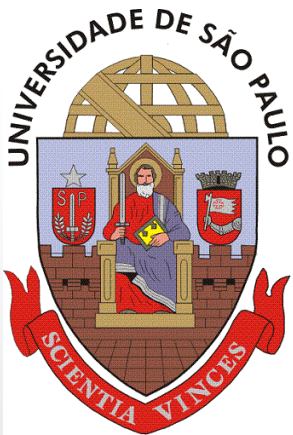


# Wave Energy: Introduction

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# Overview

- The potential for wave energy
- Wind waves in the ocean environment
- Wave mechanics
- Wave energy and its propagation
- WECs: some history
- WECs: basic features and main types
- Recent trends and perspectives
- References (for further and deeper studies)

# The potential for wave energy

- The potential for wave energy harnessing has long been known..



- Recent estimation of total world wide wave power [1]:

Total power  $\sim 2.7$  TW

# The potential for wave energy

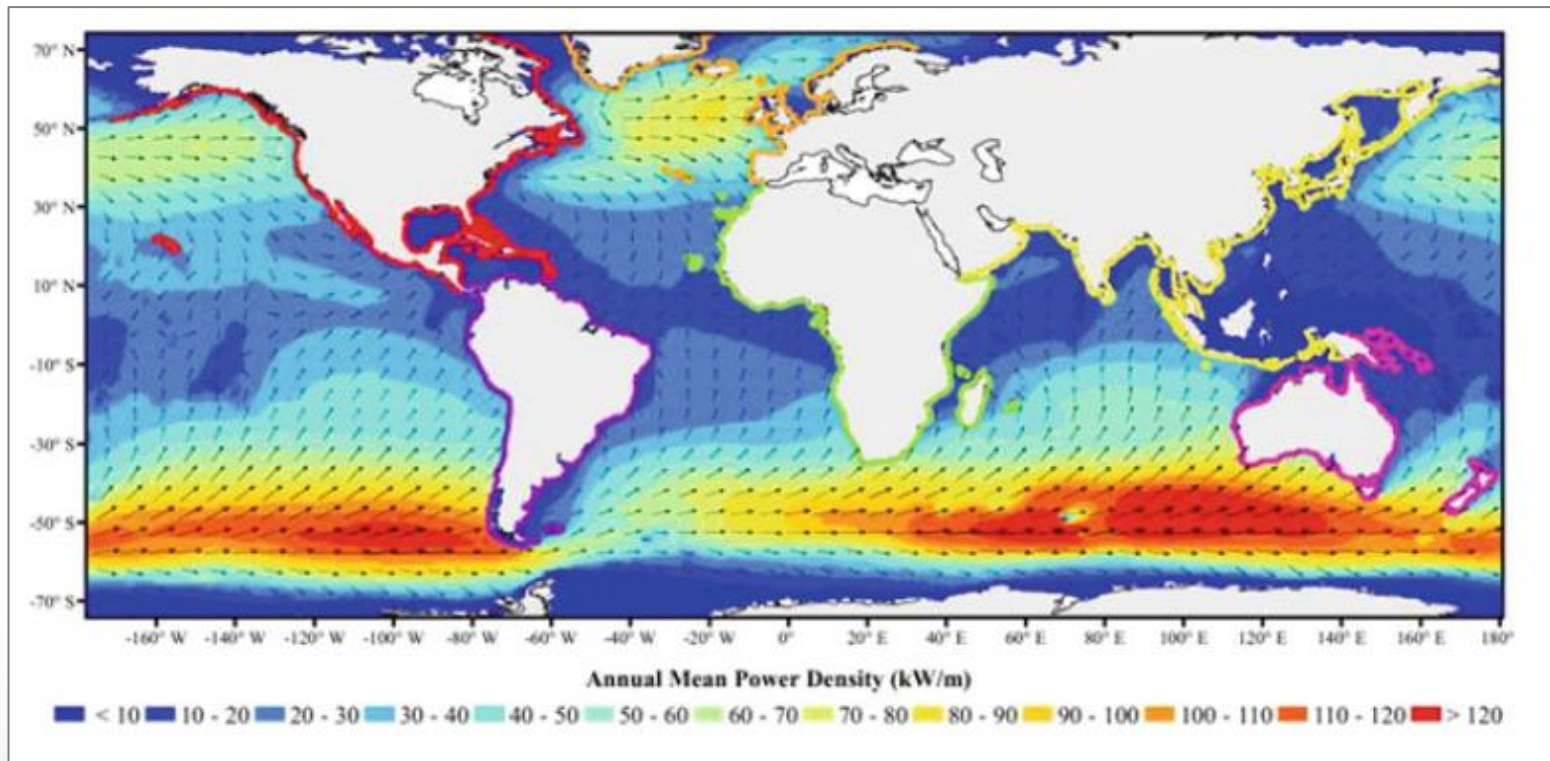
- This is only a fraction of the estimated total wind power, which in turn is only a fraction of the estimated total solar power, but the wave energy *density* is much *higher* (Power/surface area – W/m<sup>2</sup>)

$$\text{energy density} = \frac{\text{Power}}{\text{area}} \left( \frac{\text{W}}{\text{m}^2} \right)$$

- According to Falnes (2007) [2]:
  - Solar: ~ **0.1 – 0.3** kW/m<sup>2</sup> (earth surface)
  - Wind: typically **0.5** kW/m<sup>2</sup> (perpendicular to wind)
  - Waves: typically **2 – 3** kW/m<sup>2</sup> (perpendicular to waves)

# The potential for wave energy

- Estimates of mean wave energy distribution around the globe can also be found (see, for instance, [3]):



Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy*, Springer Open, Ocean Eng. and Oceanography Series V.7, 2017 [4]

# The potential for wave energy

- However, the problems for economically harvesting such energy are **MANY**, such as:
  - There is a large **seasonal variability** of the mean energy in any location (typically around 50% !).
  - In any spot and any season, there is also a **large variability of wave energy in time** (related to local wind conditions and swells coming from distant locations).
  - In a real sea condition, there is always some level of **energy spread regarding wave direction** (more intense in deep water areas).
  - The need for mechanical devices operating in a **hostile environment** (current and wind loads, corrosion, etc.), requiring intensive maintenance.
  - Wave energy is better offshore, but this requires floating systems, with large economical impacts from **moorings and power cables to the shore...**

# The potential for wave energy

- All these problems, ultimately...

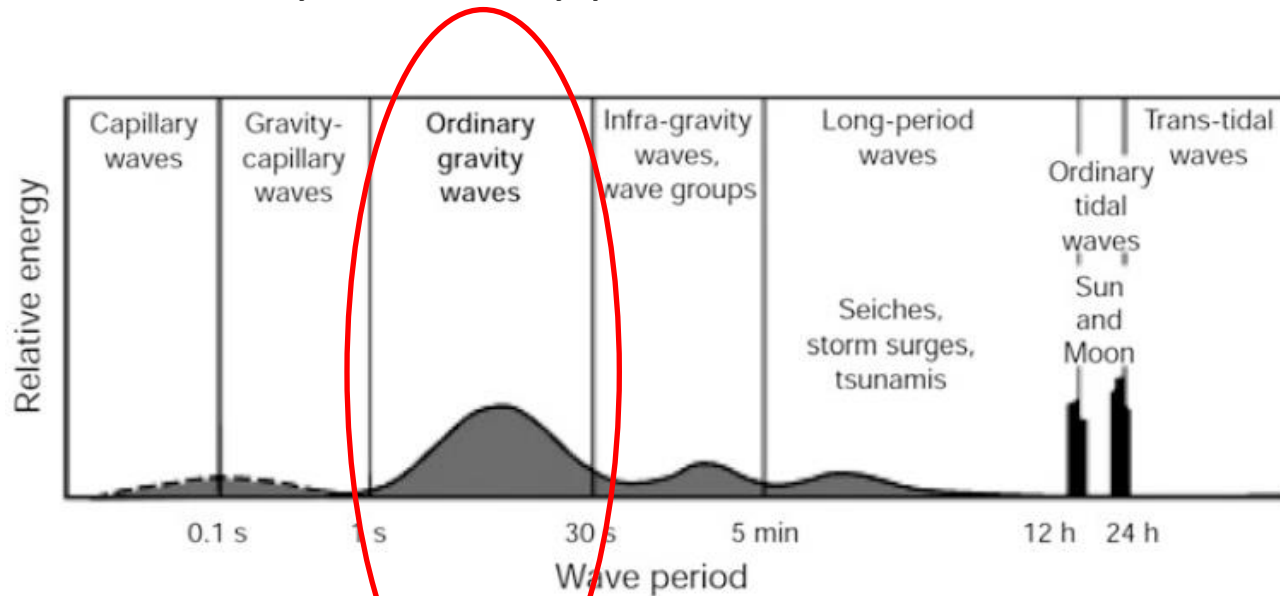
Prevent (so far) the economical feasibility of wave energy conversion devices (WECs) designed for large-scale and long-term commercial electrical power production, but...

there is always opportunity for small-scale energy production for specific sites/applications, and the economics change depending on many variables (environmental constraints, oil/gas prices, development of smart-grids, etc...)



# Wind waves in the ocean environment

- There are many oscillatory phenomena in the ocean:

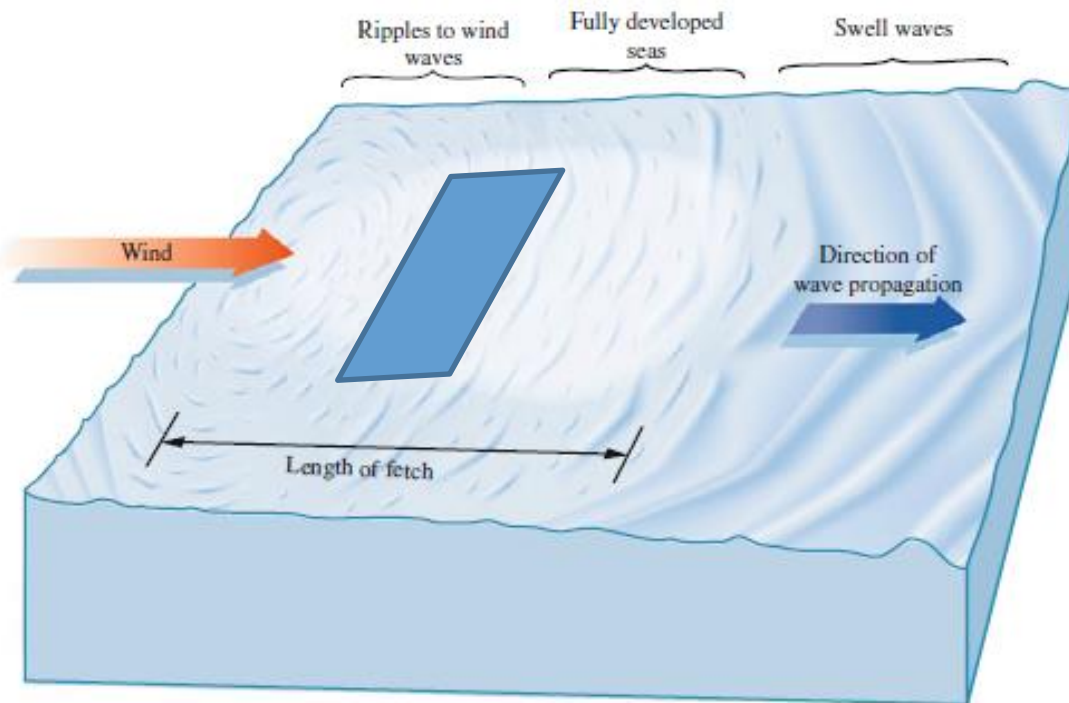


Restoring force is the water weight;  
Wind waves



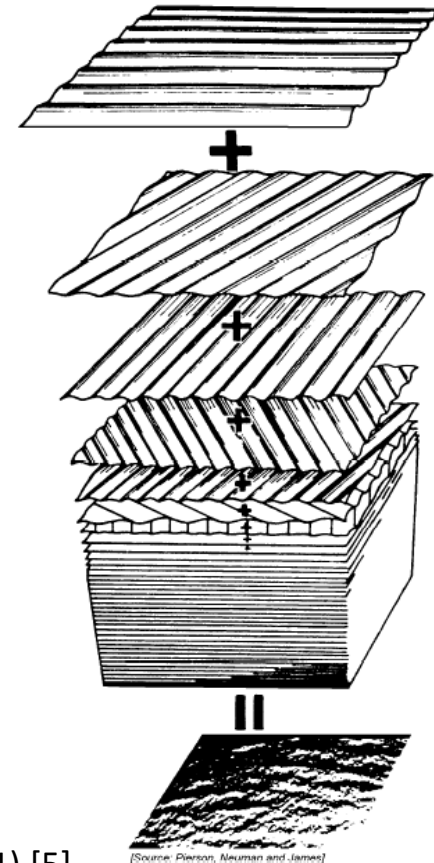
# Wind waves in the ocean environment

- Waves generated by wind action:
  - Quite efficient mechanism of energy transmission
  - Different characteristics as move away from generation zone



# Wind waves in the ocean environment

- In or close to the generation zone: “Sea waves”
  - **Waves of various frequencies, amplitudes and directions coexist**

