

Eletromagnetismo

$$\vec{\nabla} \cdot \vec{D} = \frac{\rho}{\epsilon_0}$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

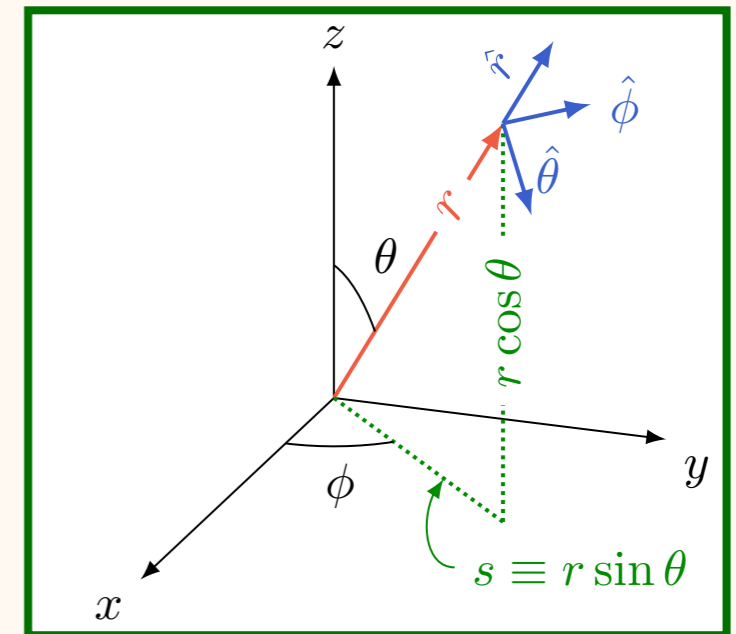
$$\vec{\nabla} \times \vec{H} = \vec{j} + \epsilon_0 \frac{\partial \vec{D}}{\partial t}$$

Aula de 14 de junho
Métodos especiais

Coordenadas esféricas

$$d\vec{\ell} = dr \hat{r} + r d\theta \hat{\theta} + r \sin \theta d\phi \hat{\phi}$$

$$\vec{\nabla} t = \frac{\partial t}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial t}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial t}{\partial \phi} \hat{\phi}$$



$$\vec{\nabla} \cdot \vec{v} = \frac{1}{r^2} \frac{\partial (r^2 v_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial (\sin \theta v_\theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial v_\phi}{\partial \phi}$$

$$\begin{aligned} \vec{\nabla} \times \vec{v} = & \frac{1}{r \sin \theta} \left[\frac{\partial}{\partial \theta} (\sin \theta v_\phi) - \frac{\partial v_\theta}{\partial \phi} \right] \hat{r} \\ & + \frac{1}{r} \left[\frac{1}{\sin \theta} \frac{\partial v_r}{\partial \phi} - \frac{\partial}{\partial r} (r v_\phi) \right] \hat{\theta} + \frac{1}{r} \left[\frac{\partial}{\partial r} (r v_\theta) - \frac{\partial v_r}{\partial \theta} \right] \hat{\phi} \end{aligned}$$

$$\nabla^2 t = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial t}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial t}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 t}{\partial \phi^2}$$

Coordenadas cilíndricas

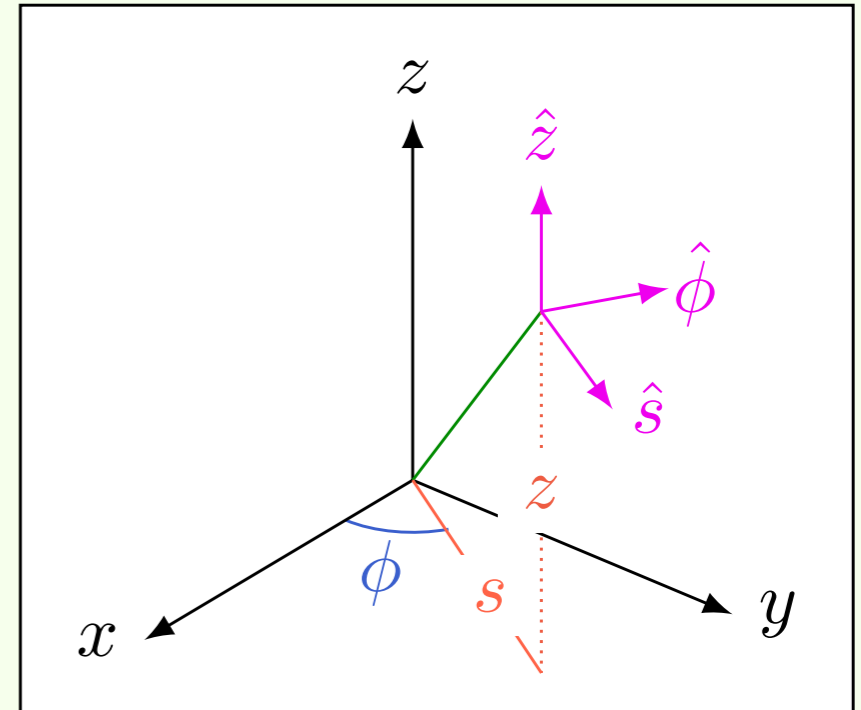
$$d\vec{\ell} = ds \hat{s} + s d\phi \hat{\phi} + dz \hat{z}$$

$$\vec{\nabla} T = \frac{\partial T}{\partial s} \hat{s} + \frac{1}{s} \frac{\partial T}{\partial \phi} \hat{\phi} + \frac{\partial T}{\partial z} \hat{z}$$

$$\vec{\nabla} \cdot \vec{v} = \frac{1}{s} \frac{\partial (sv_s)}{\partial s} + \frac{1}{s} \frac{\partial v_\phi}{\partial \phi} + \frac{\partial v_z}{\partial z}$$

$$\vec{\nabla} \times \vec{v} = \left(\frac{1}{s} \frac{\partial v_z}{\partial \phi} - \frac{\partial v_\phi}{\partial z} \right) \hat{s} + \left(\frac{\partial v_s}{\partial z} - \frac{\partial v_z}{\partial s} \right) \hat{\phi} + \frac{1}{s} \left(\frac{\partial (sv_\phi)}{\partial s} - \frac{\partial v_s}{\partial \phi} \right) \hat{z}$$

$$\nabla^2 T = \frac{1}{s} \frac{\partial}{\partial s} \left(s \frac{\partial T}{\partial s} \right) + \frac{1}{s^2} \frac{\partial^2 T}{\partial \phi^2} + \frac{\partial^2 T}{\partial z^2}$$

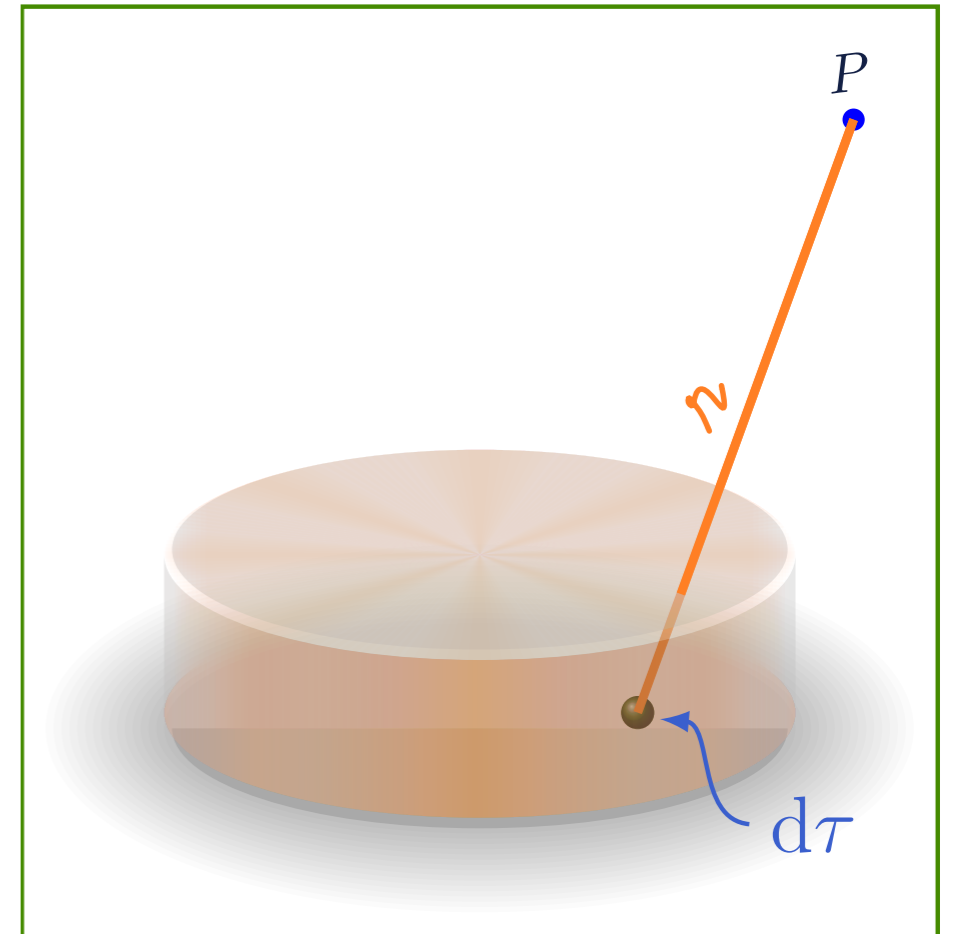


Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$\frac{1}{r} = \frac{1}{r} \sum_{\ell=0}^{\infty} \left(\frac{r'}{r}\right)^{\ell} P_{\ell}(\cos \theta')$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \sum_{n=0}^{\infty} \frac{1}{r^{n+1}} \int (r')^n P_n(\cos \theta') \rho(\vec{r}') d\tau'$$



Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$\frac{1}{r} = \frac{1}{r} \sum_{\ell=0}^{\infty} \left(\frac{r'}{r}\right)^{\ell} P_{\ell}(\cos \theta')$$

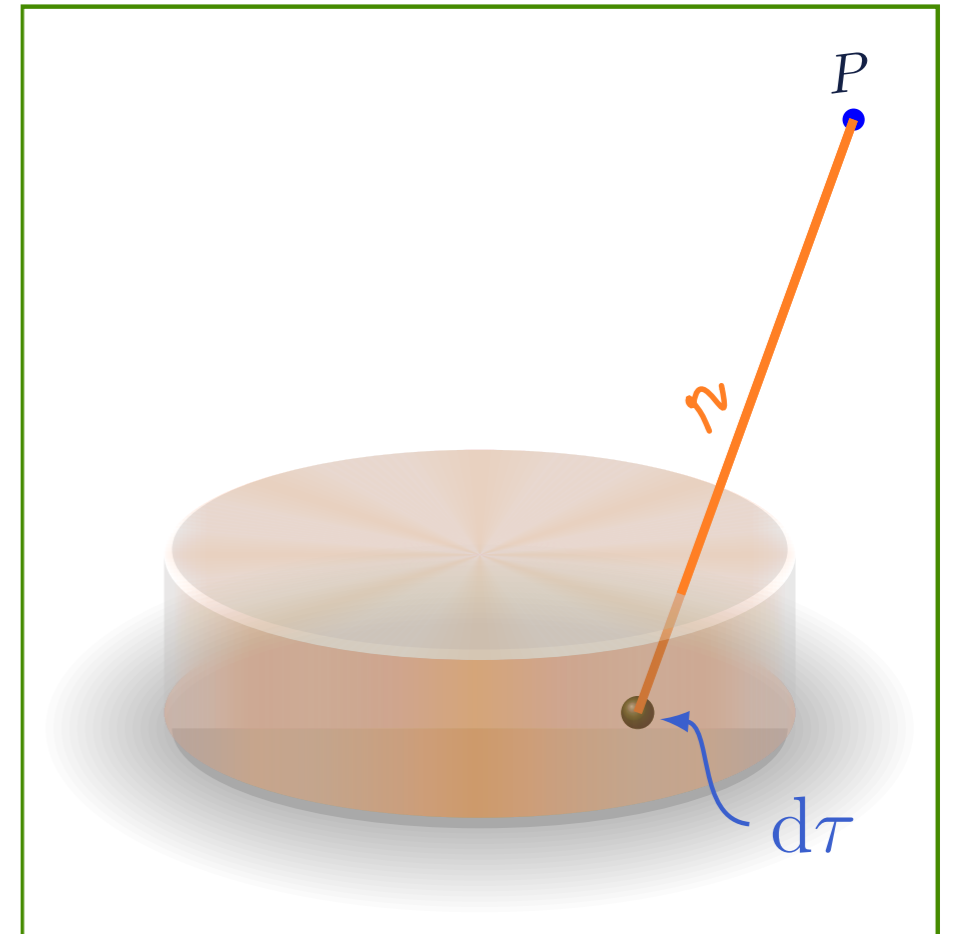
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \sum_{n=0}^{\infty} \frac{1}{r^{n+1}} \int (r')^n P_n(\cos \theta') \rho(\vec{r}') d\tau'$$

$$n = 0 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$$

$$\left[Q = \int \rho(\vec{r}') d\tau' \right]$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

