good agreement with those for cinnamic acid and 1,3 -dichloropropane. The discrepancy in the case of the nitroanilines is, however, larger than would be expected.

## Summary

The solubilities in water of sixteen slightly soluble organic substances have been determined by means of an analytical method employing an interferometer.

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Received August 23, 1932
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## [Contribution from the Department of Chemistry of Yale University]

## The Dissociation Constant of Acetic Acid from 0 to $60^{\circ}$ Centigrade ${ }^{1}$

By Herbert S. Harned and Russell W. Ehlers

In a recent communication, ${ }^{2}$ we showed that it was possible to determine the dissociation constant of a weak acid with very high accuracy from electromotive force measurements of the cells

$$
\mathrm{H}_{2}\left|\mathrm{HAc}\left(m_{1}\right), \mathrm{NaAc}\left(m_{2}\right), \mathrm{NaCl}\left(m_{3}\right)\right| \mathrm{AgCl} \mid \mathrm{Ag}
$$

Values of the dissociation constants were determined from 0 to $35^{\circ}$ inclusive at $5^{\circ}$ intervals. More recently, we have obtained data from which this important constant may be obtained from 0 to $60^{\circ}$ at $5^{\circ}$ intervals. This determination involves values of the normal potential of the silversilver chloride electrode through this temperature range. The values of this quantity which we shall employ have been revised slightly by us between 0 and $35^{\circ}$ and determined between 35 and $60^{\circ} .^{3}$

The method of calculation of $K$ is described fully in our earlier contribution and was adhered to in all its detail. The equation for the electromotive force, $E$, of the cell is

$$
\begin{equation*}
E-E_{0}+\frac{R T}{F} \ln \frac{m_{\mathrm{HAc}} m_{\mathrm{Cl}}}{m_{\mathrm{Ac}}}=-\frac{R T}{F} \ln \frac{\gamma_{\mathrm{H}} \gamma_{\mathrm{Cl}} \gamma_{\mathrm{HAc}}}{\gamma_{\mathrm{H}} \gamma_{\mathrm{Ac}}}-\frac{R T}{F} \ln K \tag{1}
\end{equation*}
$$

$E_{0}$ is the normal potential of the cell, $K$, the dissociation constant, and the " $m$ 's" and " $\gamma$ ' $s$ " are the molalities and activity coefficients of the species denoted by subscripts. $m_{\mathrm{HAc}}$ and $m_{\mathrm{Ac}}$ were evaluated as previously described. As before, we let the right side of the equation equal $-R T / F$ $\ln K^{\prime}$, and then plot this quantity against $\mu$. At zero $\mu, K^{\prime}$ equals $K$. The extrapolation is easily carried out accurately as indicated by Fig. 1 of the former investigation. The value of $K$ at $35^{\circ}$ was redetermined and the

[^0]result agreed with the revised result of the earlier data. In Table I are giverı the electromotive forces of the cells. In the present instance $m_{1}, m_{2}$ and $m_{3}$ were all at the same concentration. In the second part of the table are the values of $K^{\prime}$ and of $K$ determined by extrapolation. The values of $E_{0}$ employed are given at the bottom of the table.

## Table I

| Electromotive Forces of the Cells: $\mathrm{H}_{2}\left\|\mathrm{HAc}\left(m_{1}\right), \mathrm{NaAc}\left(m_{2}\right), \mathrm{NaCl}\left(m_{8}\right)\right\| \mathrm{AgCl} \mid \mathrm{Ag}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $m_{\text {: }}=m_{2}=m_{2}$ | $E_{\text {ss }}$ | E* | $E_{45}$ | Eto | $E_{s 6}$ | $E_{\infty}$ |
| 0.006313 | 0.64143 | 0.64511 | 0.64887 | 0.65247 | 0.65623 | 0.65980 |
| . 012869 | . 62267 | . 62594 | . 62936 |  |  | . 63943 |
| . 021015 | . 60965 | . 61281 | . 61596 | . 61898 | . 62215 | . 62534 |
| . 047973 | . 58775 | . 59049 | . 59331 | . 59594 | . 59873 | . 60146 |
| . 07613 | . 57553 | . 57802 | . 58067 | . 58316 | . 58569 | . 58821 |
| . 10031 | . 56837 | . 57083 | . 57316 | . 57561 | . 57799 | . 58039 |
| . 008419 | . 63386 | . 63738 | . 64091 | . 64447 | . 64796 | . 65149 |
| . 010131 | . 62895 | . 63239 |  | . 63939 | . 64279 | . 64624 |
| . 011845 | . 62474 | . 62815 | . 63155 | . 63493 | . 63829 | . 64165 |
| . 014868 | . 61875 | . 62201 | . 62533 | . 62858 | . 63184 | . 63509 |

