

# Estruturas Hidráuicas I

Aula 5

Extravasores 4

Soleiras Labirinto & Piano Keys

Bom dia a todos.

J Rodolfo S Martins ([scarati@usp.br](mailto:scarati@usp.br))

[www.pha.poli.usp.br](http://www.pha.poli.usp.br)

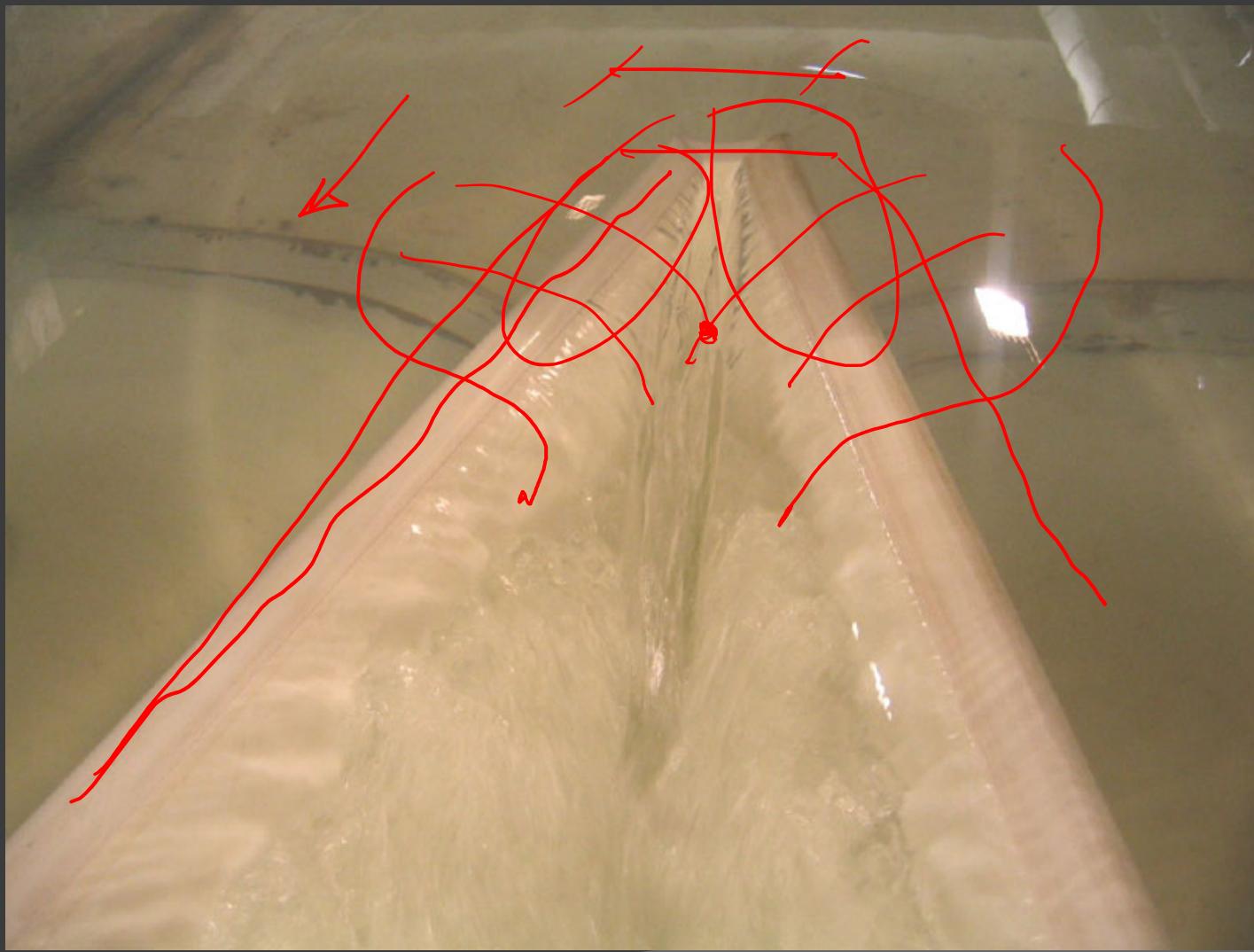
# Bibliografia

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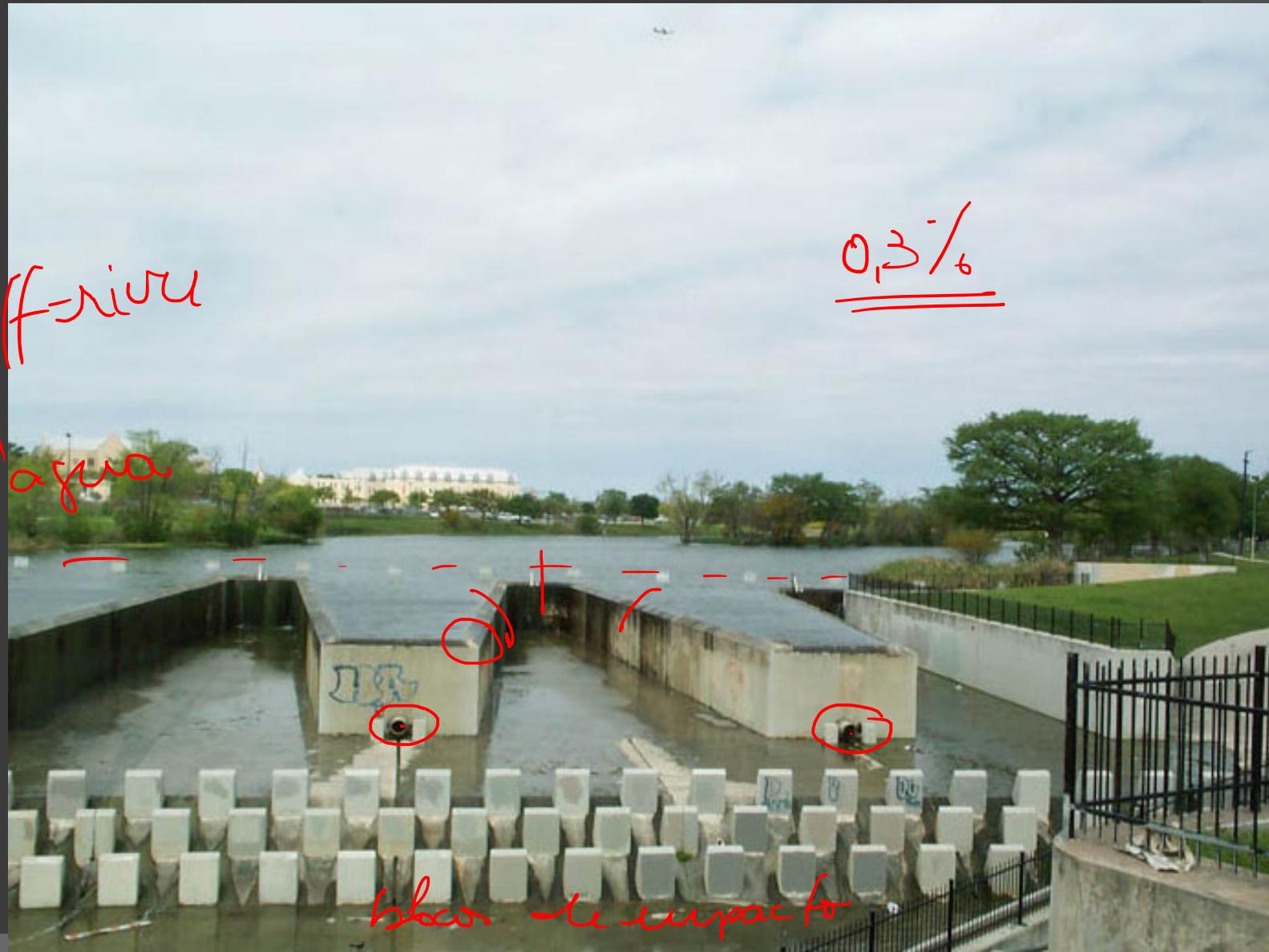




