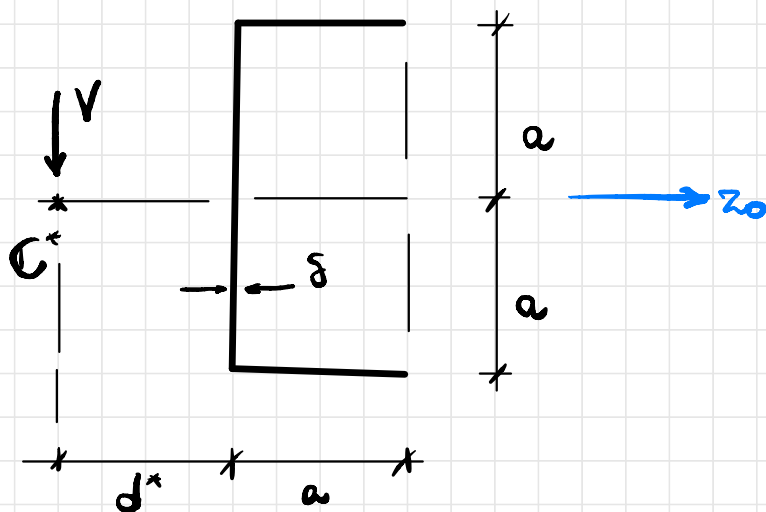


A seção delgada da figura tem espessura $\delta \ll a$.
 Achar a distribuição das tensões de cisalhamento para
 uma força cortante V , aplicada em C^* :

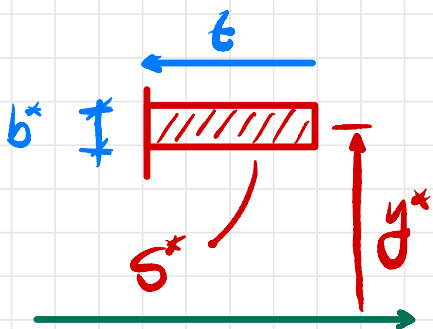


Propriedades da seção:

$$I_{z_0} = \frac{\delta (2a)^3}{12} + 2 \left(\cancel{\frac{a\delta^3}{12}} + a^2 \cdot \delta a \right)$$

$$I_{z_0} = \frac{8}{3} \delta a^3$$

Tensão nas flanges:



$$y^* = a$$

$$S^* = \delta t$$

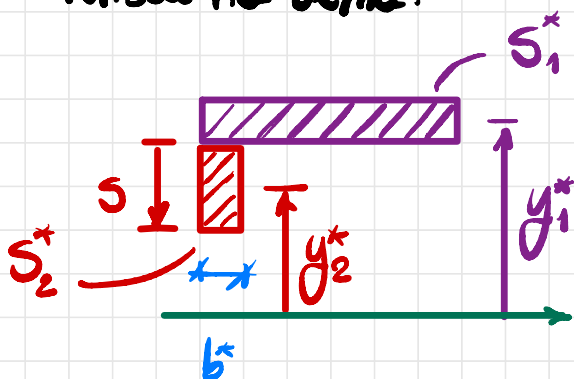
$$b^* = \delta$$

$$M_s^* = S^* y^* = \delta a t$$

$$\tau = \frac{V \cdot M_s^*}{b^* \cdot I_{z0}} = \frac{V \cdot \cancel{\delta} a t}{\cancel{\delta} \cdot \frac{3}{8} \delta a^3} \rightarrow \tau = \frac{3}{8} \frac{V t}{\delta a^2}$$

$$\tau(0) = 0 ; \tau(a) = \frac{3}{8} V / \delta a$$

Tensão na alma:



$$b^* = \delta$$

$$S_1^* = \delta a$$

$$y_1^* = a$$

$$S_2^* = \delta s$$

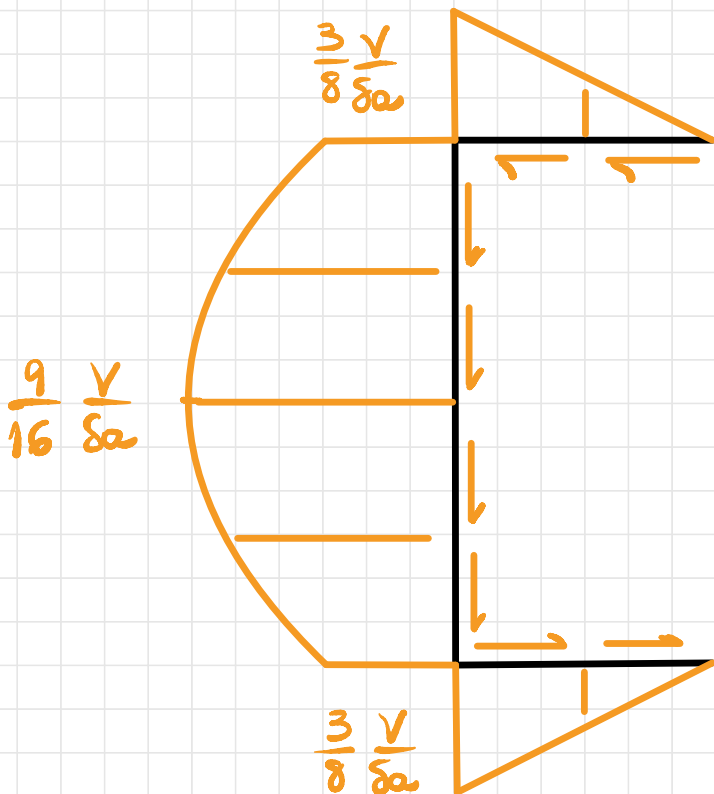
$$y_2^* = a - \frac{s}{2} = \frac{2a - s}{2}$$

$$M_s^* = \frac{\delta}{2} (2a^2 + 2as - s^2)$$

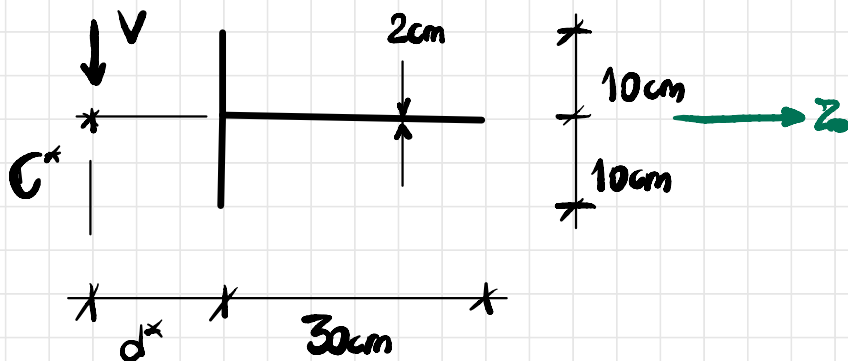
$$\tau = \frac{VM_s^*}{b^* I_{20}} = V \cdot \frac{\cancel{8}}{2} (2a^2 + 2as - s^2) \cdot \frac{\cancel{1}}{\cancel{8}} \cdot \frac{3}{8\delta a^3}$$

$$\tau = \frac{3}{16} \frac{V}{\delta a^3} (2a^2 + 2as - s^2)$$

$$\tau(0) = \frac{3}{8} \frac{V}{\delta a} ; \tau(a) = \frac{9}{16} \frac{V}{\delta a} ; \tau(a) = \frac{3}{8} \frac{V}{\delta a}$$



Seja $V = 79.200 \text{ kgf}$, achar a distribuição das
tensões tangenciais, supondo V aplicada em C^* :

