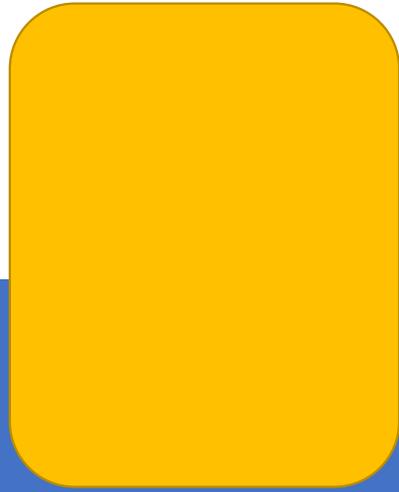
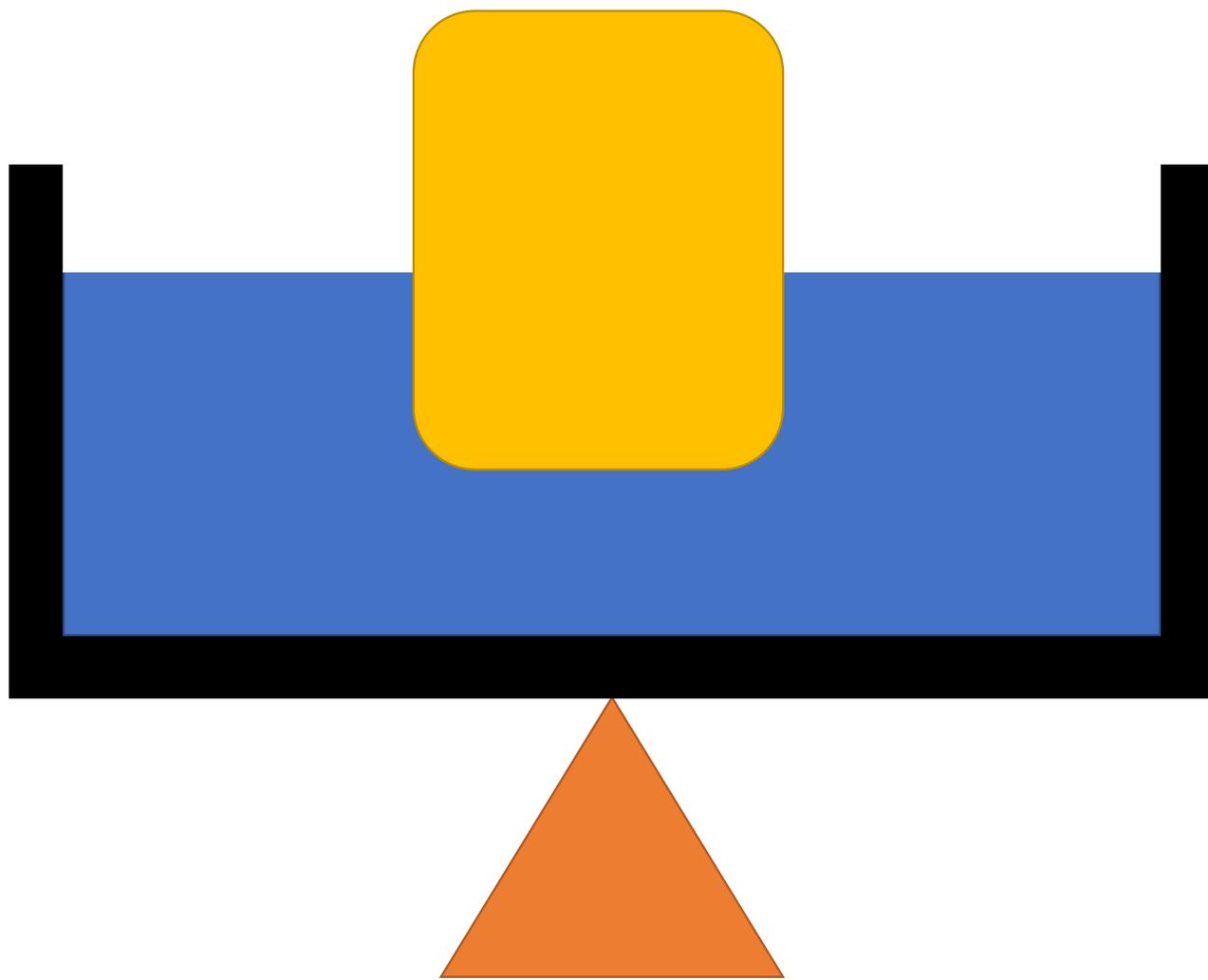