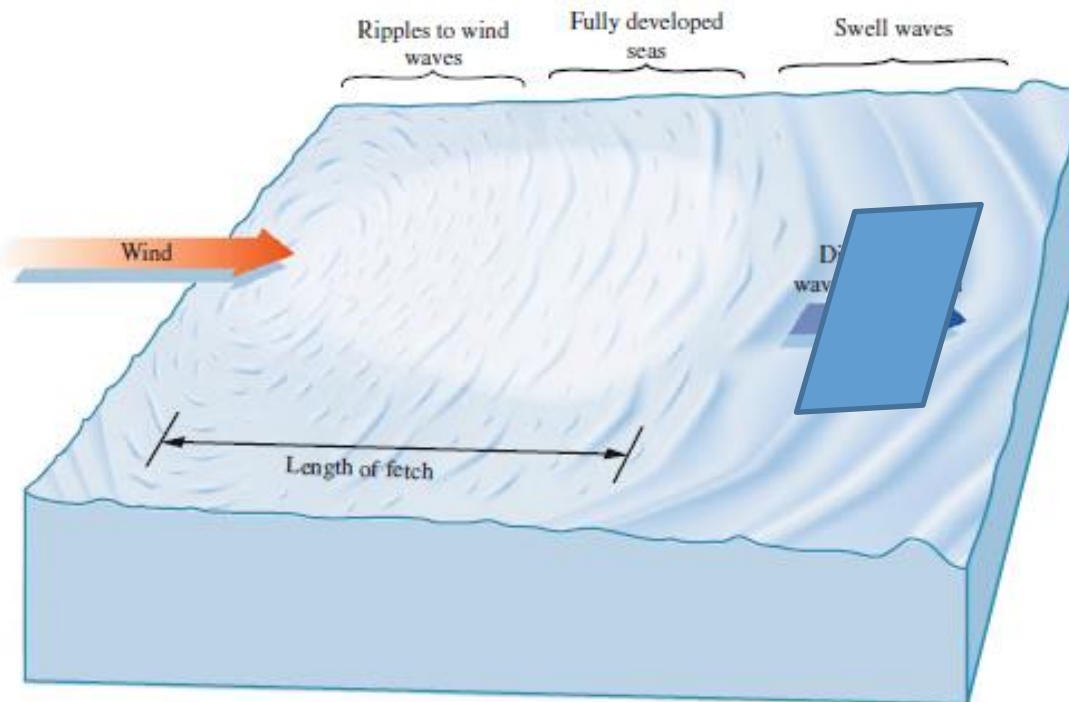


Source: Journée & Massie (2001) [5]

[Source: Pierson, Neuman and James]

# Wind waves in the ocean environment

- Waves generated by wind action:
  - Quite efficient mechanism of energy transmission
  - **Different characteristics as move away from generation zone**



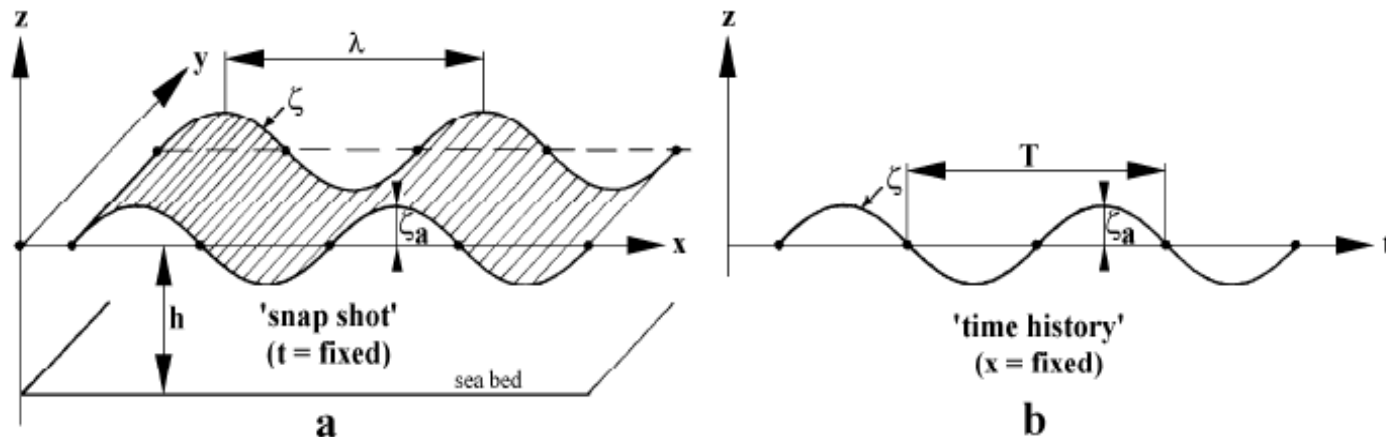
# Wind waves in the ocean environment

- Far from the generation zone: “Swell waves”
  - **Only waves of approx. equal frequencies coexist in each location**



# Wave Mechanics

- Let us examine the mechanics of wind waves:
- **Suppose a “regular” progressive wave:**



Source: Journée & Massie (2001) [5]

- 3 parameters define the wave:

- Amplitude (m):  $A$

- Wavelength (m):  $\lambda$

- Period (s):  $T$



Wave number (rad/m):

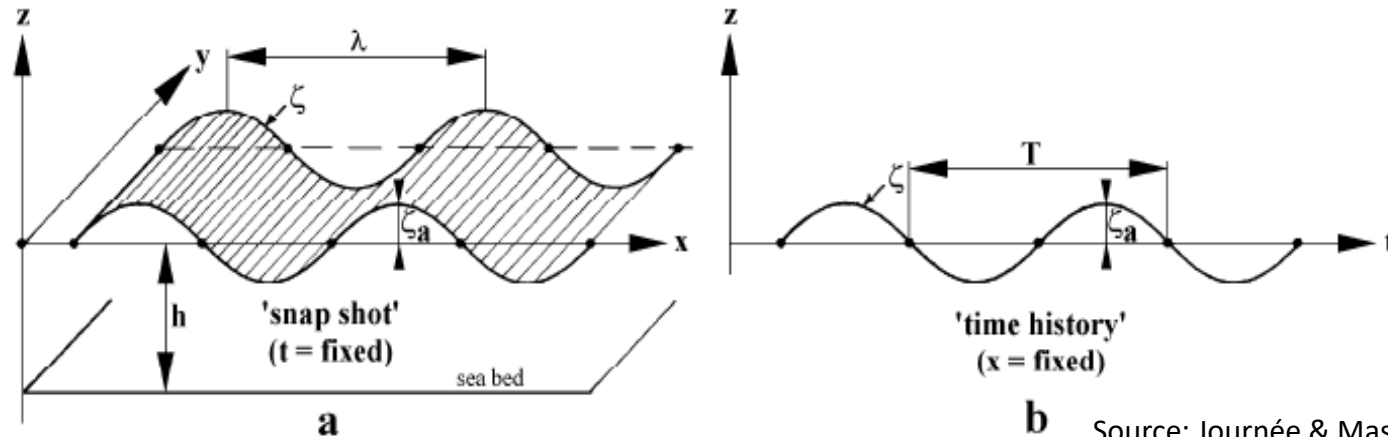
$$k = 2\pi/\lambda$$

Wave frequency (rad/s):

$$\omega = 2\pi/T$$



# Wave Mechanics



Source: Journée & Massie (2001) [5]

- It progresses in the  $x+$  direction with velocity (**celerity**):

$$c = \frac{\lambda}{T} = \frac{\omega}{k}$$

- and, if the ratio  $A/\lambda$  is small (typically below **3%**), the wave is considered **linear**, and the wave equation is given simply by:

$$\zeta(x, t) = A \cos(kx - \omega t)$$

# Wave Mechanics

- Gravity waves are **dispersive waves**: there is a nonlinear relation between wavelength ( $\lambda$ ) and wave period (T)
- For *linear waves in a constant depth*  $h$ , the dispersion relation is given by:

$$k = \frac{\omega^2}{g \tanh(kh)}$$

- Thus:

$$\lambda = \frac{gT^2 \tanh(kh)}{2\pi}$$



Longer waves have higher periods

$$c = \frac{gT \tanh(kh)}{2\pi}$$

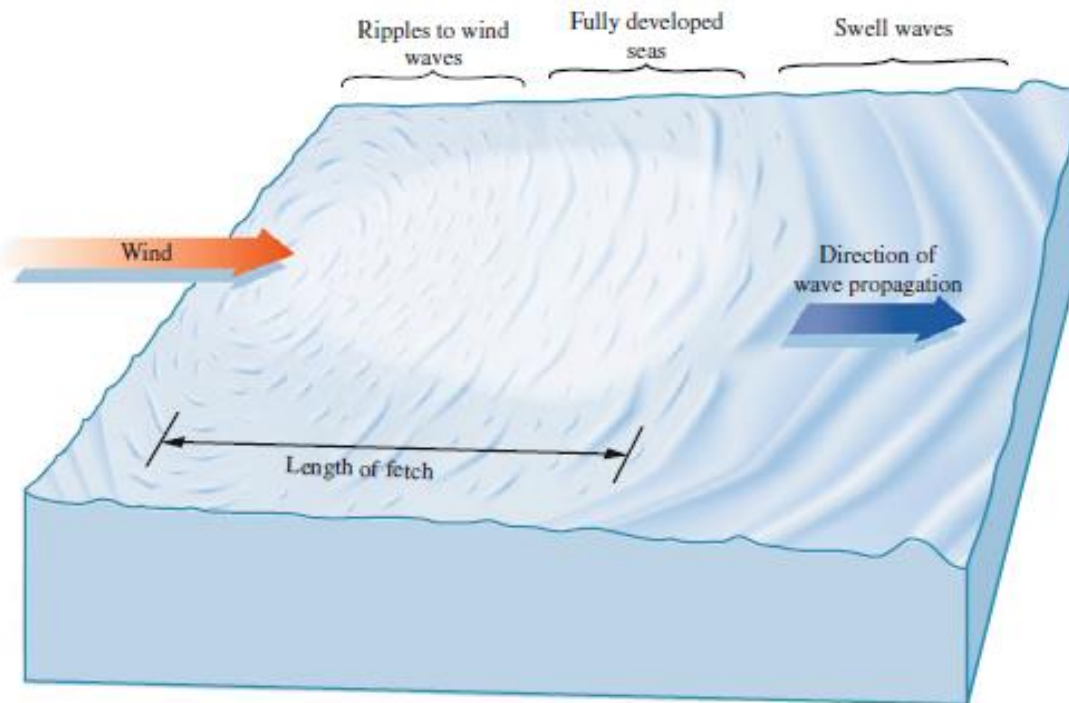


Longer waves have **higher speeds**



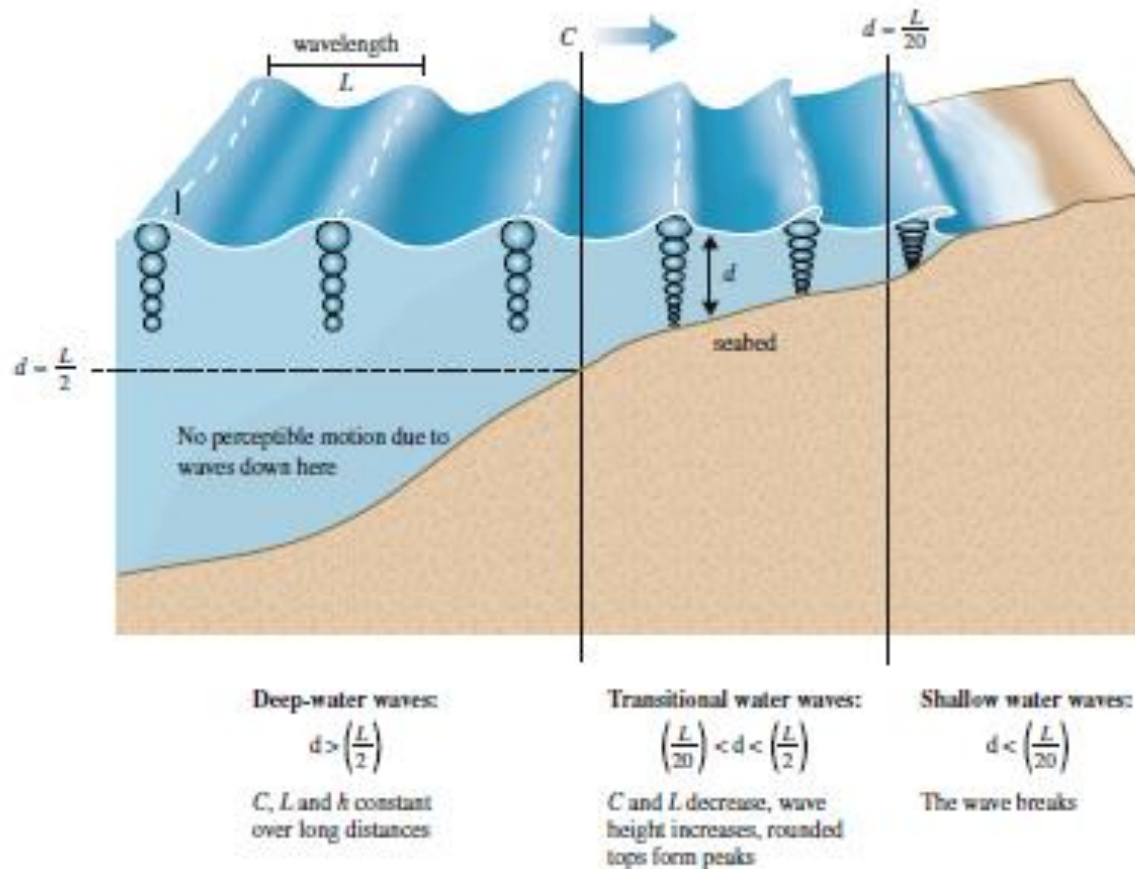
# Wave Mechanics

- This explains the *regularization process* the waves undergo as they move away from the generation zone: *each wave component has a different speed (dispersion)*



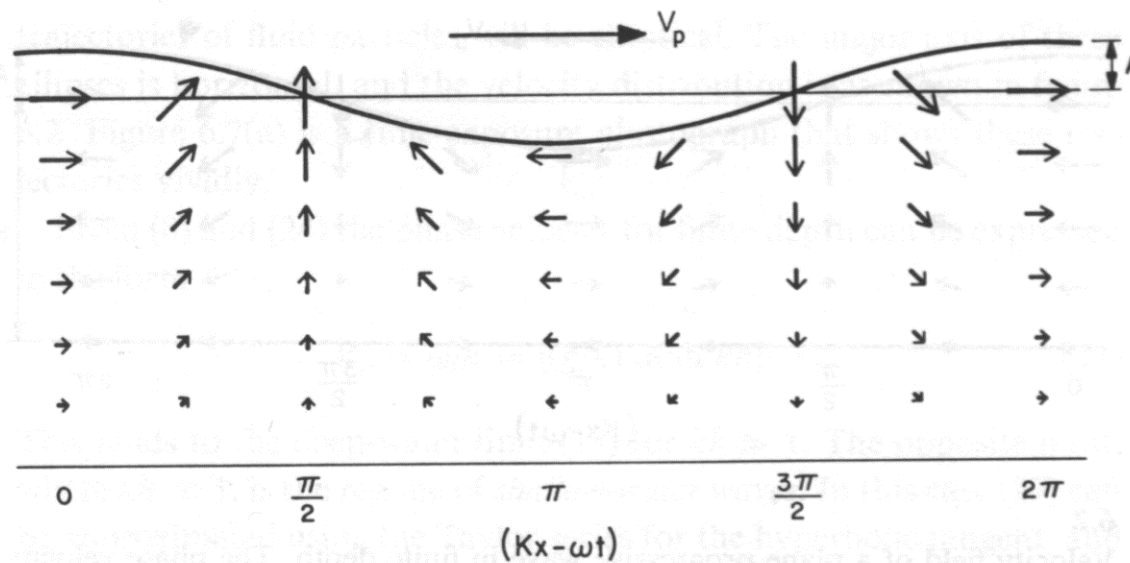
# Wave Mechanics

- Surface waves are associated with a periodic water flow:



# Wave Mechanics

- For **deep waters** ( $h > \lambda/2$ ), orbits are essentially circular and their radius **decay exponentially** with depth;
- The flow velocity field exhibits the following behavior:



# Wave Mechanics

- ...and velocities in any point of the flow can be calculated as:

$$\vec{v}(x, z, t) = u(x, z, t)\vec{i} + w(x, z, t)\vec{k}$$

- with:

$$u(x, z, t) = \omega A e^{kz} \cos(kx - \omega t)$$

$$w(x, z, t) = \omega A e^{kz} \sin(kx - \omega t)$$

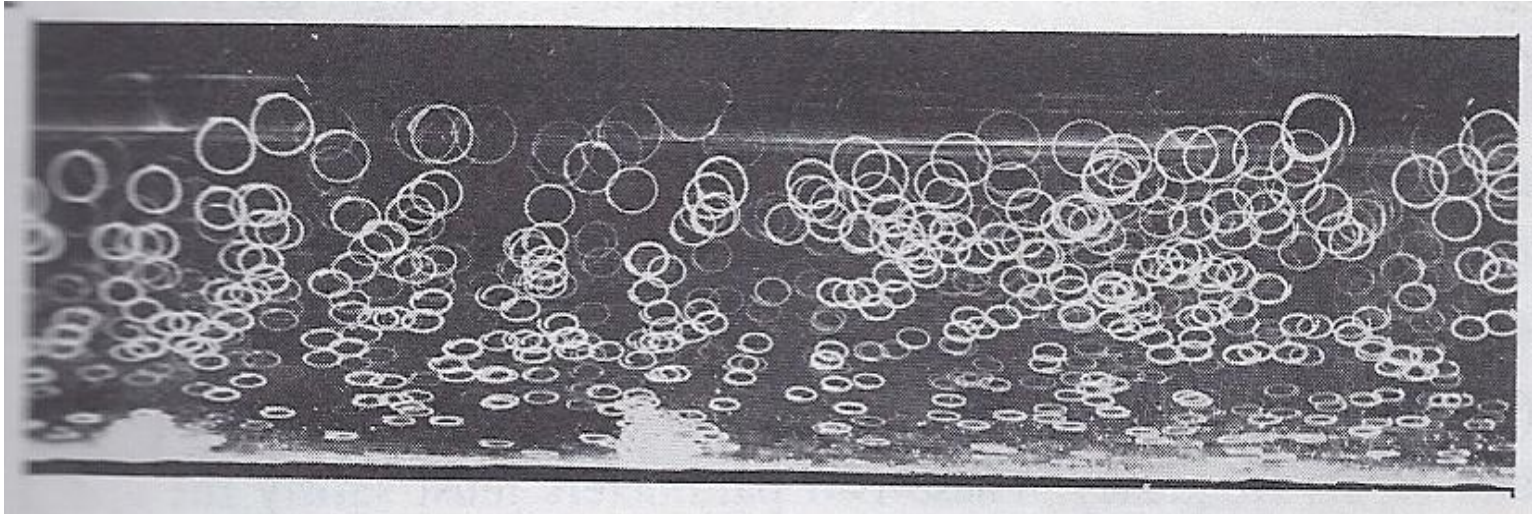
- Thus:

$$|\vec{v}(x, z, t)| = \omega A e^{kz}$$

**Flow energy is  
concentrated  
close to the  
surface**

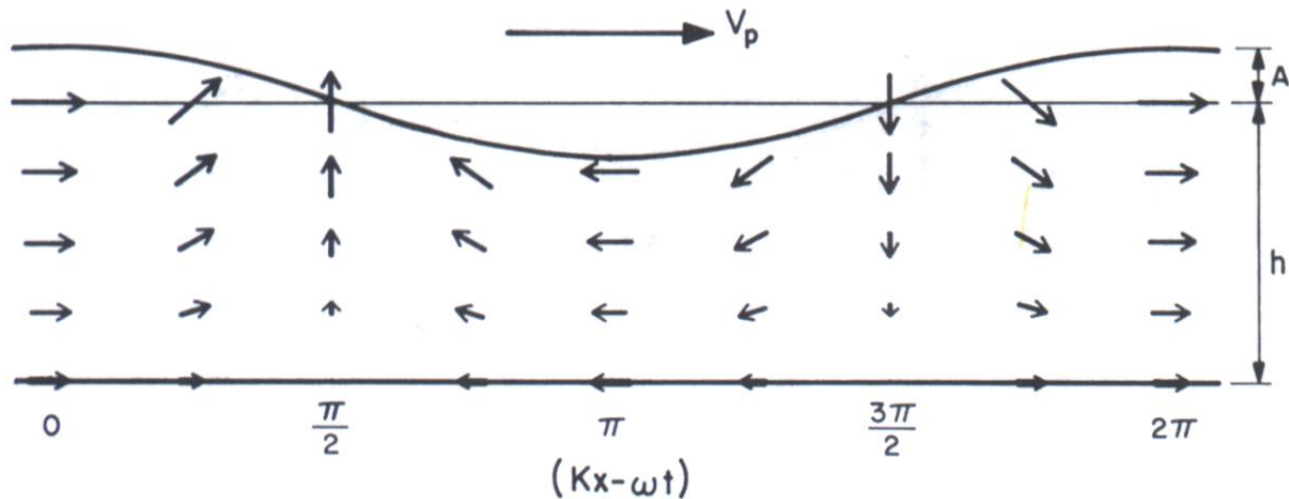
# Wave Mechanics

- For **finite water depths** ( $h < \lambda/2$ ), orbits are essentially elliptic and decay hyperbolically with depth:



# Wave Mechanics

- The flow velocity field exhibits the following behavior:



# Wave Mechanics

- ...and velocities in any point of the flow can be calculated as:

$$\vec{v}(x, z, t) = u(x, z, t)\vec{i} + w(x, z, t)\vec{k}$$

- with:

$$u(x, z, t) = \omega A \frac{\cosh k(z + h)}{\sinh(kh)} \cos(kx - \omega t)$$

$$w(x, z, t) = \omega A \frac{\sinh k(z + h)}{\sinh(kh)} \sin(kx - \omega t)$$



# Wave energy and its propagation

- **Wave energy** is composed of:
  - **Potential energy**, associated to wave elevation
  - **Kinetic energy**, associated with fluid flow
- For a regular progressive wave:

$$Energy = \frac{1}{2} \rho g A^2$$

Mean wave energy  
per surface area of  
the sea  
(J/m<sup>2</sup>)

# Wave energy and its propagation

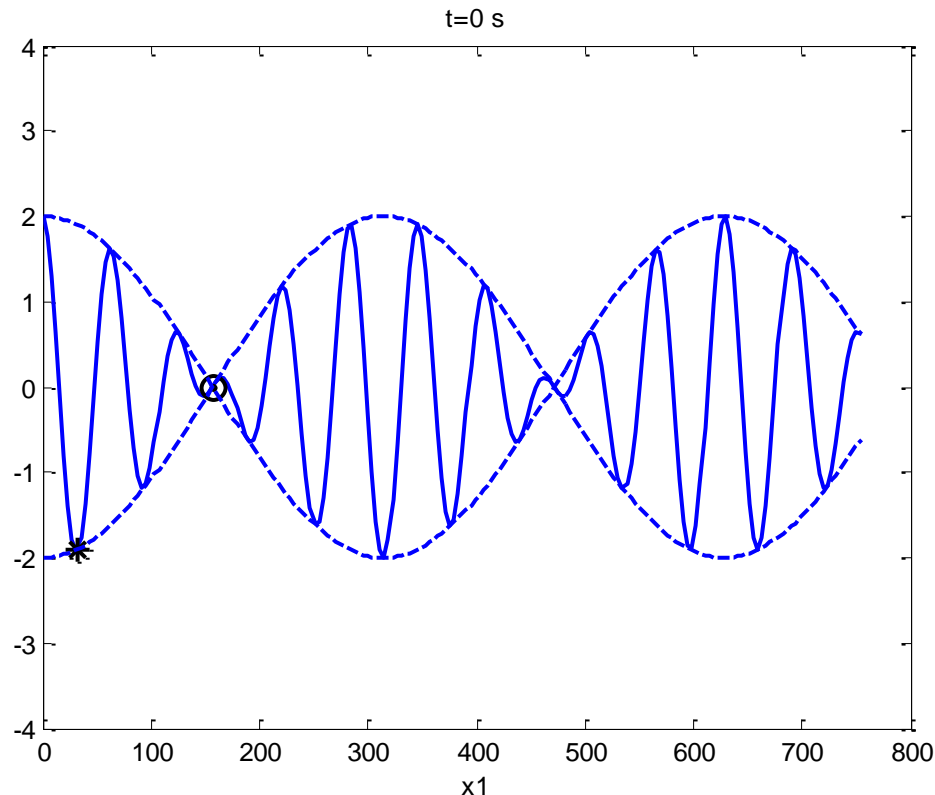
- However, in general, **this energy is not transmitted with the wave celerity ( $c$ ), but rather with a smaller velocity named **group velocity ( $c_g$ )****
- For understanding this, let's consider two waves of same amplitude  $A/2$  and almost the same frequencies  $\{(\omega - \delta\omega)$  and  $(\omega + \delta\omega)\}$ , which propagate in the same direction. It is easy to show that, in this case, the wave equation is given by

$$\zeta(x, t) = A \cos(\delta k x - \delta \omega t) \cos(k x - \omega t)$$

Wave **modulation**:  
Large wavelength:  $2\pi/\delta k$   
High period:  $2\pi/\delta \omega$

# Wave energy and its propagation

- The wave moves with celerity  $c$ , but it is confined in a “wave group” ...

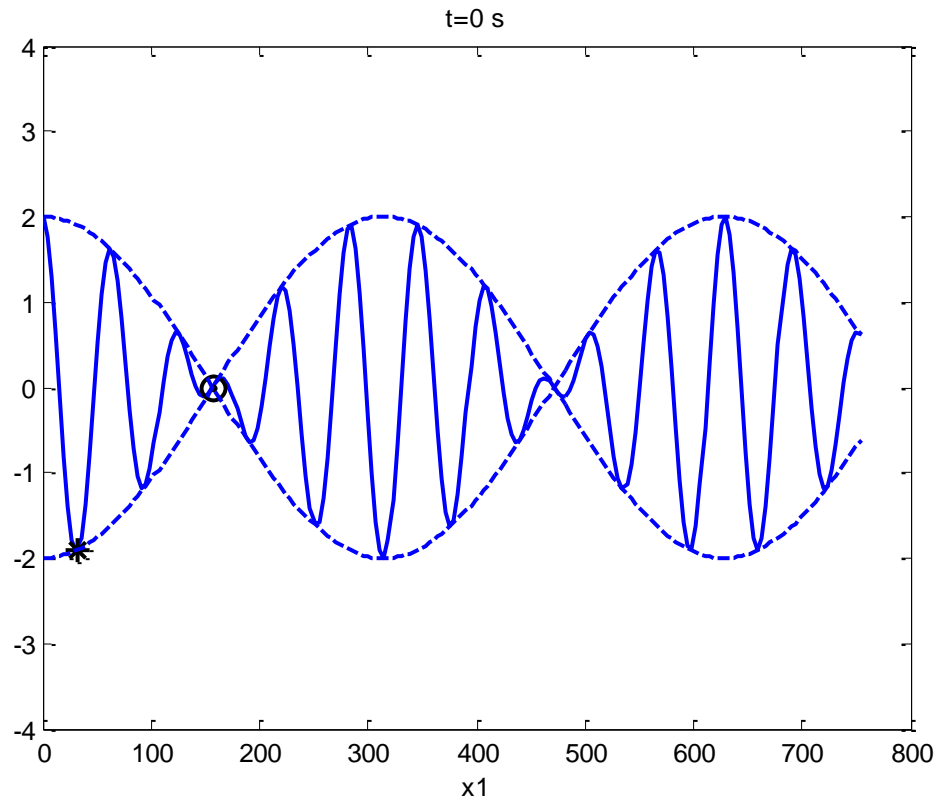


- ...which moves with *group velocity*:

$$c_g = \frac{d\omega}{dk}$$

# Wave energy and its propagation

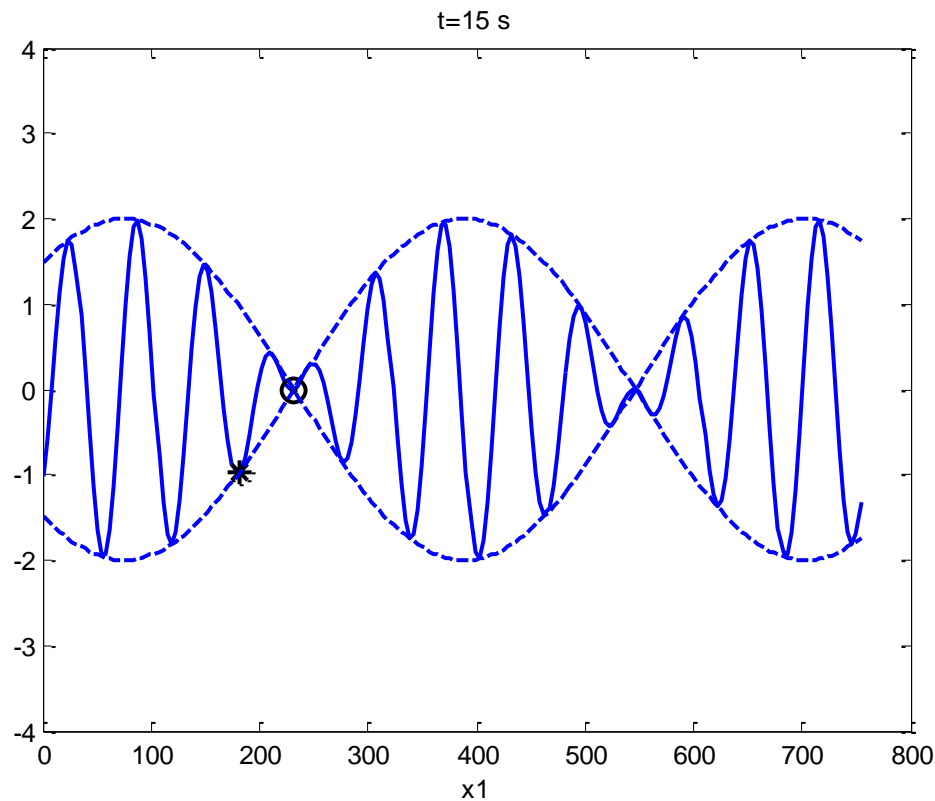
- As an example: the next figures show the evolution in time of a wave point (with  $c$ ) and of a group point (with  $c_g$ )



wave celerity (\*) and group velocity (o)