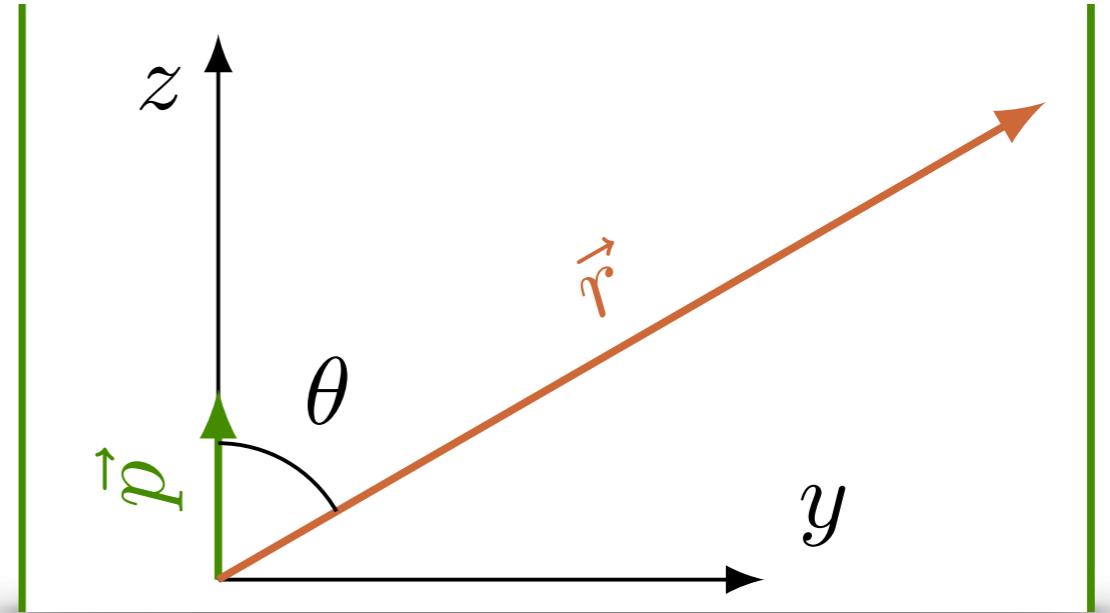
$$\left[\vec{p} = \int \vec{r}' \rho(\vec{r}') d\tau' \right]$$



Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$



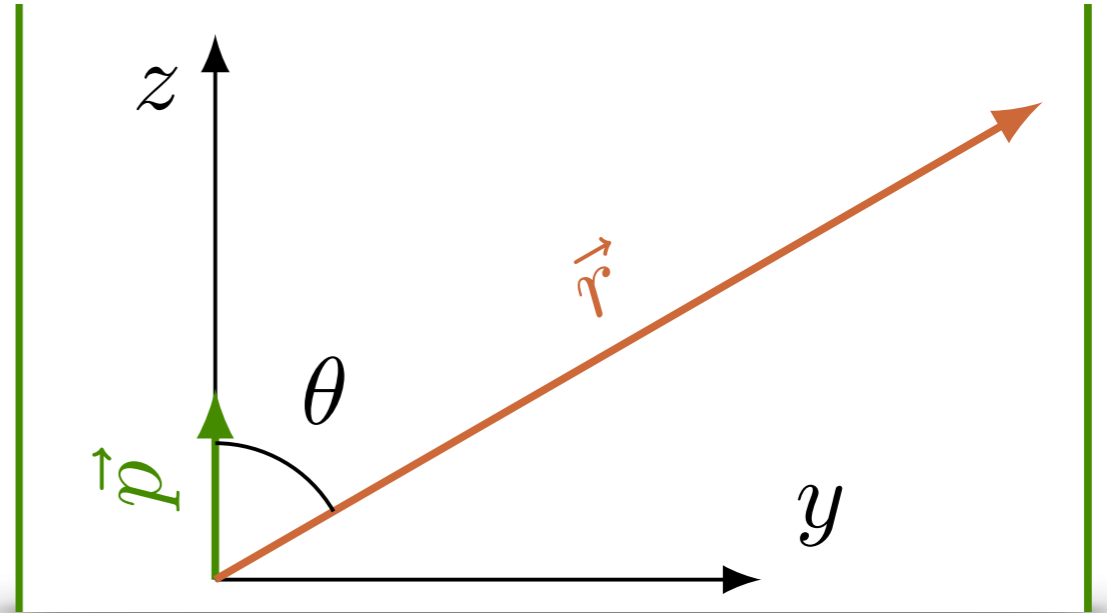
$$\vec{E} = -\vec{\nabla}V(r, \theta, \phi)$$

Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$



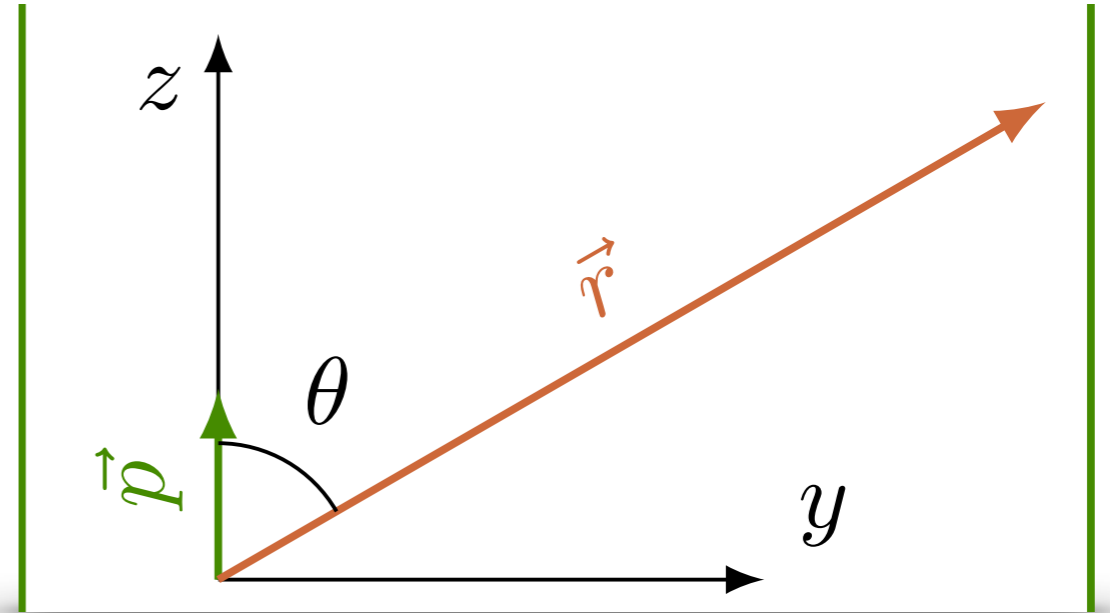
Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$

$$\vec{E} = -\vec{\nabla} V(r, \theta, \phi)$$



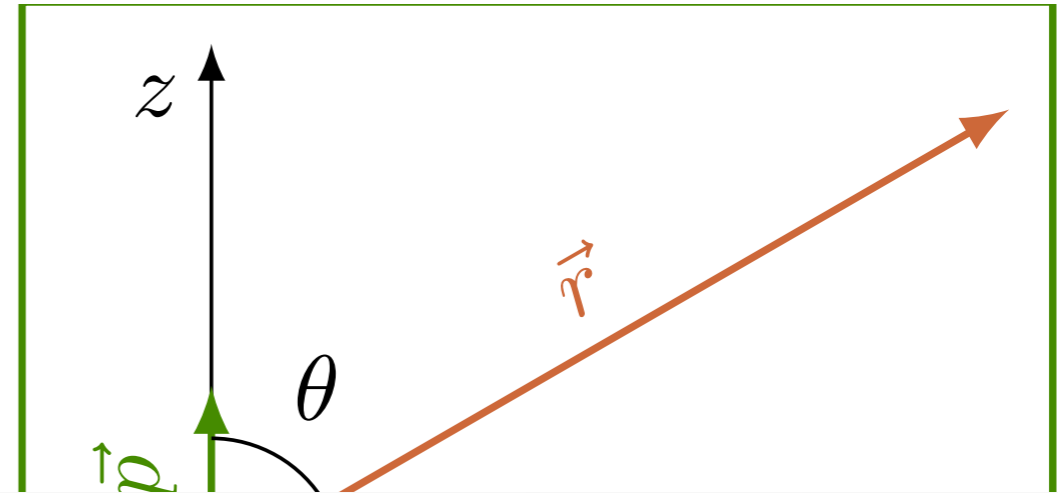
Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$

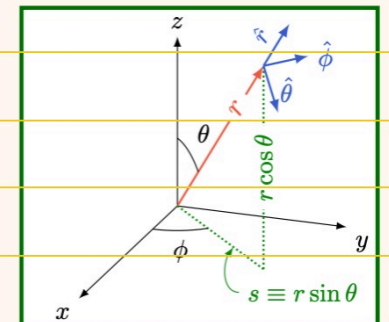
$$\vec{E} = -\vec{\nabla} V(r, \theta, \phi)$$



Coordenadas esféricas

$$d\vec{\ell} = dr \hat{r} + r d\theta \hat{\theta} + r \sin \theta d\phi \hat{\phi}$$

$$\vec{\nabla} t = \frac{\partial t}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial t}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial t}{\partial \phi} \hat{\phi}$$



$$\vec{\nabla} \cdot \vec{v} = \frac{1}{r^2} \frac{\partial (r^2 v_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial (\sin \theta v_\theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial v_\phi}{\partial \phi}$$

$$\vec{\nabla} \times \vec{v} = \frac{1}{r \sin \theta} \left[\frac{\partial}{\partial \theta} (\sin \theta v_\phi) - \frac{\partial v_\theta}{\partial \phi} \right] \hat{r} + \frac{1}{r} \left[\frac{1}{\sin \theta} \frac{\partial v_r}{\partial \phi} - \frac{\partial}{\partial r} (r v_\phi) \right] \hat{\theta} + \frac{1}{r} \left[\frac{\partial}{\partial r} (r v_\theta) - \frac{\partial v_r}{\partial \theta} \right] \hat{\phi}$$

$$\nabla^2 t = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial t}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial t}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 t}{\partial \phi^2}$$

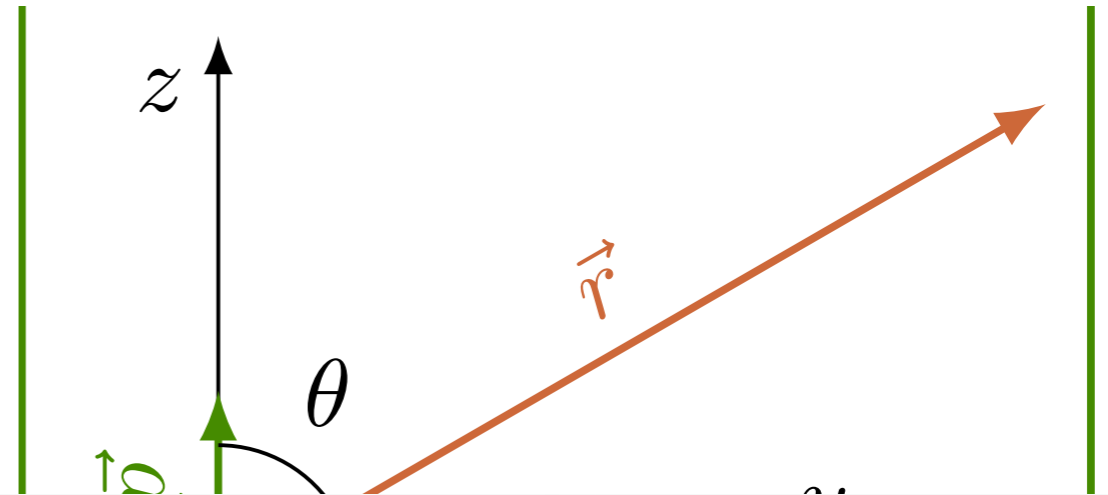
Expansão em multipolos

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \left(\frac{2p \cos \theta}{r^3} \hat{r} + \frac{p \sin \theta}{r^3} \hat{\theta} \right)$$