Dinâmica de Sistemas Navais e Oceânicos

PNV3314 Dinâmica de Sistemas

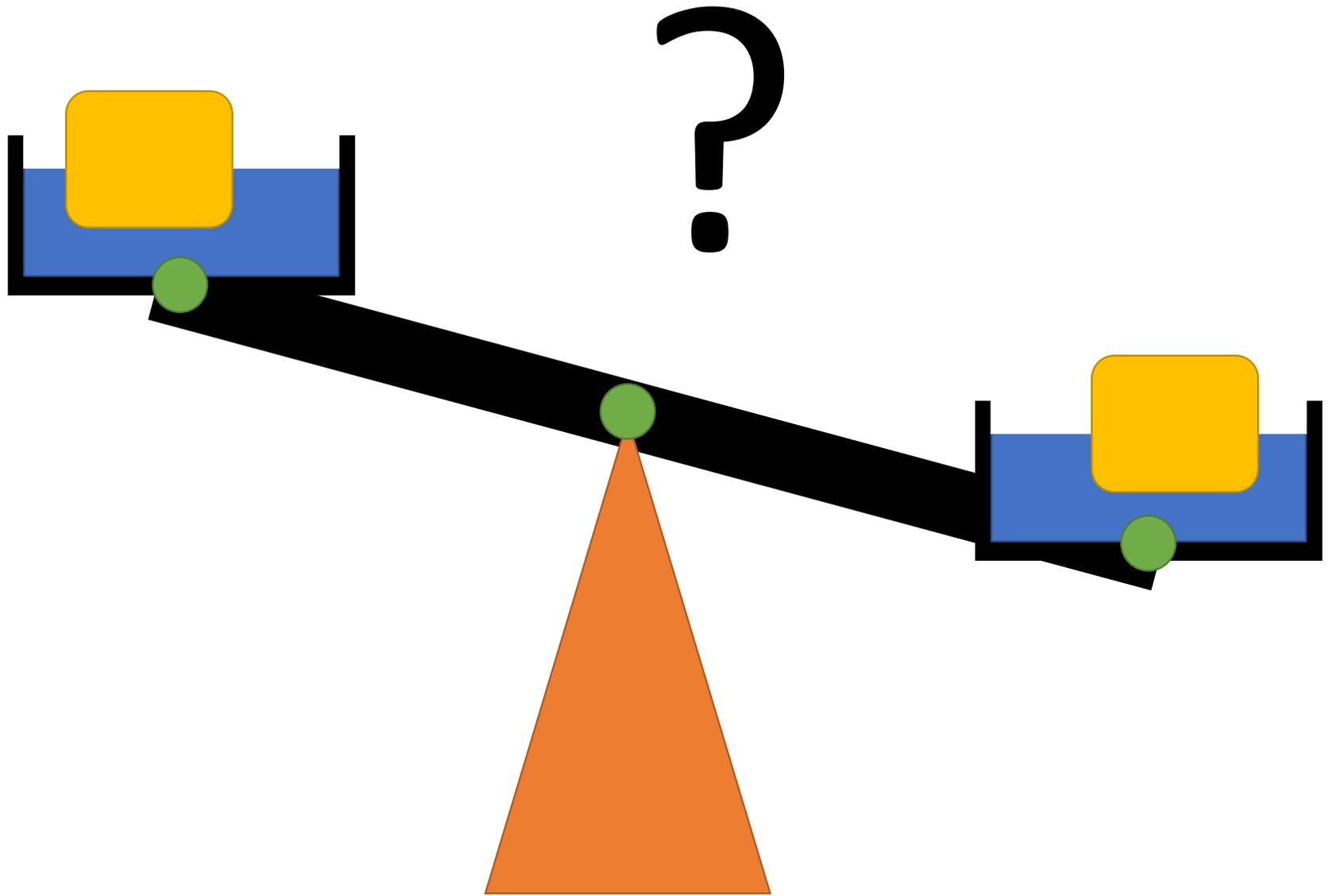
Aula 4

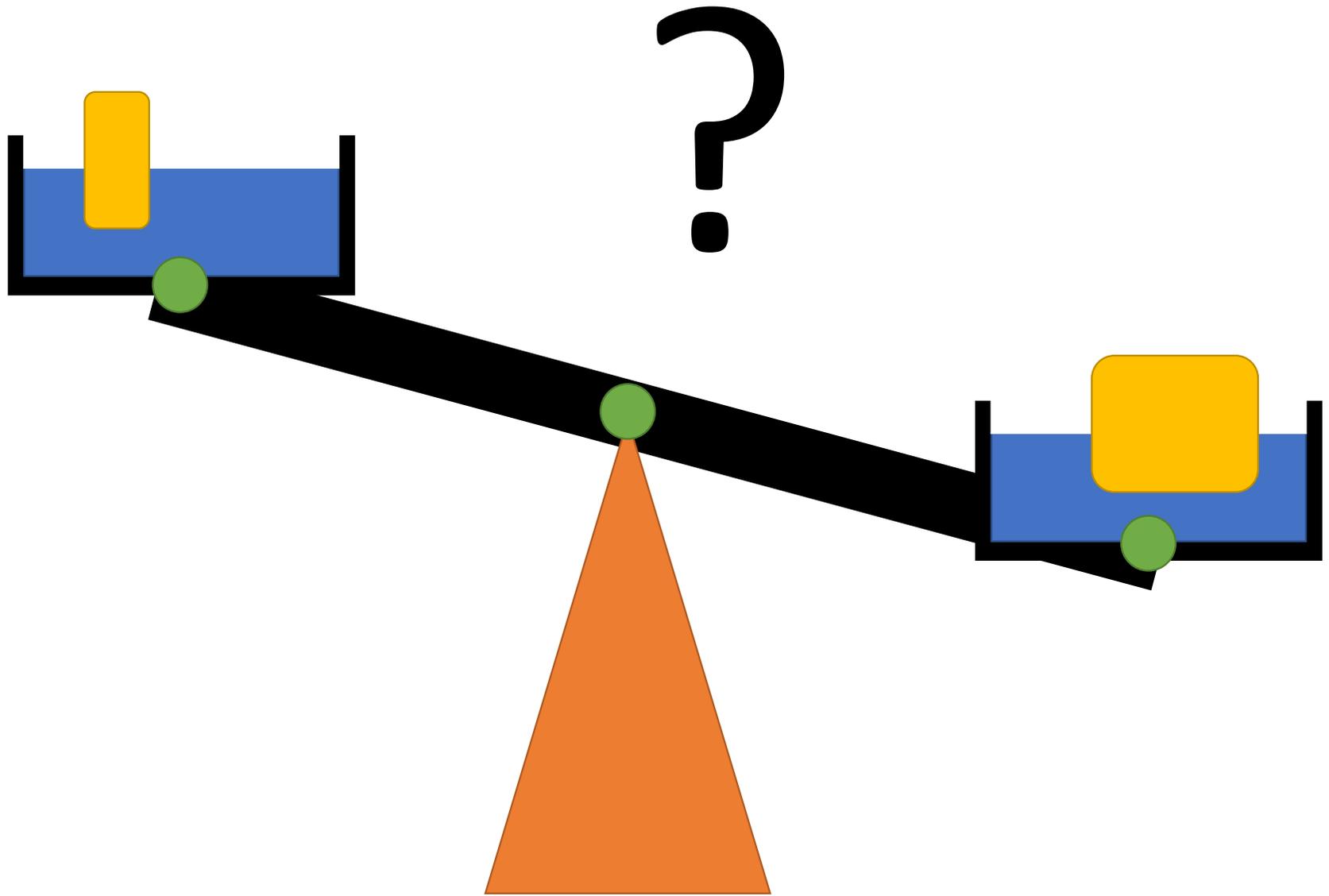


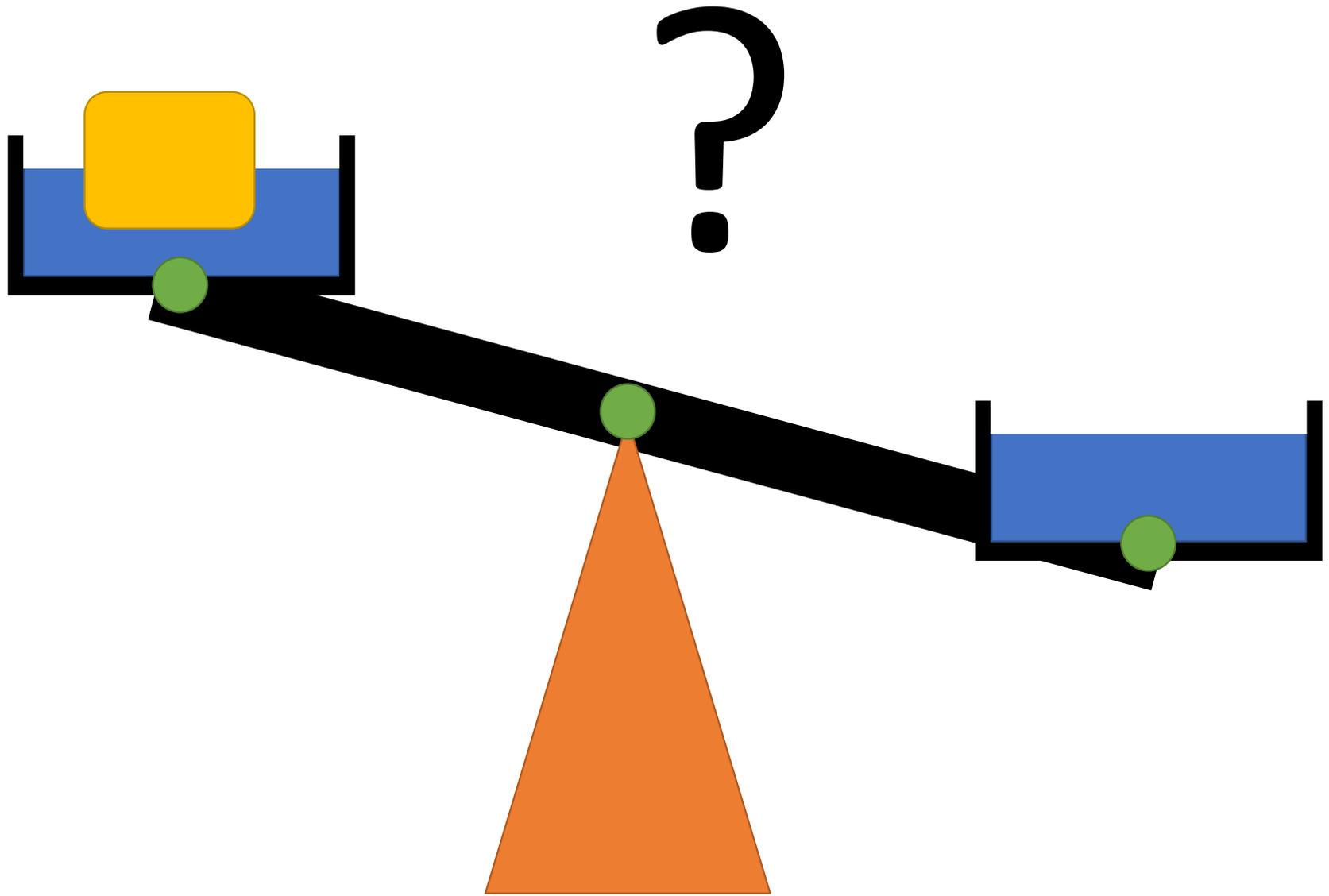


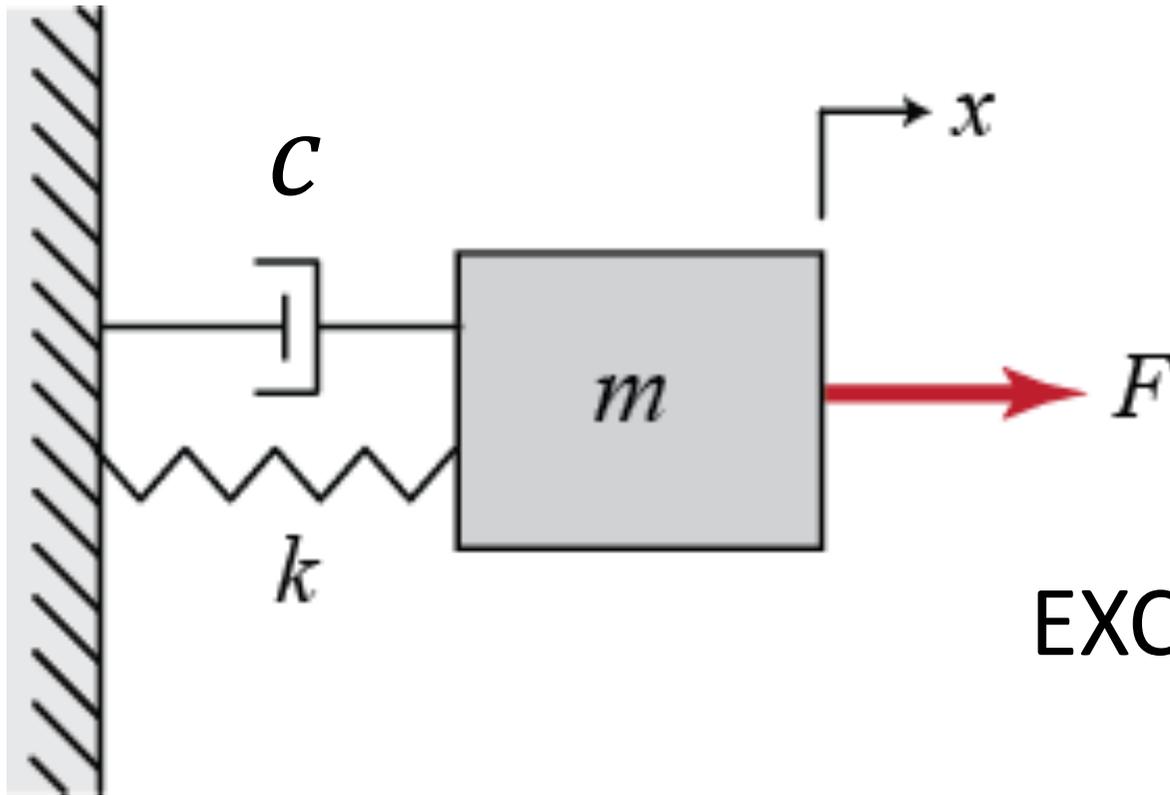












EXCITAÇÃO EXTERNA
INÉRCIA
RIGIDEZ
AMORTECIMENTO

Equação do movimento:
eq. diferencial ordinária linear de segunda ordem

$$x = x(t)$$

Derivadas de uma única
função (x) de uma
variável independente (t)

