

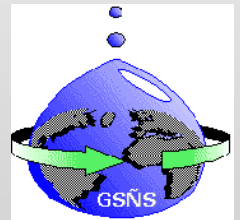
Unsaturated Soil Mechanics

Lesson 3

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2020



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Unsaturated Soil Mechanics

- **Basic Concepts**
 - Effective stress principle
 - Mohr-Coulomb and Tresca failure criteria
- **Meteorological aspects and soil water balance**
 - Rain and evaporation
 - Infiltration
 - Retention
- **Soil as a particulate media**
 - Mass and volume relations
 - Pore size distribution
- **Capillary and suction concepts**
 - Matrix suction
 - Osmotic suction
 - Total suction
- **Soil suction measurement**
- **The Soil Water Retention Curve - SWRC**
 - Interpretation of the SWRC
 - Fitting models for the SWRC
- **Shear strength for unsaturated soils**
 - Shear strength parameters
 - Laboratory tests
 - Bishop's concepts
 - Fredlund's concepts
 - Models using the SWRC
- **Applications**
 - Slopes
 - Dams
 - Mining

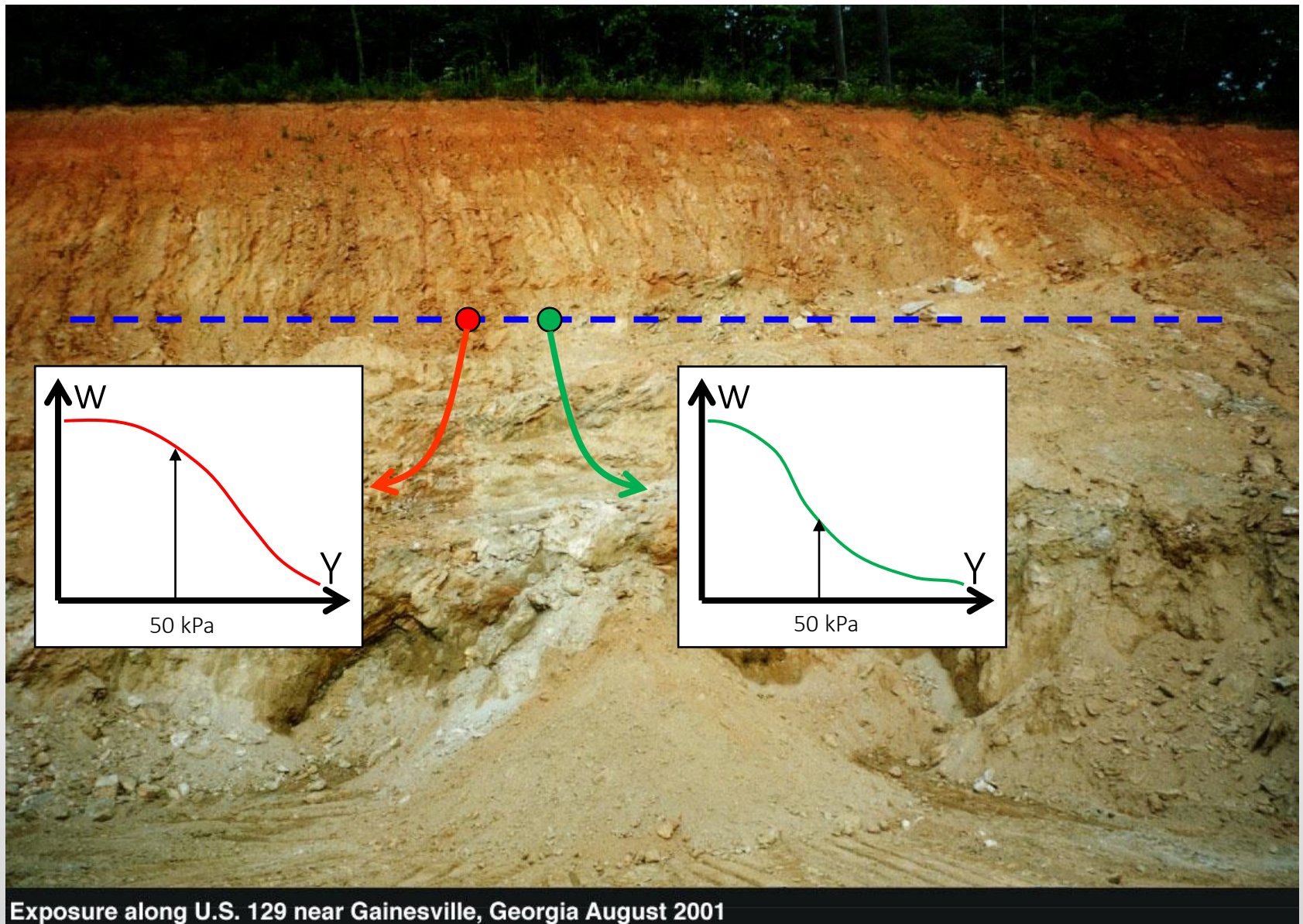
- **Soil suction measurement**



“When one starts already with a complicated, expensive apparatus, HE IS SLAVE OF HIS INSTRUMENT”

Terzaghi

Suction or Water Content, what is more difficulty to measure?



Exposure along U.S. 129 near Gainesville, Georgia August 2001

What does the sensors measure?

Table 1.2. Surrogate measures used by different θ_v sensors

Method	Surrogate Measurement	Explanation
Neutron moisture meter	Count of slow neutrons around a source of fast neutrons	A radioactive source emits fast neutrons (5 MeV), which lose energy as they collide with other atoms, in particular hydrogen. The surrogate is the concentration of slow neutrons. Since the only rapidly changing source of hydrogen in the soil is water, θ_v can be calibrated vs. the count of slow neutrons.
Thermal sensors	Heat conductivity or heat capacity of the soil	A pulse of heat is generated and the subsequent rise or fall in temperature of adjacent soil is measured over time. Soil is a poor conductor of heat, and water a good one, so the amount of heat or rate of heat transmission is closely related to θ_v .
Time domain reflectometer (TDR)	Travel time of an electromagnetic pulse	A fast rise time electromagnetic pulse is injected into a waveguide inserted into or buried in the soil. The time required for the pulse to travel along the metal rods of the waveguide is determined by the bulk electrical permittivity of the soil. The θ_v is a major factor influencing the bulk permittivity (BEC). True TDR involves capture of a waveform and analysis to find the travel time of the highest frequency part of the pulse.
Campbell FDR	Repetition time for a fast rise time electromagnetic pulse	See TDR sensors; same, except reliance on reflected pulse reaching a set voltage rather than waveform analysis causes the method to be more influenced by BEC and temperature.
Capacitive sensors	Frequency of an oscillating circuit	An oscillating current is induced in a circuit, part of which is a capacitor that is arranged so that the soil becomes part of the dielectric medium affected by the electromagnetic field between the capacitor's electrodes. The θ_v influences the electrical permittivity of the soil, which in turn affects the capacitance, causing the frequency of oscillation to shift.
Conductivity sensors (e.g., granular matrix sensors and gypsum blocks)	Electrical conductivity of a porous medium in contact with the soil	An alternating current voltage is placed on two electrodes in a porous material in contact with the soil, and the amount of current is a measure of the conductivity and amount of water in the porous material between the electrodes. These are used for estimation of soil water tension (suction), not θ_v .
Tensiometers	Matric and gravitational soil water potential components	Capillary forces retaining water in the soil pores are connected through the soil water to water in a porous cup connected to a tube filled with water. This generates a negative pressure within the tube, which can be measured with a vacuum gauge. These are used for estimation of soil water tension (suction), not θ_v .



In this cases suction is measured

What interferes with measurements of each sensor?

Table 1.4. Characteristics of some types of soil water sensor

Technology	Sensed volume	Interferences
NMM	$3 \times 10^4 \text{ cm}^3$ (wet soil) $28 \times 10^4 \text{ cm}^3$ (dry soil)	Cl, B, Fe, C
TDR	Soil volume along length of probe rods, and ~10 mm above and below the plane of the rods, and 10 mm to the side of the plane of the rods (e.g., ~320 cm^3 for a 20 cm probe with 3 rods and 3 cm rod-to-rod spacing).	Salt, electrical conductivity of soil and temperature, magnetic minerals (uncommon)
Capacitive, FDR	Highly variable — usually 90% of reading comes from within 20 mm of the sensitive face of the sensor, but sometimes the sensed volume is smaller than the height of the sensors. Typically ~200– 400 cm^3 .	Salt, electrical conductivity of soil (including clay type, content, and water content) and temperature
Heat dissipation	Highly variable — 20 mm zone around sensor, which is small.	Metallic soil components
Conductivity sensors (e.g. gypsum blocks)	Will equilibrate with a volume of soil that is determined by the soil hydraulic conductivity. Typically 500 cm^3 in wet soil, but much smaller in dry soil.	Temperature, salts other than the CaSO_4 used in the sensor

Table 4.2 Devices for Measuring Soil Suction and Its Components

Name of Device	Suction Component Measured	Range, kPa	Comments
Psychrometers (Peltier type)	Total	100 ^a to ~8000	Constant-temperature environment required
Filter paper	Total	Entire range	May measure matric suction when in good contact with moist soil
Tensiometers	Negative pore-water pressures or matric suction when pore-air pressure is atmospheric	0–90	Difficulties with cavitation and air diffusion through ceramic cup
Null-type pressure plate (axis translation)	Matric	0–1500	Range of measurement is a function of the air-entry value of ceramic disk
Thermal conductivity sensors	Matric	10 to ~1500	Indirect measurement using variable-pore-size ceramic sensor
Pore fluid squeezer	Osmotic	Entire range	Used in conjunction with psychrometer or electrical conductivity measurement

^aControlled temperature environment to $\pm 0.001^{\circ}\text{C}$.

Table 2.3 Methods for measuring soil suction (after Ridley and Wray, 1995)

<i>Device</i>	<i>Measurement mode</i>	<i>Range (kPa)</i>	<i>Approximate equilibrium time</i>
Thermocouple psychrometer	Total	100 to 7,500	Minutes
Thermisor/Transistor psychrometer	Total	100 to 71,000	Minutes
Filter paper (in-contact)	Matric	30 to 30,000	7 days
Filter paper (no-contact)	Total	400 to 30,000	7–14 days
Porous block	Matric	30 to 3,000	Weeks
Thermal conductivity probe	Matric	0 to 300	Weeks
Pressure plate	Matric	0 to 1,500	Hours
Standard tensiometer	Matric	0 to –100	Minutes
Tensiometer suction probe	Matric	0 to –1,800	Minutes

Table 2.1 Approximate measurement ranges and times for equilibration in measurement and control of soil suction.

Instrument	Suction component measured	Typical measurement range (kPa)	Equilibration time
<i>Suction measurement</i>			
Pressure plate	Matric	0–1,500	Several hours to days
Tensiometers and suction probes	Matric	0–1,500	Several minutes
Thermal conductivity sensors	Matric	1–1,500	Several hours to days
Electrical conductivity sensors	Matric	50–1,500	Several hours to weeks
Filter paper contact	Matric	0–10,000 or greater	2–57 days
Thermocouple psychrometers	Total	100–8,000	Several minutes to several hours
Transistor psychrometers	Total	100–70,000	About 1 hour
Chilled mirror psychrometer	Total	1–60,000	3–10 minutes
Filter paper non-contact	Total	1,000–10,000 or greater	2–14 days
Electrical conductivity of pore water extracted using pore fluid squeezer	Osmotic	entire range	—
<i>Suction control</i>			
Negative (or Hanging) water column technique	Matric	0–30 or greater with multiple columns or vacuum control	Several hours to days
Axis translation technique	Matric	0–1,500	Several hours to days
Osmotic technique	Matric	0–10,000	up to 2 months
Vapour equilibrium technique	Total	4,000–600,000	1–2 months

Measurements made with different sensors at the same location in the same time interval.

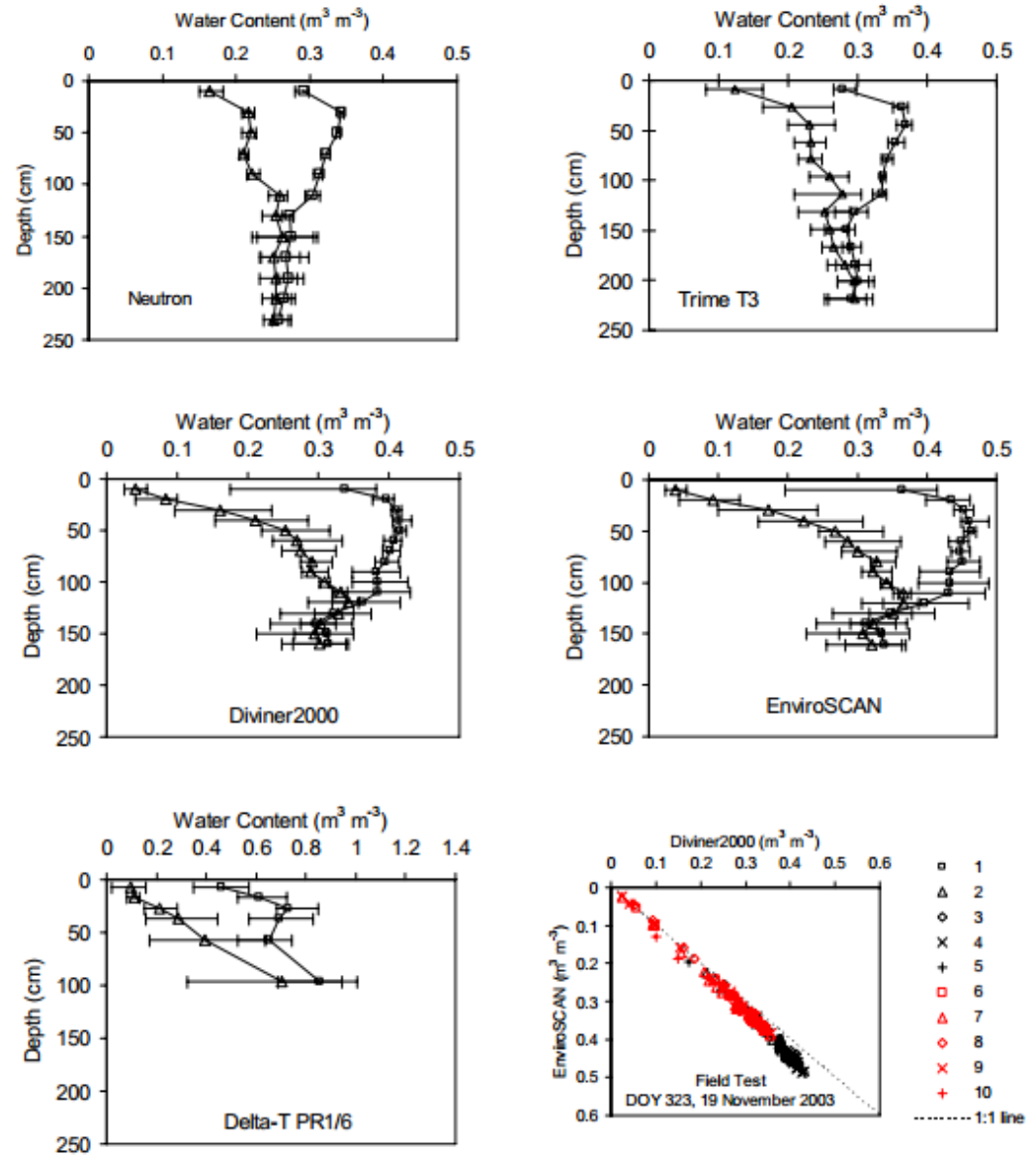


Figure 1.1. Soil water contents reported by five different sensors in access tubes in two plots irrigated weekly to 100% replenishment of soil water to field capacity (squares) and to 33% of the 100% amount (triangles indicate this deficit irrigation). Ten access tubes for each sensor were in the 100% plot and ten each in the 33% plot. Bars indicate the maximum and minimum values of θ_v for each plot and depth, and solid lines indicate the mean value of θ_v .

