



*Escola de Engenharia de São Carlos  
Universidade de São Paulo*

# **PID – Sistemas não-oscilatórios**

## **Aula 23**

**SEM 0169 – Sistemas de Controle**

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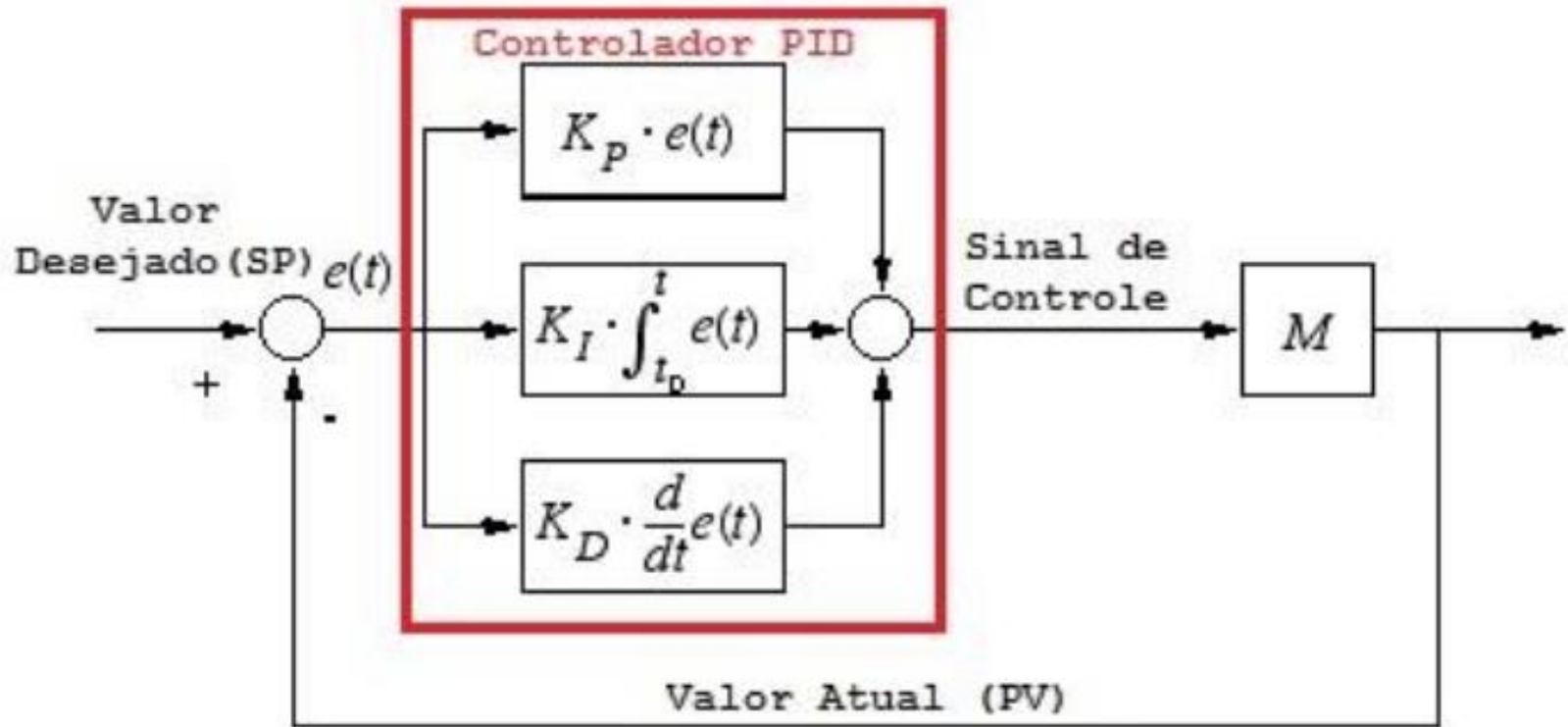
(16) 9 9291 8310



# Objetivo

Apresentar uma abordagem sistemática para projetar PID para sistemas que não oscilam.