# Wave energy and its propagation

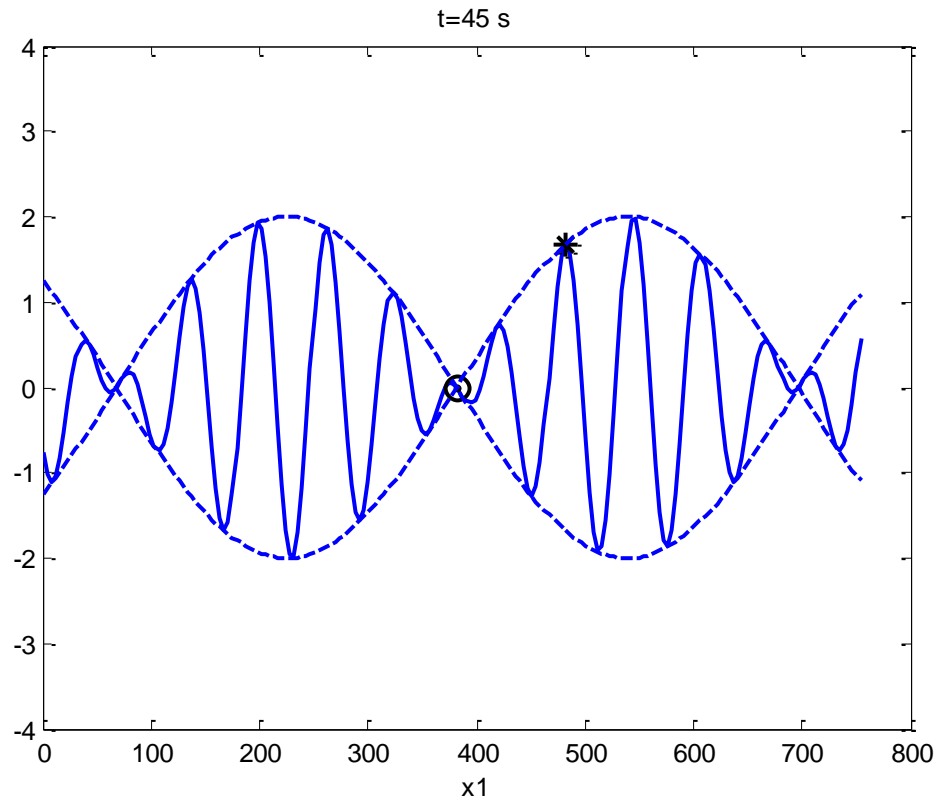
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wave celerity (\*) and group velocity (o)

# Wave energy and its propagation

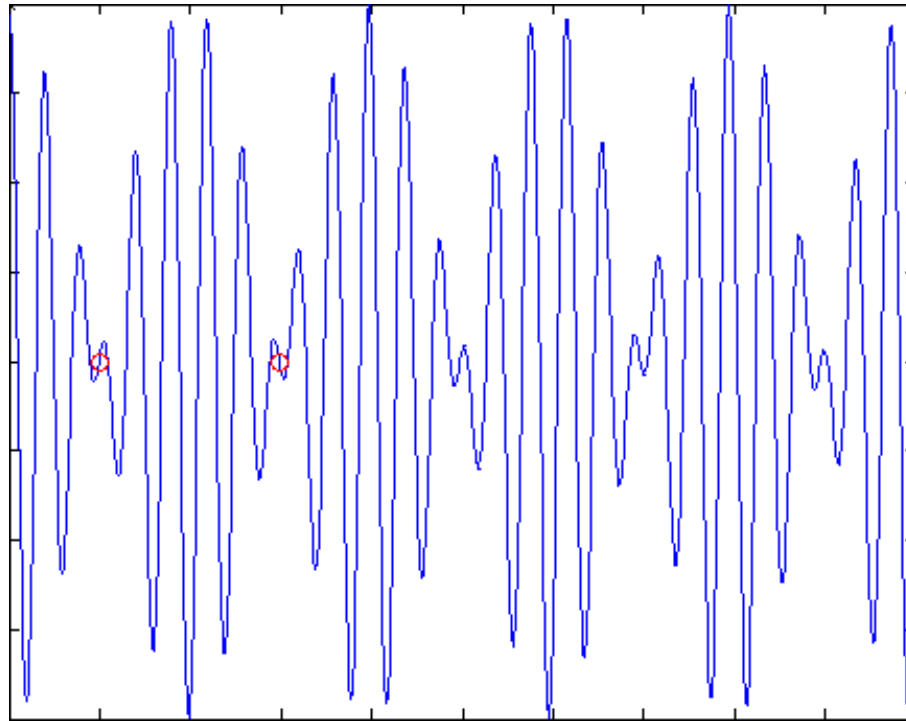
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# Wave energy and its propagation

- As an example: the next figures show the evolution in time of a wave point (with  $c$ ) and of a group point (with  $c_g$ )

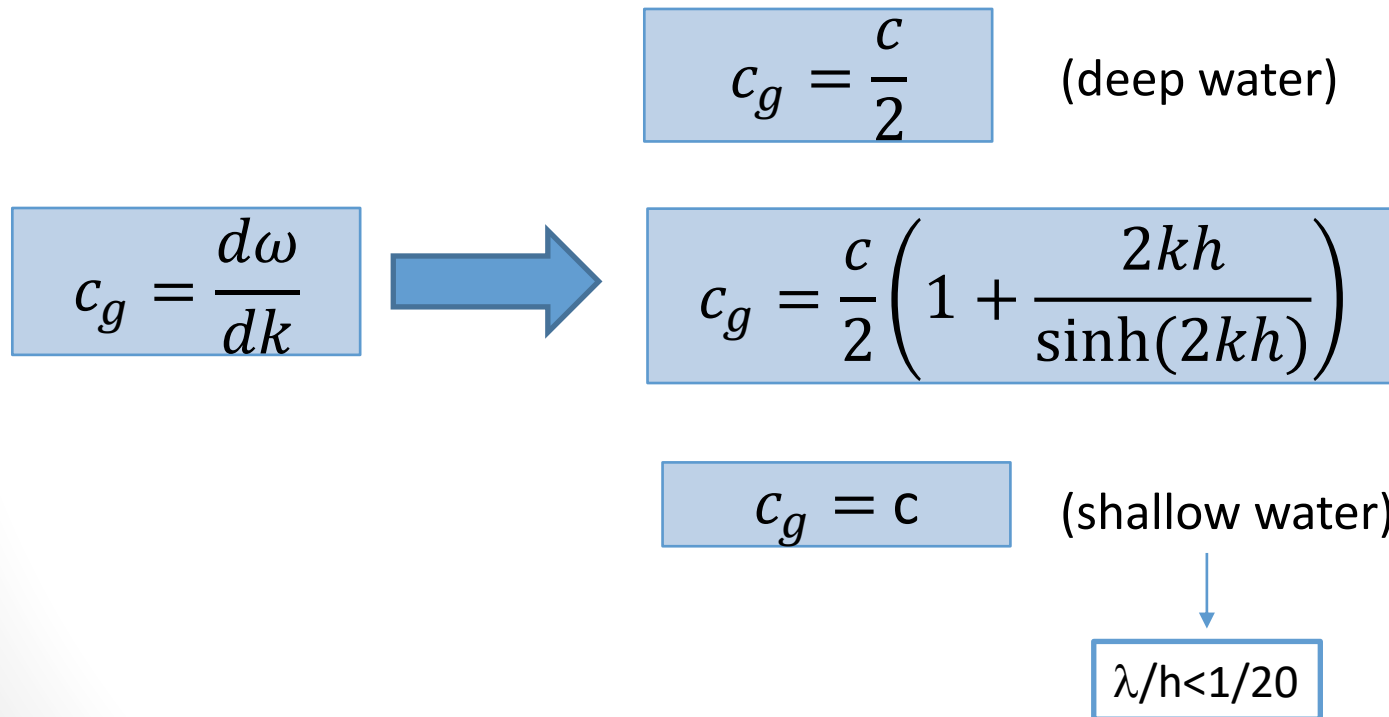


wave celerity (\*) and group velocity (o)



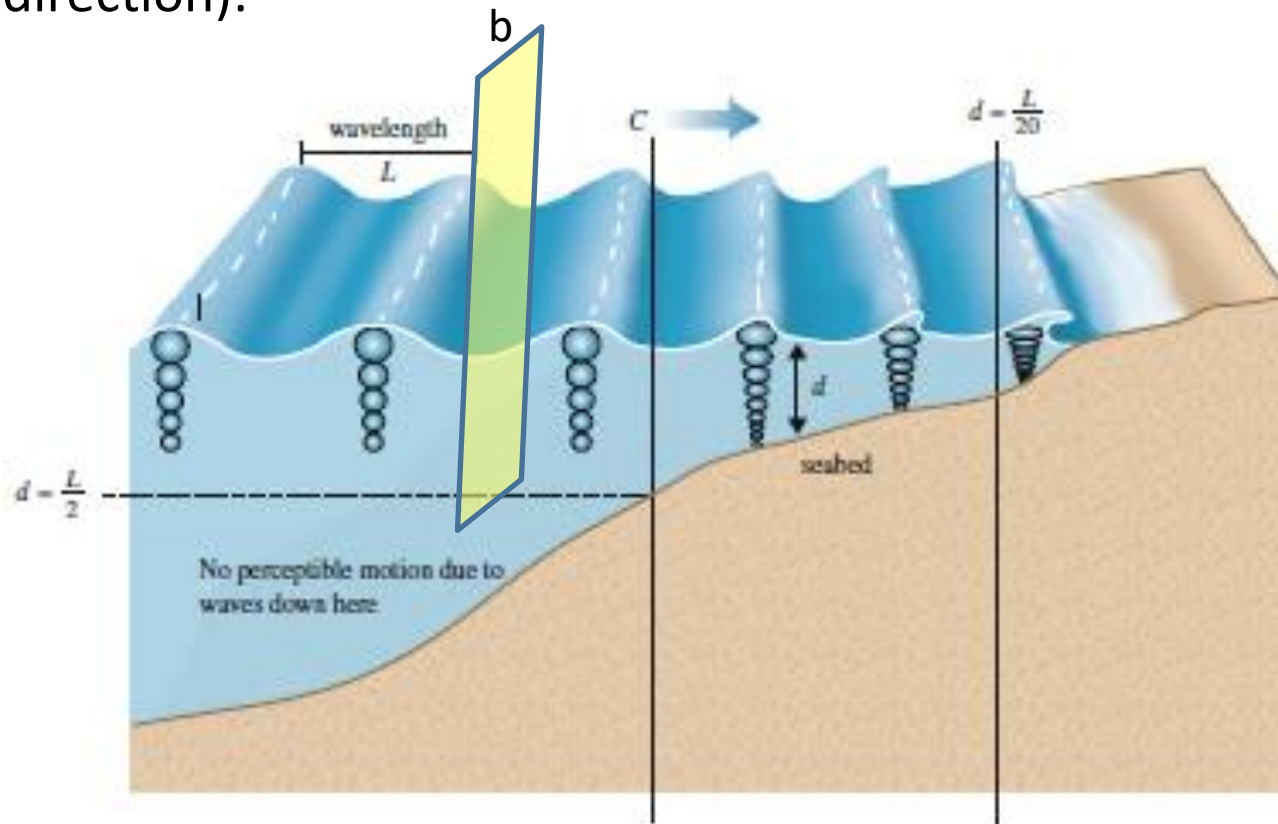
# Wave energy and its propagation

- Thus, the **mean wave energy propagates with the group velocity** which, *in its turn, depends on the water depth*:



# Wave energy and its propagation

- Therefore, if we want to know the **wave mean energy flux (power) through a section of width  $b$**  (perpendicular to the wave direction):



# Wave energy and its propagation

- This **mean power** will be:

$$power = \frac{1}{2} \rho g A^2 c_g b \quad (\text{W})$$

This is the maximum available power that can be extracted from a width  $b$  parallel to the wave crests in the sea

