### Modern Solid State NMR Techniques for the Study of Molecular Solids

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### **Current Research Agenda**

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NMR Methods	Glass	Li Ion Battery	Optical	Catalysts
Development	Science	Components	Materials	Biomaterials
SSNMR, ESR	Structure	Electrode	Luminescent	FLP, Zeolite
Dipolar	Dynamics,	Electrolytes,	Ceramics,	Nanocomposites
Techniques	Sol-Gel	Ceramics	Hybrids	Bioceramics

#### Support

Industry: Corning, Schott, Ivoclar, Nippon Glass DFG, DFG-SFB, IRTG, BMBF CNPq Universal, FAPESP, CEPID, CNPq

### **Outline**

#### Solid State NMR – General Aspects Anisotropic Interactions:

magnetic shielding dipole-dipole coupling nuclear electric quadrupole coupling

**Manipulation of Interactions** 

high-resolution NMR in crystalline Systems dipolar spectroscopy cross-polarization

NMR Studies of Insensitive Nuclei NMR Studies of Supramolecular Systems NMR Studies of Frustrated Lewis Pairs

## Literature

#### **Highlight articles**

D. Laws, H. M. Bitter, A. Jerschow, Angew. Chem. Int. Ed. 41 (2002), 3096.M. J. Duer, Ann. Rep. NMR Spectrosc. 43 (2000), 1.

#### **Fundamental Principles (Theory)**

A. Abragam, *The Principles of Nuclear Magnetism*, Clarendon Press Oxford (1961).
C. P. Slichter, *Principles of Magnetic Resonance*, Springer Verlag Heidelberg 1978.
B.C. Gerstein, C.R. Dybowski, *Transient Techniques in NMR of Solids*, Academic Press Inc (1985).

M. Mehring, *Principles of High Resolution NMR in Solids*, Springer Verlag Heidelberg (1983)

R.R. Ernst, G. Bodenhausen, A. Wokaun, *Principles of Nuclear Magnetic Resonance in One and Two Dimensions*, Clarendon Press, Oxford (1987)

#### **NMR Applications to Materials Sciences**

J. Klinowski, Ed. New Techniques in Solid State NMR,
Topics in Current Chemistry, 246, Springer-Verlag Heidelberg 2005.
K. Schmidt-Rohr, H.W. Spiess, Multidimensional Solid-State NMR and
Polymers, Academic Press, London (1996).
M. J. Duer, Introduction into Solid State NMR Spectroscopy, Blackwell Publ. 2004

## **NMR = Nuclear Magnetic Resonance**

- **N: Property of the Atomic Nuclei in Matter**
- M: Magnetic Property, arising from Spin Angular Momentum
- R: Interaction with electromagnetic waves spectroscopy

## **Relationship Spin-magnetic moment**

Classical model: charge q on a circle with radius r



 $\mu$  = current  $\times$  area

Charge q on a circle: velocity:

 $v = 2\pi r/t \to t = 2\pi r/v$ 

current =  $q/t = qv/2\pi r$  $\mu = q v r/2$ area =  $\pi r^2$ 

Angular momentum:  $J = p \times r = m v r$ 

Magnetic moment:  $\mu = J q/2m$  (classical)  $\mu = J \gamma$  (quantum mechanical) γ: gyromagnetic ratio (units T<sup>-1</sup>s<sup>-1</sup>) Magnetic moments interact with magnetic fields

#### **Zeeman interaction:** $E = -\mu B$

B is called "magnetic flux density" and characterizes the strength of the magnetic field: units 1Tesla = Vs/m<sup>2</sup>

Orientational quantization of spin:  $|S_z| = m h/2\pi$ 



#### $F = -dE/dz = -\mu (dB/dz) \cos(\mu,B)$

In an inhomogeneous magnetic field (magnetic field gradient) different spin orientations experience forces of different strengths

