

# Física IV

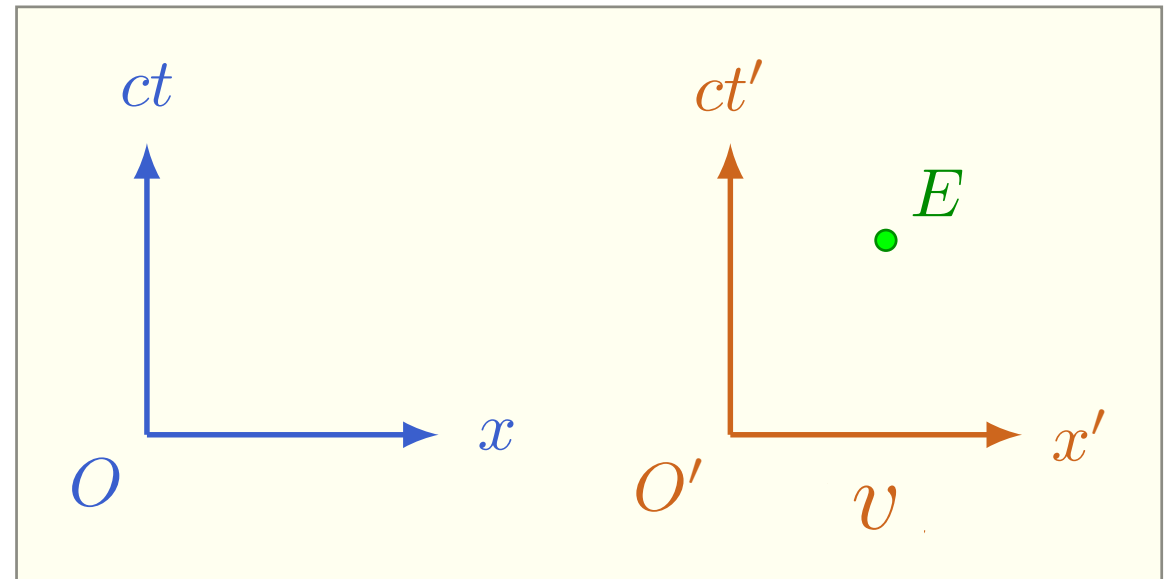
8 dezembro

Relatividade restrita

# Relatividade restrita

## Transformação de Lorentz

$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$



$$\gamma \equiv \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

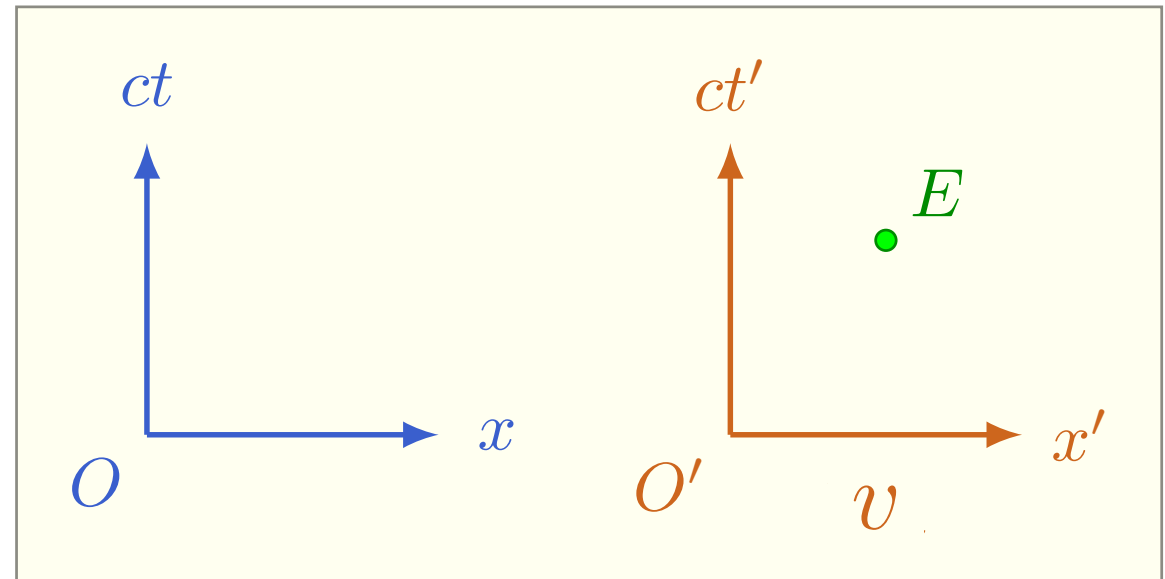
$$\beta \equiv \frac{v}{c}$$

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$$\tanh(a) \equiv \beta$$



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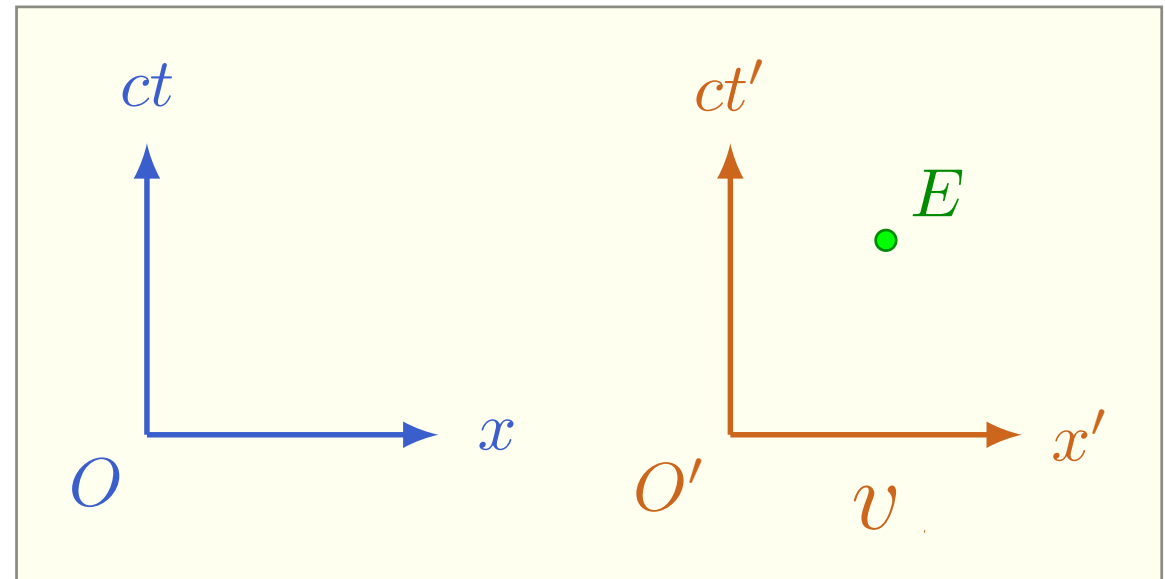
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$$\tanh(a) \equiv \beta$$