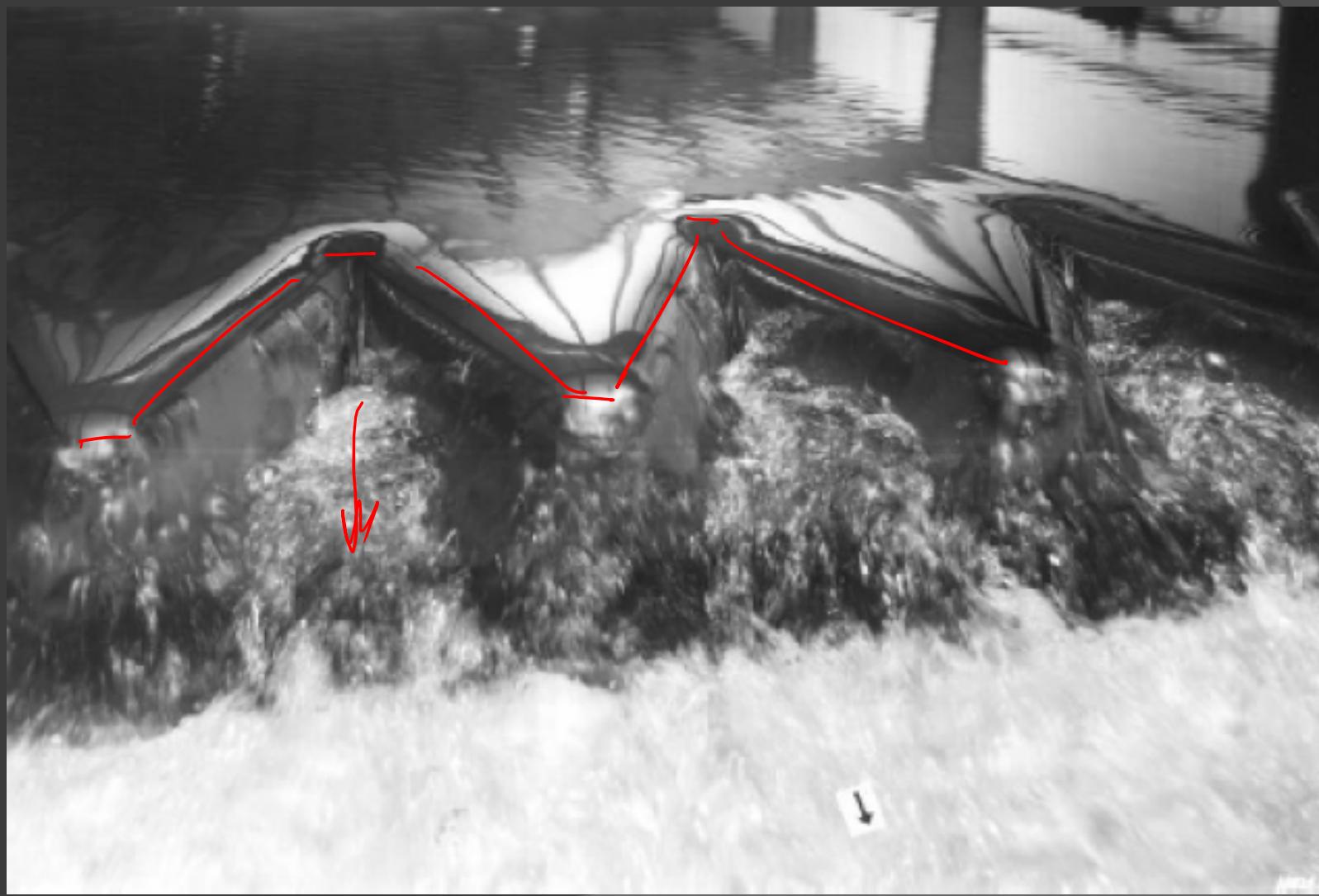
run-off-river

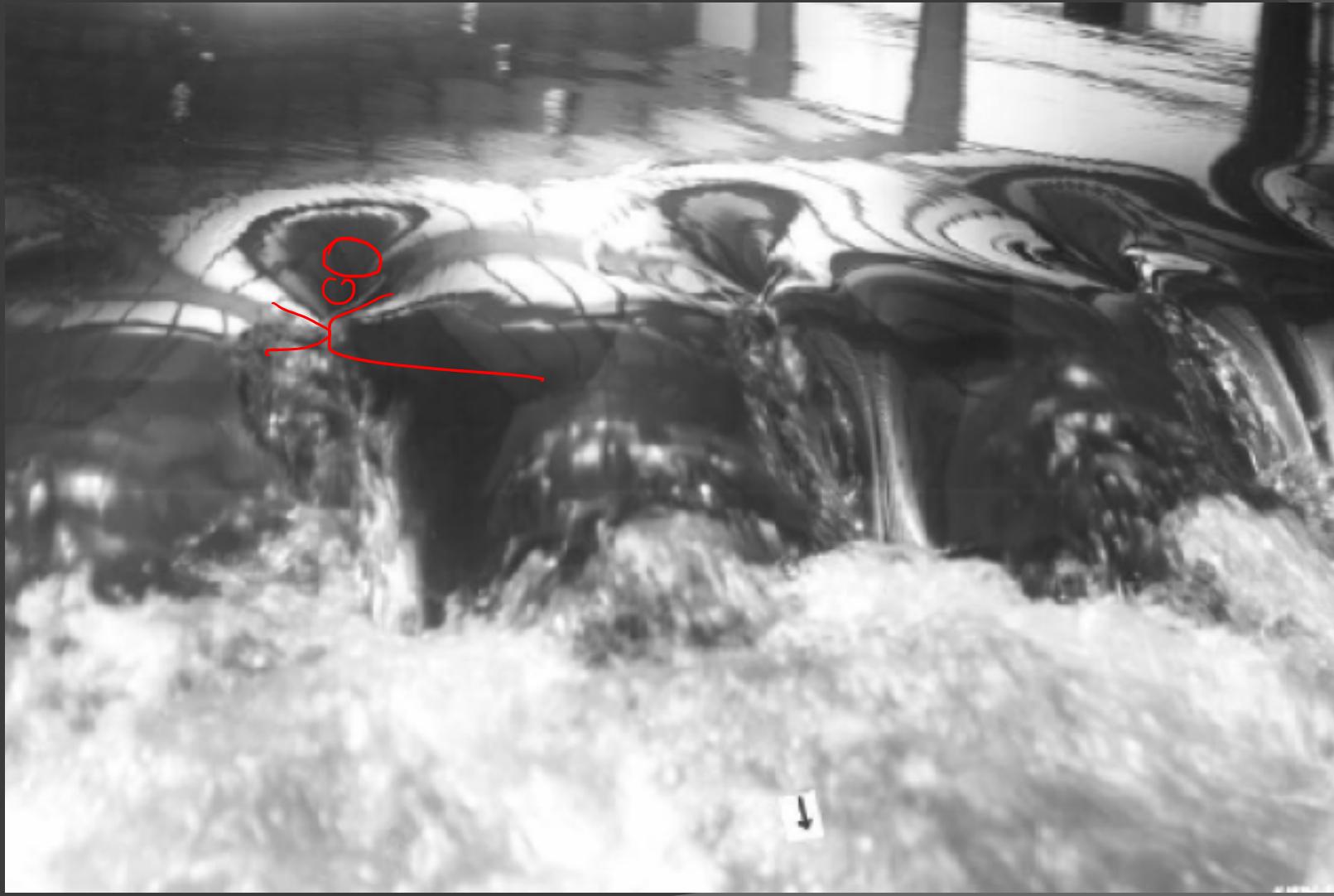
flood'agua

0,3%









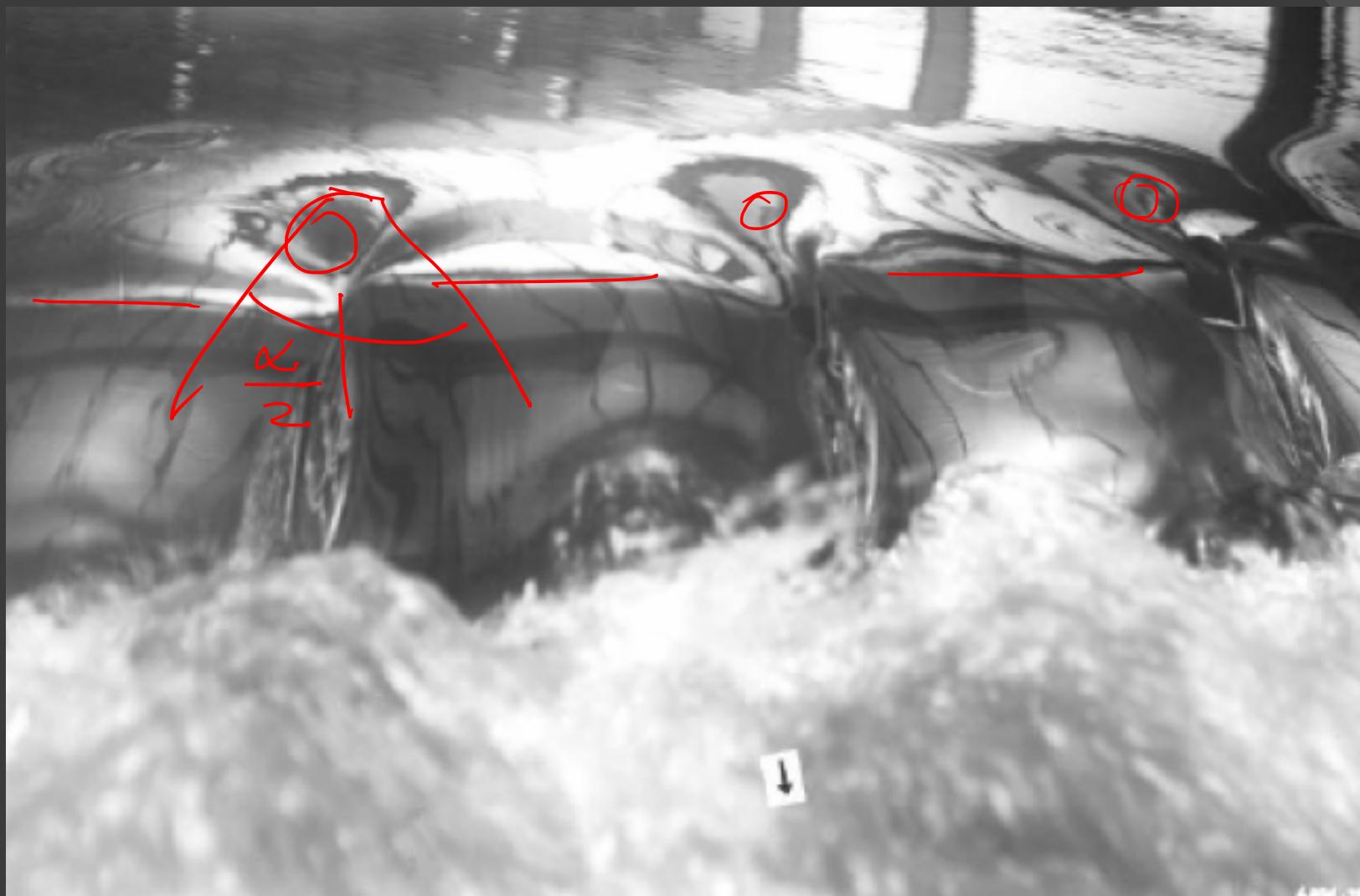
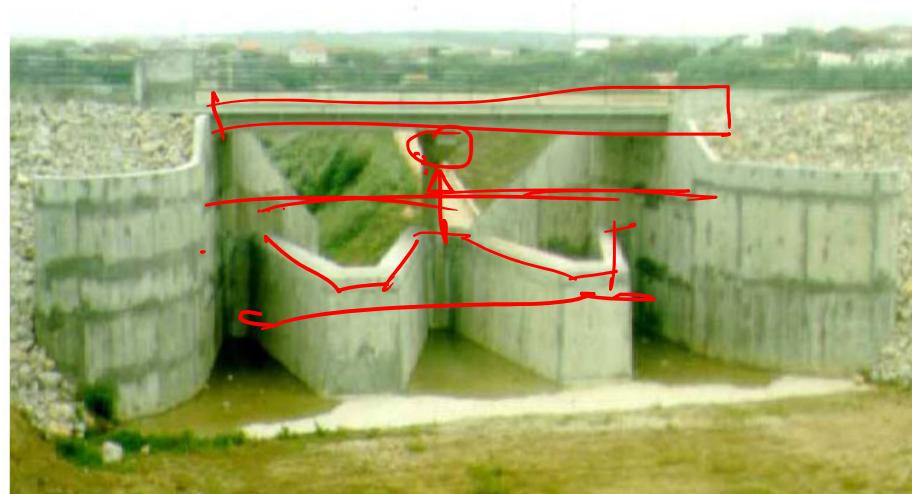
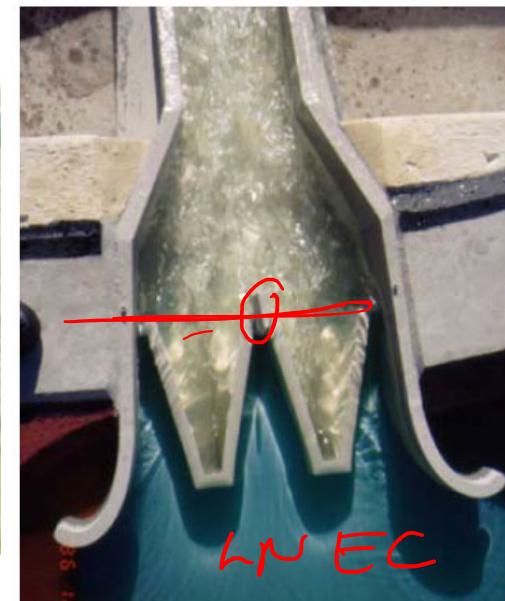


Fig. 1 - S. Domingos labyrinth spillway, Portugal (1991): a) prototype; b) physical model (courtesy of A. Pinto de Magalhães).