#### **Case spin-1/2: Two nuclear spin orientations**

**E(m) = -**  $m\gamma\hbar B_0$  (Zeeman-interaction) The two orientations have different energies, difference depends on the values of  $B_0$  and  $\gamma$ 



# **Stern - Gerlach experiment**



### The Stern – Gerlach experiment, 1922



## **Experiment of Rabi**



**Resonance:**  $\omega = \gamma B_o$ 

# History \*

- 1922 **Stern-Gerlach** Experiment
- 1938 **Rabi-** Experiment
- 1945/46 Purcell/Pound, Bloch: first NMR in cond. matter
- 1948 Bloembergen, Purcell, Pound: relaxation
- 1948 Pake, van-Vleck: dipolar analysis
- 1949 **KNIGHT** shift in metals
- 1950 **Dickinson, Proctor, Yu:** chemical shift
- 1950-s: commercial spectrometers (VARIAN)
- 1952 Gutowsky, Slichter spin-spin coupling
- 1950s Hahn, Slichter, pulsed NMR, spin echo

\*Nobel laureates

## Important milestones

1958	Andrew: magic-angle sample spinning
1966	Ernst, Anderson: pulsed Fourier Transf. NMR
early 1970-s	Lauterbur, Mansfield: NMR Imaging
early 1970s	Jeener, Ernst, Bax: 2-D NMR
1970-s	Wüthrich: Protein structure solutions
1975	Schaefer: cross-polarization
1980-s	Spiess: Polymer dynamics via NMR
1985	Weitekamp: Para Hydrogen polarizaiton
1989	Pines: Xe- and He Hyperpolarizaiton
1990	Tycko: Laser polarization
1990-s	Griffin, Levitt, S. Vega: multipulse NMR 1995
	Frydman: High-res. NMR of Q-nuclei
2000:	Nielsen: SIMPSON software
2000-s:	High-field magnet technology-> 23.6 T
2000-s:	Kutzelnigg, Gauss, Schwarz: DFT-calculations
2000-s	Griffin, Emsley, Bodenhausen: DNP/MAS

## **Nuclear Magnetism**

Nuclear magnetic moment:  $\mu = \gamma \hat{J} = \gamma \hbar \hat{I}$ 

I, the angular momentum, is subject to quantization Z laws, concerning both magnitude and orientation

$$\hat{\vec{\mathbf{I}}}^{2}|I,m\rangle = \mathbf{I}(\mathbf{I}+1)|I,m\rangle$$
$$\hat{\mathbf{I}}_{z}|I,m\rangle = \mathbf{m}|I,m\rangle$$

I: spin quantum number m: orientational quantum number with m=-I,-I+1,...I-1,I 2I +1 orientational states



## **Nuclear spin quantum numbers**



Spin quantum number

#### **Case spin-1/2: Two nuclear spin orientations**

E(m) = - mγħB<sub>0</sub> (Zeeman-interaction) The two orientations have different energies, difference depends on the value of  $\gamma$ 



**NMR is element selective** 

### Precession



The precession (Larmor) frequency of the nuclei is given by

 $\omega_{p} = \gamma B_{eff}$ 

where  $B_{eff} = B_0 + B_{int}$ 

**B**<sub>int</sub> contains important structural and chemical information **NMR measures the precession (Larmor) frequency** 

## How is it done?

By application of a second magnetic field fluctuating with frequency  $\omega_0 \sim \omega_p$ 



**Resonance absorption occurs if**  $\omega_o \sim \omega_p$ 

## Macro-sample: Boltzmann distribution $\implies$ Magnetization $M_z = \sum_i \frac{\mu_i}{V} \left(\frac{A}{m}\right)$

**Calculation of M<sub>z</sub>:** 

$$\mathbf{E}/\mathbf{V} = \Sigma_{i} \mathbf{B}_{0} \mathbf{n}_{i} \boldsymbol{\mu}_{i} / \mathbf{V} = \mathbf{M}_{z} \mathbf{B}_{0}$$

where: 
$$\mu_i = m_i \gamma \hbar$$
  $n_i = \frac{\exp -E_i/k_B T}{\sum_i \exp -E_i/k_B T} N$ 

$$exp - \frac{E_i}{k_B T} \approx 1 - \frac{E_i}{k_B T} \qquad E_i = -m_i \gamma \hbar B_0$$
  