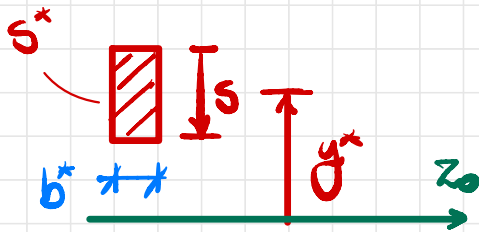


Propriedades da seção:

$$I_{z0} = \frac{30 \cdot 2^3}{12} + 2 \left(\frac{2 \cdot 10^3}{12} + 5^2 \cdot 20 \right)$$

$$I_z = \frac{4000}{3} \text{ cm}^4$$

Tensões nas almas:



$$b^* = 2$$

$$s^* = 2s$$

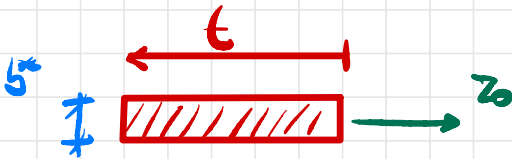
$$y^* = 10 - s/2$$

$$M_s^* = 20s - s^2$$

$$\tau = \frac{V \cdot M_s^*}{b^* \cdot I_{z_0}} = \frac{79200 \cdot (20s - s^2)}{2 \cdot 4000/3} = 29,7 (20s - s^2)$$

$$\tau(0) = 0 ; \tau(10) = 2970 \text{ kgf/cm}^2 ; \tau(20) = 0$$

Tensões na flange:



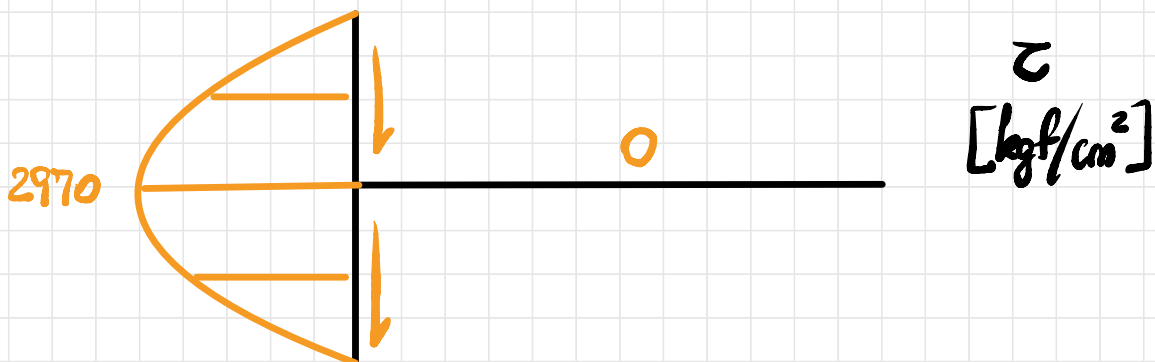
$$y^* = 0$$

$$s^* = 2t$$

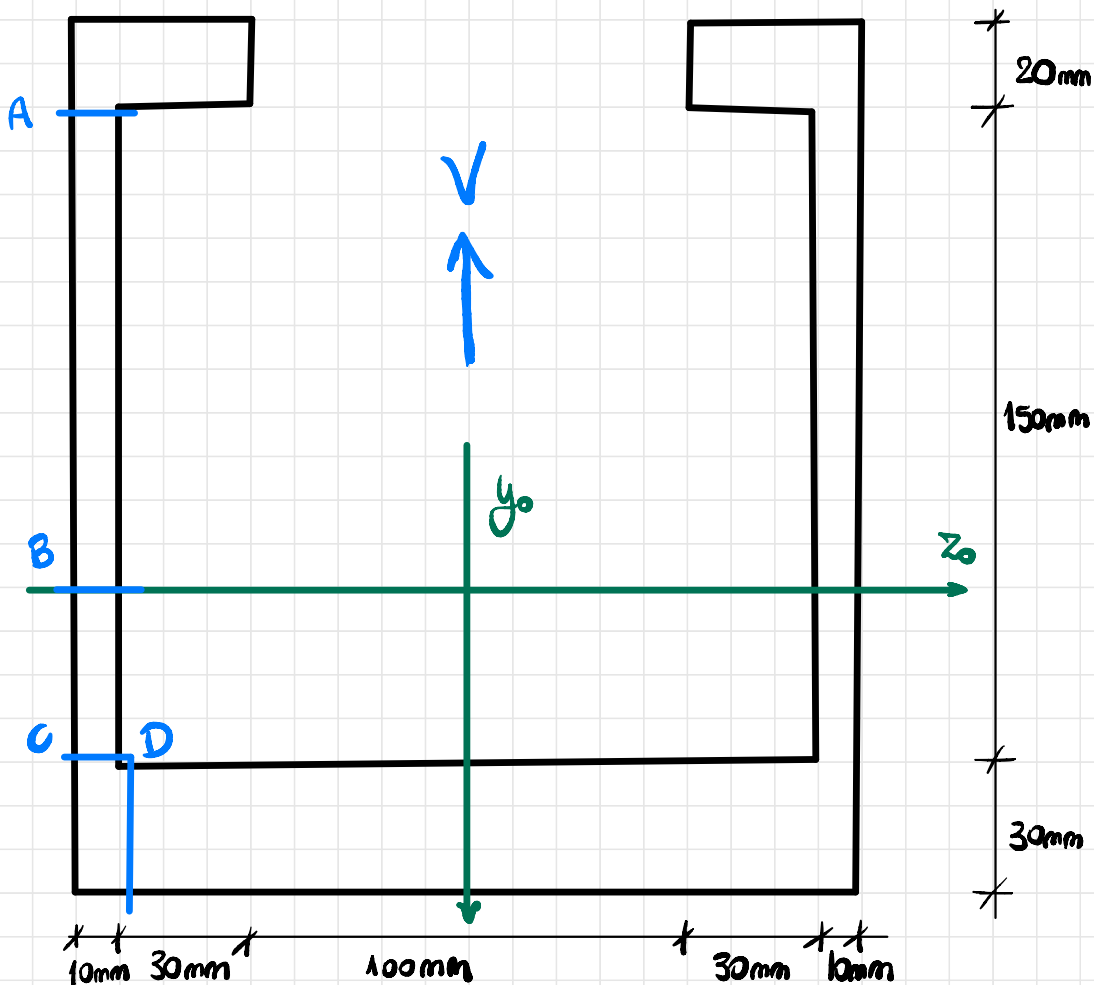
$$M_s^* = 0$$

$$\therefore \underline{\underline{\tau = 0}}$$

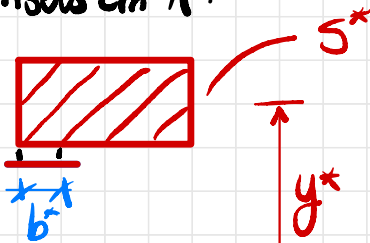
Distribuição de tensões:



Determine, para a seção abaixo, as tensões de cisalhamento, em MPa, nos pontos A, B, C e D, para uma força cortante $V = 250 \text{ kN}$. Estabeleça o diagrama e o fluxo das tensões de cisalhamento ao longo da seção. São dados $I_{z_0} = 4913,34 \cdot 10^4 \text{ mm}^4$ e $y_G = 70 \text{ mm}$.



Tensões em A:



$$b^* = 10 \text{ mm}$$

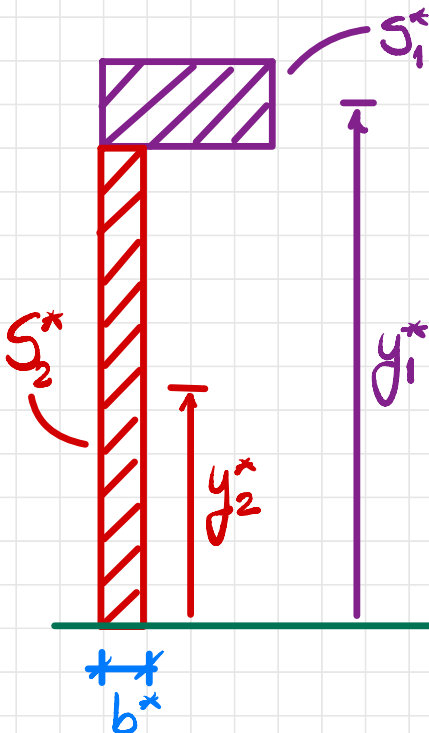
$$S^* = 40 \cdot 20 = 800 \text{ mm}^2$$