# Wave energy and its propagation

- **Example:**
- Let's consider a wave in deep water, with amplitude  $A=1\text{m}$  and period  $T=10\text{s}$ . Then:

$$\rho = 1025 \text{ kg/m}^3$$

$$g = 9,81 \text{ m/s}^2$$

$$c_g = 1/2c = 1/2(gT/2\pi) = 7,81 \text{ m/s}$$

$$\text{power/m} = \frac{1}{2} \rho g A^2 c_g = 39,25 \text{ (kW/m)}$$

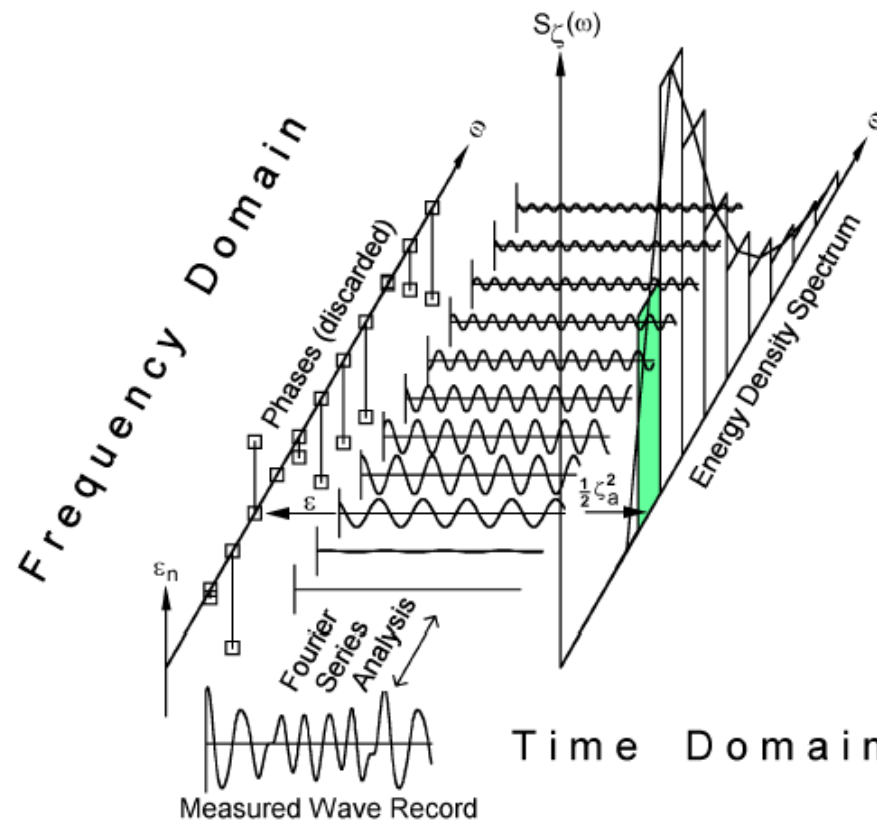
# Wave energy and its propagation

- Have in mind that WECs are designed considering:
  - **An optimum wave frequency (or wavelength), and**
  - **An optimum wave direction**



# Wave energy and its propagation

- **However**, in a **real sea**, there is always a *spread of wave energy in the different wave frequencies* (represented by a **wave energy spectrum**):



# Wave energy and its propagation

- **Main statistical quantities:**

- Spectral moments: 
$$m_k = \int_0^{\infty} \omega^k S_{\zeta}(\omega).d\omega$$

- Standar deviation: 
$$\sigma = RMS = \sqrt{m_0} = \left[ \int_0^{\infty} S_{\zeta}(\omega).d\omega \right]^{1/2}$$

- Significant wave amplitude/height 
$$A_{1/3} = 2\sqrt{m_0}$$
$$H_{1/3} = 4\sqrt{m_0}$$

- (Mean) Central period: 
$$T_1 = 2\pi \frac{m_0}{m_1}$$

- Zero up-crossing period: 
$$T_2 = 2\pi \sqrt{\frac{m_0}{m_2}}$$



# Wave energy and its propagation

- **For example, the JONSWAP energy spectrum:**

- *Joint North Sea Wave Project (1968-1969)*
- *North Sea – 100 nm from Sylt Island*
- *Fetch limited seas*
- ITTC (1984) recommended:

$$S_{\zeta}(\omega) = \frac{320.H_{1/3}^2}{T_p^4} \omega^{-5} \exp\left\{\frac{-1950}{T_p^4} \omega^{-4}\right\} \gamma^A$$

Peakedness factor

$$\gamma = 3.3$$

Nowadays  $\gamma$  is a  
3<sup>rd</sup> parameter:  
universality

$$A = \exp\left\{-\left(\frac{\frac{\omega}{\omega_p} - 1}{\sigma\sqrt{2}}\right)^2\right\} \quad \begin{array}{ll} \sigma = 0.07; & \omega < \omega_p \\ \sigma = 0.09; & \omega > \omega_p \end{array}$$

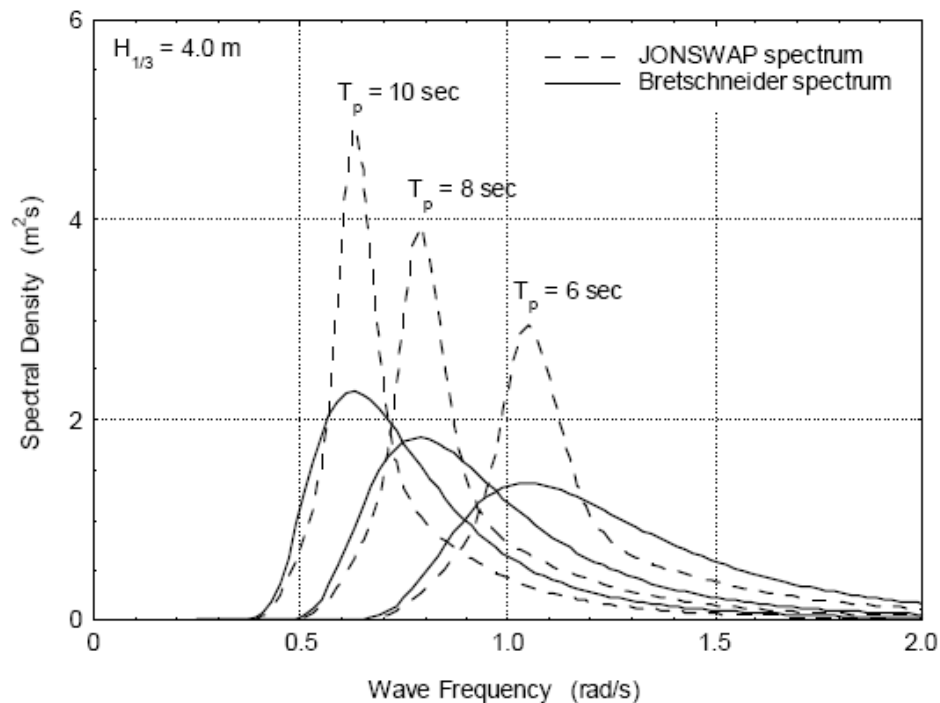
$$T_p = 1.199T_1 = 1.287T_2$$

# Wave energy and its propagation

- For example, the JONSWAP energy spectrum:
  - *Comparison with Bretschneider spectrum (for fully developed seas)*

IF:  $\gamma^A = 1.522$

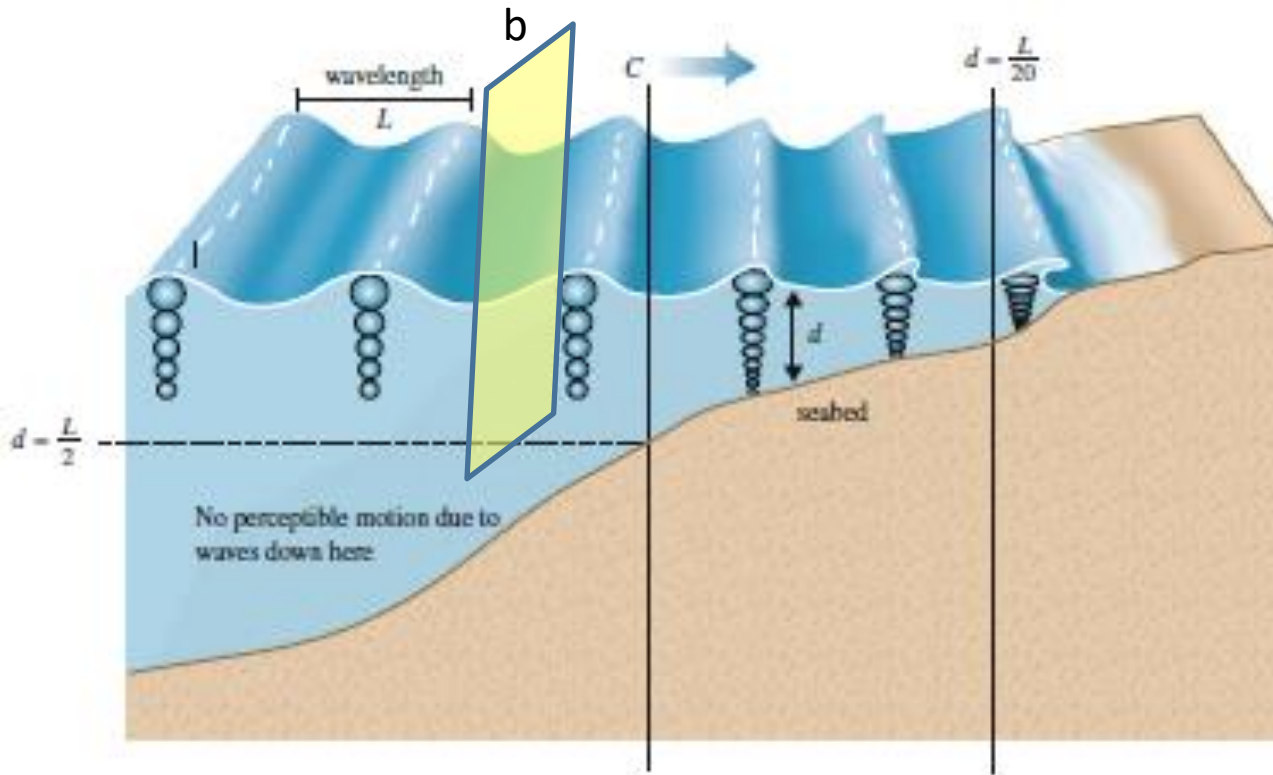
JONSWAP=Bretsch.



# Wave energy and its propagation

We saw that:

$$power = \frac{1}{2} \rho g A^2 c_g b \quad (\text{W})$$



# Wave power in irregular waves (real sea)

For a regular wave:

$$\bar{W}/_b = \frac{1}{2} \rho g A^2 c_g \quad (\text{W/m})$$

with: 
$$c_g(\omega) = \frac{c}{2} \left( 1 + \frac{2kh}{\sinh(2kh)} \right)$$

Thus, for a given sea state (wave spectrum):

$$\bar{W}_s/_b = \int_0^\infty \frac{1}{2} \rho g A^2(\omega) c_g(\omega) d\omega \quad (\text{W/m})$$

$$\bar{W}_s/_b = \rho g \int_0^\infty S(\omega) c_g(\omega) d\omega \quad (\text{W/m})$$

# Wave power in irregular waves (real sea)

For practical purposes, a simpler statistical measure is usefull:

$$\overline{W_s}/_b = \frac{1}{2} \rho g A_{1/3}^2 c_g(\omega_p) \quad (\text{W/m})$$

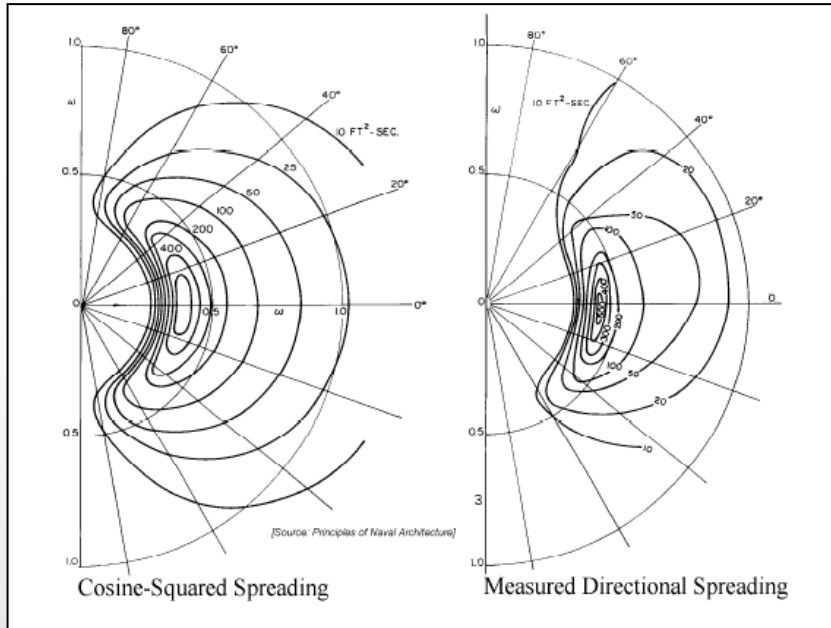
or:

$$\overline{W_s}/_b = \frac{1}{8} \rho g H_{1/3}^2 c_g(\omega_p) \quad (\text{W/m})$$

...from which statistical wave data (metocean data) for a given location can be easily applied for a prediction of its wave power potential

# Wave energy and its propagation

- **Spread of wave energy in direction:**
  - *In a real sea, there will always be some spreading of energy (power) in different wave directions;*
  - *Directional wave spectrum:  $S(\omega, \theta) = S(\omega)G(\theta)$* 
    - *Example: cosine-squared model:*

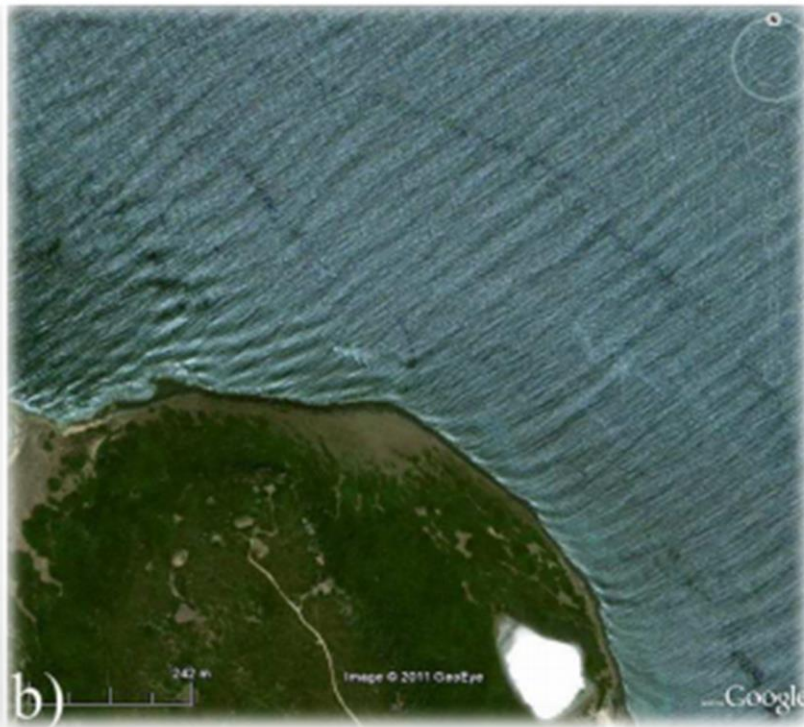


$$S_z(\omega, \theta) = \left\{ \frac{2}{\pi} \cos^2(\theta - \bar{\theta}) \right\} S_z(\omega)$$

$$-\frac{\pi}{2} \leq (\theta - \bar{\theta}) \leq \frac{\pi}{2}$$

# Wave energy and its propagation

- In open sea, wave direction is usually **highly variable** (local wind direction and swell coming from distant regions)...
- **Near the shore** (shallow waters), waves undergo *refraction* and tend to align with the shore line...