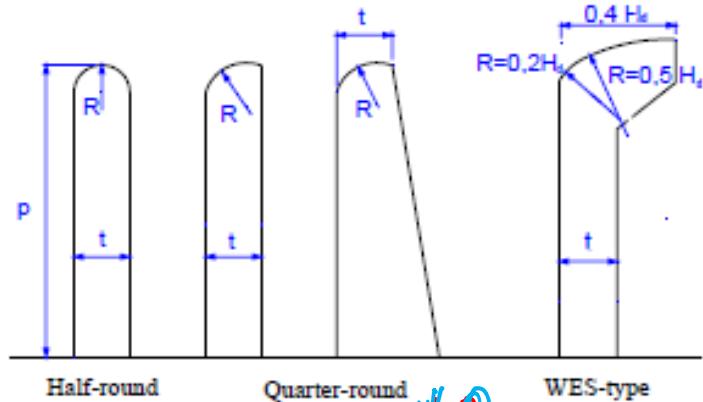


a)

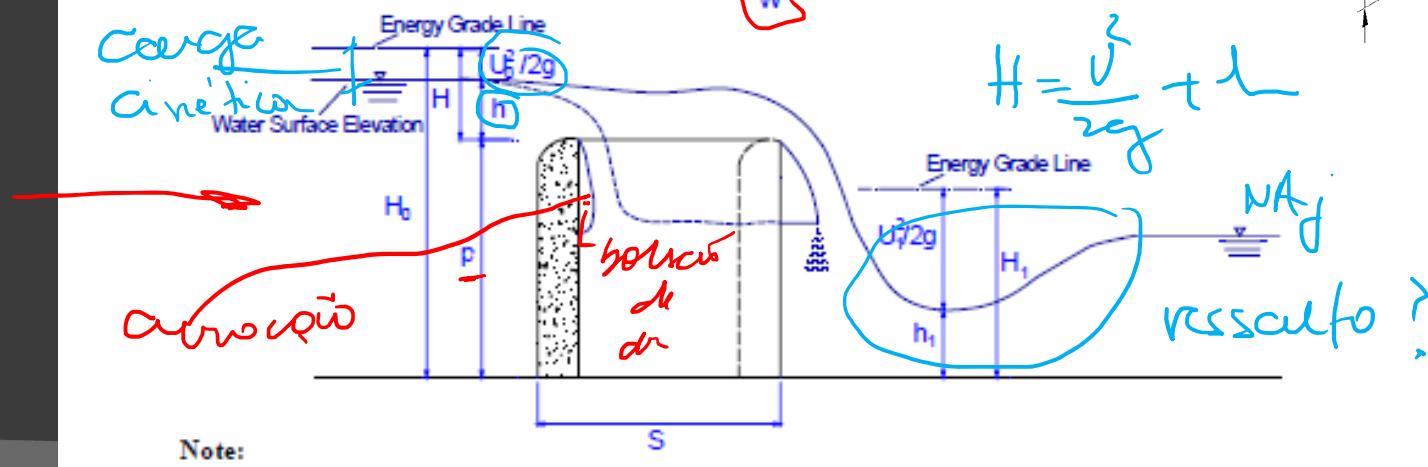
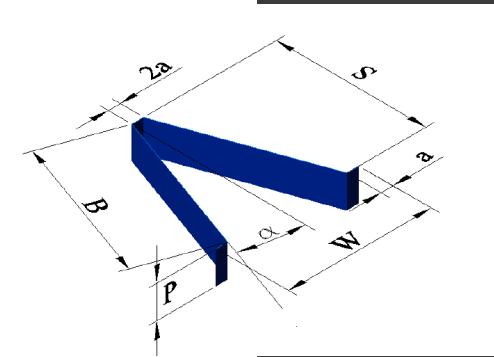
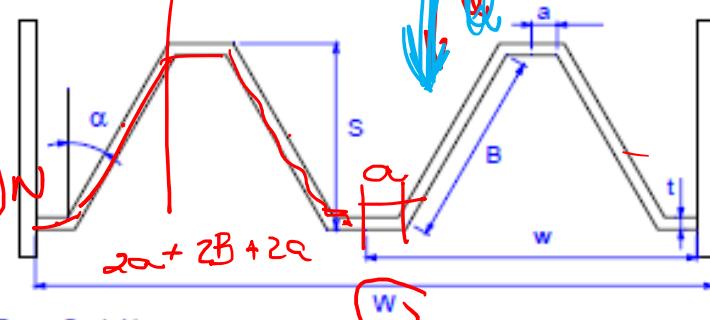


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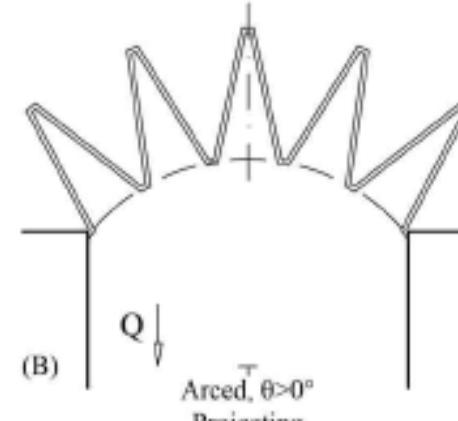
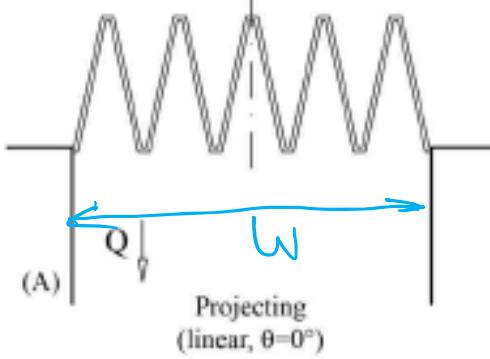




3D

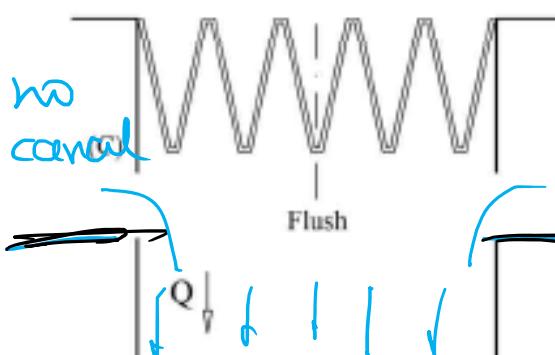


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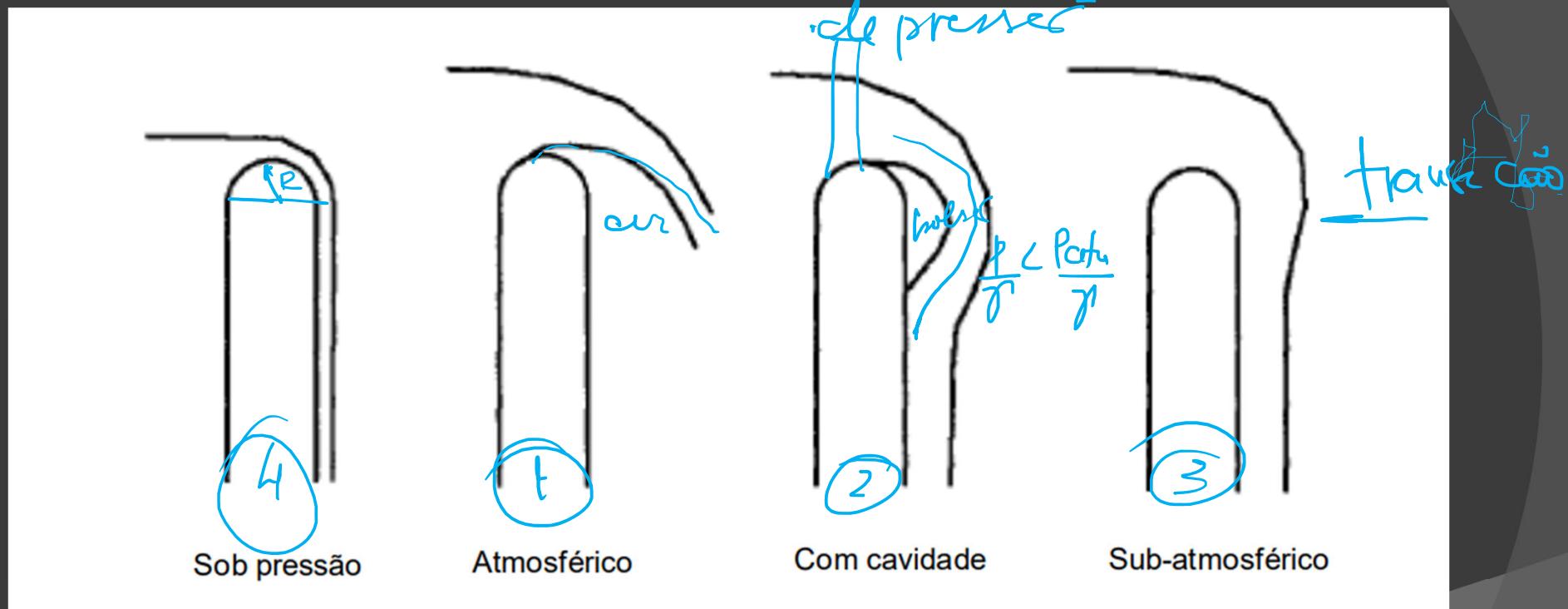
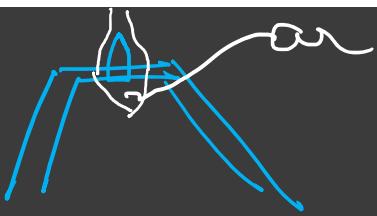
*Karim*