# PID



# P - Proporcional

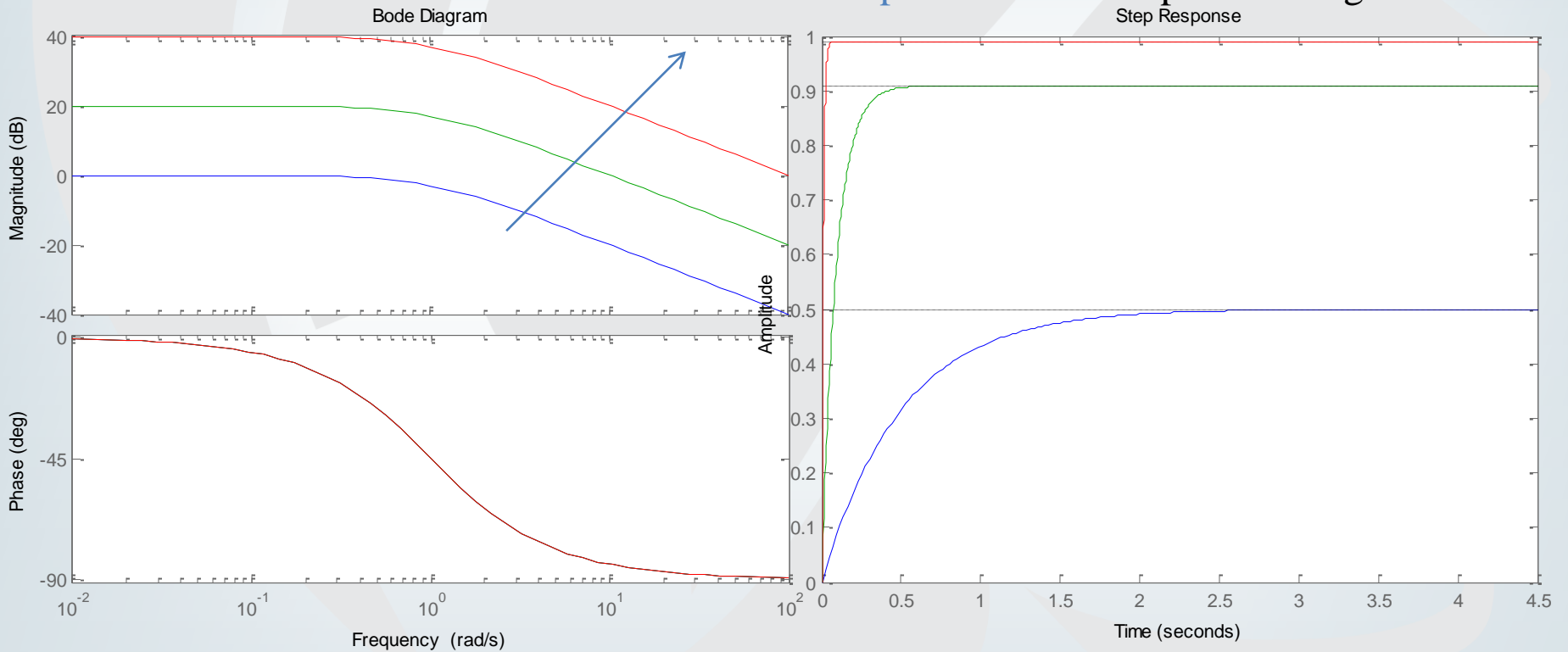
Controle\_aula23\_ex1.ipynb

$K_p$ : ação proporcional ao erro

FRF da malha aberta

Aumentando o  $K_p$

Resposta ao degrau



Acelera a resposta!

