

# 1. Simple Features for R

- What is a feature?
  - Dimensions
  - Simple feature geometry types
  - Coordinate reference system
- How simple features in R are organized
  - sf: objects with simple features
  - sfc: simple feature geometry list-column
  - Mixed geometry types
  - sfg: simple feature geometry
  - Well-known text, well-known binary, precision
    - WKT and WKB
    - Precision
  - Reading and writing
    - Driver-specific options
    - Create, read, update and delete
    - Benchmarks
    - Connection to spatial databases
  - Coordinate reference systems and transformations
  - Conversion, including to and from sp
  - Geometrical operations
  - Non-valid geometries
- Units
- How attributes relate to geometries

Simple features ([https://en.wikipedia.org/wiki/Simple\\_Features](https://en.wikipedia.org/wiki/Simple_Features)) or *simple feature access* (<http://www.opengeospatial.org/standards/sfa>) refers to a formal standard (ISO 19125-1:2004) that describes how objects in the real world can be represented in computers, with emphasis on the *spatial* geometry of these objects. It also describes how such objects can be stored in and retrieved from databases, and which geometrical operations should be defined for them.

The standard is widely implemented in spatial databases (such as PostGIS), commercial GIS (e.g., ESRI ArcGIS (<http://www.esri.com/>)) and forms the vector data basis for libraries such as GDAL (<http://www.gdal.org/>). A subset of simple features forms the GeoJSON (<http://geojson.org/>) standard.

R has well-supported classes for storing spatial data (sp (<https://CRAN.R-project.org/package=sp>)) and interfacing to the above mentioned environments (rgdal (<https://CRAN.R-project.org/package=rgdal>), rgeos (<https://CRAN.R-project.org/package=rgeos>)), but has so far lacked a complete implementation of simple features, making conversions at times convoluted, inefficient or incomplete. The package sf (<http://github.com/r-spatial/sf>) tries to fill this gap, and aims at succeeding sp (<https://CRAN.R-project.org/package=sp>) in the long term.

This vignette:

- explains what is meant by features, and by simple features
- shows how they are implemented in R
- provides examples of how you can work with them
- shows how they can be read from and written to external files or resources
- discusses how they can be converted to and from sp objects
- shows how they can be used for meaningful spatial analysis

# What is a feature?

A feature is thought of as a thing, or an object in the real world, such as a building or a tree. As is the case with objects, they often consist of other objects. This is the case with features too: a set of features can form a single feature. A forest stand can be a feature, a forest can be a feature, a city can be a feature. A satellite image pixel can be a feature, a complete image can be a feature too.

Features have a *geometry* describing *where* on Earth the feature is located, and they have attributes, which describe other properties. The geometry of a tree can be the delineation of its crown, of its stem, or the point indicating its centre. Other properties may include its height, color, diameter at breast height at a particular date, and so on.

The standard says: "A simple feature is defined by the OpenGIS Abstract specification to have both spatial and non-spatial attributes. Spatial attributes are geometry valued, and simple features are based on 2D geometry with linear interpolation between vertices." We will see soon that the same standard will extend its coverage beyond 2D and beyond linear interpolation. Here, we take simple features as the data structures and operations described in the standard (<http://www.opengeospatial.org/standards/sfa>).

## Dimensions

All geometries are composed of points. Points are coordinates in a 2-, 3- or 4-dimensional space. All points in a geometry have the same dimensionality. In addition to X and Y coordinates, there are two optional additional dimensions:

- a Z coordinate, denoting altitude
- an M coordinate (rarely used), denoting some *measure* that is associated with the point, rather than with the feature as a whole (in which case it would be a feature attribute); examples could be time of measurement, or measurement error of the coordinates

The four possible cases then are:

1. two-dimensional points refer to x and y, easting and northing, or longitude and latitude, we refer to them as XY
2. three-dimensional points as XYZ
3. three-dimensional points as XYM
4. four-dimensional points as XYZM (the third axis is Z, fourth M)

## Simple feature geometry types

The following seven simple feature types are the most common, and are for instance the only ones used for GeoJSON (<https://tools.ietf.org/html/rfc7946>):

type	description
POINT	zero-dimensional geometry containing a single point
LINestring	sequence of points connected by straight, non-self intersecting line pieces; one-dimensional geometry
POLYGON	geometry with a positive area (two-dimensional); sequence of points form a closed, non-self intersecting ring; the first ring denotes the exterior ring, zero or more subsequent rings denote holes in this exterior ring

<b>type</b>	<b>description</b>
MULTIPOINT	set of points; a MULTIPOINT is simple if no two Points in the MULTIPOINT are equal
MULTILINESTRING	set of linestrings
MULTIPOLYGON	set of polygons
GEOMETRYCOLLECTION	set of geometries of any type except GEOMETRYCOLLECTION

Each of the geometry types can also be a (typed) empty set, containing zero coordinates (for POINT the standard is not clear how to represent the empty geometry). Empty geometries can be thought of being the analogue to missing ( NA ) attributes, NULL values or empty lists.

The remaining geometries 10 are more rare, but increasingly find implementations:

<b>type</b>	<b>description</b>
CIRCULARSTRING	The CIRCULARSTRING is the basic curve type, similar to a LINESTRING in the linear world. A single segment requires three points, the start and end points (first and third) and any other point on the arc. The exception to this is for a closed circle, where the start and end points are the same. In this case the second point MUST be the center of the arc, ie the opposite side of the circle. To chain arcs together, the last point of the previous arc becomes the first point of the next arc, just like in LINESTRING. This means that a valid circular string must have an odd number of points greater than 1.
COMPOUNDCURVE	A compound curve is a single, continuous curve that has both curved (circular) segments and linear segments. That means that in addition to having well-formed components, the end point of every component (except the last) must be coincident with the start point of the following component.
CURVEPOLYGON	Example compound curve in a curve polygon: CURVEPOLYGON(COMPOUNDCURVE(CIRCULARSTRING(0 0,2 0, 2 1, 2 3, 4 3),(4 3, 4 5, 1 4, 0 0)), CIRCULARSTRING(1.7 1, 1.4 0.4, 1.6 0.4, 1.6 0.5, 1.7 1) )
MULTICURVE	A MultiCurve is a 1-dimensional GeometryCollection whose elements are Curves, it can include linear strings, circular strings or compound strings.
MULTISURFACE	A MultiSurface is a 2-dimensional GeometryCollection whose elements are Surfaces, all using coordinates from the same coordinate reference system.
CURVE	A Curve is a 1-dimensional geometric object usually stored as a sequence of Points, with the subtype of Curve specifying the form of the interpolation between Points
SURFACE	A Surface is a 2-dimensional geometric object

type	description
POLYHEDRALSURFACE	A PolyhedralSurface is a contiguous collection of polygons, which share common boundary segments
TIN	A TIN (triangulated irregular network) is a PolyhedralSurface consisting only of Triangle patches.
TRIANGLE	A Triangle is a polygon with 3 distinct, non-collinear vertices and no interior boundary

Note that `CIRCULASTRING`, `COMPOUNDCURVE` and `CURVEPOLYGON` are not described in the SFA standard, but in the SQL-MM part 3 standard (<https://www.iso.org/standard/38651.html>). The descriptions above were copied from the PostGIS manual ([http://postgis.net/docs/using\\_postgis\\_dbmanagement.html](http://postgis.net/docs/using_postgis_dbmanagement.html)).

## Coordinate reference system

Coordinates can only be placed on the Earth's surface when their coordinate reference system (CRS) is known; this may be an spheroid CRS such as WGS84, a projected, two-dimensional (Cartesian) CRS such as a UTM zone or Web Mercator, or a CRS in three-dimensions, or including time. Similarly, M-coordinates need an attribute reference system, e.g. a measurement unit (<https://CRAN.R-project.org/package=units>).