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Rounded Inlet

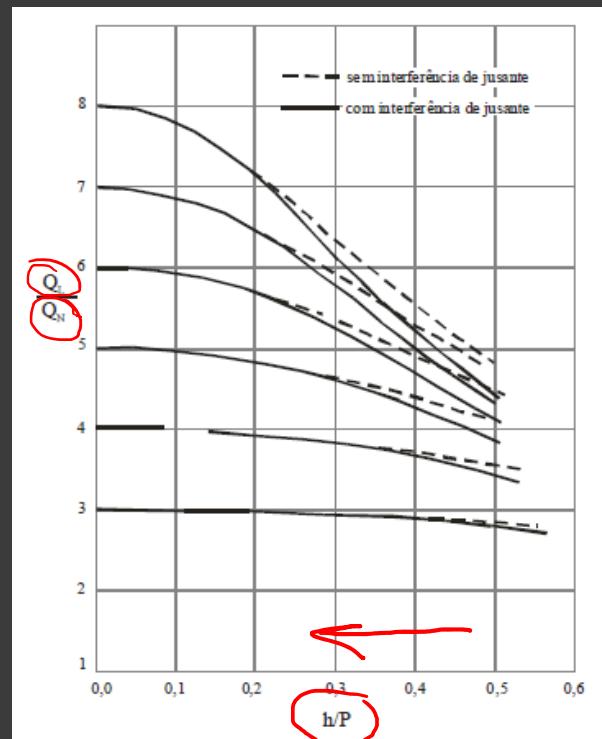


# Capacidade de Descarga

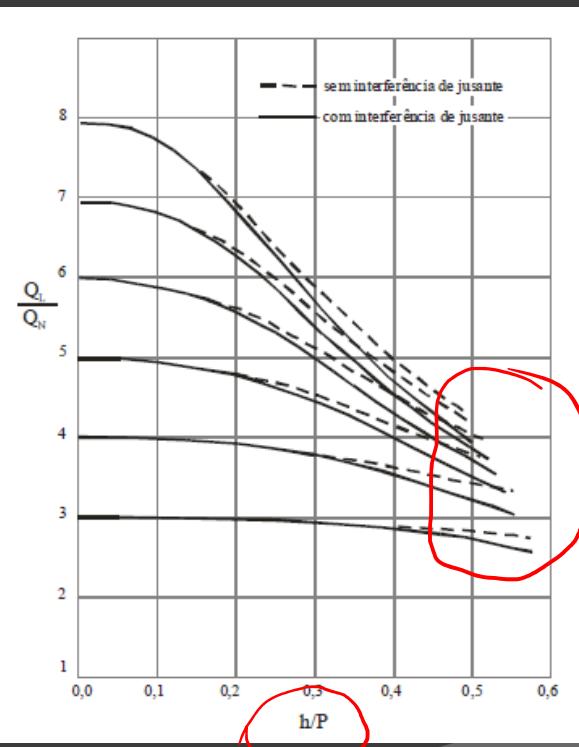
$$Q_N = C_{HT} L H^{\frac{3}{2}}$$

$$C_{HT} = 3,22 + \frac{h}{P}$$

~1905



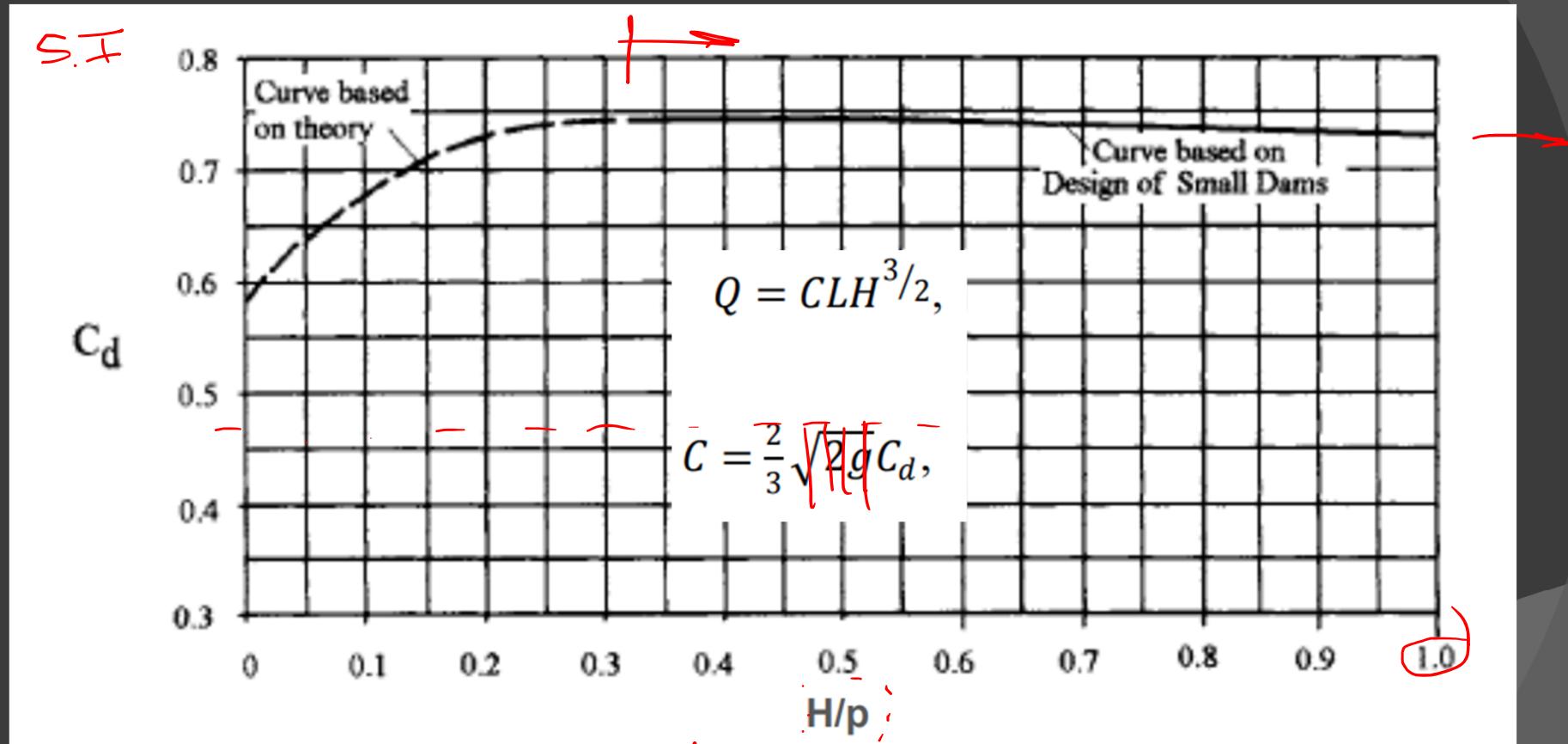
$$C_Q = \frac{2}{3} C_D \rightarrow C_Q = f(\alpha_1, \alpha_2, \dots)$$



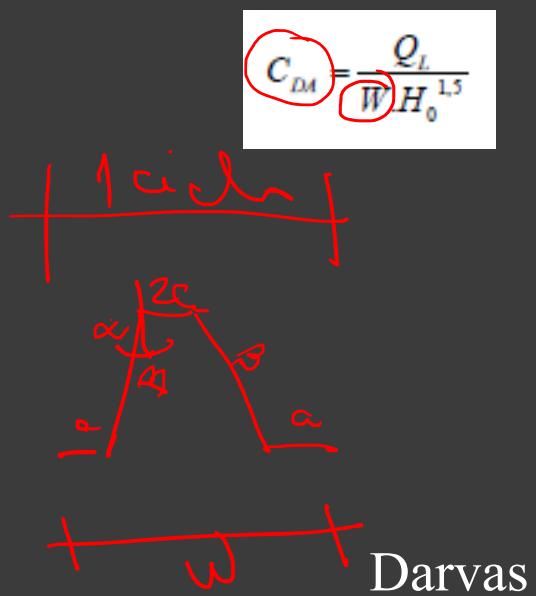
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Hayland & Taylor

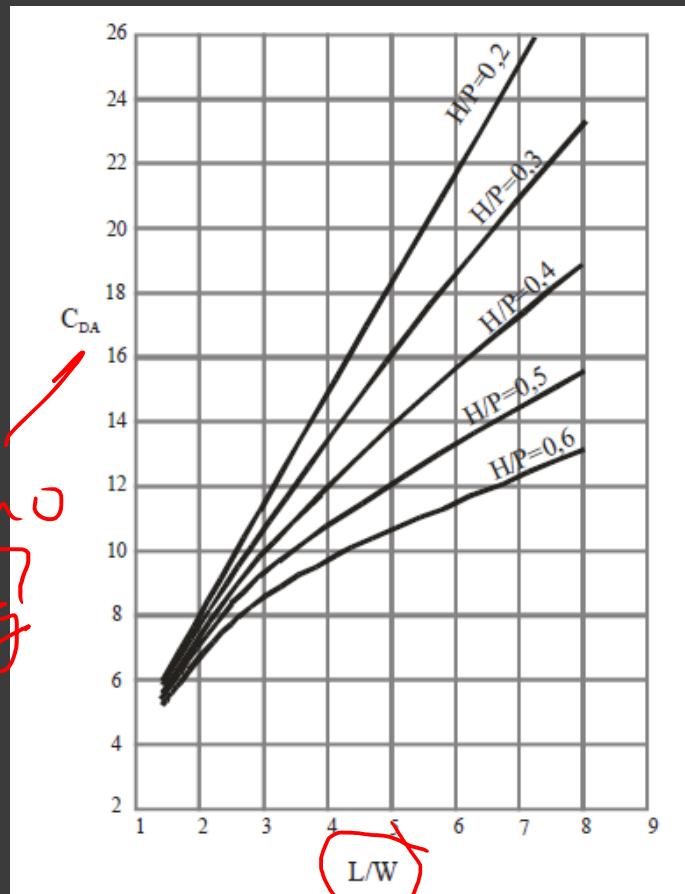
# Capacidade de descarga (USBR Small Dams)



# Capacidade de Descarga



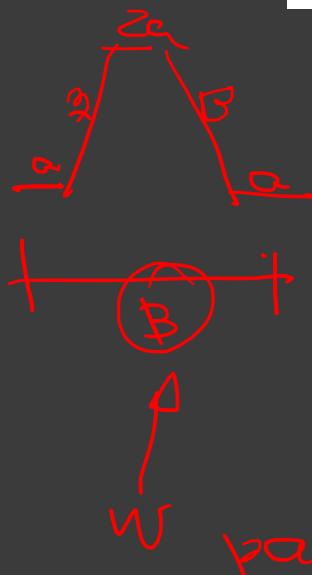
$$\frac{2}{3} \sqrt{g}$$



$$L \Rightarrow$$
$$w \Rightarrow$$
$$L = 4a + 2B$$

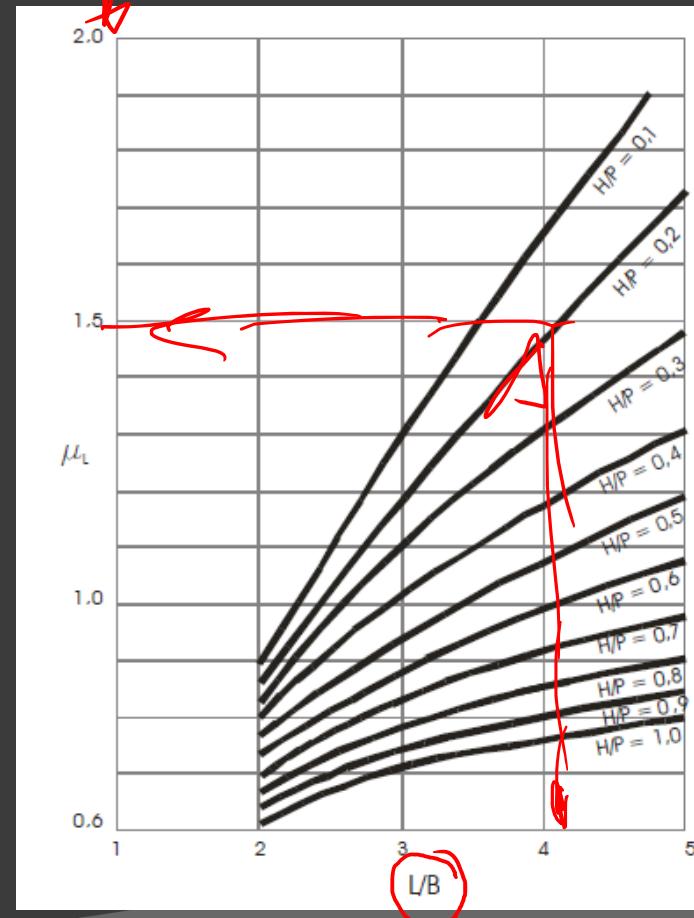
# Capacidade de Descarga

$$\mu_L = \frac{Q}{L \sqrt{2g} H^{1.5}}$$



Magalhães & Lorena  
LNEC

para o  $V \leq B/R$

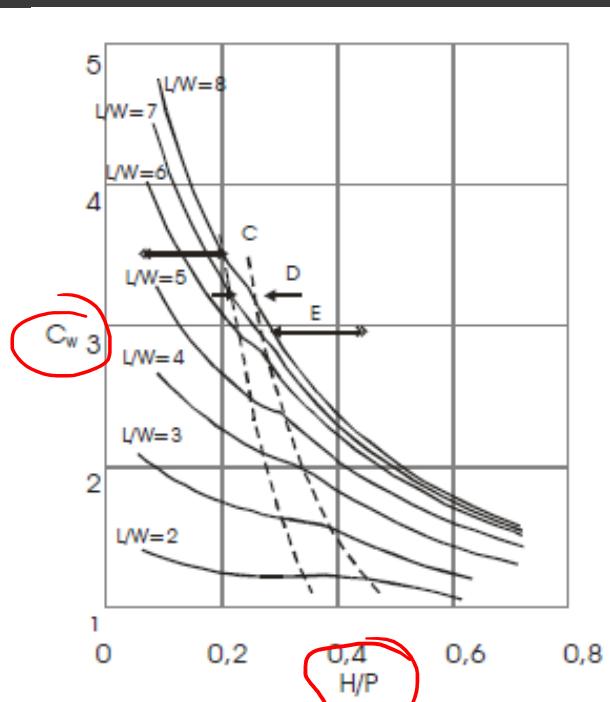
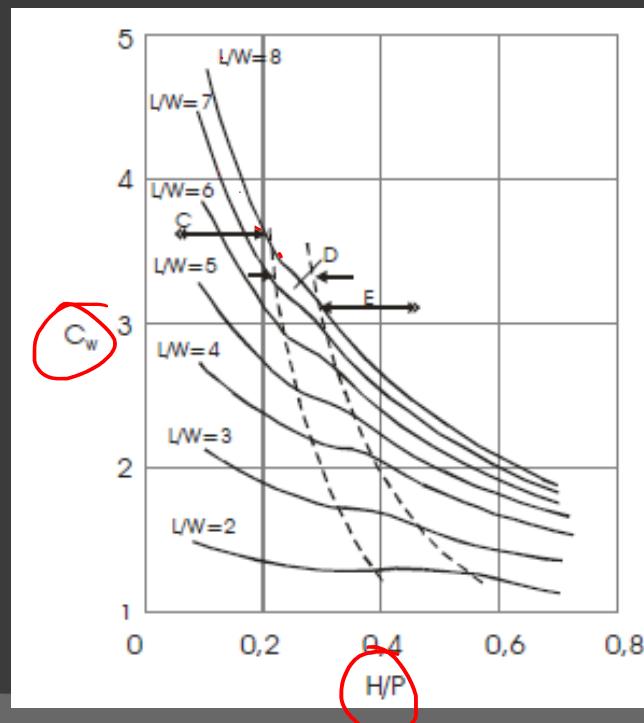