Suction Measurement and Control Technique



```
graph TD; A[Suction Measurement and Control Technique] --> B[Ordinary tensiometer]; A --> C[High capacity tensiometer]; A --> D[Filter Paper]; A --> E[Suction Plate (control)]; A --> F[Axis translation (control and measurement)];
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Ordinary tensiometer

High capacity tensiometer

Filter Paper

Suction Plate (control)

Axis translation (control and measurement)

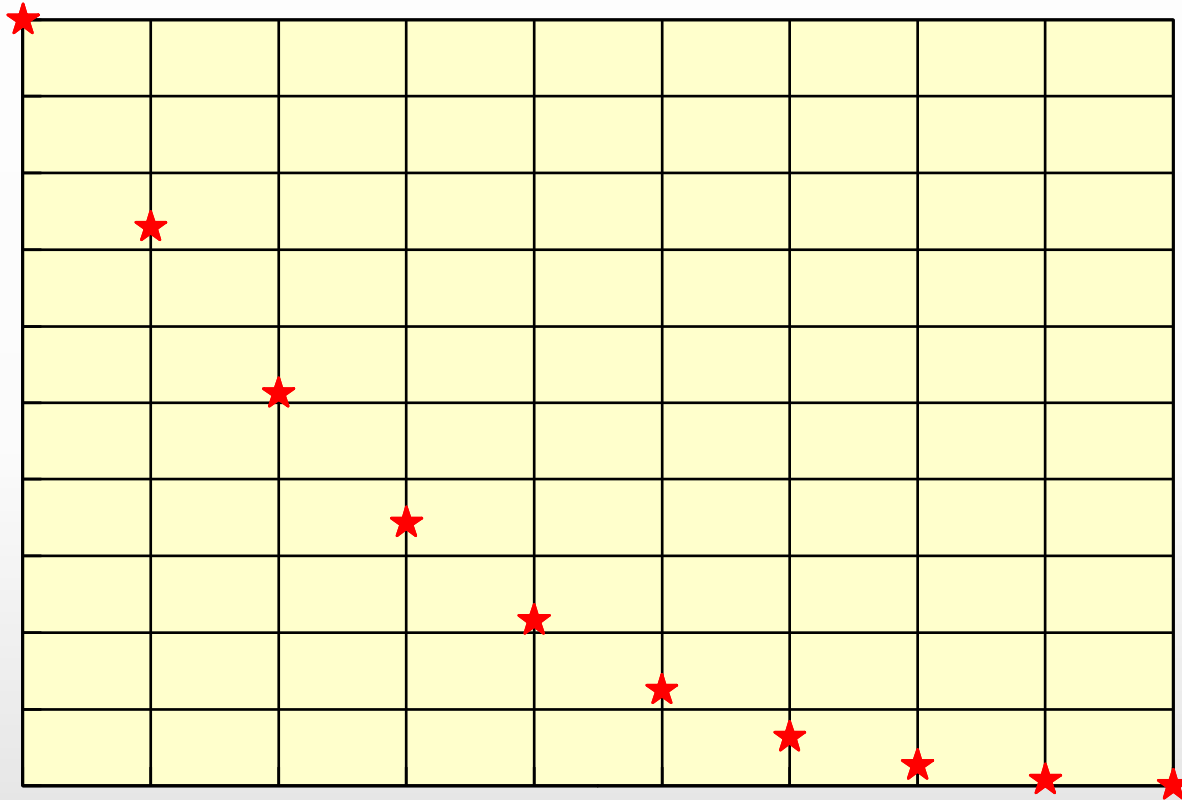
What is a sensor?

A Sensor is a device, which responds to an input quantity by generating a known output.

What is a sensor?

Water content
Resistivity
Wave velocity
etc....

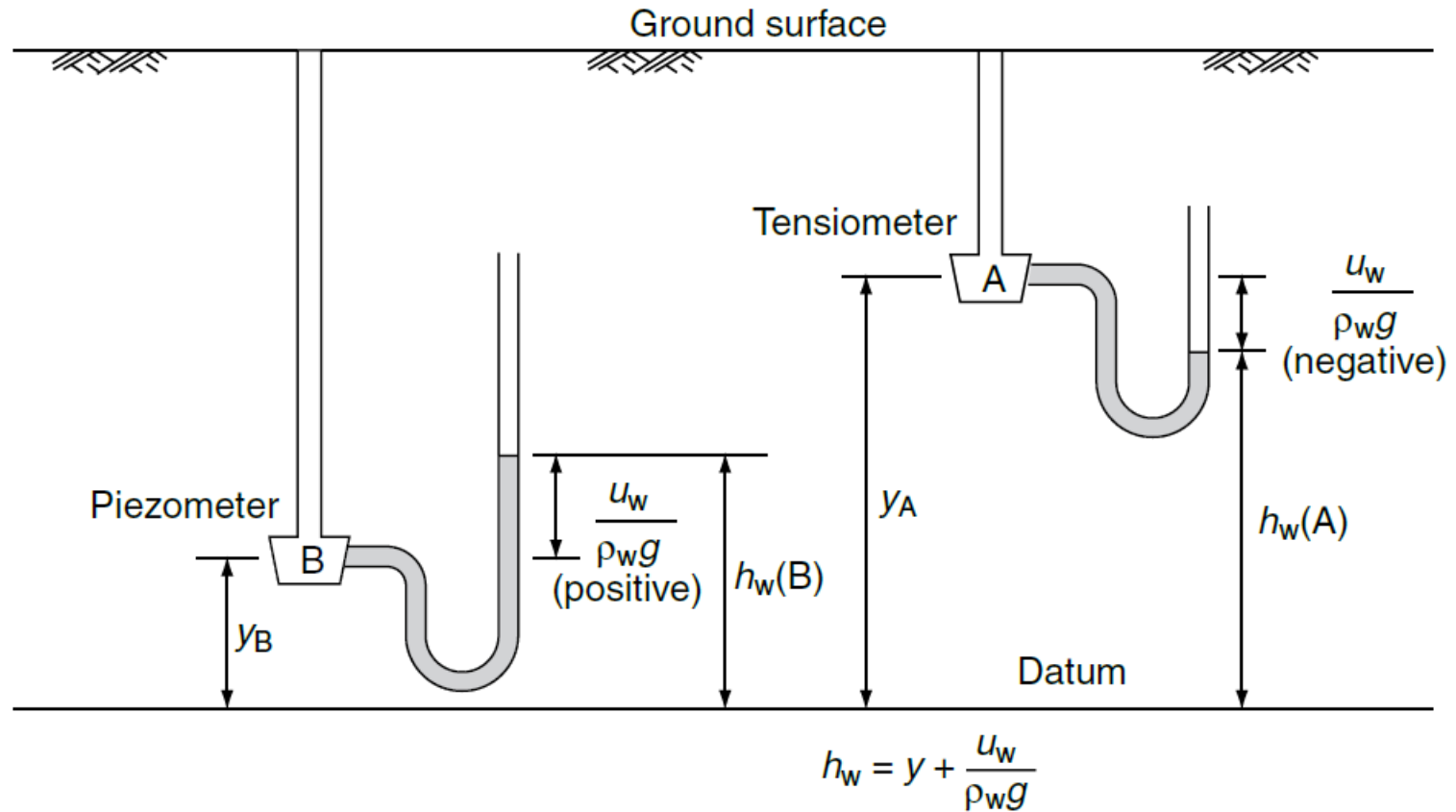
Output



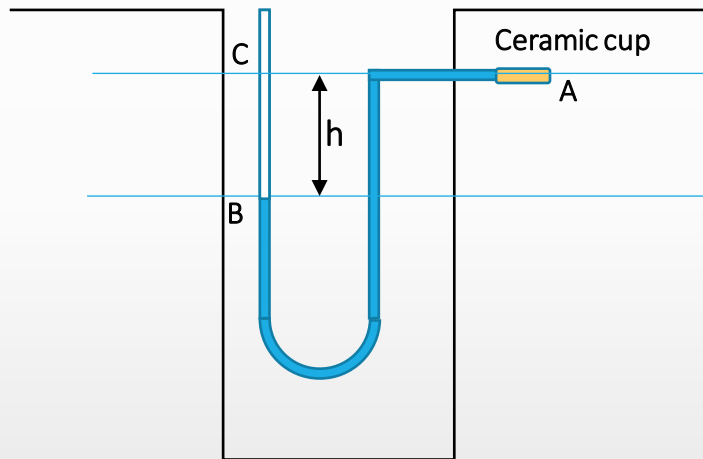
Suction

Input

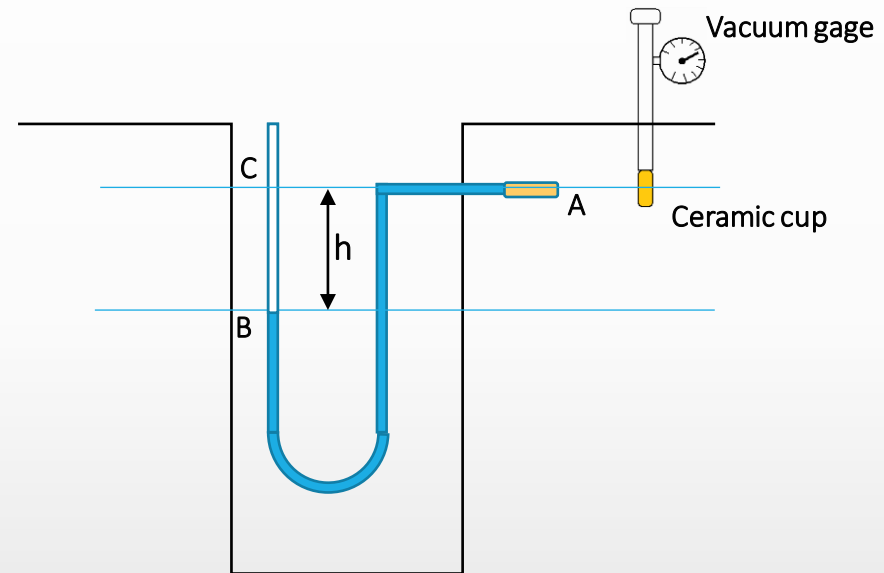
Concept of potential and head for saturated soils



Working Principle of a Tensiometer

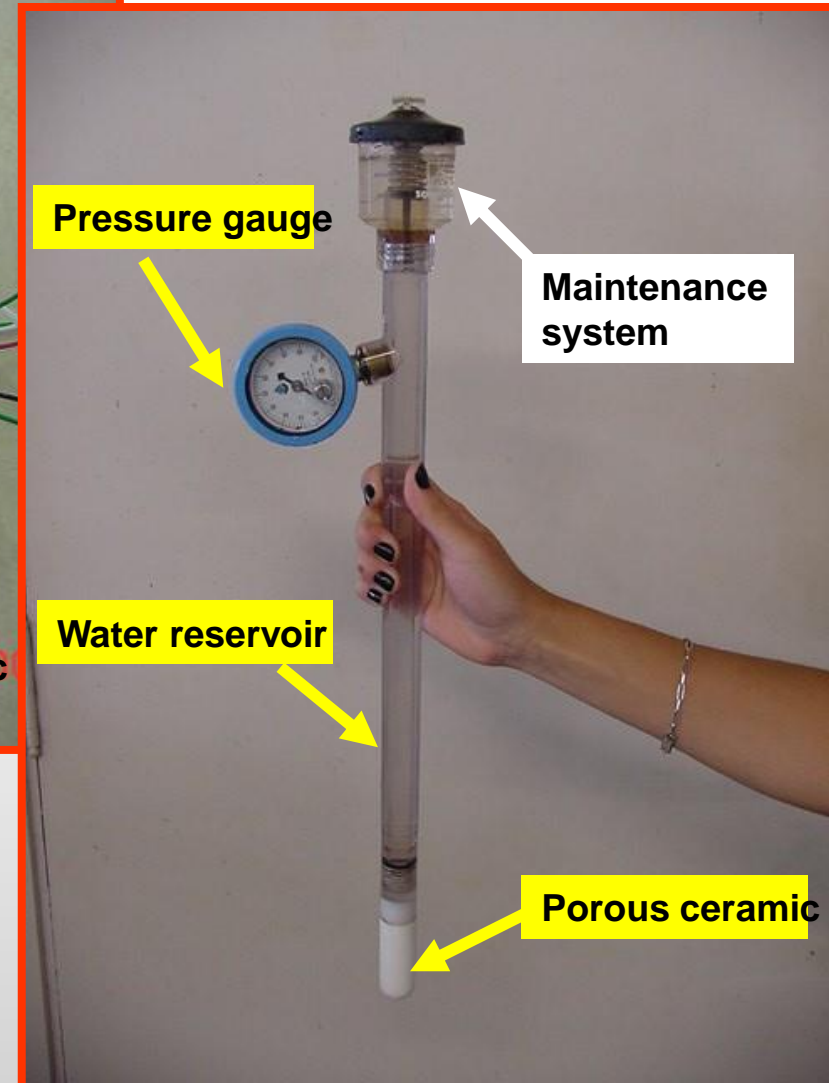
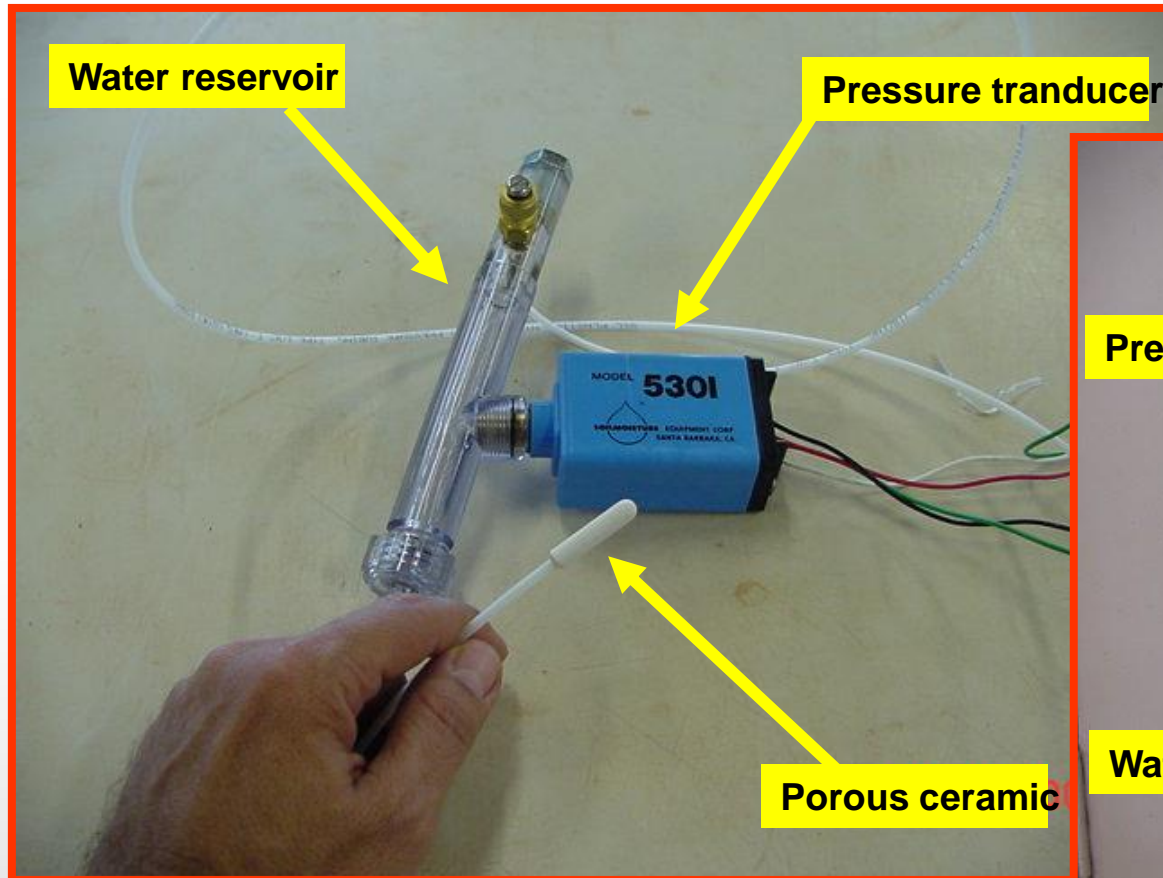


$$\text{Pressure} = -h * \gamma_w$$
$$\text{Suction} = h * \gamma_w$$



$$\text{Pressure} = -h * \gamma_w$$
$$\text{Suction} = h * \gamma_w$$

Ordinary Tensiometer



Working Principle of a High Capacity Tensiometer

Capillarity

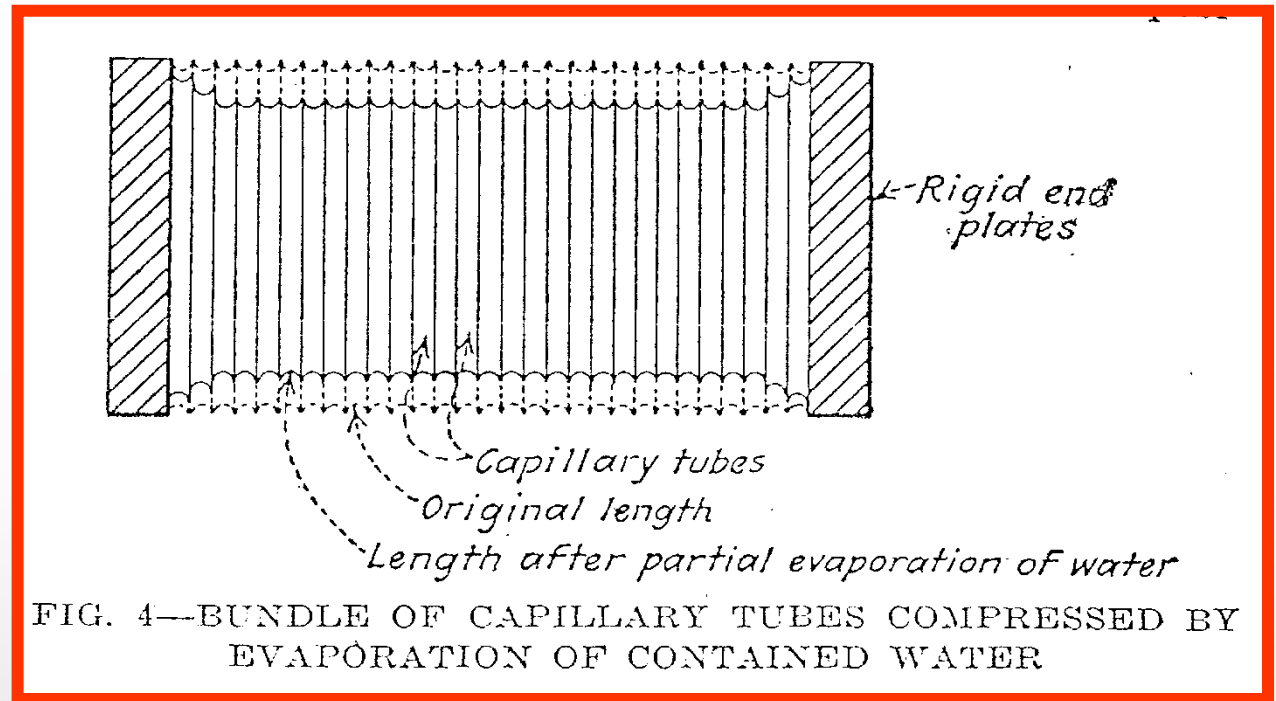
Soil



Voids

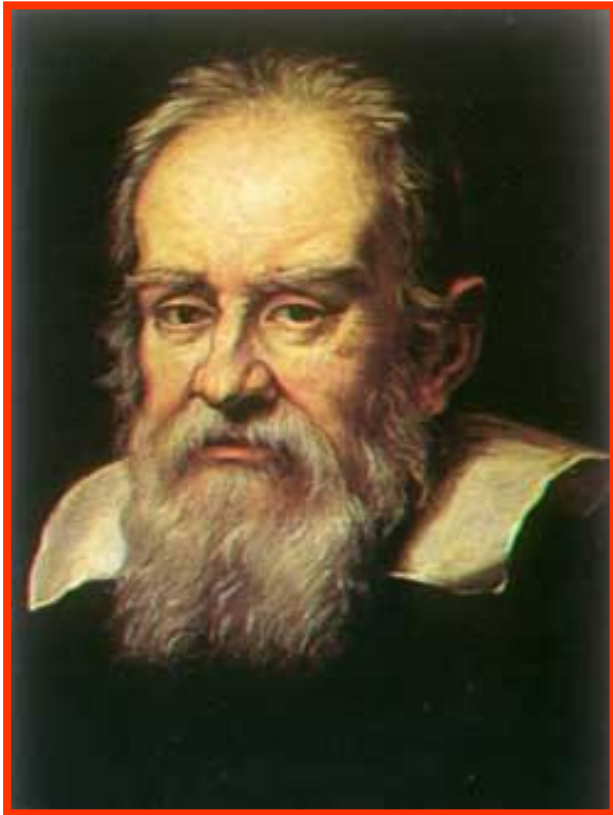


Capillary phenomena



Terzaghi (1925)

Galileo-Galilei

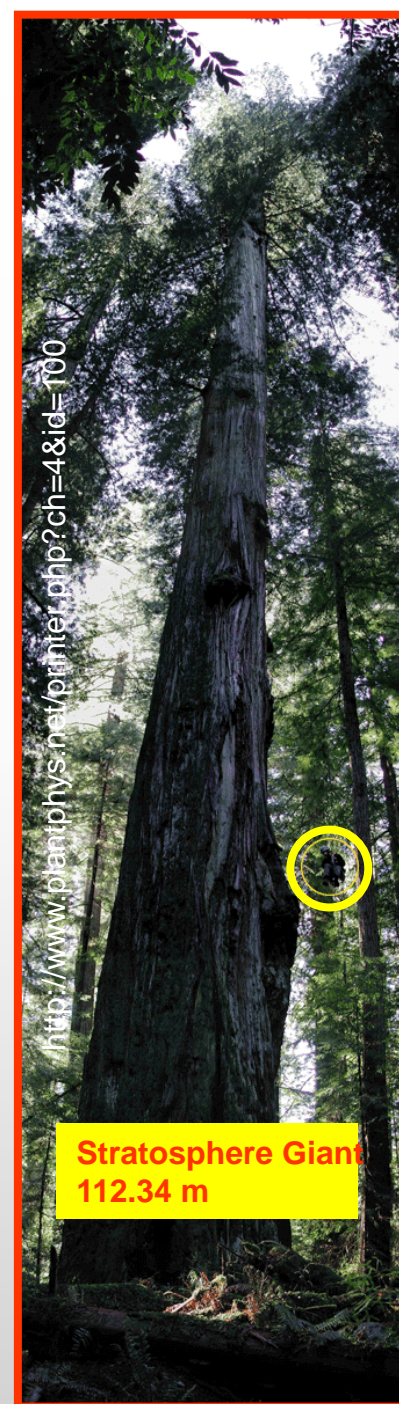
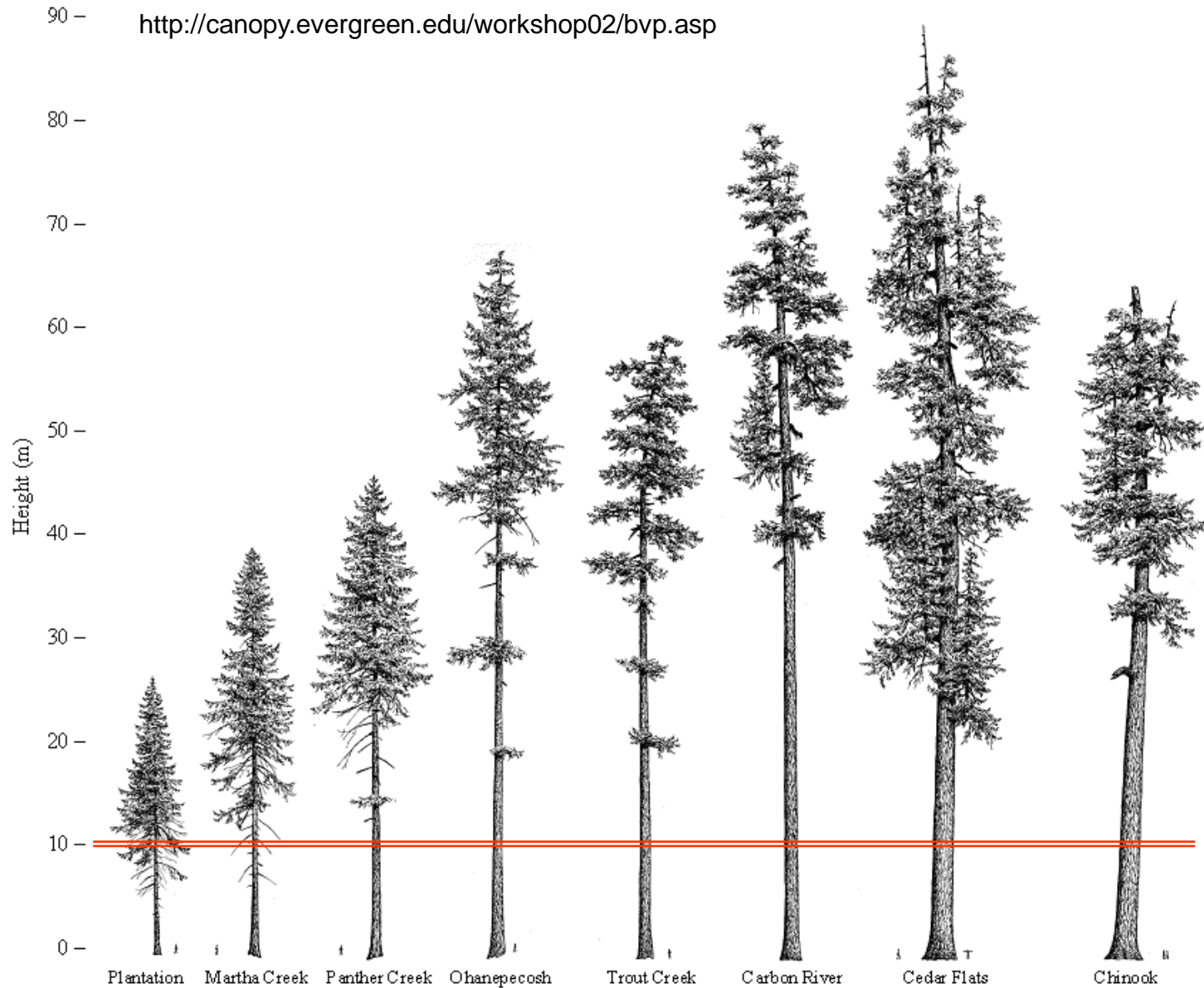