Coordenadas esféricas

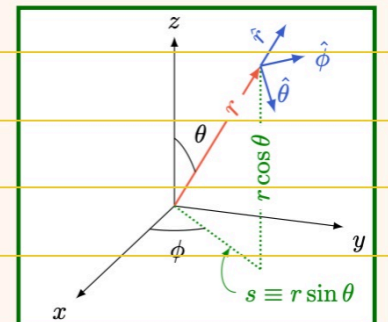
$$d\vec{\ell} = dr \hat{r} + r d\theta \hat{\theta} + r \sin \theta d\phi \hat{\phi}$$

$$\vec{\nabla} t = \frac{\partial t}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial t}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial t}{\partial \phi} \hat{\phi}$$

$$\vec{\nabla} \cdot \vec{v} = \frac{1}{r^2} \frac{\partial (r^2 v_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial (\sin \theta v_\theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial v_\phi}{\partial \phi}$$

$$\vec{\nabla} \times \vec{v} = \frac{1}{r \sin \theta} \left[\frac{\partial}{\partial \theta} (\sin \theta v_\phi) - \frac{\partial v_\theta}{\partial \phi} \right] \hat{r} + \frac{1}{r} \left[\frac{1}{\sin \theta} \frac{\partial v_r}{\partial \phi} - \frac{\partial}{\partial r} (r v_\phi) \right] \hat{\theta} + \frac{1}{r} \left[\frac{\partial}{\partial r} (r v_\theta) - \frac{\partial v_r}{\partial \theta} \right] \hat{\phi}$$

$$\nabla^2 t = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial t}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial t}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 t}{\partial \phi^2}$$



Expansão em multipolos

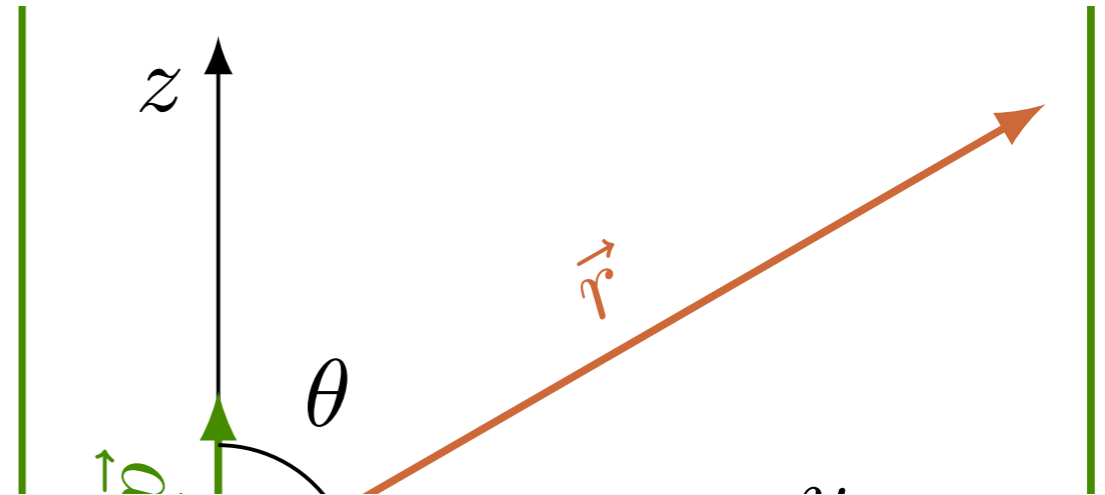
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \left(\frac{2p \cos \theta}{r^3} \hat{r} + \frac{p \sin \theta}{r^3} \hat{\theta} \right)$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{p}{r^3} (2 \cos \theta \hat{r} + \sin \theta \hat{\theta})$$



Coordenadas esféricas

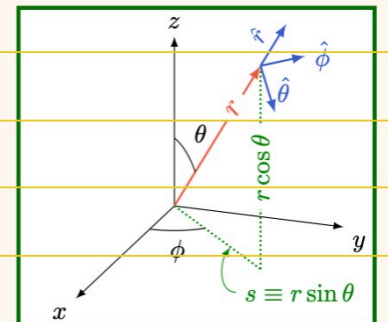
$$d\vec{\ell} = dr \hat{r} + r d\theta \hat{\theta} + r \sin \theta d\phi \hat{\phi}$$

$$\vec{\nabla} t = \frac{\partial t}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial t}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial t}{\partial \phi} \hat{\phi}$$

$$\vec{\nabla} \cdot \vec{v} = \frac{1}{r^2} \frac{\partial (r^2 v_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial (\sin \theta v_\theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial v_\phi}{\partial \phi}$$

$$\vec{\nabla} \times \vec{v} = \frac{1}{r \sin \theta} \left[\frac{\partial}{\partial \theta} (\sin \theta v_\phi) - \frac{\partial v_\theta}{\partial \phi} \right] \hat{r} + \frac{1}{r} \left[\frac{1}{\sin \theta} \frac{\partial v_r}{\partial \phi} - \frac{\partial}{\partial r} (r v_\phi) \right] \hat{\theta} + \frac{1}{r} \left[\frac{\partial}{\partial r} (r v_\theta) - \frac{\partial v_r}{\partial \theta} \right] \hat{\phi}$$

$$\nabla^2 t = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial t}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial t}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 t}{\partial \phi^2}$$



Expansão em multipolos

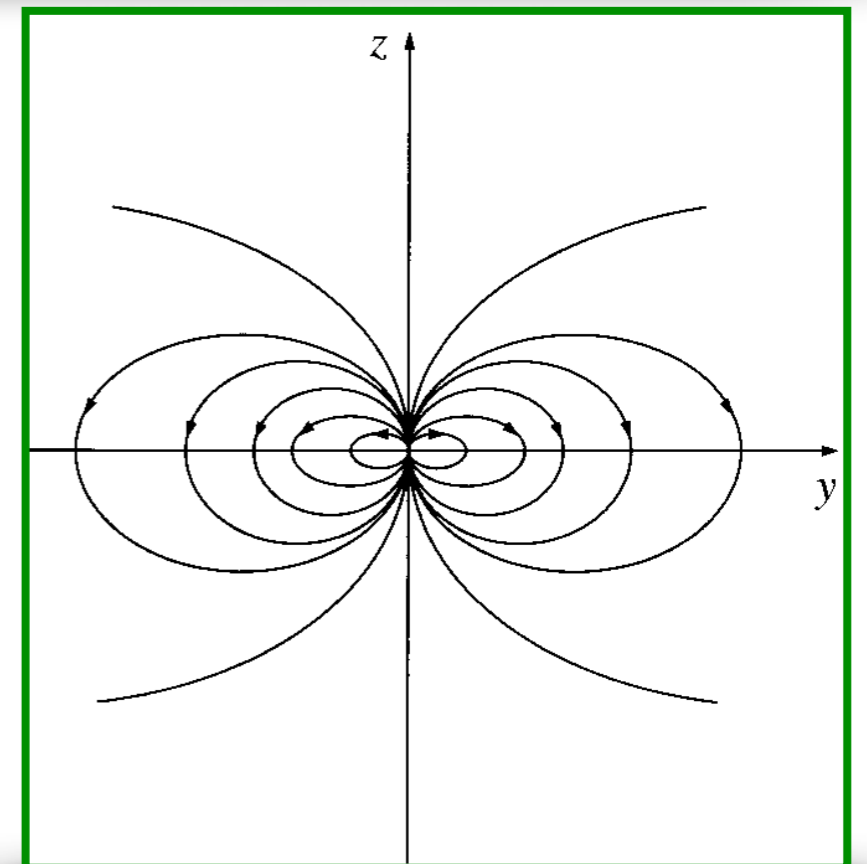
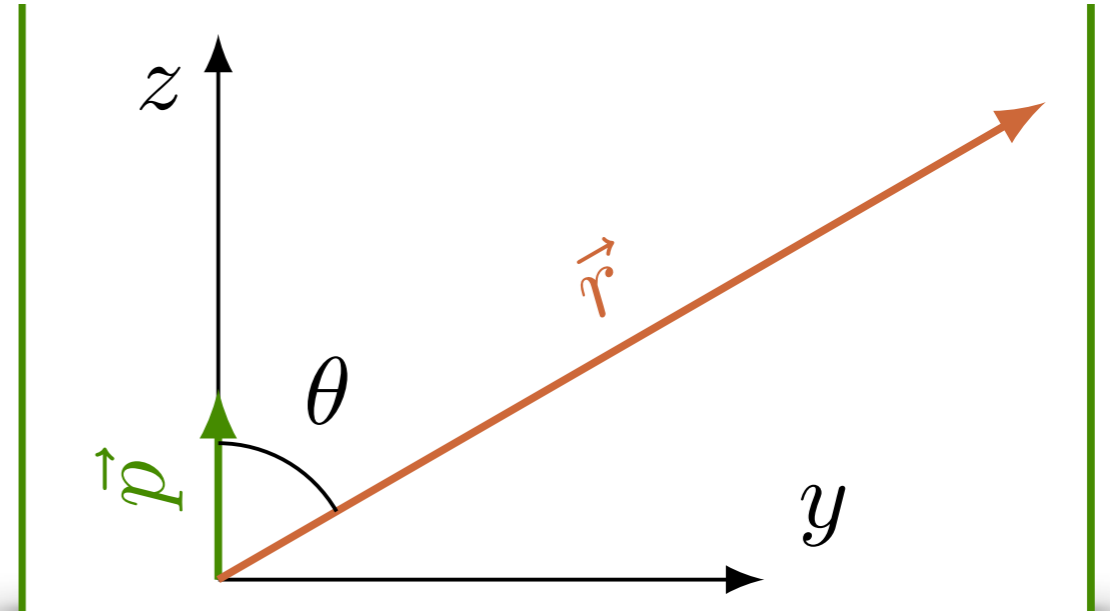
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{r} d\tau$$

$$n = 1 \Rightarrow V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \left(\frac{2p \cos \theta}{r^3} \hat{r} + \frac{p \sin \theta}{r^3} \hat{\theta} \right)$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{p}{r^3} (2 \cos \theta \hat{r} + \sin \theta \hat{\theta})$$



Eletromagnetismo

$$\vec{\nabla} \cdot \vec{D} = \frac{\rho}{\epsilon_0}$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

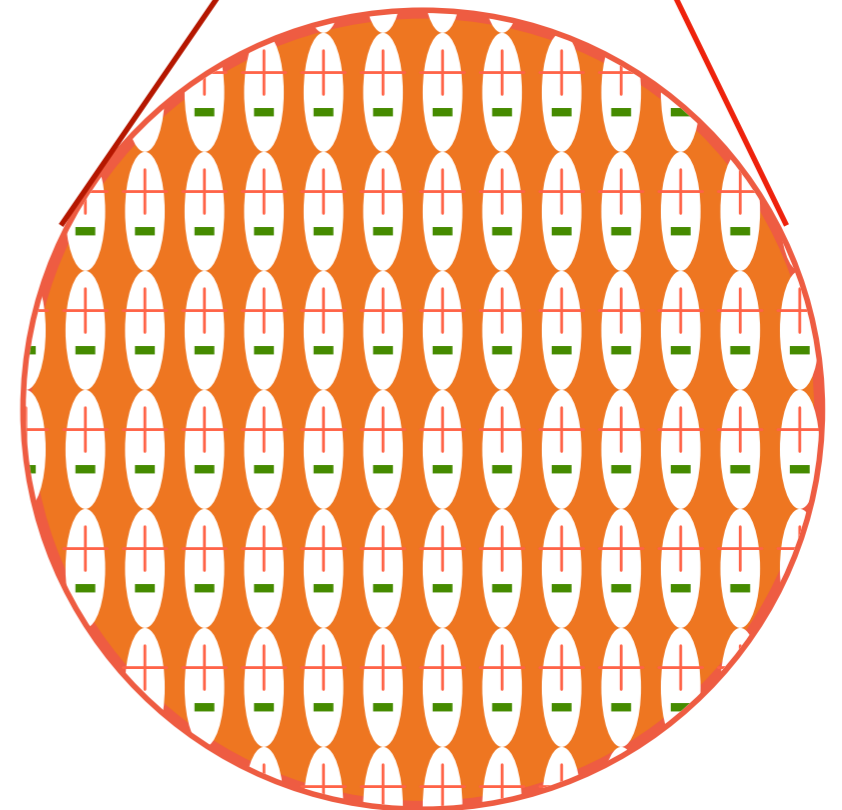
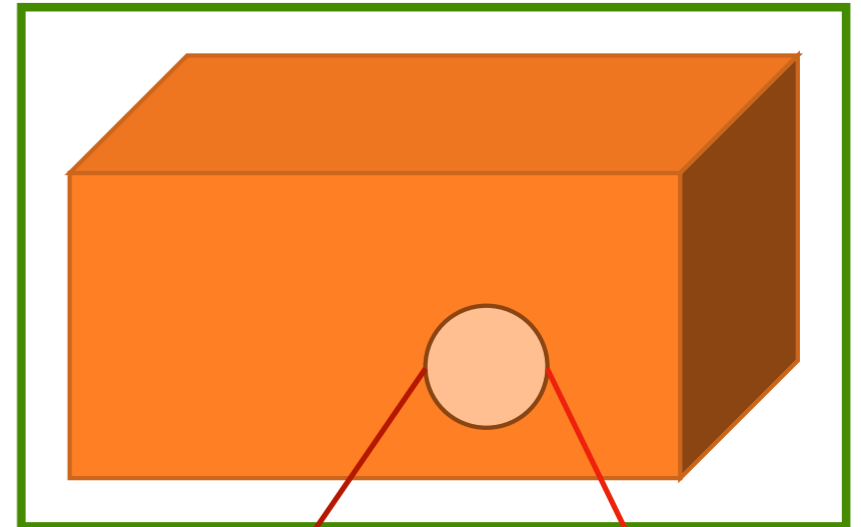
$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\vec{\nabla} \times \vec{H} = \vec{j} + \epsilon_0 \frac{\partial \vec{D}}{\partial t}$$