## How simple features in R are organized

Package `sf` represents simple features as native R objects. Similar to PostGIS (<http://postgis.net/>), all functions and methods in `sf` that operate on spatial data are prefixed by `st_`, which refers to *spatial and temporal*; this makes them easily findable by command-line completion. Simple features are implemented as R native data, using simple data structures (S3 classes, lists, matrix, vector). Typical use involves reading, manipulating and writing of sets of features, with attributes and geometries.

As attributes are typically stored in `data.frame` objects (or the very similar `tbl_df`), we will also store feature geometries in a `data.frame` column. Since geometries are not single-valued, they are put in a list-column, a list of length equal to the number of records in the `data.frame`, with each list element holding the simple feature geometry of that feature. The three classes used to represent simple features are:

- `sf`, the table (`data.frame`) with feature attributes and feature geometries, which contains
- `sfc`, the list-column with the geometries for each feature (record), which is composed of
- `sfg`, the feature geometry of an individual simple feature.

We will now discuss each of these three classes.

## sf: objects with simple features

As we usually do not work with geometries of single simple features, but with datasets consisting of sets of features with attributes, the two are put together in `sf` (simple feature) objects. The following command reads the `nc` dataset from a file that is contained in the `sf` package:

```
library(sf)
## Linking to GEOS 3.6.2, GDAL 2.2.3, proj.4 4.9.3
nc <- st_read(system.file("shape/nc.shp", package="sf"))
## Reading layer `nc' from data source `/tmp/Rtmpaq4C0b/Rinst79437936646a/sf/shape/nc.shp' using driver `ESRI Shapefile'
## Simple feature collection with 100 features and 14 fields
## geometry type:  MULTIPOLYGON
## dimension:      XY
## bbox:           xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965
## epsg (SRID):   4267
## proj4string:    +proj=LongLat +datum=NAD27 +no_defs
```

(Note that users will not use `system.file` but give a `filename` directly, and that shapefiles consist of more than one file, all with identical basename, which reside in the same directory.) The short report printed gives the file name, the driver (ESRI Shapefile), mentions that there are 100 features (records, represented as rows) and 14 fields (attributes, represented as columns). This object is of class

```
class(nc)
## [1] "sf"      "data.frame"
```

meaning it extends (and "is" a) `data.frame`, but with a single list-column with geometries, which is held in the column with name

```
attr(nc, "sf_column")
## [1] "geometry"
```

If we print the first three features, we see their attribute values and an abridged version of the geometry

```
print(nc[9:15], n = 3)
```

which would give the following output:

```
## Simple feature collection with 100 features and 6 fields
## geometry type:  MULTIPOLYGON
## dimension:      XY
## bbox:           xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965
## epsg (SRID):   4267
## proj4string:    +proj=longlat +datum=NAD27 +no_defs
## precision:     double (default; no precision model)
## First 3 features:
```

	BIR74	SID74	NWBIR74	BIR79	SID79	NWBIR79	geom
## 1	1091	1	10	1364	0	19	MULTIPOLYGON((( -81.47275543...
## 2	487	0	10	542	3	12	MULTIPOLYGON((( -81.23989105...
## 3	3188	5	208	3616	6	260	MULTIPOLYGON((( -80.45634460...

Simple feature

Simple feature geometry list-column (sfc)

Simple feature geometry (sfg)

In the output we see:

- in green a simple feature: a single record, or `data.frame` row, consisting of attributes and geometry
- in blue a single simple feature geometry (an object of class `sfg`)
- in red a simple feature list-column (an object of class `sfc`, which is a column in the `data.frame`)
- that although geometries are native R objects, they are printed as well-known text

Methods for `sf` objects are

```

methods(class = "sf")
## [1] $<- [ [[<-
## [4] aggregate as.data.frame cbind
## [7] coerce dbDataType dbWriteTable
## [10] identify initialize merge
## [13] plot print rbind
## [16] show slotsFromS3 st_agr
## [19] st_agr<- st_as_sf st_bbox
## [22] st_boundary st_buffer st_cast
## [25] st_centroid st_collection_extract st_convex_hull
## [28] st_coordinates st_crs st_crs<-
## [31] st_difference st_geometry st_geometry<-
## [34] st_intersection st_is st_line_merge
## [37] st_node st_point_on_surface st_polygonize
## [40] st_precision st_segmentize st_set_precision
## [43] st_simplify st_snap st_sym_difference
## [46] st_transform st_triangulate st_union
## [49] st_voronoi st_wrap_dateline st_write
## [52] st_zm
## see '?methods' for accessing help and source code

```

It is also possible to create `data.frame` objects with geometry list-columns that are not of class `sf`, e.g. by

```

nc.no_sf <- as.data.frame(nc)
class(nc.no_sf)
## [1] "data.frame"

```

However, such objects:

- no longer register which column is the geometry list-column
- no longer have a plot method, and
- lack all of the other dedicated methods listed above for class `sf`

## sfc: simple feature geometry list-column

The column in the `sf data.frame` that contains the geometries is a list, of class `sfc`. We can retrieve the geometry list-column in this case by `nc$geom` or `nc[[15]]`, but the more general way uses `st_geometry`:

```

(nc_geom <- st_geometry(nc))
## Geometry set for 100 features
## geometry type: MULTIPOLYGON
## dimension: XY
## bbox: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965
## epsg (SRID): 4267
## proj4string: +proj=LongLat +datum=NAD27 +no_defs
## First 5 geometries:
## MULTIPOLYGON (((-81.47276 36.23436, -81.54084 3...
## MULTIPOLYGON (((-81.23989 36.36536, -81.24069 3...
## MULTIPOLYGON (((-80.45634 36.24256, -80.47639 3...
## MULTIPOLYGON (((-76.00897 36.3196, -76.01735 36...
## MULTIPOLYGON (((-77.21767 36.24098, -77.23461 3...

```

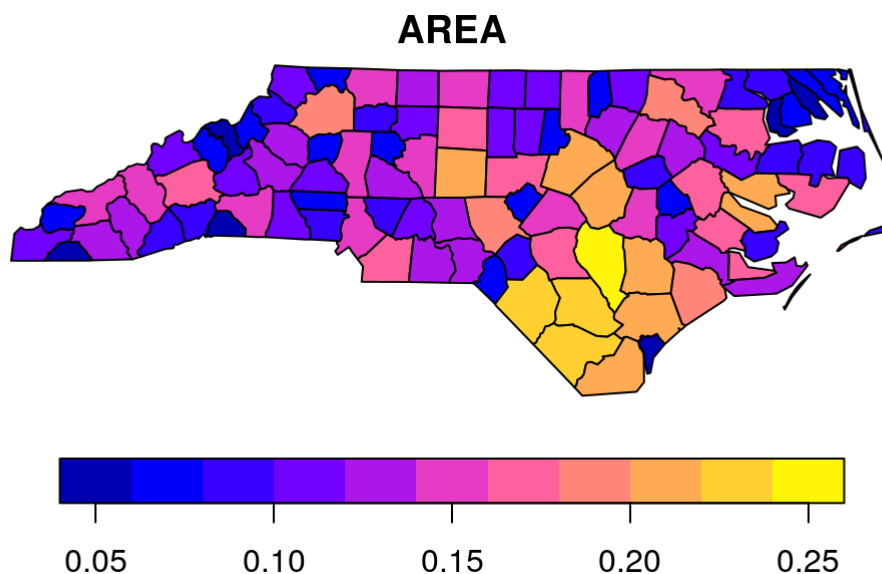
Geometries are printed in abbreviated form, but we can view a complete geometry by selecting it, e.g. the first one by

```
nc_geom[[1]]
## MULTIPOLYGON (((-81.47276 36.23436, -81.54084 36.27251, -81.56198 36.27359, -81.63306 36.3
4069, -81.74107 36.39178, -81.69828 36.47178, -81.7028 36.51934, -81.67 36.58965, -81.3453 3
6.57286, -81.34754 36.53791, -81.32478 36.51368, -81.31332 36.4807, -81.26624 36.43721, -81.2
6284 36.40504, -81.24069 36.37942, -81.23989 36.36536, -81.26424 36.35241, -81.32899 36.3635,
-81.36137 36.35316, -81.36569 36.33905, -81.35413 36.29972, -81.36745 36.2787, -81.40639 36.
28505, -81.41233 36.26729, -81.43104 36.26072, -81.45289 36.23959, -81.47276 36.23436)))
```