Sem produtos
entre x , \dot{x} e \ddot{x}

$$\ddot{x}(t)$$

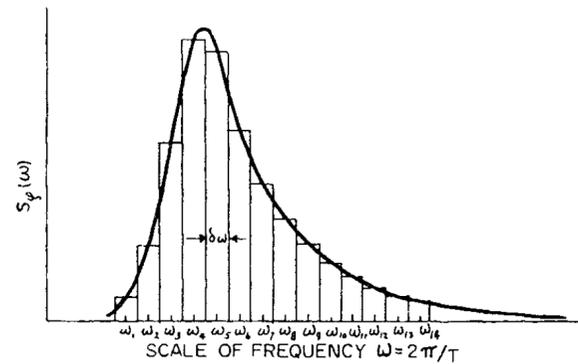
$$m\ddot{x} + c\dot{x} + kx = F(t)$$

INERCIAL

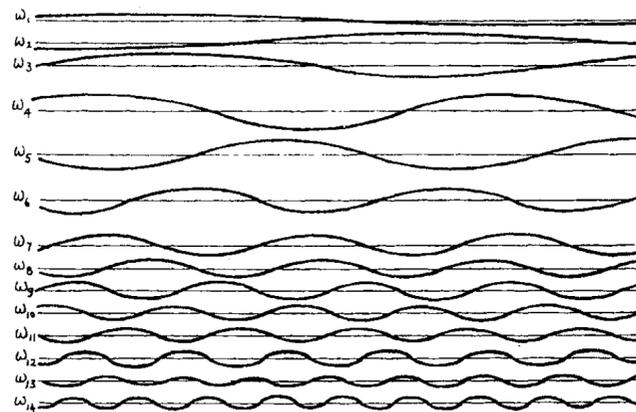
AMORTECIMENTO
(DISSIPACÃO)

RIGIDEZ
(RESTAURAÇÃO)

FORÇA EXTERNA
(EXCITAÇÃO)



(a) SPECTRUM



SCALE OF TIME OR DISTANCE

(b) COMPONENT WAVES

Fig. 8 Typical variance spectrum of waves, showing approximation by a finite sum of components

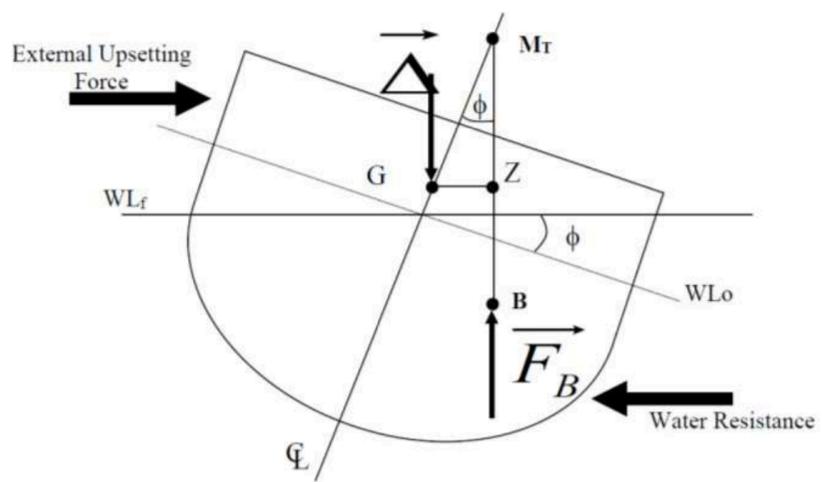


Figure 2.1: Heeled Ship due to an external moment

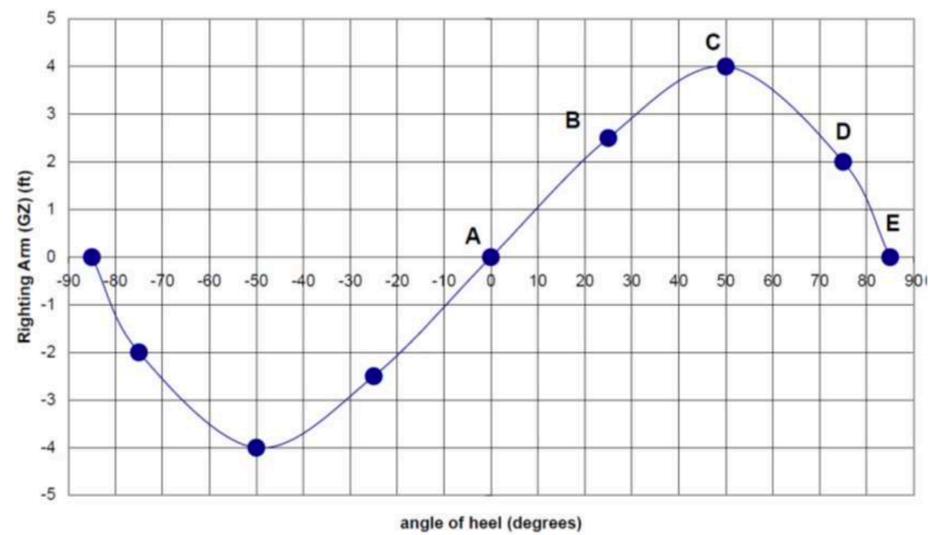
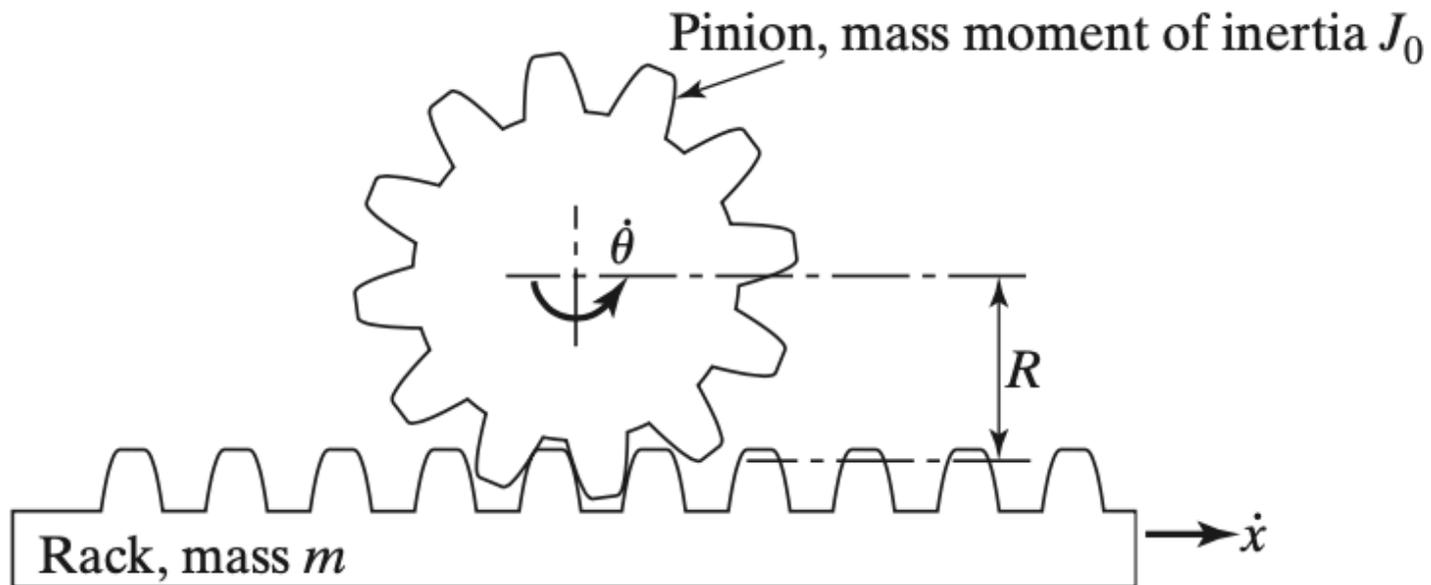
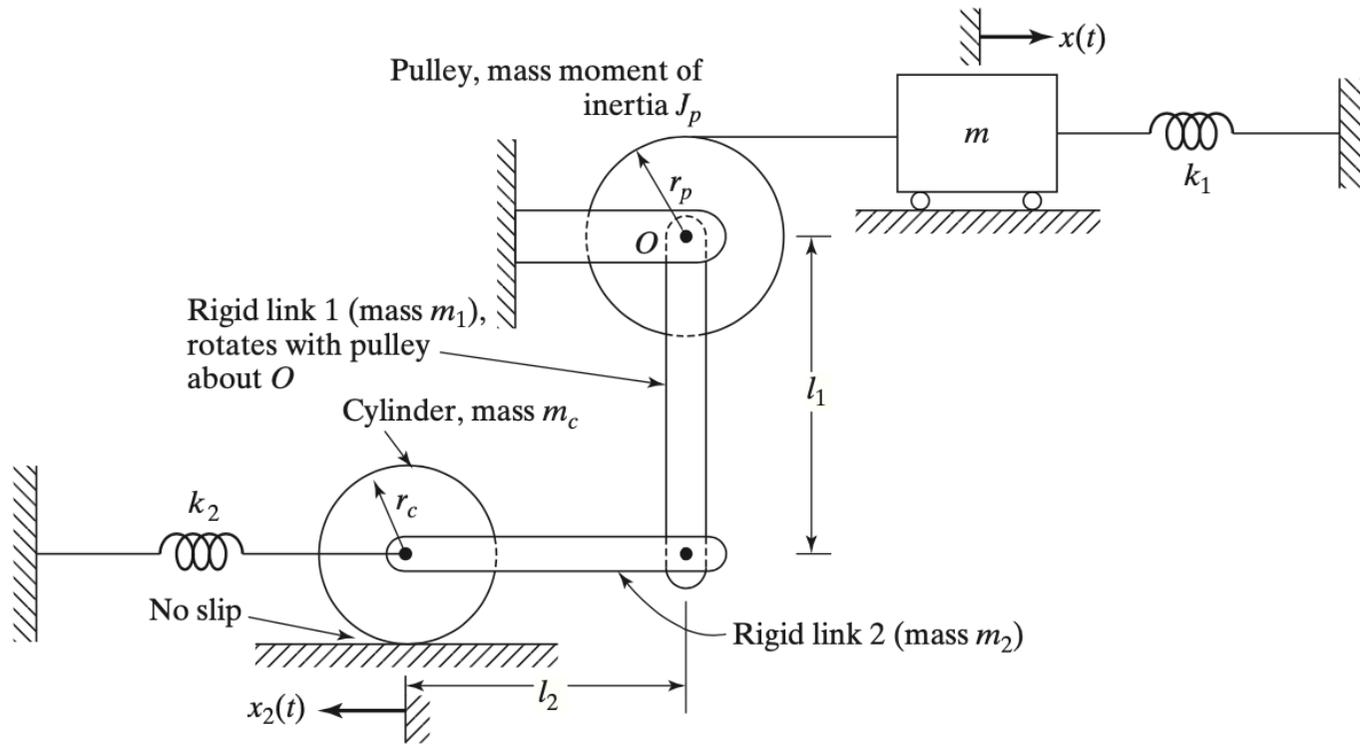