# D - Derivativo

$K_d$ : ação proporcional à derivada do erro

FRF da malha aberta

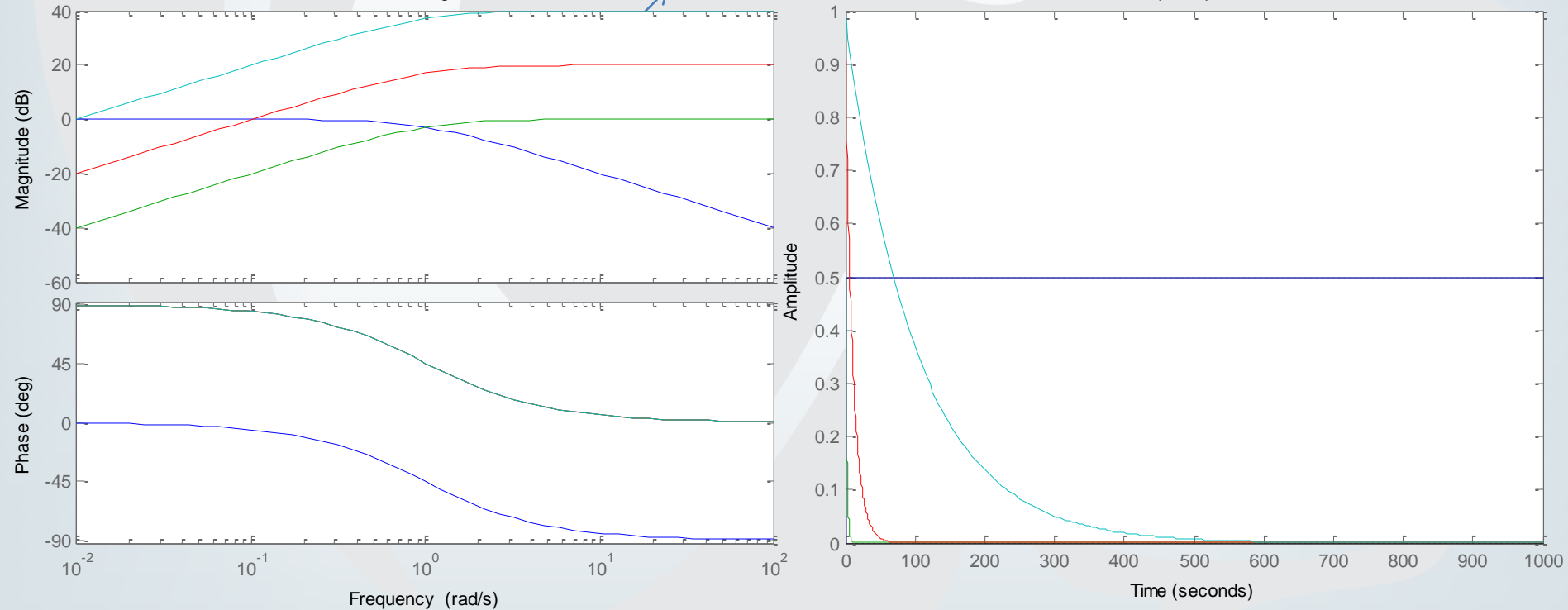
Aumentando o  $K_d$

Resposta ao degrau

Bode Diagram



Step Response



Desacelera a resposta, reduz oscilações!

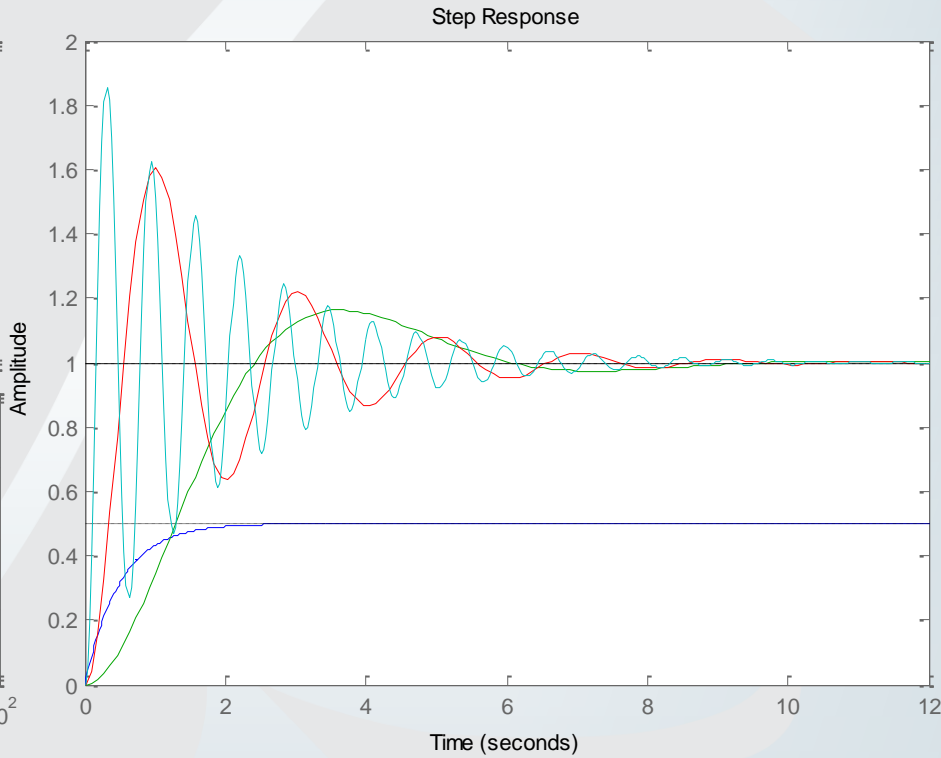
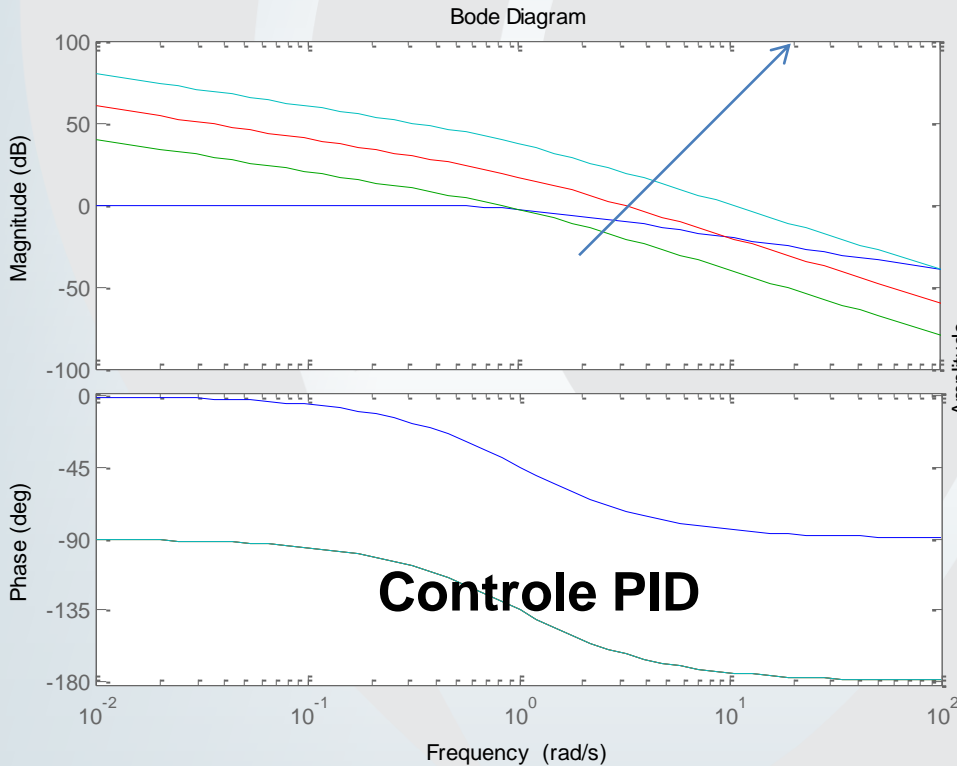
# I - Integral