$$\cosh(a) = \frac{1}{\sqrt{1 - \tanh^2(a)}}$$

$$\gamma \equiv \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

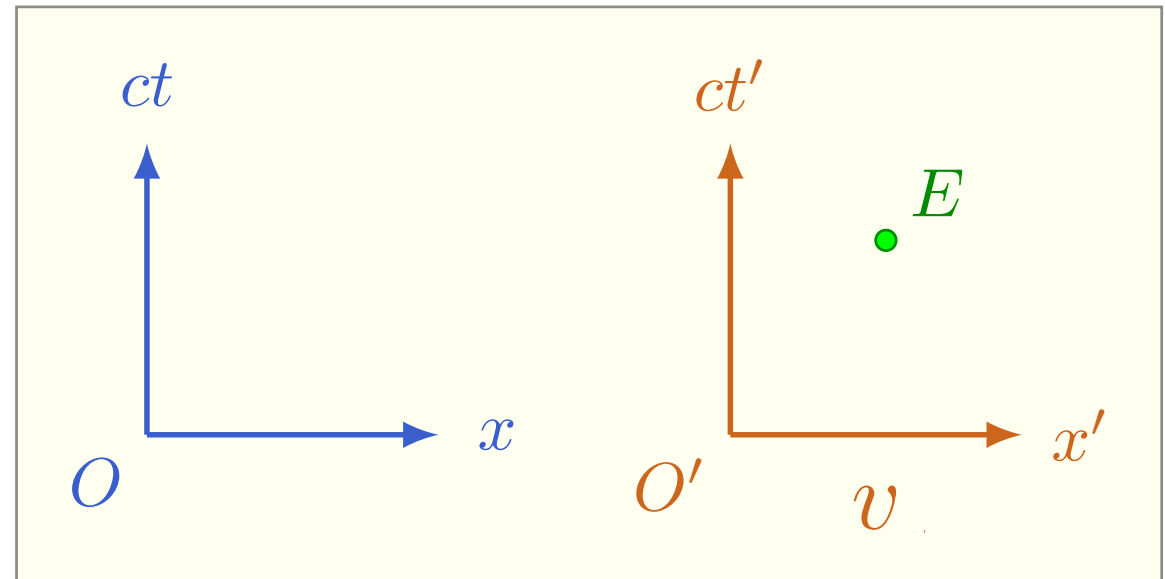
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$$\tanh(a) \equiv \beta$$



$$\cosh(a) = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \gamma$$

$$\gamma \equiv \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$\beta \equiv \frac{v}{c}$$

# Relatividade restrita

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$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