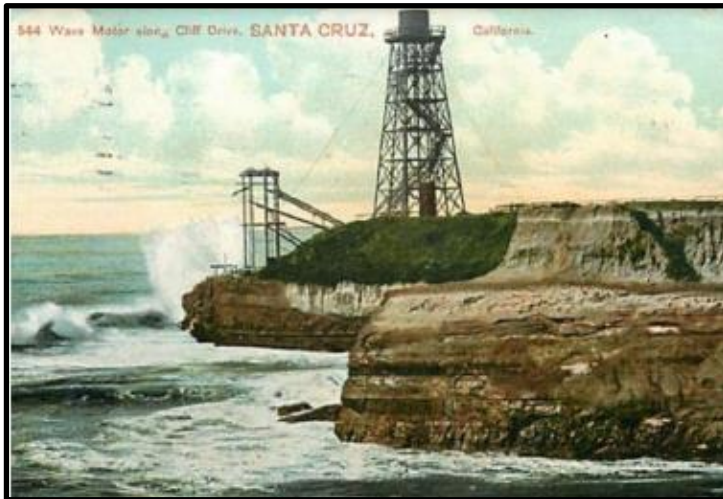


... in this case, at least, the **wave direction is more stable** and known in advance;

Also, the **directional energy spreading is reduced** as the waters get shallower.

# WECs: some history

- The idea goes way back in time:
  - **In 1799 – Girard pere et fils**, in France, proposed the use of a raft to convert wave energy into mechanical energy (first patent) !!
  - Other experiments took place during the 1800s:



The Santa Cruz wave-motor experiment

Source: Pecher, A. & Kofoed, J.P. (editors),  
*Handbook of Ocean Wave Energy* [4]

- **Modern advances** came through mainly **after the oil crisis in the 1970s**;
- **By the early 1980s** there were already **more than 1000 patents [7]!**



# WECs: some history

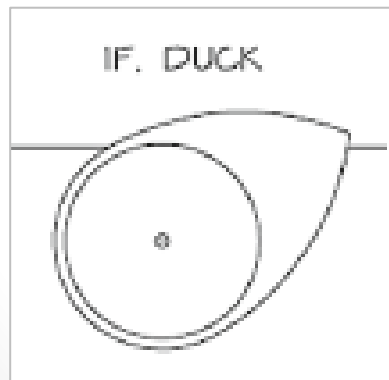
- During the 1970s and 1980s, some of the main developments happened in Europe (Scotland, Norway) and Japan.
- Special note must be given to the work of Prof. Stephen Salter, and the development of the [Salter' Duck](#)...

A rotating floating device that would extract the *wave energy from the wave flow*

- ...and the history of this development is quite illustrative of the principles, challenges and drawbacks of many modern WEC devices.

# WECs: some history

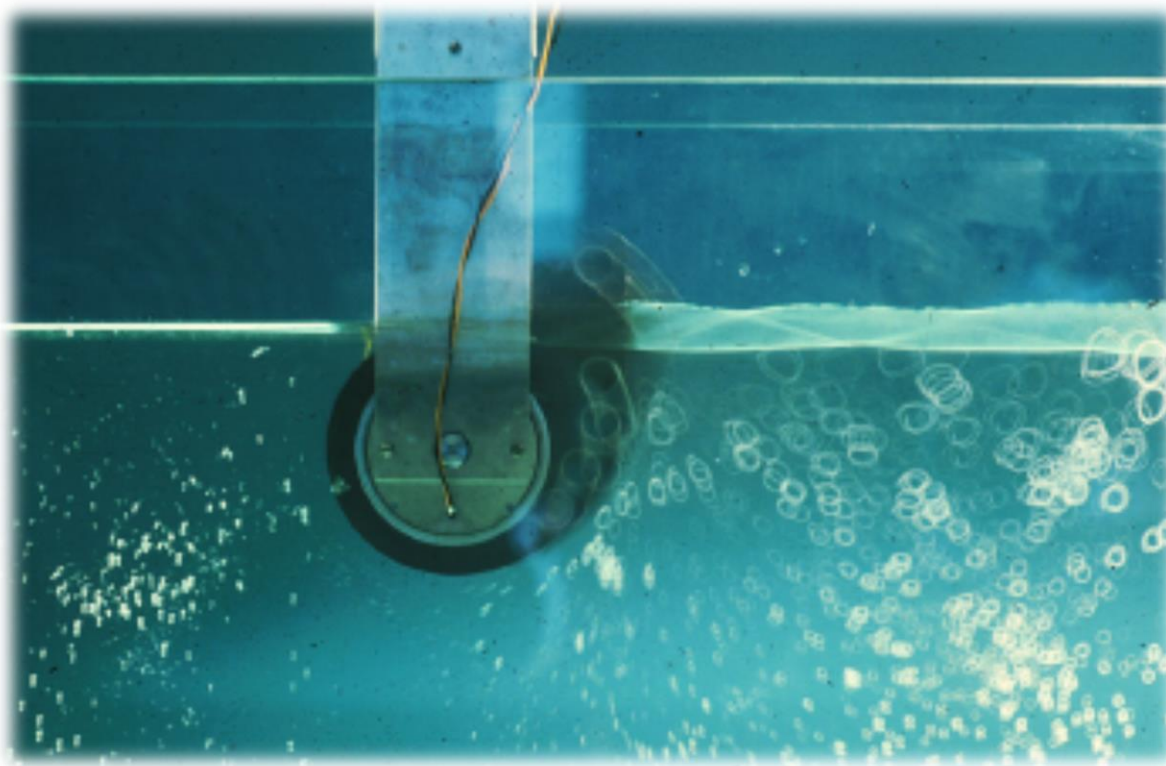
- There are many reasons why **rotating devices** would be **preferable** over translating ones (see, e.g., [8]):
  - Less energy dissipation
  - Don't require stops
  - Easier to seal
  - Less maintenance
- With the help of small-scale models in a wave flume (2D), they devised an optimum hydrodynamic shape (the duck):



90% efficiency in  
absorbing wave  
power!!

# WECs: some history

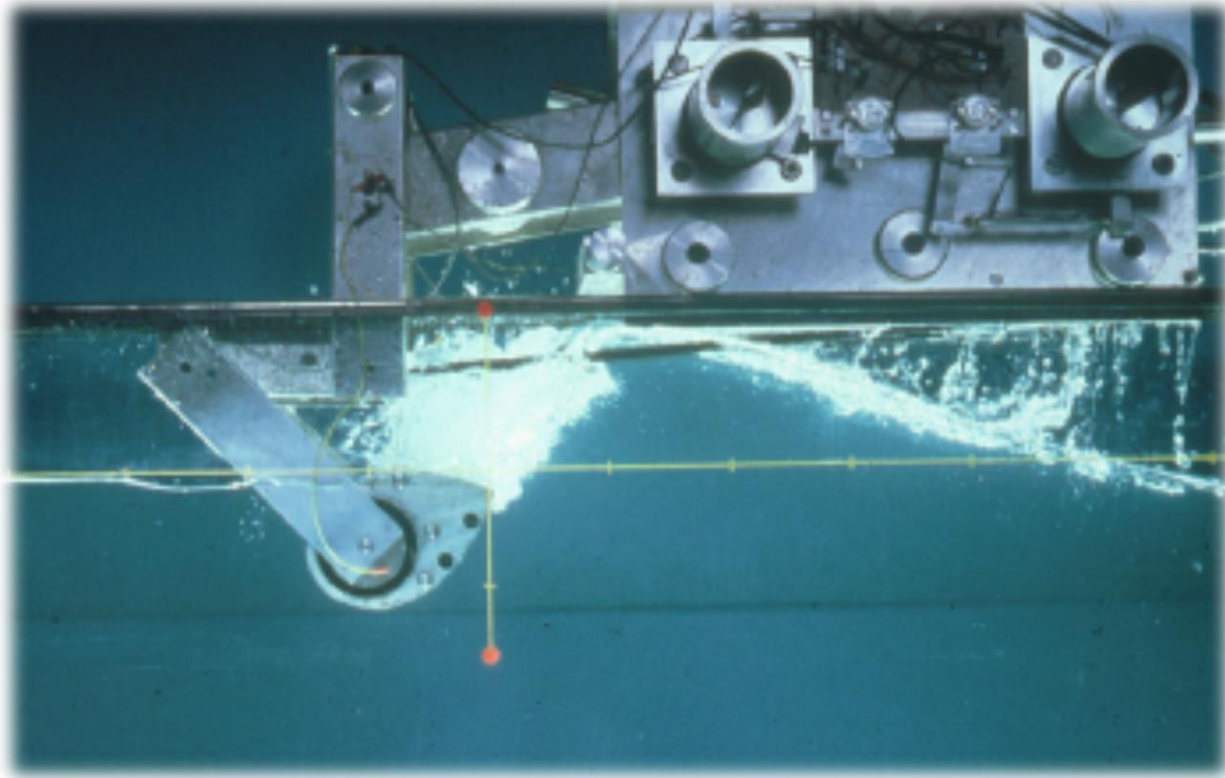
- The “trick” of the shape was to follow the exponential decay of wave action with depth...



Source: Salter, S. (2016) [8]

# WECs: some history

- The “trick” of the shape was to follow the exponential decay of wave action with depth...



Source: Salter, S. (2016) [8]

# WECs: some history

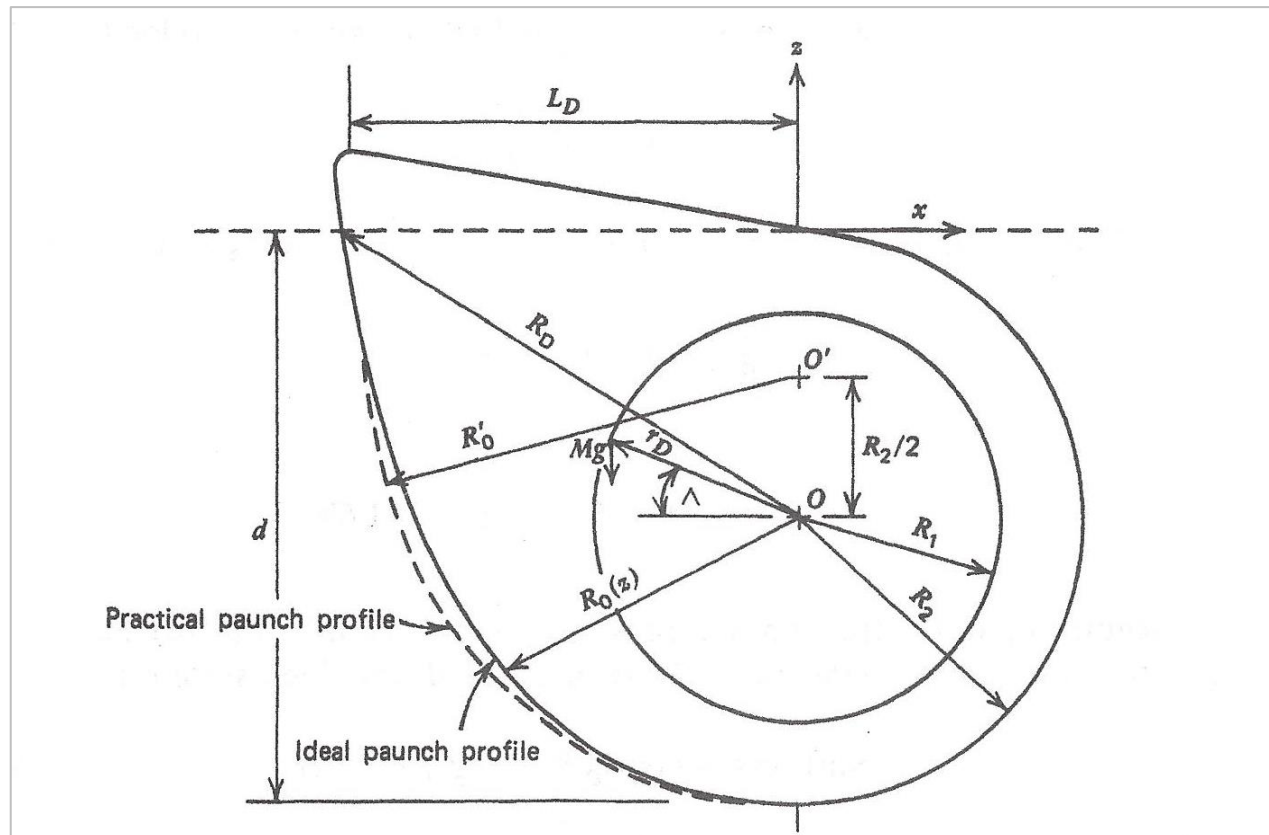
- In order to maximize motions, another common feature of the WECs is to *tune natural period of motion (in the duck's case, pitch) to the incoming wave period...*

$$T_{n,pitch} = 2\pi \sqrt{\frac{inertia}{stiffness}} = T_{wave}$$

WECs explore RESONANCE!