$K_i$ : ação proporcional à integral do erro

FRF da malha aberta

Aumentando o  $K_i$

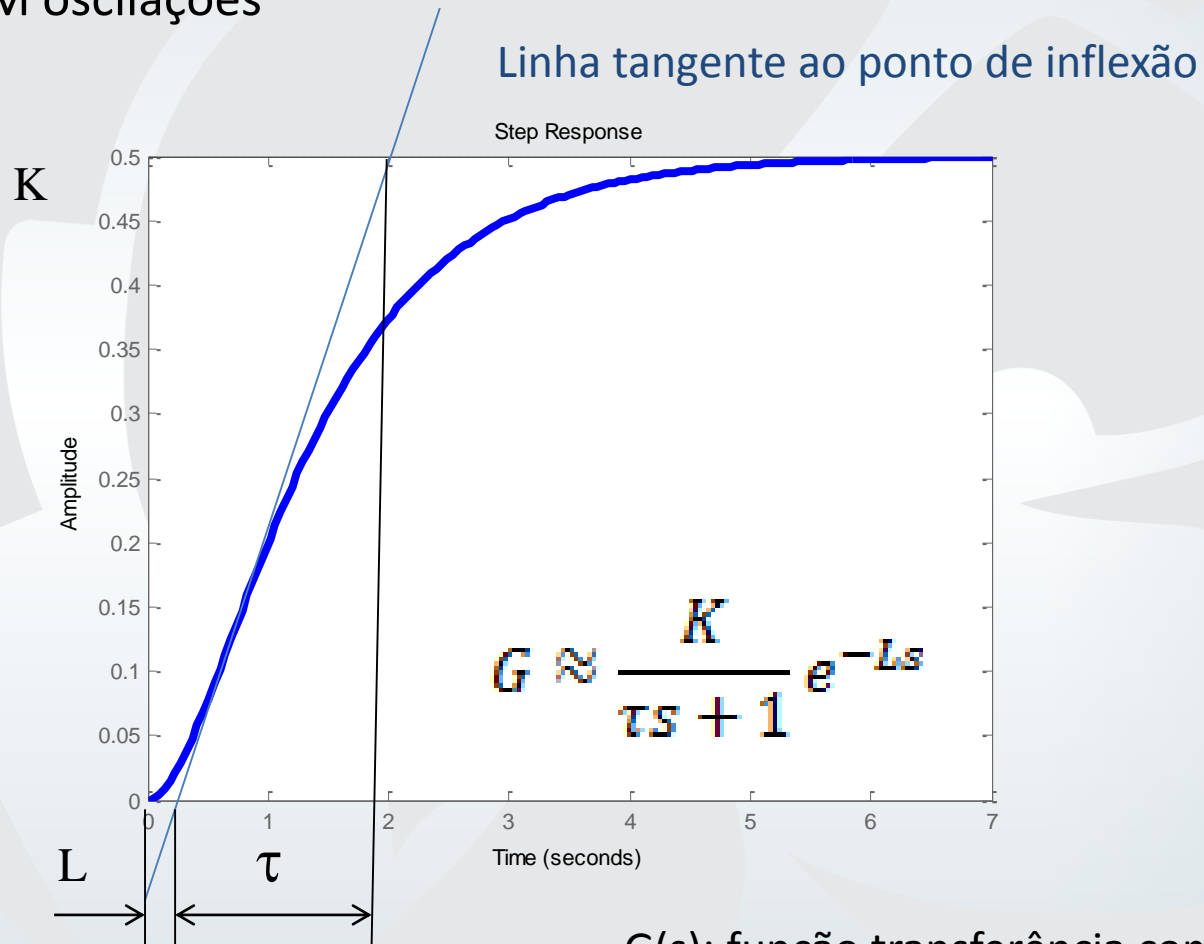
Resposta ao degrau



Acelera a resposta e elimina o erro de regime permanente!