Values of $K^{\prime}$ and Extrapolated Values of the Dissociation Constant $K$

| $\substack{\mu=\\ m_{2}+m_{z}+m_{\mathrm{H}} \\ t=35^{\circ} \\ 0.01266}$ | 1.728 | 1.700 | 1.664 | 1.633 | 1.585 | 1.543 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| .02577 | 1.714 | 1.693 | 1.659 |  |  |  |
| .04206 | 1.712 | 1.684 | 1.654 | 1.628 | 1.587 | 1.536 |
| .09598 | 1.709 | 1.686 | 1.654 | 1.630 | 1.585 | 1.543 |
| .14229 | 1.706 | 1.686 | 1.653 | 1.625 | 1.582 | 1.542 |
| .20066 | 1.696 |  | 1.650 | 1.617 | 1.580 | 1.537 |
| .01687 | 1.722 | 1.696 | 1.666 | 1.631 | 1.590 | 1.544 |
| .02030 | 1.720 | 1.694 |  | 1.625 | 1.586 | 1.536 |
| .02372 | 1.723 | 1.694 | 1.664 | 1.631 | 1.590 | 1.544 |
| .02977 | 1.723 | 1.694 | 1.663 | 1.631 | 1.590 | 1.545 |
| $E_{0}$ (obs.) | 0.21563 | 0.21200 | 0.20821 | 0.20437 | 0.20035 | 0.19620 |
| $K \times 10^{5}$ | 1.729 | 1.701 | 1.668 | 1.633 | 1.590 | 1.542 |

One further refinement has been carried out. By the method of least squares, we have computed $E_{0}$ as a function of the temperature. ${ }^{3}$ Its value is given by the equation

$$
\begin{array}{r}
E_{0}=0.22239-645.52 \times 10^{8}(t-25)-3.284 \times 10^{-8}(t-25)^{2}+ \\
9.948 \times 10^{-9}(t-25)^{3} \tag{2}
\end{array}
$$

If we employ the values computed by this equation which are given in column two of Table II, we obtain the values of $K$ in the third column. These we regard as our final values. At $25^{\circ}$ our result of $1.754 \times 10^{-5}$ checks very closely that of $1.753 \times 10^{-5}$ recently determined by MacInnes and Shedlovsky ${ }^{4}$ from conductance measurements. We have no accurate values with which to compare our results at other temperatures. In Fig. 1 we have plotted $K$ against the temperature. All points except that at $30^{\circ}$

[^1]fall on the smooth curve to within $\pm 2$ in the third decimal place which corresponds to an error of $\pm 0.03$ of a millivolt. It is apparent that $K$ increases, reaches a maximum at about $23^{\circ}$ and then decreases with increasing temperature.


Fig. 1.-The dissociation constant of acetic acid as a function of the temperature.

To determine the heat content of ionization of the acid, we employed the equation

$$
\begin{align*}
\frac{\mathrm{d} \ln K}{\mathrm{~d} T} & =\frac{\Delta H}{R T^{2}} \quad \text { or }  \tag{3}\\
\frac{\mathrm{d} \ln K}{\mathrm{~d}(1 / T)} & =-\Delta H \tag{4}
\end{align*}
$$

$\ln K$ was plotted against $1 / T$, and $\Delta H$ was evaluated from the slope. A plot of these values of $\Delta H$ against $T$ revealed that $\Delta H$ varied approximately linearly with the temperature. This suggested that the problem could be treated in the usual way. $\Delta H$ was taken to vary with the temperature according to

$$
\begin{equation*}
\Delta H=a+b T+c T^{2} \tag{5}
\end{equation*}
$$

Upon substituting this value of $\Delta H$ in equation (3) and performing the integration

$$
\begin{equation*}
\log K=-\frac{a}{2.303 R T}+\frac{b}{R} \log T+\frac{c}{2.303 R} T+d \tag{6}
\end{equation*}
$$

is obtained in which $a, b, c$ and $d$ are empirical constants. By substitution of the known values of $K$ and $T$ in equation (6), thirteen equations were obtained from which the constants were evaluated by the method of least squares. The equation with the empirical constants was

$$
\begin{equation*}
\log K=-\frac{1500.65}{T}-6.50923 \log T-0.0076792 T+18.67257 \tag{7}
\end{equation*}
$$

Values of $K$ computed by this equation are given in the fourth column of Table II. The differences between the observed and calculated results are given in the fifth column. At the higher and lower temperatures the calculated values are slightly higher than the observed, while in the middle range of temperature they are somewhat lower. We have previously noted this behavior when dealing with a similar calculation and function, ${ }^{3}$ and found that another term, $d T^{3}$, is necessary in equation (5) in order to represent the results within the experimental error throughout the entire concentration range. In the present treatment, we have not resorted to this refinement. On the whole the agreement is good. The mean deviation is $\pm 0.003$, which corresponds to about $\pm 0.04$ millivolt.