(HT approximation) 
$$\Sigma_i exp - E_i / k_B T = 2I + 1$$

$$\mathbf{E}/\mathbf{V} = \Sigma_{i}(\mathbf{1} + \frac{\mathbf{m}_{i}\gamma\hbar\mathbf{B}_{0}}{k_{B}T})\mathbf{m}_{i}\gamma\hbar\frac{\mathbf{N}}{\mathbf{V}} = \mathbf{M}_{z}\mathbf{B}_{0}$$

Macroscopic magnetization in z-direction :

$$M_{z} = M_{o} = \frac{N/V}{3kT} B_{o}$$
 No net   
NMR is quantitative

No net magnetization in x- or y-direction



## **Macroscopic Sample**



M<sub>z</sub> is the source of the signal:

needs to be made time dependent to measure the precession frequency.

# **The Rotating Frame**

In contrast to the  $B_0$  field, the  $B_1$  field changes direction in time with the frequency  $\omega_0$ 

To simplify the description of the magnetization's time dependence a rotating frame is introduced



Rotating frame rotates with frequency  $\omega_0$  of B<sub>1</sub>

90° pulse:rotates the z-magnetization into the x-y-plane180° pulse:flips the z-magnetization into the -z-direction

# **Measuring NMR spectra**

#### = Detection of Larmor frequencies present in the sample

1.  $B_1$  field is irradiated for a short time  $t_p$  along the x,y direction 2. If  $\gamma B_1 t_p = \pi/2$  then  $M_z$  is flipped by 90 degrees (90° pulse) 3. After the pulse, precession of M induces voltage in the coil. 4. This voltage, oscillating with  $\omega_p$ , is the NMR signal



# **The Basic NMR Experiment**



## **Schematic Experimental Set-up**



# Equipment

magnet

probe

Sample in coil

Console: signal excitation and detection



## **Relaxation Processes**



**Transverse relaxation (T\_2):** dephasing of spins in the x-y plane (distribution of precession frequencies, spin-spin interactions)

**Longitudinal relaxation (T<sub>1</sub>):** build-up of z-magnetization (return to equilibrium, energy exchange with surroundings (lattice)

## **Spatial distribution models in glasses**



Prof. Dr. Hellmut Eckert

### Selective measurement by spin-echo decay



Selective for homonuclear dipole coupling strengths

$$S/S_0 = exp - (2t^2M_2)$$

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# **Four distinct interactions**

- magnetic shielding
- Electric quadrupole coupling
- Indirect spin-spin coupling
- magnetic dipole coupling

In the solid state: anisotropy: ω<sub>p</sub> ~ 3cos<sup>2</sup>θ - 1

# **Magnetic Shielding**

**Resonance frequency (bare nucleus):** 

Effective magnetic field at nucleus:

**Resonance frequency (real sample)** 

$$\omega_0 = \gamma B_0$$
$$B_{eff} = B_0 (1 - \sigma)$$
$$\omega_L = \gamma B_0 (1 - \sigma)$$

**Chemical shift** 

Effective magnetic field arises from shielding or deshielding of the external magnetic field by electrons

**Probe for electronic environment (bonding)** 

$$\mathcal{S} \equiv \frac{\omega_L^x - \omega_L^{ref}}{\omega_L^{ref}}$$

$$\delta \equiv \frac{\omega_L^x - \omega_L'}{c}$$

## **Chemical Shielding Anisotropy**

#### Solid state : chemical shielding is anisotropic: → tensorial description



## **Example : <sup>31</sup>P NMR of Phosphates**



# **Indirect spin-spin Coupling**

- Spin-spin interaction transmitted via polarization of bonding electrons
- HAMILTONIAN