# PID – Ziegler Nichols

Sistemas SEM oscilações

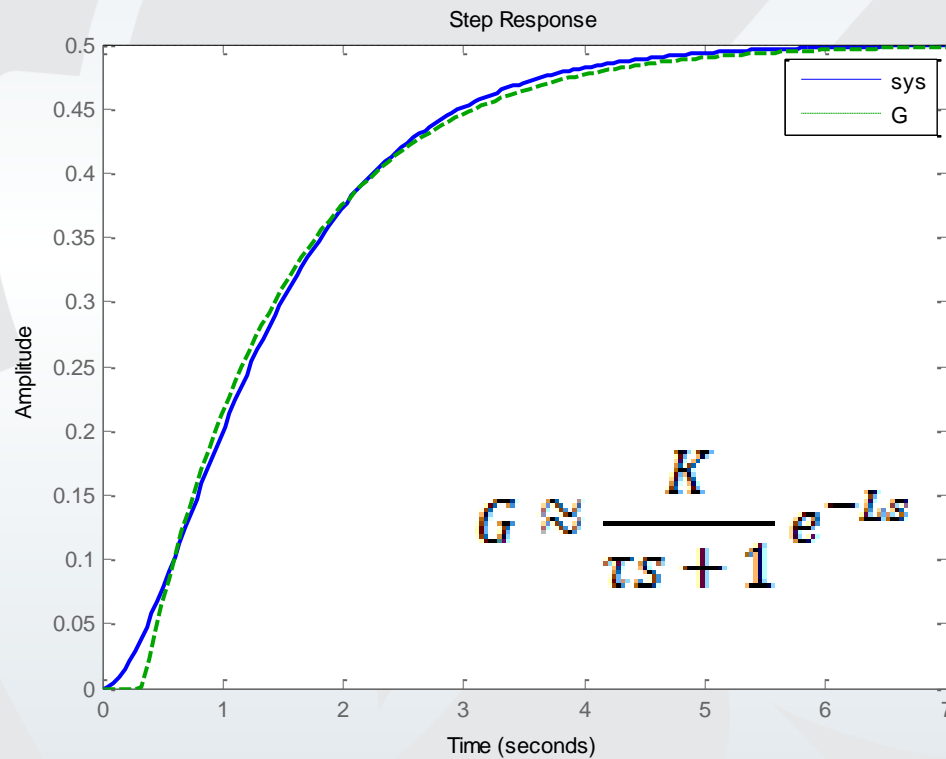


$G(s)$ : função transferência com delay que aproxima a original



# PID – Ziegler Nichols

Sistemas SEM oscilações



G(s): função transferência com delay que aproxima a original

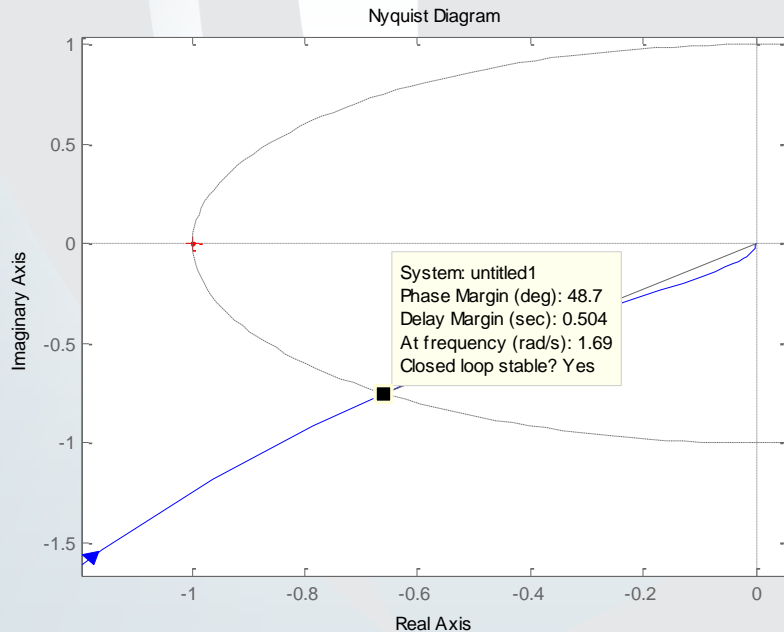
# PID – Ziegler Nichols

Sistemas SEM oscilações

$$G \approx \frac{K}{\tau s + 1} e^{-Ls}$$



$$C_{PID} \approx \frac{0.6\tau(s + 1/L)^2}{s}$$



Margem de ganho: infinito  
Margem de fase: 45°

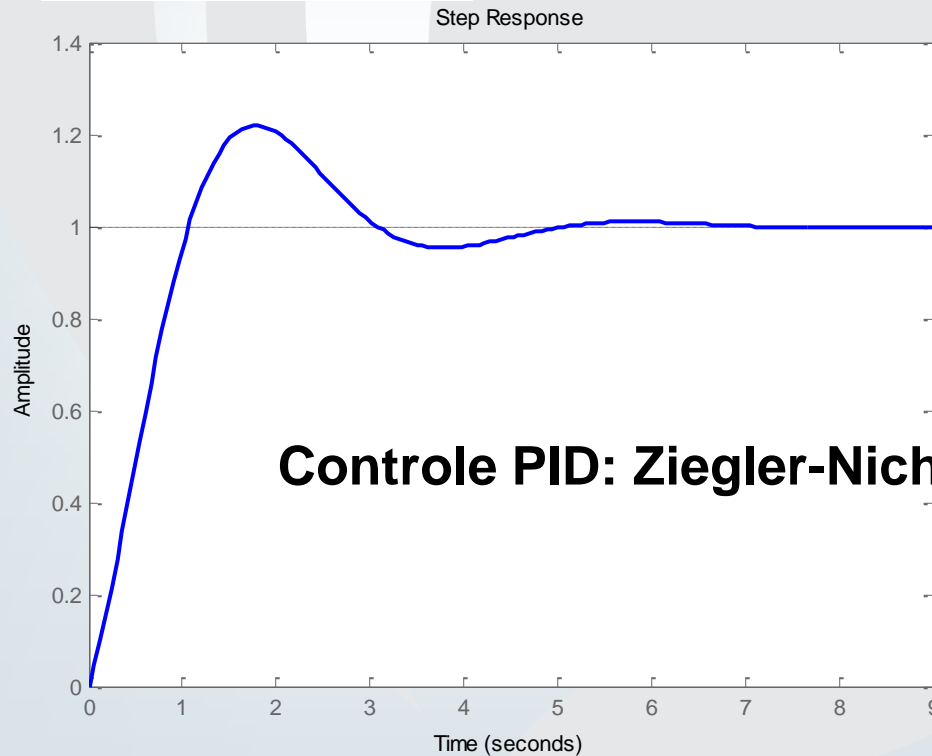
# PID – Ziegler Nichols

Sistemas SEM oscilações

$$G \approx \frac{K}{\tau s + 1} e^{-Ls}$$



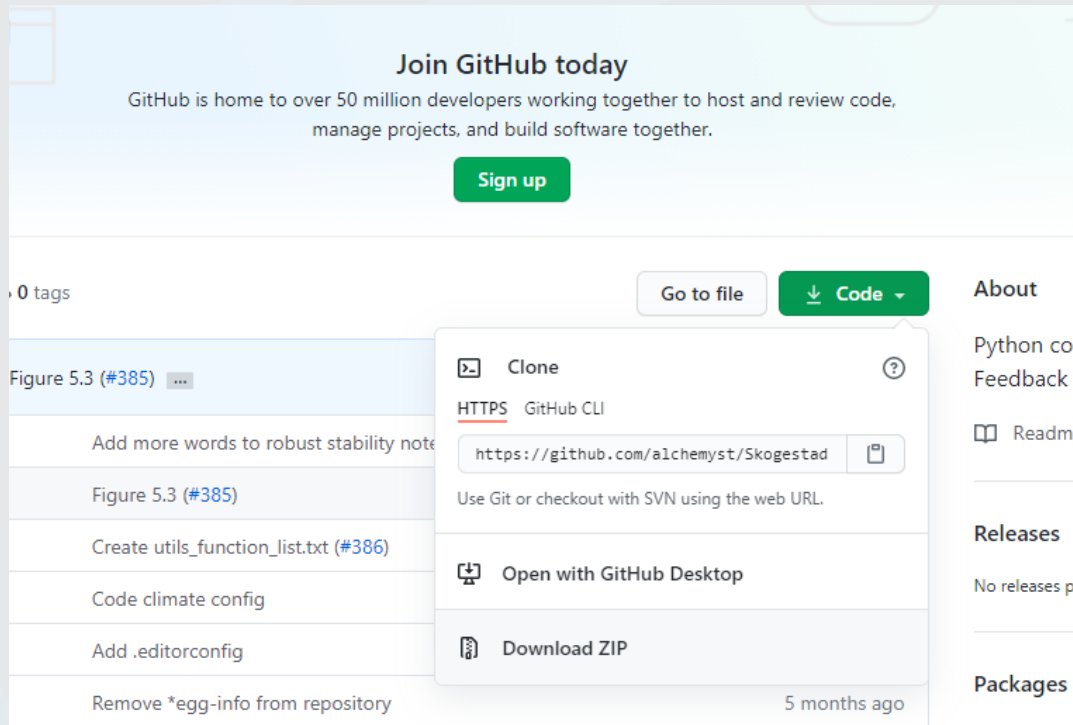
$$C_{PID} \approx \frac{0.6\tau(s + 1/L)^2}{s}$$



Sobressinal: 20%

# Exemplo

<https://github.com/alchemyst/Skogestad-Python>



Vai até o diretório onde está o arquivo zip usando o Windows Power Shell  
# pip install ./Skogestad-Python-master.zip

```
robustcontrol==0.1.0) (1.4-1)
Requirement already satisfied: matplotlib>=3.1 in c:\users\maira\anaconda3\lib\site-packages (from robustcontrol==0.1.0) (3.1.0)
Requirement already satisfied: numpy>=1.18 in c:\users\maira\anaconda3\lib\site-packages (from robustcontrol==0.1.0) (1.18.1)
Requirement already satisfied: scipy>=1.4 in c:\users\maira\anaconda3\lib\site-packages (from robustcontrol==0.1.0) (1.4.1)
Processing c:\users\maira\documents\python scripts\skogestad-python-master\downloads\skogestad-python-master.zip
(base) PS C:\Users\Maira\Documents\Python Scripts\Skogestad-Python-master>
(base) PS C:\Users\Maira\Documents\Python Scripts\Skogestad-Python-master>
(base) PS C:\Users\Maira\Documents\Python Scripts\Skogestad-Python-master> cd ..
(base) PS C:\Users\Maira\Documents\Python Scripts> pip install ./Skogestad-Python-master.zip
```

