

Propagação de erros 1

Fórmula geral

Soma e subtração de constante

Multiplicação e divisão de constante

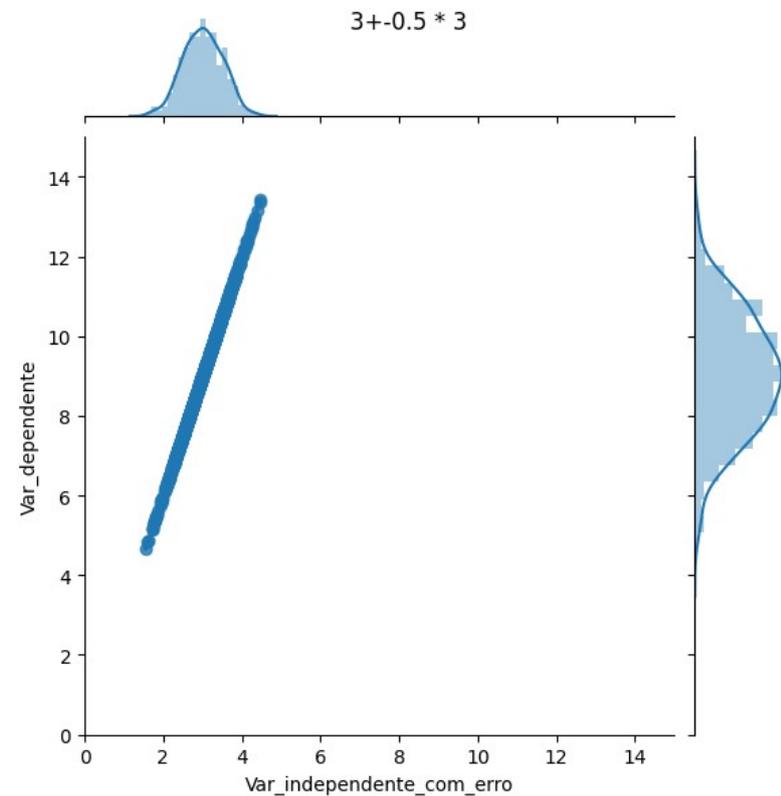
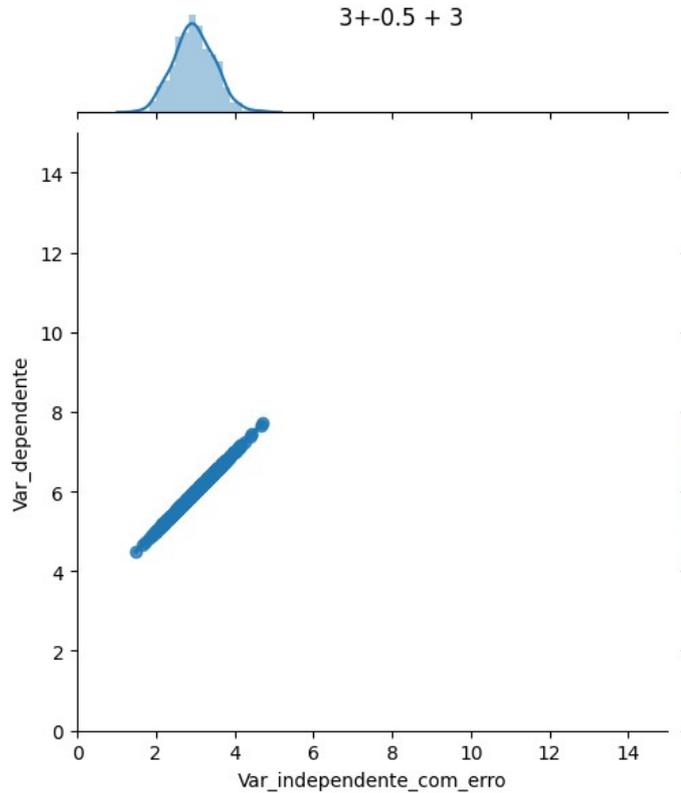
Covariância e erros

Propagação de erros - mais de uma variável

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$$\Delta Z^2 = \left(\frac{\delta f(X, Y)}{\delta X} \Delta X \right)^2 + \left(\frac{\delta f(X, Y)}{\delta Y} \Delta Y \right)^2$$