Figure 2.2: Curve of Intact Statical Stability

Inércia equivalente

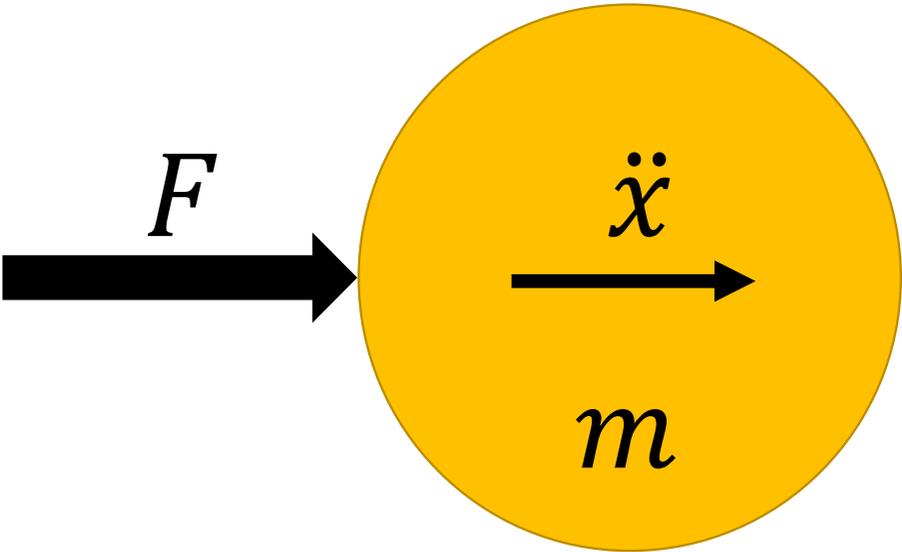


Inércia equivalente





Inércia adicional

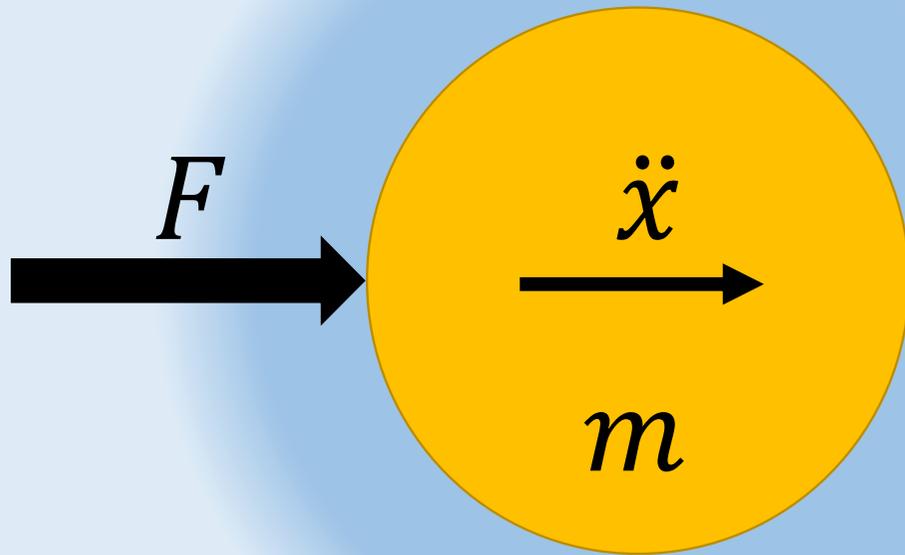


$$F = m\ddot{x}$$

NO VÁCUO



Inércia adicional



$$F = m\ddot{x} + m_a\ddot{x}$$

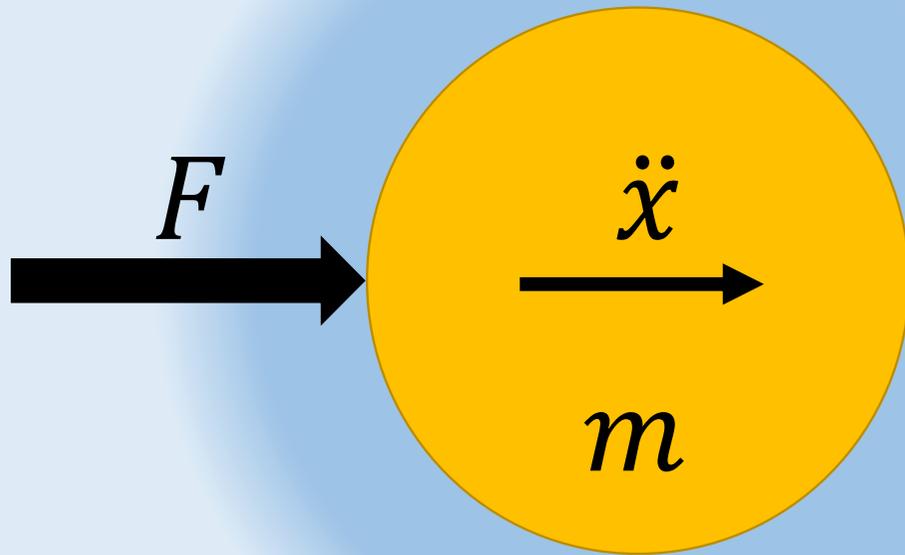
$$F = (m + m_a)\ddot{x}$$

massa adicional

NA ÁGUA



Inércia adicional



$$F = (m + m_a)\ddot{x}$$

$$\frac{m_a}{\rho V} = C_a$$

Depende da geometria do corpo e do movimento

Coeficiente de massa adicional

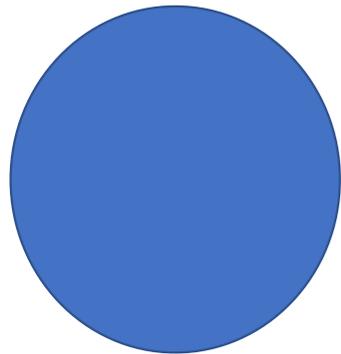
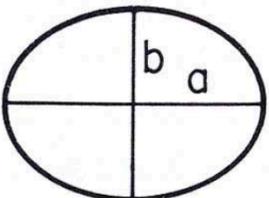
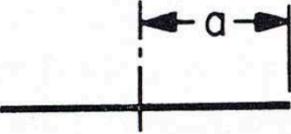
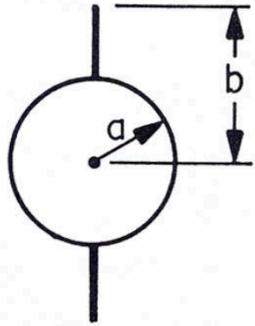
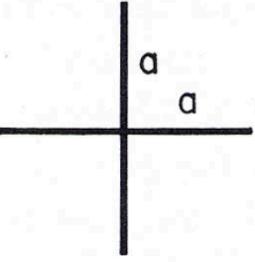
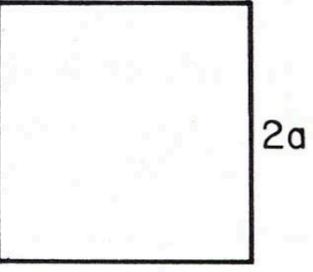
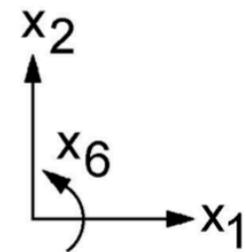


Table 4.3
 Added-Mass Coefficients for Various Two-Dimensional Bodies.