# Capacidade de Descarga

*2 g/m*

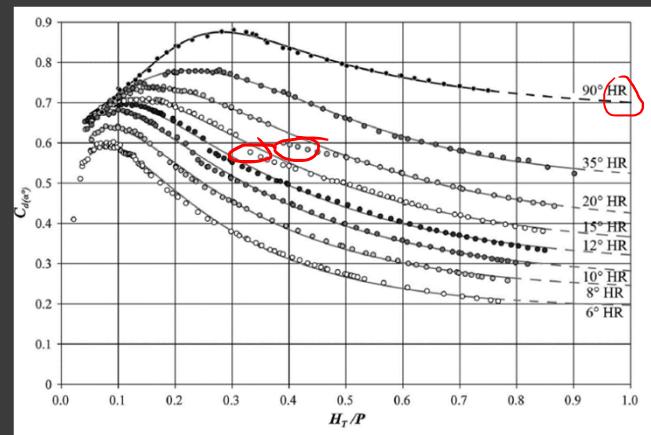
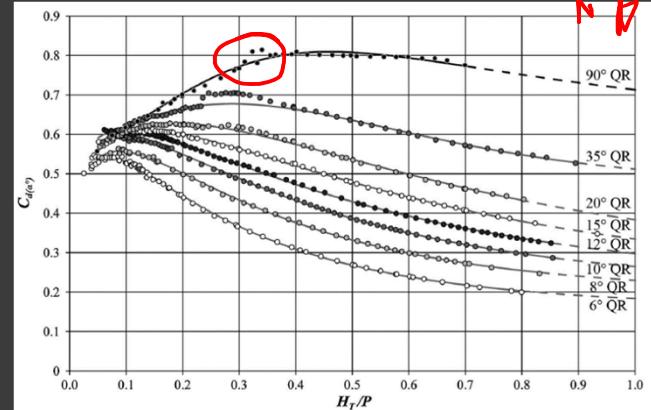
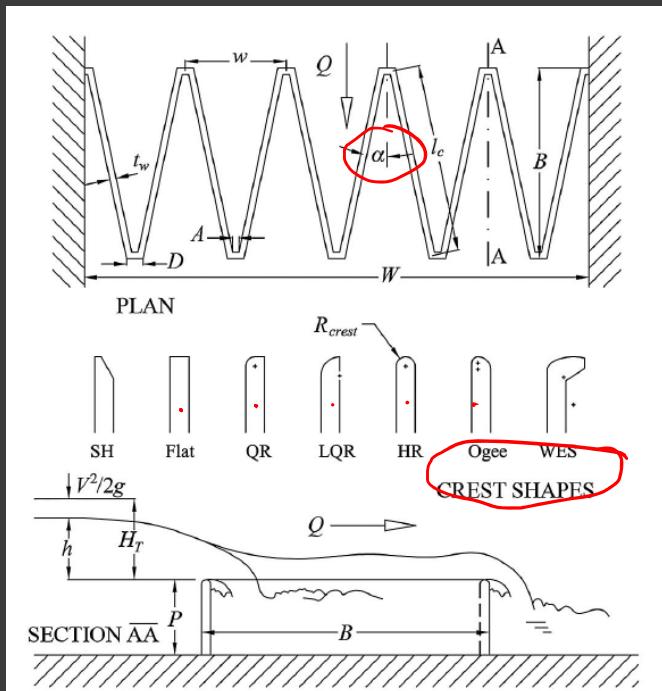
$$Q = C_w \left( \frac{W}{\frac{W}{P} + k} \right) W H \sqrt{g H}, \text{ válida para } W/P \geq 2$$