Soma dos quadrados das derivadas parciais vezes o erro da variável



Premissa das fórmulas gerais:
Os erros de cada variável não são correlacionados

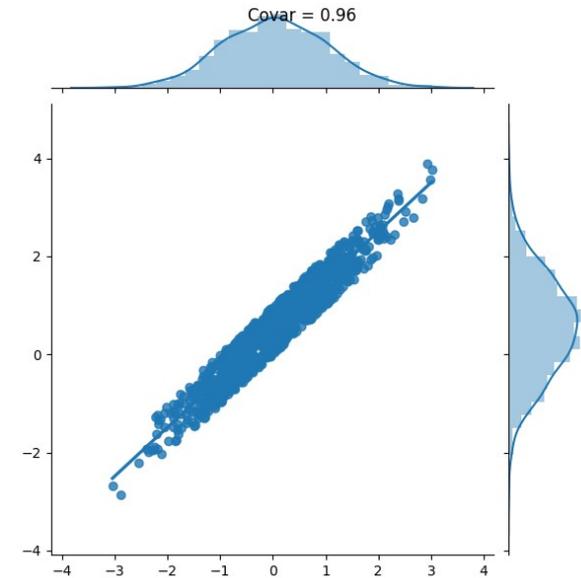
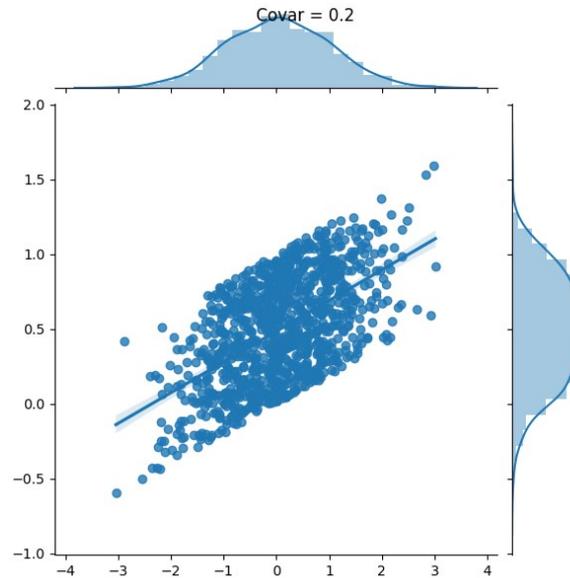
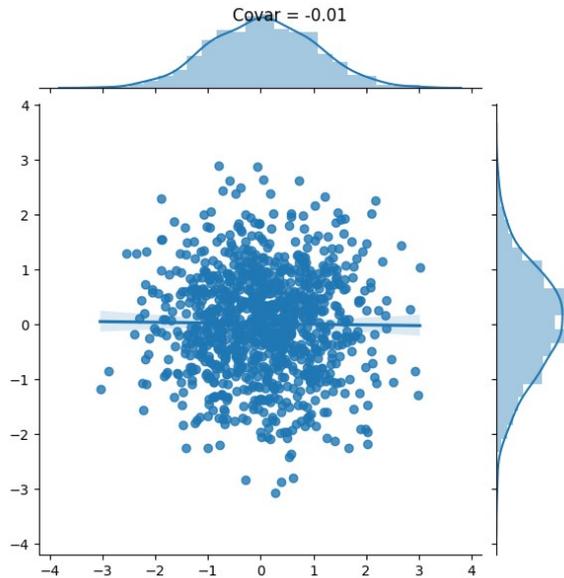
Variância:

$$\sigma_A^2 = \frac{1}{n} \sum (x_i - \bar{x})^2$$

Covariância:

$$\sigma_{AB} = \frac{1}{n} \sum (x_i - \bar{x})(y_i - \bar{y})$$

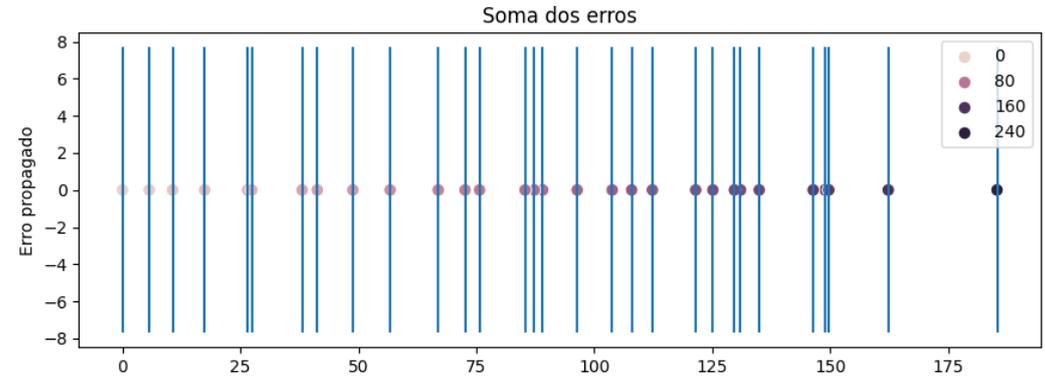
$$\sigma_{AB} = \frac{1}{n} \sum (x_i - \bar{x})(y_i - \bar{y})$$



$$z = x + y$$

$$z = x - y$$

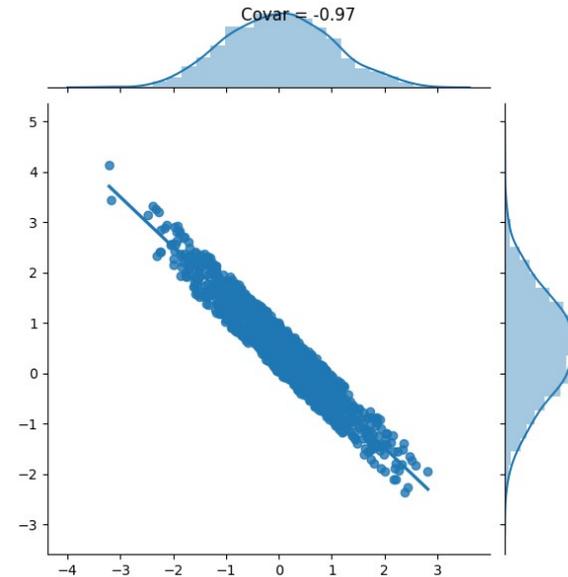
$$\sigma z = \sqrt{\sigma x^2 + \sigma y^2}$$



para $\sigma_{xy} \neq 0$

$$\sigma z = \sqrt{\sigma x^2 + \sigma y^2 + 2\sigma_{xy}}$$

$$\sigma z = \sqrt{\sigma x^2 + \sigma y^2 - 2\sigma_{xy}}$$

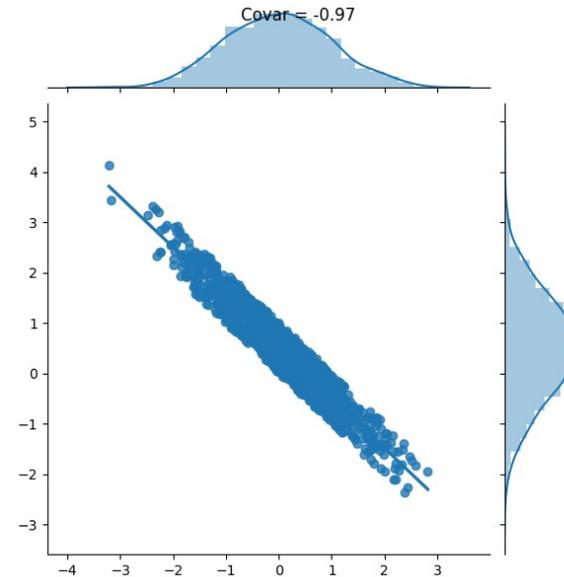


$$Z = X * Y \quad Z = \frac{X}{Y} \quad \sigma_Z = z \sqrt{\left(\frac{\sigma_X}{X}\right)^2 + \left(\frac{\sigma_Y}{Y}\right)^2}$$