Dielétricos

Polarização

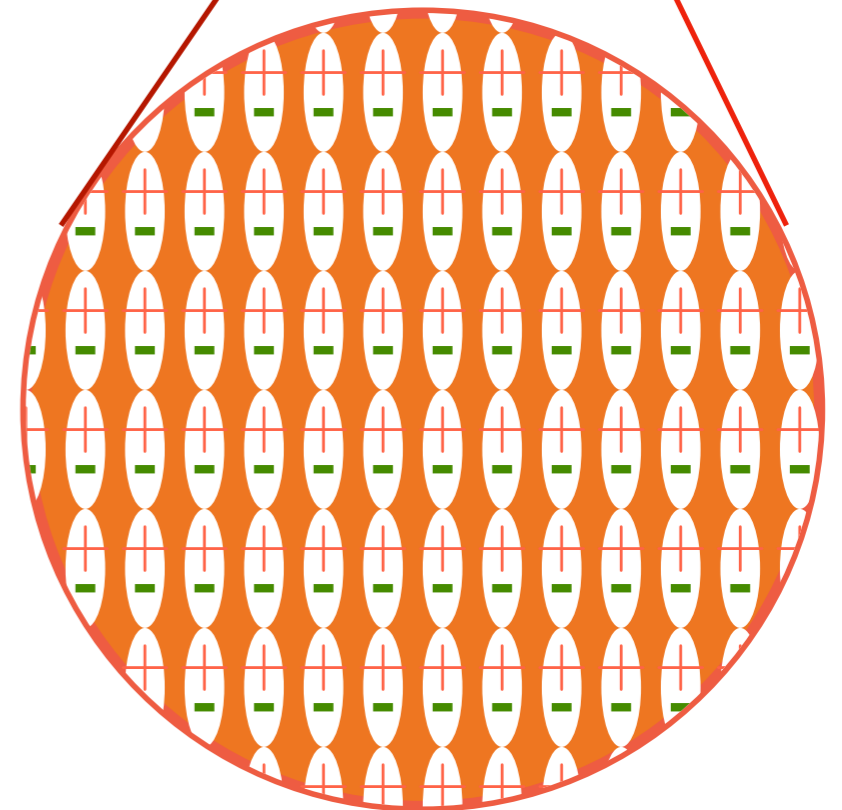
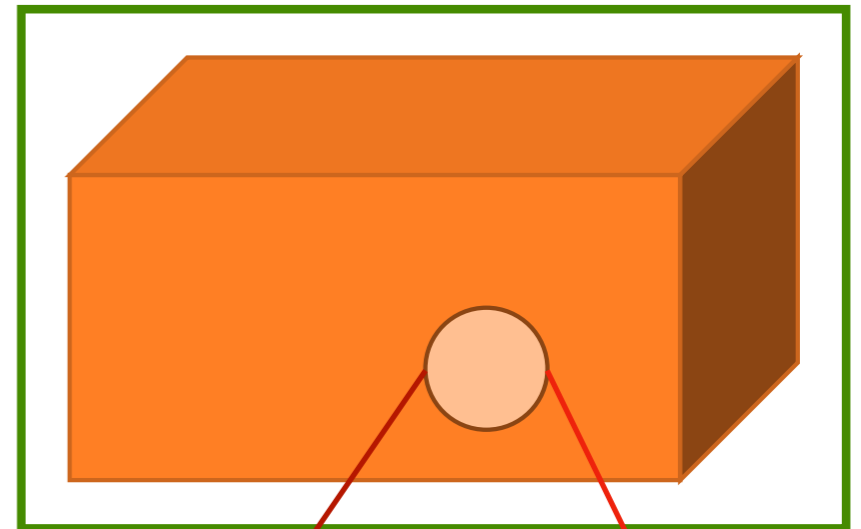
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$



Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$\vec{P} = \frac{\sum_j \vec{p}_j}{\Delta\tau} \quad (\text{Polarização})$$

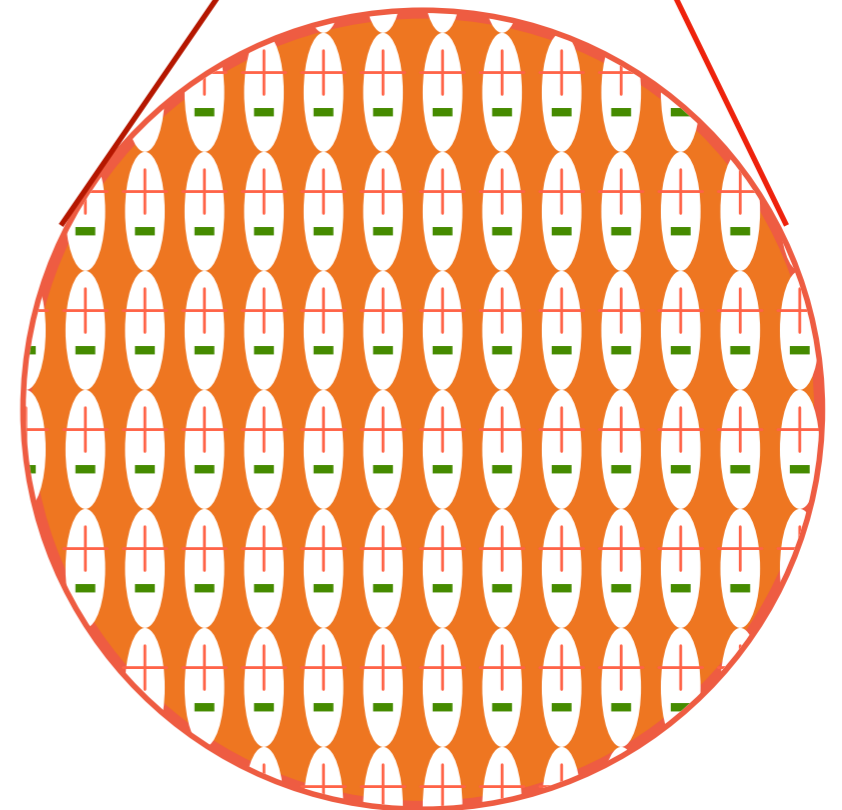
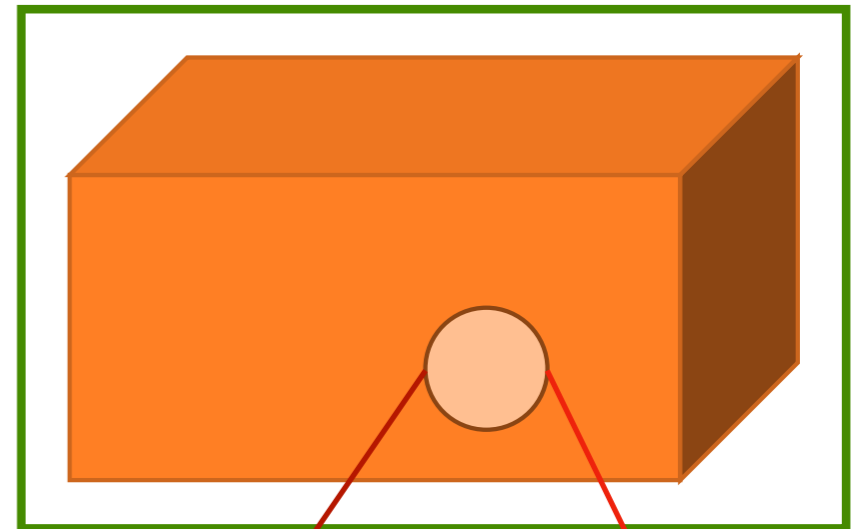


Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$\vec{P} = \frac{\sum_j \vec{p}_j}{\Delta\tau}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\hat{r} \cdot \vec{P}(\vec{r}')}{r^2} d\tau'$$



Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

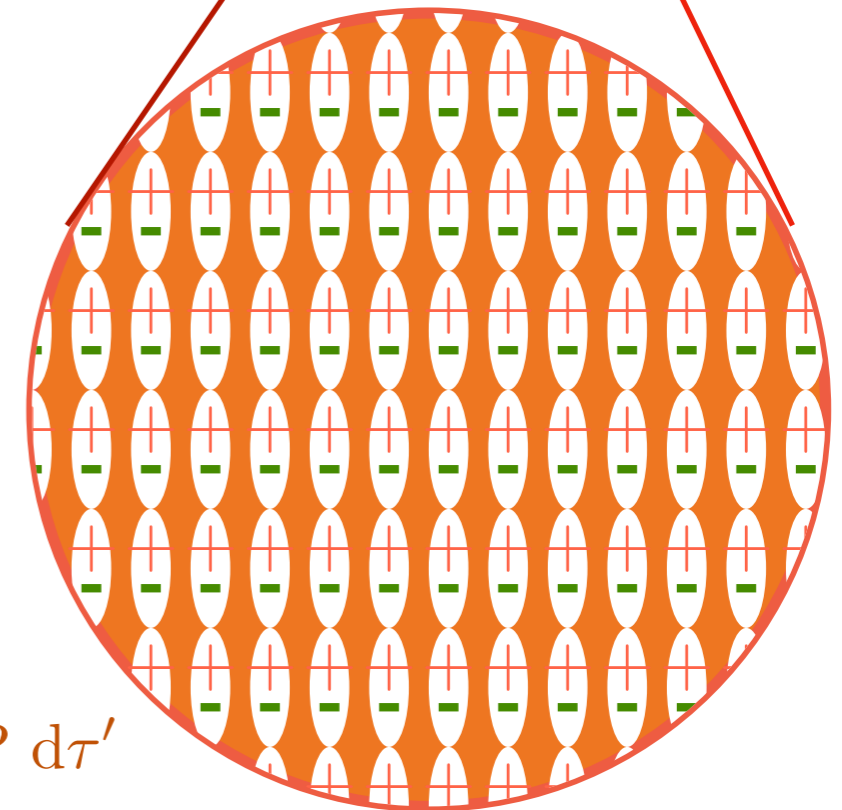
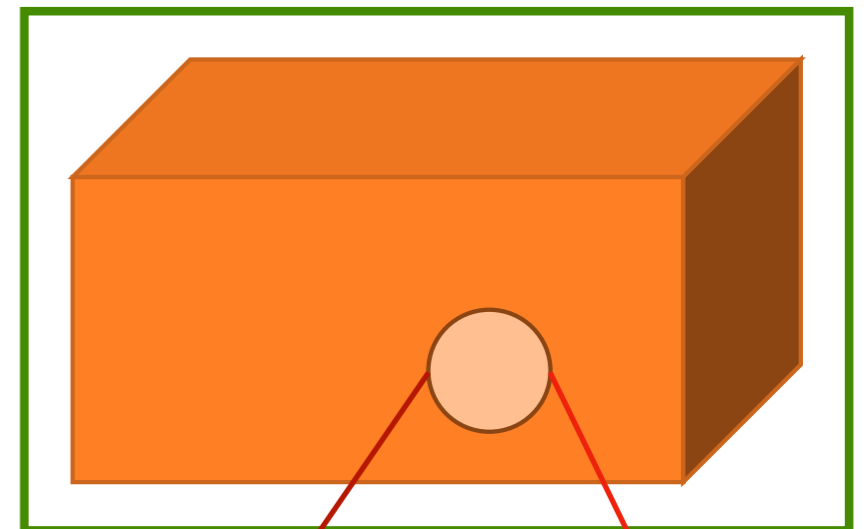
$$\vec{P} = \frac{\sum_j \vec{p}_j}{\Delta\tau}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\hat{r} \cdot \vec{P}(\vec{r}')}{r^2} d\tau'$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \vec{P}(\vec{r}') \cdot \vec{\nabla}' \left(\frac{1}{r} \right) d\tau'$$

$$\vec{\nabla}' \cdot \left(\frac{\vec{P}}{r} \right) = \frac{1}{r} \vec{\nabla}' \cdot \vec{P} + \vec{P} \cdot \vec{\nabla}' \left(\frac{1}{r} \right)$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \vec{\nabla}' \cdot \left(\frac{\vec{P}(\vec{r}')}{r} \right) d\tau' - \frac{1}{4\pi\epsilon_0} \int \frac{1}{r} \vec{\nabla}' \cdot \vec{P} d\tau'$$