		
$m_{11}: \pi\rho a^2$ $m_{22}: \pi\rho a^2$ $m_{66}: 0$	$\pi\rho b^2$ $\pi\rho a^2$ $\frac{1}{8}\pi\rho(a^2 - b^2)^2$	0 $\pi\rho a^2$ $\frac{1}{8}\pi\rho a^4$
		
$m_{11}: \pi\rho[a^2 + (b^2 - a^2)^2/b^2]$ $m_{22}: \pi\rho a^2$ $m_{66}: *$	$\pi\rho a^2$ $\pi\rho a^2$ $\frac{2}{\pi}\rho a^4$	$4.754 \rho a^2$ $4.754 \rho a^2$ $0.725 \rho a^4$



[Newman, 1977]

*For the finned circle the added moment of inertia is given by the formula

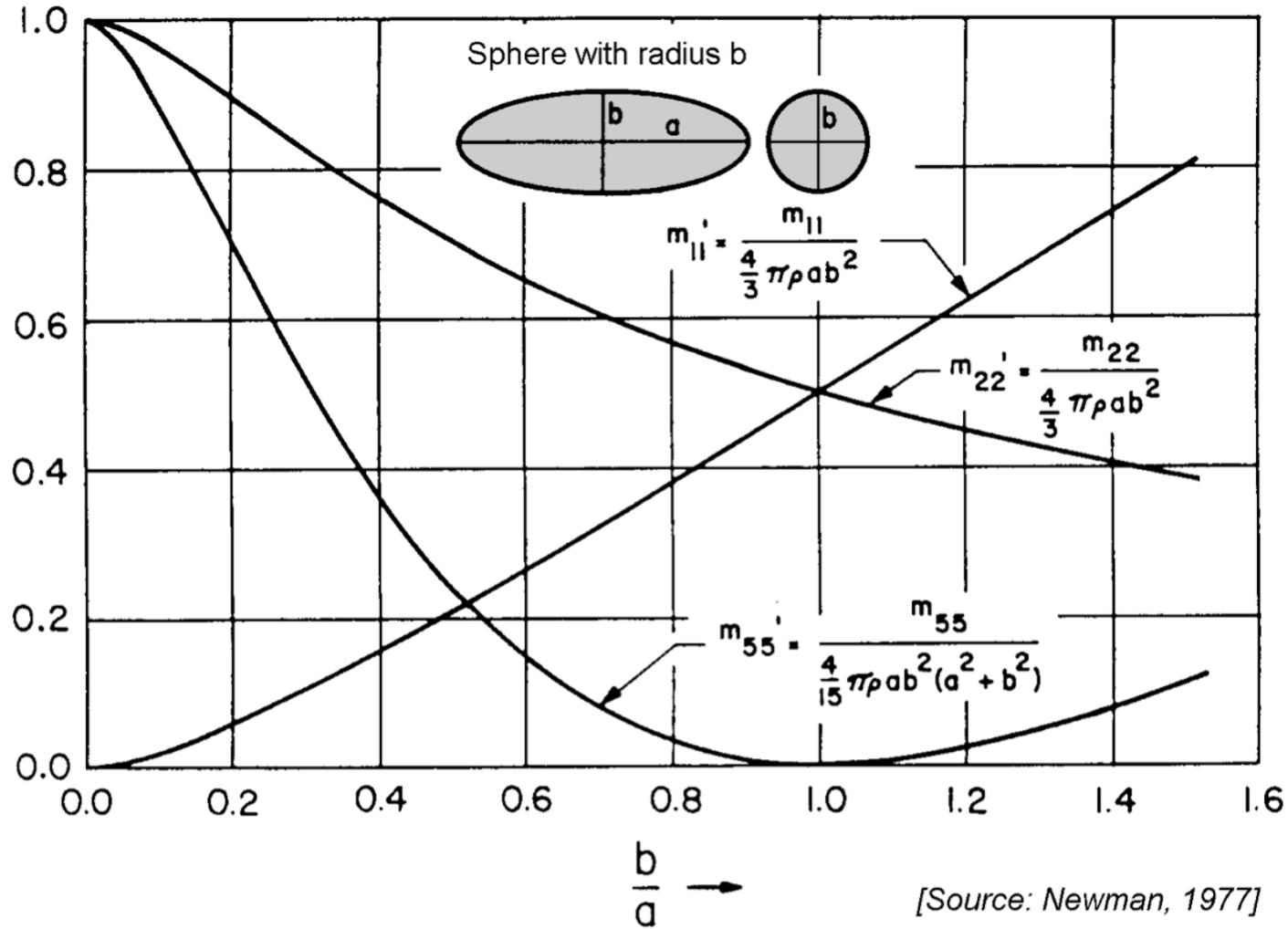


Figure 6.10: Added Mass Coefficients of Ellipsoids

Matriz de massa adicional

$$m_a = \rho \nabla C_a = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} & m_{15} & m_{16} \\ m_{21} & m_{22} & m_{23} & m_{24} & m_{25} & m_{26} \\ m_{31} & m_{32} & m_{33} & m_{34} & m_{35} & m_{36} \\ m_{41} & m_{42} & m_{43} & m_{44} & m_{45} & m_{46} \\ m_{51} & m_{52} & m_{53} & m_{54} & m_{55} & m_{56} \\ m_{61} & m_{62} & m_{63} & m_{64} & m_{65} & m_{66} \end{bmatrix}$$