The way this is printed is called *well-known text*, and is part of the standards. The word `MULTIPOLYGON` is followed by three parenthesis, because it can consist of multiple polygons, in the form of `MULTIPOLYGON(POL1,POL2)`, where `POL1` might consist of an exterior ring and zero or more interior rings, as of `(EXT1,HOLE1,HOLE2)`. Sets of coordinates are held together with parenthesis, so we get `((crds_ext)(crds_hole1)(crds_hole2))` where `crds_` is a comma-separated set of coordinates of a ring. This leads to the case above, where `MULTIPOLYGON(((crds_ext)))` refers to the exterior ring (1), without holes (2), of the first polygon (3) - hence three parentheses.

We can see there is a single polygon with no rings:

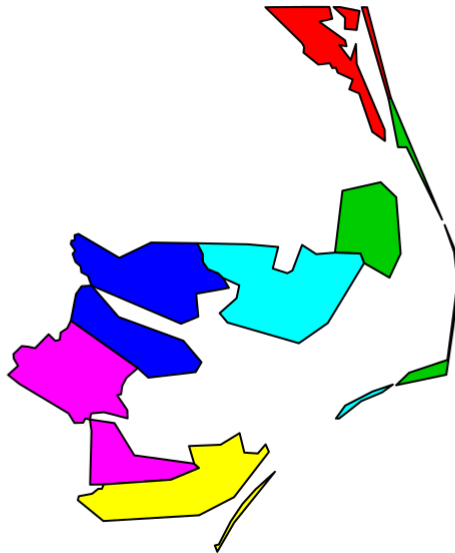
```
par(mar = c(0,0,1,0))
plot(nc[1])
plot(nc[1,1], col = 'grey', add = TRUE)
```



but some of the polygons in this dataset have multiple exterior rings; they can be identified by

```
par(mar = c(0,0,1,0))
(w <- which(sapply(nc_geom, length) > 1))
## [1] 4 56 57 87 91 95
plot(nc[w,1], col = 2:7)
```

## AREA



Following the MULTIPOLYGON datastructure, in R we have a list of lists of lists of matrices. For instance, we get the first 3 coordinate pairs of the second exterior ring (first ring is always exterior) for the geometry of feature 4 by

```
nc_geom[[4]][[2]][[1]][1:3,]
##           [,1]      [,2]
## [1,] -76.02717 36.55672
## [2,] -75.99866 36.55665
## [3,] -75.91192 36.54253
```

Geometry columns have their own class,

```
class(nc_geom)
## [1] "sfc_MULTIPOLYGON" "sfc"
```

Methods for geometry list-columns include

```
methods(class = 'sfc')
## [1] Ops           [           [<-
## [4] as.data.frame c           coerce
## [7] format        identify   initialize
## [10] print         rep        show
## [13] slotsFromS3   st_as_binary st_as_text
## [16] st_bbox       st_boundary st_buffer
## [19] st_cast      st_centroid st_collection_extract
## [22] st_convex_hull st_coordinates st_crs
## [25] st_crs<-     st_difference st_geometry
## [28] st_intersection st_is       st_line_merge
## [31] st_node      st_point_on_surface st_polygonize
## [34] st_precision st_segmentize st_set_precision
## [37] st_simplify  st_snap     st_sym_difference
## [40] st_transform st_triangulate st_union
## [43] st_voronoi   st_wrap_dateline st_write
## [46] st_zm        str         summary
## see '?methods' for accessing help and source code
```



Coordinate reference systems ( `st_crs` and `st_transform` ) are discussed in the section on coordinate reference systems. `st_as_wkb` and `st_as_text` convert geometry list-columns into well-known-binary or well-known-text, explained below. `st_bbox` retrieves the coordinate bounding box.

Attributes include

```
attributes(nc_geom)
## $n_empty
## [1] 0
##
## $crs
## Coordinate Reference System:
##   EPSG: 4267
##   proj4string: "+proj=LongLat +datum=NAD27 +no_defs"
##
## $class
## [1] "sfc_MULTIPOLYGON" "sfc"
##
## $precision
## [1] 0
##
## $bbox
##      xmin      ymin      xmax      ymax
## -84.32385  33.88199 -75.45698  36.58965
```

## Mixed geometry types

The class of `nc_geom` is `c("sfc_MULTIPOLYGON", "sfc")`: `sfc` is shared with all geometry types, and `sfc_TYPE` with `TYPE` indicating the type of the particular geometry at hand.

There are two “special” types: `GEOMETRYCOLLECTION`, and `GEOMETRY`. `GEOMETRYCOLLECTION` indicates that each of the geometries may contain a mix of geometry types, as in

```
(mix <- st_sfc(st_geometrycollection(list(st_point(1:2))),
  st_geometrycollection(list(st_linestring(matrix(1:4,2))))))
## Geometry set for 2 features
## geometry type:  GEOMETRYCOLLECTION
## dimension:      XY
## bbox:           xmin: 1 ymin: 2 xmax: 2 ymax: 4
## epsg (SRID):   NA
## proj4string:    NA
## GEOMETRYCOLLECTION (POINT (1 2))
## GEOMETRYCOLLECTION (LINESTRING (1 3, 2 4))
class(mix)
## [1] "sfc_GEOMETRYCOLLECTION" "sfc"
```

Still, the geometries are here of a single type.

The second `GEOMETRY`, indicates that the geometries in the geometry list-column are of varying type:

```
(mix <- st_sfc(st_point(1:2), st_linestring(matrix(1:4,2))))
## Geometry set for 2 features
## geometry type:  GEOMETRY
## dimension:      XY
## bbox:          xmin: 1 ymin: 2 xmax: 2 ymax: 4
## epsg (SRID):   NA
## proj4string:    NA
## POINT (1 2)
## LINESTRING (1 3, 2 4)
class(mix)
## [1] "sfc_GEOMETRY" "sfc"
```

These two are fundamentally different: `GEOMETRY` is a superclass without instances, `GEOMETRYCOLLECTION` is a geometry instance. `GEOMETRY` list-columns occur when we read in a data source with a mix of geometry types. `GEOMETRYCOLLECTION` is a single feature's geometry: the intersection of two feature polygons may consist of points, lines and polygons, see the example below.

## sfg: simple feature geometry

Simple feature geometry ( `sfg` ) objects carry the geometry for a single feature, e.g. a point, linestring or polygon.