The first observation that water cannot rise indefinitely has been attributed to Galileo Galilei.

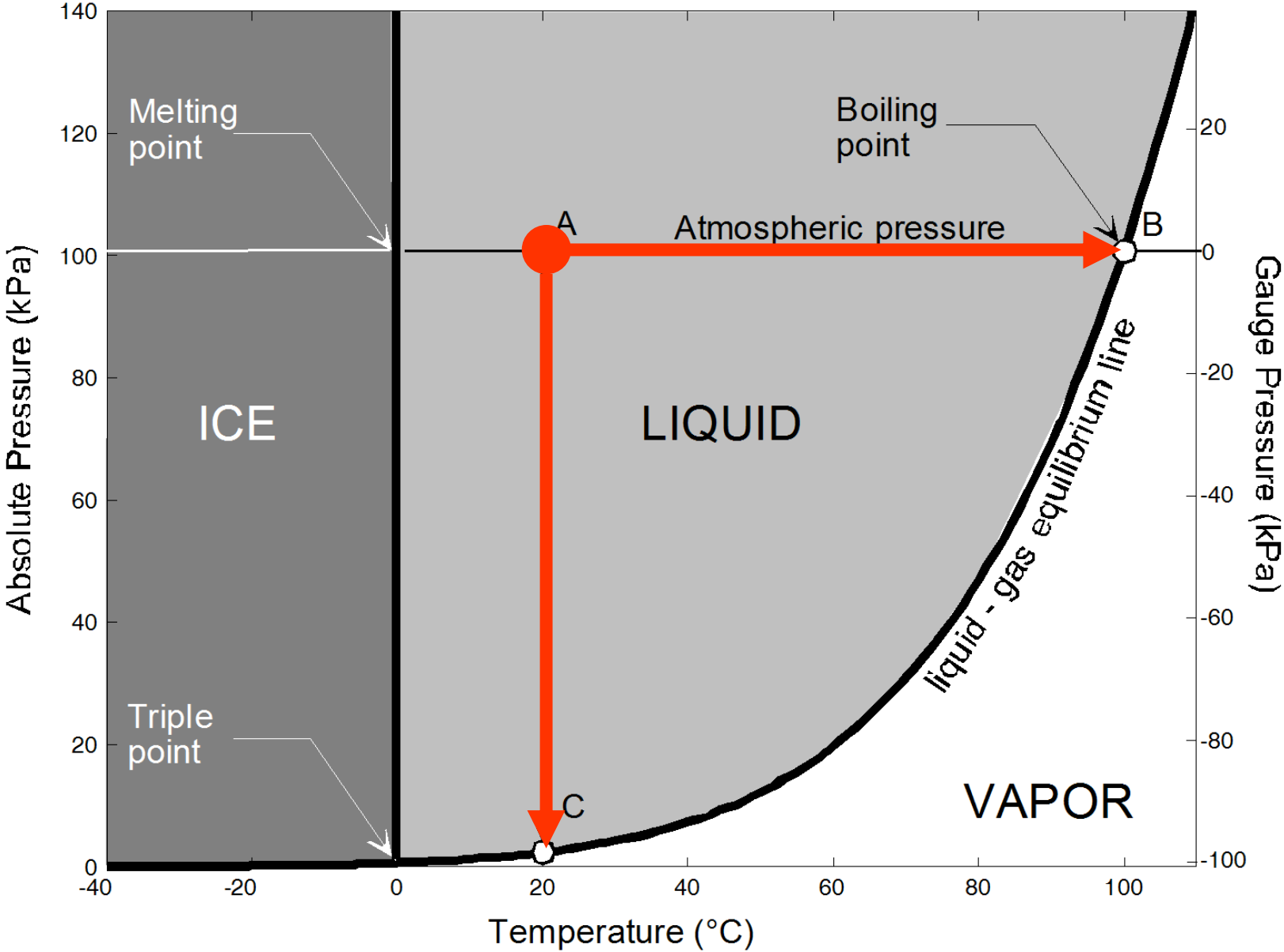
He found that 10m was the limit to which the water could rise in a suction pump.

This limit is determined by the phenomena of cavitation

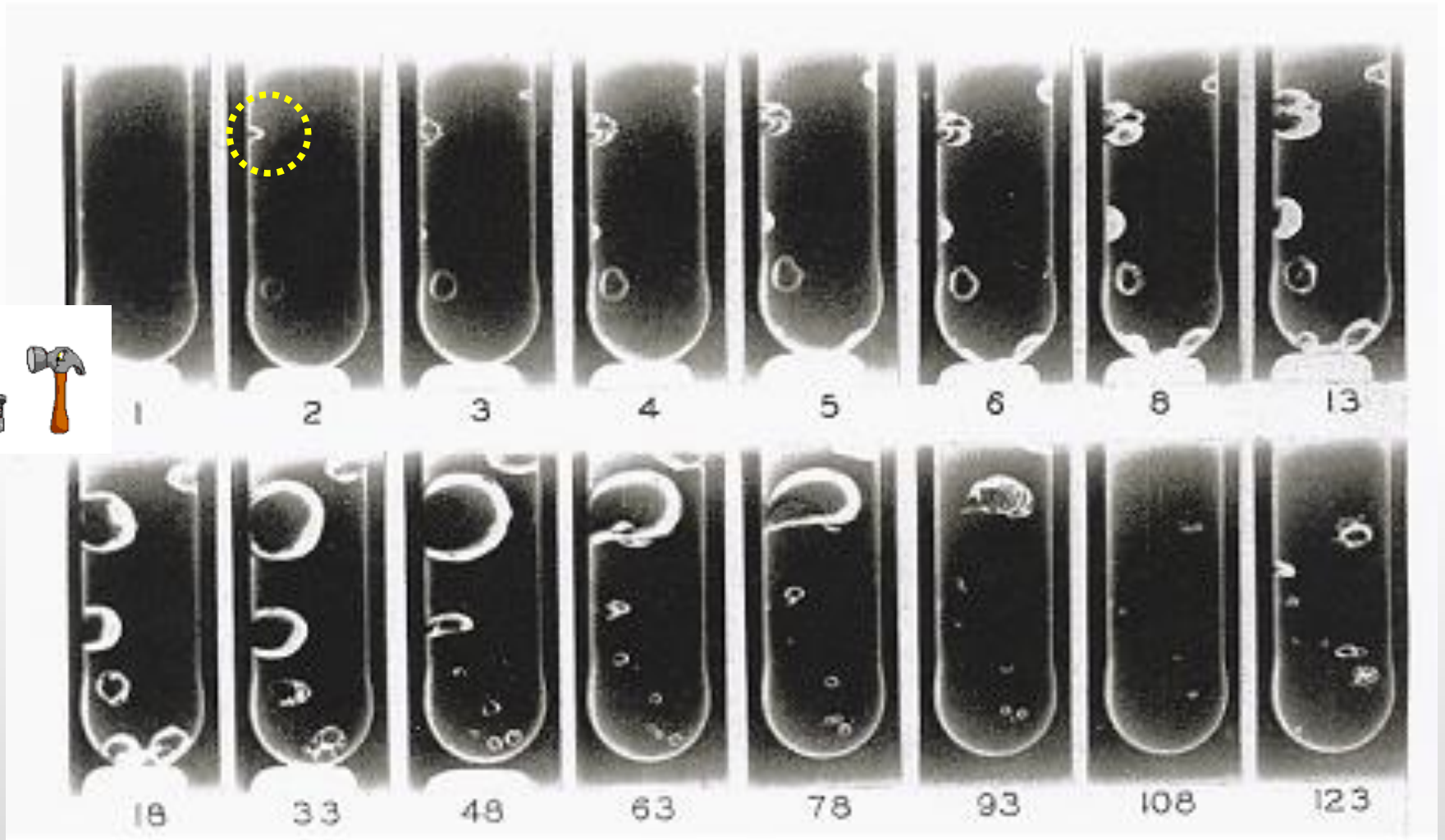
Water rise



Cavitation

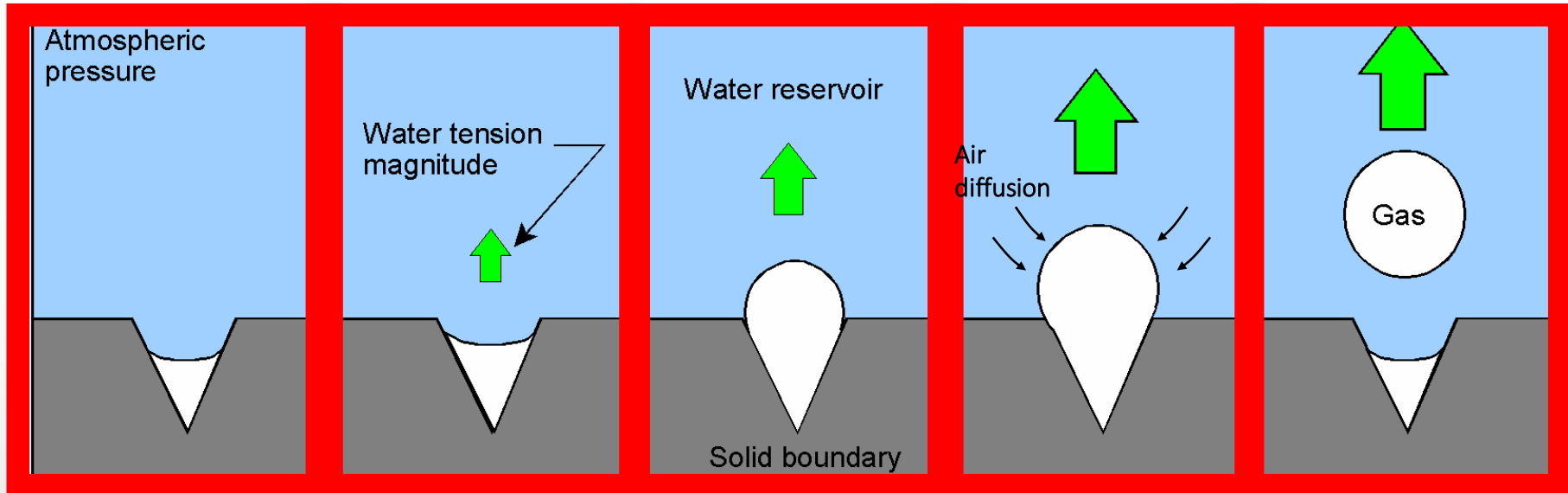


Cavitation



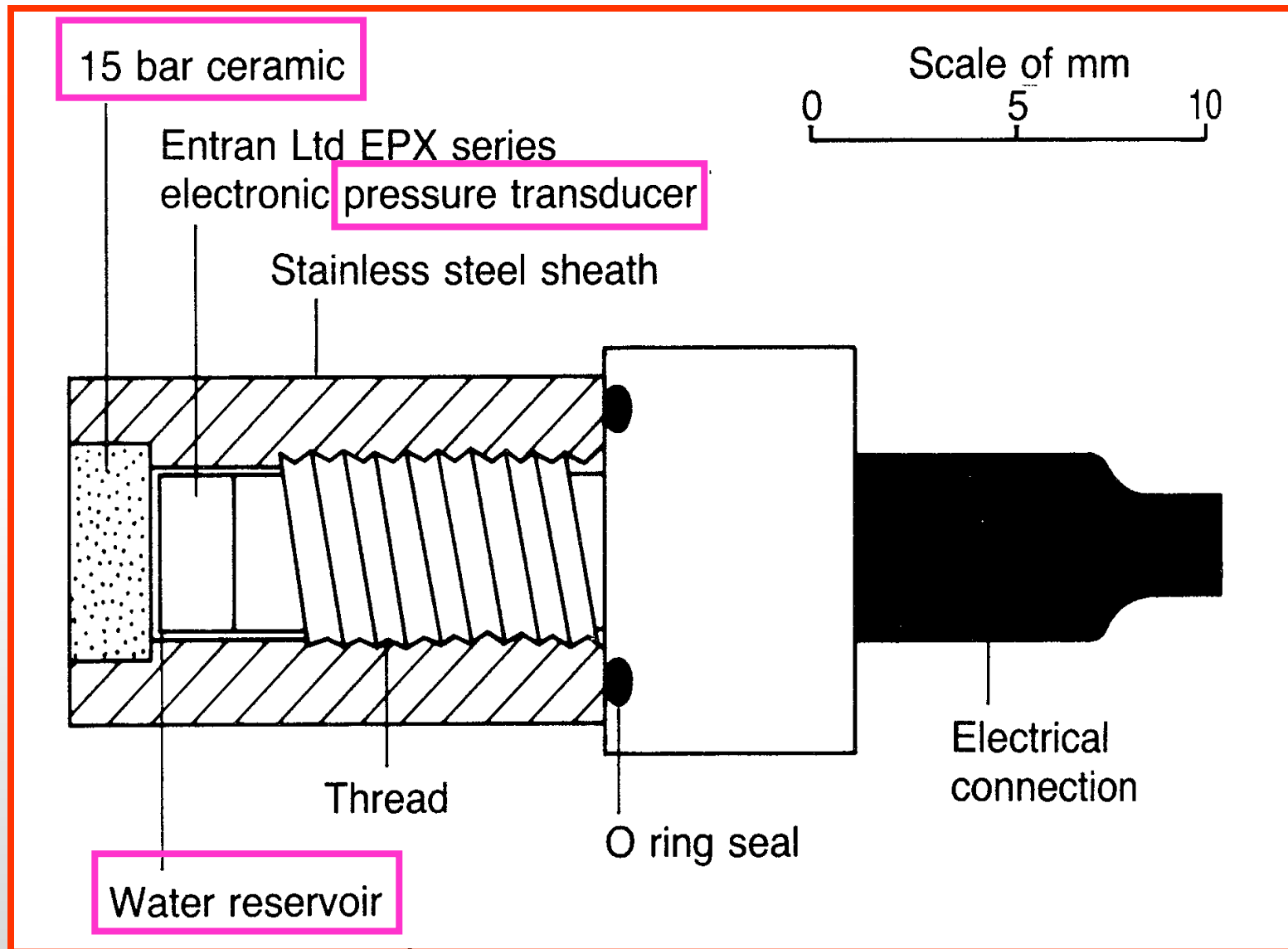
Air bubbles arising in a glass tube. (Harvey et al., 1944)

A Cavitation Mechanism (Harvey et al, 1944)

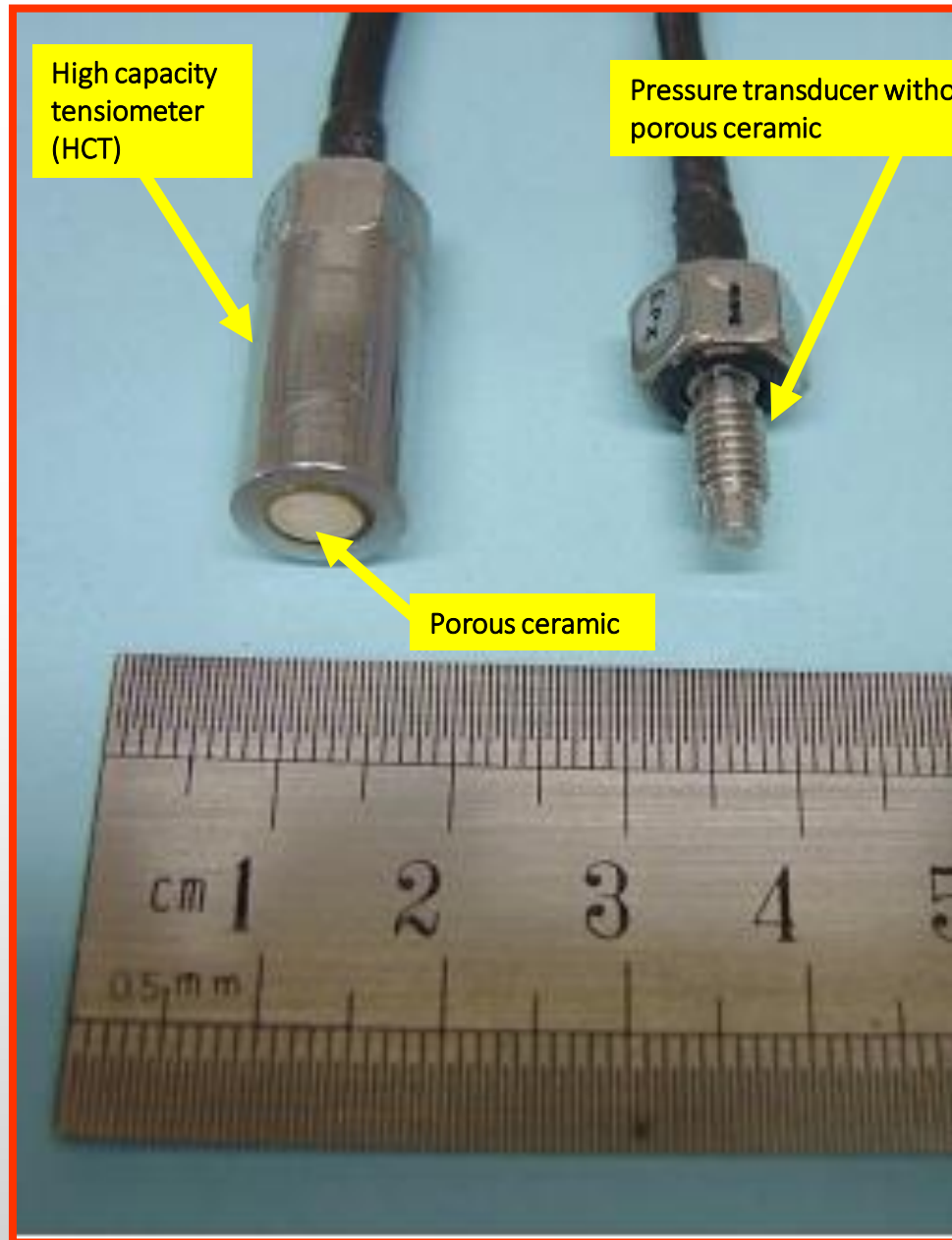


Does this mean that tensiometers are limited to - 1atm?

The design of a HCT



High Capacity Tensiometer



The Tensiometer: Saturation

Initial Saturation:

- Evacuation of tensiometer reservoir / ceramic
- Importance of initially dry ceramic (e.g. Take & Bolton, 2003)
- Rotational technique (low air entry value ceramics)
- Two chamber technique (higher air entry value ceramics)

Pre-pressurisation (Conditioning):

- Application of a large positive water pressure
- Cycles of cavitation and pressurisation (Tarantino & Mongiovì, 2001)

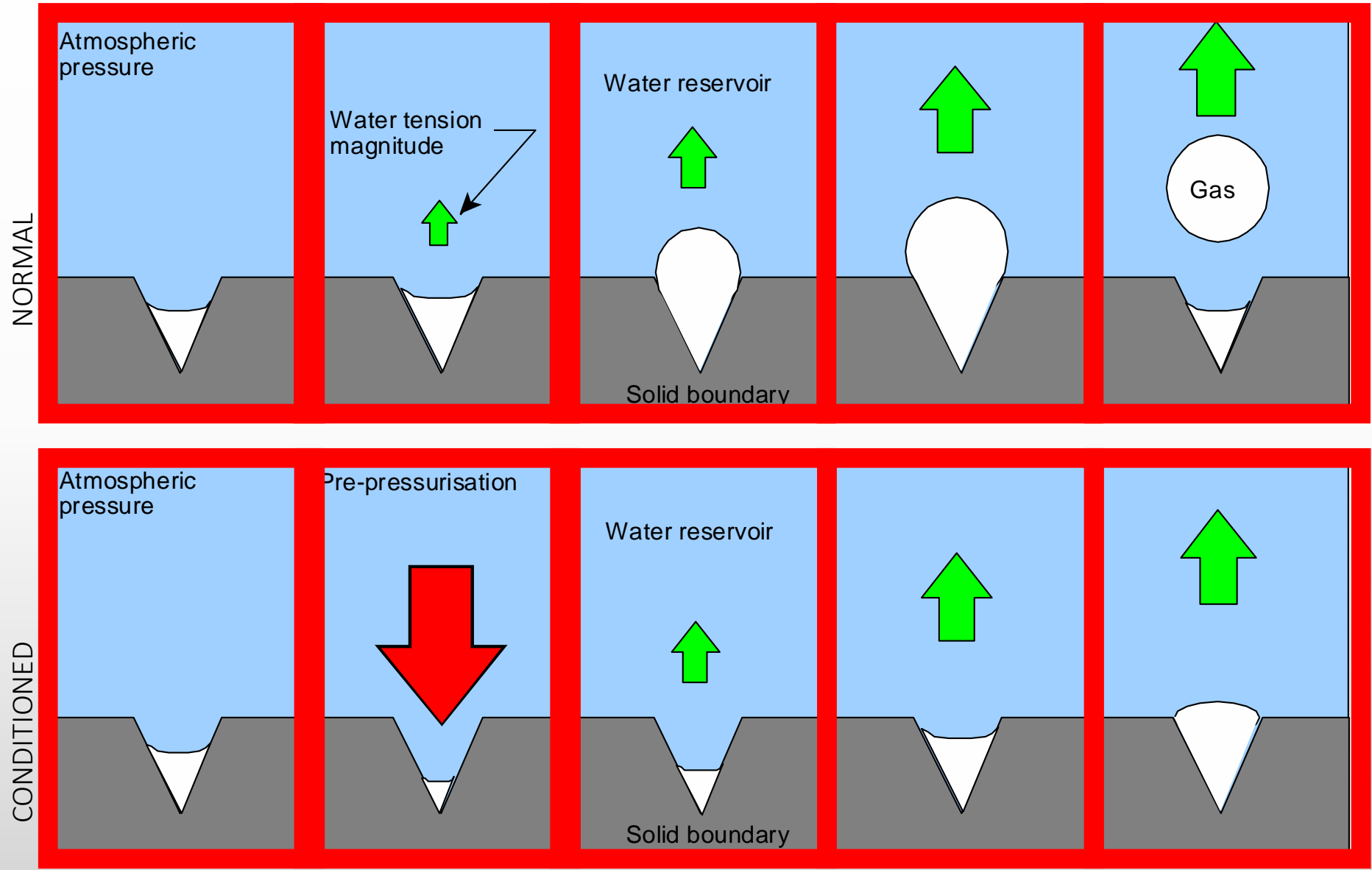
Difficulty of Saturation

- Increases with air-entry value (AEV)
- Required conditioning pressure increase with AEV

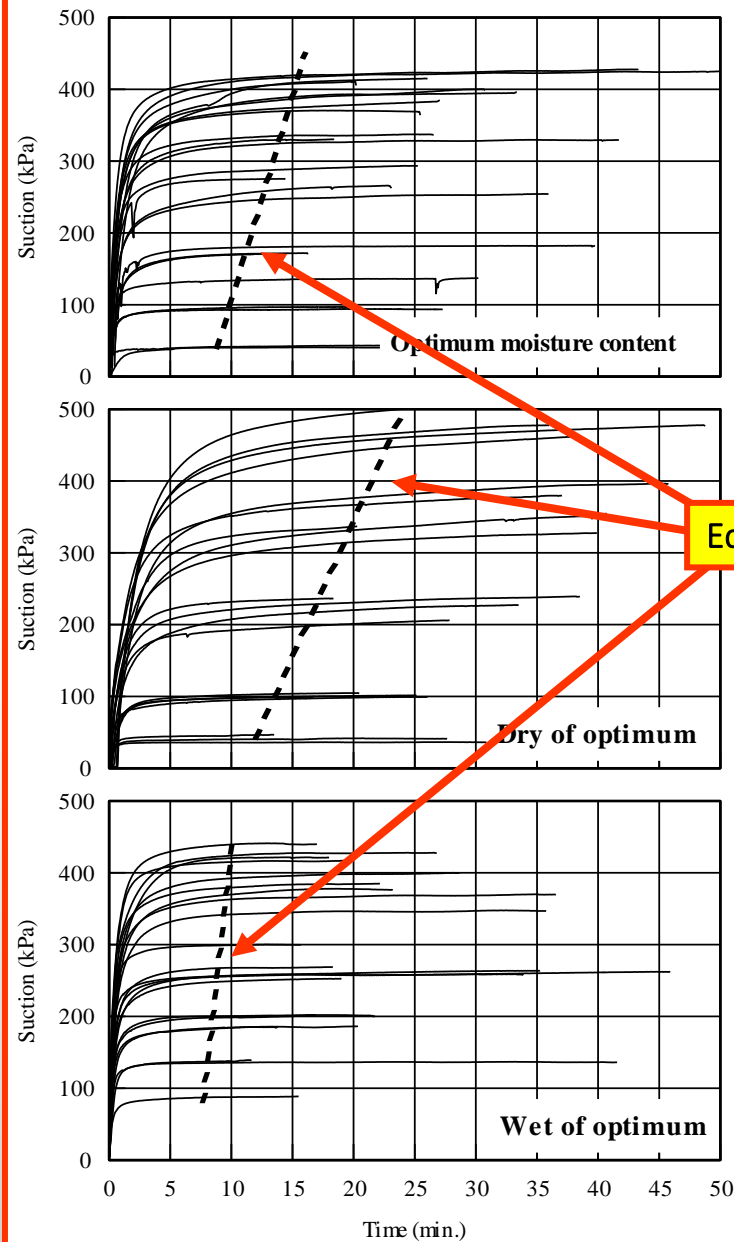
Chemical Treatment

- May help in the reduction of number of cavitation nuclei?

The Tensiometer: Saturation