$$y^* = 190 - 70 = 120 \text{ mm}$$

$$M_s^* = S^* y^* = 96000 \text{ mm}^3$$

$$\tau_A = \frac{V M_s^*}{b^* I_{z_0}} = \frac{250 \cdot 10^3 \cdot 96000}{10 \cdot 4913,34 \cdot 10^4} = \underline{48,85 \text{ MPa}}$$

Tensões em B:



$$b^* = 10 \text{ mm}$$

$$S_1^* = 800 \text{ mm}^2$$

$$y_1^* = 120 \text{ mm}$$

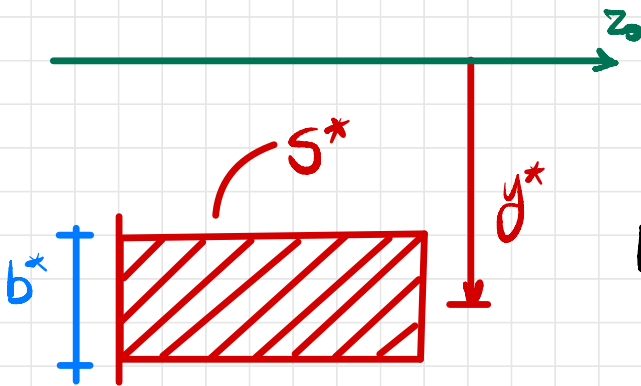
$$S_2^* = 10 \cdot 110 = 1100 \text{ mm}^2$$

$$y_2^* = 110/2 = 55 \text{ mm}$$

$$M_s^* = S_1^* y_1^* + S_2^* y_2^* = 156500 \text{ mm}^3$$

$$\tau_B = \frac{250 \cdot 10^3 \cdot 156500}{10 \cdot 4913,34 \cdot 10^4} = \underline{79,63 \text{ MPa}}$$

Tensão em D:



$$b^* = 30 \text{ mm}$$

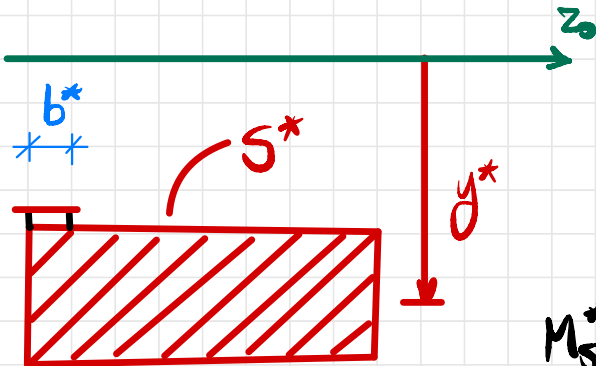
$$S^* = 30 \cdot 80 = 2400 \text{ mm}^2$$

$$y^* = 70 - 15 = 55 \text{ mm}$$

$$M_S^* = S^* y^* = 132000 \text{ mm}^3$$

$$\tau_D = \frac{250 \cdot 10^3 \cdot 132000}{30 \cdot 4913,34 \cdot 10^4} = \underline{22,39 \text{ MPa}}$$

Tensão em C:



$$b^* = 10 \text{ mm}$$

$$S^* = 90 \cdot 30 = 2700 \text{ mm}^2$$

$$y^* = 55 \text{ mm}$$

$$M_S^* = S^* y^* = 148500 \text{ mm}^3$$

$$\tau_C = \frac{250 \cdot 10^3 \cdot 148500}{10 \cdot 4913,34 \cdot 10^4} = \underline{75,56 \text{ MPa}}$$

Diagrama de tensões e fluxo:

