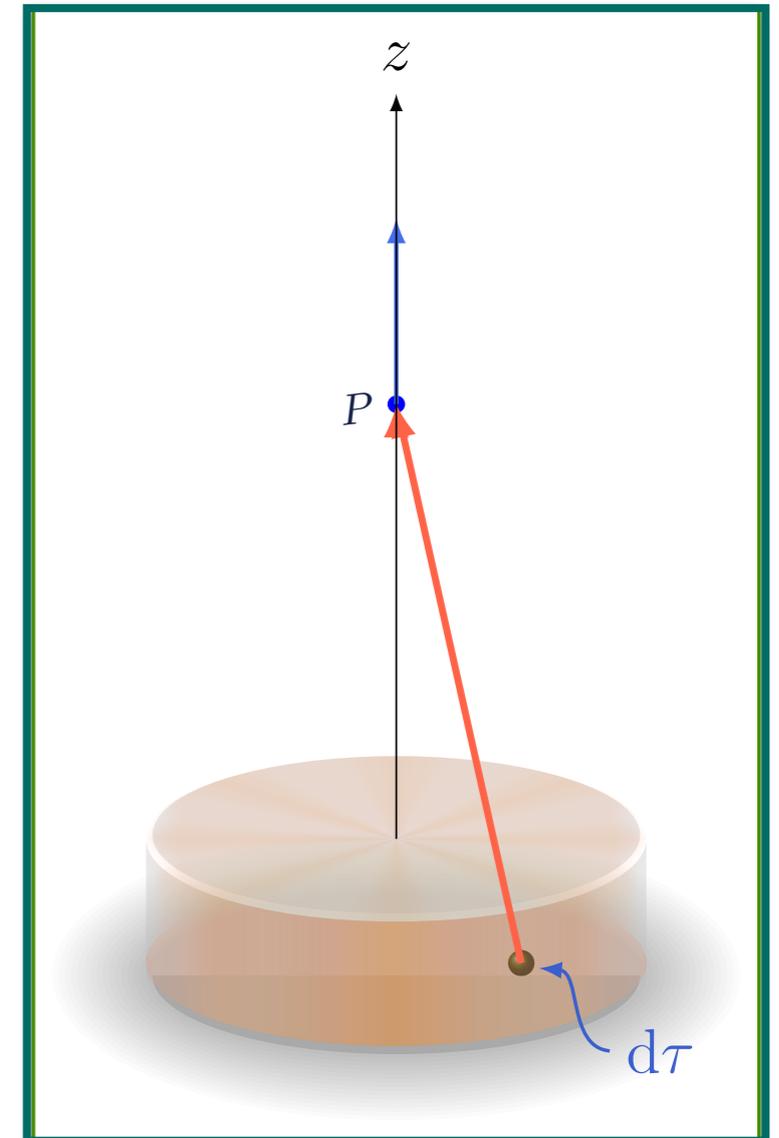
# Potencial de distribuição de cargas

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

$$\Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_V \frac{1}{r} dq$$

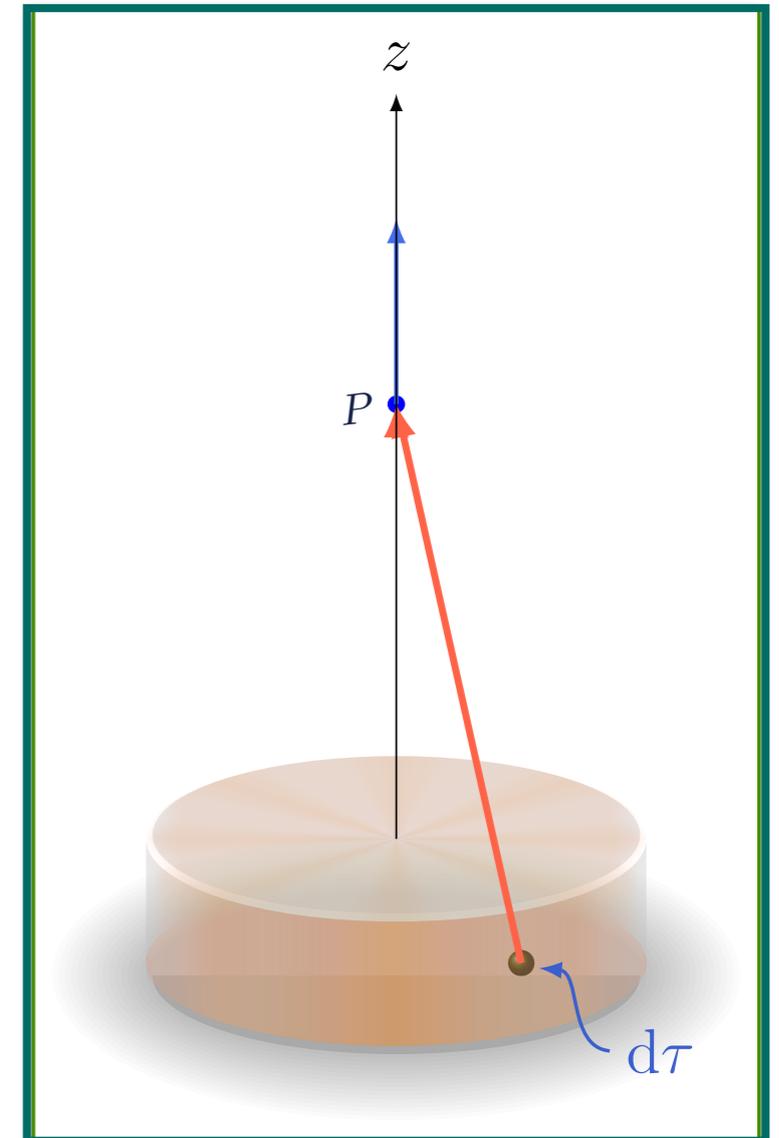
$$\Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho(\vec{r}')}{r} d\tau'$$

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Pratique o que aprendeu

$$V(\vec{r}) = ?$$