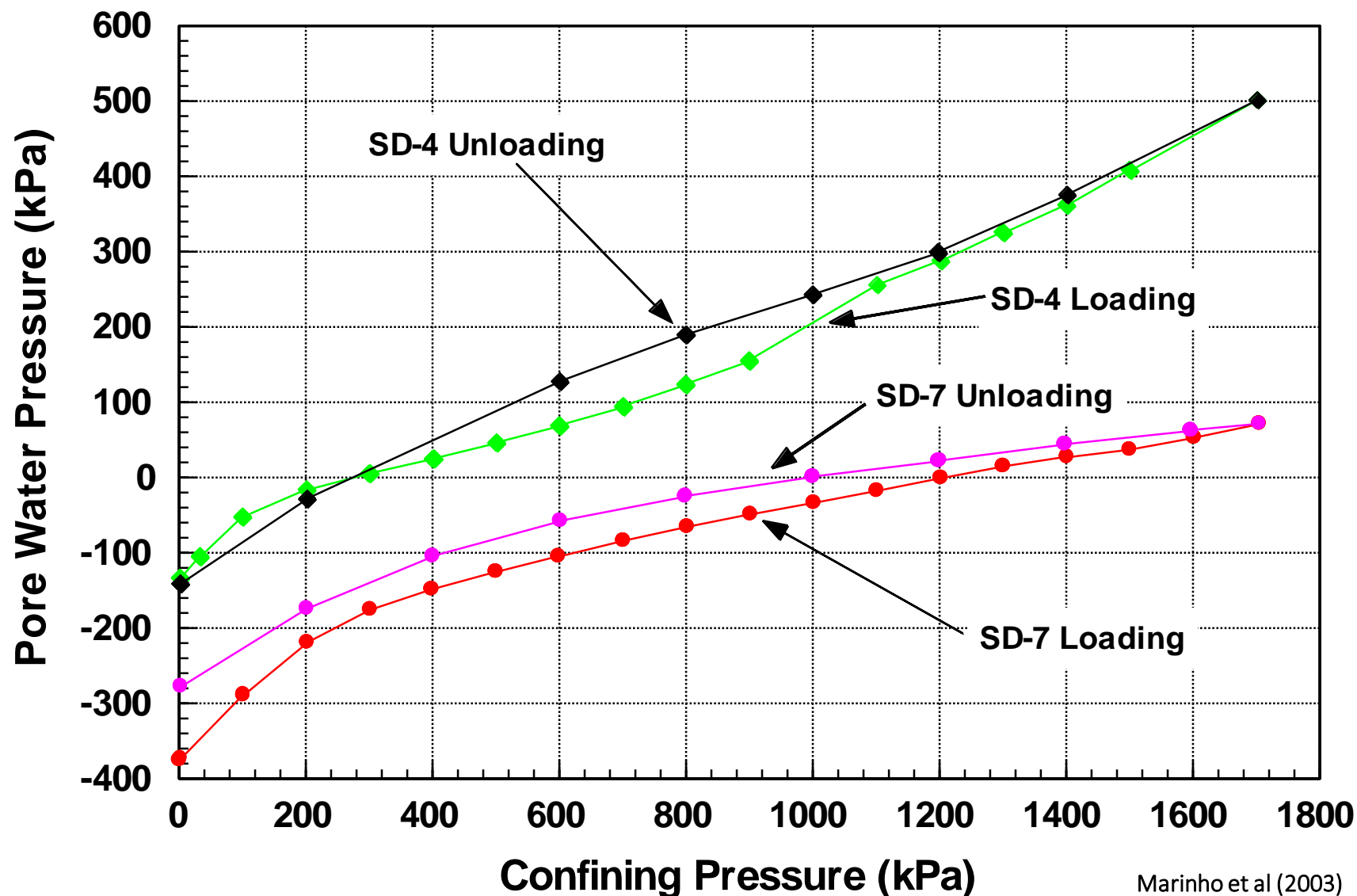


The HCT: Applications



Equilibrium time line

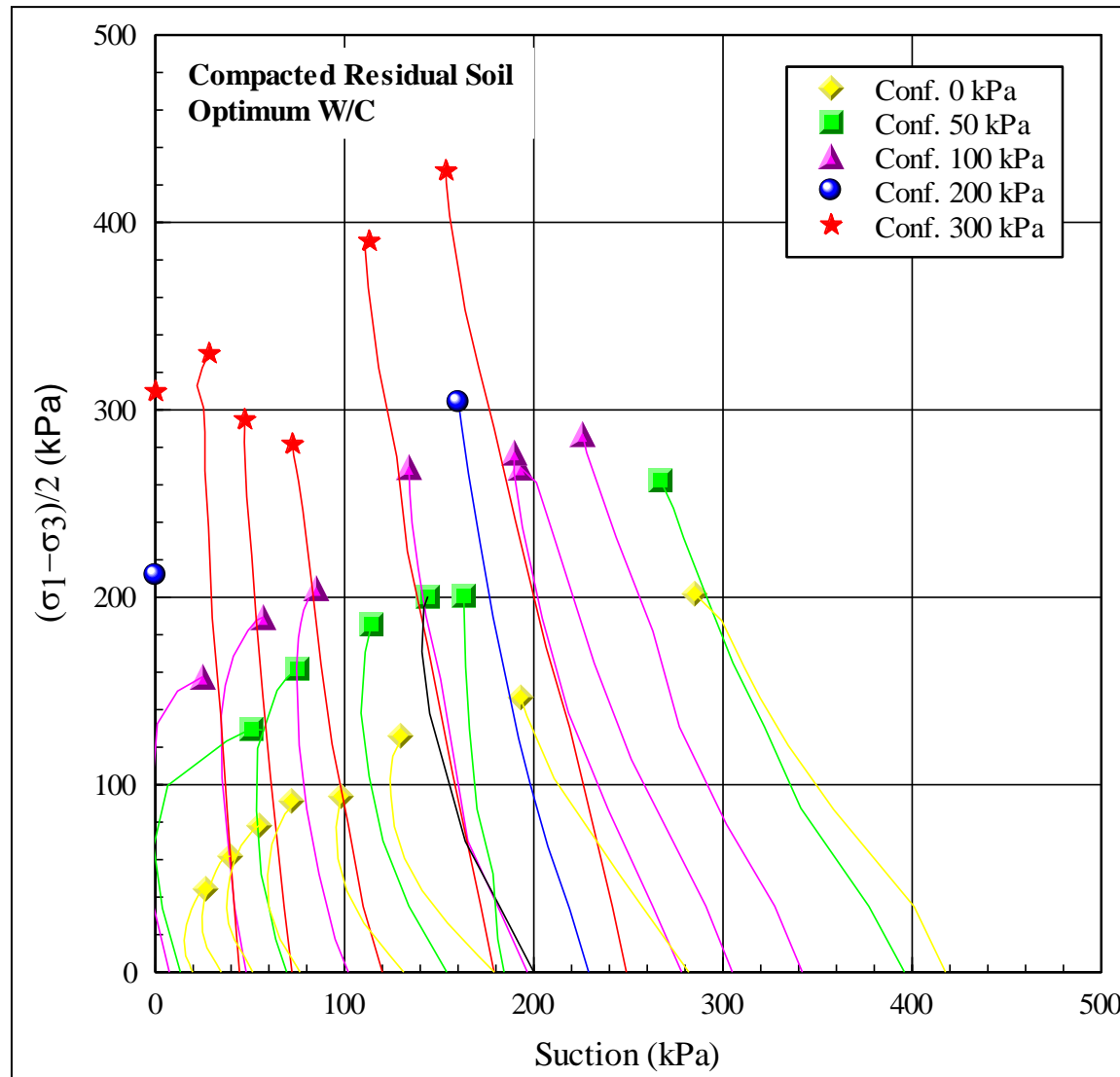
The Tensiometer: Applications



Marinho et al (2003)

The effect of loading and unloading on suction (compacted residual soil)

The HCT: Applications



Oliveira (2004)

Suction path during triaxial test on compacted residual soil

High Capacity Tensiometer

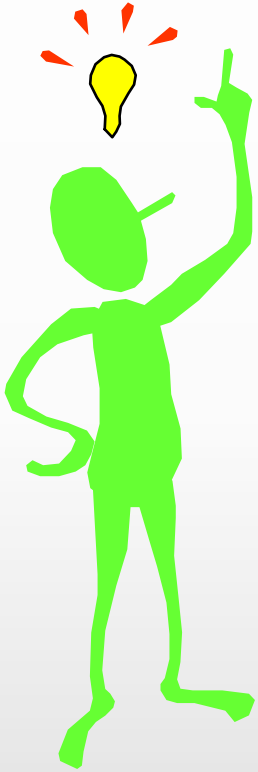
0 – 200kPa



Filter Paper Technique



The Filter Paper Technique

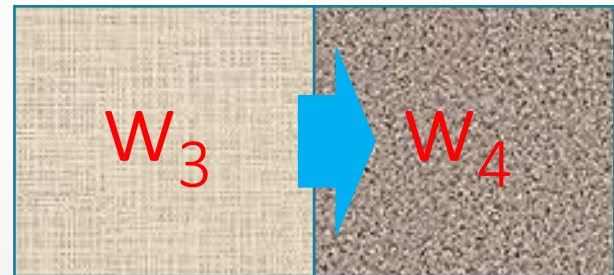


Two materials
two water contents and two suctions

Initial flow (Absorption)
Moving to equilibrium of suction

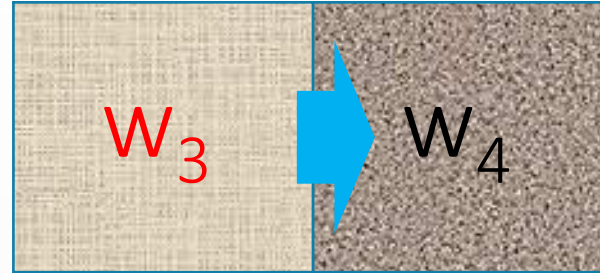
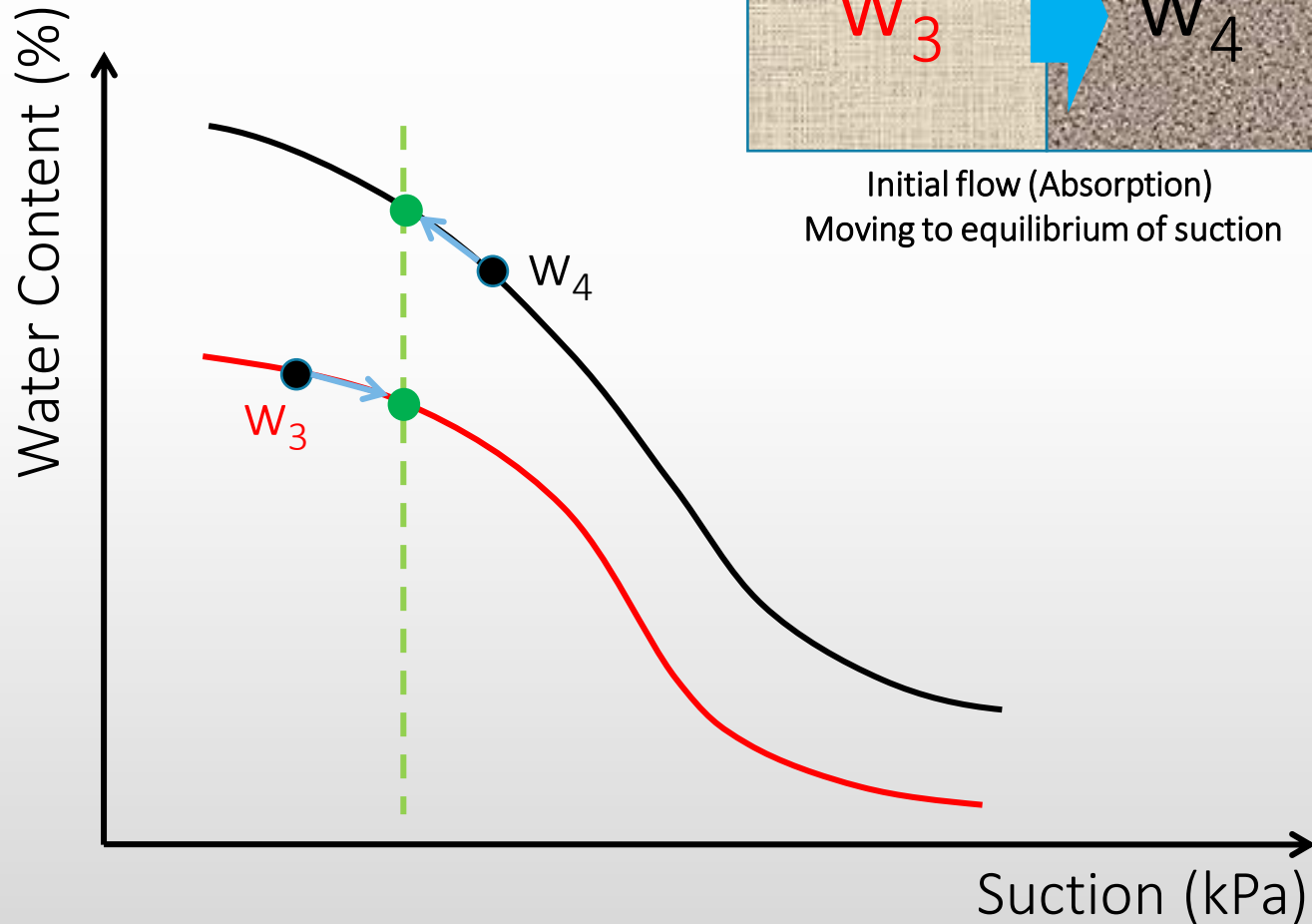
Equilibrium (no flow)
two water contents and same suction

Absortion



The Filter Paper Technique

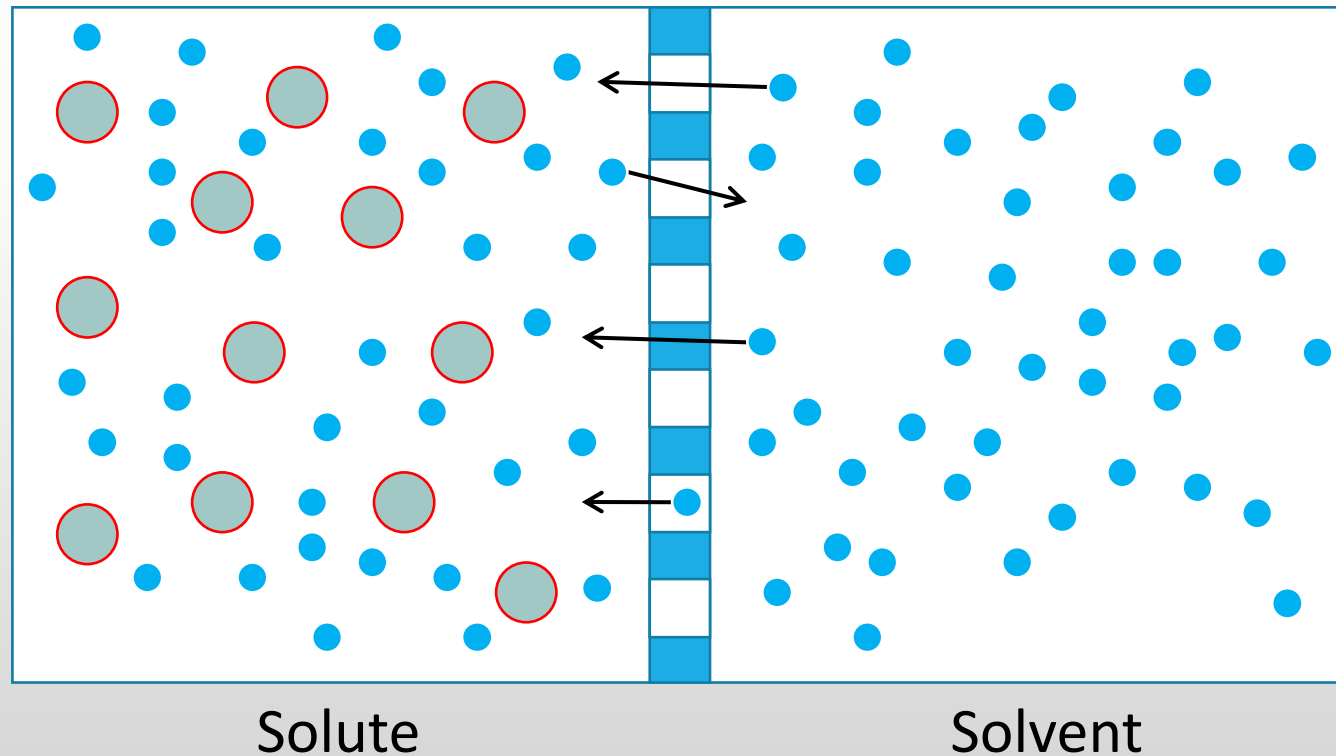
Absorption



The Filter Paper Technique

Absorption / Osmotic effect

There is a net flow of small molecules through a semi-permeable membrane. The flow is stopped if a pressure is applied against the direction of the flow. This is the osmotic pressure



The Filter Paper Technique

Absorption / Osmotic effect

Shull (1916)



Solution



Soil

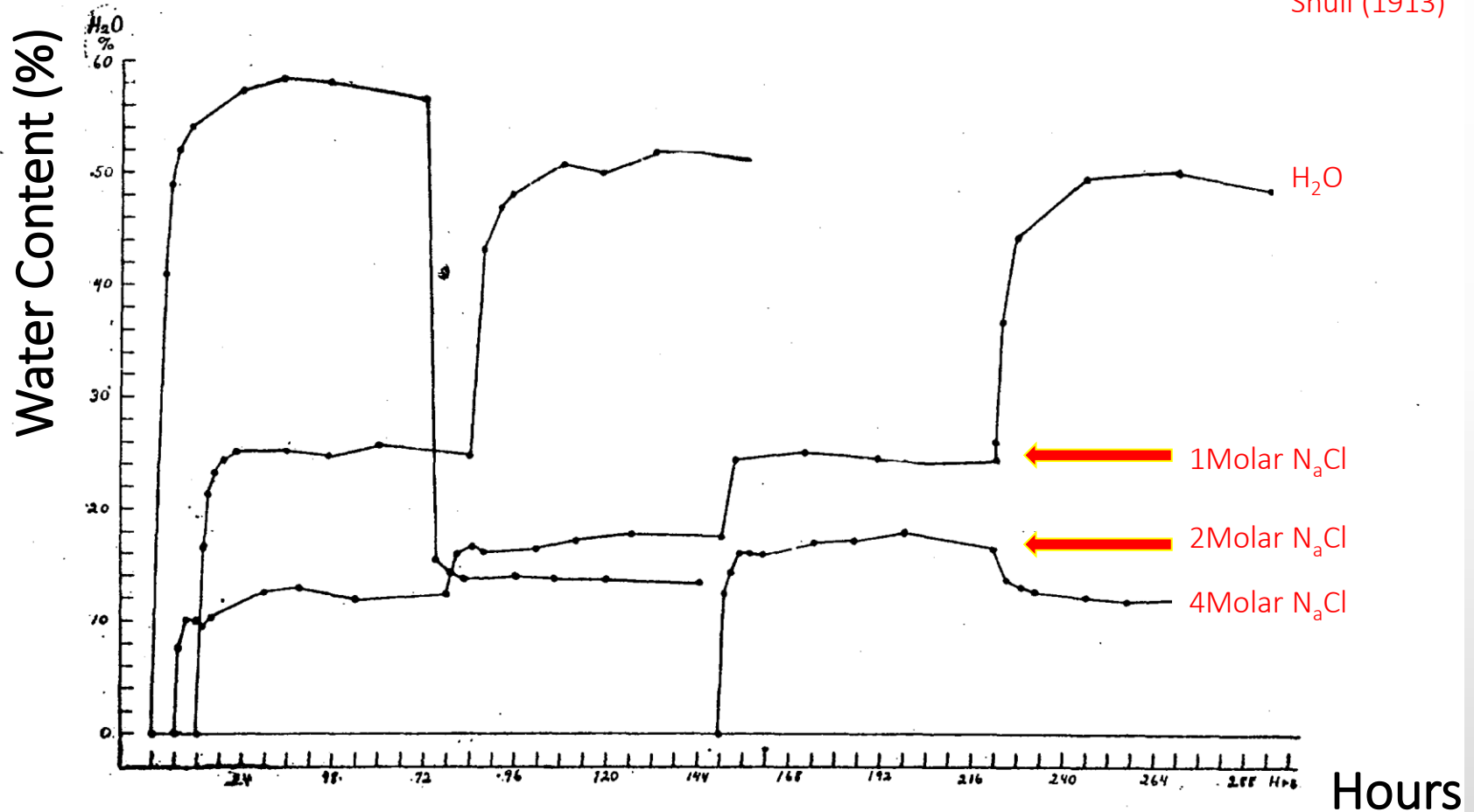


The Filter Paper Technique

Absorption / Osmotic effect

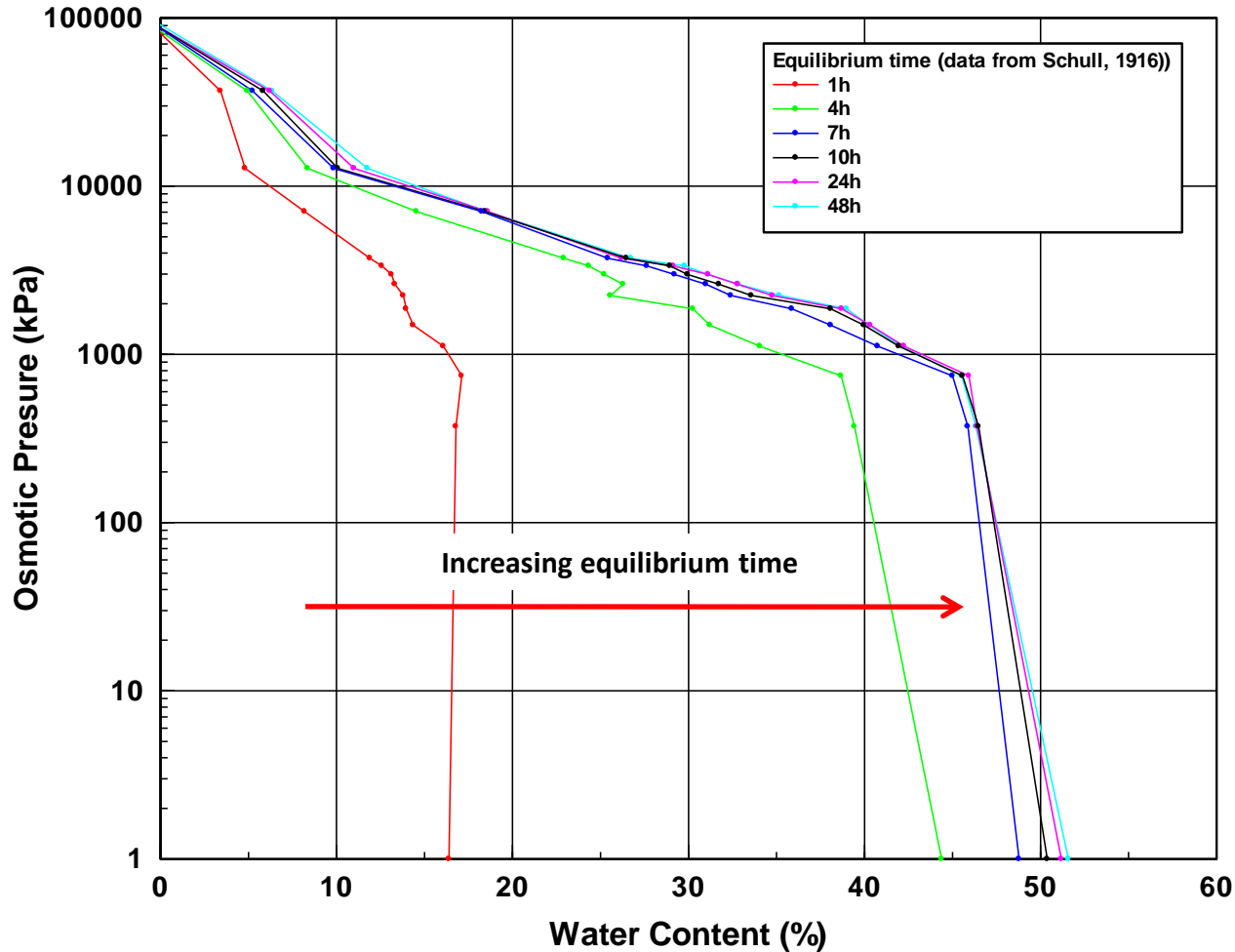
Response time of seeds placed within solutions

Shull (1913)



The Filter Paper Technique

