

## Non-idealities in operational amplifiers

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## Summary of non-ideal OpAmps

- (1) Small signal errors
  - (a) Differential and common-mode gains
  - (b) Input and output resistances
- (2) Frequency limitation
  - (a) Finite bandwidth
  - (b) Product gain×frequency
- (3) Large signal limitation
  - (a) Slew-rate
  - (b) Voltage distortion due to saturation
- (4) DC imperfections
  - (a) Input offset voltage
  - (b) Input bias and offset currents

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## Ideal OpAmps

- (1) Useful for circuit behavior analysis



- (2) Because these **golden** rules applies:

- (a) Inexistence of input currents

$$\begin{cases} I_p = 0 \text{ A} \\ I_n = 0 \text{ A} \end{cases}$$

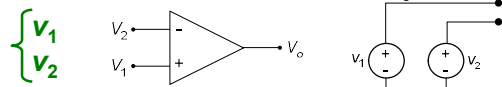
- (b) Equal voltages in the both inputs

$$\begin{cases} v_p = v_n \\ v_d = v_p - v_n = 0 \text{ V} \end{cases}$$

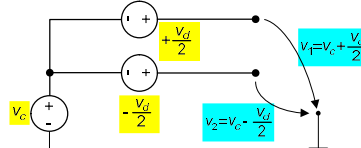
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## Differential and common-mode gains

- (1) Excitations of a differential amplifier:



- (2) The later excitations can be replaced by:



- (3) Where:  $v_d = v_1 - v_2$

$$v_c = \frac{1}{2} (v_1 + v_2)$$

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## Non-ideal OpAmps

- (1) Ideal behavior useful in initial design steps

- (2) Non-idealities must be considered on specific cases:

- (a) Signals with very low amplitudes
- (b) High-frequency signals

- (3) The general method combines:

- (a) An ideal OpAmp with
- (b) An electric model of the non-ideality

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## Differential and common-mode gains

- (1) The output of such an amplifier is:

$$v_o = A \cdot v_d + A_c \cdot v_c$$

- (2) In an ideal OpAmp we have:

$$A = \infty \text{ and } A_c = 0$$

- (3) The *Common-Mode Reject Ratio* (CMRR) is:

$$\text{CMRR} = A/A_c$$

- (4) Typical CMRR @ low frequencies :

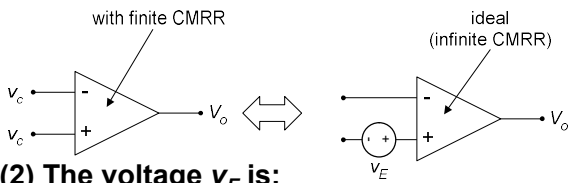
$$\text{CMRR} = 80\text{-}100 \text{ dB } (10^4\text{-}10^5)$$

PARAMETER	TEST CONDITIONS	TA†	µA741C			µA741L, µA741M			UNIT
			MIN	TYP	MAX	MIN	TYP	MAX	
CMRR	Common-mode rejection ratio	V <sub>IC</sub> = V <sub>ICmin</sub>	25°C	F0	90	-	70	90	dB
			Full range	70	-	-	70	-	

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## Differential and common-mode gains

(1) A OpAmp with finite CMRR is equivalent to:



(2) The voltage  $v_E$  is:

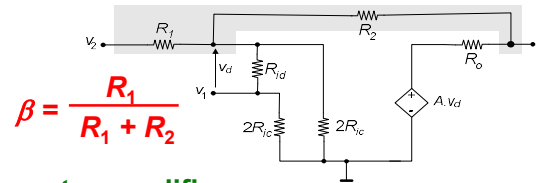
$$v_E = \frac{A_c \cdot v_c}{A} = \frac{v_c}{\text{CMRR}}$$

(3) This effect is important for:

$v_d$  signals with very small amplitudes associated to  $v_c$  signals with high amplitudes

## Input resistance

Input resistances of inv & non-inv amplifiers



$$\beta = \frac{R_1}{R_1 + R_2}$$

(a) Inverter amplifier

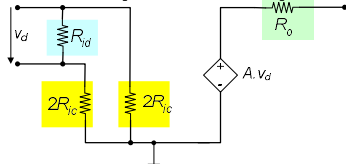
$v_1 = 0 \text{ V}$  and  $v_2 \neq 0 \rightarrow R_{if} \approx R_1$