para $\sigma_{xy} \neq 0$

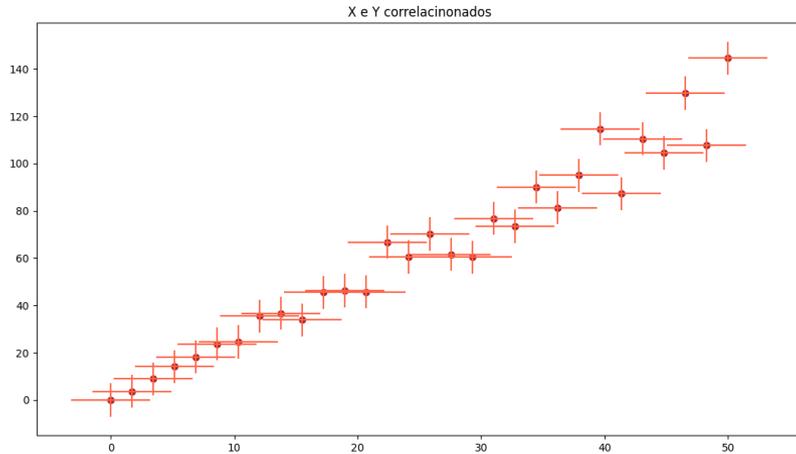
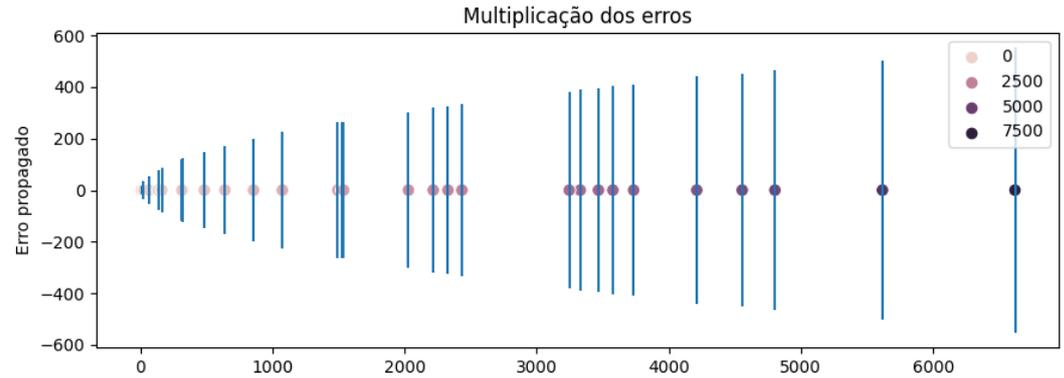
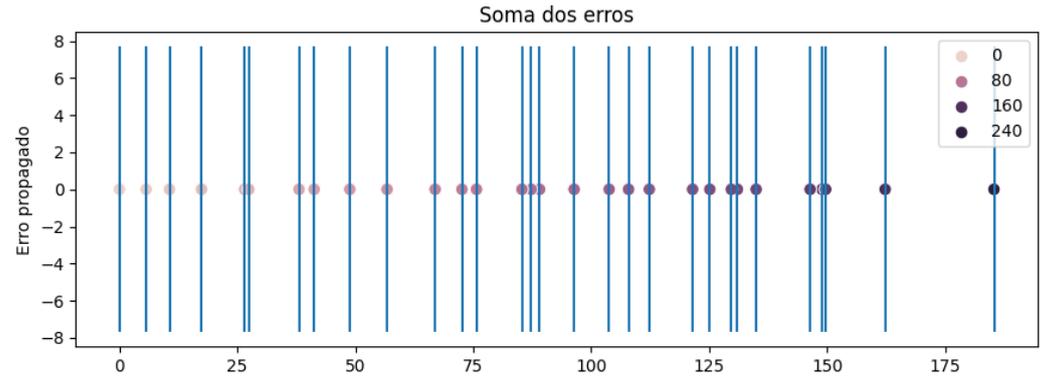
$$\sigma_Z = z \sqrt{\left(\frac{\sigma_X}{X}\right)^2 + \left(\frac{\sigma_Y}{Y}\right)^2 + \frac{2\sigma_{xy}}{xy}}$$

$$\sigma_Z = z \sqrt{\left(\frac{\sigma_X}{X}\right)^2 + \left(\frac{\sigma_Y}{Y}\right)^2 - \frac{2\sigma_{xy}}{xy}}$$