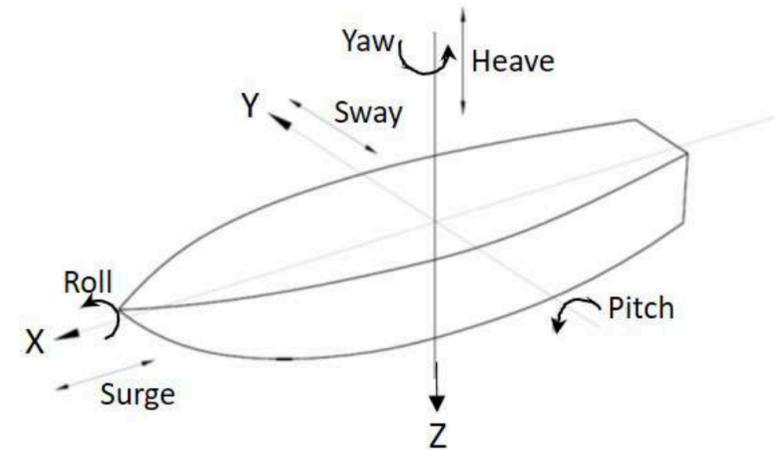
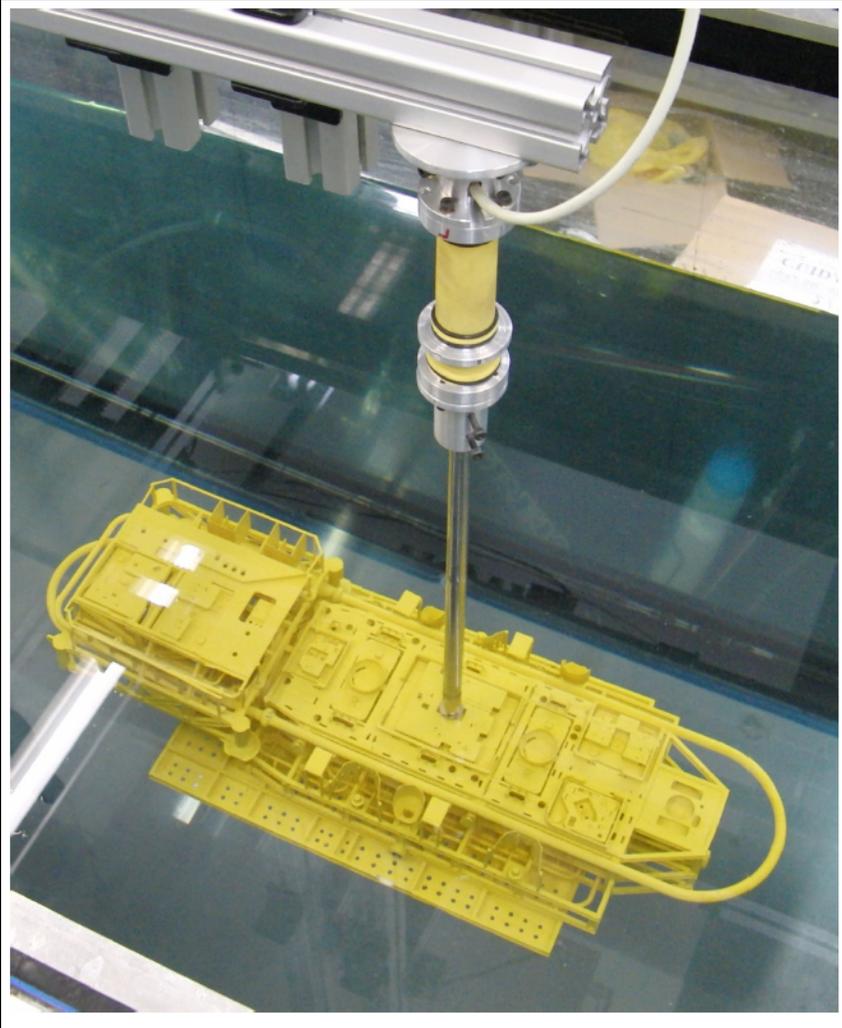
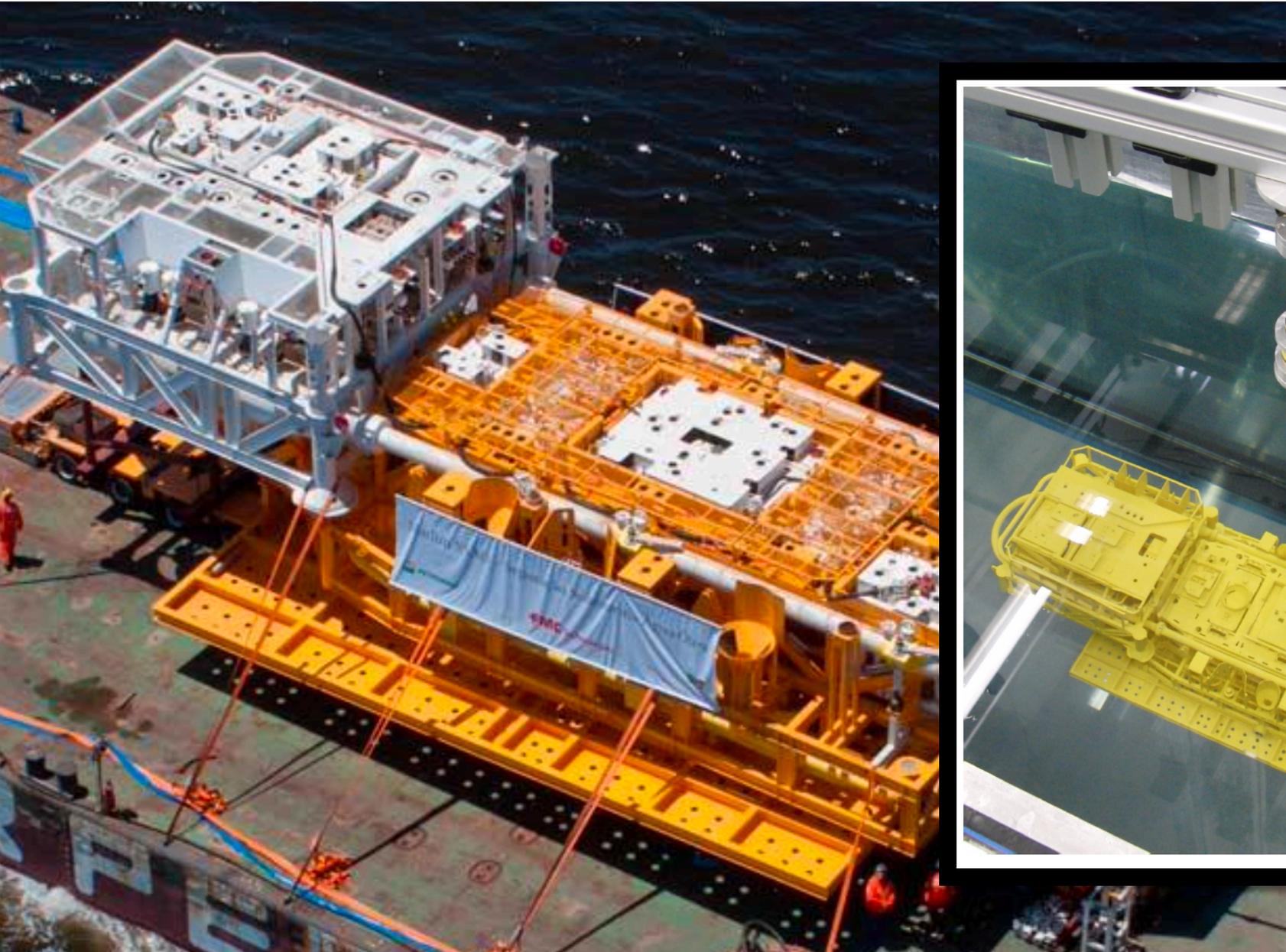
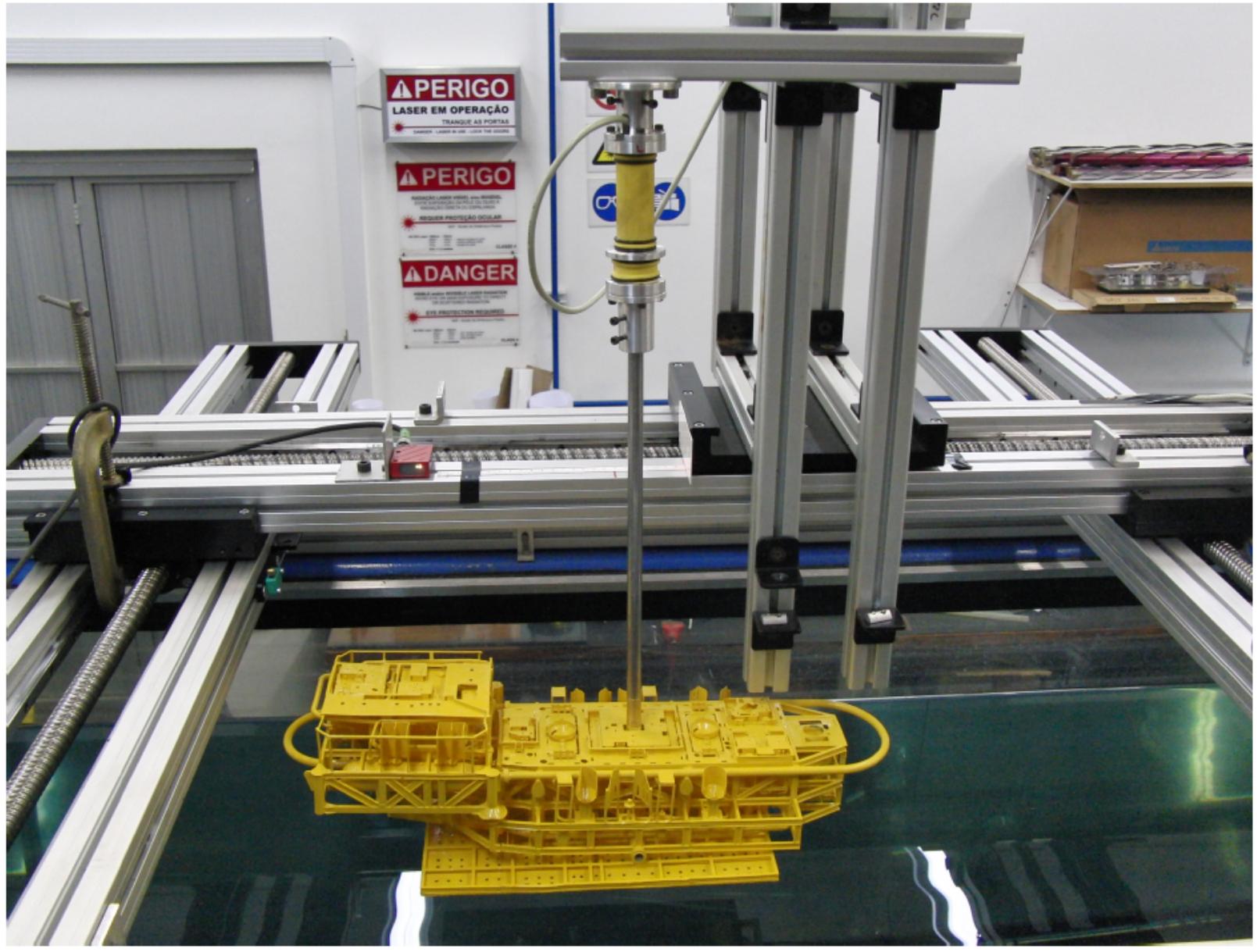


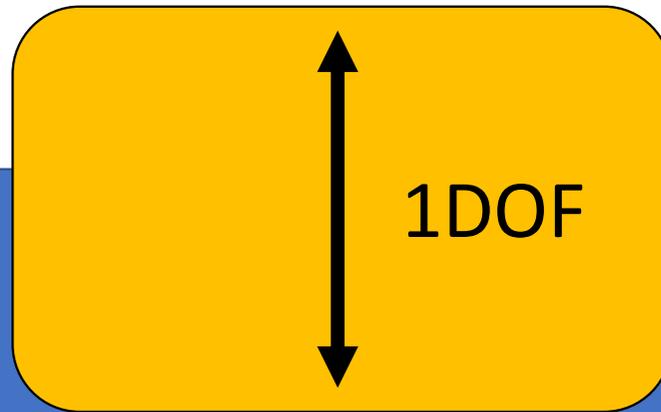
Figure 1.1: Tehe Six Degrees of Freedom (6DOF)