(b) Non-inverter amplifier

$v_1 \neq 0 \text{ V}$  and  $v_2 = 0 \rightarrow R_{if} \approx 2R_{ic} \parallel (1+A\beta) \cdot R_{id}$   
 $A\beta \gg 1 \rightarrow R_{if} \gg R_{id}$  **IMPROVEMENT!**

## Input and output resistances

(1) OA model with input and output resistances



(2) The resistances are such that

$$R_{ic} \gg R_{id} \gg R_o$$

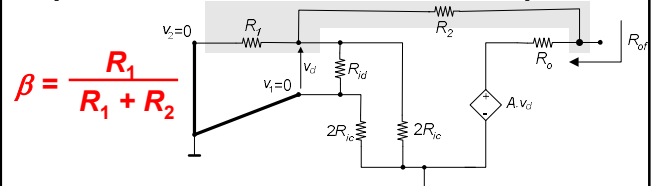
(3) Typical values for  $R_{ic}$ ,  $R_{id}$  and  $R_o$  can be:

100 M $\Omega$ , 1 M $\Omega$  and 100  $\Omega$  (respectively)

(4) It exists OAs with even higher  $R_{ic}$  and  $R_{id}$

## Output resistances

Output resistance of inv & non-inv amplifiers



$$\beta = \frac{R_1}{R_1 + R_2}$$

(a) It is possible to demonstrate

$$R_{of} \approx \frac{R_o}{1 + A\beta}$$

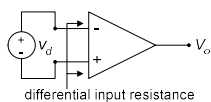
(b)  $R_o$  is low, therefore with feedback ( $A\beta \gg 1$ )

$R_{of}$  is even more lower **IMPROVEMENT!**

## Input resistances

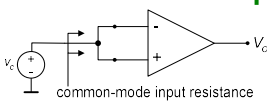
Types of input resistances:

(a) Differential input resistance



$\approx R_{id}$  because  $R_{ic} \gg R_{id}$

(b) Common-mode input resistance



$= R_{ic}$  because is  $2R_{ic} \parallel 2R_{ic}$

## Input offset voltage

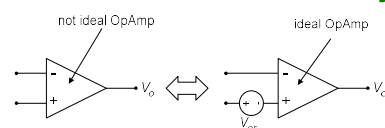
In an ideal OpAmp:

If  $v_d = 0 \text{ V} \rightarrow v_o = 0 \text{ V}$

Due to internal asymmetries in the OpAmp:

(a)  $v_o \neq 0 \text{ V}$  when  $v_d = 0 \text{ V}$

(b) This effect can be modeled by:



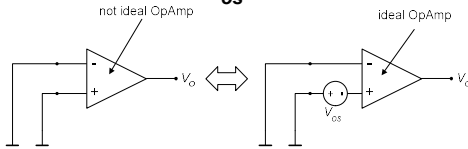
$v_{os}$  is the input offset voltage

## Input offset voltage

$V_{os}$ : random variable & asymmetry dependent

In the most common OAs:  $|v_{os}|_{max} = 1-5 \text{ mV}$

Without feedback:  $V_{os}$  saturates the amplifier



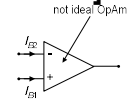
With  $V_{os} = 1 \text{ mV}$  and  $A = 10^5$  (100 dB):

(a)  $A \cdot V_{os} = 100 \text{ V}$

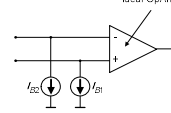
(b)  $A \cdot V_{os}$  much higher than the saturation voltage<sup>13</sup>

## Input bias and offset currents

(1) OAs [on bipolar tech] has input currents:



(a) This non-ideality can be modeled as:



(b) The non-idealities can be quantified as:

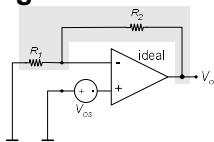
- Input bias current:  $I_B = \frac{1}{2} (I_{B1} + I_{B2})$

- Input offset current:  $I_{OS} = I_{B1} - I_{B2}$

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## Input offset voltage

For the inverting and non-inverting amplifiers



The output voltage is:

$$v_o = - \left(1 + \frac{R_2}{R_1}\right) \cdot V_{os}$$

The effect of  $V_{os}$  can be severe on signals with:

(a) reduced amplitudes

(b) low frequencies  $\rightarrow$  masked by  $V_{os}$

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## Input bias and offset current

(1) The previous equations results in:

$$\begin{cases} I_{B1} = I_B + \frac{I_{OS}}{2} \\ I_{B2} = I_B - \frac{I_{OS}}{2} \end{cases}$$