Simple feature geometries are implemented as R native data, using the following rules

1. a single `POINT` is a numeric vector
2. a set of points, e.g. in a `LINestring` or ring of a `POLYGON` is a `matrix`, each row containing a point
3. any other set is a `list`

Creator functions are rarely used in practice, since we typically bulk read and write spatial data. They are useful for illustration:

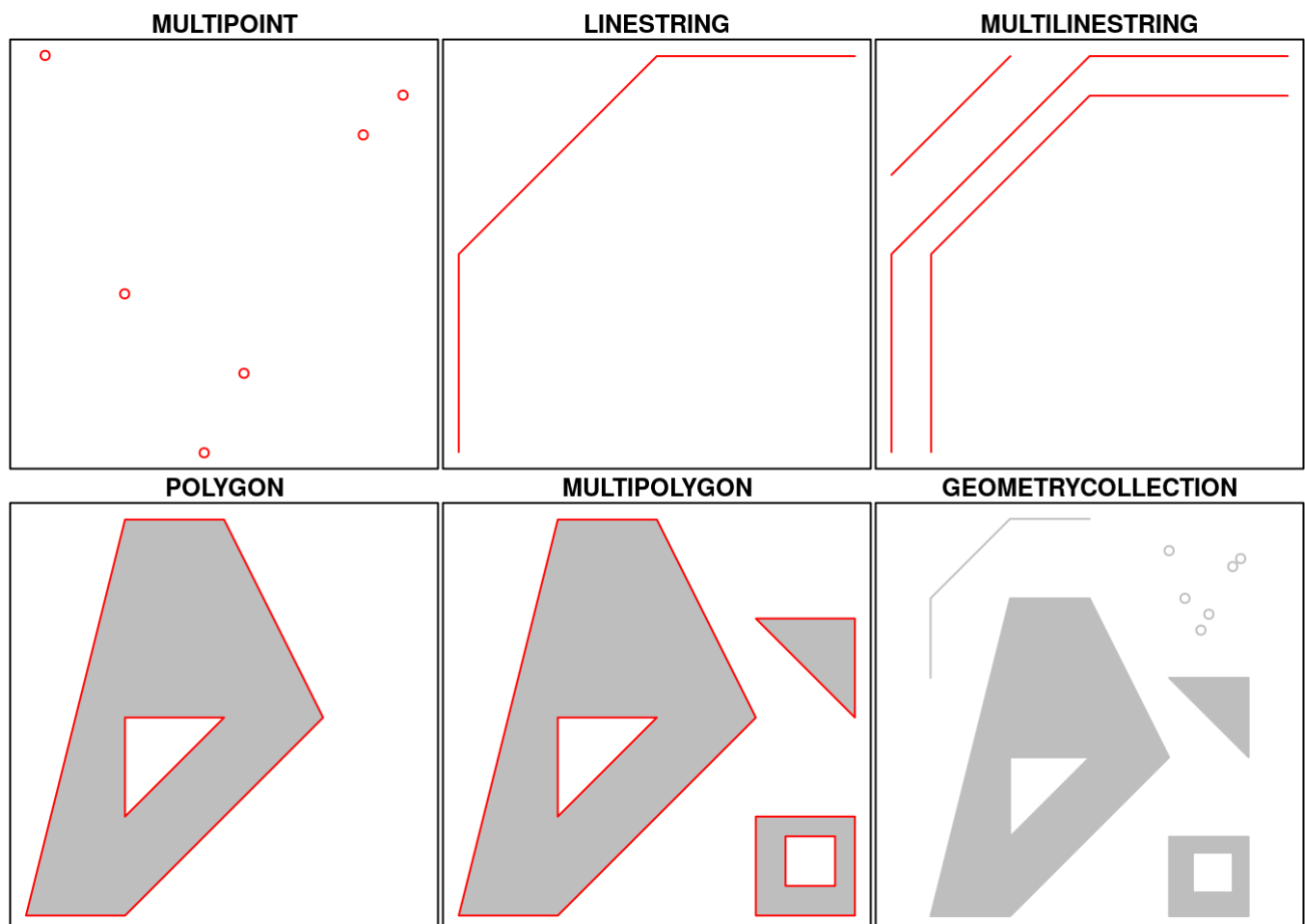
```
(x <- st_point(c(1,2)))
## POINT (1 2)
str(x)
## Classes 'XY', 'POINT', 'sfg' num [1:2] 1 2
(x <- st_point(c(1,2,3)))
## POINT Z (1 2 3)
str(x)
## Classes 'XYZ', 'POINT', 'sfg' num [1:3] 1 2 3
(x <- st_point(c(1,2,3), "XYM"))
## POINT M (1 2 3)
str(x)
## Classes 'XYM', 'POINT', 'sfg' num [1:3] 1 2 3
(x <- st_point(c(1,2,3,4)))
## POINT ZM (1 2 3 4)
str(x)
## Classes 'XYZM', 'POINT', 'sfg' num [1:4] 1 2 3 4
st_zm(x, drop = TRUE, what = "ZM")
## POINT (1 2)
```

This means that we can represent 2-, 3- or 4-dimensional coordinates. All geometry objects inherit from `sfg` (simple feature geometry), but also have a type (e.g. `POINT`), and a dimension (e.g. `XYM`) class name. A figure illustrates six of the seven most common types.

With the exception of the `POINT` which has a single point as geometry, the remaining six common single simple feature geometry types that correspond to single features (single records, or rows in a `data.frame`) are created like this

```
p <- rbind(c(3.2,4), c(3,4.6), c(3.8,4.4), c(3.5,3.8), c(3.4,3.6), c(3.9,4.5))
(mp <- st_multipoint(p))
## MULTIPOINT (3.2 4, 3 4.6, 3.8 4.4, 3.5 3.8, 3.4 3.6, 3.9 4.5)
s1 <- rbind(c(0,3),c(0,4),c(1,5),c(2,5))
(ls <- st_linestring(s1))
## LINESTRING (0 3, 0 4, 1 5, 2 5)
s2 <- rbind(c(0.2,3), c(0.2,4), c(1,4.8), c(2,4.8))
s3 <- rbind(c(0,4.4), c(0.6,5))
(mls <- st_multilinestring(list(s1,s2,s3)))
## MULTILINESTRING ((0 3, 0 4, 1 5, 2 5), (0.2 3, 0.2 4, 1 4.8, 2 4.8), (0 4.4, 0.6 5))
p1 <- rbind(c(0,0), c(1,0), c(3,2), c(2,4), c(1,4), c(0,0))
p2 <- rbind(c(1,1), c(1,2), c(2,2), c(1,1))
(pol <- st_polygon(list(p1,p2)))
p3 <- rbind(c(3,0), c(4,0), c(4,1), c(3,1), c(3,0))
p4 <- rbind(c(3.3,0.3), c(3.8,0.3), c(3.8,0.8), c(3.3,0.8), c(3.3,0.3))[5:1,]
p5 <- rbind(c(3,3), c(4,2), c(4,3), c(3,3))
(mpol <- st_multipolygon(list(list(p1,p2), list(p3,p4), list(p5))))
## MULTIPOLYGON (((0 0, 1 0, 3 2, 2 4, 1 4, 0 0), (1 1, 1 2, 2 2, 1 1)), ((3 0, 4 0, 4 1, 3
1, 3 0), (3.3 0.3, 3.3 0.8, 3.8 0.8, 3.8 0.3, 3.3 0.3)), ((3 3, 4 2, 4 3, 3 3)))
(gc <- st_geometrycollection(list(mp, mpol, ls)))
## GEOMETRYCOLLECTION (MULTIPOINT (3.2 4, 3 4.6, 3.8 4.4, 3.5 3.8, 3.4 3.6, 3.9 4.5), MULTIPOLY
LYGON (((0 0, 1 0, 3 2, 2 4, 1 4, 0 0), (1 1, 1 2, 2 2, 1 1)), ((3 0, 4 0, 4 1, 3 1, 3 0),
(3.3 0.3, 3.3 0.8, 3.8 0.8, 3.8 0.3, 3.3 0.3)), ((3 3, 4 2, 4 3, 3 3))), LINESTRING (0 3, 0
4, 1 5, 2 5))
```