Variation of the seeds water content with osmotic pressure for different equilibrium times

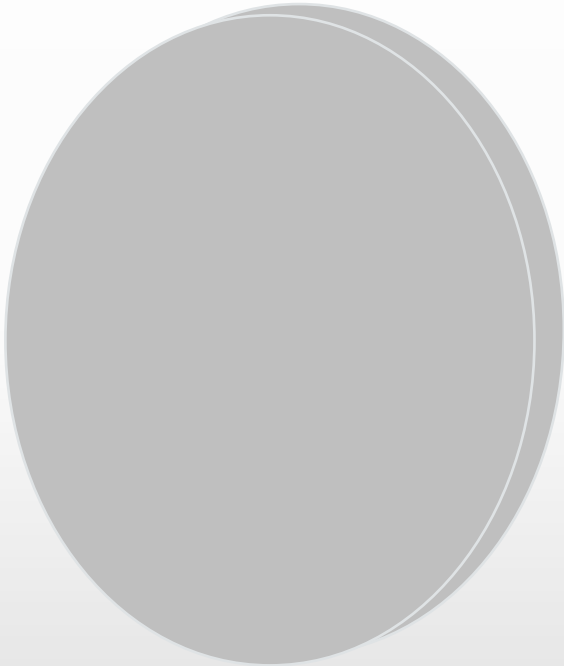


The Filter Paper Technique



The Filter Paper Technique

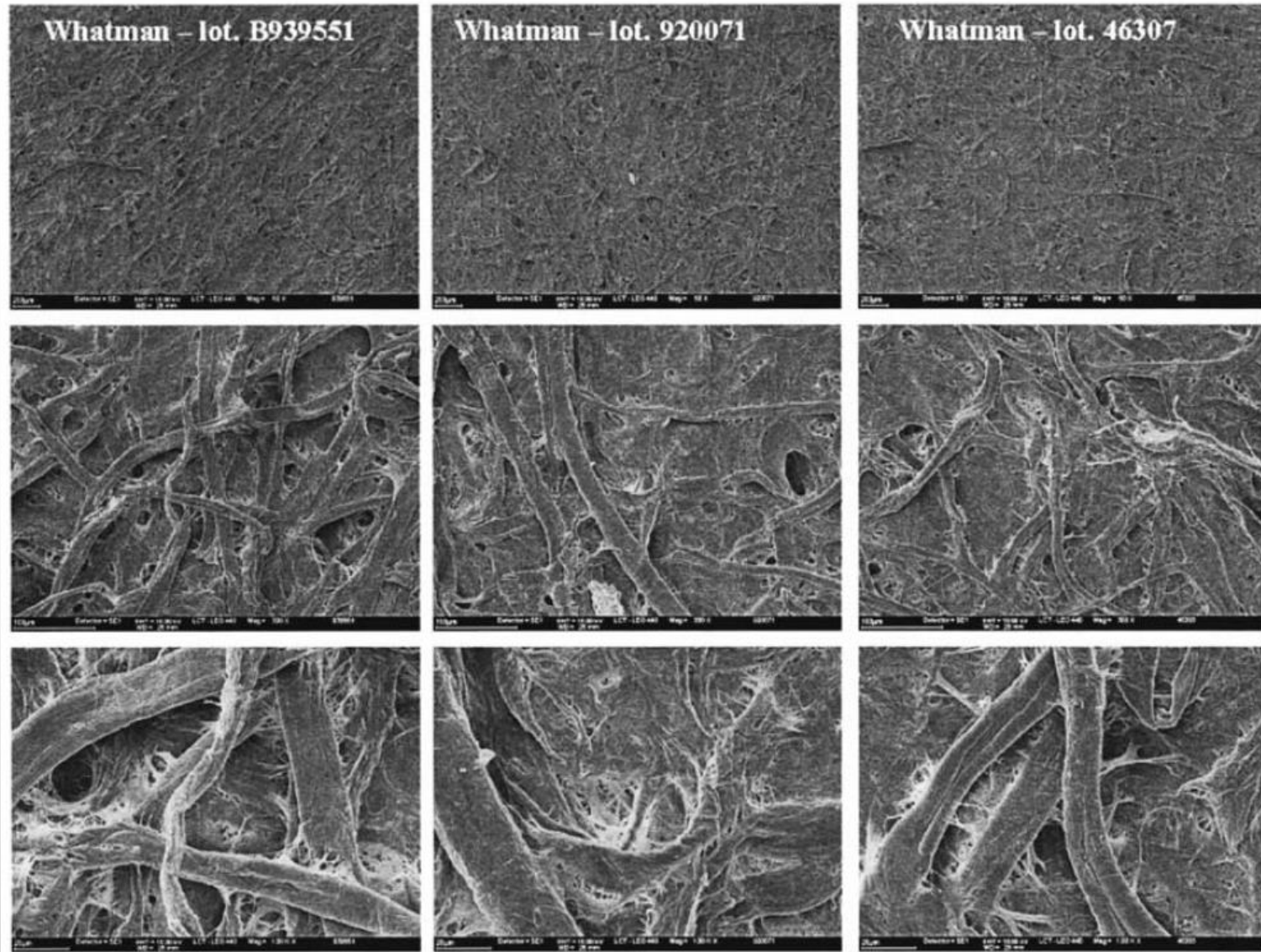
Quantitative filter paper



Ordinary paper

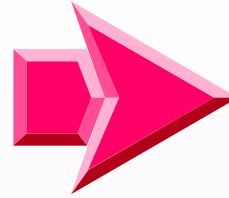


The Filter Paper

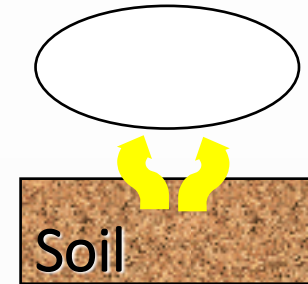


The Filter Paper Technique

Total Suction

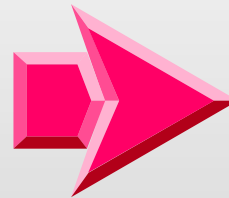


Vapour flow

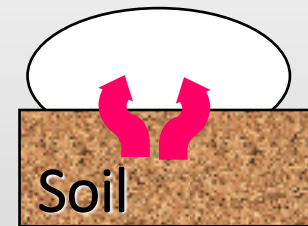


or

Matrix Suction

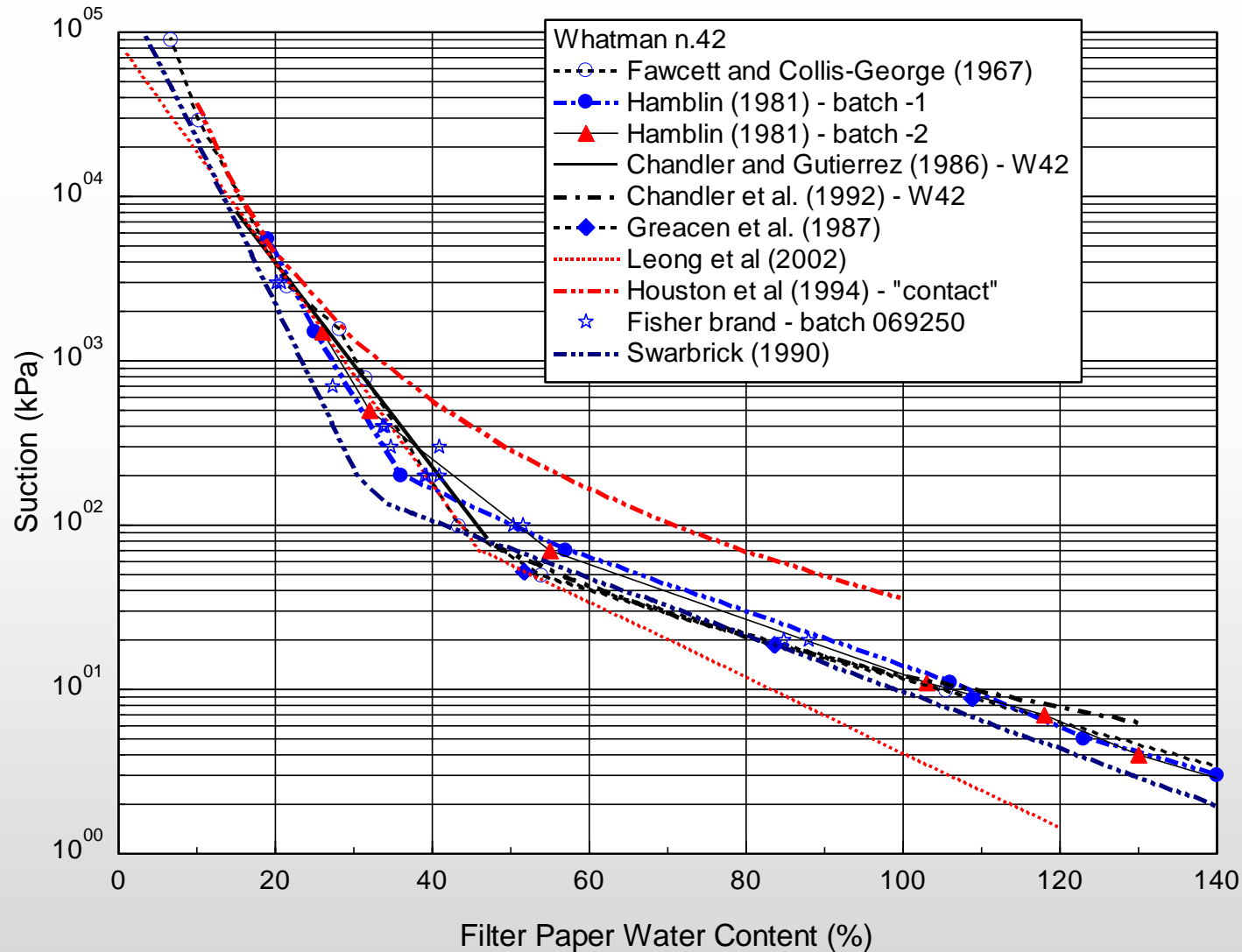


Capillary flow

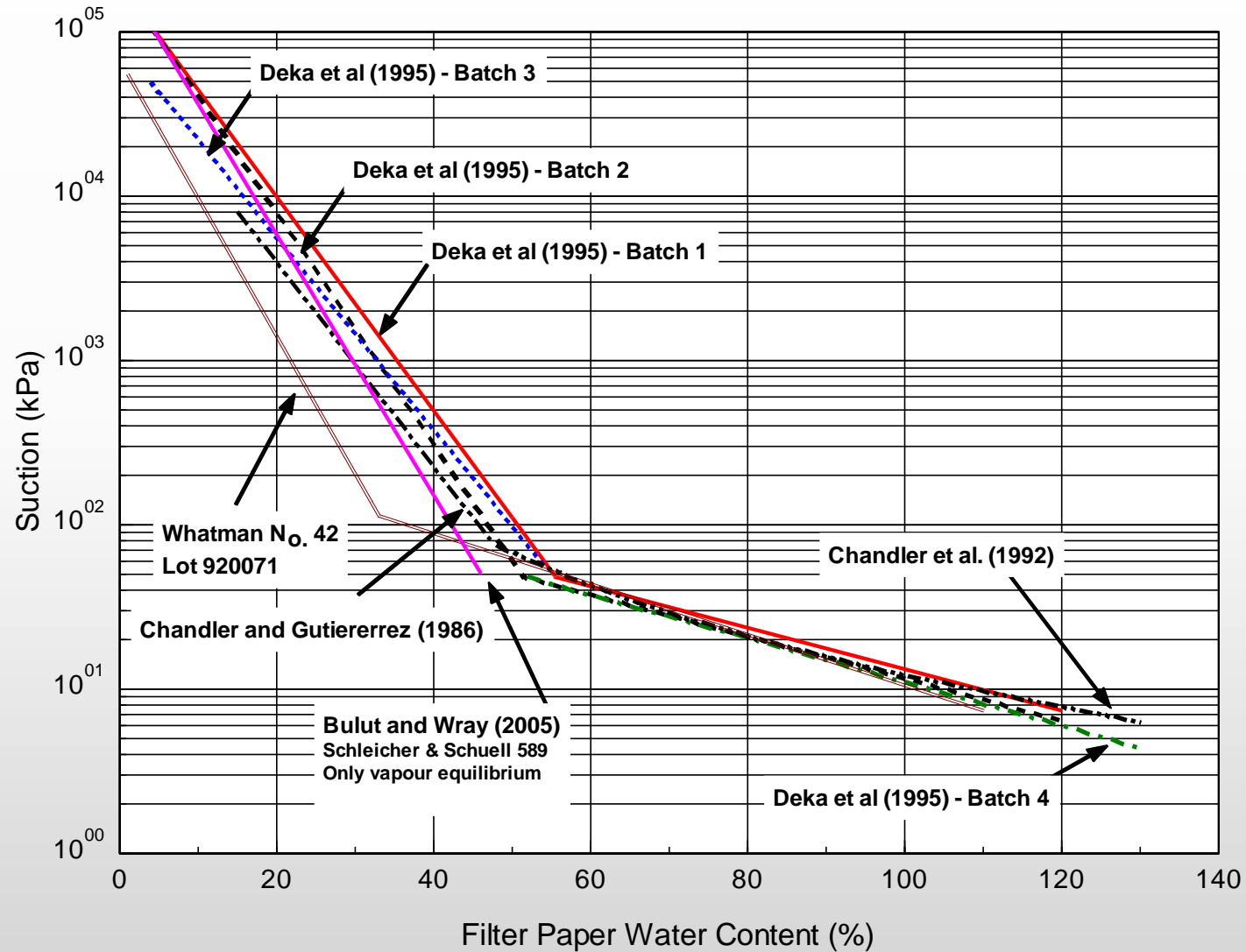


The Filter Paper Technique

Calibration Curve



Calibration Curve



The Filter Paper Technique

Calibration Curve

Chandler and Gutierrez (1986)

Chandler et al.(1992)

For filter paper $w/c > 47\%$

$$Suction(kPa) = 10^{(6.05 - 2.48 \log w)}$$

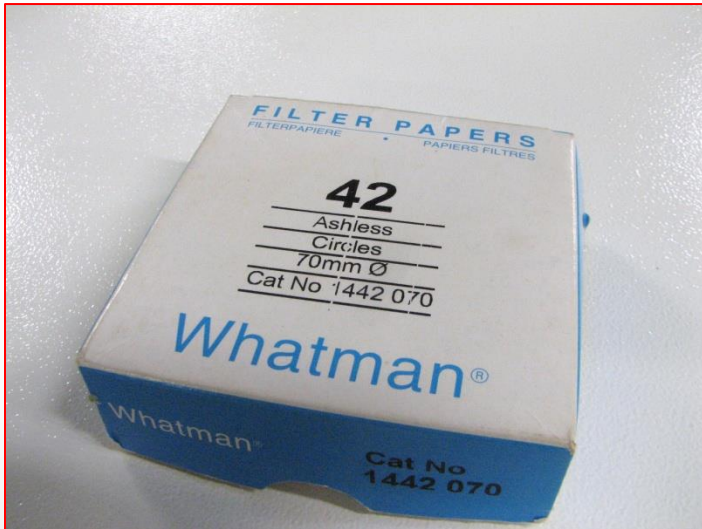
For filter paper $w/c \leq 47\%$

$$Suction(kPa) = 10^{(4.84 - 0.0622 w)}$$

The Filter Paper Technique

Procedure

Filter paper at “natural” water content



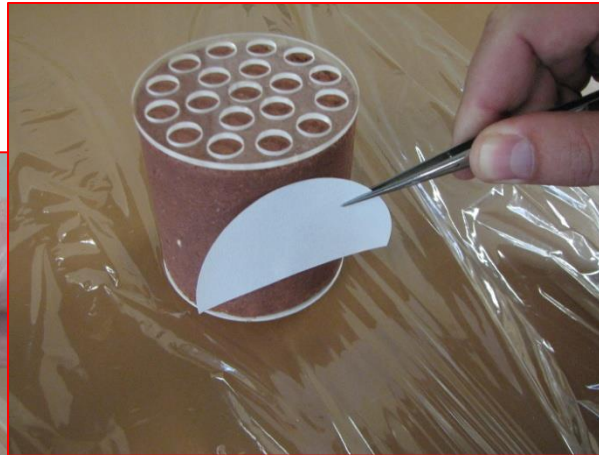
Twizers to manipulate the filter paper



The Filter Paper Technique

Procedure

Filter paper placed in contact with the soil



Filter paper placed without contact with the soil



Perforate disk used for total suction measurement



The Filter Paper Technique

Procedure

Wrapping (firmly) the sample using cling film