(2)  $I_{os}$  is also a random variable

It is possible to have:

$$\begin{cases} I_B = 100 \text{ nA} \\ |I_{OS}| < 10 \text{ nA} \end{cases}$$

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## Input offset voltage

(1)  $V_{os}$  can be compensated:

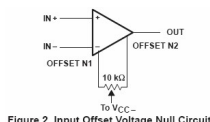
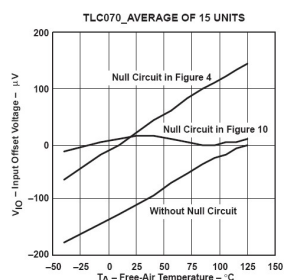


Figure 2. Input Offset Voltage Null Circuit

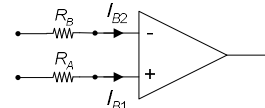
(2) Not fully effective:

$V_{os}$  mainly affected by  $T$



## Input bias and offset current

The input bias currents can be compensated:



(a) The voltage  $V(R_A)$  must be equal to  $V(R_B)$ :

(b) This can be achieved with:

$$R_A I_{B1} = R_B I_{B2}$$

(c)  $V(R_A)$ ,  $V(R_B)$  are common-mode voltages.

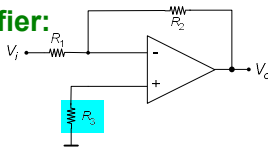
(d)  $V(R_A)$ ,  $V(R_B)$  "don't appear" in the output

Naturally, they are subjected to the CMRR

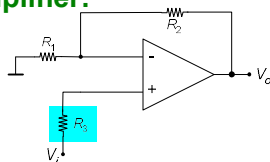
## Input bias and offset current

Compensation in basic amplifiers:

(a) Inverting amplifier:



(b) Non-inverting amplifier:



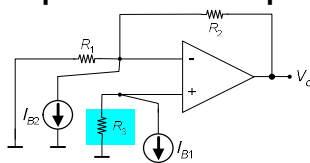
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## Frequency limitation

- (1) The differential gain  $A$  is not infinite
- (2) But even worse,  $A$  is frequency dependent
- (3) Contrary to others, this one can't be neglected
- (4) The frequency response is a critical issue  
Can affect the stability of feedback amplifiers
- (6) In general purpose OAs, the freq. comp.
  - (a) Is done internally
  - (b) Using the dominant pole technique
  - (c) Whose value is very low (typically 10 Hz)

## Input bias and offset current

This circuit represent both amplifiers with  $V_i=0$



Applying the superposition principle:

$$v_o = -I_{B1}R_3 \times \left(1 + \frac{R_2}{R_1}\right) + I_{B2}R_2$$

$I_{OS}$  is random  $\rightarrow$  the compensation is for  $I_{B1} = I_{B2}$

The condition to get  $v_o = 0$  V is:

$$R_3 = R_1 // R_2$$

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## Frequency limitation

Illustrating the dominant pole technique

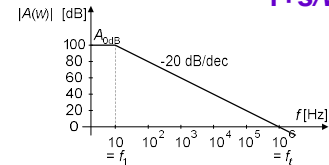
(a) Imagining:

- dominant pole in 10 Hz (i.e.,  $f_1 = 10$  Hz)
- DC gain of 100 dB (i.e.,  $A_{0dB} = 100$  dB)

(b) Dif. gain is (1<sup>st</sup> order):

$$A(s) = \frac{A_0}{1+s/w_1}$$

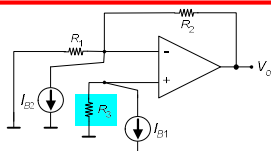
(c) Therefore:



$$(d) f_t = f_1 \cdot A_0 = f_1 \times 10^{A_{0dB}/20} = 10^6 \text{ Hz}$$

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## Input bias and offset current



(1) With: (a)  $R_3 = R_1 // R_2$

(b) and  $I_{B1} \neq I_{B2}$

$$\begin{cases} I_{B1} = I_B + \frac{I_{OS}}{2} \\ I_{B2} = I_B - \frac{I_{OS}}{2} \end{cases}$$

(2) The output is  $v_o = -I_{OS}R_2$

(3) Comparing  $v_o$  with  $R_3 = 0 \Omega$ :