The equation for the change in heat content of the dissociation of acetic acid derived from equation (7) is

$$
\begin{equation*}
\Delta H=6871.0-12.9436 T-0.035161 T^{2} \tag{8}
\end{equation*}
$$

Values of $\Delta H$ computed by this equation are given in the sixth column of Table II. In column seven, $\Delta C_{p}$, the differences in specific heat of the ions and the undissociated molecule of acetic acid computed from the equation

$$
\begin{equation*}
\Delta C_{p}=-12.9436-0.070322 T \tag{9}
\end{equation*}
$$

are compiled.
Table II
Dissociation Constant and Heat of Ionization of Acetic Actd

| $t,{ }^{\circ} \mathrm{C}$. | $E_{0}$ | ${ }_{\text {(obs.) }} \times 10^{5}$ | $\begin{gathered} K \times 10^{5} \\ \text { (Equation } 6 \text { ) } \end{gathered}$ | $\Delta$ | $\Delta H$ | $\Delta C_{p}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.23632 | 1.657 | 1.667 | +0.010 | 714 | -32.15 |
| 5 | 23391 | 1.700 | 1.702 | $+.002$ | 552 | -32.50 |
| 10 | 23130 | 1.729 | 1.728 | +. 002 | 389 | -32.85 |
| 15 | 22851 | 1.745 | 1.745 | . 000 | 223 | -33.20 |
| 20 | . 22554 | 1.753 | 1.752 | -. 001 | 57 | -33.55 |
| 25 | 22239 | 1.754 | 1.751 | -. 003 | - 112 | -33.91 |
| 30 | . 21908 | 1.750 | 1.741 | $-.009$ | - 282 | -34.26 |
| 35 | . 21561 | 1.728 | 1.724 | - . 004 | - 455 | -34.61 |
| 40 | 21200 | 1.703 | 1.700 | -. 003 | - 628 | -34.96 |
| 45 | . 20825 | 1.670 | 1.669 | -. 001 | - 804 | -35.31 |
| 50 | . 20436 | 1.633 | 1.633 | . 000 | - 982 | -35.66 |
| 55 | . 20033 | 1.589 | 1.592 | $+.003$ | -1161 | -36.02 |
| 60 | 19620 | 1.542 | 1.547 | +.005 | -1342 | -36.37 |

## Summary

1. Measurements of the cells

$$
\mathrm{H}_{3}\left|\mathrm{HAc}\left(m_{1}\right), \mathrm{NaAc}\left(m_{2}\right), \mathrm{NaCl}\left(m_{3}\right)\right| \mathrm{AgCl} \mid \mathrm{Ag}
$$

have been made from 35 to $60^{\circ}$ at $5^{\circ}$ intervals.
2. By a method previously described by us, the dissociation constant of acetic acid has been computed from 35 to $60^{\circ}$ at $5^{\circ}$ intervals from these results. Our earlier results from 0 to $35^{\circ}$ have been recomputed by the use of more recently determined values of the normal potential of the silver-
silver chloride electrode. Final values of the dissociation constant of acetic acid from 0 to $60^{\circ}$ at $5^{\circ}$ intervals have been tabulated. Our value of $1.754 \times 10^{-5}$ agrees excellently with the value, $1.753 \times 10^{-5}$, determined from the conductance measurements by MacInnes and Shedlovsky.
3. The dissociation constant is given by the equation

$$
\log K=-\frac{1500.65}{T}-6.50923 \log T-0.0076792 T^{2}+18.67257
$$

4. The heat of dissociation is given by the equation $\Delta H=6871.0-12.9436 T-0.035161 T^{2}$
New Haven, Connecticut
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[Contribution from the Chemical Laboratory of the University of Illinois]

## Types of Chemical Reactions

## By William Albert Noyes

A study of the interaction of nitrogen trichloride with nitric oxide and with nitrogen tetroxide has given results from which, in conjunction with other experimental evidence and with current electronic theories, it is possible to define accurately, with a high degree of probability, the electronic course of several types of reactions.

The discussion which follows applies, primarily, to elements with atomic weights of 40 or below. For elements of higher atomic weights the outer shell of valence electrons seems to be less sharply defined.

Three principles are used. (1) On account of their "spin" and for other reasons, the electrons of the valence shell of an atom are usually, not always, associated in pairs, octets or sextets. (2) Every atom must have the positive charge of its nucleus balanced by the electrons immediately associated with it, or it must be an ion or form part of a complex ion, which is held to or in the neighborhood of another ion of the opposite sign, by static attraction. (3) In balancing the positive charge of the nucleus of an atom the pair of electrons of a covalence is equivalent to a single unshared electron.

## 1. Formation of Ions

A. Permanent ions, formed with an outer shell of electrons (usually an octet) for some atom, in such a manner that the positive charge of the kernel or nucleus is overbalanced or underbalanced by the electrons surrounding it: (a) by the gain or loss of one or more electrons, as for sodium, calcium, chlorine or sulfur; (b) by the addition of a positive hydrogen or methyl ion to ammonia or to a tertiary amine, a positive hydroxyl group


[^2]
[^0]:    (1) This contribution contains material which constituted a part of a Thesis presented to the Graduate School by Russell W. Ehlers in partial fulfilment of the requirements of the degree of Doctor of Philosophy, June, 1932.
    (2) Harned and Ehlers, This Journal, 54, 1350 (1932).
    (3) The considerations and new data which have led to the review of the normal eletrode potential, $E_{0}$, will be published in another contribution.

[^1]:    (4) MacInnes and Shedlovsky, This Journai, 64, 1429 (1932).

[^2]:    $\stackrel{\ddot{\mathrm{C}}}{\mathrm{H}}{ }_{3}$