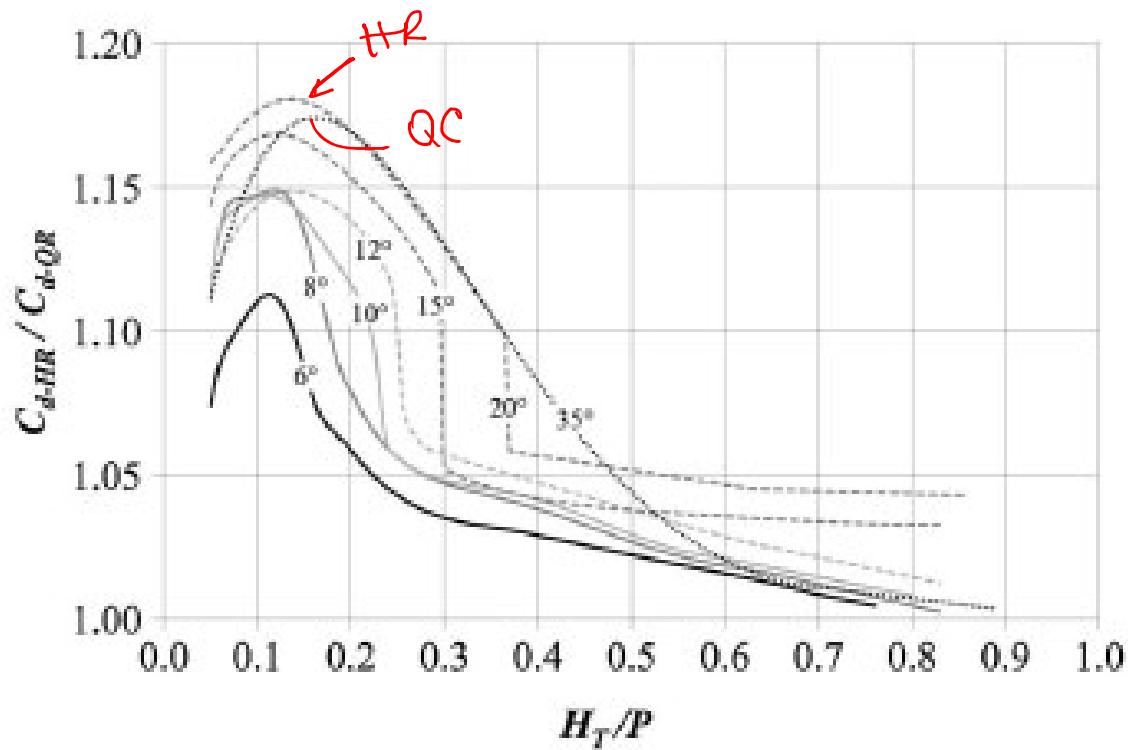
Lux & Hinchliff



# Capacidade de Descarga - Crookston &

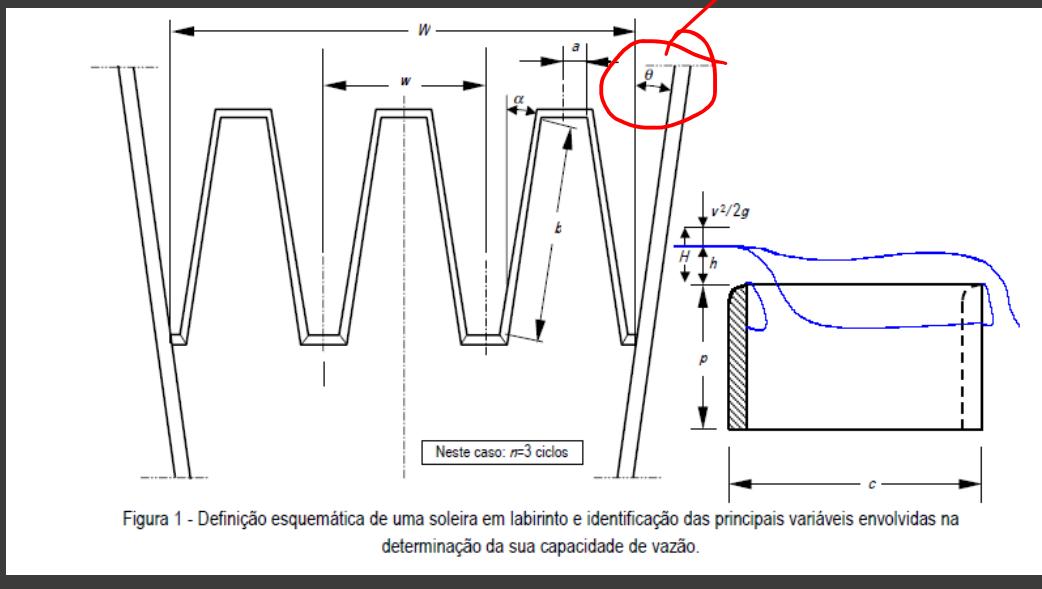
B - Tullis



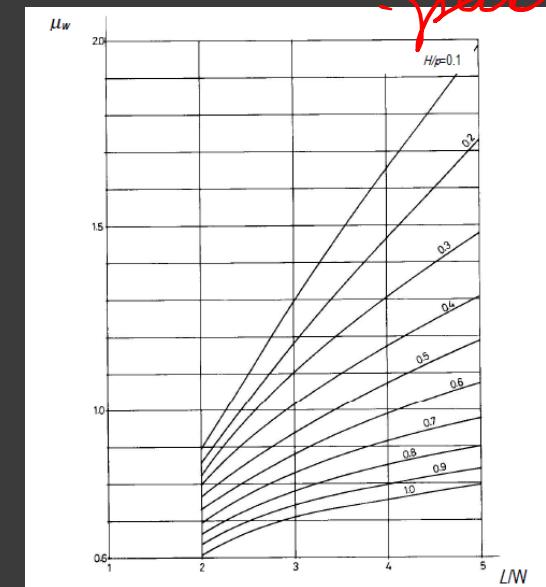


**Fig. 4.** Comparison of half-round and quarter-round crest shape on hydraulic performance of labyrinth weirs

# Paredes Convergentes

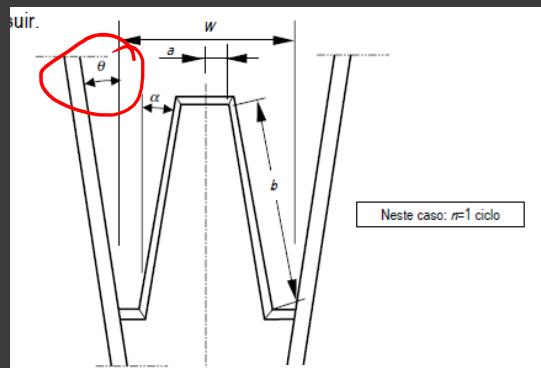


$$\mu_w = \frac{Q}{W\sqrt{2gH^{1.5}}}$$



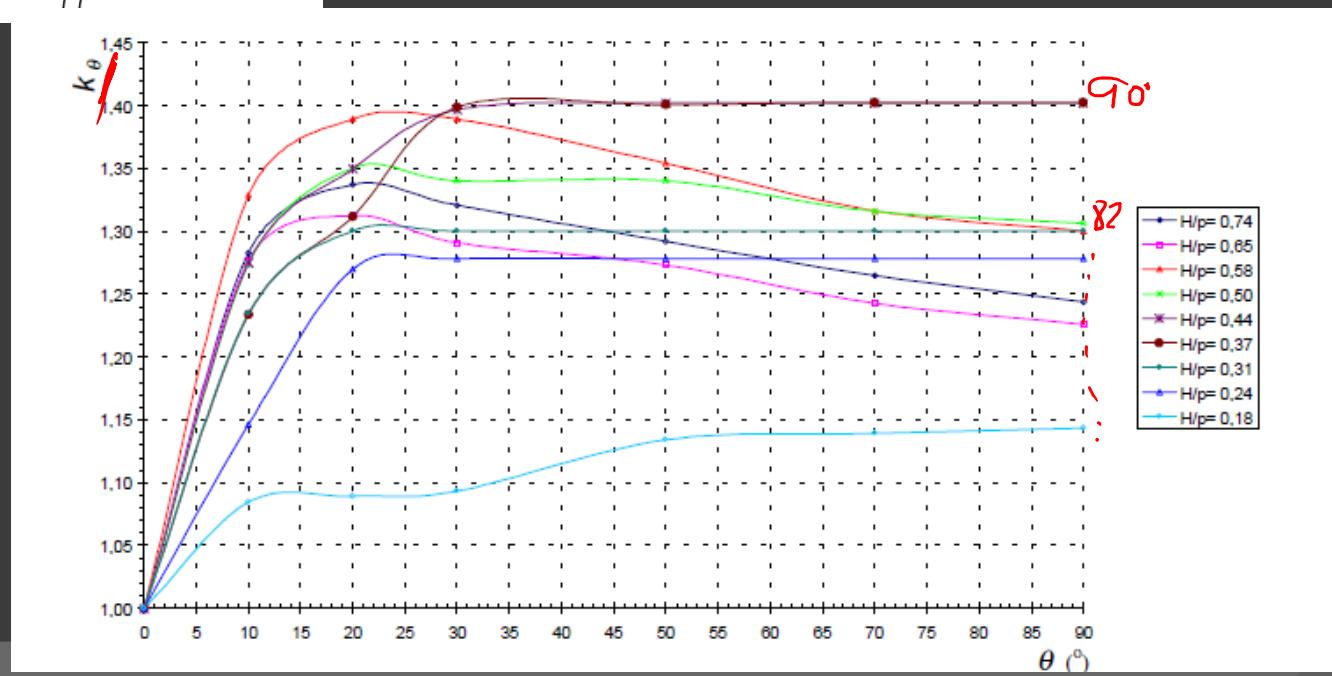
Falcão & Ramos

# Paredes Convergentes

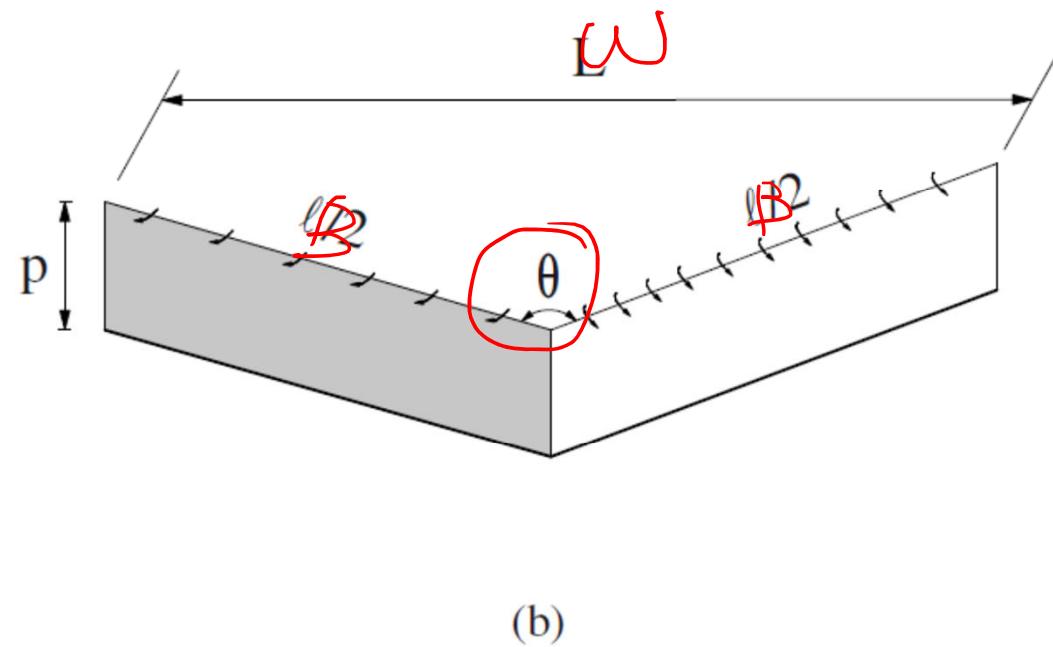
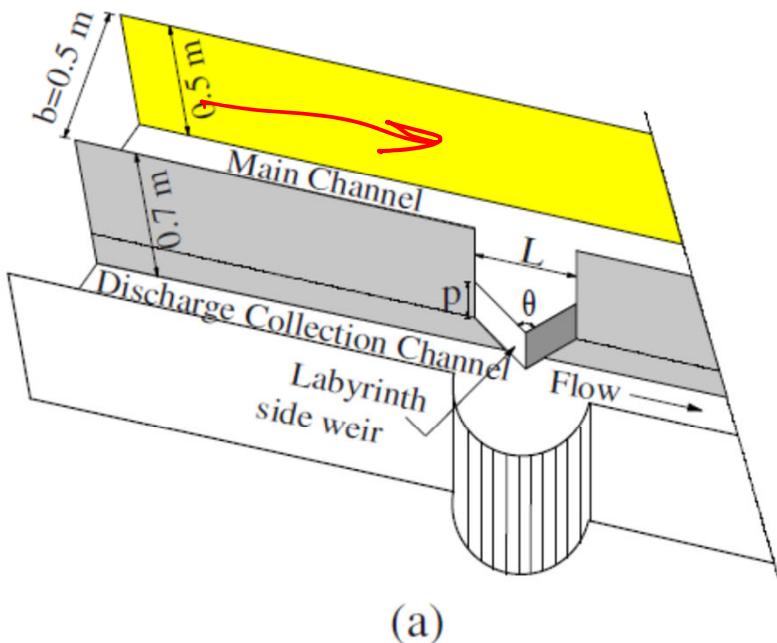


$$(2/3)$$

$$Q = K_\theta u_w W \sqrt{2gH^{1.5}}$$



# Soleira lateral labirinto (zigzag)



# Capacidade de descarga - soleira lateral regular

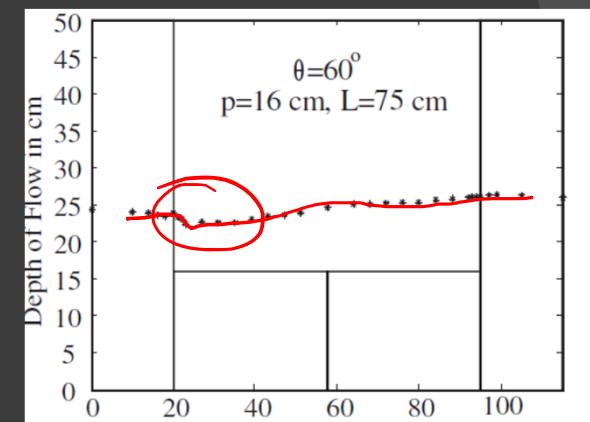
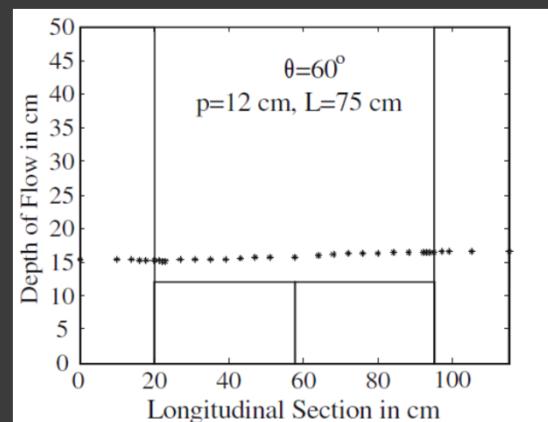
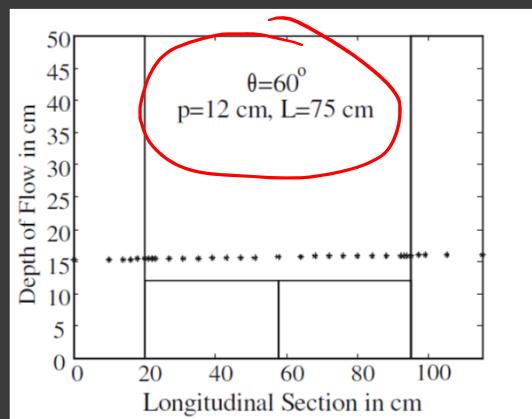
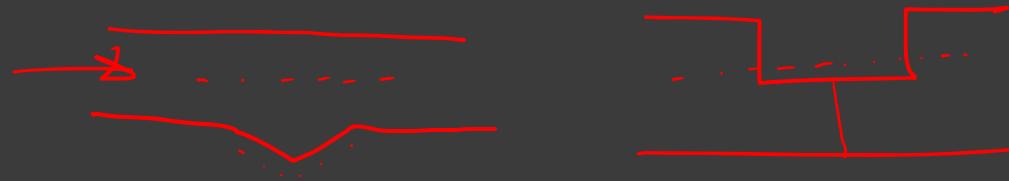
*(do seu uso passado)*