The objects created are shown here:



Geometries can also be empty, as in

```
(x <- st_geometrycollection())
## GEOMETRYCOLLECTION EMPTY
length(x)
## [1] 0
```

## Well-known text, well-known binary, precision

### WKT and WKB

Well-known text (WKT) and well-known binary (WKB) are two encodings for simple feature geometries. Well-known text, e.g. seen in

```
x <- st_linestring(matrix(10:1,5))
st_as_text(x)
## [1] "LINESTRING (10 5, 9 4, 8 3, 7 2, 6 1)"
```

(but without the leading `## [1]` and quotes), is human-readable. Coordinates are usually floating point numbers, and moving large amounts of information as text is slow and imprecise. For that reason, we use well-known binary (WKB) encoding

```
st_as_binary(x)
## [1] 01 02 00 00 00 05 00 00 00 00 00 00 00 00 24 40 00 00 00 00 00 00
## [24] 14 40 00 00 00 00 00 00 22 40 00 00 00 00 00 10 40 00 00 00 00 00
## [47] 00 20 40 00 00 00 00 00 08 40 00 00 00 00 00 00 1c 40 00 00 00 00
## [70] 00 00 00 40 00 00 00 00 00 18 40 00 00 00 00 00 00 f0 3f
```

WKT and WKB can both be transformed back into R native objects by

```
st_as_sfc("LINESTRING(10 5, 9 4, 8 3, 7 2, 6 1)")[[1]]
## LINESTRING (10 5, 9 4, 8 3, 7 2, 6 1)
st_as_sfc(structure(list(st_as_binary(x)), class = "WKB"))[[1]]
## LINESTRING (10 5, 9 4, 8 3, 7 2, 6 1)
```

GDAL, GEOS, spatial databases and GIS read and write WKB which is fast and precise. Conversion between R native objects and WKB is done by package `sf` in compiled (C++/Rcpp) code, making this a reusable and fast route for I/O of simple feature geometries in R.

### Precision

One of the attributes of a geometry list-column ( `sfc` ) is the `precision` : a double number that, when non-zero, causes some rounding during conversion to WKB, which might help certain geometrical operations succeed that would otherwise fail due to floating point representation. The model is that of GEOS, which copies from the Java Topology Suite (JTS (<http://tsusiatsoftware.net/jts/main.html>)), and works like this:

- if precision is zero (default, unspecified), nothing is modified
- negative values convert to float (4-byte real) precision
- positive values convert to `round(x*precision)/precision`.

For the precision model, see also here

(<http://tsusiatsoftware.net/jts/javadoc/com/vividsolutions/jts/geom/PrecisionModel.html>), where it is written that: "... to specify 3 decimal places of precision, use a scale factor of 1000. To specify -3 decimal

places of precision (i.e. rounding to the nearest 1000), use a scale factor of 0.001." Note that all coordinates, so also Z or M values (if present) are affected. Choosing values for precision may require some experimenting.

## Reading and writing

As we've seen above, reading spatial data from an external file can be done by

```
filename <- system.file("shape/nc.shp", package="sf")
nc <- st_read(filename)
## Reading Layer `nc` from data source `/tmp/Rtmpaq4C0b/Rinst79437936646a/sf/shape/nc.shp' using driver `ESRI Shapefile'
## Simple feature collection with 100 features and 14 fields
## geometry type: MULTIPOLYGON
## dimension: XY
## bbox: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965
## epsg (SRID): 4267
## proj4string: +proj=LongLat +datum=NAD27 +no_defs
```

we can suppress the output by adding argument `quiet=TRUE` or by using the otherwise nearly identical but more quiet

```
nc <- read_sf(filename)
```

Writing takes place in the same fashion, using `st_write`:

```
st_write(nc, "nc.shp")
## Writing Layer `nc` to data source `nc.shp' using driver `ESRI Shapefile'
## features: 100
## fields: 14
## geometry type: Multi Polygon
```

If we repeat this, we get an error message that the file already exists, and we can overwrite by

```
st_write(nc, "nc.shp", delete_layer = TRUE)
## Deleting Layer `nc` using driver `ESRI Shapefile'
## Writing Layer `nc` to data source `/tmp/Rtmpaq4C0b/Rbuild7943369cd14d/sf/vignettes/nc.shp' using driver `ESRI Shapefile'
## features: 100
## fields: 14
## geometry type: Multi Polygon
```

or its quiet alternative that does this by default,

```
write_sf(nc, "nc.shp") # silently overwrites
```

## Driver-specific options

The `dsn` and `layer` arguments to `st_read` and `st_write` denote a data source name and optionally a layer name. Their exact interpretation as well as the options they support vary per driver, the GDAL driver documentation ([http://www.gdal.org/ogr\\_formats.html](http://www.gdal.org/ogr_formats.html)) is best consulted for this. For instance, a PostGIS table in database `postgis` might be read by

```
meuse <- st_read("PG:dbname=postgis", "meuse")
```

where the `PG:` string indicates this concerns the PostGIS driver, followed by database name, and possibly port and user credentials. When the `layer` and `driver` arguments are not specified, `st_read` tries to guess them from the datasource, or else simply reads the first layer, giving a warning in case there are more.

`st_read` typically reads the coordinate reference system as `proj4string`, but not the EPSG (SRID). GDAL cannot retrieve SRID (EPSG code) from `proj4string` strings, and, when needed, it has to be set by the user. See also the section on `crs` (`crs`).

`st_drivers()` returns a `data.frame` listing available drivers, and their metadata: names, whether a driver can write, and whether it is a raster and/or vector driver. All drivers can read. Reading of some common data formats is illustrated below:

`st_layers(dsn)` lists the layers present in data source `dsn`, and gives the number of fields, features and geometry type for each layer:

```
st_layers(system.file("osm/overpass.osm", package="sf"))
## Driver: OSM
## Available Layers:
##      Layer_name      geometry_type features fields
## 1      points          Point          NA      10
## 2      lines          Line String    NA       9
## 3 multilinestrings  Multi Line String NA       4
## 4 multipolygons    Multi Polygon  NA      25
## 5 other_relations  Geometry Collection NA       4
```

we see that in this case, the number of features is `NA` because for this xml file the whole file needs to be read, which may be costly for large files. We can force counting by

```
Sys.setenv(OSM_USE_CUSTOM_INDEXING="NO")
st_layers(system.file("osm/overpass.osm", package="sf"), do_count = TRUE)
## Driver: OSM
## Available Layers:
##      Layer_name      geometry_type features fields
## 1      points          Point           1      10
## 2      lines          Line String     0       9
## 3 multilinestrings  Multi Line String 0       4
## 4 multipolygons    Multi Polygon   13      25
## 5 other_relations  Geometry Collection 0       4
```

Another example of reading kml and kmz files is:

```
# Download .shp data
u_shp <- "http://coagisweb.cabq.gov/datadownload/biketrails.zip"
download.file(u_shp, "biketrails.zip")
unzip("biketrails.zip")
u_kmz <- "http://coagisweb.cabq.gov/datadownload/BikePaths.kmz"
download.file(u_kmz, "BikePaths.kmz")
# Read file formats
biketrails_shp <- st_read("biketrails.shp")
if(Sys.info()[1] == "Linux") # may not work if not Linux
  biketrails_kmz <- st_read("BikePaths.kmz")
u_kml = "http://www.northeasttraces.com/oxonraces.com/nearme/safe/6.kml"
download.file(u_kml, "bikeraces.kml")
bikeraces <- st_read("bikeraces.kml")
```

## Create, read, update and delete

GDAL provides the crud ([https://en.wikipedia.org/wiki/Create,\\_read,\\_update\\_and\\_delete](https://en.wikipedia.org/wiki/Create,_read,_update_and_delete)) (create, read, update, delete) functions to persistent storage. `st_read` (or `read_sf`) are used for reading. `st_write` (or `write_sf`) creates, and has the following arguments to control update and delete:

- `update=TRUE` causes an existing data source to be updated, if it exists; this options is by default `TRUE` for all database drivers, where the database is updated by adding a table.
- `delete_layer=TRUE` causes `st_write` try to open the the data source and delete the layer; no errors are given if the data source is not present, or the layer does not exist in the data source.
- `delete_dsn=TRUE` causes `st_write` to delete the data source when present, before writing the layer in a newly created data source. No error is given when the data source does not exist. This option should be handled with care, as it may wipe complete directories or databases.