(a)  $v_o \approx -I_B R_2$

(b) A clear reduction in  $v_o$  because  $|I_{OS}| < 0.1 I_B$

## Frequency limitation

(1) The gain of a non-inverter amplifier is

$$A_f(s) = \frac{A(s)}{1+\beta A(s)}$$

(2)  $\beta = 1/100 \wedge A_0 = 100$  dB

$\rightarrow A_{f0} = 100$

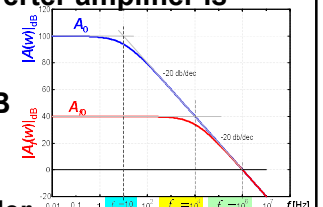
(or  $A_{f0dB} = 40$  dB)

(3)  $A_f(s)$  is also of 1<sup>st</sup> order

$$A_f(s) = \frac{A_{f0}}{1+s/w_a} \rightarrow \begin{cases} A_{f0} = A_0 / (1+\beta A_0) \\ w_a = w_1 \times (1+\beta A_0) \gg w_1 \end{cases}$$

(4) The small value of  $f_1$  isn't a problem 😊

(5) Increasing  $A_{f0}$   
Decreases  $w_a$  (i.e., the bandwidth)



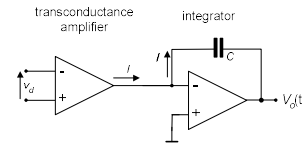
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## Frequency limitation

- (1)  $w_a$  decreases, but the product **GBP**
  - (a) Is equal to  $A_{f0} \cdot w_a$  and keeps constant
  - (b) Is equal to  $A_0 \cdot w_1$
- (2) **GBP** constant is a limitation of technology
- (3) It is easy to obtain
  - (a) Large gain, low bandwidth
  - (b) Large bandwidth, low gain
- (4) But hard to have both simultaneously large

## Slew-rate

- (1) **C** is for internal compensation (dom. pole)



- (2) The current  $i$  is such that

$$i = -C \frac{dv_o}{dt}$$

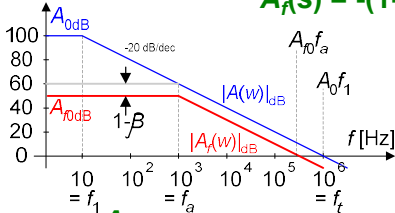
- (3) Therefore

$$SR = \left| \frac{dv_o}{dt} \right|_{max} = \frac{I_{max}}{C}$$

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## Frequency limitation

- (1) Inverter amplifier:  $A_f(s) = -(1-\beta) \times \frac{A(s)}{1+\beta A(s)}$



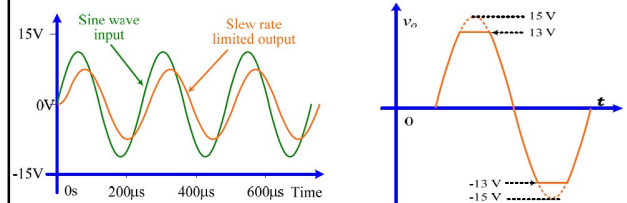
$$A_f(s) = \frac{A_{f0}}{1+s/w_a} \rightarrow \begin{cases} A_{f0} = -(1-\beta)A_0/(1+\beta A_0) \\ w_a = w_1 \times (1+\beta A_0) \end{cases}$$

- (2) For  $\beta A_0 \gg 1 \rightarrow A_{f0} \approx -\frac{1-\beta}{\beta} = -\frac{R_2}{R_1}$
- (3) **GBP** =  $A_{f0} w_a = (1-\beta)A_0 w_1$  is not constant <sup>26</sup>

## Slew-rate

- (1) For  $v_o(t) = V_{om} \cos(\omega t)$   $\left| \frac{dv_o}{dt} \right|_{max} = V_{om} \omega < SR$

- (2) This means that  $\omega_M = SR/|v_{o}|_{max}$
- (3)  $\omega_M$  is the full power frequency
- (4) The **SR** is a not-linear phenomena

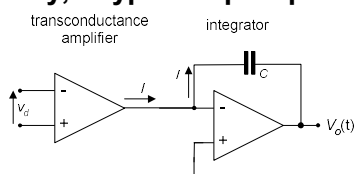


## Slew-rate

- (1) The output voltage can't change more fast than the slew-rate, **SR**
- (2) The slew-rate is defined as

$$SR = \left| \frac{dv_o}{dt} \right|_{max}$$

- (3) Internally, a typical OpAmp can be seen as:



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## Selected bibliography



**Tack för er  
uppmärksamhet**

**Jag är öppen för frågor**

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