# Exemplo

Controle\_aula23\_ex1.ipynb

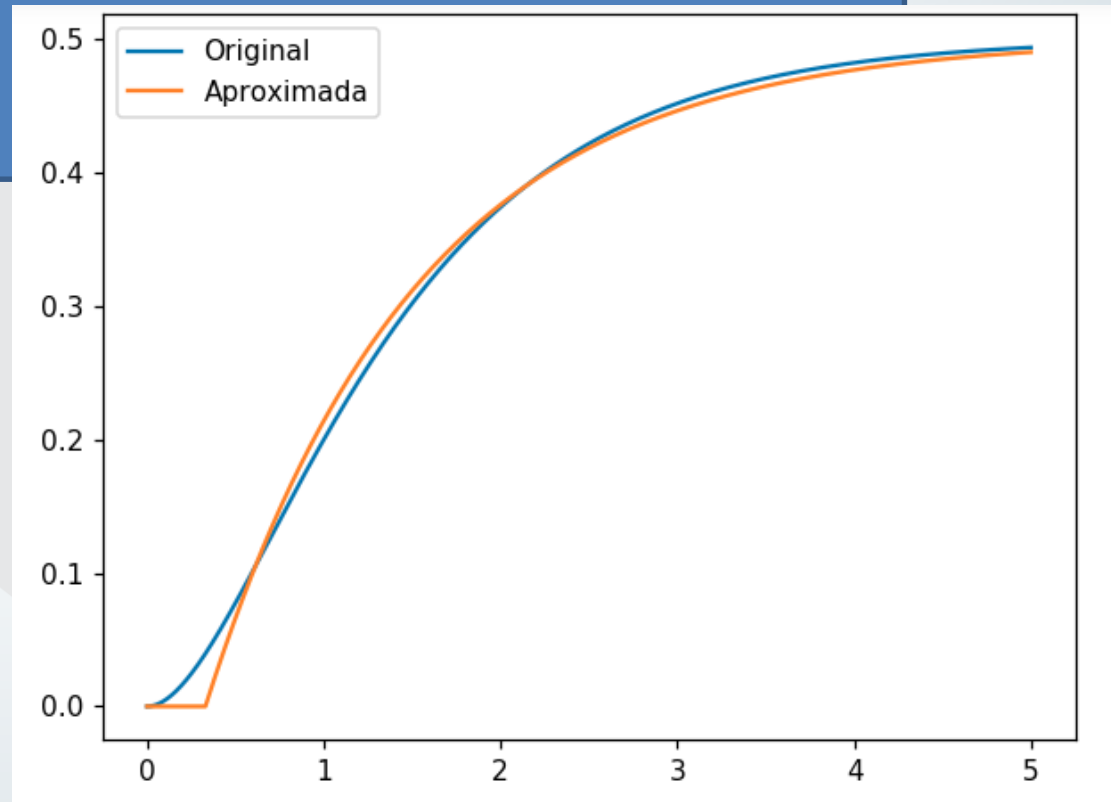
```
sys = tf([1],[1,3,2]); # polos em -1 e -2 (sem oscilação)
```

```
K = 0.5;
```

```
L = 0.33;
```

```
tau = 1.2;
```

```
G = tf(K,[tau,1],deadtime = L)
```

