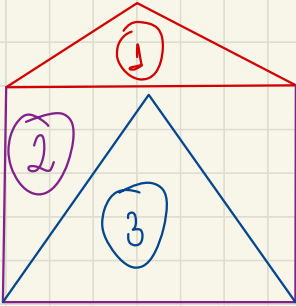



Q11 a) Por simetria, $S_G = 4 \text{ cm}$

Cálculo de r_G :



Elemento 1 $r_{G1} = 7 \text{ cm}$

$$A_1 = \frac{8 \cdot 3}{2} = 12 \text{ cm}^2$$

$$I_1 = \frac{8 \cdot 3^3}{36} = 6 \text{ cm}^4$$

Elemento 2: $r_{G2} = 3 \text{ cm}$
 $A_2 = 8 \cdot 6 = 48 \text{ cm}^2$

$$I_2 = \frac{8 \cdot 6^3}{12} = 144 \text{ cm}^4$$

Elemento 3: $r_{G3} = 2 \text{ cm}$

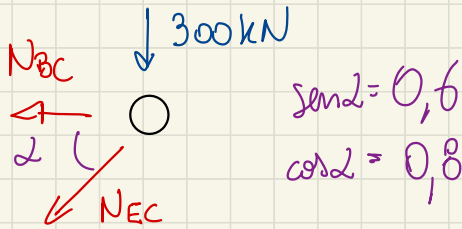
$$A_3 = \frac{8 \cdot 6}{2} = 24 \text{ cm}^2 \quad I_3 = \frac{8 \cdot 6^3}{36} = 48 \text{ cm}^4$$

$$r_G = \frac{A_1 r_{G1} + A_2 r_{G2} - A_3 r_{G3}}{A_1 + A_2 - A_3} = 5 \text{ cm}$$

$$I_y = I_1 + A_1 (r_{G1} - r_G)^2 + I_2 + A_2 (r_{G2} - r_G)^2 - I_3 - A_3 (r_{G3} - r_G)^2$$

$$I_y = 126 \text{ cm}^4$$

Q2) a)



$$\sum F_y = 0 \Rightarrow N_{EC} \sin \alpha = -300$$

$$\Leftrightarrow N_{EC} = \frac{-300}{0,6} = -500 \text{ kN}$$

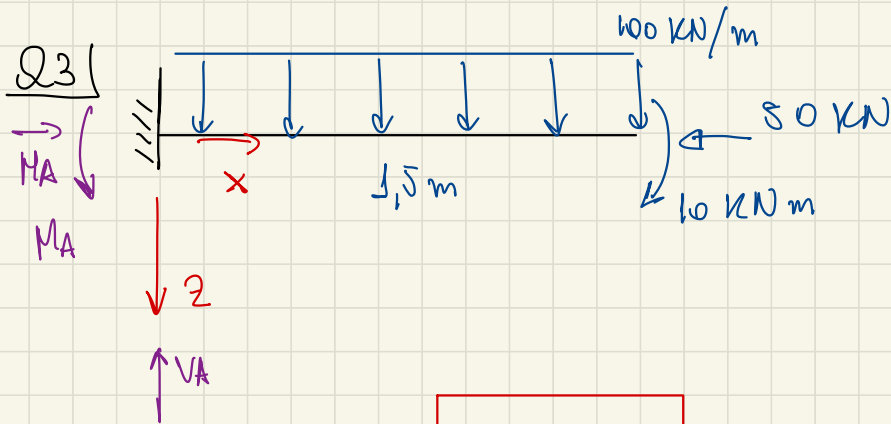
$$\sum F_x = 0 \Rightarrow N_{BC} + N_{EC} \cos \alpha = 0$$

$$\Leftrightarrow N_{BC} - N_{EC} \cos \alpha = 400 \text{ kN}$$

b) EC: $\frac{|N_{EC}|}{A_{EC}} = \bar{\sigma} = 20 \cdot 10^6 \Leftrightarrow A_{EC} = \frac{500 \cdot 10^3}{20 \cdot 10^6}$

$$A_{EC} = 25 \cdot 10^{-3} \text{ m}^2 = 0,025 \text{ m}^2$$

BE: $\frac{|N_{BE}|}{A_{BE}} = \bar{\sigma} = 20 \cdot 10^6 \Leftrightarrow A_{BE} = \frac{400 \cdot 10^3}{20 \cdot 10^6} = 20 \cdot 10^{-3} \text{ m}^2$



a) Reações de apoio

$$H_A = 50 \text{ kN}$$

$$V_A = 150 \text{ kN}$$

$$M_A = \frac{100 \cdot 1,5^2}{2} + 10 = 122,5 \text{ kNm}$$

$$= 12250 \text{ kNcm}$$

$$b) \sigma = \frac{N}{A} + \frac{Mz}{I_y} = -\frac{50}{40 \cdot 20} - \frac{12250}{106,666} \cdot z$$

$$\sigma = -0,0625 - 0,1148 z \quad \frac{\text{kN}}{\text{cm}^2}$$

$$c) \sigma = 0 \Rightarrow z = -\frac{0,0625}{0,1148} = -0,544 \text{ cm}$$

d) A máxima tensão de tração ocorre para $z = -20 \text{ cm}$

$$\sigma(z = -20) = 2,2335 \text{ kN/cm}^2$$