**Table 1.** Side-Weir Discharge Coefficient Equations Presented in the Literature for Straight Channels

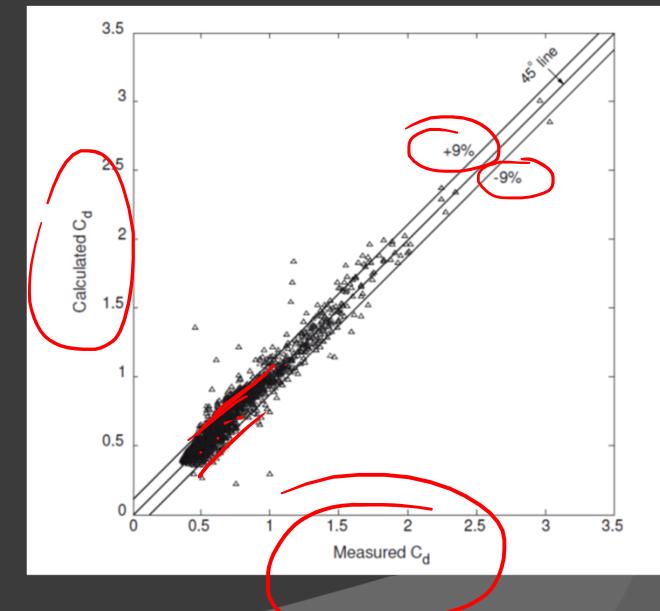
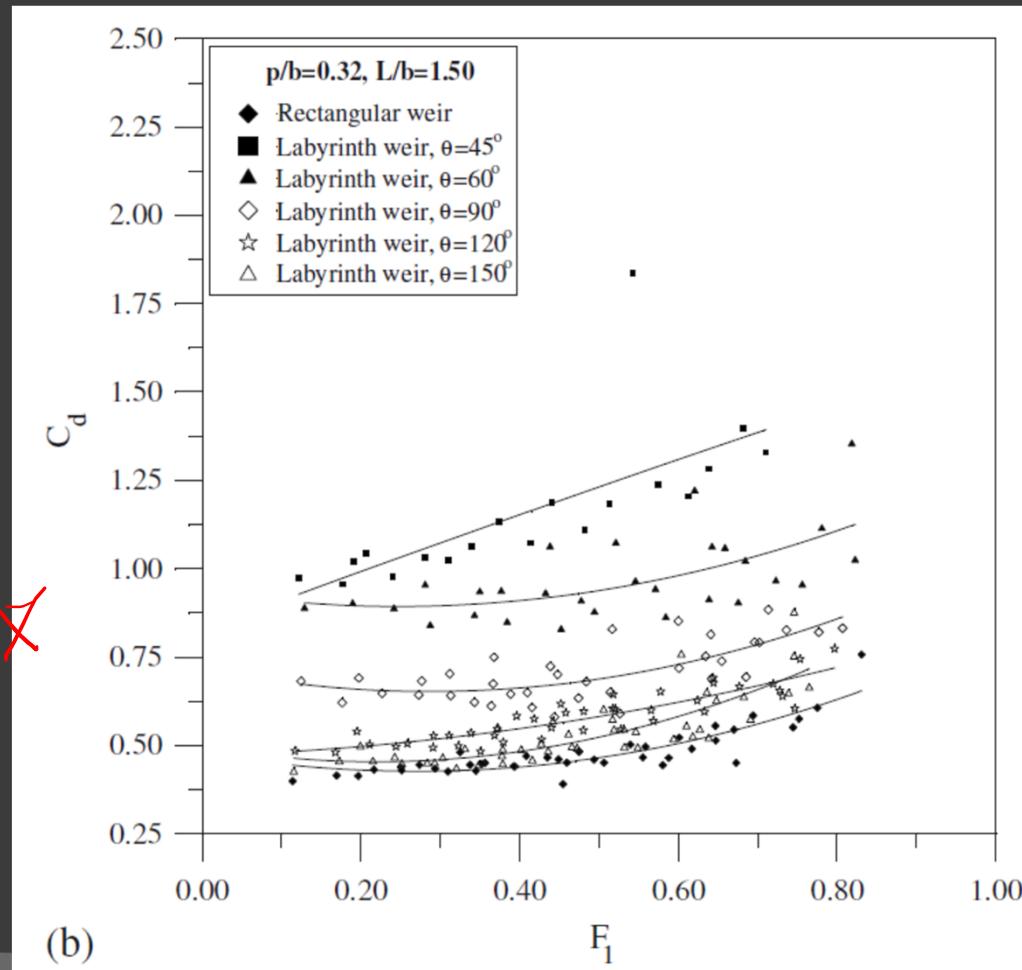
Reference	Discharge coefficient	Froude number	$L/b$	$p/h_1$
Subramanya and Awasthy (1972)	$C_d=0.864\{1-F_1^2/2+F_1^2\}^{0.5}$	0.02–0.85	0.2–1.0	0.2–0.96
Yu-Tech (1972)	$C_d=0.415-0.148F_1$	—	—	0.2–0.5
Nandesamoothy and Thomson (1972)	$C_d=0.288\{2-F_1^2/1+2F_1^2\}^{0.5}$	—	—	( $p=0.0-0.6$ m)
Ranga Raju et al. (1979)	$C_d=0.54-0.40F_1$	0.10–0.50	0.10–0.70	( $p=0.2-0.5$ m)
Hager (1987)	$C_d=0.485\{2+F_1^2/2+3F_1^2\}^{0.5}$	0.0–0.87	3.33	( $p=0.0-0.2$ m)
Cheong (1991), for trapezoidal channel	$C_d=0.30-0.14F_1^2$	0.28–0.78	0.50–1.64	0.42–0.85
Singh et al. (1994)	$C_d=0.33-0.18.F_1+0.49p/h_1$	0.23–0.43	0.25–0.50	0.42–0.85
Borghei et al. (1999)	$C_d=0.7-0.48F_1-0.3p/h_1+0.06L/b$	0.1–0.9	0.67–2.33	( $p=0.01-0.19$ m)



# Linhos d'água e perfis de velocidade

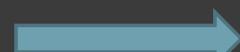


# Efeito do Número de Froude



# Capacidad de descarga combinada

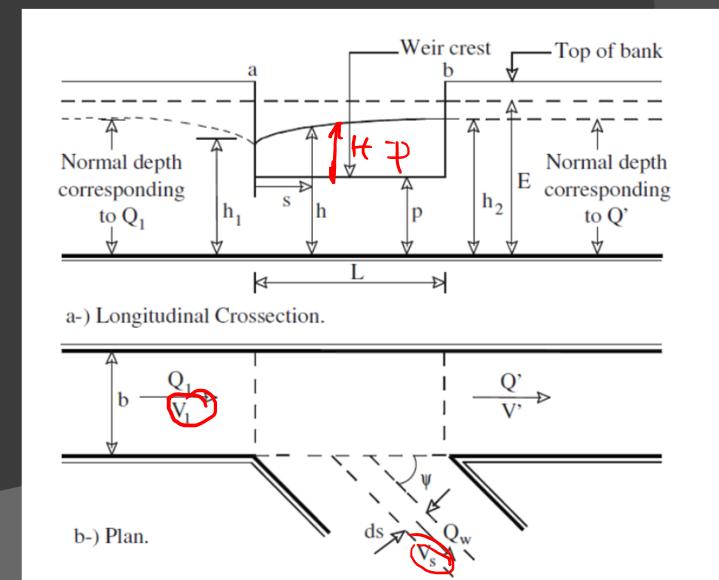
$$-\frac{dQ}{ds} = \frac{2}{3} C_d \sqrt{2g} [h - p]^{3/2}$$



$$C_d = f\left(F_1 = \frac{V_1}{\sqrt{gh_1}}, \frac{L}{b}, \frac{L}{h_1}, p/h_1, \psi\right)$$

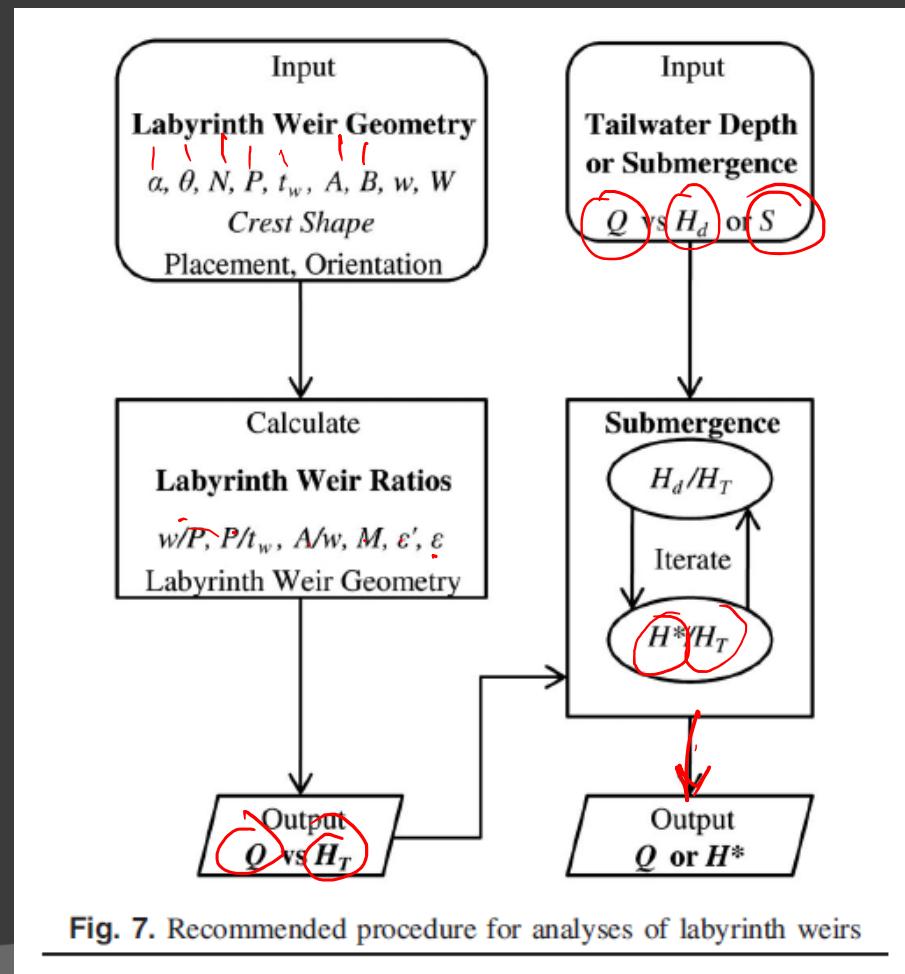
$$\sin \psi = \sqrt{1 - \left(\frac{V_1}{V_s}\right)^2}$$

$$C_d = \left[ 18.6 - 23.535 \left( \frac{L}{b} \right)^{0.012} + 6.769 \left( \frac{L}{l} \right)^{0.112} - 0.502 \left( \frac{p}{h_1} \right)^{4.024} + 0.094 \sin \theta - 0.393 F_1^{2.155} \right]^{-1.431} \quad (6)$$