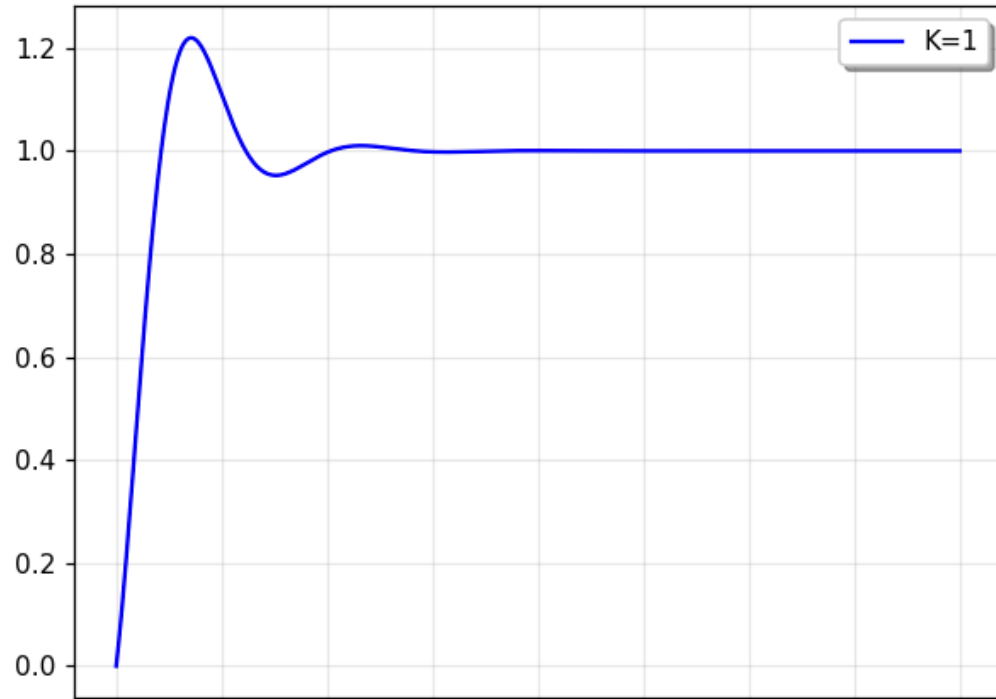


# Exemplo

Controle\_aula23\_ex1.ipynb

```
G = TransferFunction([1],[1,3,2]);  
# PID por Ziegler Nichols  
Cpid = TransferFunction(0.6*tau*np.convolve([1,1/0.33],[1,1/0.33]),[1,0]);  
# Bode e Nyquist da Malha aberta  
L = Cpid*G
```

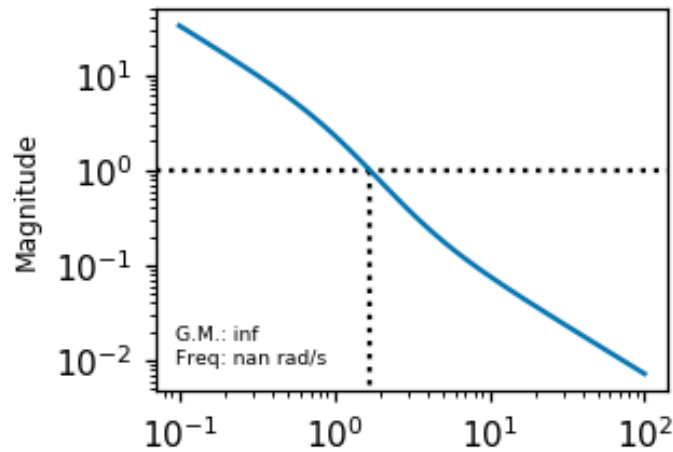
```
MF = feedback(1*L, 1)
```



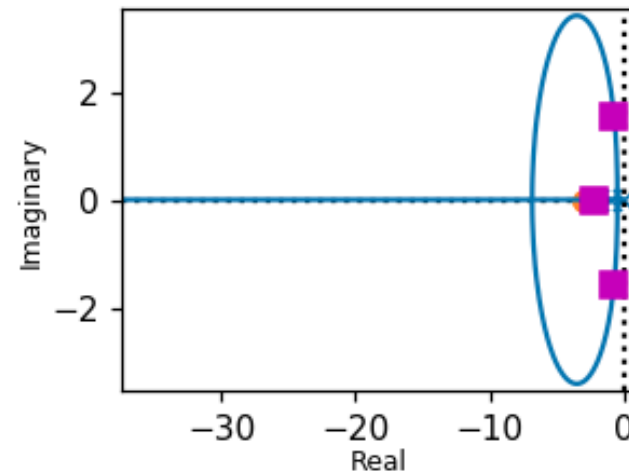
# Exemplo

Controle\_aula23\_ex1.ipynb

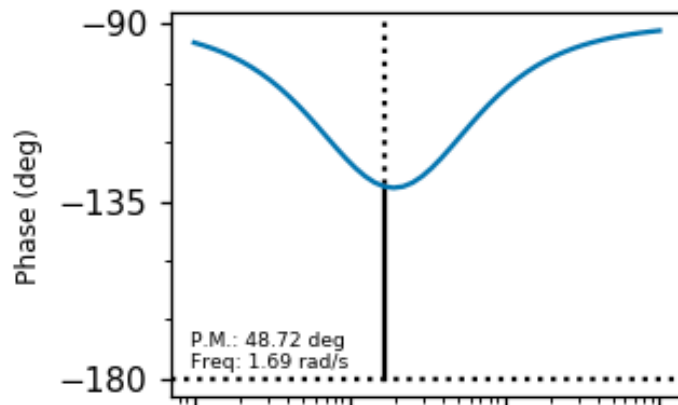
Bode magnitude



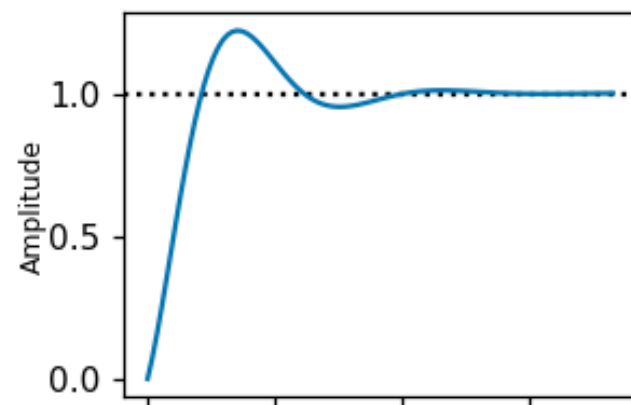
Root locus



Bode phase



Step response



# Conclusões

- Aprendemos a usar uma técnica de projeto e avalia-la usando métodos de estabilidade e desempenho





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