# WECs: some history

- The geometry of the duck was designed in order to maximize the absorption of the wave flow:



Source: McCormick, ME. Ocean Wave Energy Conversion [7]

# WECs: some history

- Floating devices (cylindrical spines) were devised for holding an array of ducks and augment the wave power extraction in sea



Source: Falnes, J. (2007) [9]

- The duck's relative motions would drive a hydraulic power take-off mechanism.

# WECs: some history

- However:

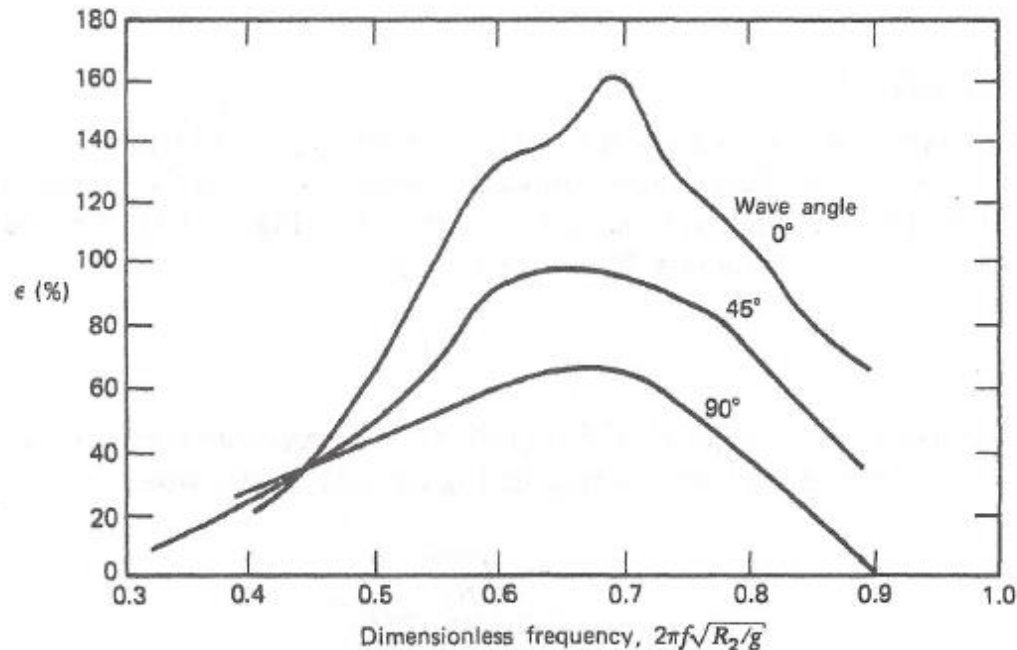
“The change from testing in regular waves to more realistic irregular ones with a Gaussian distribution of wave amplitudes is an unpleasant experience for wave inventors.” [8]

- Many drawbacks made the **efficiency of the real device drop** (see [7]), mainly:
  - Wave frequency spread
  - Variability in wave direction
  - The dynamic effects induced by **mooring** devices...
- which ultimately threatened *economical* viability of the devices.



# WECs: some history

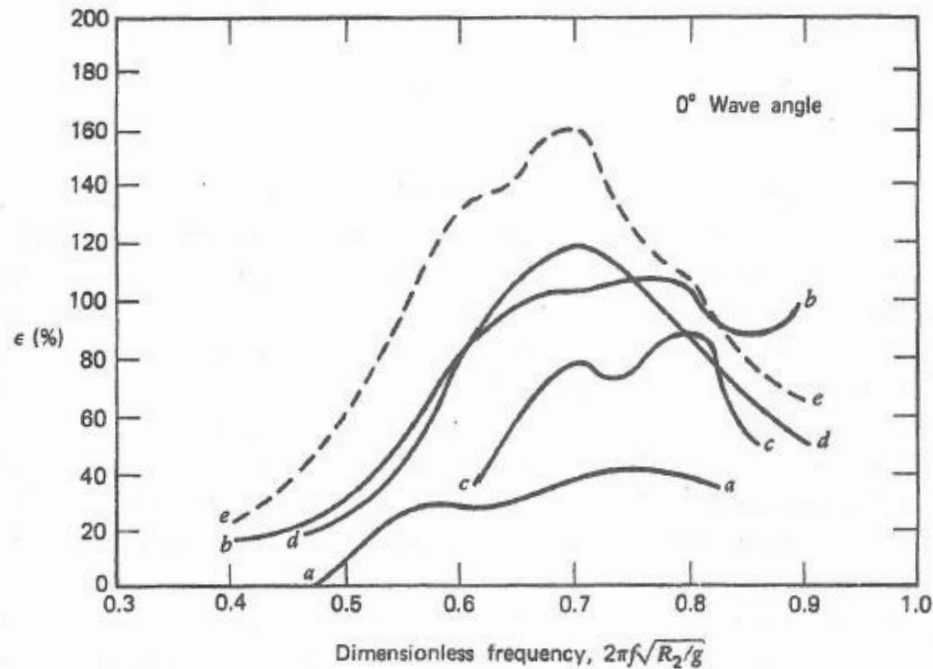
- Effect of wave frequency and direction on the energy absorption efficiency:



Note: Efficiencies larger than 100% measured in the tests result from interaction between incident and radiated waves

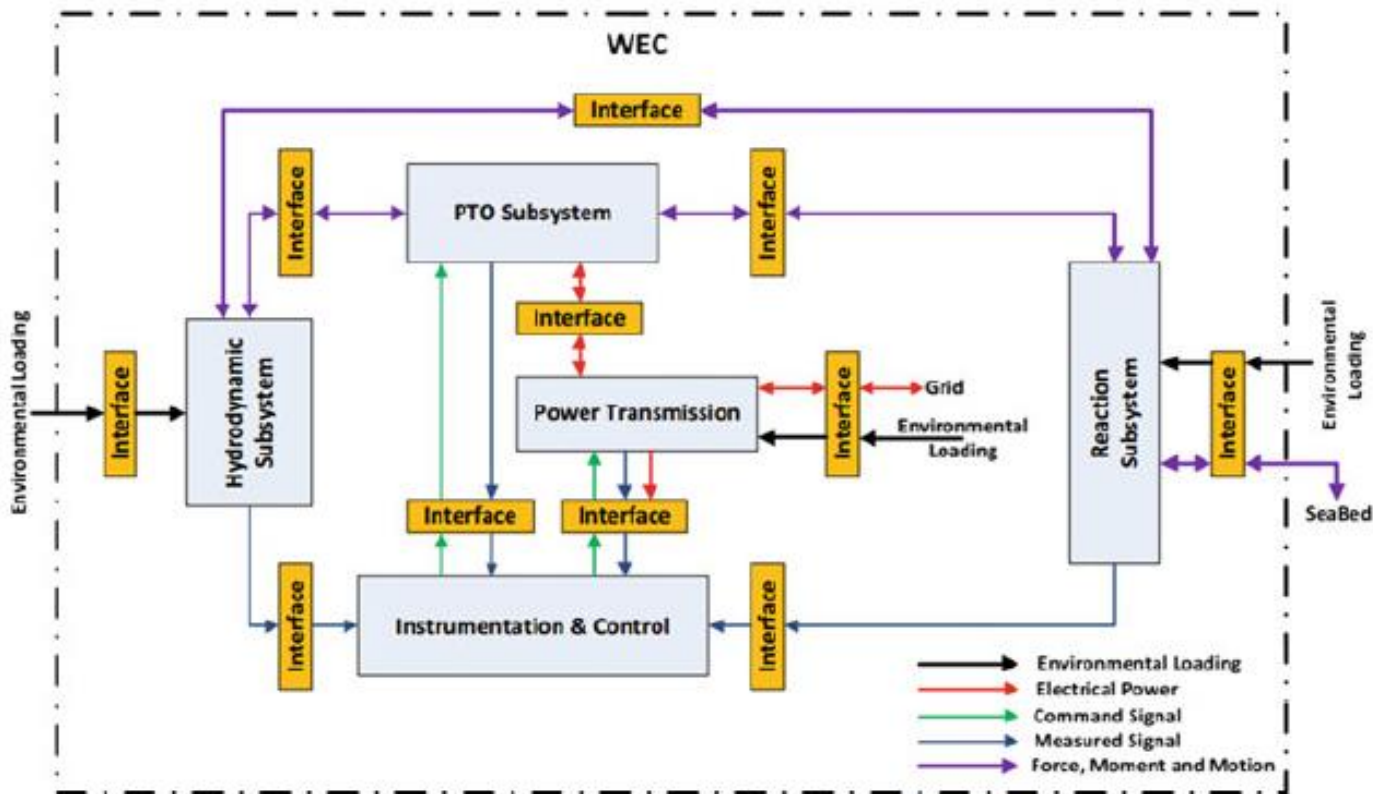
# WECs: some history

- Effect of mooring dynamics on the energy absorption efficiency:



a – slack moorings  
b – chain taut moorings  
c – single taut moorings  
d – four chain taut  
e – rigid frame

# WECs: basic features and main types



WEC system design breakdown

# WECs: basic features and main types

- Some rule-of-thumb figures for comparing the main categories of WECs can be given.
- Regarding the wave power absorption efficiency, an **indicative capture ratio** is provided below (according to [4]):

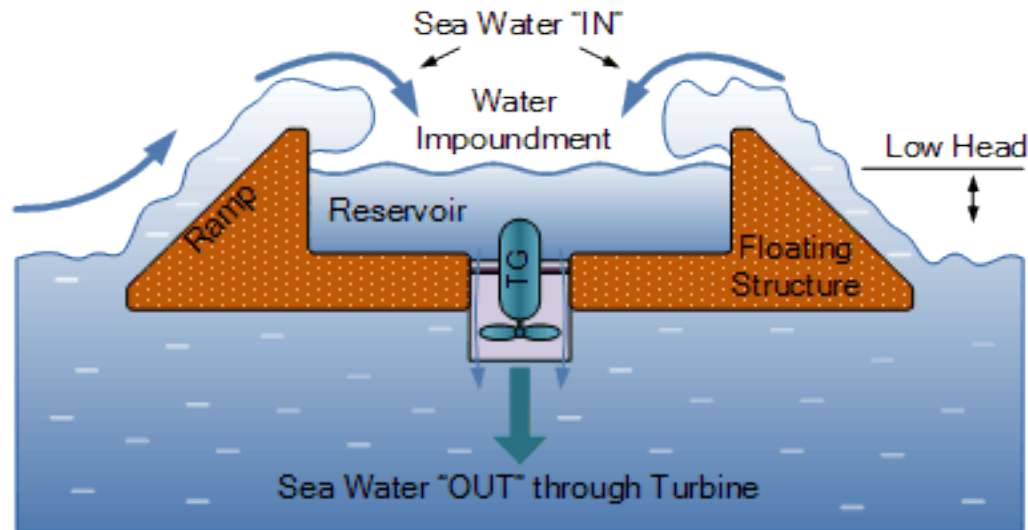
WEC type	Capture width ratio (%)
Floating overtopping device	17
Oscillating water column	29
Point absorber	16
Pitching flap (bottom fixed)	37

# WECs: basic features and main types

- There are numerous concepts of WECs (*remember there are thousands of patents by now!!*).
- The pitching flaps resemble the nodding duck, so next we will review the main features and examples of:
  - **Overtopping devices**
  - **Point absorbers**
  - **Oscillating Water Columns (OWCs)**
- For a more extensive review, students may refer to the suggested references, mainly [4], [7] and [9]

# WECs: basic features and main types

- **OVERTOPPING DEVICES**
- **Principle:** wave runs-up a structure, embarks and then flows out running a hydro-power turbine.
- For this sort of WEC, much more complicated hydrodynamics must be used to predict the run-up and amount of water taken in.



Source: [blackfishengineering.com](http://blackfishengineering.com)

# WECs: basic features and main types

- **OVERTOPPING DEVICES**
- **Example:** The *Wave Dragon* – 1:4.5 scaled grid-connected prototype tested in Denmark

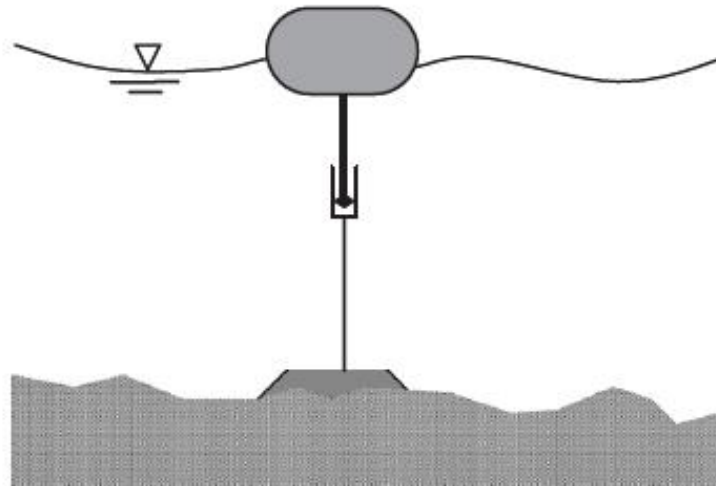


Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy* [4]

# WECs: basic features and main types

- **POINT ABSORBERS**

- **Principle:** A floating device explores the potential wave energy to excite motions (preferably resonant) and run a PTO system (e.g., a hydraulic pump)