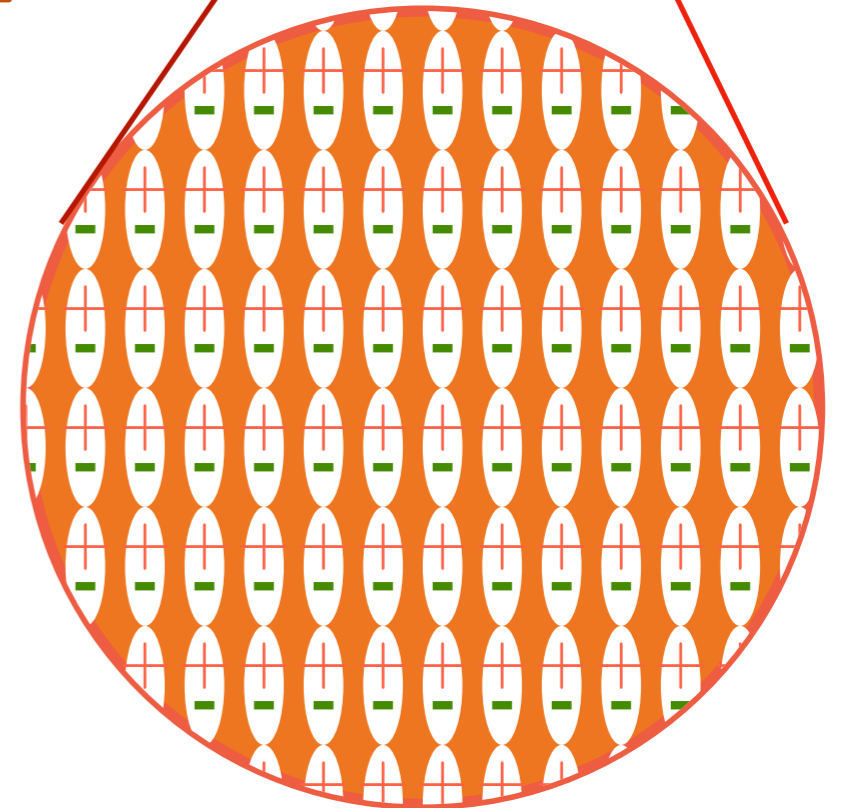
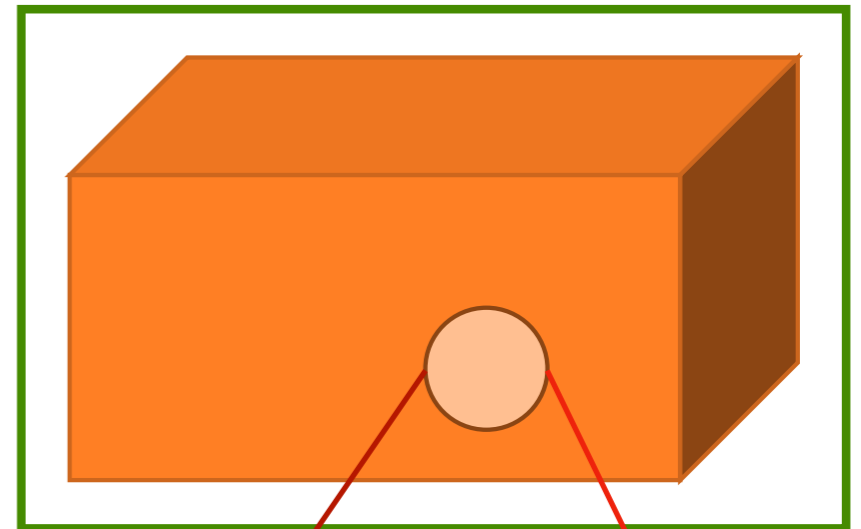


Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

$$\vec{P} = \frac{\sum_j \vec{p}_j}{\Delta\tau}$$

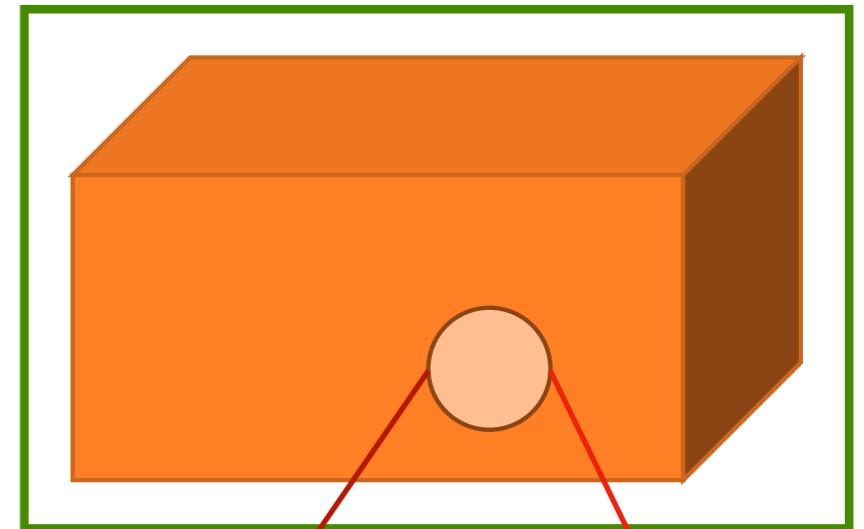
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \vec{\nabla}' \cdot \left(\frac{\vec{P}(\vec{r}')}{r} \right) d\tau' - \frac{1}{4\pi\epsilon_0} \int \frac{1}{r} \vec{\nabla}' \cdot P d\tau'$$



Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}$$

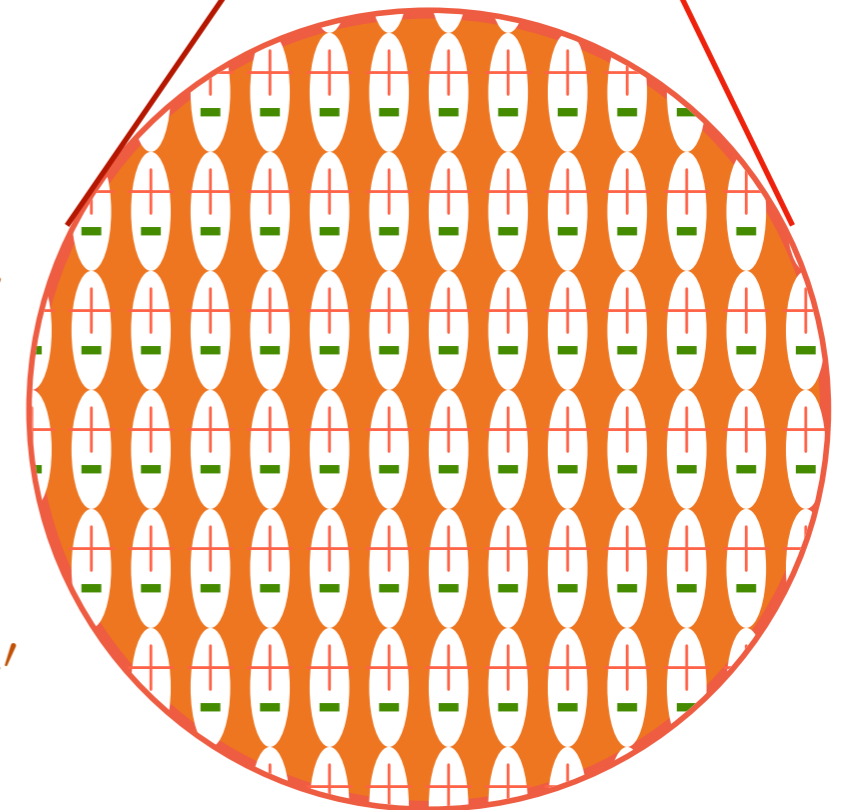
$$\vec{P} = \frac{\sum_j \vec{p}_j}{\Delta\tau}$$



$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{1}{r} \vec{P}(\vec{r}') \cdot \hat{n} \, d\tau' - \frac{1}{4\pi\epsilon_0} \int \frac{1}{r} \vec{\nabla}' \cdot \vec{P} \, d\tau'$$

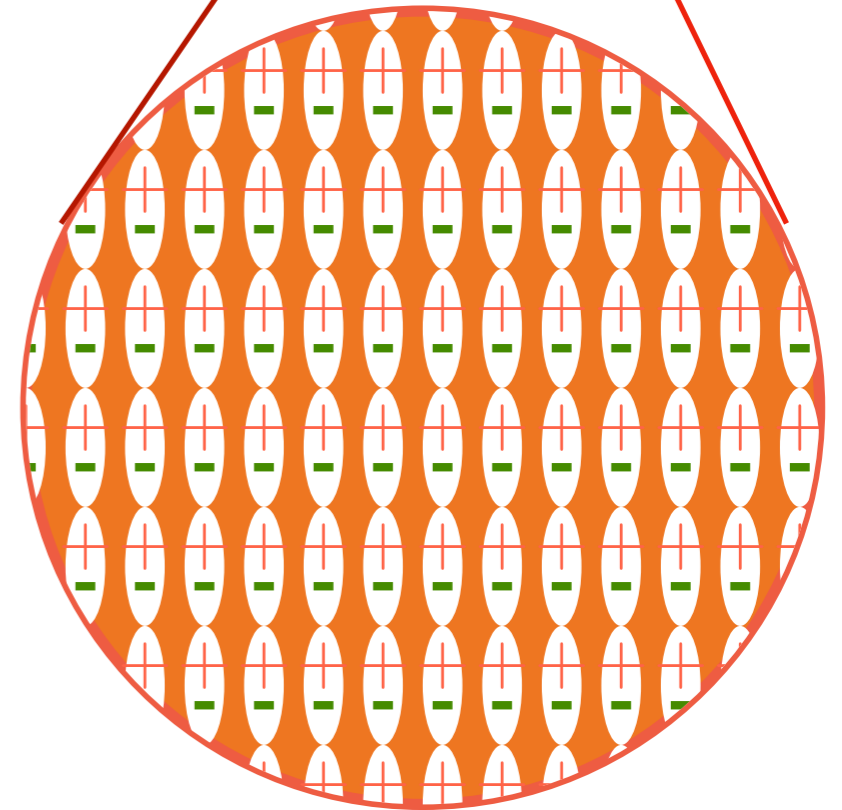
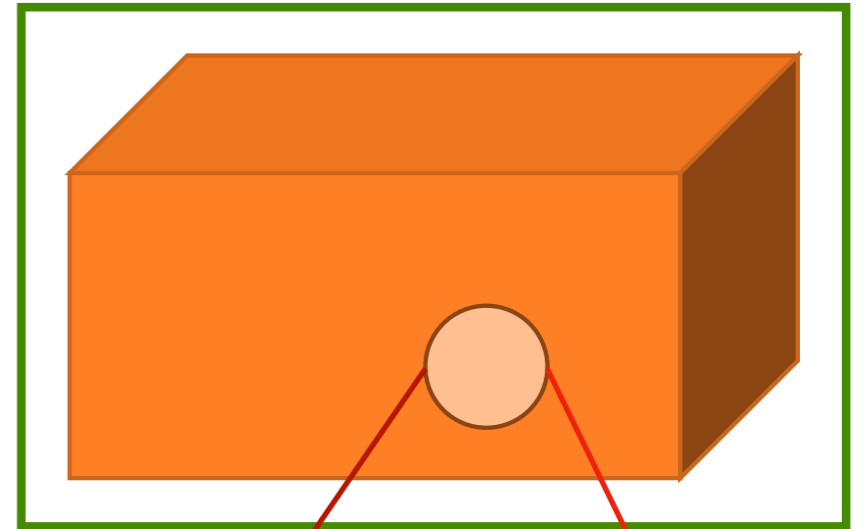
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{1}{r} \vec{P}(\vec{r}') \cdot \hat{n} \, d\tau' - \frac{1}{4\pi\epsilon_0} \int \frac{1}{r} \vec{\nabla}' \cdot \vec{P} \, d\tau'$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{1}{r} \vec{P}(\vec{r}') \cdot \hat{n} \, dA - \frac{1}{4\pi\epsilon_0} \int_V \frac{1}{r} \vec{\nabla}' \cdot \vec{P} \, d\tau'$$



Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_{\mathcal{S}} \frac{1}{r} \vec{P}(\vec{r}') \cdot \hat{n} \, dA - \frac{1}{4\pi\epsilon_0} \int_{\mathcal{V}} \frac{1}{r} \vec{\nabla}' \cdot \vec{P} \, d\tau'$$

