

# Eletrromagnetismo Avançado


2º ciclo  
Aula de 15 outubro

# Potencial e potencial vetor

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

# Potencial e potencial vetor

$$\begin{array}{l} \vec{B} = \vec{\nabla} \times \vec{A} \\ \vec{E} = -\vec{\nabla}V - \frac{\partial \vec{A}}{\partial t} \end{array} \quad \begin{array}{l} \vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \\ \vec{\nabla} \cdot \vec{B} = 0 \end{array}$$


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$$\vec{\nabla} \cdot \vec{\mathbf{B}} = 0$$

$$\vec{\nabla} \cdot \vec{\mathbf{E}} = \frac{\rho}{\epsilon_0}$$

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$$\vec{\nabla} \cdot \vec{\mathbf{B}} = 0$$

$$\vec{\nabla} \cdot \vec{\mathbf{E}} = \frac{\rho}{\epsilon_0}$$

$$\vec{\nabla} \times \vec{\mathbf{B}} = \mu_0 \vec{\mathbf{J}} + \mu_0 \epsilon_0 \frac{\partial \vec{\mathbf{E}}}{\partial t}$$

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$$\vec{\nabla} \times (\vec{\nabla} \times \vec{\mathbf{A}}) = \mu_0 \vec{\mathbf{J}} - \mu_0 \epsilon_0 \left( \vec{\nabla} \left( \frac{\partial V}{\partial t} \right) + \frac{\partial^2 \vec{\mathbf{A}}}{\partial t^2} \right)$$

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$$\vec{\nabla} \times \vec{\mathbf{B}} = \mu_0 \vec{\mathbf{J}} + \mu_0 \epsilon_0 \frac{\partial \vec{\mathbf{E}}}{\partial t}$$

$$\vec{\nabla} (\vec{\nabla} \cdot \vec{\mathbf{A}}) - \nabla^2 \vec{\mathbf{A}} = \mu_0 \vec{\mathbf{J}} - \mu_0 \epsilon_0 \left( \vec{\nabla} \left( \frac{\partial V}{\partial t} \right) + \frac{\partial^2 \vec{\mathbf{A}}}{\partial t^2} \right)$$



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$$\vec{\nabla} \times \vec{B} = \mu_0 \vec{J} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

$$\nabla^2 \vec{A} - \mu_0 \epsilon_0 \frac{\partial^2 \vec{A}}{\partial t^2} - \vec{\nabla} \left( \vec{\nabla} \cdot \vec{A} + \mu_0 \epsilon_0 \frac{\partial V}{\partial t} \right) = -\mu_0 \vec{J}$$

GAUGE DE COULOMB  $\Rightarrow \vec{\nabla} \cdot \vec{A} = 0$

$$\Rightarrow \nabla^2 V = -\rho / \epsilon_0 \quad \leftarrow \text{POISSON} \quad \text{😊}$$

$$\Rightarrow \nabla^2 \vec{A} - \mu_0 \epsilon_0 \frac{\partial^2 \vec{A}}{\partial t^2} - \mu_0 \epsilon_0 \frac{\partial}{\partial t} \nabla^2 V = -\mu_0 \vec{J} \quad \text{😞}$$

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$$\nabla^2 \vec{\mathbf{A}} - \mu_0 \epsilon_0 \frac{\partial^2 \vec{\mathbf{A}}}{\partial t^2} - \vec{\nabla} \left( \vec{\nabla} \cdot \vec{\mathbf{A}} + \mu_0 \epsilon_0 \frac{\partial V}{\partial t} \right) = -\mu_0 \vec{\mathbf{J}}$$

$$\vec{\nabla} \times \vec{\mathbf{B}} = \mu_0 \vec{\mathbf{J}} + \mu_0 \epsilon_0 \frac{\partial \vec{\mathbf{E}}}{\partial t}$$

$$\vec{\nabla} \cdot \vec{\mathbf{A}} + \mu_0 \epsilon_0 \frac{\partial V}{\partial t} = 0 \quad \text{Gauge de Lorenz}$$

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$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\nabla^2 V - \frac{1}{c^2} \frac{\partial^2 V}{\partial t^2} = -\frac{\rho}{\epsilon_0}$$