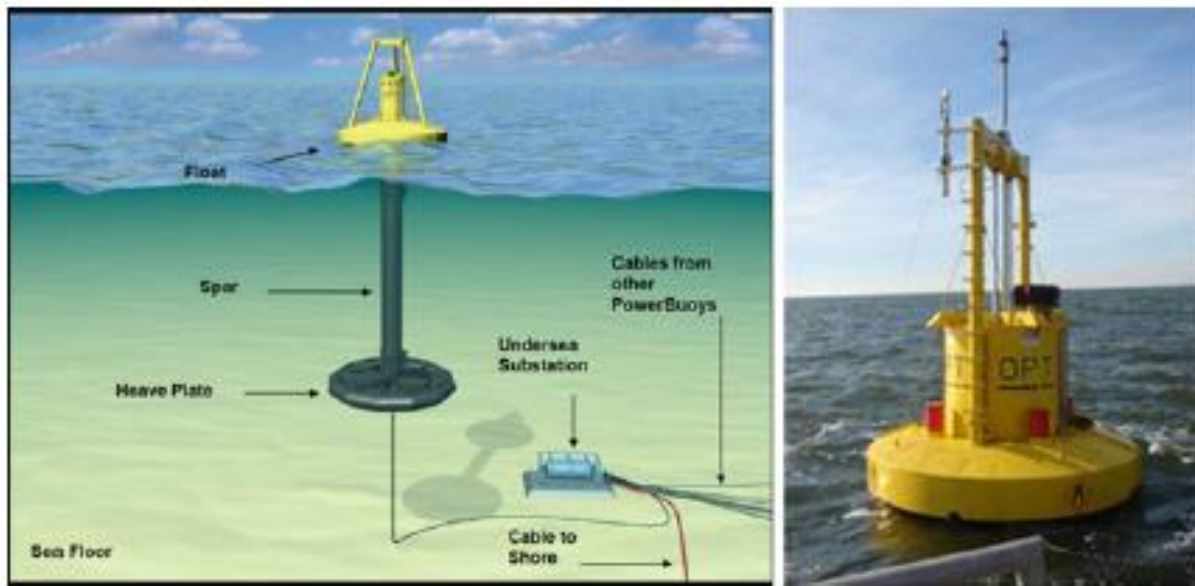


Source: Falnes, J. (2007) [9]



# WECs: basic features and main types

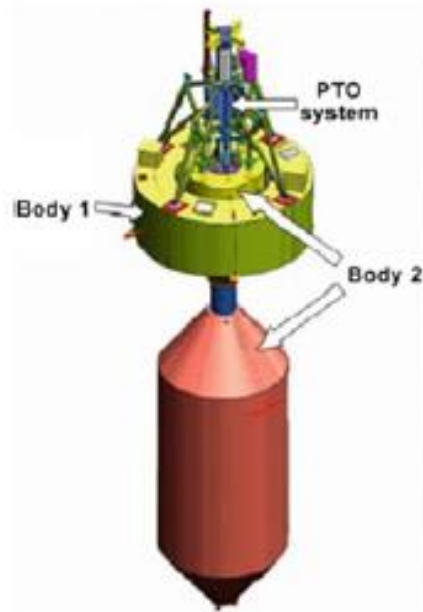
- **POINT ABSORBERS**
- **Example:** OPT's Powerbuoy PT40 (40kW)



Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy* [4]

# WECs: basic features and main types

- **POINT ABSORBERS**
- **Example:** The *Wavebob*



Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy* [4]

# WECs: basic features and main types

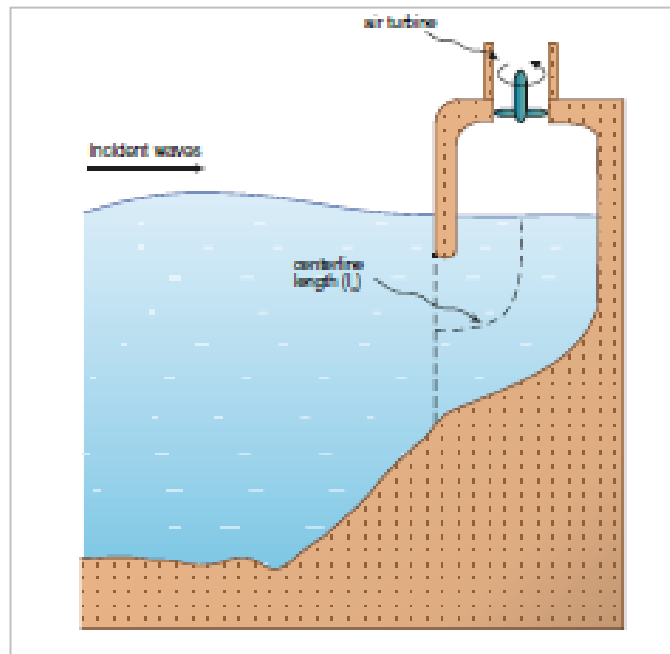
- **POINT ABSORBERS**
- **Example:** Wave energy converter prototype installed at Pecém port, northern Brazil



# WECs: basic features and main types

- **OSCILLATING WATER COLUMN (OWC)**
- **Principle:** wave resonance in a cavity/moonpool moves an air column; a double-action turbine (e.g. Wells type) converts kinetic energy of the high velocity air flow into electrical energy.

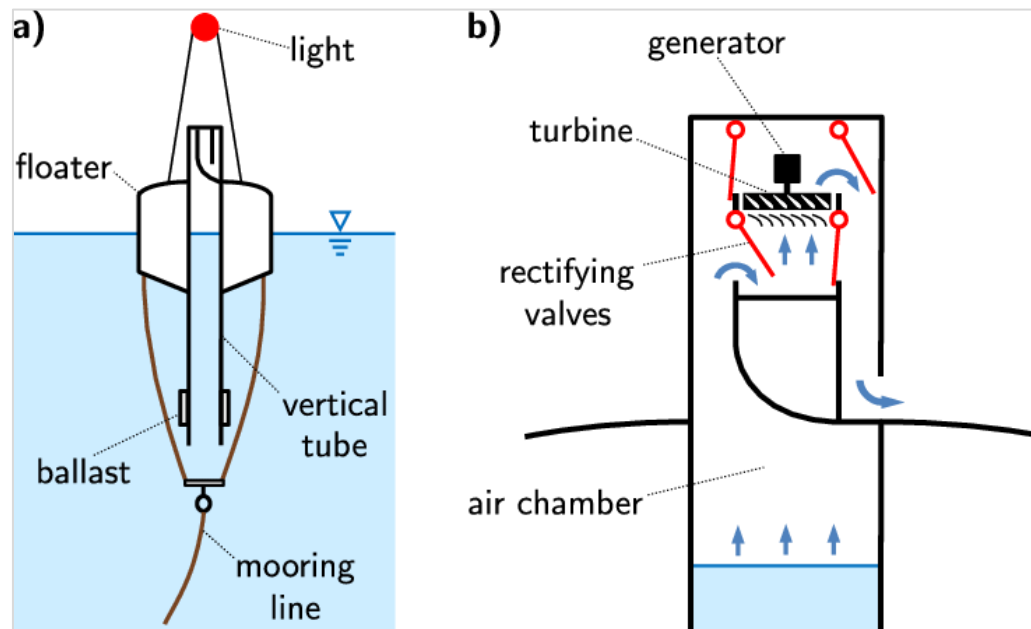
Resonance of the water column motion is also explored for increasing power



Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy* [4]

# WECs: basic features and main types

- **OSCILLATING WATER COLUMN (OWC)**
- **History:** Thanks to the work of Yoshido Masuda in the 1960's, a small-scale power OWC was used in many commercial buoys (first example of commercial application)



Source: *Henriques J.C.C. et al. [10]*

# WECs: basic features and main types

- **OSCILLATING WATER COLUMN (OWC)**
- **History:** He was also involved in JAMSTEC's *Kaimei* experiments (1st round 1978-1979, 2<sup>nd</sup> round 1985-1986), in which many OWC chambers were mounted on an 80m long ship-shaped barge, moored northwest of the town of Yura (40m depth).



Source: Falcão, A.F.O and Henriques J.C.C. (2016). [11]



# WECs: basic features and main types

- **OSCILLATING WATER COLUMN (OWC)**
- **Recent Example:** OceanLynx, Australia



Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy* [4]

# WECs: basic features and main types

- **OSCILLATING WATER COLUMN (OWC)**
- **Recent Example:** Oceantec's MARMOK-A-5, SPAIN (5m diameter, 42 meter draft floating OWC being tested at BIMEP testing site in Biscay bay)

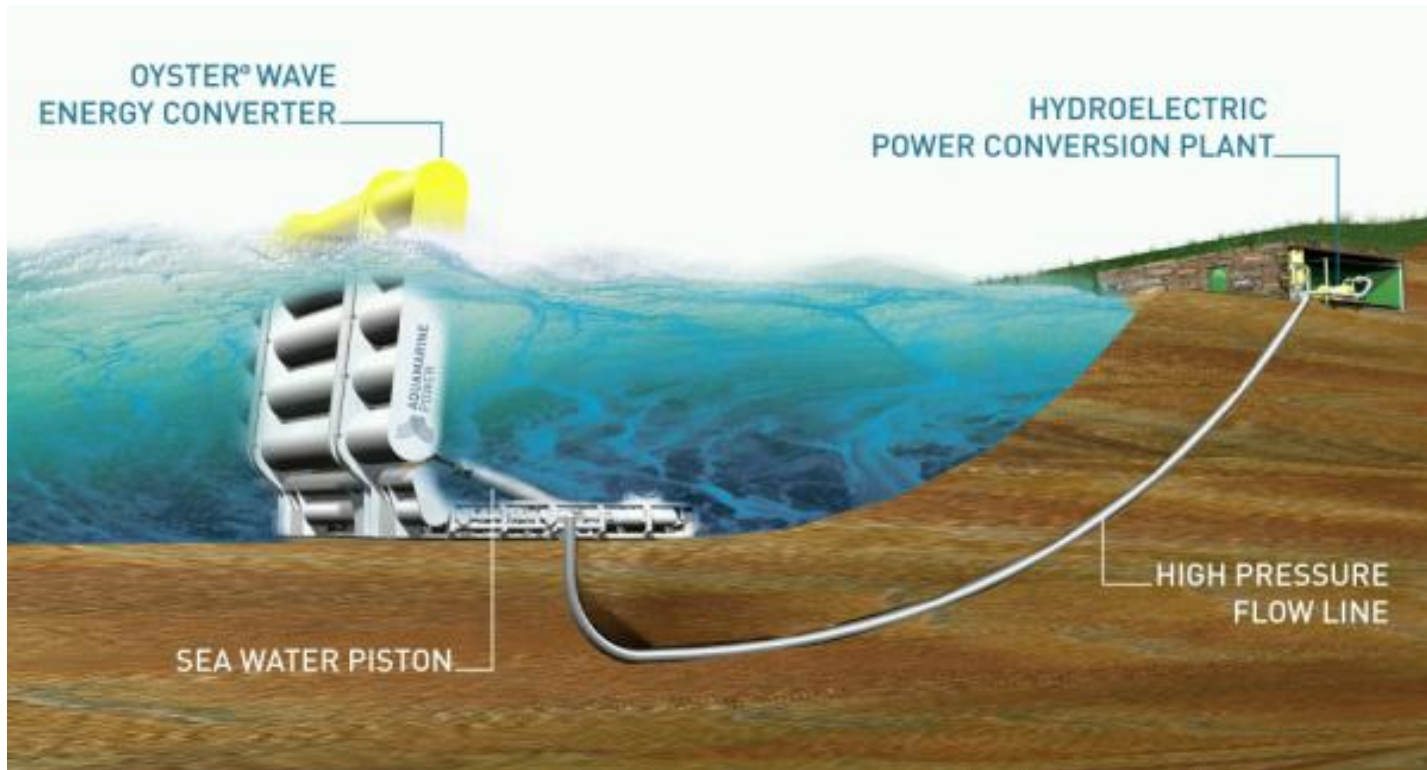


Source: *tecnalia.com*



# WECs: basic features and main types

- **PITCHING FLAPS**
- There are many recent examples on this kind of device



Ex: Oyster<sup>®</sup>

# WECs: basic features and main types

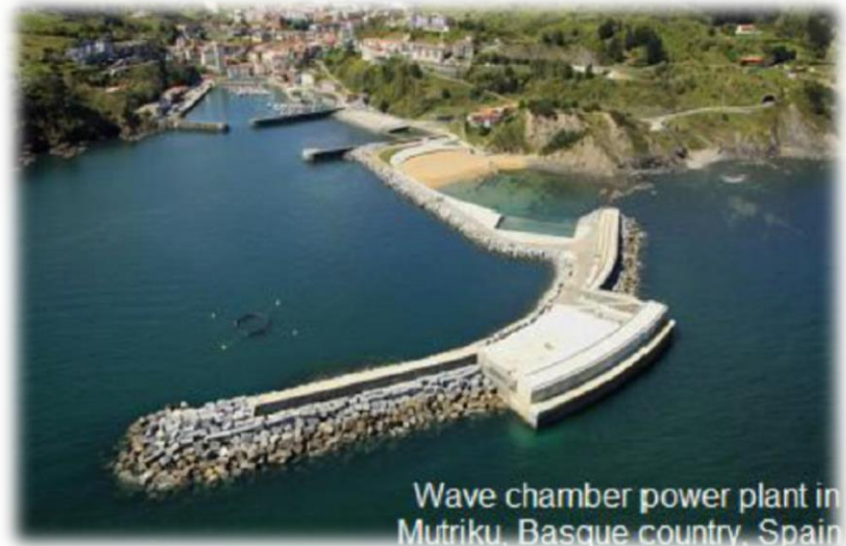
- **OTHER TYPES OF WECs**
- Include a large range of devices, such as:



Ex: Pelamis<sup>®</sup>

# Recent trends and perspectives

- According to a recent analysis by Stephen Salter [8]: “*The challenge eventually must be to reduce costs of wave energy by a factor of about two.*”
- Fixed coastal structures have a better cost prospective, but are more prone to face problems with environmental aspects. A promising policy seems to be **joining this devices to existing breakwaters**, as for example:



Source: Pecher, A. & Kofoed, J.P.  
(editors), *Handbook of Ocean Wave  
Energy* [4]

# Recent trends and perspectives

- New PTO technologies are in continuous development, with the main goal of reducing wave energy costs. More advanced examples include the application of piezoelectric materials, among other techniques.
- Floating devices still struggle with costs, which in this case also include **offshore maintenance, moorings and power cable to the shore**. Apparently, there is a trend in favor of floating OWCs.



# Recent trends and perspectives

- A promising strategy for floating devices seems to be their application in **hybrid offshore power plants** (floating wind turbines + WECs), which attenuates the relative costs for the WEC.

Floating Power Plant:  
multiple Point  
Absorbers in Vindeby's  
offshore wind farm  
(Denmark)



Source: Pecher, A. & Kofoed, J.P. (editors), *Handbook of Ocean Wave Energy* [4]

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