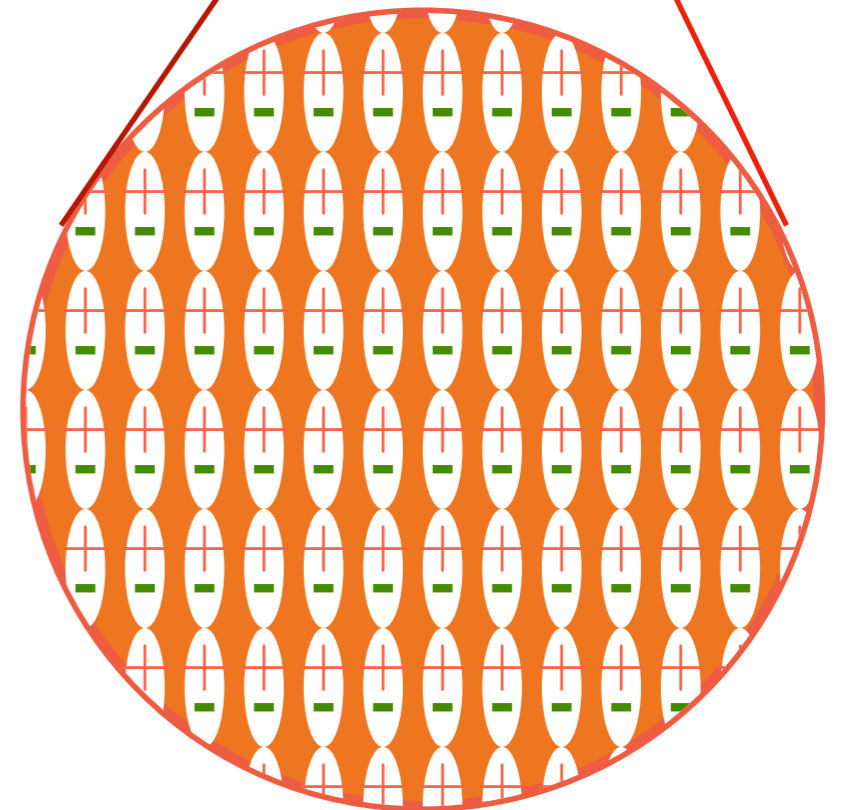
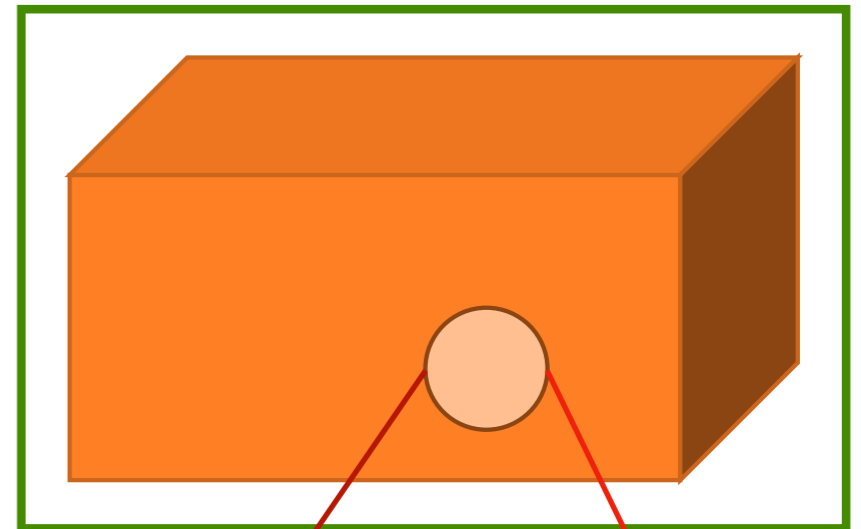


Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_{\mathcal{S}} \frac{1}{r} \vec{P}(\vec{r}') \cdot \hat{n} \, dA - \frac{1}{4\pi\epsilon_0} \int_{\mathcal{V}} \frac{1}{r} \vec{\nabla}' \cdot \vec{P} \, d\tau'$$

$$\sigma_b \equiv \vec{P} \cdot \hat{n}$$

$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$



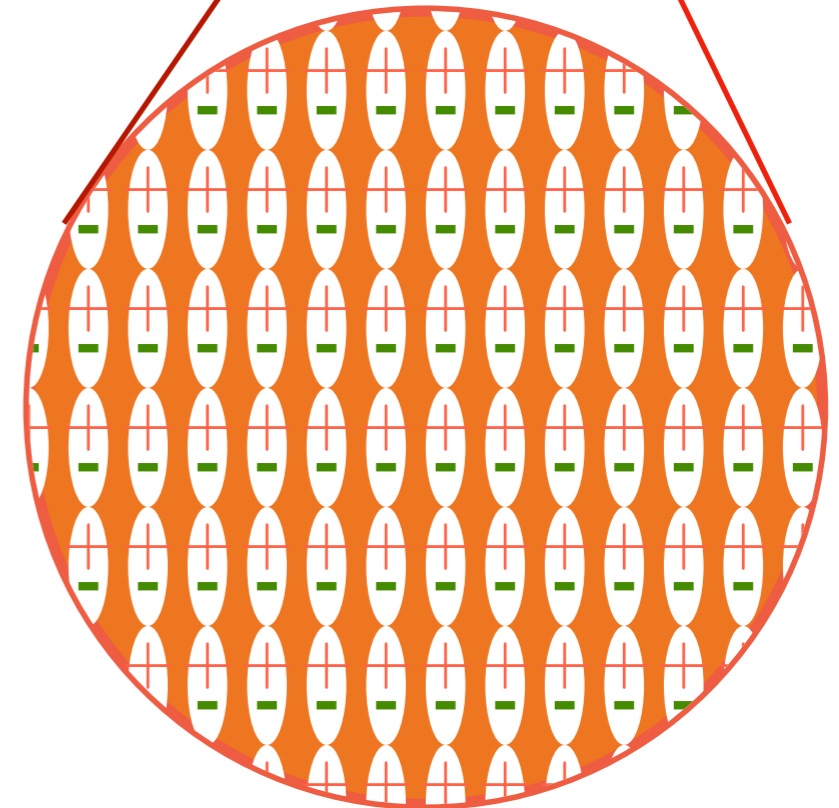
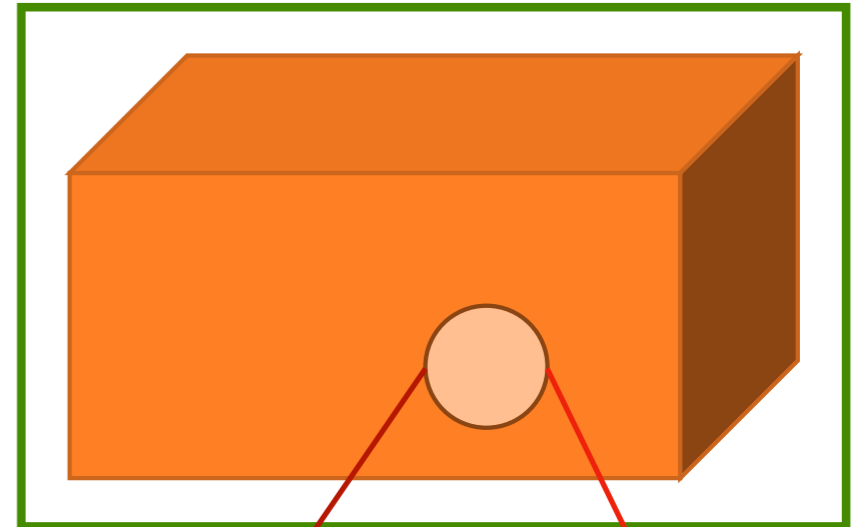
Polarização

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{1}{r} \vec{P}(\vec{r}') \cdot \hat{n} \, dA - \frac{1}{4\pi\epsilon_0} \int_V \frac{1}{r} \vec{\nabla}' \cdot \vec{P} \, d\tau'$$

$$\sigma_b \equiv \vec{P} \cdot \hat{n}$$

$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{\sigma_b}{r} \, dA' + \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho_b}{r} \, d\tau'$$

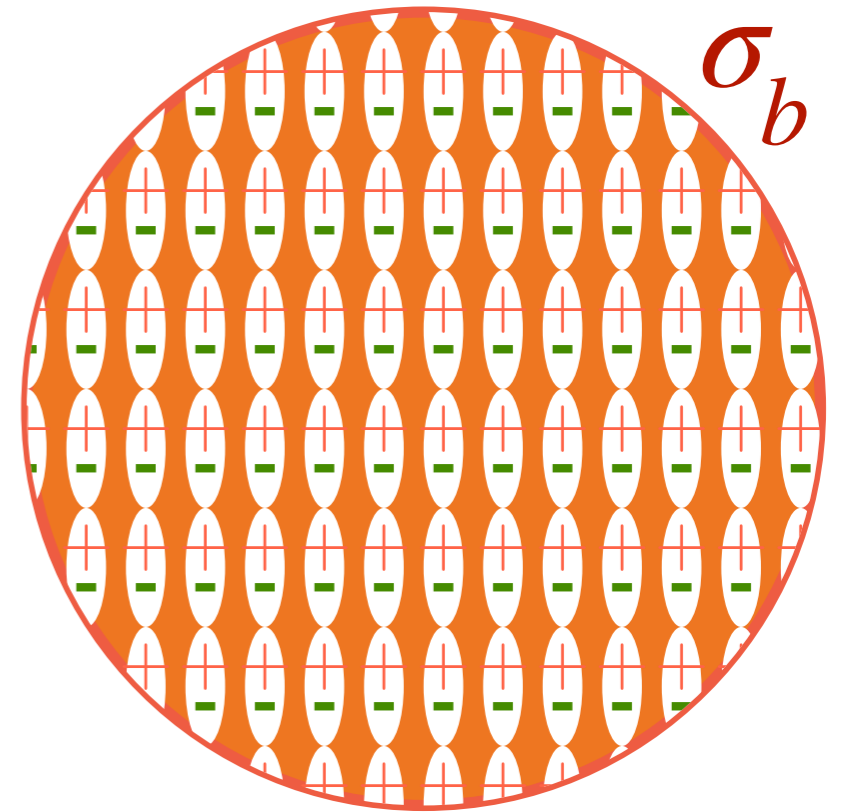


Polarização

Interpretação física

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{\sigma_b}{r} dA' + \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho_b}{r} d\tau'$$

$$\sigma_b \equiv \vec{P} \cdot \hat{n}$$

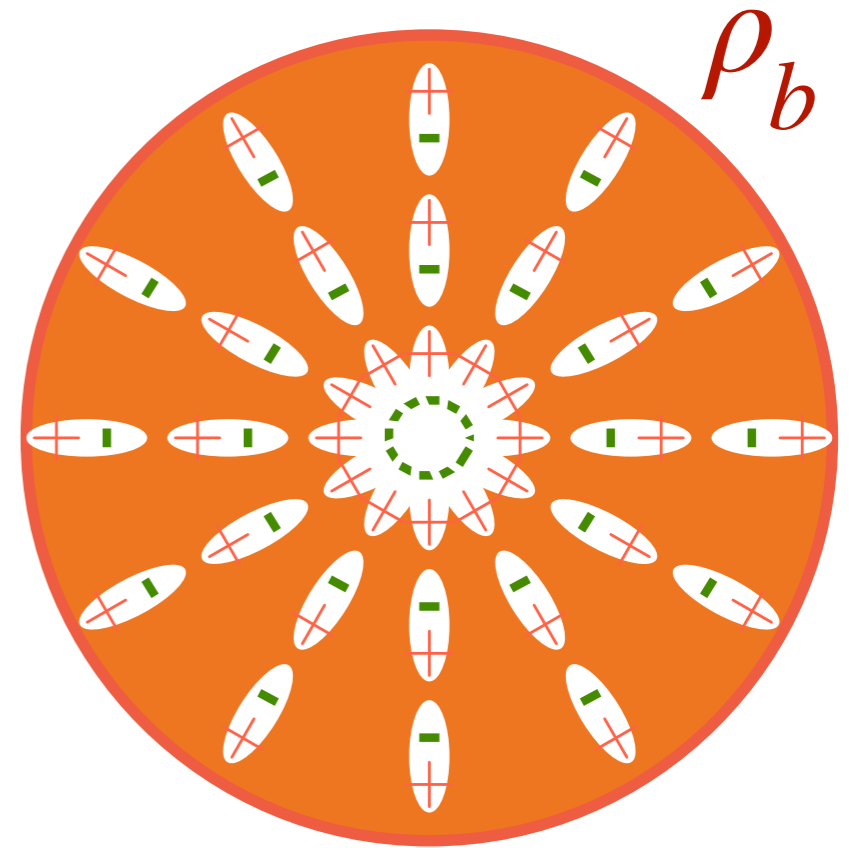


Polarização

Interpretação física

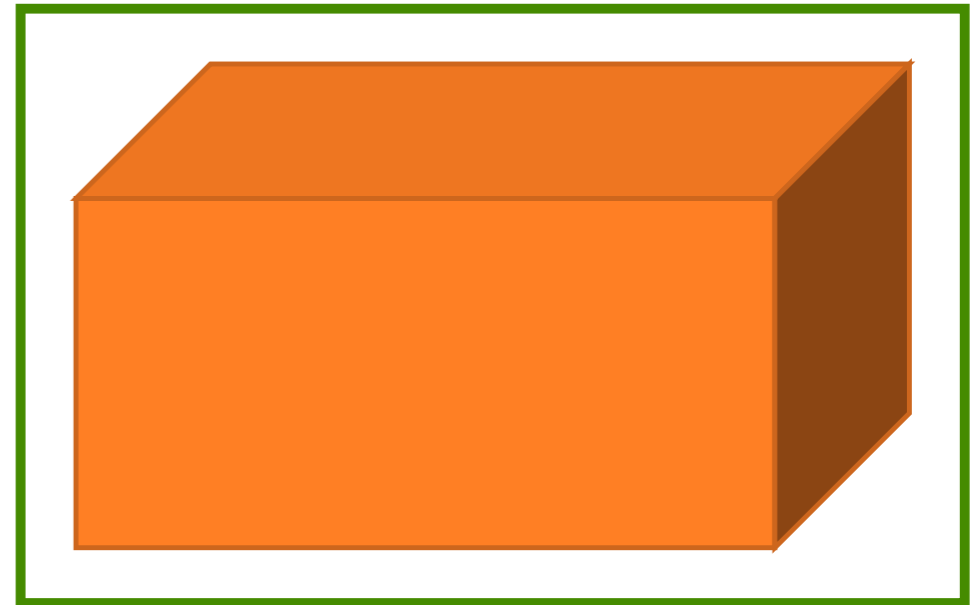
$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int_S \frac{\sigma_b}{r} dA' + \frac{1}{4\pi\epsilon_0} \int_V \frac{\rho_b}{r} d\tau'$$