- | | |
|----------|----------|
| 1. Surge | 4. Roll |
| 2. Sway | 5. Pitch |
| 3. Heave | 6. Yaw |





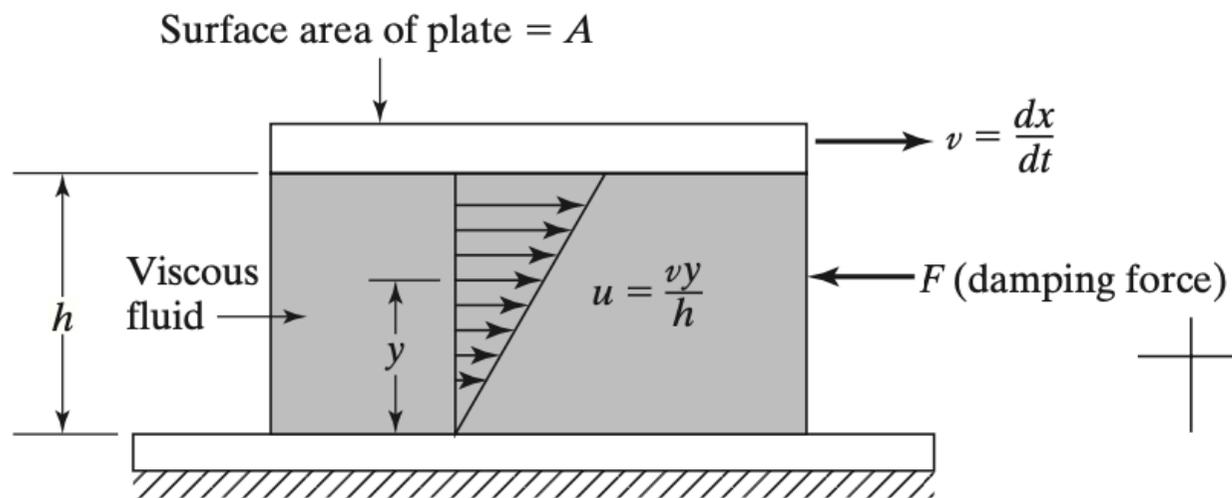
$$(a + m)\ddot{x} + b\dot{x} + cx = F_0 \sin \omega t.$$



Amortecimento seco (de Coulomb)

- Força de amortecimento é constante, independe da velocidade.
- Exemplo: atrito seco entre duas peças sólidas (sem lubrificante).

Amortecimento viscoso



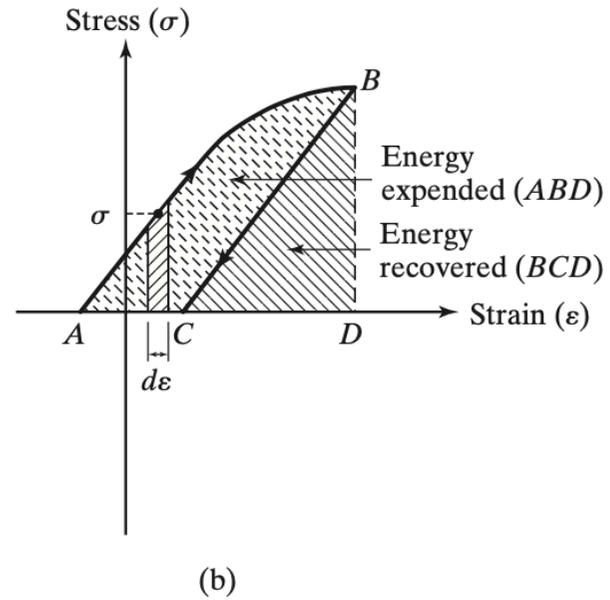
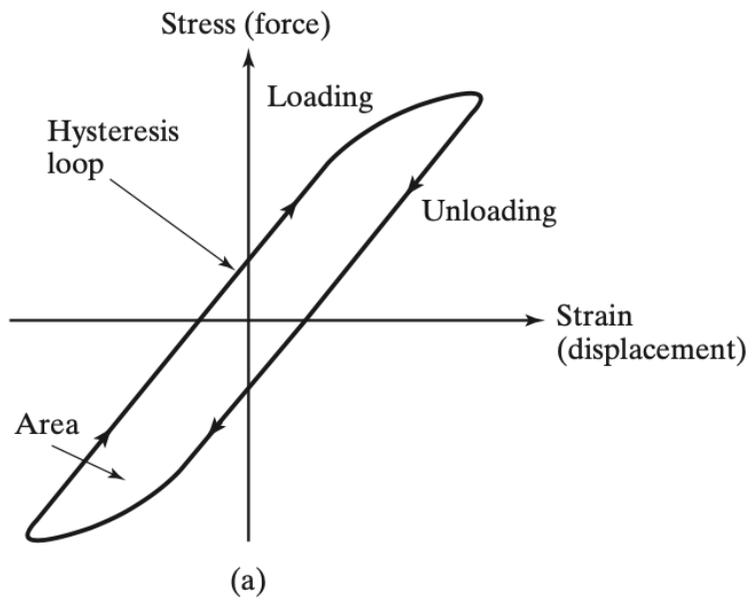
$$\tau = \mu \frac{du}{dy}$$