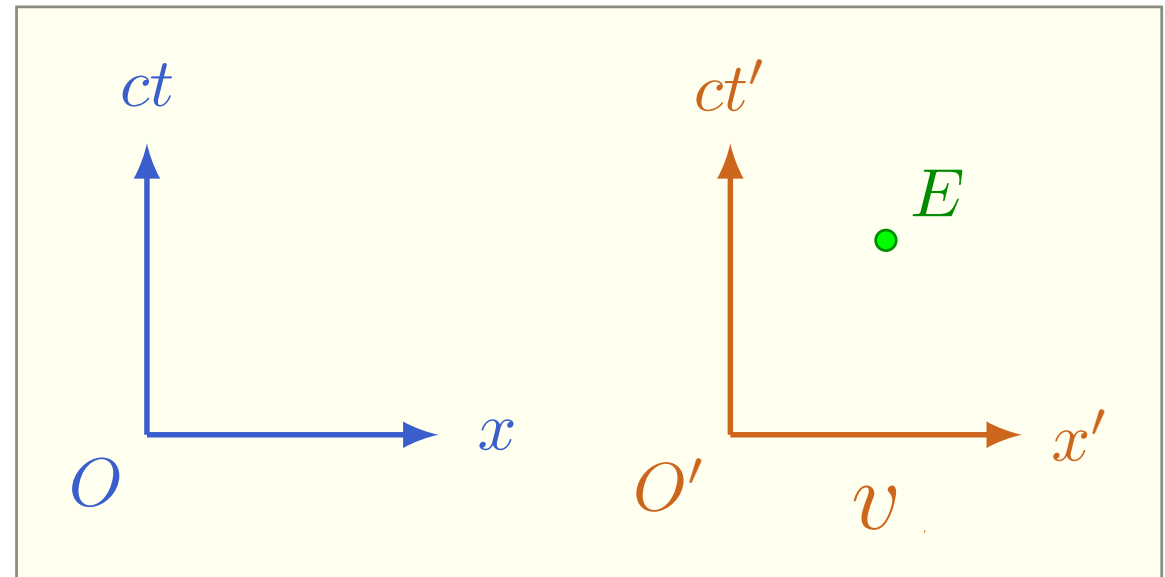
$$\tanh(a) \equiv \beta$$

$$\cosh(a) = \gamma$$

$$\sinh(a) = \beta\gamma$$

$$\gamma \equiv \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$\beta \equiv \frac{v}{c}$$

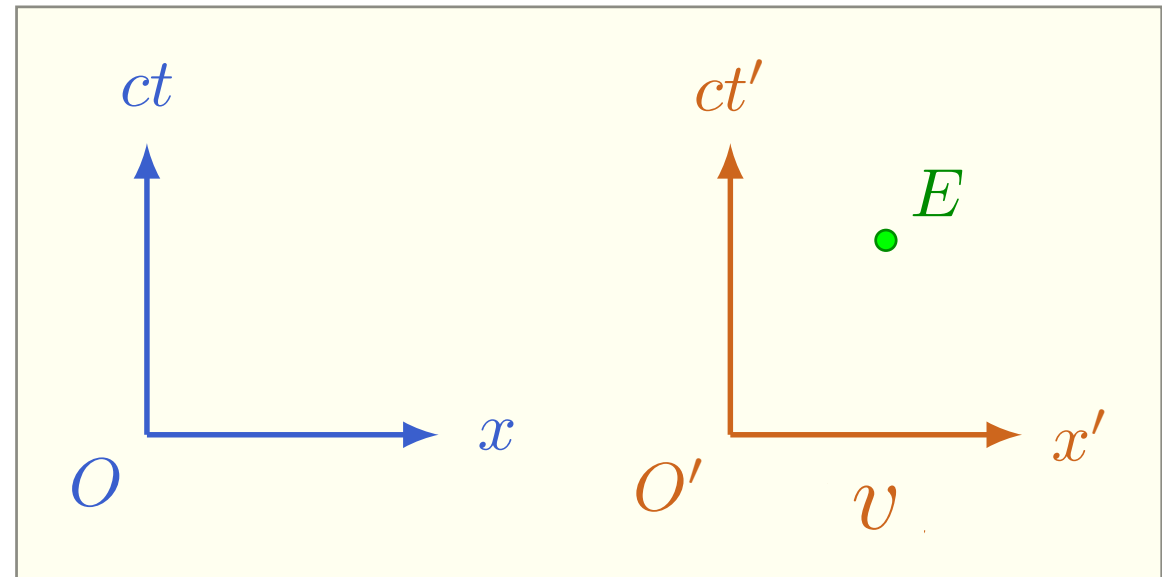


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## Transformação de Lorentz

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$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

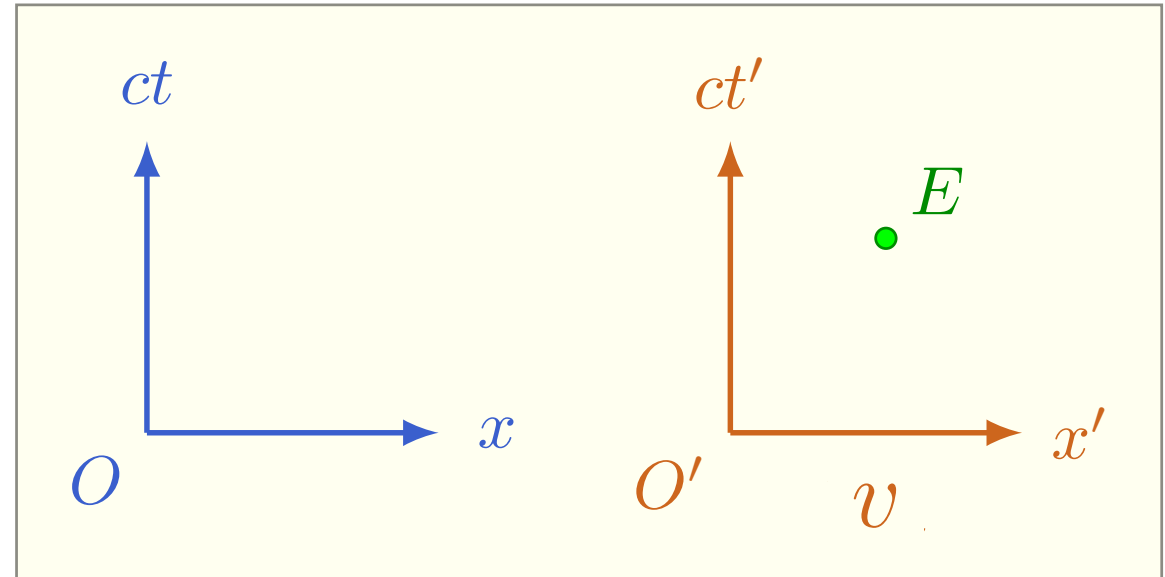
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## Transformação de Lorentz