Wrapping the sample using aluminium foil



Placing the samples within the isolated box.



The Filter Paper Technique

Procedure

Removing the filter paper after equilibration time is reached



Placing the F.P inside the zip lock plastic bag



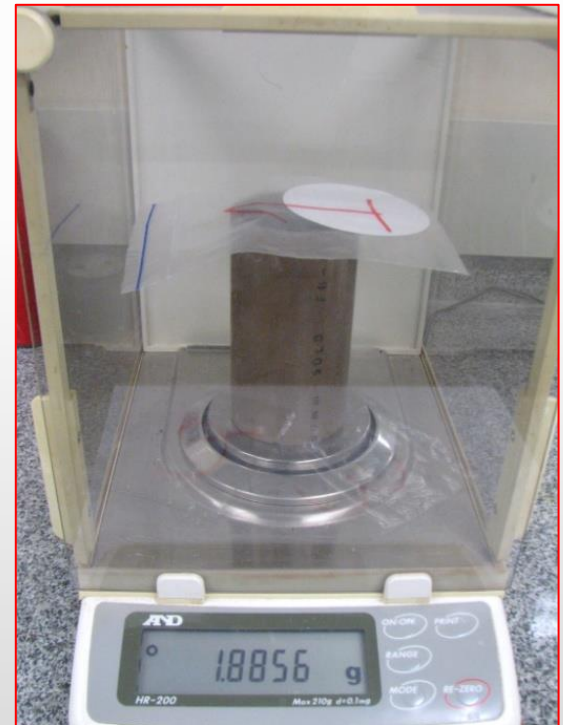
The Filter Paper Technique

Procedure

Weighting the plastic bag without filter paper



Weighting the filter paper within the plastic bag

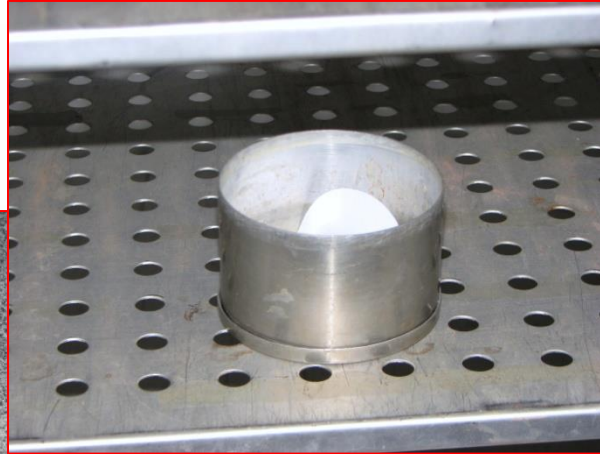


Tube used to avoid static effect from the plastic in the balance

The Filter Paper Technique

Procedure

Placing the F.P in the oven at 105° C
for at least two hours



Removing the filter paper from
the oven



The Filter Paper Technique

Procedure



The Filter Paper Technique

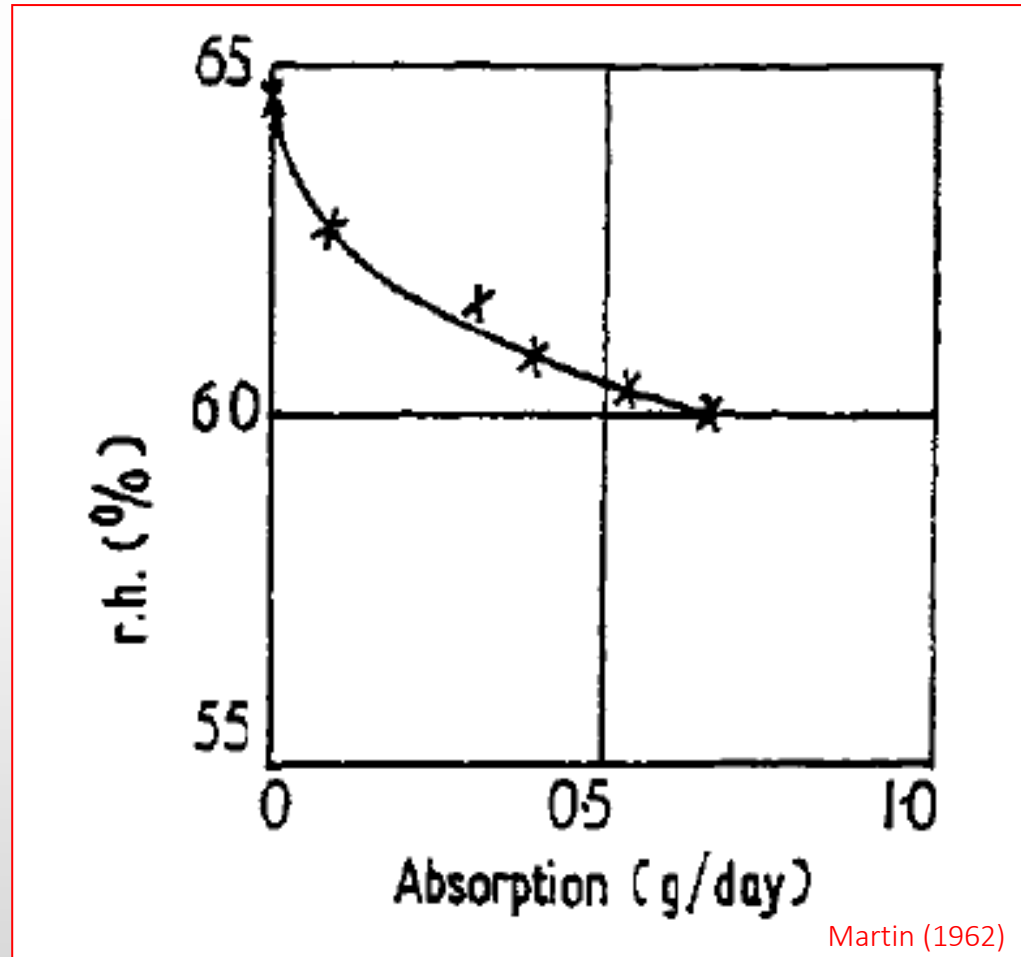
Why There is Only One Calibration Curve
for Matrix and Total Suction



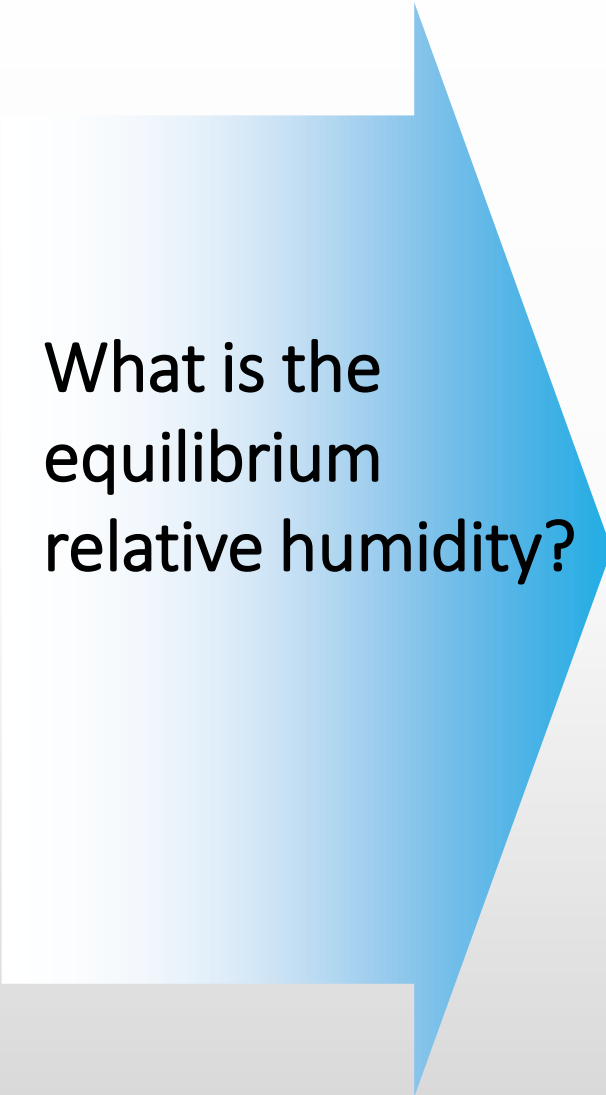
The Filter Paper Technique

One Calibration Curve

Effect of the presence of an absorbent material on the relative humidity



The Filter Paper Technique



What is the equilibrium relative humidity?

The equilibrium concept

It is the relative humidity when the movement of moisture from a material to the environment (and vice versa) have equalized.

This Equilibrium Relative Humidity balance is achieved when vapor pressures (within the material and the environment) have equalized.

At this point the moisture level of a material can be expressed in terms of equilibrium relative humidity.