- $\mathcal{H}_{J} = 2\pi \hat{I}_{1} \hat{J} \hat{I}_{2}$  homonuclear  $\mathcal{H}_{J} = 2\pi \hat{I} \hat{J} \hat{S}$  heteronuclear
- Anisotropy accounted for by tensorial description
- Isotropic component: J<sub>iso</sub> (scalar, isotropic coupling constant)
- Liquid-state and MAS-NMR: only J<sub>iso</sub> relevant: Π<sub>i</sub> (2n<sub>i</sub>l<sub>i</sub> +1) multiplicity rule
- n<sub>i</sub> = number of equivalent spins of quantum number I<sub>i</sub> the observed nucleus is coupled to

#### **Mechanism: Spin polarization of bonding electrons**

#### One bond: <sup>1</sup>J >0

Observe nucleus

Observe nucleus





Perturbing Nucleus, m =1/2

Perturbing Nucleus, m = -1/2

#### Two bonds: <sup>2</sup>J < 0



#### Three bonds: <sup>3</sup>J > 0



#### <sup>1</sup>H NMR spectrum of ethanol



### **Examples of Spin-Spin Coupling Multiplicities**


# **Karplus-Relation for J-coupling**



For <sup>3</sup>J (<sup>1</sup>H-<sup>1</sup>H) coupling:

$$J(\phi) = C\cos 2\phi + B\cos \phi + A$$

$$A = 4.22, B = -0.5, \text{ and } C = 4.5 \text{ Hz.}$$

Important for conformational studies (protein folding) Nobel Prize 2013

#### **MAS conditions: isotropic peak splitting**



G. Brunklaus, J. C.C. Chan, H. Eckert, S. Reiser, T. Nilges, A. Pfitzner, Phys. Chem. Chem. Phys. 5, 3678 (2003)

# **Magnetic dipole interactions**

Magnetic moments of nearby spins affect the local magnetic field and thus the resonance frequency. "Through-space" interaction



#### **Dipolar Hamiltonian Terms**



#### Lineshape of a two-spin system



In the liquid state and under MAS conditions: dipole coupling averaged to zero

#### **Second Moment Description of Multi-Spin Interactions**

Specification of an average dipolar coupling in multi-spin systems Where details of the spin geometry are not well known. Using this method distance scenarios can be tested



#### **Relation to structure:**

$$M_{2} = \frac{4}{15} \left(\frac{\mu_{0}}{4\pi}\right)^{2} \gamma_{I}^{2} \gamma_{S}^{2} \hbar^{2} S(S+1) \sum \frac{1}{r_{ij}^{6}} \text{ (hetero)}$$
$$M_{2} = \frac{3}{5} \left(\frac{\mu_{0}}{4\pi}\right)^{2} \gamma^{4} \hbar^{2} I(I+1) \sum \frac{1}{r_{ij}^{6}} \text{ (homo)}$$

 $\sum \frac{1}{r_{ij}^6}$ . Convergence at 4 times the shortest distance

# **Spatial distribution models in glasses**



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### Selective measurement by spin-echo decay



Selective for homonuclear dipole coupling strengths

$$S/S_0 = exp - (2t^2M_2)$$

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### **Spatial Atomic Distributions in P-Se Glasses**



#### P-Se vs. P-P- bonding

D. Lathrop, H. Eckert, J. Am. Chem. Soc. 111 (1989), 3536 D. Lathrop, H. Eckert, Phys. Rev. B 43 (1991), 7279



I = 0 I = 1/2 I  $\ge 1$ ; eQ > 0 I  $\ge 1$ ; eQ < 0 eQ ~ 10<sup>-25</sup> to 10<sup>-30</sup> m<sup>2</sup>

## **Outline**

#### Solid State NMR – General Aspects Anisotropic Interactions: magnetic shielding nuclear electric quadrupole coupling dipole-dipole coupling indirect spin-spin coupling