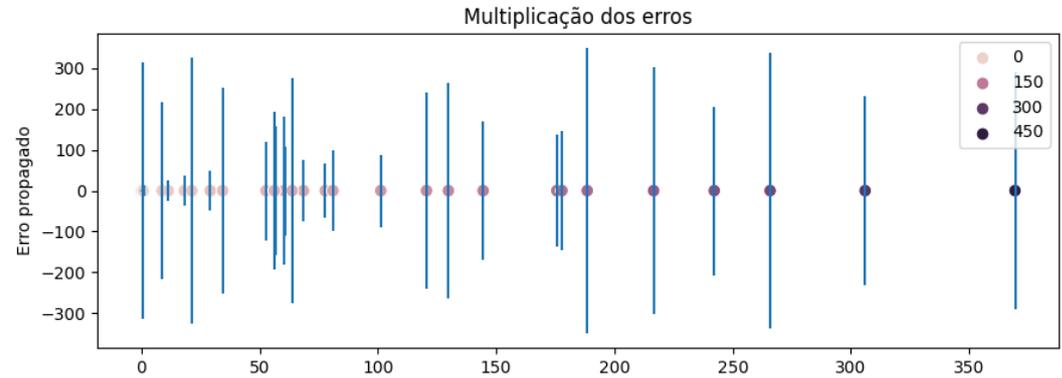
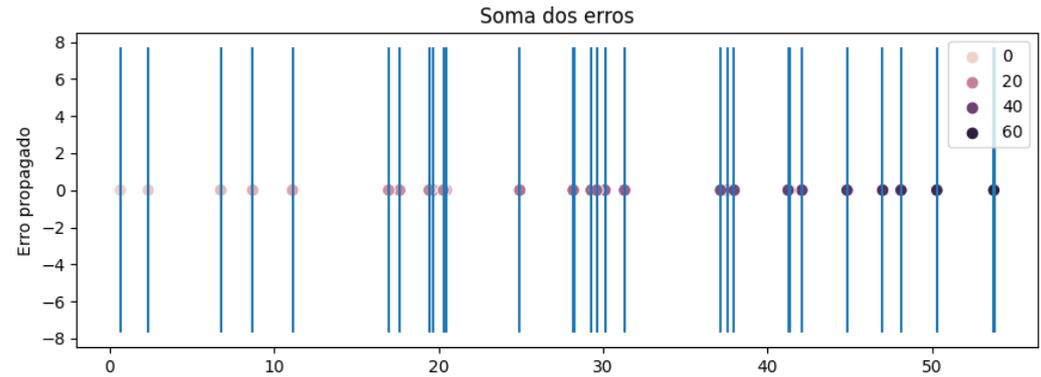
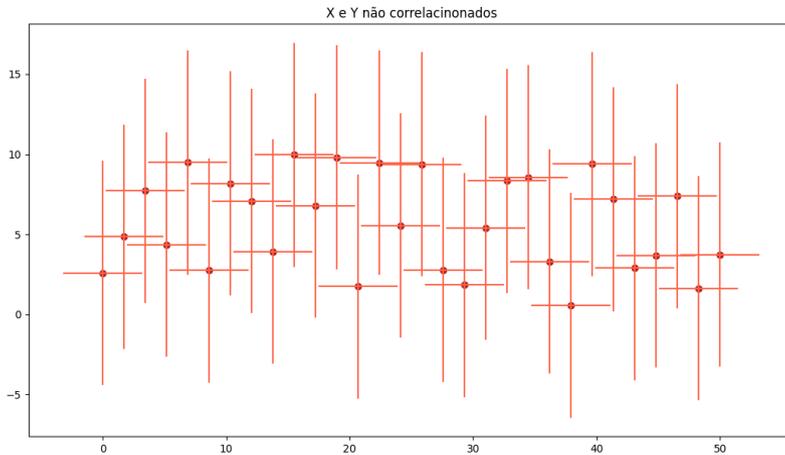
$$Z = X * Y \quad Z = \frac{X}{Y}$$

$$\frac{\Delta Z}{Z} = \sqrt{\left(\frac{\Delta X}{X}\right)^2 + \left(\frac{\Delta Y}{Y}\right)^2}$$



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$$Z = \ln(X)$$

$$\Delta Z = \left| \frac{\delta \ln(X)}{\delta X} \Delta X \right|$$

$$\Delta Z = \left| \frac{\Delta X}{X} \right|$$

$$Z = e^X$$

$$\Delta Z = \left| \frac{\delta e^X}{\delta X} \Delta X \right|$$

$$\Delta Z = |e^X \Delta X|$$

$$Z = \text{sen}(X)$$

$$\Delta Z = \left| \frac{\delta \text{sen}(X)}{\delta X} \Delta X \right|$$

$$\Delta Z = |\cos(X) \Delta X|$$