## Benchmarks

Benchmarks show that `st_read()` is faster than `rgdal::readOGR()`, for example:

```
shp_read_sp <- function() rgdal::readOGR(dsn = ".", layer = "biketrails")
shp_read_sf <- function() st_read("biketrails.shp")
if(Sys.info()[1] == "Linux") {
  kmz_read_sp <- function() rgdal::readOGR(dsn = "BikePaths.kmz")
  kmz_read_sf <- function() st_read("BikePaths.kmz")
} else {
  kmz_read_sp <- function() message("NA")
  kmz_read_sf <- function() message("NA")
}
kml_read_sp <- function() rgdal::readOGR("bikeraces.kml")
kml_read_sf <- function() st_read("bikeraces.kml")
microbenchmark::microbenchmark(shp_read_sp(), shp_read_sf(),
                                kmz_read_sp(), kmz_read_sf(),
                                kml_read_sp(), kml_read_sf(), times = 10)
```

On a laptop with an Intel i5-4300M CPU @ 2.60GHz with ssd the results were as follows:

```

Unit: milliseconds
      expr      min      lq      mean      median      uq
shp_read_sp() 4993.954530 5010.798950 5072.94155 5049.68057 5116.050416
shp_read_sf()  331.580349  341.608044  352.99233  353.00169  364.601151
kmz_read_sp() 4940.108931 4966.177983 5021.47680 4989.82589 5038.393259
kmz_read_sf() 1086.925988 1088.850196 1103.04846 1090.15794 1100.518670
kml_read_sp()  167.556454  176.395750  182.10324  185.31941  187.720235
kml_read_sf()   8.132629   8.268952   10.44328   8.52626   9.420043
      max neval  cld
5186.16240  10    e
 376.64045  10    c
5282.25874  10    e
1178.42358  10    d
 189.29191  10    b
  26.20221  10    a

```

This shows that `sf::st_read()` is substantially faster than `rgdal::readOGR()`: by a factor of 14-18 for the Shapefile and KML files, and more than a factor of 4 for the KMZ file used in this benchmark, respectively.

## Connection to spatial databases

Read and write functions, `st_read()` and `st_write()`, can handle connections to spatial databases to read WKB or WKT directly without using GDAL. Although intended to use the DBI interface, current use and testing of these functions are limited to PostGIS.

## Coordinate reference systems and transformations

Coordinate reference systems (CRS) are like measurement units for coordinates: they specify which location on Earth a particular coordinate pair refers to. We saw above that `sfc` objects (geometry list-columns) have two attributes to store a CRS: `epsg` and `proj4string`. This implies that all geometries in a geometry list-column must have the same CRS. Both may be `NA`, e.g. in case the CRS is unknown, or when we work with local coordinate systems (e.g. inside a building, a body, or an abstract space).

`proj4string` is a generic, string-based description of a CRS, understood by the PROJ.4 (<http://proj4.org/>) library. It defines projection types and (often) defines parameter values for particular projections, and hence can cover an infinite amount of different projections. This library (also used by GDAL) provides functions to convert or transform between different CRS. `epsg` is the integer ID for a particular, known CRS that can be resolved into a `proj4string`. Some `proj4string` values can be resolved back into their corresponding `epsg` ID, but this does not always work.

The importance of having `epsg` values stored with data besides `proj4string` values is that the `epsg` refers to particular, well-known CRS, whose parameters may change (improve) over time; fixing only the `proj4string` may remove the possibility to benefit from such improvements, and limit some of the provenance of datasets, but may help reproducibility.

Coordinate reference system transformations can be carried out using `st_transform`, e.g. converting longitudes/latitudes in NAD27 to web mercator (EPSG:3857) can be done by



```
nc.web_mercator <- st_transform(nc, 3857)
st_geometry(nc.web_mercator)[[4]][[2]][[1]][1:3,]
##           [,1]      [,2]
## [1,] -8463267 4377519
## [2,] -8460094 4377510
## [3,] -8450437 4375553
```

## Conversion, including to and from sp

sf objects and objects deriving from `Spatial` (package `sp`) can be coerced both ways:

```
showMethods("coerce", classes = "sf")
## Function: coerce (package methods)
## from="Spatial", to="sf"
## from="sf", to="Spatial"
methods(st_as_sf)
## [1] st_as_sf.Spatial*      st_as_sf.data.frame* st_as_sf.lpp*
## [4] st_as_sf.map*            st_as_sf.ppp*        st_as_sf.psp*
## [7] st_as_sf.sf*
## see '?methods' for accessing help and source code
methods(st_as_sfc)
## [1] st_as_sfc.SpatialLines*    st_as_sfc.SpatialMultiPoints*
## [3] st_as_sfc.SpatialPixels*   st_as_sfc.SpatialPoints*
## [5] st_as_sfc.SpatialPolygons* st_as_sfc.WKB*
## [7] st_as_sfc.bbox*            st_as_sfc.blob*
## [9] st_as_sfc.character*       st_as_sfc.dimensions*
## [11] st_as_sfc.factor*          st_as_sfc.list*
## [13] st_as_sfc.map*             st_as_sfc.raw*
## see '?methods' for accessing help and source code
# anticipate that sp::CRS will expand proj4strings:
p4s <- "+proj=longlat +datum=NAD27 +no_defs +ellps=clrk66 +nadgrids=@conus,@alaska,@ntv2_0.gsb,@ntv1_can.dat"
st_crs(nc) <- p4s
## Warning: st_crs<- : replacing crs does not reproject data; use st_transform
## for that
# anticipate geometry column name changes:
names(nc)[15] = "geometry"
attr(nc, "sf_column") = "geometry"
nc.sp <- as(nc, "Spatial")
class(nc.sp)
## [1] "SpatialPolygonsDataFrame"
## attr(,"package")
## [1] "sp"
nc2 <- st_as_sf(nc.sp)
all.equal(nc, nc2)
## [1] "Attributes: < Component \"class\": Lengths (4, 2) differ (string compare on first 2) >"
## [2] "Attributes: < Component \"class\": 1 string mismatch >"

## [3] "Component \"geometry\": Attributes: < Component \"crs\": Component \"epsg\": 'is.NA' value mismatch: 1 in current 0 in target >"
```

As the `Spatial*` objects only support `MULTILINESTRING` and `MULTIPOLYGON`, `LINestring` and `POLYGON` geometries are automatically coerced into their `MULTI` form. When converting `Spatial*` into `sf`, if all geometries consist of a single `POLYGON` (possibly with holes), a `POLYGON` and otherwise all geometries are

returned as MULTIPOLYGON : a mix of POLYGON and MULTIPOLYGON (such as common in shapefiles) is not created. Argument `forceMulti=TRUE` will override this, and create MULTIPOLYGON s in all cases. For LINES the situation is identical.

## Geometrical operations

The standard for simple feature access defines a number of geometrical operations.