Manipulation of Interactions magic-angle spinning cross-polarization -J-spectroscopy/INADEQUATE rotational echo double resonance

# **Solid State NMR**

- element-selective
- locally selective
- quantitative
- experimentally flexible: Selective

averaging



# Magic Angle Spinning - MAS



High-resolution spectra, governed by chemical shifts

- -- bonding partners
- -- coordination numbers

# **Magic Angle Spinning**



# **MAS-NMR probe**







Macor Kel-F ZrO<sub>2</sub> BN Vespel

# The effect of spinning speed





I = 0 I = 1/2 I  $\ge 1$ ; eQ > 0 I  $\ge 1$ ; eQ < 0 eQ ~ 10<sup>-25</sup> to 10<sup>-30</sup> m<sup>2</sup>

# The physical picture



This quadrupole moment interacts with local electric field gradients created by the bonding environment of the nuclei. -> probe of local symmetry

#### For axially symmetric EFG, the 1<sup>st</sup> order correction is:

$$\left< m \left| \hat{H}_{Q} \right| m \right> = \frac{e^2 q Q}{4I(2I-1)} \left[ 3m^2 \cos^2 \theta + \frac{3}{2}I(I+1)\sin^2 \theta - \frac{3}{2}m^2 \sin^2 \theta - I(I+1) \right]$$

$$E_{m}^{(1)} = -m\gamma\hbar B_{o} + \frac{e^{2}qQ}{4I(2I-1)} \left[3m^{2} - I(I+1)\right] \frac{3\cos^{2}\theta - 1}{2}$$

#### **Energy level diagram for I = 3/2**





#### **Powder samples: orientational averaging case I = 3/2**



# **Powder pattern for spin-7/2**



# **Stronger Quadrupole Coupling:**

#### **Second-order perturbation theory**



### **Solid State NMR Periodic Table**

<sup>1</sup> H		I															<sup>3</sup> He
<sup>7</sup> Li	<sup>9</sup> Be											<sup>11</sup> B	<sup>13</sup> C	<sup>15</sup> N	<sup>17</sup> O	<sup>19</sup> F	<sup>21</sup> Ne
<sup>23</sup> Na	<sup>25</sup> Mg											<sup>27</sup> AI	<sup>29</sup> Si	<sup>31</sup> P	<sup>33</sup> S	<sup>35</sup> Cl	Ar
<sup>39</sup> K	<sup>43</sup> Ca	<sup>45</sup> Sc	<sup>49</sup> Ti	<sup>51</sup> V	<sup>53</sup> Cr	<sup>55</sup> Mn	<sup>57</sup> Fe	<sup>59</sup> Co	<sup>61</sup> Ni	<sup>63</sup> Cu	<sup>67</sup> Zn	<sup>71</sup> Ga	<sup>73</sup> Ge	<sup>75</sup> As	<sup>77</sup> Se	<sup>79</sup> Br	<sup>87</sup> Kr
<sup>87</sup> Rb	<sup>87</sup> Sr	<sup>89</sup> Y	<sup>91</sup> Zr	<sup>93</sup> Nb	<sup>95</sup> Mo	<sup>99</sup> Tc	<sup>99</sup> Ru	¹⁰³Rh	<sup>105</sup> Pd	<sup>109</sup> Ag	<sup>113</sup> Cd	<sup>115</sup> ln	<sup>117</sup> Sn	<sup>121</sup> Sb	<sup>125</sup> Te	127	<sup>129</sup> Xe
<sup>133</sup> Cs	<sup>137</sup> Ba	<sup>139</sup> La	<sup>179</sup> Hf	<sup>181</sup> Ta	183 <b>W</b>	<sup>185</sup> Re	<sup>187</sup> Os	<sup>191</sup> lr	<sup>195</sup> Pt	<sup>197</sup> Au	<sup>199</sup> Hg	205 <b>T</b>	<sup>207</sup> Pb	<sup>209</sup> Bi	Ро	At	Rn
Fr	Ra	Ac														L	J