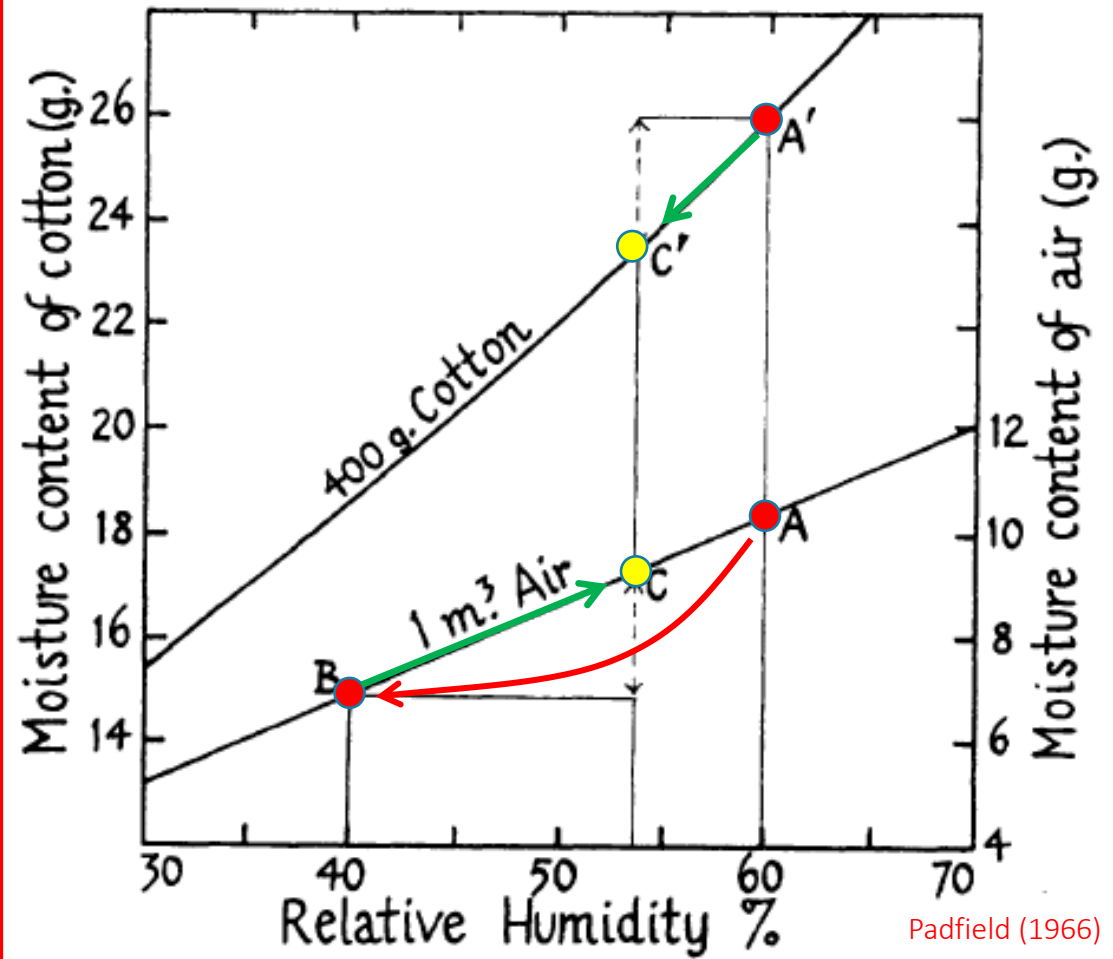
At equilibrium the free energy of all components of the system are the same.

The Filter Paper Technique

The equilibrium concept



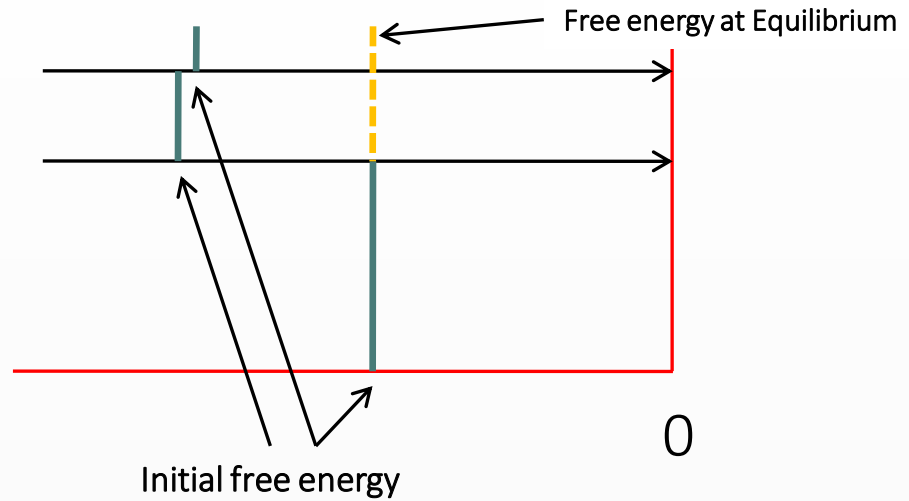
Museums showcase



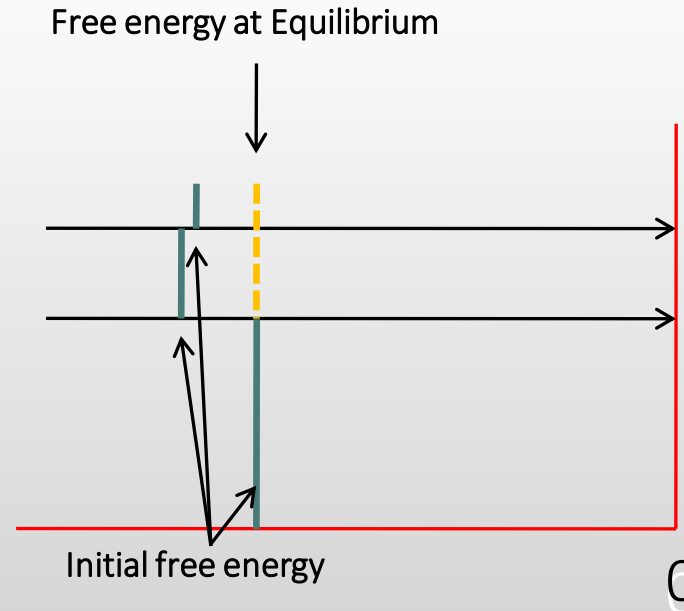
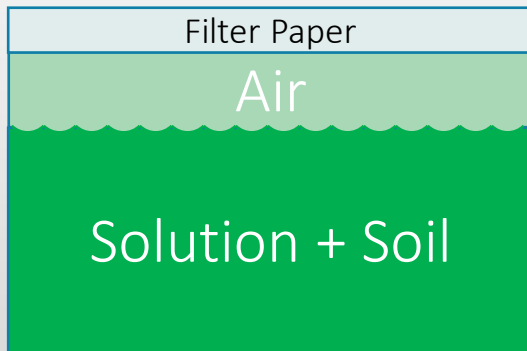
The Filter Paper Technique

The equilibrium concept

A



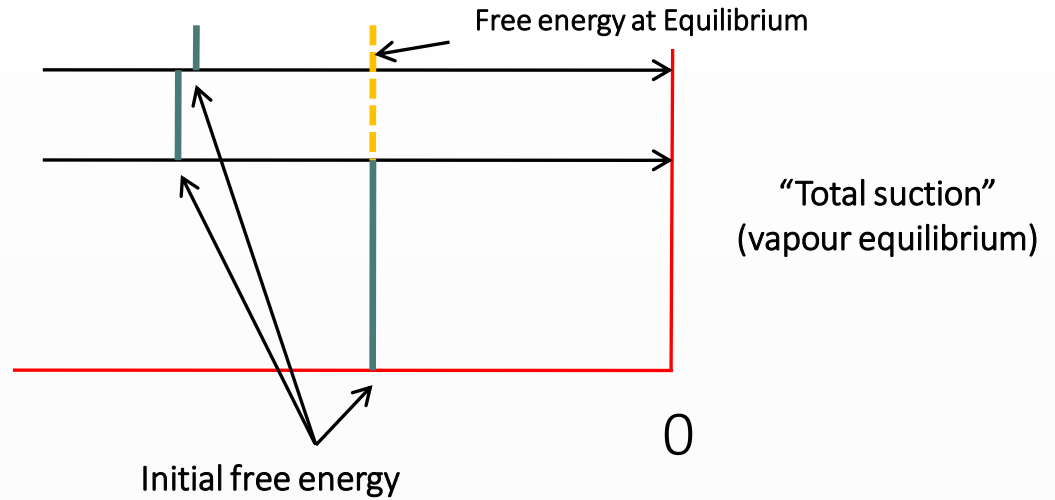
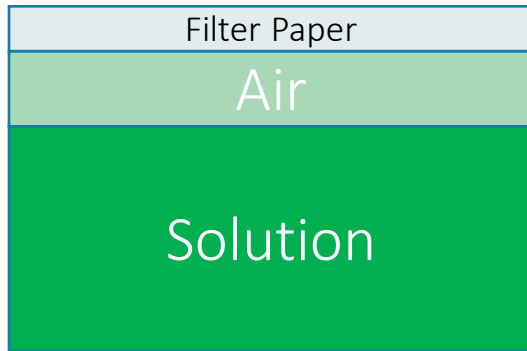
B



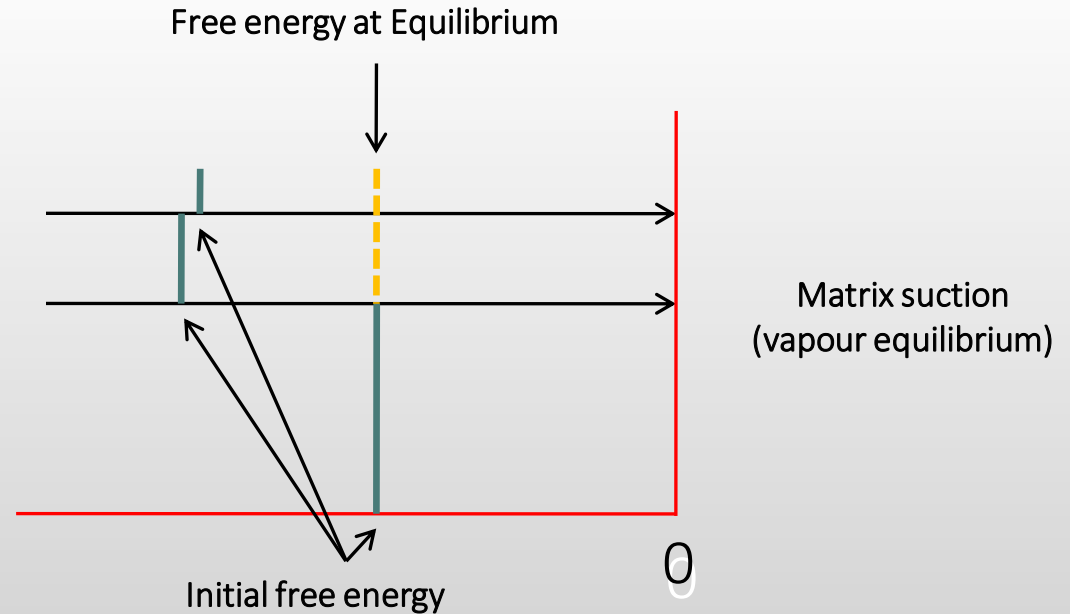
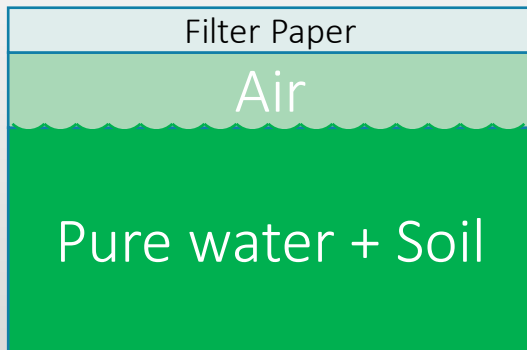
The Filter Paper Technique

The equilibrium concept

A



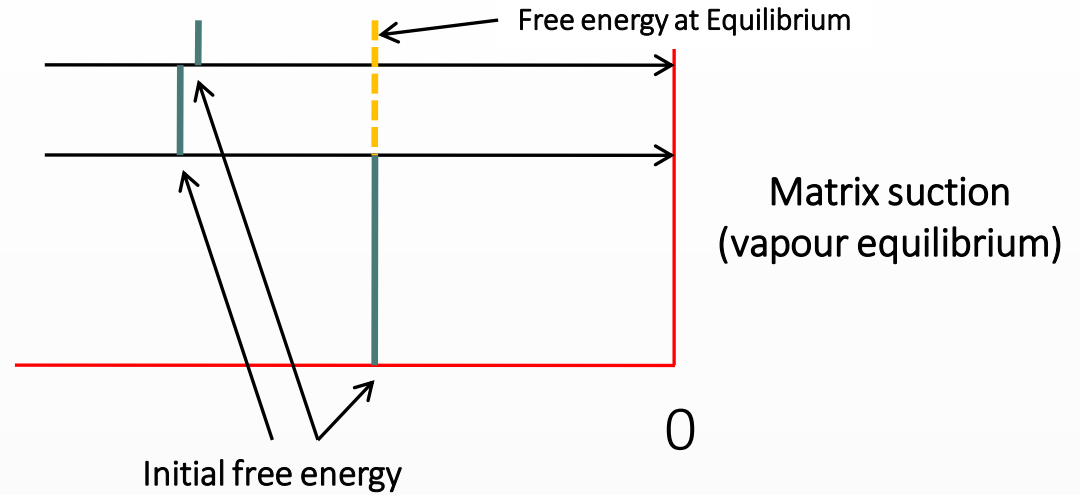
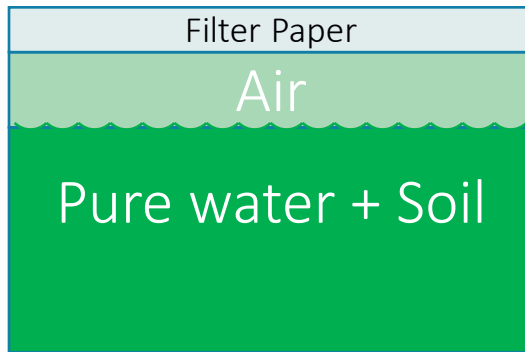
B



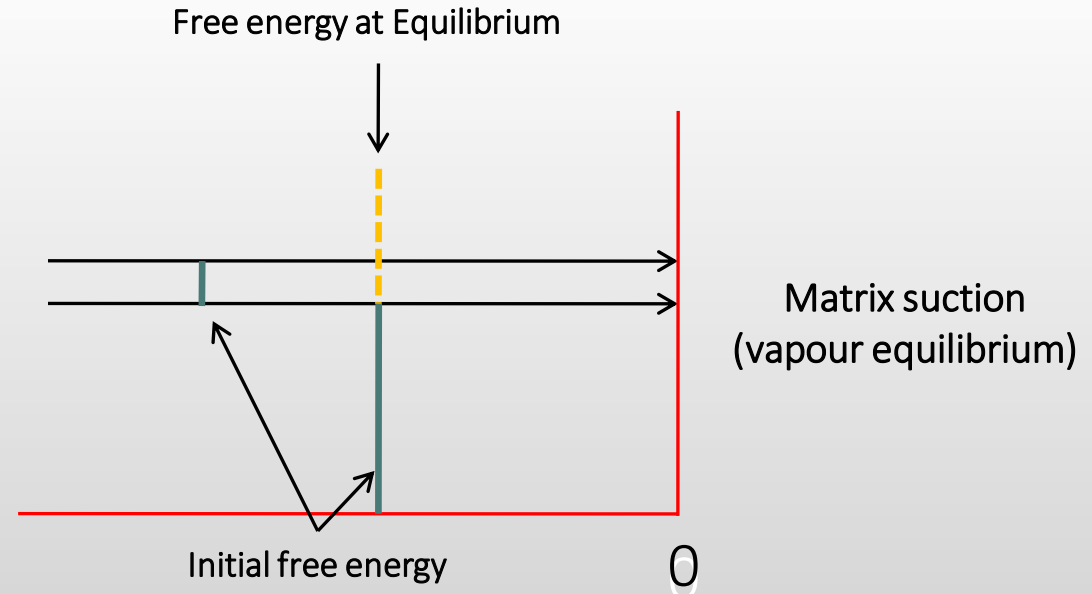
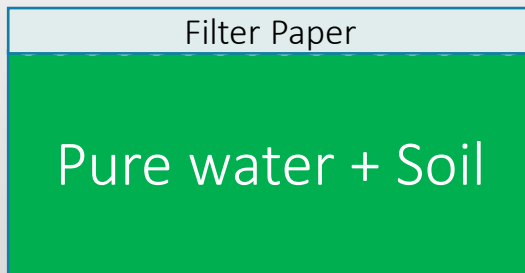
The Filter Paper Technique

The equilibrium concept

A

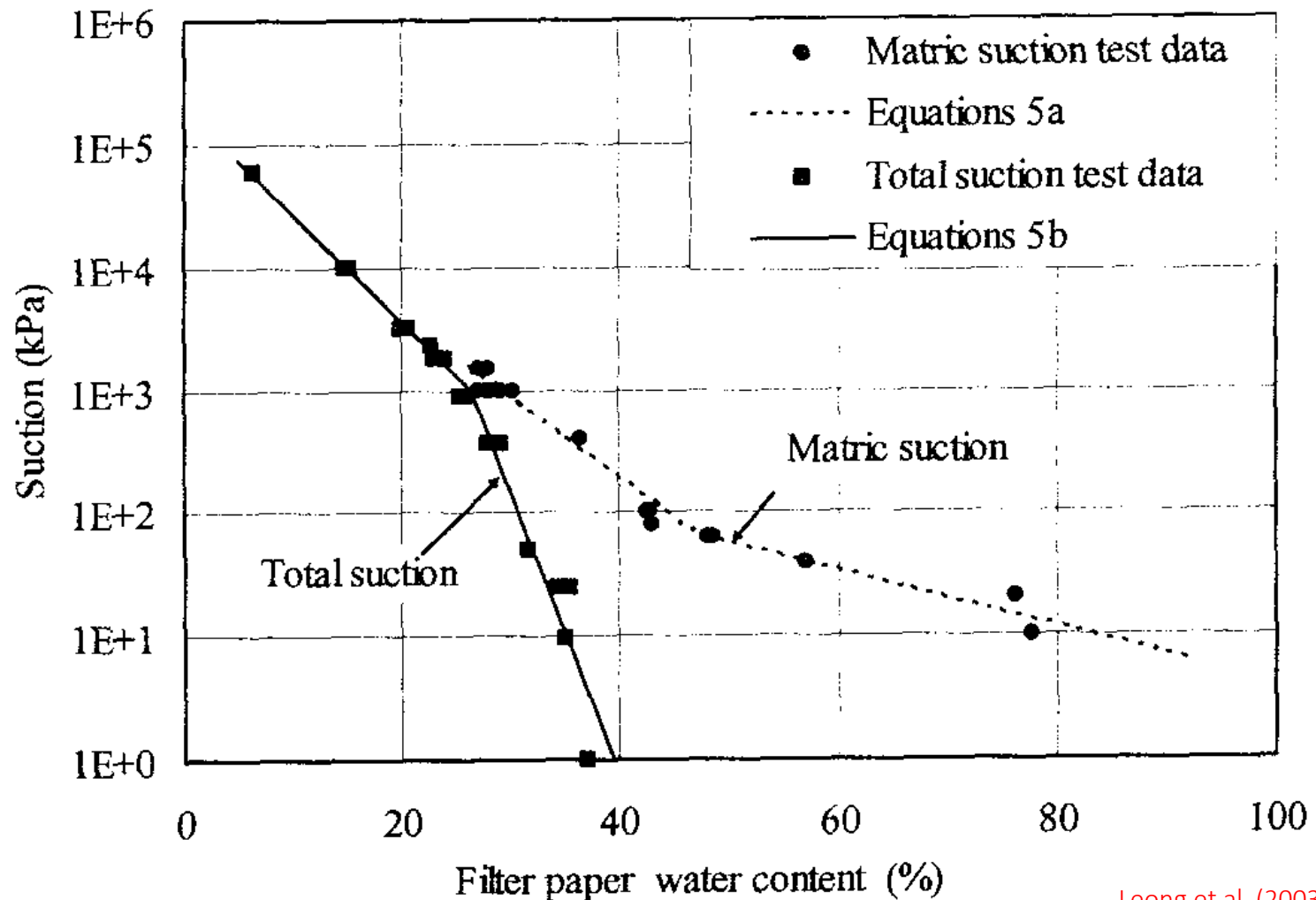


B



The Filter Paper Technique

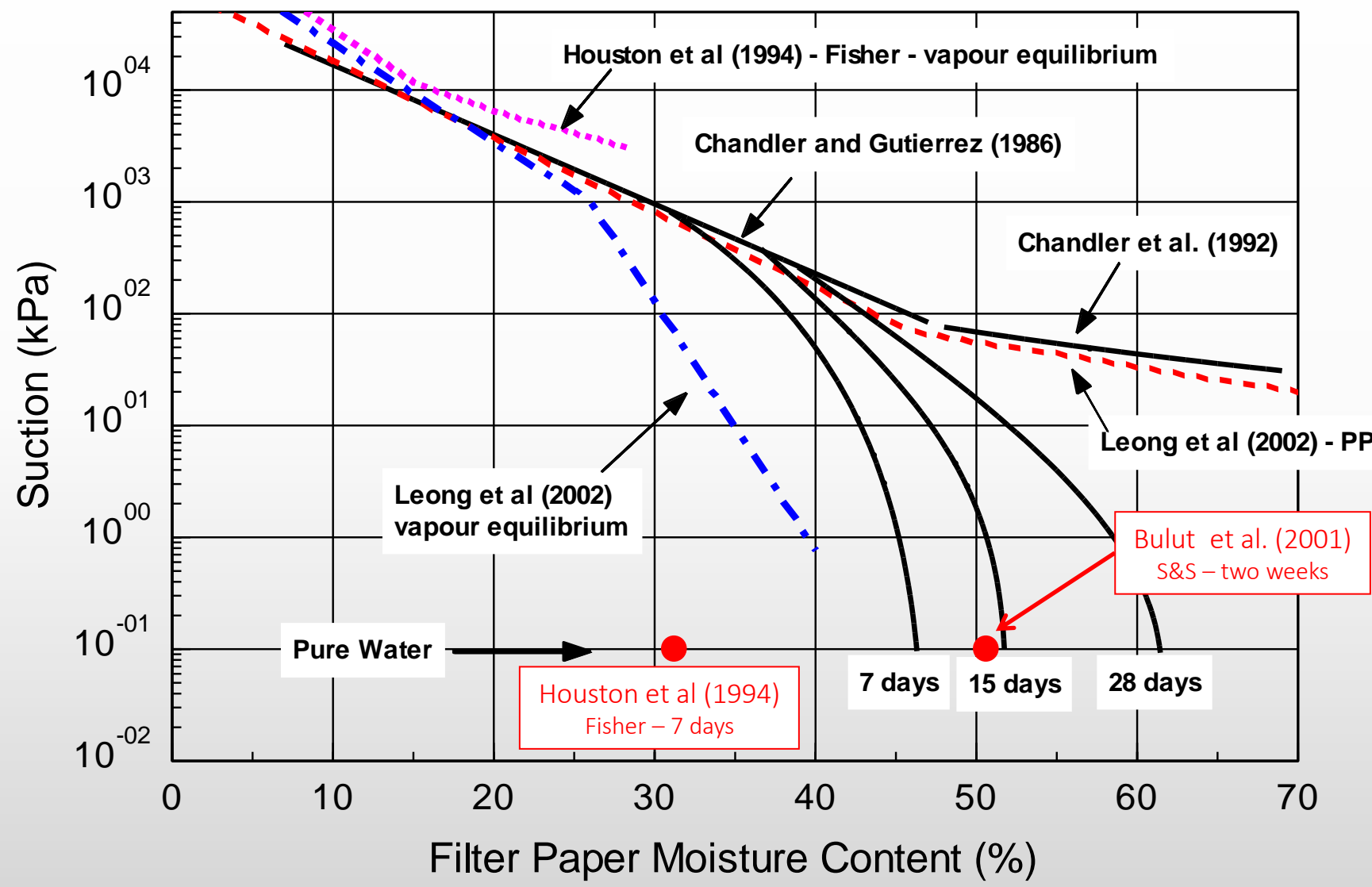
One Calibration Curve



Leong et al. (2003)

The Filter Paper Technique

One Calibration Curve



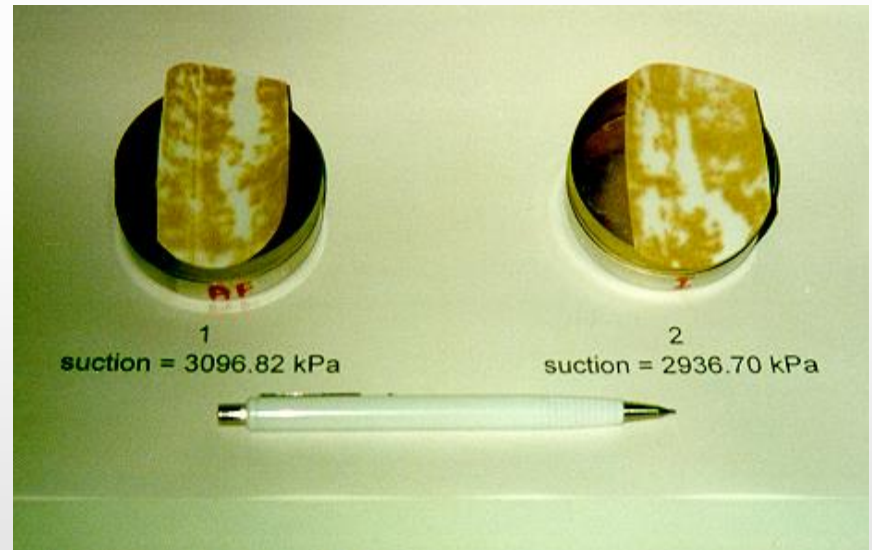
The Filter Paper Technique

The effect of contact

Shroud of Turin

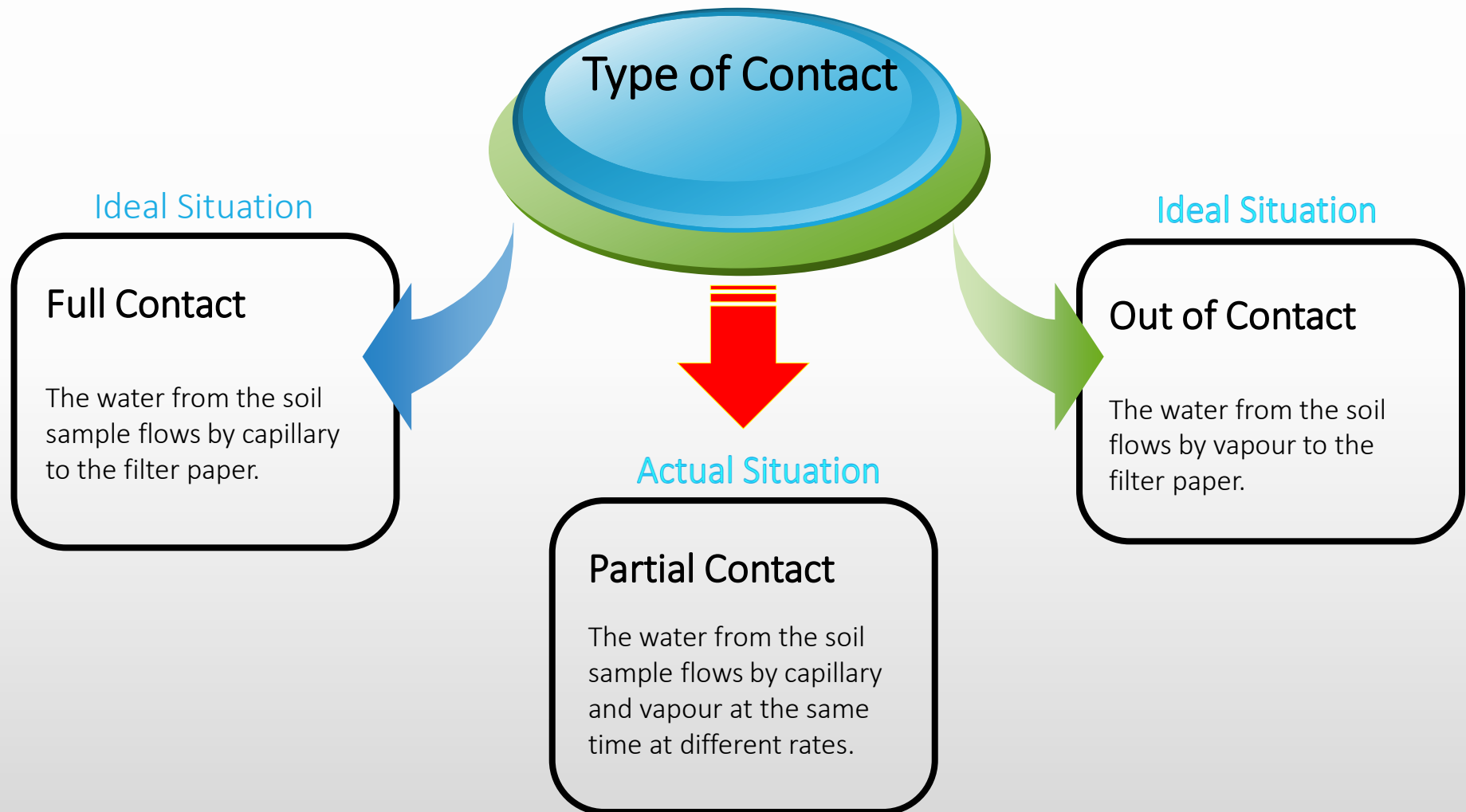


Filter Paper



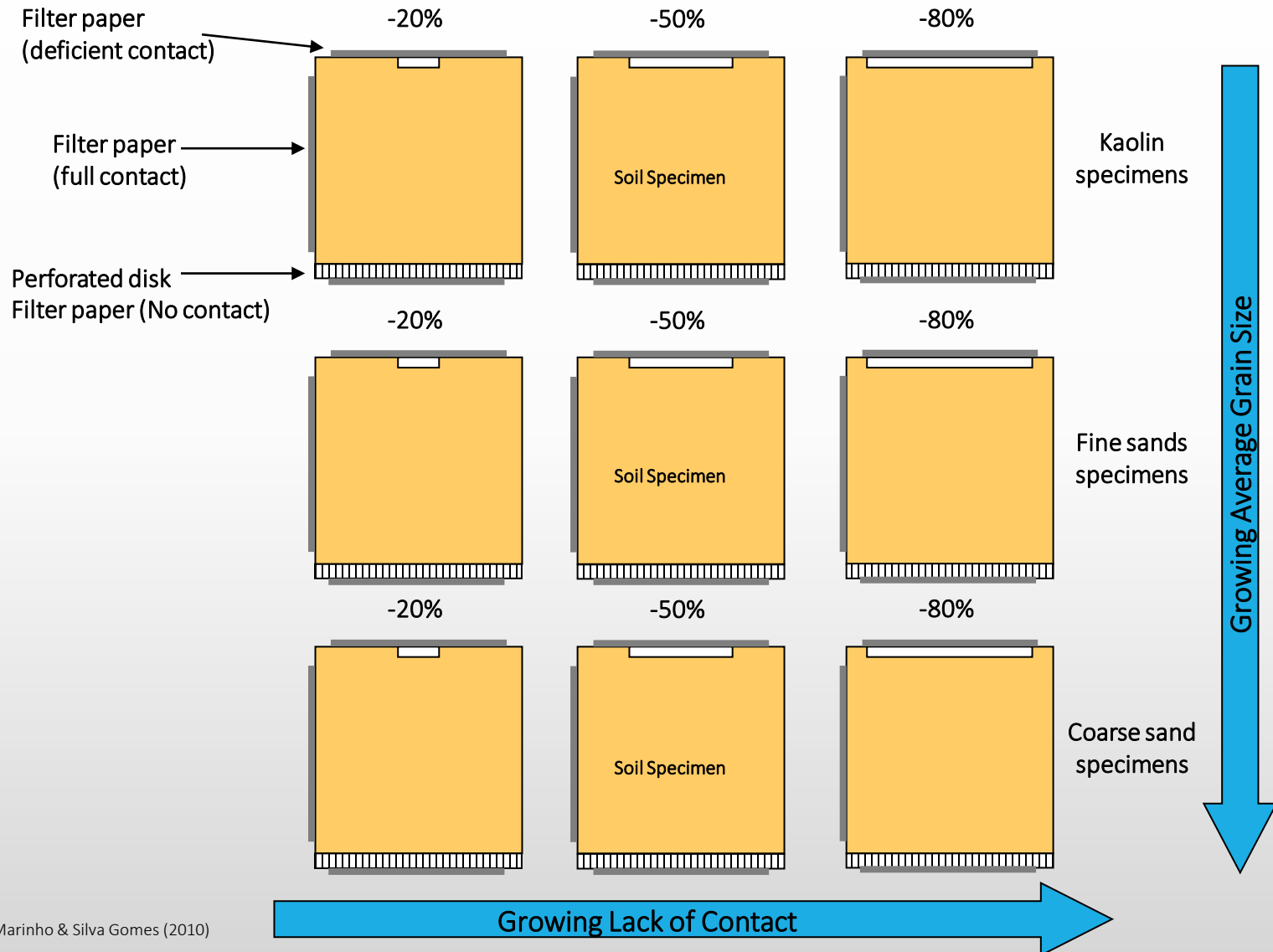
The Filter Paper Technique

The effect of contact



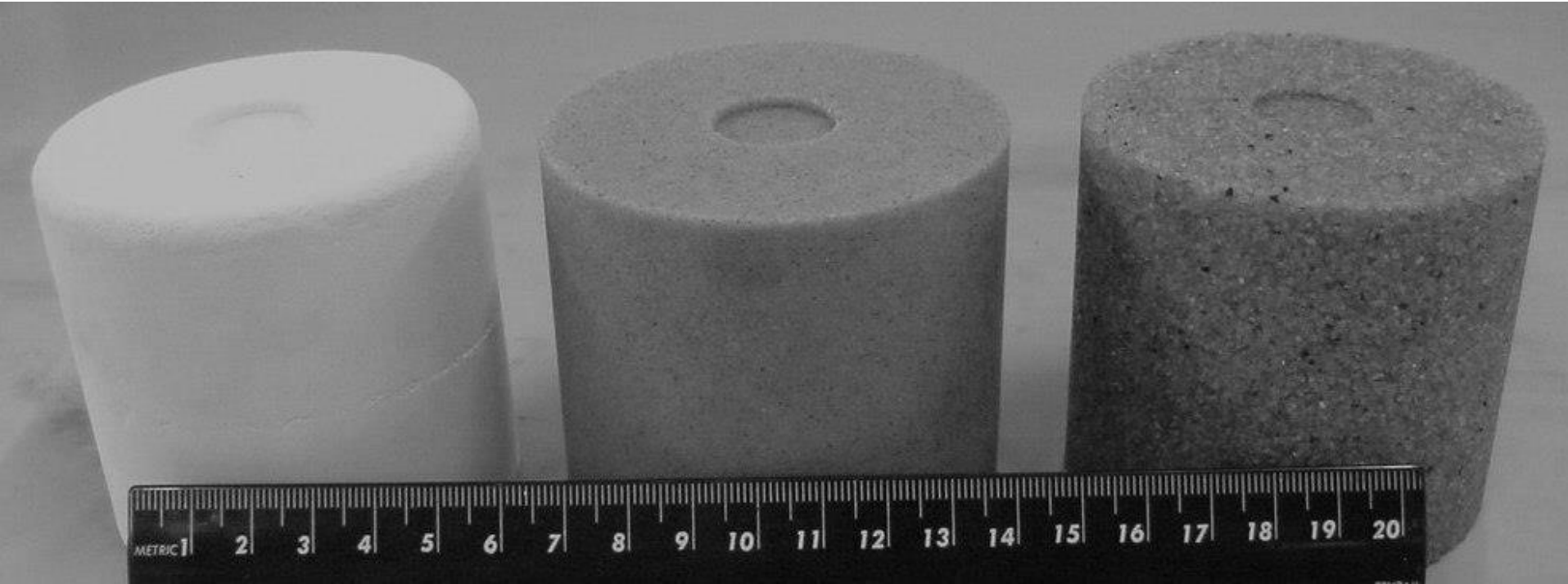
The Filter Paper Technique

The effect of contact



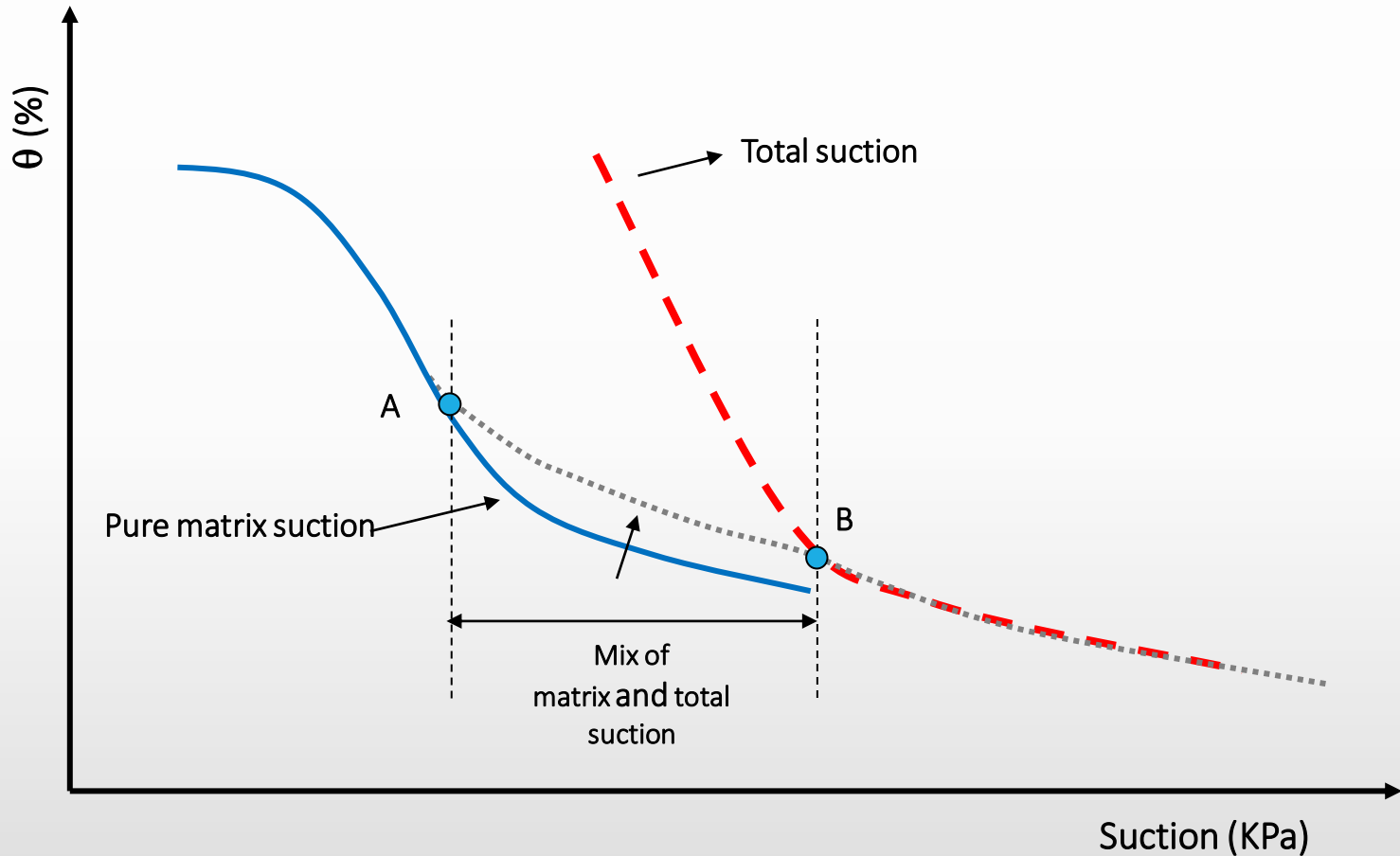