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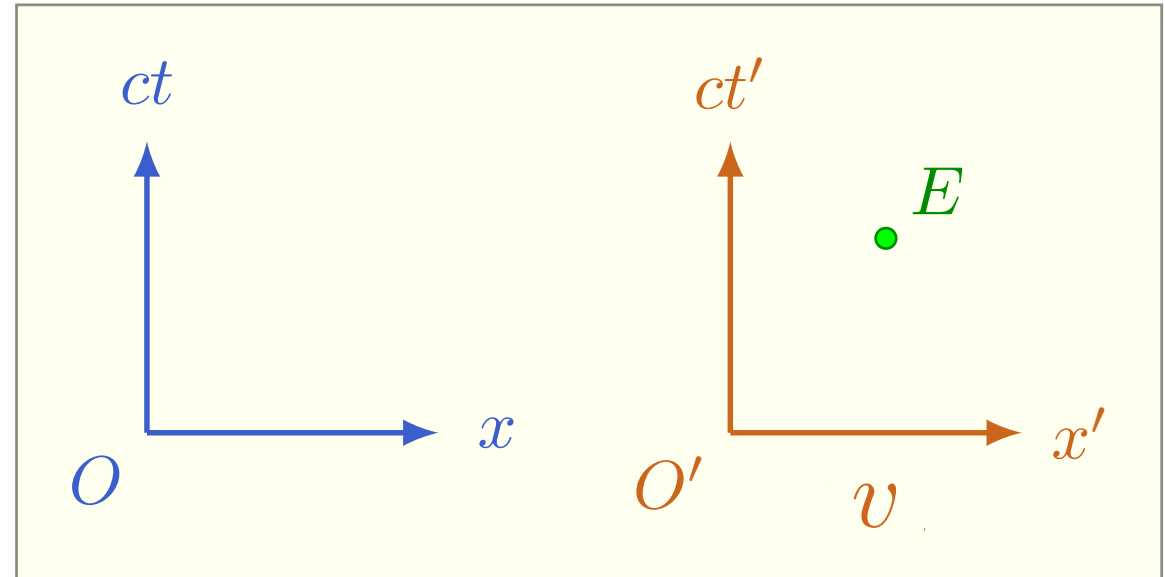
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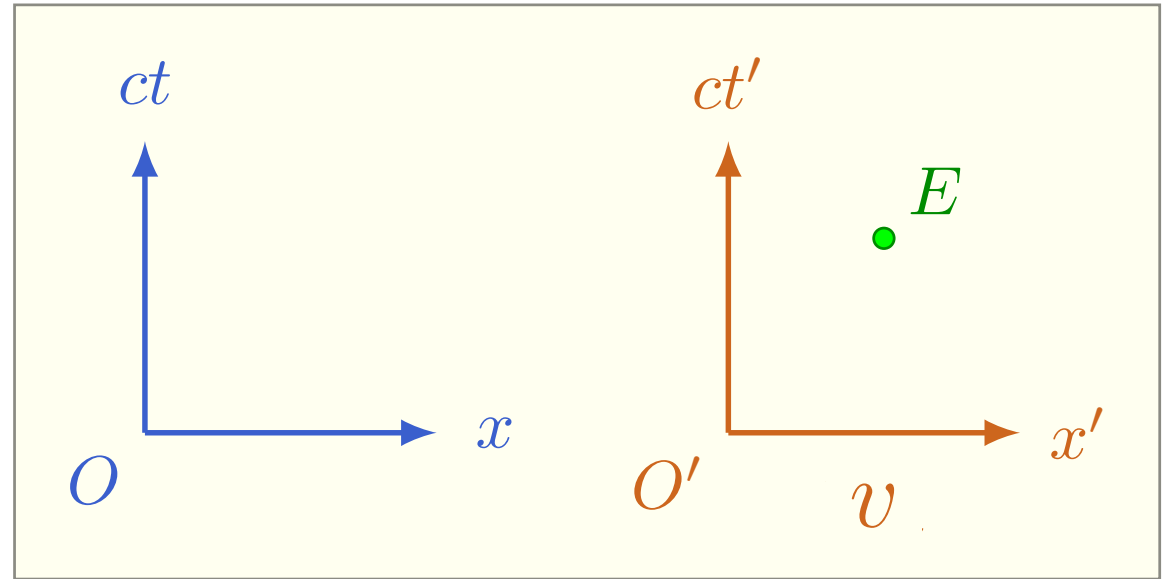
$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$