$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$



Vetor deslocamento

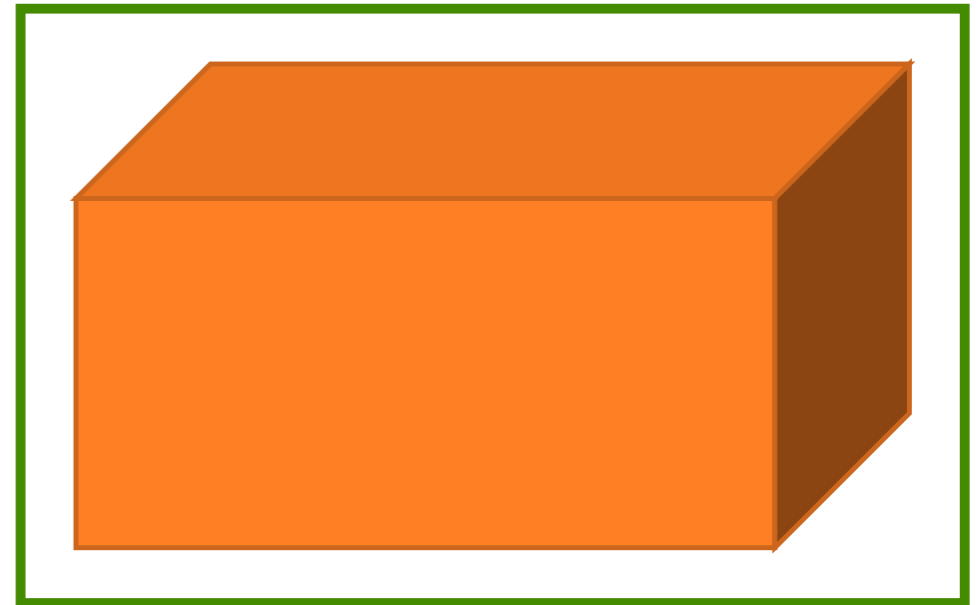
$$\rho = \rho_f + \rho_b$$



Vetor deslocamento

$$\rho = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f + \rho_b$$



Vetor deslocamento

$$\rho = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f + \rho_b$$



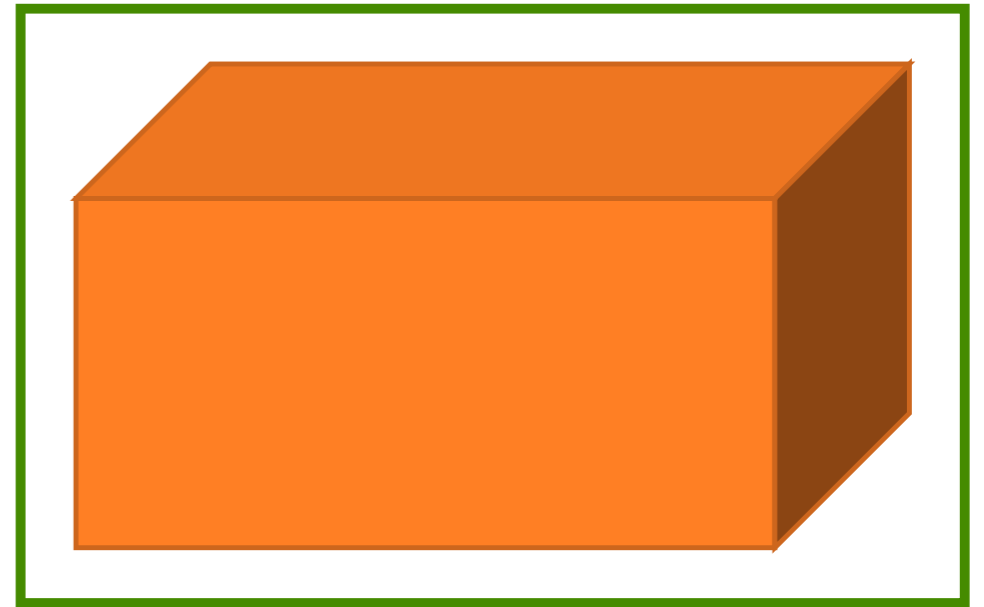
$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$

Vetor deslocamento

$$\rho = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f - \vec{\nabla} \cdot \vec{P}$$



$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$

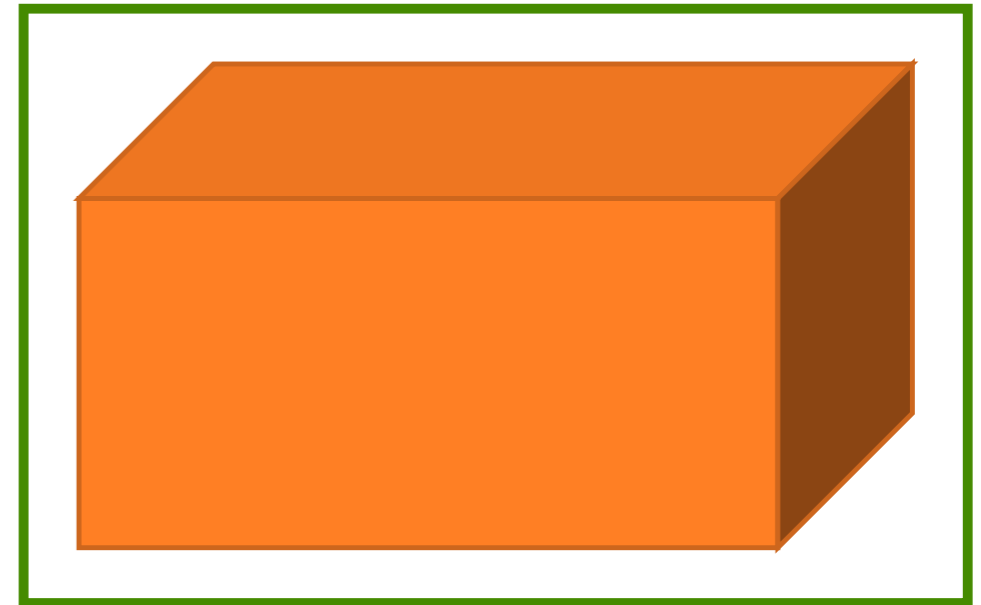
Vetor deslocamento

$$\rho = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f - \vec{\nabla} \cdot \vec{P}$$

$$\vec{\nabla} \cdot (\epsilon_0 \vec{E} + \vec{P}) = \rho_f$$



$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$

Vetor deslocamento

$$\rho = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f - \vec{\nabla} \cdot \vec{P}$$

$$\vec{\nabla} \cdot (\epsilon_0 \vec{E} + \vec{P}) = \rho_f$$

$$\vec{D} \equiv \epsilon_0 \vec{E} + \vec{P}$$

$$\vec{\nabla} \cdot \vec{D} = \rho_f$$



$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$

Vetor deslocamento

$$\rho = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f + \rho_b$$

$$\epsilon_0 \vec{\nabla} \cdot \vec{E} = \rho_f - \vec{\nabla} \cdot \vec{P}$$

$$\vec{\nabla} \cdot (\epsilon_0 \vec{E} + \vec{P}) = \rho_f$$

$$\vec{D} \equiv \epsilon_0 \vec{E} + \vec{P}$$

$$\vec{\nabla} \cdot \vec{D} = \rho_f$$

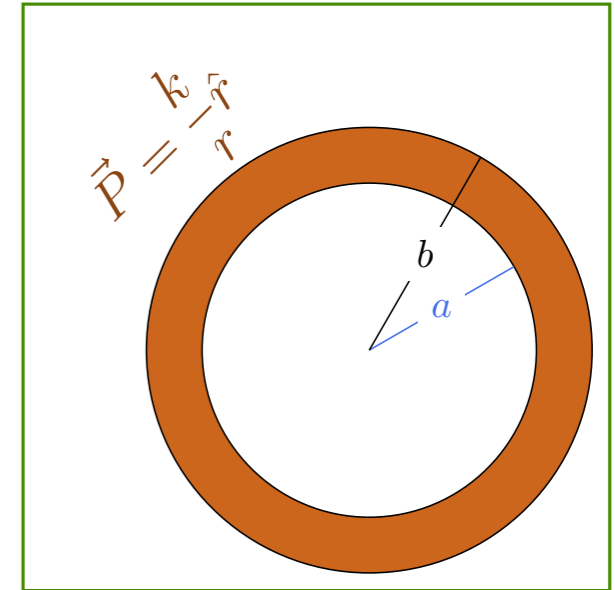
$$\int_A \vec{D} \cdot \hat{n} \, dA = Q_f$$