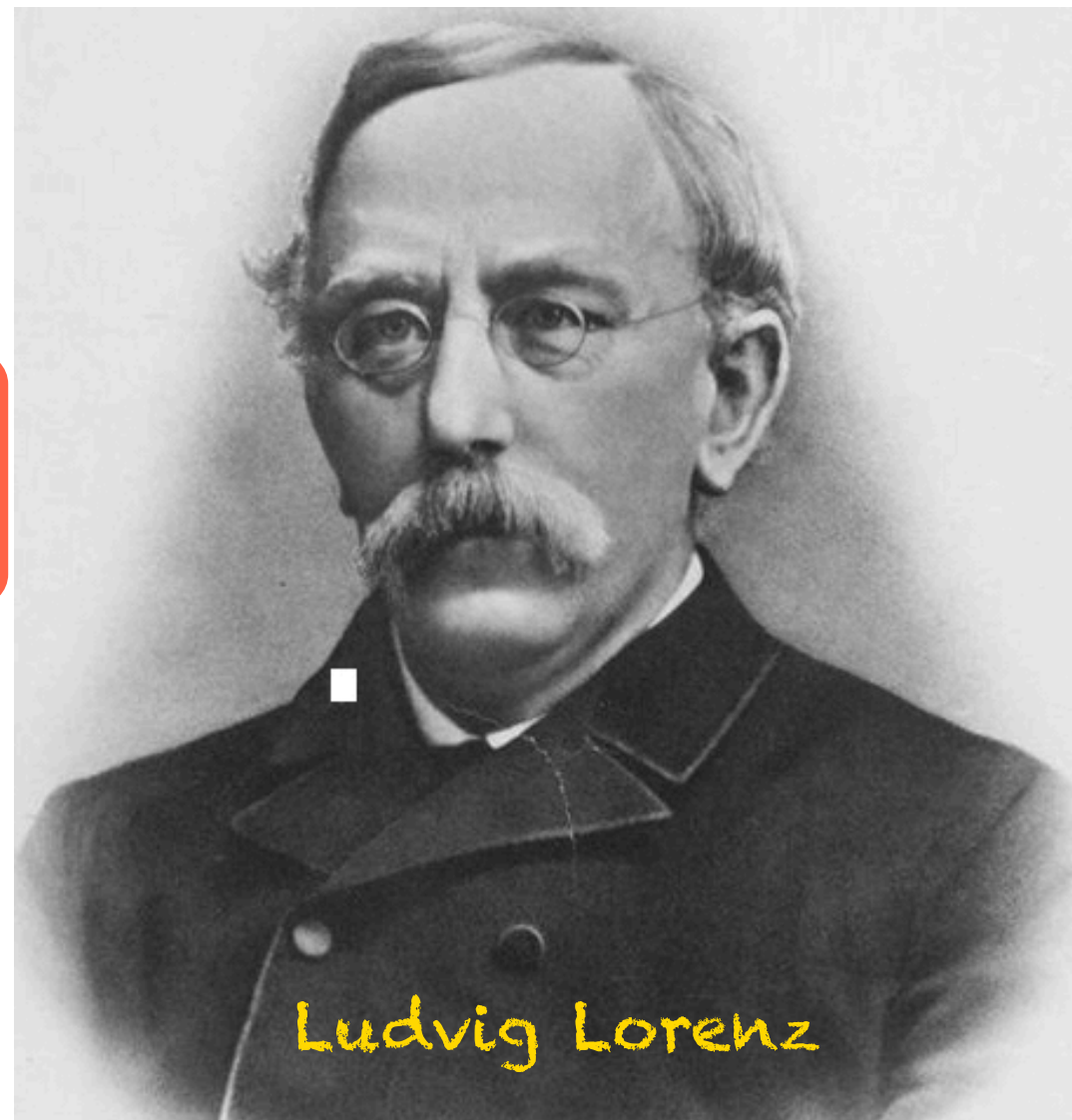


$$\nabla^2 \vec{A} - \frac{1}{c^2} \frac{\partial^2 \vec{A}}{\partial t^2} = -\mu_0 \vec{J}$$



$$\vec{\nabla} \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\mu_0 \vec{J} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$



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$$\nabla^2 V - \frac{1}{c^2} \frac{\partial^2 V}{\partial t^2} = -\frac{\rho}{\epsilon_0}$$

$$\square^2 V = -\frac{\rho}{\epsilon_0}$$

$$\nabla^2 \vec{A} - \frac{1}{c^2} \frac{\partial^2 \vec{A}}{\partial t^2} = -\mu_0 \vec{J}$$

$$\square^2 \vec{A} = -\mu_0 \vec{J}$$

EQUIVALENTES

$$\square^2 \equiv \nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2}$$