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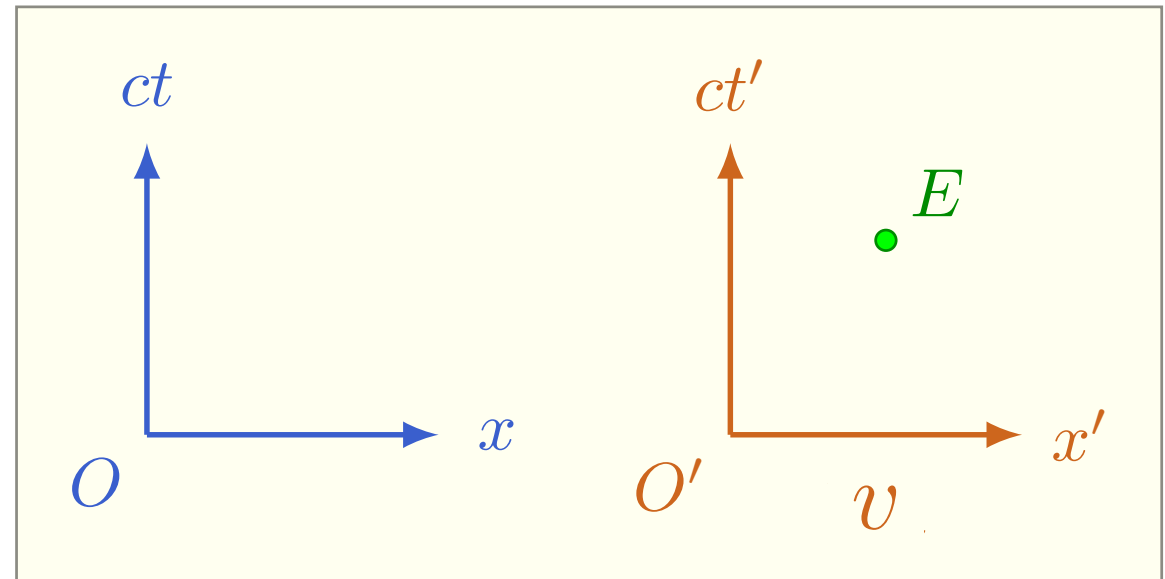
$$\begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix}^{-1} \begin{bmatrix} ct' \\ x' \end{bmatrix} = \begin{bmatrix} ct \\ x \end{bmatrix}$$



# Transformação de Lorentz

$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

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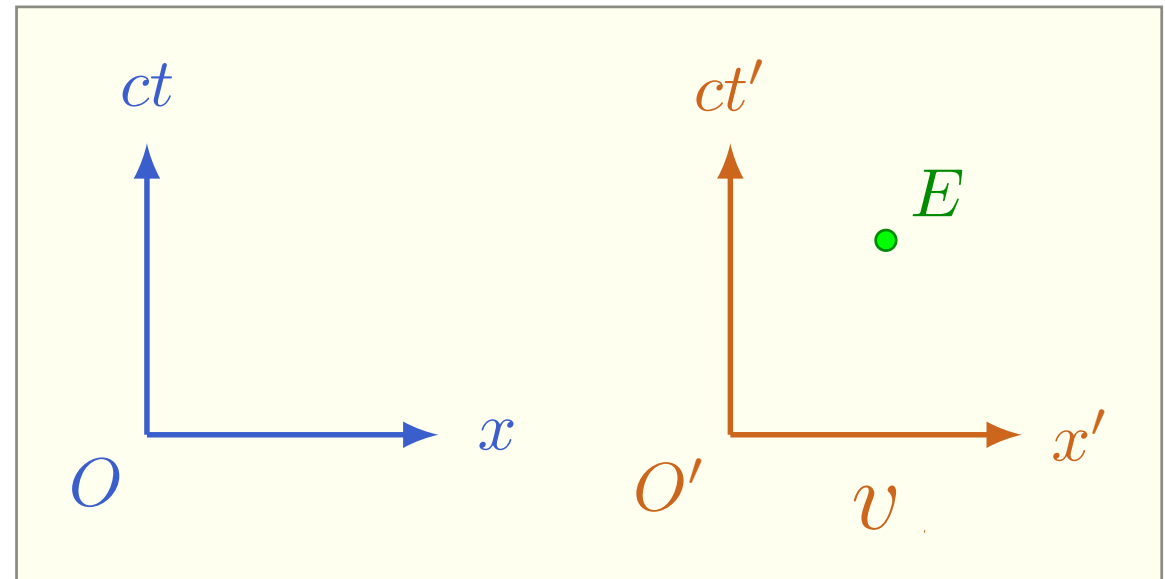


$$\det \begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix} = 1$$

# Transformação de Lorentz

$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

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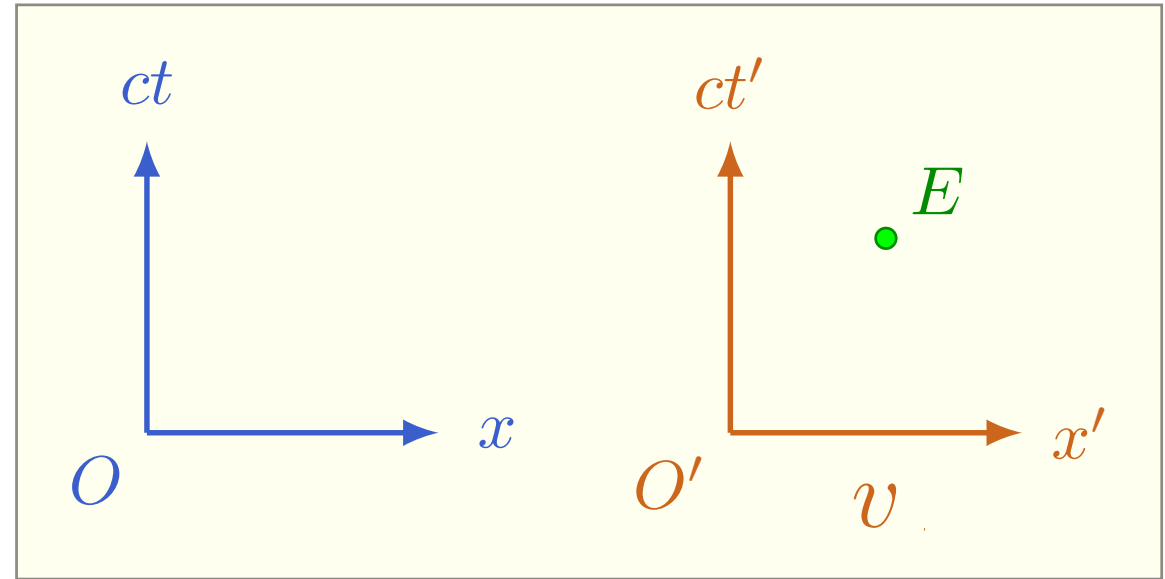
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# Transformação de Lorentz