$$F = \tau A = \frac{\mu A v}{h}$$

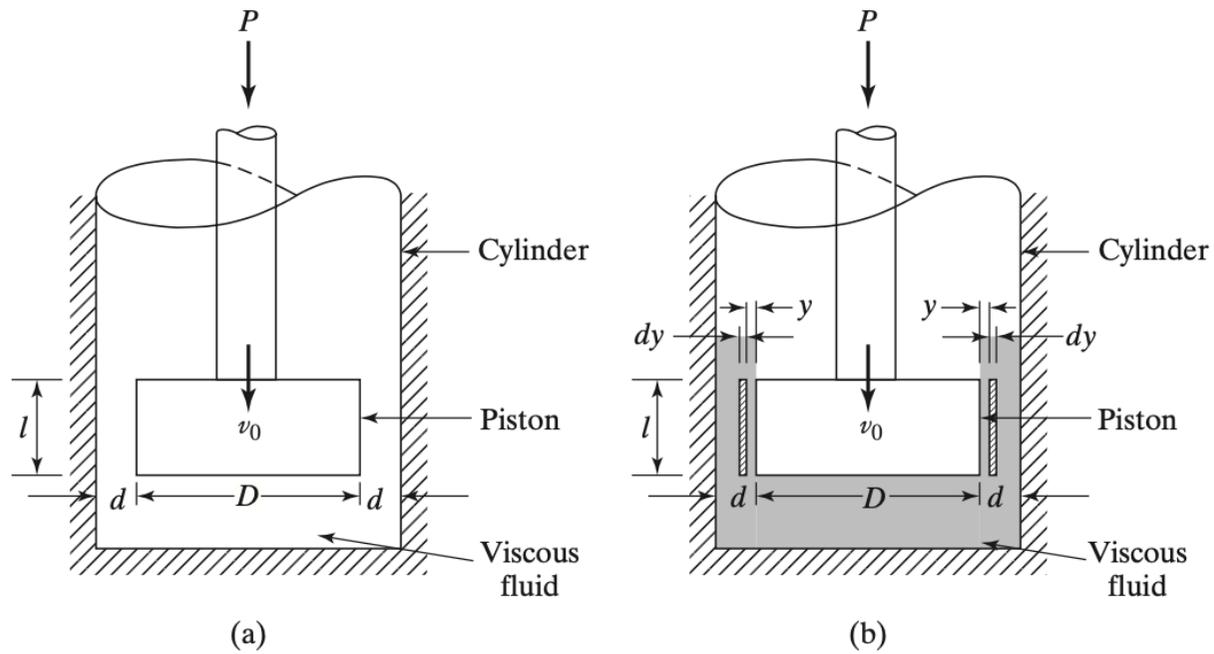
$$F = c v$$

$$c = \frac{\mu A}{h}$$

Amortecimento histerético

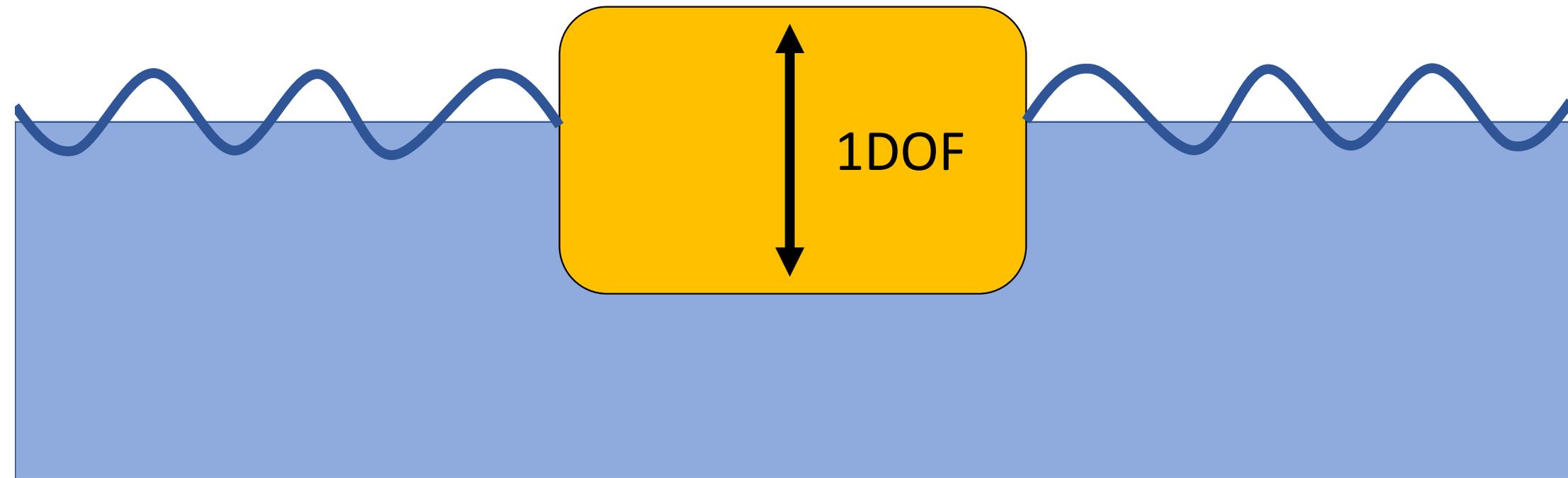


Exemplo: pistão

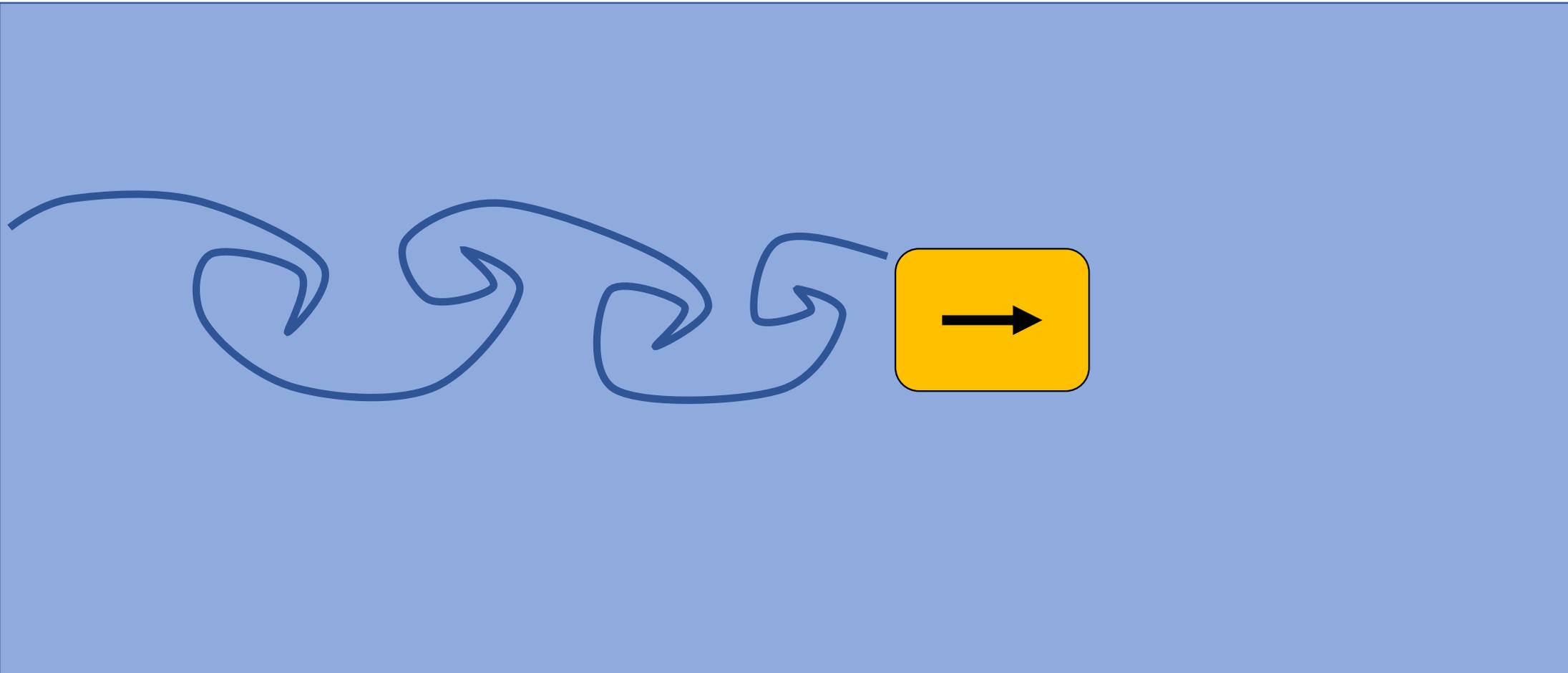


$$c = \mu \left[\frac{3\pi D^3 l}{4d^3} \left(1 + \frac{2d}{D} \right) \right]$$

Amortecimento: radiação de onda



Amortecimento: arrasto hidrodinâmico



Amortecimento equivalente

Parallel dampers: $c_{eq} = c_1 + c_2$

Series dampers: $\frac{1}{c_{eq}} = \frac{1}{c_1} + \frac{1}{c_2}$

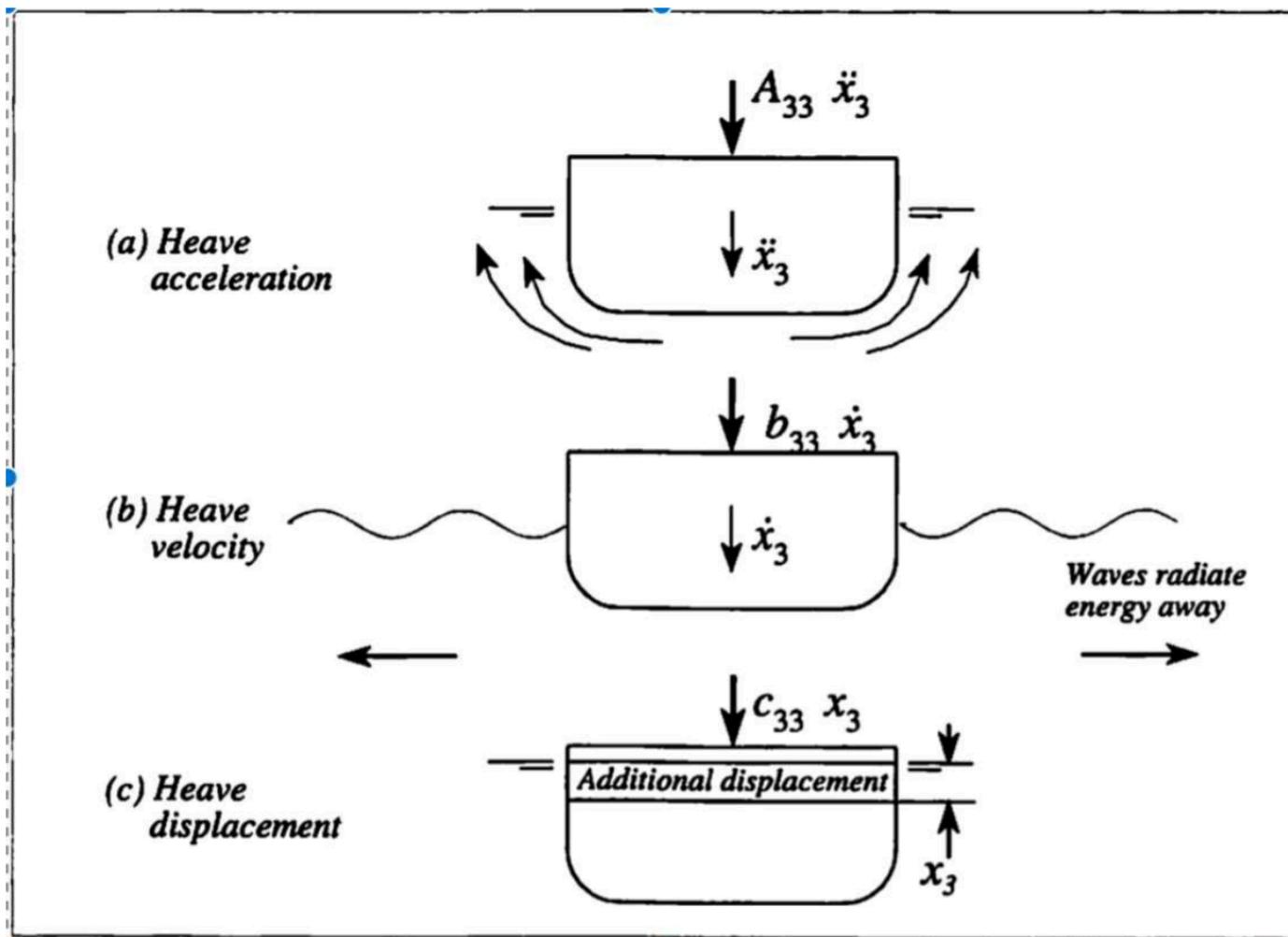


Figure 4.3: Effects of terms in the Equation of Motion (EOM) (Figure 3.4 in reference 2)