$$\rho_b \equiv -\vec{\nabla} \cdot \vec{P}$$

Pratique o que aprendeu

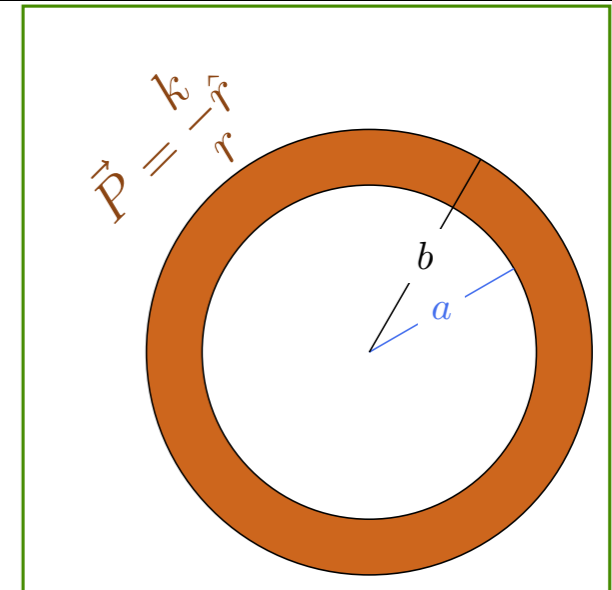
$$\vec{E} = ?$$



Pratique o que aprendeu

$$\vec{E} = ?$$

$$\vec{D} = 0$$

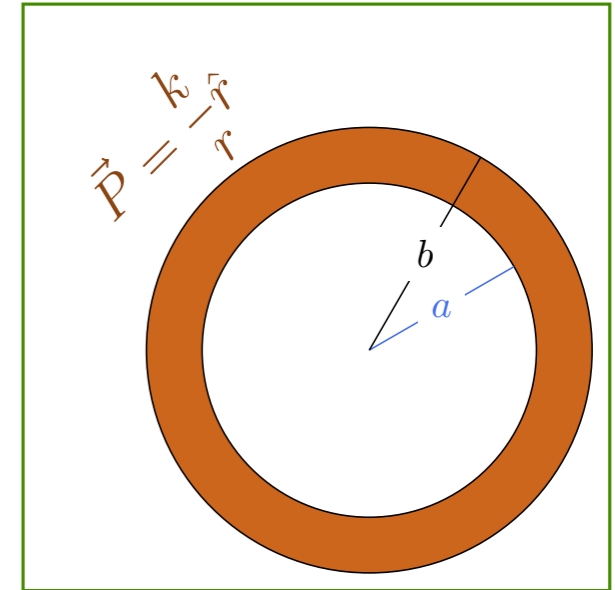


Pratique o que aprendeu

$$\vec{E} = ?$$

$$\vec{D} = 0$$

$$\Rightarrow \epsilon_0 \vec{E} + \vec{P} = 0$$



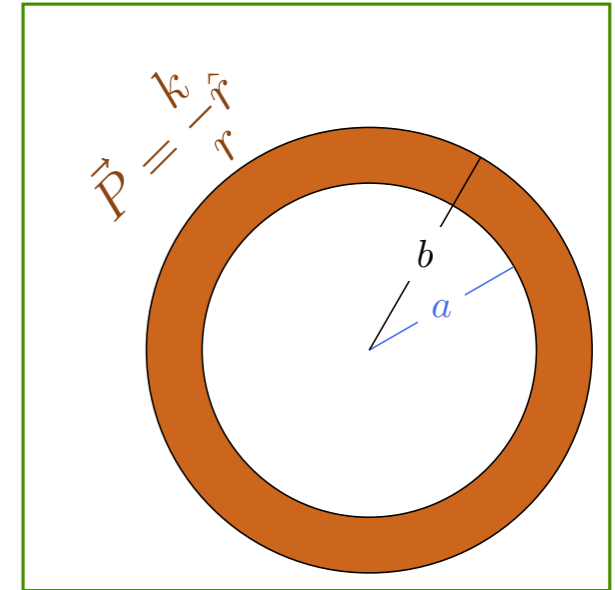
Pratique o que aprendeu

$$\vec{E} = ?$$

$$\vec{D} = 0$$

$$\Rightarrow \epsilon_0 \vec{E} + \vec{P} = 0$$

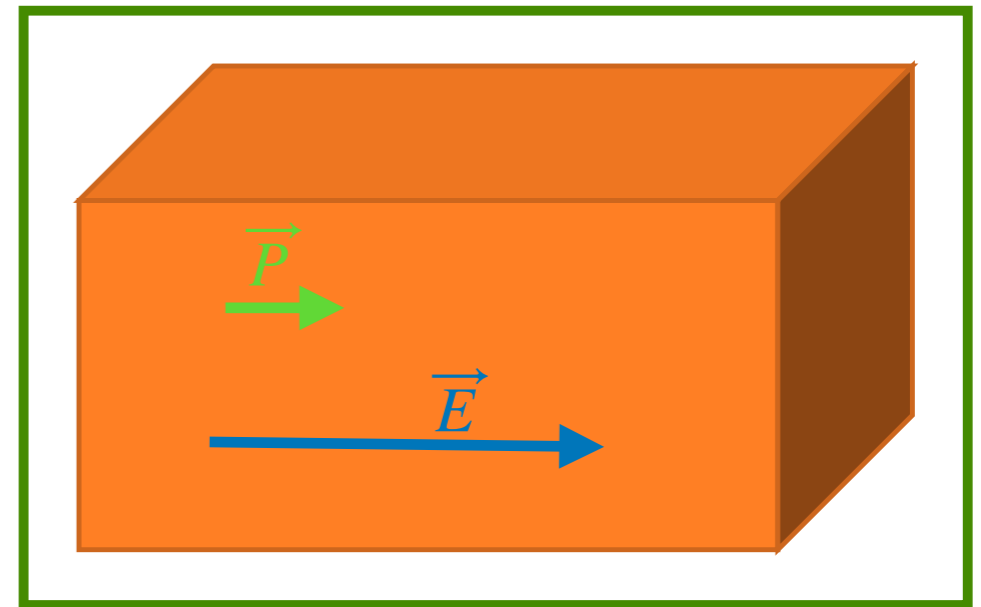
$$\Rightarrow \begin{cases} \vec{E} = 0 & (r < a \text{ e } r > b) \\ \vec{E} = -\frac{k}{\epsilon_0 r} \hat{r} & (a < r < b) \end{cases}$$



Meios lineares

$$\vec{P} = \chi_e \epsilon_0 \vec{E}$$

Susceptibilidade

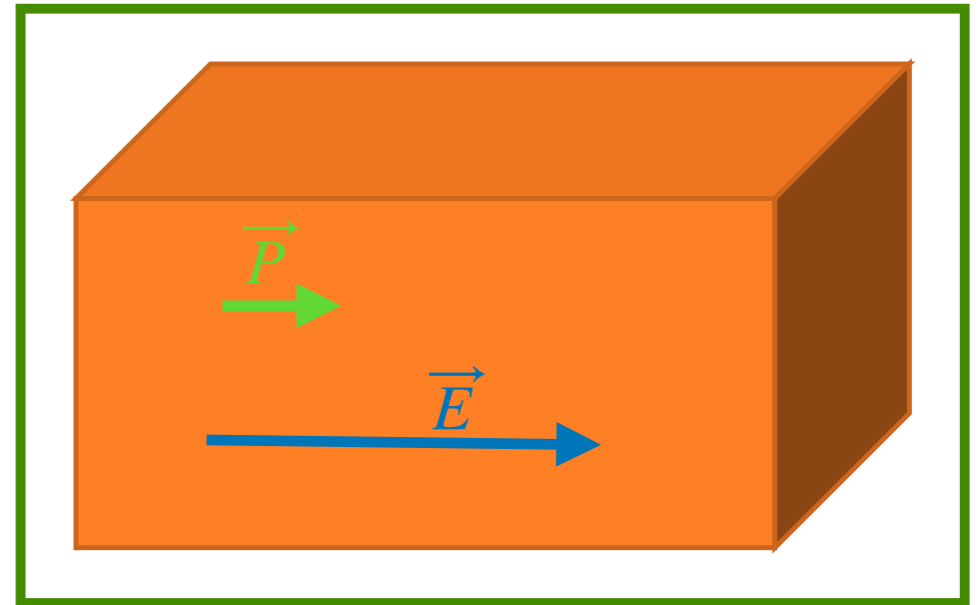


Meios lineares

$$\vec{P} = \chi_e \epsilon_0 \vec{E}$$

Susceptibilidade

$$\vec{D} = \epsilon_0 \vec{E} + \chi_e \epsilon_0 \vec{E}$$



Meios lineares

$$\vec{P} = \chi_e \epsilon_0 \vec{E}$$

Susceptibilidade

$$\vec{D} = \epsilon_0 \vec{E} + \chi_e \epsilon_0 \vec{E}$$

$$\vec{D} = (1 + \chi_0) \epsilon_0 \vec{E}$$

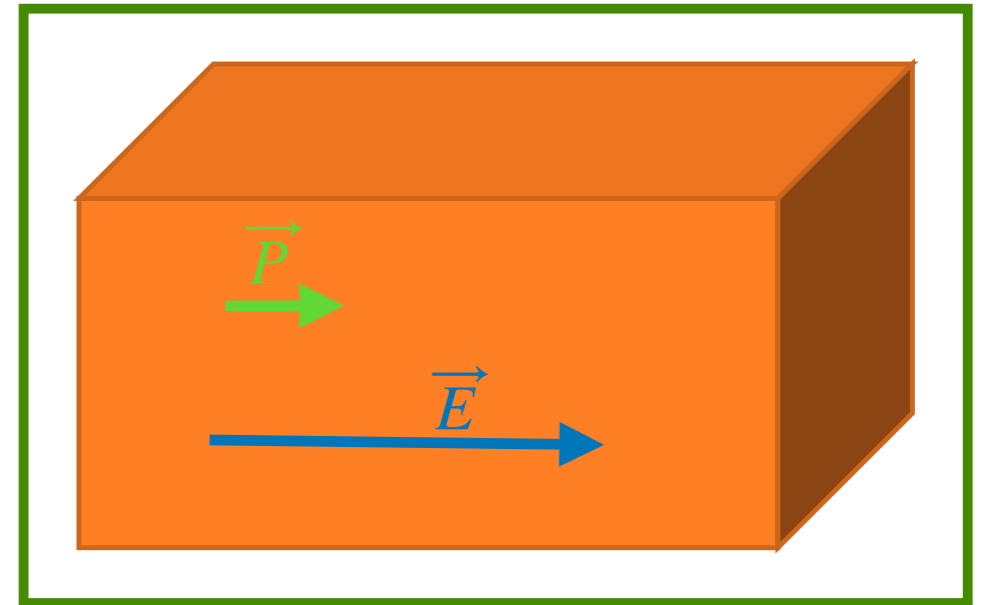
$$\epsilon = (1 + \chi_0) \epsilon_0$$

Permissividade

$$\epsilon_r = 1 + \chi_0$$

Constante dielétrica

$$\vec{D} = \epsilon \vec{E} = \epsilon_r \epsilon_0 \vec{E}$$



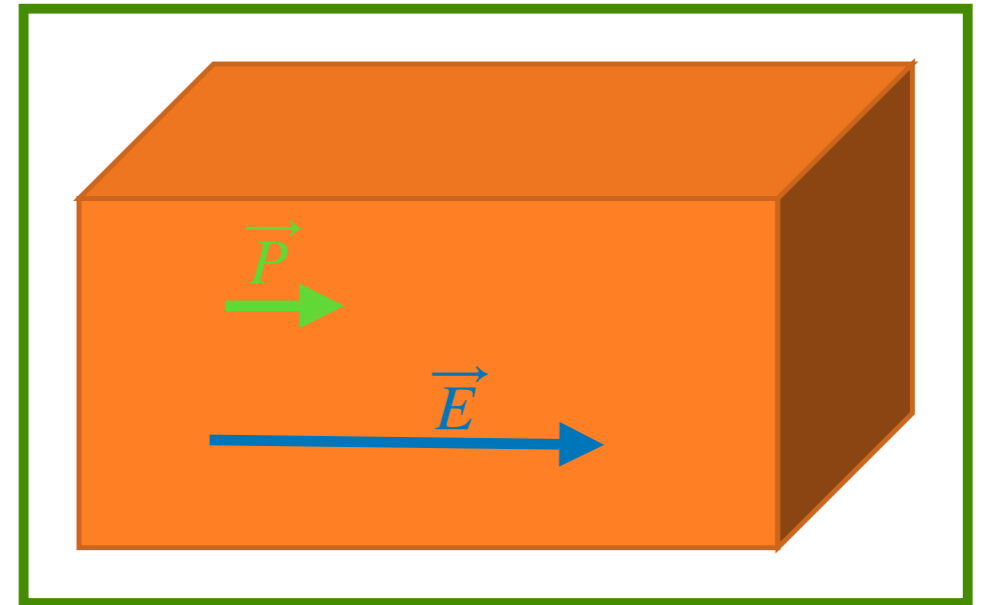
Meios lineares

$$\vec{P} = \chi_e \epsilon_0 \vec{E}$$

Susceptibilidade

$$\vec{D} = \epsilon \vec{E} = \epsilon_r \epsilon_0 \vec{E}$$

$$\epsilon_r = 1 + \chi_0$$



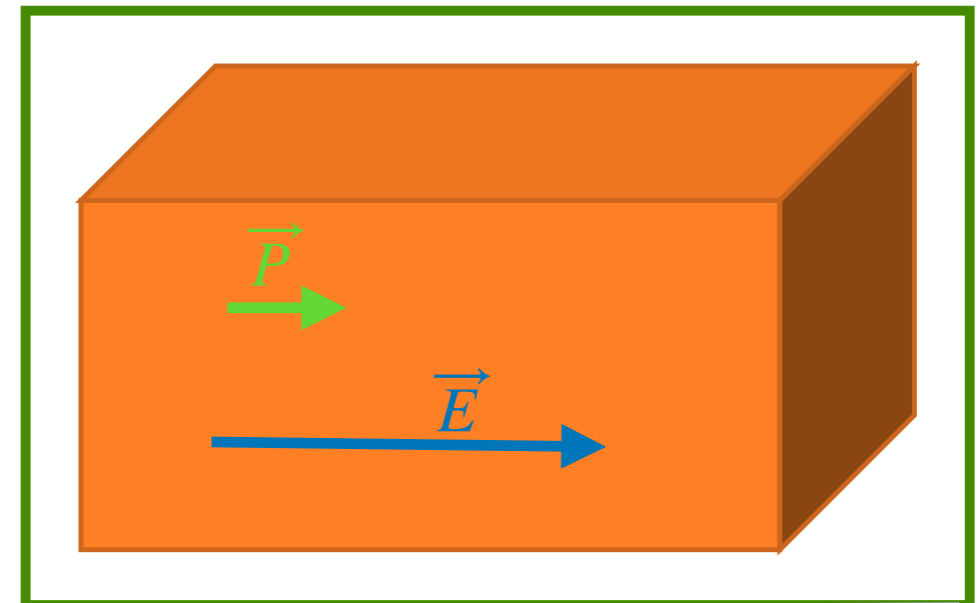
Meios lineares

$$\vec{P} = \chi_e \epsilon_0 \vec{E}$$

Susceptibilidade

$$\vec{D} = \epsilon \vec{E} = \epsilon_r \epsilon_0 \vec{E}$$

$$\epsilon_r = 1 + \chi_0$$



Material	Dielectric Constant	Material	Dielectric Constant
Vacuum	1	Benzene	2.28
Helium	1.000065	Diamond	5.7
Neon	1.00013	Salt	5.9
Hydrogen	1.00025	Silicon	11.8
Argon	1.00052	Methanol	33.0
Air (dry)	1.00054	Water	80.1
Nitrogen	1.00055	Ice (-30° C)	99
Water vapor (100° C)	1.00587	KTaNbO ₃ (0° C)	34,000

Pratique o que aprendeu

$$\vec{E} = ?$$