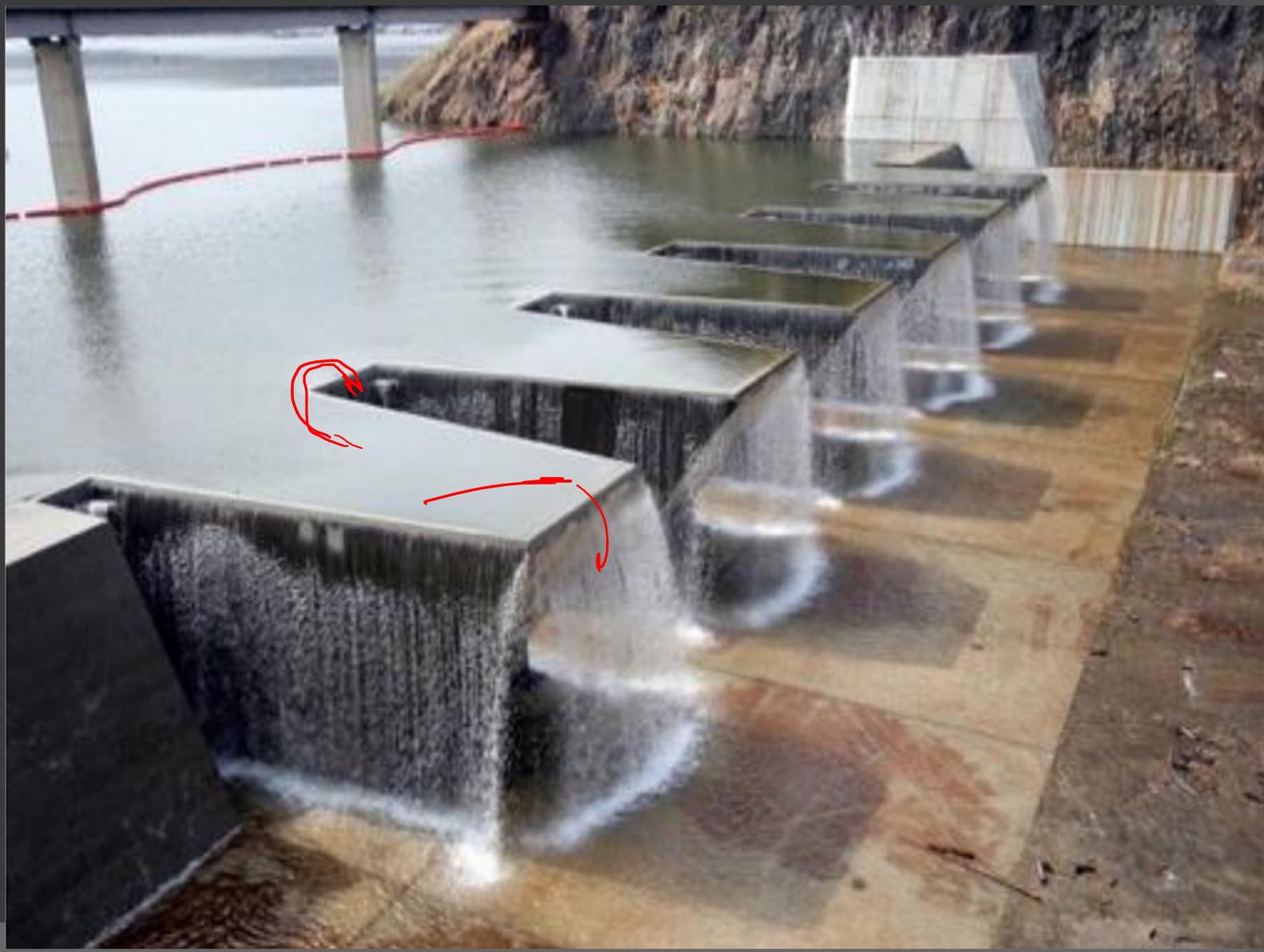
# Roteiro de Cálculo

$$B = \frac{1}{2}a + \frac{w}{2}$$

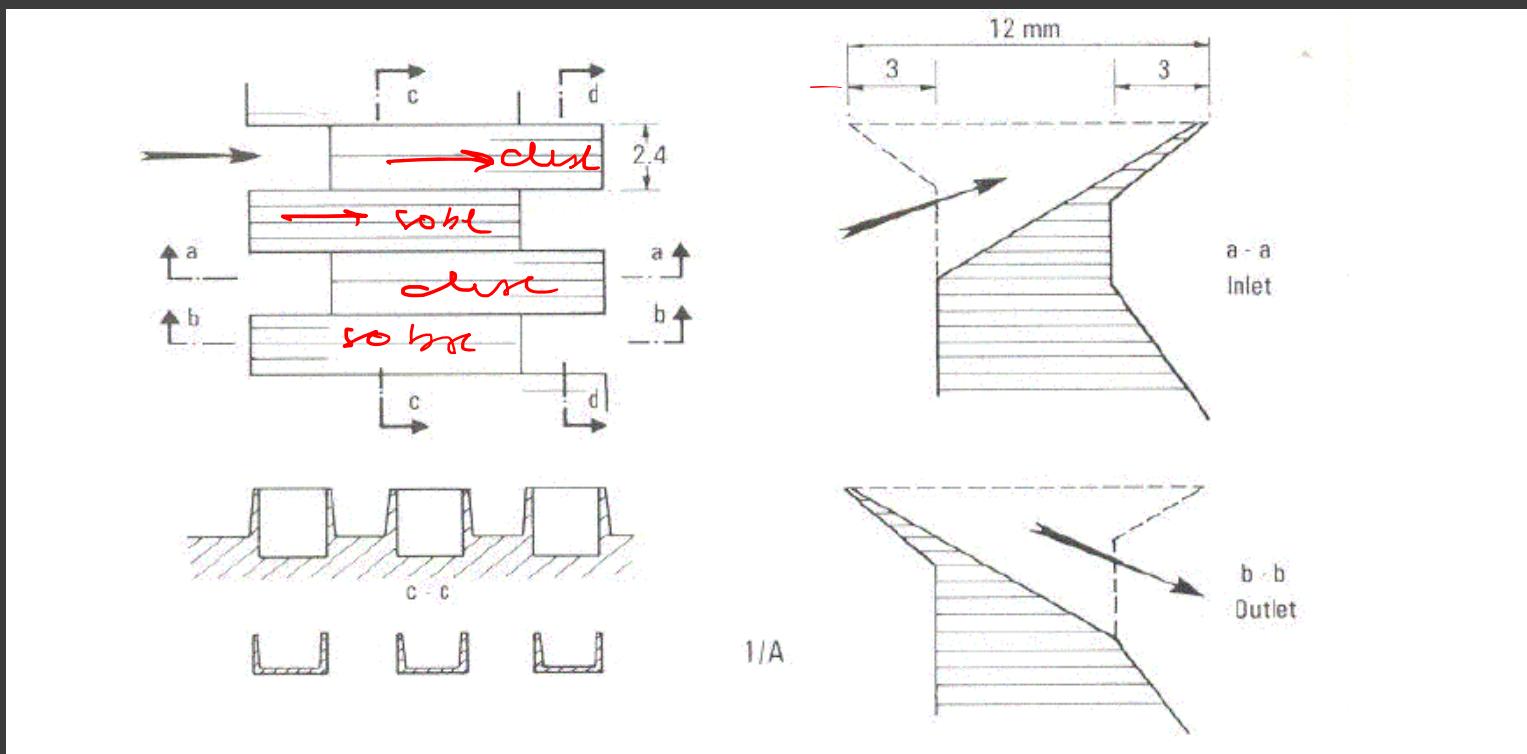


# Soleiras Piano Keys

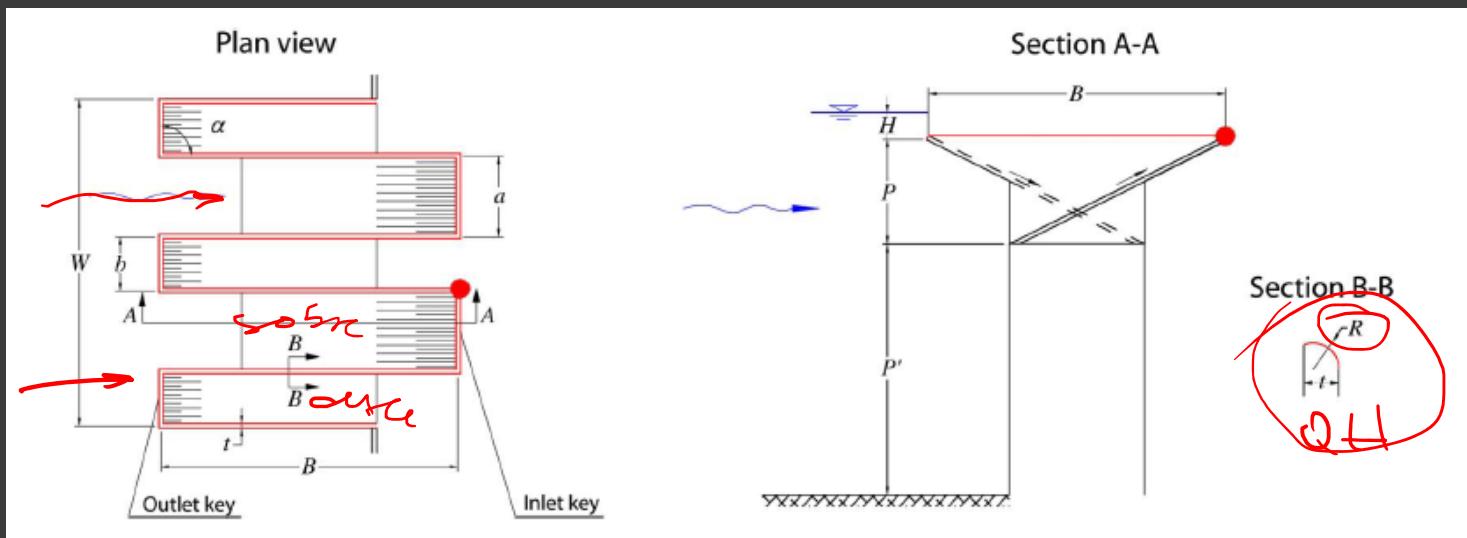




# Piano Keys



# Coeficiente de Descarga



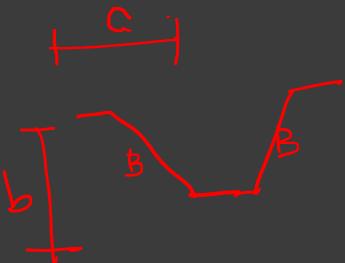
$$Q_{PKW} = f(\rho, g, \nu, \sigma, H, L, P, P', W, a, b, B, s_{in}, s_{out}, \alpha, t, R)$$

$$C_{PKW} = \frac{Q_{PKW}}{LH^{\frac{3}{2}}\sqrt{2g}}$$

$\frac{2}{3} C_D$

$$C_{PKW} = f\left(\frac{L}{W}, \frac{a}{b}, \frac{P}{P'}, \frac{t}{P'P}, \frac{H}{R}, \frac{a}{t}, s_{in}, s_{out}, F, R, W\right)$$

# Coeficiente de Descarga



$$\frac{L}{W} = \frac{a + b + 2B}{a + b}$$

$$r = \frac{Q_{PKW}}{Q_W} = \frac{C_{PKW} L H^{\frac{3}{2}} \sqrt{2g}}{C_d W H^{\frac{3}{2}} \sqrt{2g}}$$

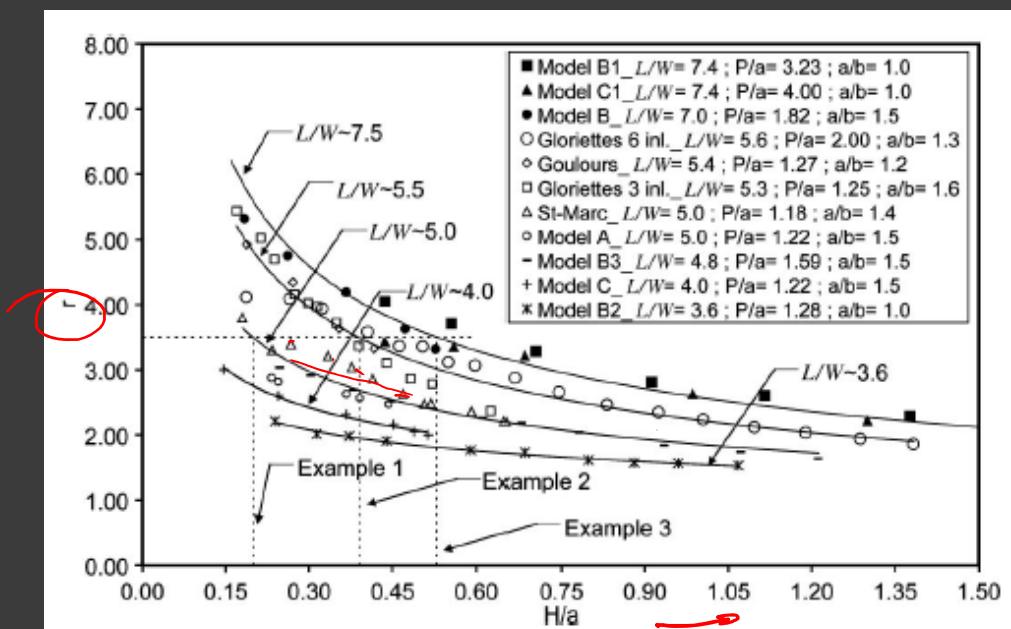


Fig. 3. Discharge enhancement ratio  $r$  as a function of  $H/a$  for different PK-Weirs and three solutions ( $L/W$ ) for a given value of  $r$

Redimensionar o vertedouro do exercício da aula 2 considerando uma necessidade de elevar a crista em 2m, reduzindo assim a carga máxima a ser observada para 1m. Dicas

Falcão & Ramos

B. Tullis

# Exercício