

$$(A - \lambda_2 I) v_2 = 0 \Rightarrow \begin{bmatrix} 1+1 & 1 \\ 0 & -1+1 \end{bmatrix} \begin{bmatrix} v_{21} \\ v_{22} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{21} \\ v_{22} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \Rightarrow \begin{cases} 2v_{21} + 1v_{22} = 0 \\ 0v_{21} + 0v_{22} = 0 \end{cases} \Rightarrow$$

$$\Rightarrow \begin{cases} v_{21} = \text{QUALQUER (P. EX., } v_{21} = 1) \\ v_{22} = -2 \cdot v_{21} \Rightarrow v_{22} = -2 \end{cases}$$

PORTANTO, $\lambda_2 = -1$, $v_2 = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$ (VERIFICAR)

EXEMPLO 2

$$A = \begin{bmatrix} -1 & -1 \\ 1 & -1 \end{bmatrix} ; (A - sI) = \begin{bmatrix} -1-s & -1 \\ 1 & -1-s \end{bmatrix}$$

$$\det(A - sI) = (-1-s)(-1-s) - 1 \cdot (-1) = s^2 + 2s + 2$$

$$\lambda^2 + 2\lambda + 2 = 0 \Rightarrow \lambda = \frac{-2 \pm \sqrt{2^2 - 4 \cdot 1 \cdot 2}}{2 \cdot 1} \Rightarrow \begin{cases} \lambda_1 = -1 + i \\ \lambda_2 = -1 - i \end{cases}$$