$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \begin{bmatrix} \cosh(a) & -\sinh(a) \\ -\sinh(a) & \cosh(a) \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} ct \\ x \end{bmatrix} = \begin{bmatrix} \cosh(a) & \sinh(a) \\ \sinh(a) & \cosh(a) \end{bmatrix} \begin{bmatrix} ct' \\ x' \end{bmatrix}$$

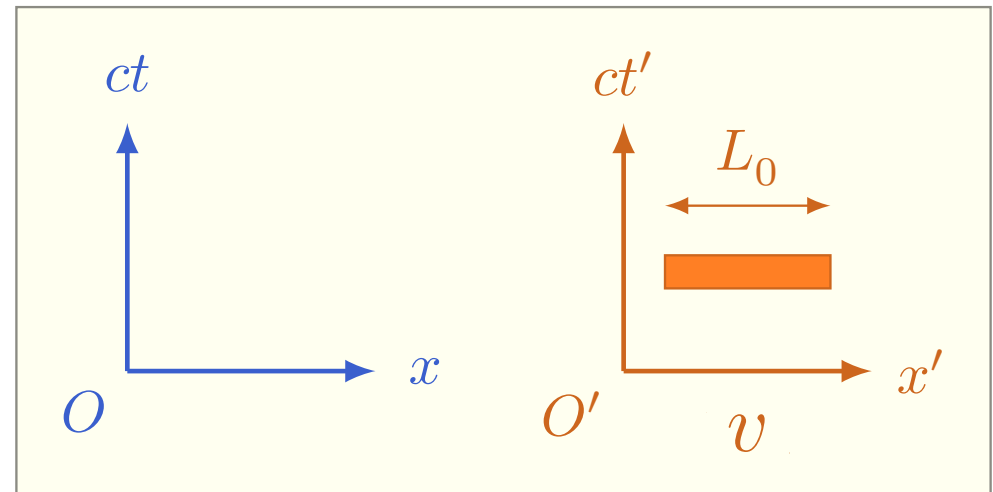


$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

$$\begin{bmatrix} c\Delta t' \\ L_0 \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} 0 \\ L \end{bmatrix}$$

$$L = \frac{L_0}{\gamma} < L_0$$



$$\gamma \equiv \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$\beta \equiv \frac{v}{c}$$

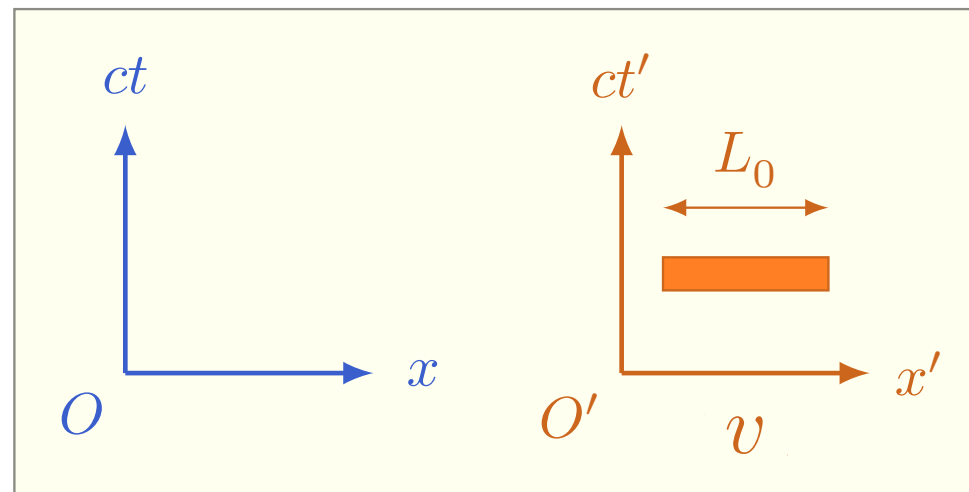
$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

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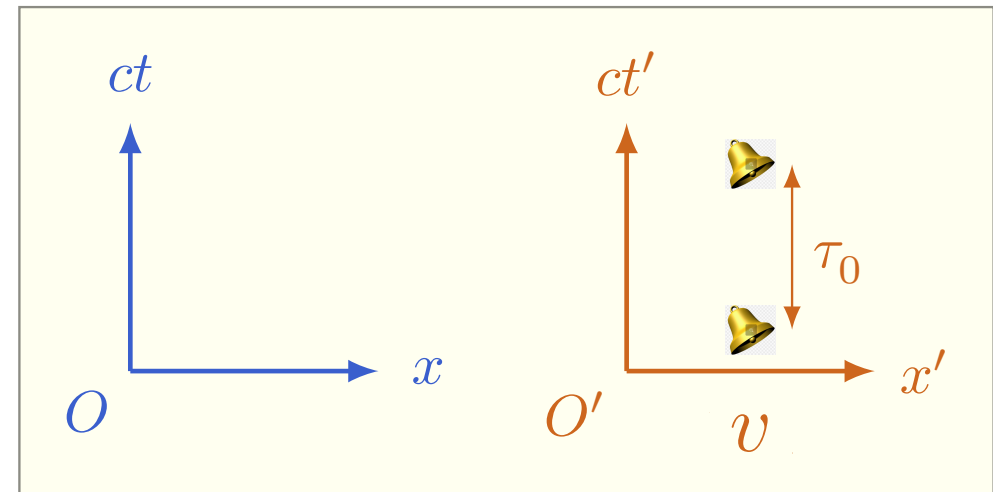
Contração espacial



$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

$$\tau = ?$$



$$\gamma \equiv \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

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$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

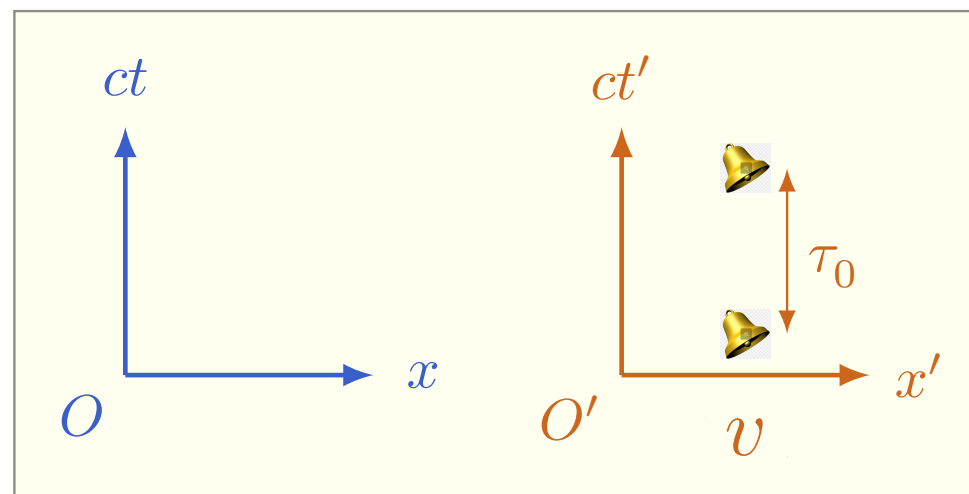
## Eventos

$$x'_i = x_0$$

$$t'_i = 0$$

$$x'_f = x_0$$

$$t'_f = \tau_0$$



$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

## Eventos

$$x'_i = x_0$$

$$t'_i = 0$$

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$$t'_f = \tau_0$$

$$x_i = ?$$

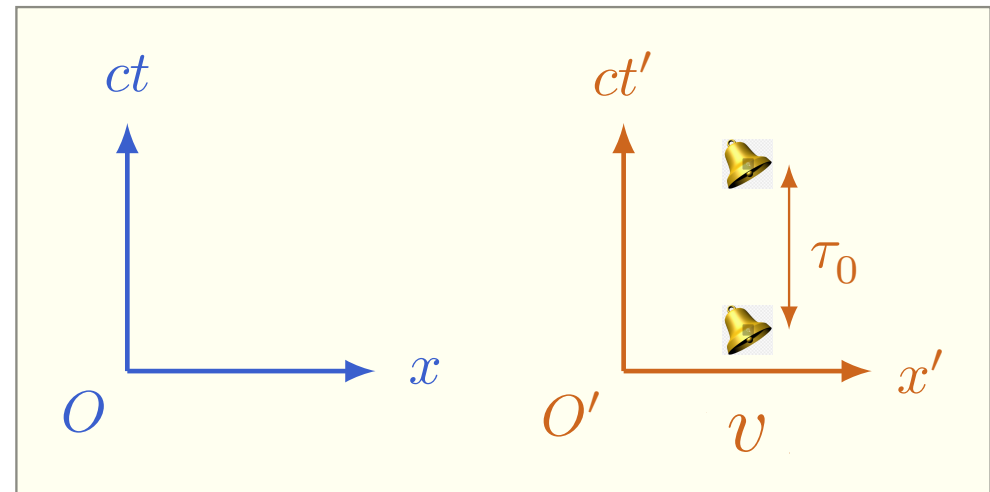
$$t_i = ?$$

$$x_f = ?$$

$$t_f = ?$$

$$\begin{bmatrix} c\Delta t' \\ \Delta x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} c\Delta t \\ \Delta x \end{bmatrix}$$

$$\begin{bmatrix} c\tau_0 \\ 0 \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} c\tau \\ \Delta x \end{bmatrix}$$



$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

## Eventos

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$$x'_f = x_0$$

$$t'_f = \tau_0$$

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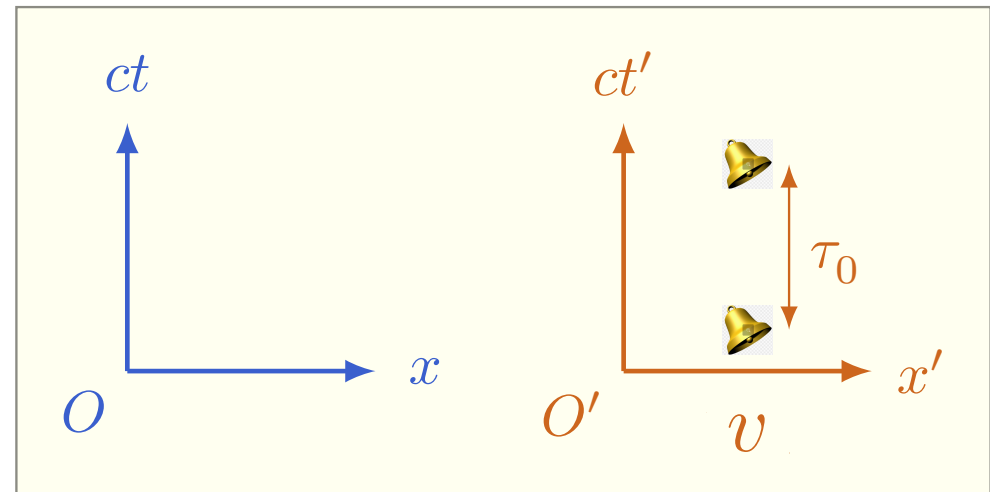
$$t_i = ?$$

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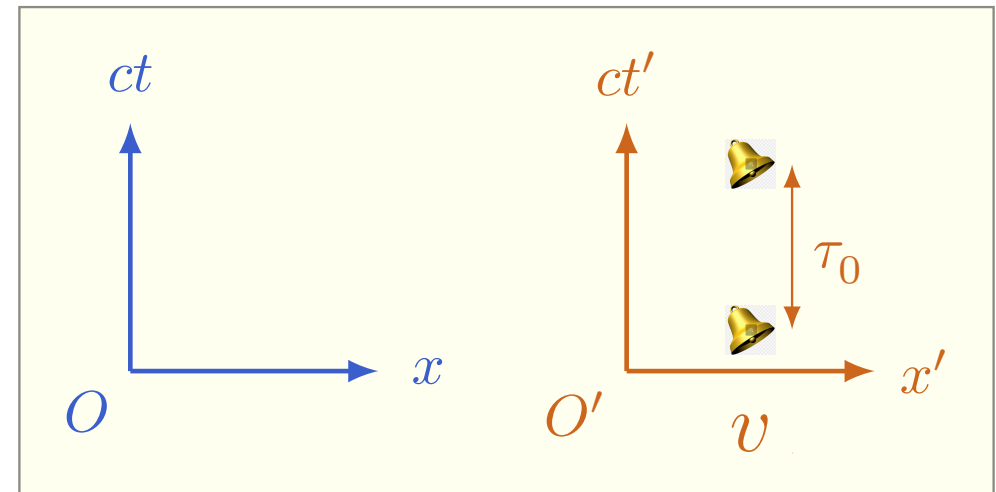
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Pratique o que aprendeu

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$$\begin{bmatrix} c\tau \\ \Delta x \end{bmatrix} = \gamma \begin{bmatrix} 1 & \beta \\ \beta & 1 \end{bmatrix} \begin{bmatrix} c\tau_0 \\ 0 \end{bmatrix}$$

$$\Rightarrow c\tau = \gamma c\tau_0$$

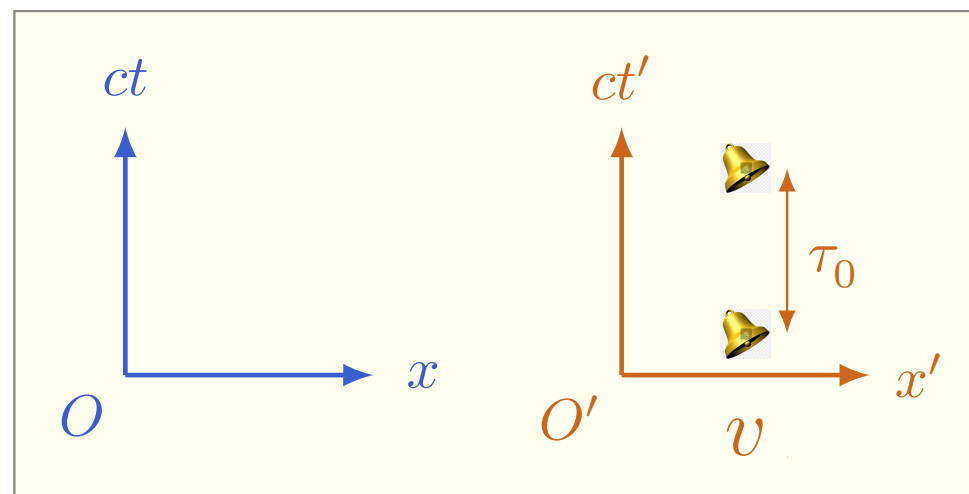


$$\begin{bmatrix} ct' \\ x' \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} ct \\ x \end{bmatrix}$$

Pratique o que aprendeu

$$\begin{bmatrix} c\tau_0 \\ 0 \end{bmatrix} = \gamma \begin{bmatrix} 1 & -\beta \\ -\beta & 1 \end{bmatrix} \begin{bmatrix} c\tau \\ \Delta x \end{bmatrix}$$



$$\begin{bmatrix} c\tau \\ \Delta x \end{bmatrix} = \gamma \begin{bmatrix} 1 & \beta \\ \beta & 1 \end{bmatrix} \begin{bmatrix} c\tau_0 \\ 0 \end{bmatrix}$$



$$\tau = \gamma\tau_0$$

Dilatação temporal

# Trabalhos criativos

✚  Grupo 1: Holografia 

✚  Grupo 3: Dispersão no índice de refração 

✚  Grupo 4: Ótica da visão 

✚  Grupo 8: Polimerização via absorção de dois fótons 

✚  Grupo 15: Espectro de ionização de gases e sólidos (texto) 

✚  Grupo 15: Espectro de ionização de gases e sólidos (vídeo) 

✚  Grupo 16: Retificador de onda completo 

✚  Grupo 18: Fibras óticas 