#### Standard

Isotope enrichment required

NMR restricted by quadrupolar interactions

Dominant quadrupolar interaction

Very small magnetic moment

### NMR as a Technique in Solid State Sciences

Local Selectivity:	<b>Disorder/Lack of Periodicity</b>
Element Selectivity:	Compositional Complexity Low Scattering Contrast (H; Si/AI)
Interaction Selectivity:	Distance Measurements Connectivity Information Electron Density Information
Uniform Sensitivity:	Quantitative Applications
Dynamic Sensitivity:	Motional Processes on Continuous Timescale (10 <sup>2</sup> to 10 <sup>-9</sup> s)
Low Detection Sensitivity: Bulk Method:	10 <sup>17</sup> to 10 <sup>18</sup> spins required poor spatial resolution surfaces/interfaces difficult to study
Magnetic Interference:	transition metals, rare earths: limited

### NMR spectroscopy of insensitive nuclei:

**Problems with direct detection of <sup>13</sup>C, <sup>15</sup>N and others:** 

-Low natural abundance -Small magnetic moments -Long spin-lattice relaxation times

**Basic idea of cross-polarization (CP):** 

exploit dipole-dipole coupling with abundant <sup>1</sup>H nuclei in the sample to transfer magnetization from <sup>1</sup>H to <sup>13</sup>C spins

Matching of energy levels required E (flip-flop mechanism), not possible in the lab frame



## The crosspolarization pulse sequence



Hartmann-Hahn matching condition

$$\gamma_{1H}B_{1H} = \gamma_{13C}B_{13C}$$

# <sup>13</sup>C- NMR spectra of adamantane



static, with <sup>1</sup>H-decoupling ∆=500 Hz

MAS, no <sup>1</sup>H-decoupling ∆=50 Hz

MAS, with <sup>1</sup>H-decoupling  $\Delta = 5$  Hz



#### **Poly-dicarbazolyl-hexadiyne (poly DCH)**

$$\begin{bmatrix} CH_2R \\ 0 \\ C - C \equiv C - C \end{bmatrix} R - CH_2 - C \equiv C - C \equiv C - CH_2 - R$$

$$\begin{bmatrix} R - CH_2 - C \equiv C - C \equiv C - CH_2 - R \\ 0 \\ CH_2R \end{bmatrix}$$





## **Variable Contact time experiments**



### **CP MAS with delayed decoupling**





# **CPMAS of poly-DCH**



#### **2-D Heteronuclear correlation NMR**





correlates the <sup>13</sup>C resonances with those <sup>1</sup>H species from which the magnetization is transferred the fastest = typically the directly bonded protons

# High Resolution <sup>1</sup>H/<sup>13</sup>C HETCOR



#### **A Modern 2D HETCOR Sequence**





G. Paul, S. Steuernagel, H. Koller, Chem. Commun. 2007, 5194

# **Cross-polarization dynamics**



Variable contact time curves are influenced by three distinct time constants
### **Separate measurement of T<sub>1</sub>(H)**



With the further assumption that  $T_{1\rho}(^{13}C)$  is very long, these variable contact times can be fitted, yielding  $T_{CP}$ 

$$I(t) = B(1 - T_{CP} / T_{1\rho}^{H})^{-1} \left[ exp(-t / T_{1\rho}^{H}) - exp(-t / T_{CP}) \right]$$

## Variable Contact time Experiments in <sup>29</sup>Si{<sup>1</sup>H} CPMAS of amorphous silica



 $A = SiO_{4/2}$   $B = SiO_{3/2}OH$  $C = SiO_{2/2}(OH)_2$ 

# Electron-> Nuclear Dynamic Polarization (DNP)



#### **Organic Biradicals as nuclear polarizers**



#### **Pulse Sequence for Dynamic Nuclear Polarization**



### An application: surface selective NMR: Functionalization of MCM silica surface

#### **DNP enhanced <sup>13</sup>C-NMR**

