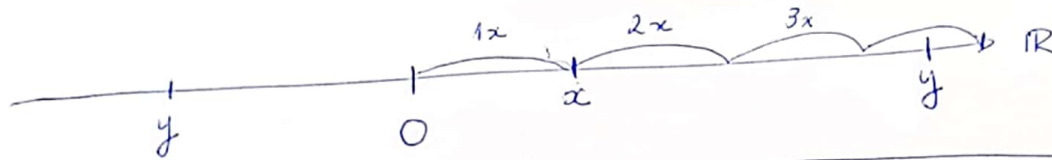


## Lista 2

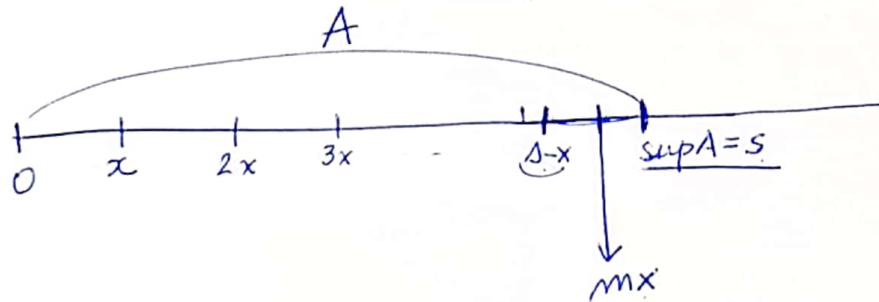
Entregar exercício 4 - Laboratório de Avaliação } dia 01/10.  
exercícios 10, 13, 15a - Para monitor  
5, 9b, 12 - vamos discutir em aula  
na 2ª feira  
3a, 7, outros do 9, } Victor.



$$\text{Se } y \leq 0 \\ 1 \cdot x > y$$

$$y > 0$$

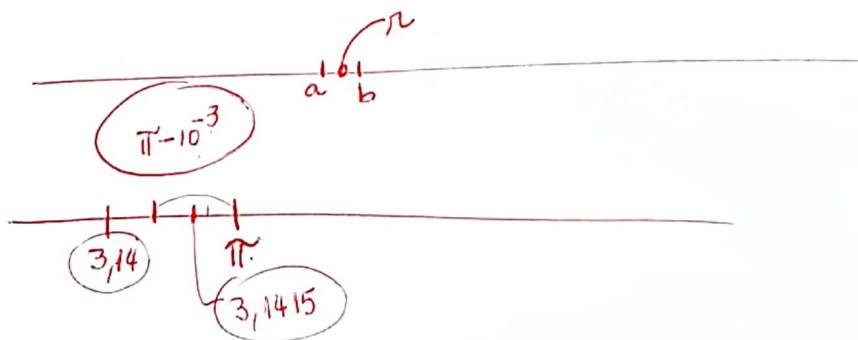
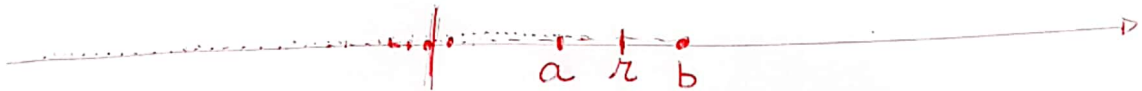
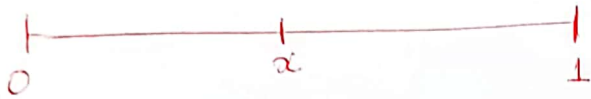
$$\exists m \in \mathbb{N} \text{ t.q. } mx > y$$

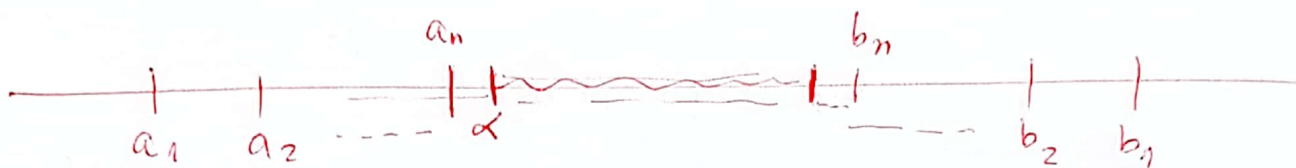
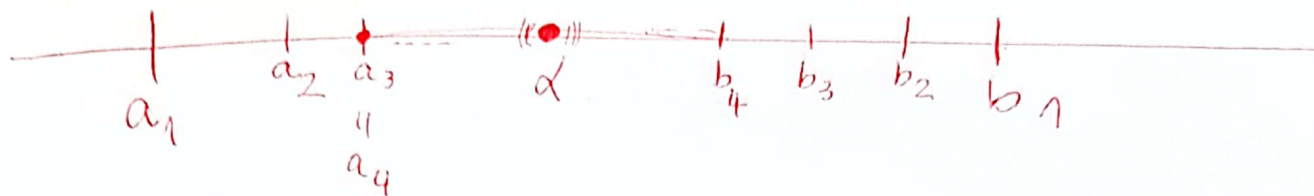


$$\delta - x < mx$$

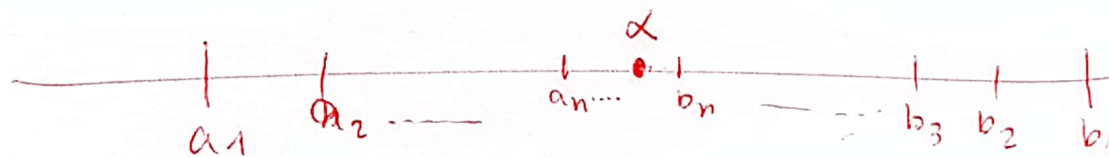
$$\delta < mx + x = \underbrace{(m+1)x}_{\in \mathbb{N}} \in A$$

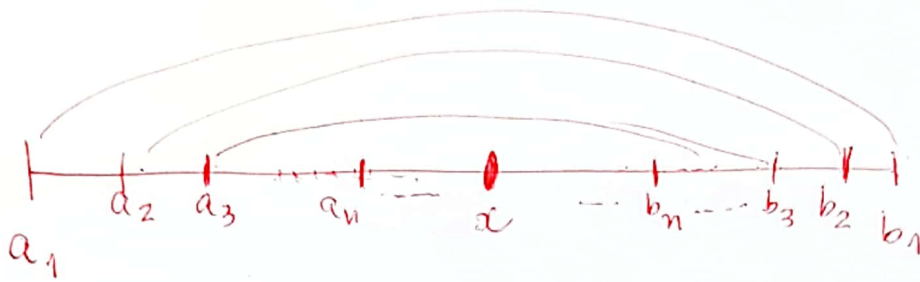
$\forall x \in \mathbb{R}, x > 0$  existe  $n \in \mathbb{N}$  tal que  $\frac{1}{n} < x$





Se  $\lim (b_n - a_n) = 0$





$$\boxed{x \in \bigcap_{n=1}^{\infty} [a_n, b_n]} \quad (\Leftrightarrow) \quad x \in \underline{[a_n, b_n]}, \quad \underline{\underline{\forall n.}}$$

$A = \{a_1, a_2, \dots\} \neq \emptyset$ , é limitado superiormente  
 $a_j \leq b_n, \quad \forall j, \forall n.$

$$\underline{\exists \sup A = \alpha}$$

$$a_n \leq \alpha \leq b_n, \quad \forall n$$

$$\underline{\alpha \in [a_n, b_n], \quad \forall n.}$$

$$I_n = ]0, \frac{1}{n}]$$

$$I_1 = ]0, 1]$$

$$I_2 = ]0, \frac{1}{2}]$$

$$I_3 = ]0, \frac{1}{3}]$$

⋮

$$\bigcap_{n=1}^{\infty} I_n = \emptyset$$

$$J_n = [0, \frac{1}{n}]$$

$$\bigcap J_n = \{0\} \quad \text{pois}$$

$$0 \in J_n, \forall n$$

$$K_n = ]0, 1 + \frac{1}{n}]$$



$$\bigcap K_n \neq \emptyset$$

$$1 \in K_n, \forall n$$