`st_is_valid` and `st_is_simple` return a boolean indicating whether a geometry is valid or simple.

```
st_is_valid(nc[1:2,])
## [1] TRUE TRUE
```

`st_distance` returns a dense numeric matrix with distances between geometries. `st_relate` returns a character matrix with the DE9-IM (<https://en.wikipedia.org/wiki/DE-9IM#Illustration>) values for each pair of geometries:

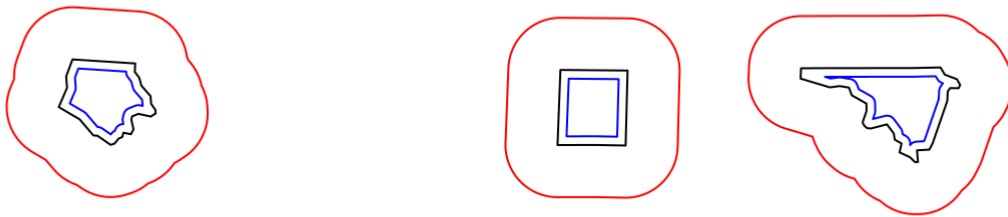
```
x = st_transform(nc, 32119)
st_distance(x[c(1,4,22),], x[c(1, 33,55,56),])
## Units: m
##      [,1]      [,2]      [,3]      [,4]
## [1,]      0.00 312184.9 128341.85 475623.3
## [2,] 440561.15 114939.7 590434.80      0.0
## [3,] 18944.03 352719.1 78756.89 517527.8
st_relate(nc[1:5,], nc[1:4,])
## although coordinates are Longitude/Latitude, st_relate assumes that they are planar
##      [,1]      [,2]      [,3]      [,4]
## [1,] "2FFF1FFF2" "FF2F11212" "FF2FF1212" "FF2FF1212"
## [2,] "FF2F11212" "2FFF1FFF2" "FF2F11212" "FF2FF1212"
## [3,] "FF2FF1212" "FF2F11212" "2FFF1FFF2" "FF2FF1212"
## [4,] "FF2FF1212" "FF2FF1212" "FF2FF1212" "2FFF1FFF2"
## [5,] "FF2FF1212" "FF2FF1212" "FF2FF1212" "FF2FF1212"
```

The commands `st_intersects`, `st_disjoint`, `st_touches`, `st_crosses`, `st_within`, `st_contains`, `st_overlaps`, `st_equals`, `st_covers`, `st_covered_by`, `st_equals_exact` and `st_is_within_distance` return a sparse matrix with matching (TRUE) indexes, or a full logical matrix:

```
st_intersects(nc[1:5,], nc[1:4,])
## although coordinates are Longitude/Latitude, st_intersects assumes that they are planar
## Sparse geometry binary predicate List of Length 5, where the predicate was `intersects'
## 1: 1, 2
## 2: 1, 2, 3
## 3: 2, 3
## 4: 4
## 5: (empty)
st_intersects(nc[1:5,], nc[1:4,], sparse = FALSE)
## although coordinates are Longitude/Latitude, st_intersects assumes that they are planar
##      [,1] [,2] [,3] [,4]
## [1,] TRUE TRUE FALSE FALSE
## [2,] TRUE TRUE TRUE FALSE
## [3,] FALSE TRUE TRUE FALSE
## [4,] FALSE FALSE FALSE TRUE
## [5,] FALSE FALSE FALSE FALSE
```

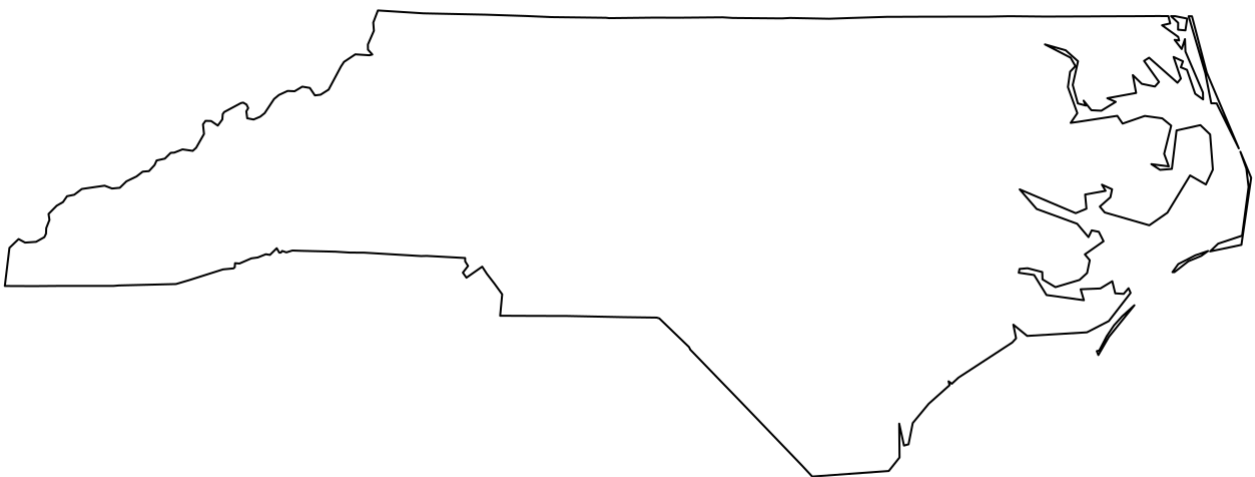
The commands `st_buffer`, `st_boundary`, `st_convexhull`, `st_union_cascaded`, `st_simplify`, `st_triangulate`, `st_polygonize`, `st_centroid`, `st_segmentize`, and `st_union` return new geometries, e.g.:

```
sel <- c(1,5,14)
geom = st_geometry(nc.web_mercator[sel,])
buf <- st_buffer(geom, dist = 30000)
plot(buf, border = 'red')
plot(geom, add = TRUE)
plot(st_buffer(geom, -5000), add = TRUE, border = 'blue')
```



Commands `st_intersection`, `st_union`, `st_difference`, `st_sym_difference` return new geometries that are a function of pairs of geometries:

```
par(mar = rep(0,4))
u <- st_union(nc)
plot(u)
```



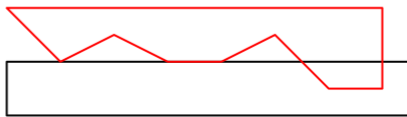
The following code shows how computing an intersection between two polygons may yield a `GEOMETRYCOLLECTION` with a point, line and polygon:

```

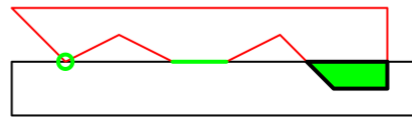
opar <- par(mfrow = c(1, 2))
a <- st_polygon(list(cbind(c(0,0,7.5,7.5,0),c(0,-1,-1,0,0))))
b <- st_polygon(list(cbind(c(0,1,2,3,4,5,6,7,7,0),c(1,0,.5,0,0,0.5,-0.5,-0.5,1,1))))
plot(a, ylim = c(-1,1))
title("intersecting two polygons:")
plot(b, add = TRUE, border = 'red')
(i <- st_intersection(a,b))
## GEOMETRYCOLLECTION (POINT (1 0), LINESTRING (4 0, 3 0), POLYGON ((5.5 0, 7 0, 7 -0.5, 6 -0.5, 5.5 0)))
plot(a, ylim = c(-1,1))
title("GEOMETRYCOLLECTION")
plot(b, add = TRUE, border = 'red')
plot(i, add = TRUE, col = 'green', lwd = 2)

```

intersecting two polygons:



GEOMETRYCOLLECTION



```
par(opar)
```

## Non-valid geometries

Invalid geometries are for instance self-intersecting lines (left) or polygons with slivers (middle) or self-intersections (right).

```

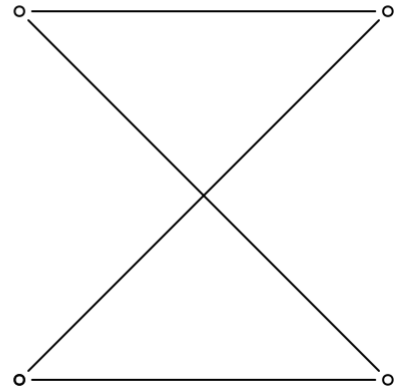
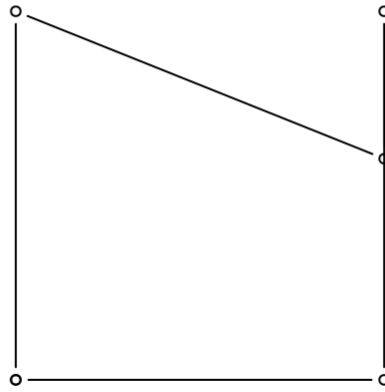
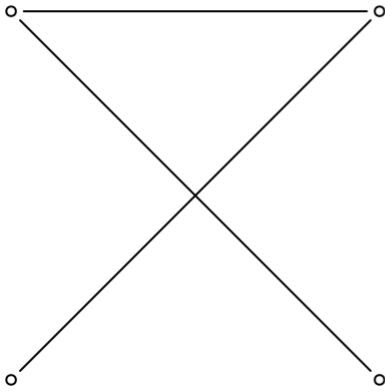
library(sf)
x1 <- st_linestring(cbind(c(0,1,0,1),c(0,1,1,0)))
x2 <- st_polygon(list(cbind(c(0,1,1,1,0,0),c(0,0,1,0.6,1,0))))
x3 <- st_polygon(list(cbind(c(0,1,0,1,0),c(0,1,1,0,0))))
st_is_simple(st_sfc(x1))
## [1] FALSE
st_is_valid(st_sfc(x2,x3))
## [1] FALSE FALSE

```

**LINSTRING** ((0 0, 1 1, 0 1, 1 0))

**POLYGON** ((0 0, 1 0, 1 1, 1 0.6, 0 1, 0 0))

**POLYGON** ((0 0, 1 1, 0 1, 1 0, 0 0))



## Units

Where possible geometric operations such as `st_distance()`, `st_length()` and `st_area()` report results with a units attribute appropriate for the CRS:

```
a <- st_area(nc[1,])
attributes(a)
## $units
## $numerator
## [1] "m" "m"
##
## $denominator
## character(0)
##
## attr("class")
## [1] "symbolic_units"
##
## $class
## [1] "units"
```

The **units** package can be used to convert between units:

```
units::set_units(a, km^2) # result in square kilometers
## 1137.389 km^2
units::set_units(a, ha) # result in hectares
## 113738.9 ha
```

The result can be stripped of their attributes if needs be:

```
as.numeric(a)
## [1] 1137388604
```

## How attributes relate to geometries

(This will eventually be the topic of a new vignette; now here to explain the last attribute of `sf` objects)

The standard documents about simple features are very detailed about the geometric aspects of features, but say nearly nothing about attributes, except that their values should be understood in another reference system (their units of measurement, e.g. as implemented in the package **units** (<https://CRAN.R-project.org/package=units>)). But there is more to it. For variables like air temperature, interpolation usually makes sense, for others like human body temperature it doesn't. The difference is that air temperature is a field, which continues between sensors, where body temperature is an object property that doesn't extend beyond the body – in spatial statistics bodies would be called a point pattern, their temperature the point marks. For geometries that have a non-zero size (positive length or area), attribute values may refer to the every sub-geometry (every point), or may summarize the geometry. For example, a state's population density summarizes the whole state, and is not a meaningful estimate of population density for a give point inside the state without the context of the state. On the other hand, land use or geological maps give polygons with constant land use or geology, every point inside the polygon is of that class. Some properties are spatially extensive ([https://en.wikipedia.org/wiki/Intensive\\_and\\_extensive\\_properties](https://en.wikipedia.org/wiki/Intensive_and_extensive_properties)), meaning that attributes would summed up when two geometries are merged: population is an example. Other properties are spatially intensive, and should be averaged, with population density the example.

Simple feature objects of class `sf` have an `agr` attribute that points to the *attribute-geometry-relationship*, how attributes relate to their geometry. It can be defined at creation time:

```
nc <- st_read(system.file("shape/nc.shp", package="sf"),
  agr = c(AREA = "aggregate", PERIMETER = "aggregate", CNTY_ = "identity",
    CNTY_ID = "identity", NAME = "identity", FIPS = "identity", FIPSNO = "identity",
    CRESS_ID = "identity", BIR74 = "aggregate", SID74 = "aggregate", NWBIR74 = "aggregat
e",
    BIR79 = "aggregate", SID79 = "aggregate", NWBIR79 = "aggregate"))
## Reading layer `nc' from data source `/tmp/Rtmpaq4C0b/Rinst79437936646a/sf/shape/nc.shp' us
ing driver `ESRI Shapefile'
## Simple feature collection with 100 features and 14 fields
## Attribute-geometry relationship: 0 constant, 8 aggregate, 6 identity
## geometry type: MULTIPOLYGON
## dimension: XY
## bbox: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965
## epsg (SRID): 4267
## proj4string: +proj=LongLat +datum=NAD27 +no_defs
st_agr(nc)
## AREA PERIMETER CNTY_ CNTY_ID NAME FIPS FIPSNO
## aggregate aggregate identity identity identity identity identity
## CRESS_ID BIR74 SID74 NWBIR74 BIR79 SID79 NWBIR79
## identity aggregate aggregate aggregate aggregate aggregate aggregate
## Levels: constant aggregate identity
data(meuse, package = "sp")
meuse_sf <- st_as_sf(meuse, coords = c("x", "y"), crs = 28992, agr = "constant")
st_agr(meuse_sf)
## cadmium copper Lead zinc elev dist om ffreq
## constant constant constant constant constant constant constant constant
## soil lime Landuse dist.m
## constant constant constant constant
## Levels: constant aggregate identity
```

When not specified, this field is filled with `NA` values, but if non-`NA`, it has one of three possibilities

value	meaning
constant	a variable that has a constant value at every location over a spatial extent; examples: soil type, climate zone, land use

value	meaning
aggregate	values are summary values (aggregates) over the geometry, e.g. population density, dominant land use
identity	values identify the geometry: they refer to (the whole of) this and only this geometry

With this information (still to be done) we can for instance

- either return missing values or generate warnings when a *aggregate* value at a point location inside a polygon is retrieved, or
- list the implicit assumptions made when retrieving attribute values at points inside a polygon when `relation_to_geometry` is missing.
- decide what to do with attributes when a geometry is split: do nothing in case the attribute is constant, give an error or warning in case it is an aggregate, change the `relation_to_geometry` to *constant* in case it was *identity*.

Further reading:

1. S. Scheider, B. Gräler, E. Pebesma, C. Stasch, 2016. Modelling spatio-temporal information generation. *Int J of Geographic Information Science*, 30 (10), 1980-2008. (pdf (<http://pebesma.staff.ifgi.de/generativealgebra.pdf>))
2. Stasch, C., S. Scheider, E. Pebesma, W. Kuhn, 2014. Meaningful Spatial Prediction and Aggregation. *Environmental Modelling & Software*, 51, (149–165, open access (<http://dx.doi.org/10.1016/j.envsoft.2013.09.006>)).