The Filter Paper Technique

The effect of contact



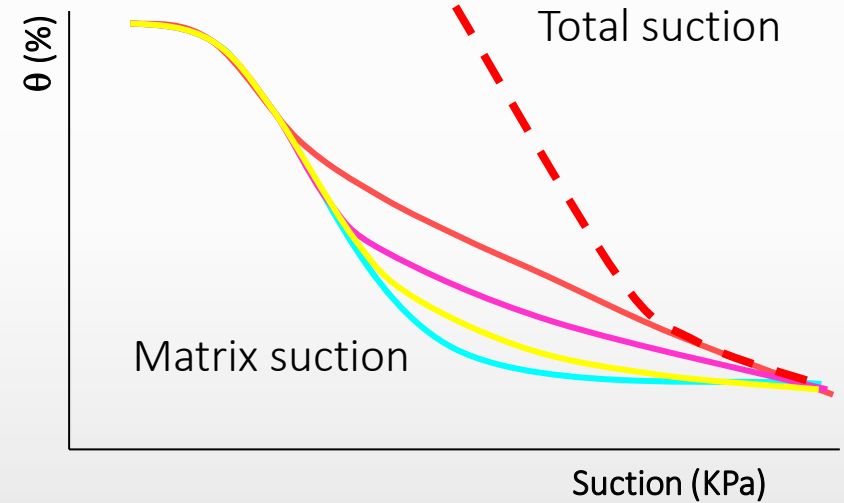
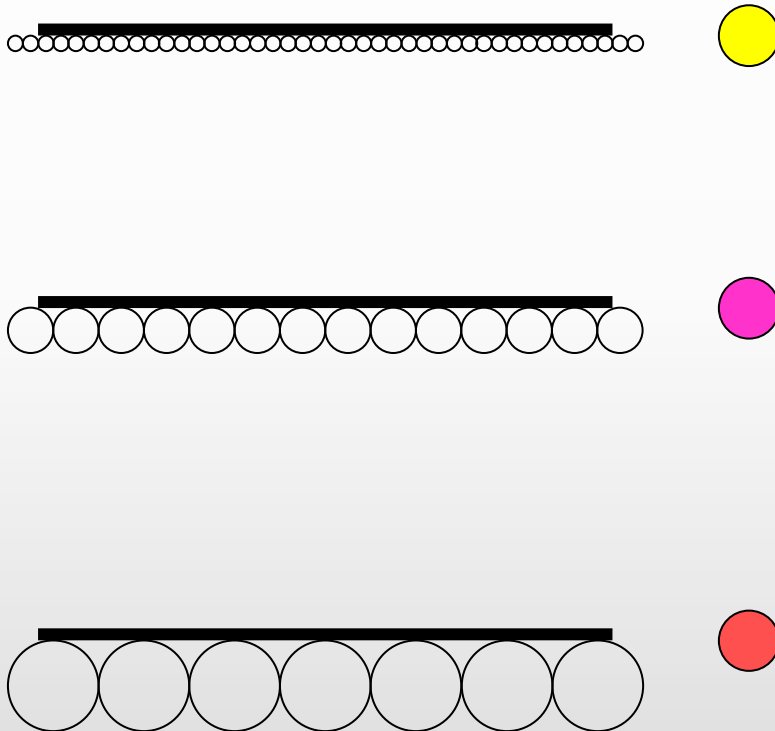
The Filter Paper Technique

The effect of contact



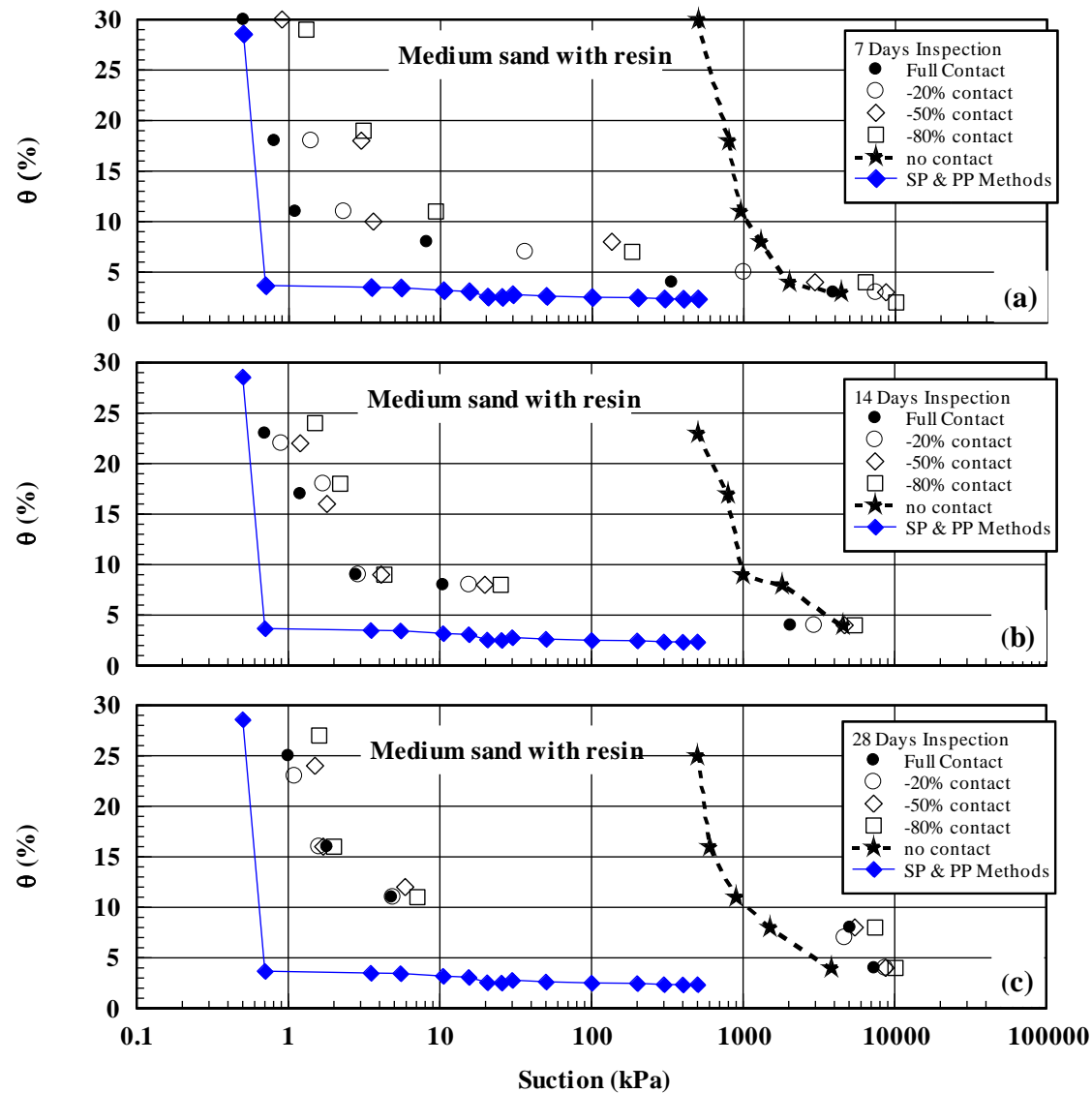
The Filter Paper Technique

The effect of contact



The Filter Paper Technique

The effect of contact



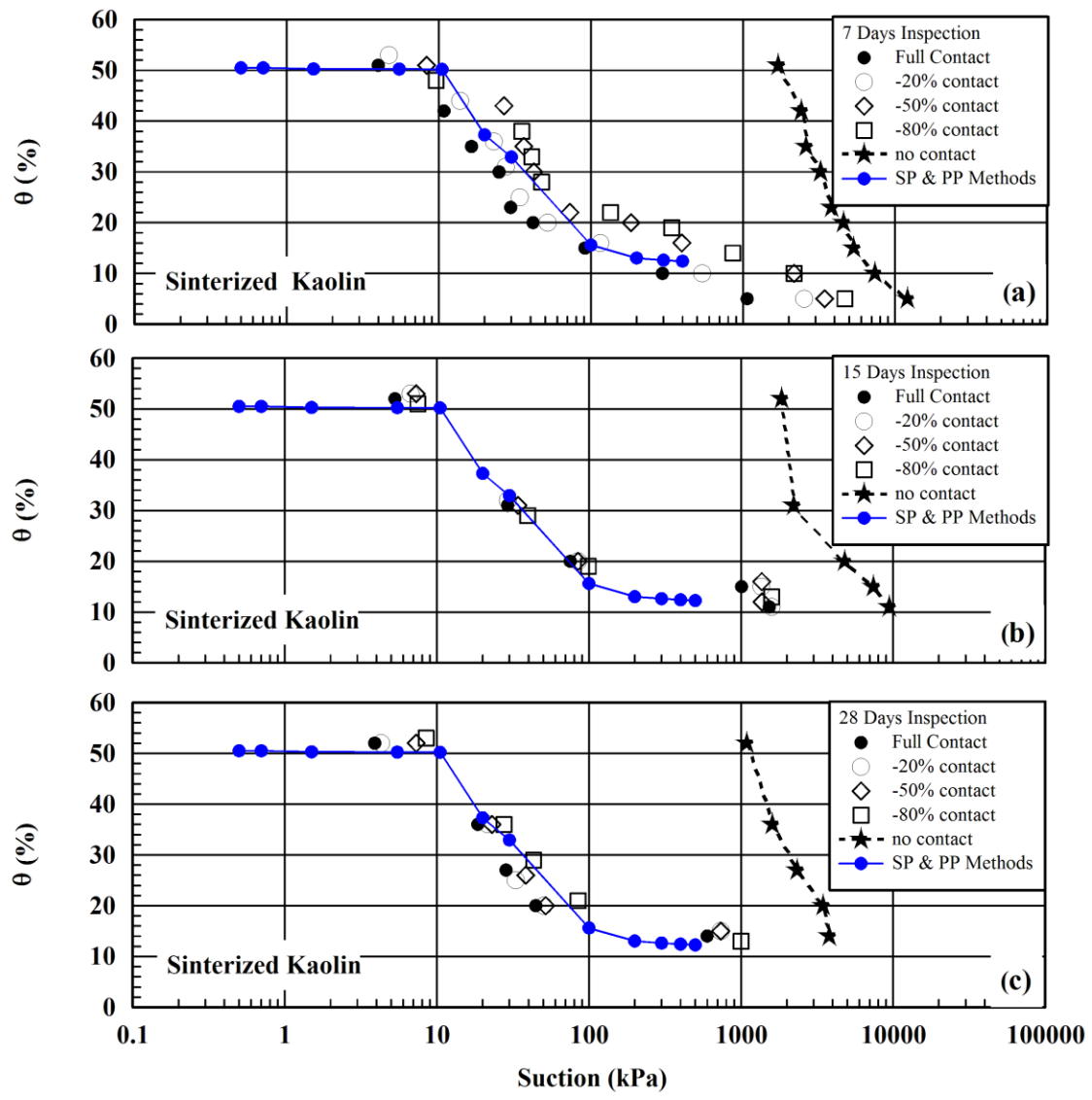
7 Days

14 Days

28 Days

The Filter Paper Technique

The effect of contact



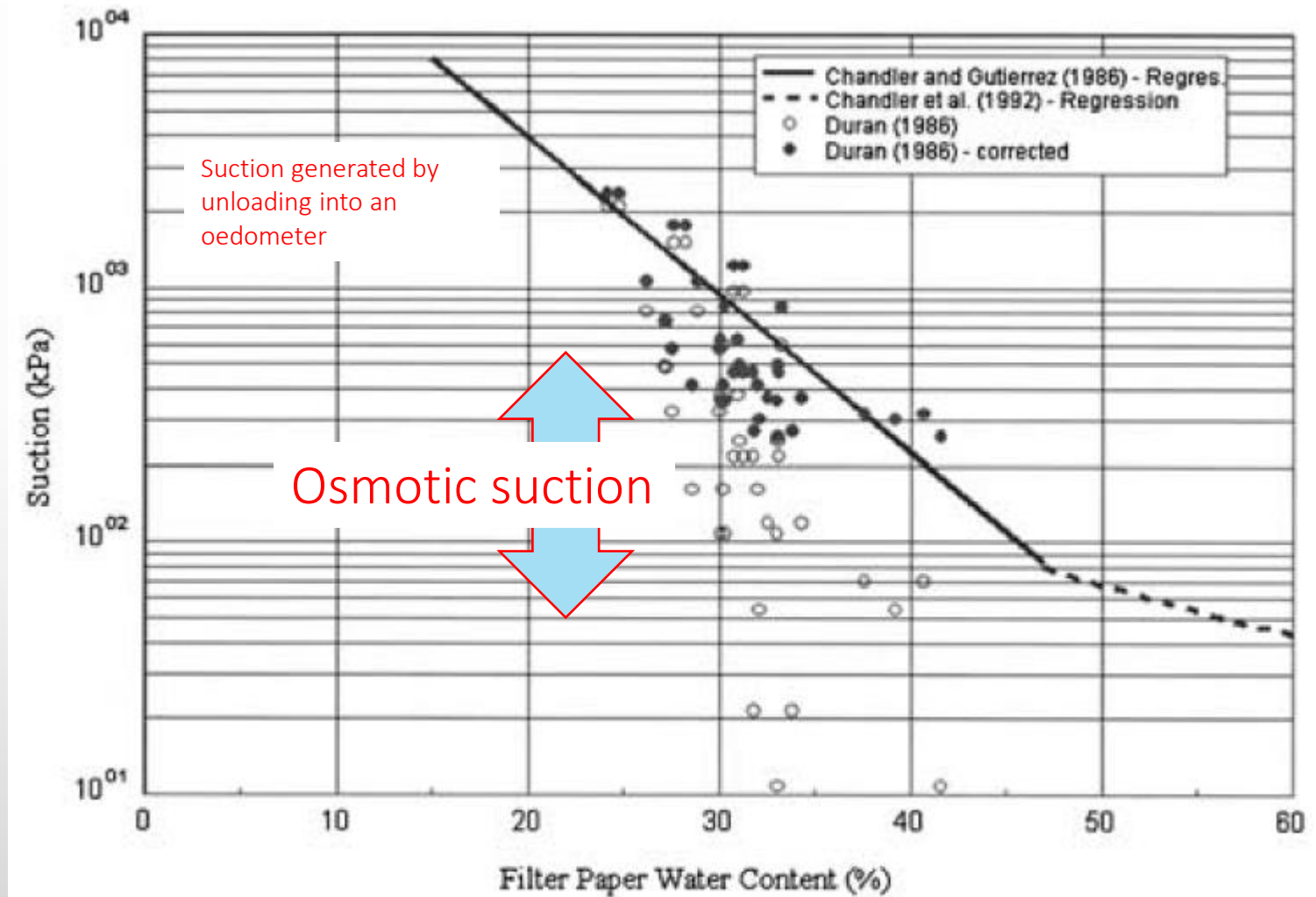
7 Days

14 Days

28 Days

The Filter Paper Technique

Interpretation



The Filter Paper Technique

Equilibrium time

Suggested equilibrium time according to the suction level

Total Suction Range (kPa)	Equilibration Time Suggested
0–100	Not determined, but certainly more than 30 days
100–250	30 days
250–1000	15 days
1000–30000	7 days

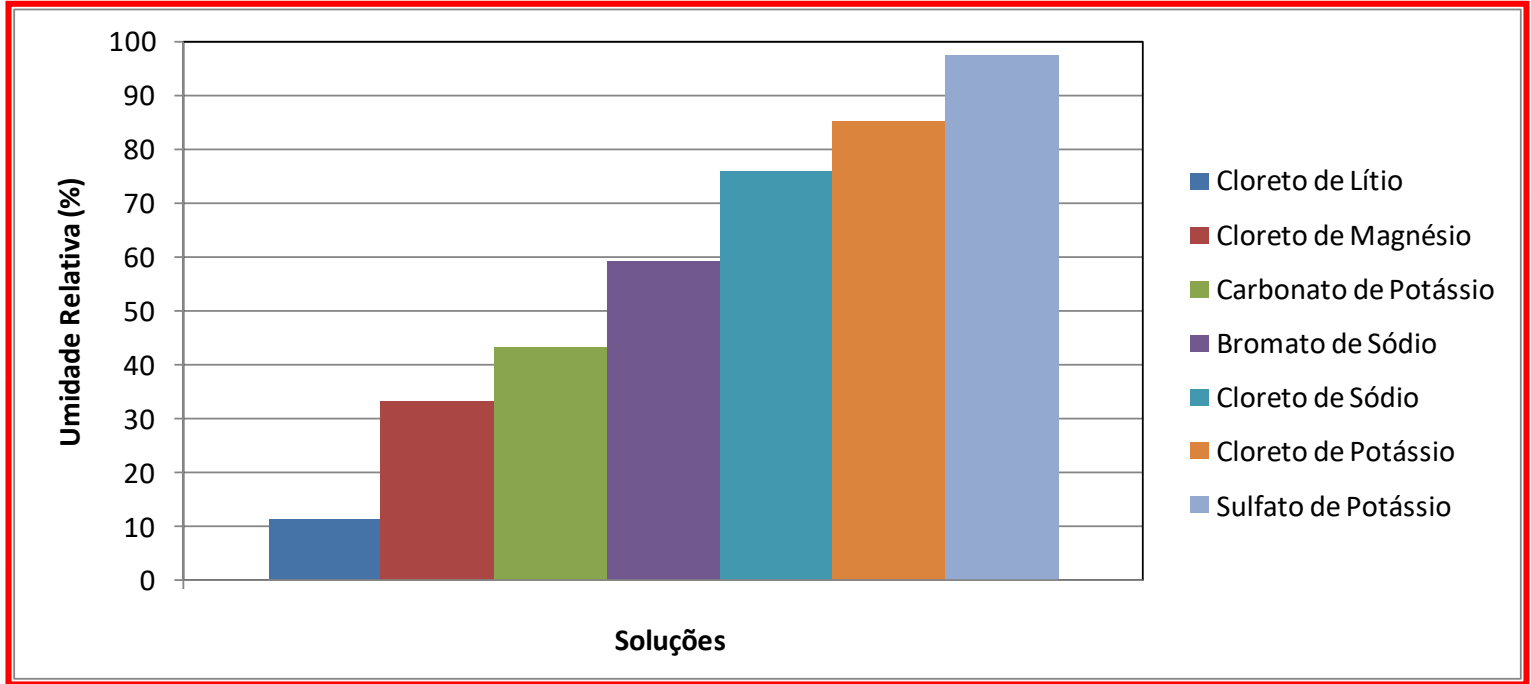
Marinho & Oliveira (2006)

To remember



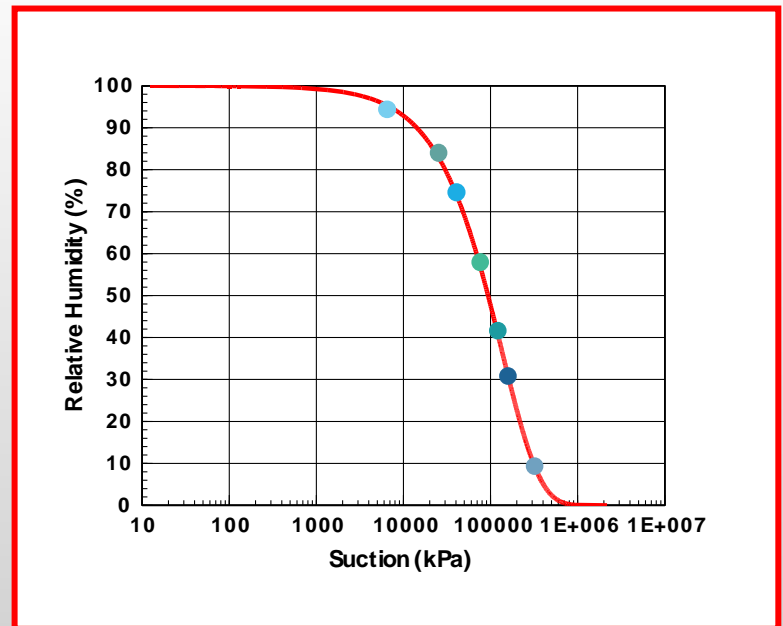
$$\psi = -\frac{RT}{M_v} \ln(RH) = -135055 \ln(RH)$$

Conceitos de Termodinâmica



Cloreto de Lítio	LiCl	11.3
Cloreto de Magnésio	MgCl	33.1
Carbonato de Potássio	K ₂ CO ₃	43.2
Bromato de Sódio	NaBrO ₃	59.1
Cloreto de Sódio	NaCl	75.7
Cloreto de Potássio	KCl	85.1
Sulfato de Potássio	K ₂ SO ₄	97.6

Dados: Department of Biology – University of Colorado



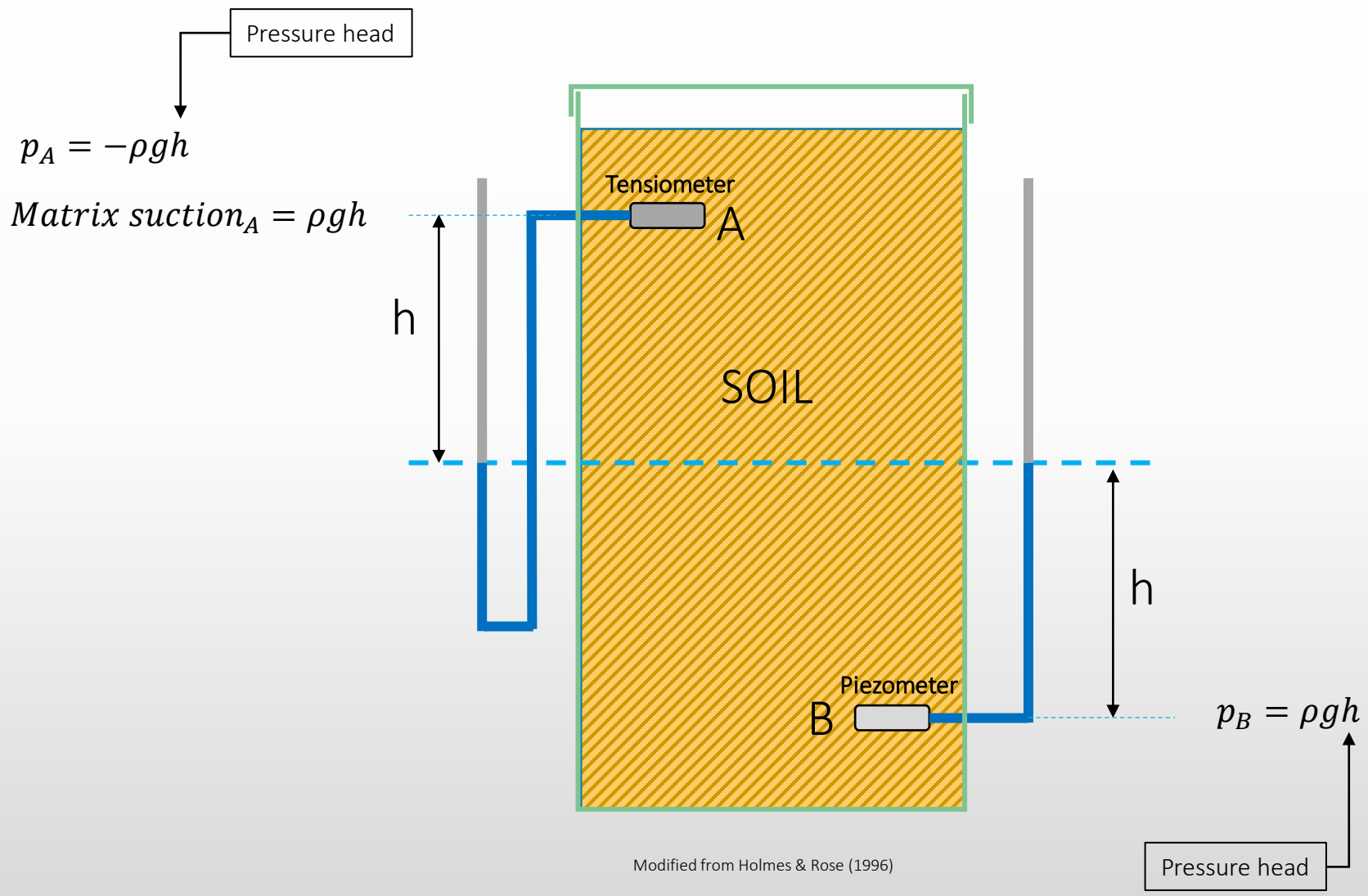
To remember

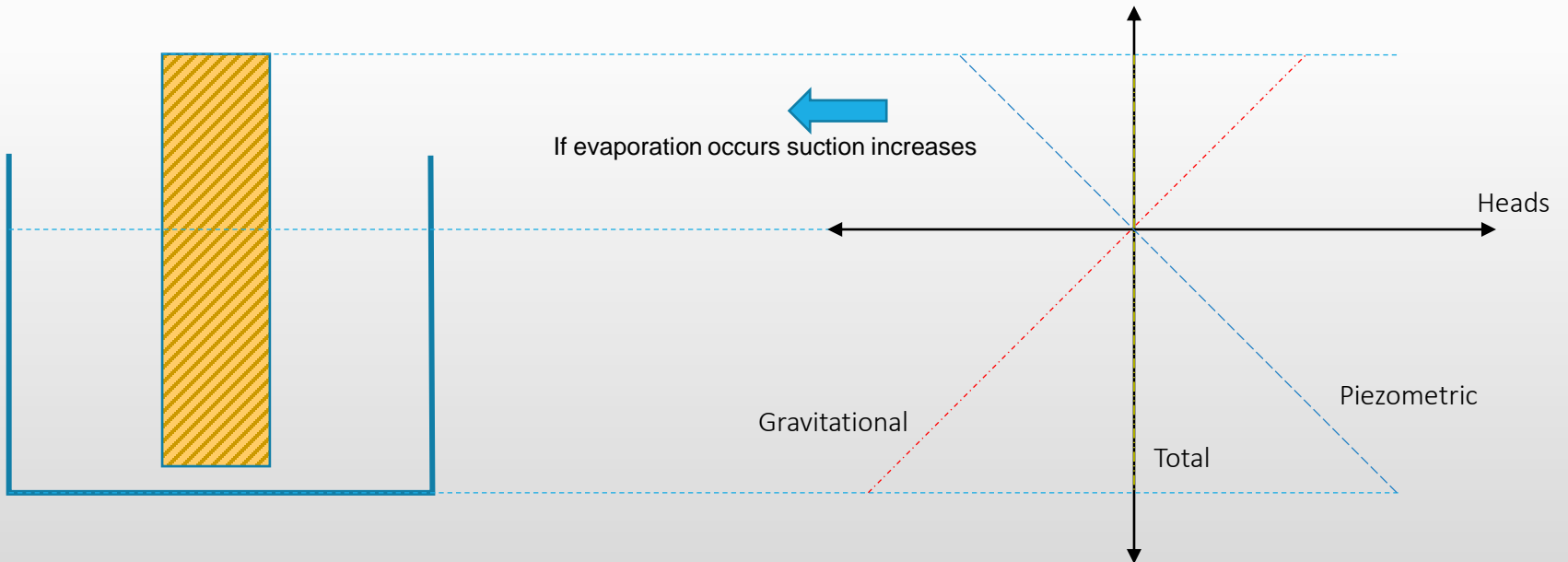
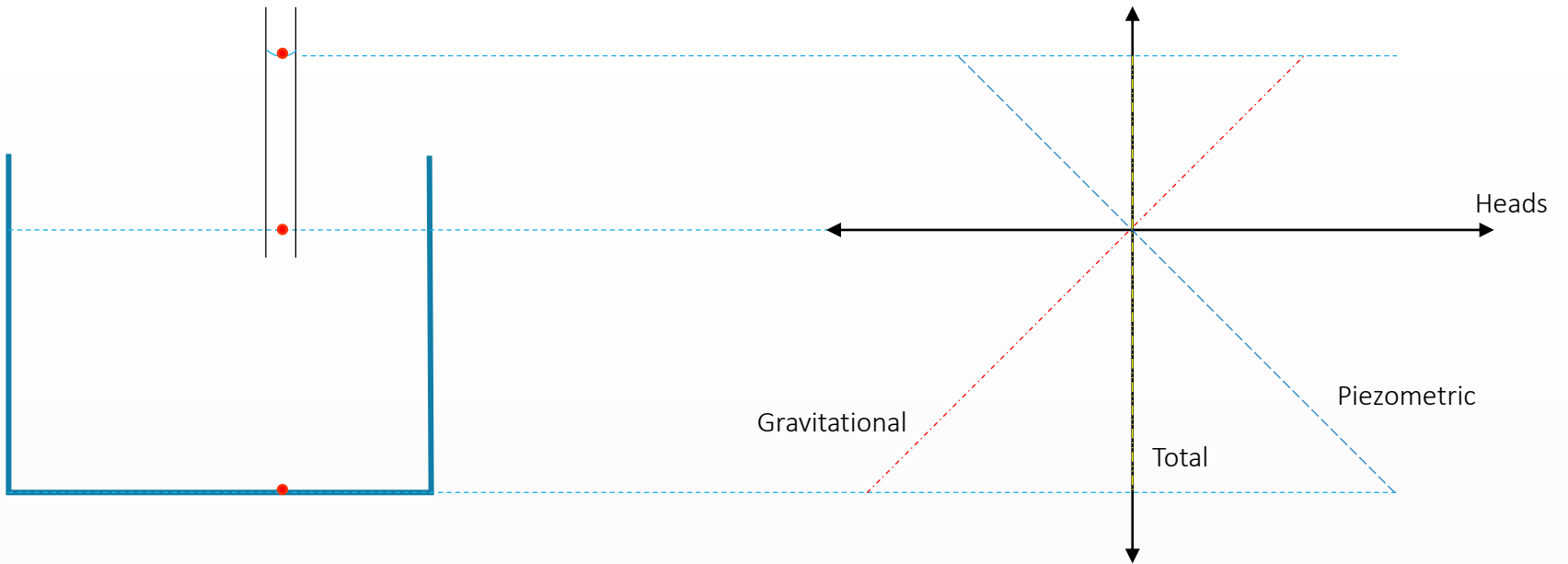


Placa de Sucção



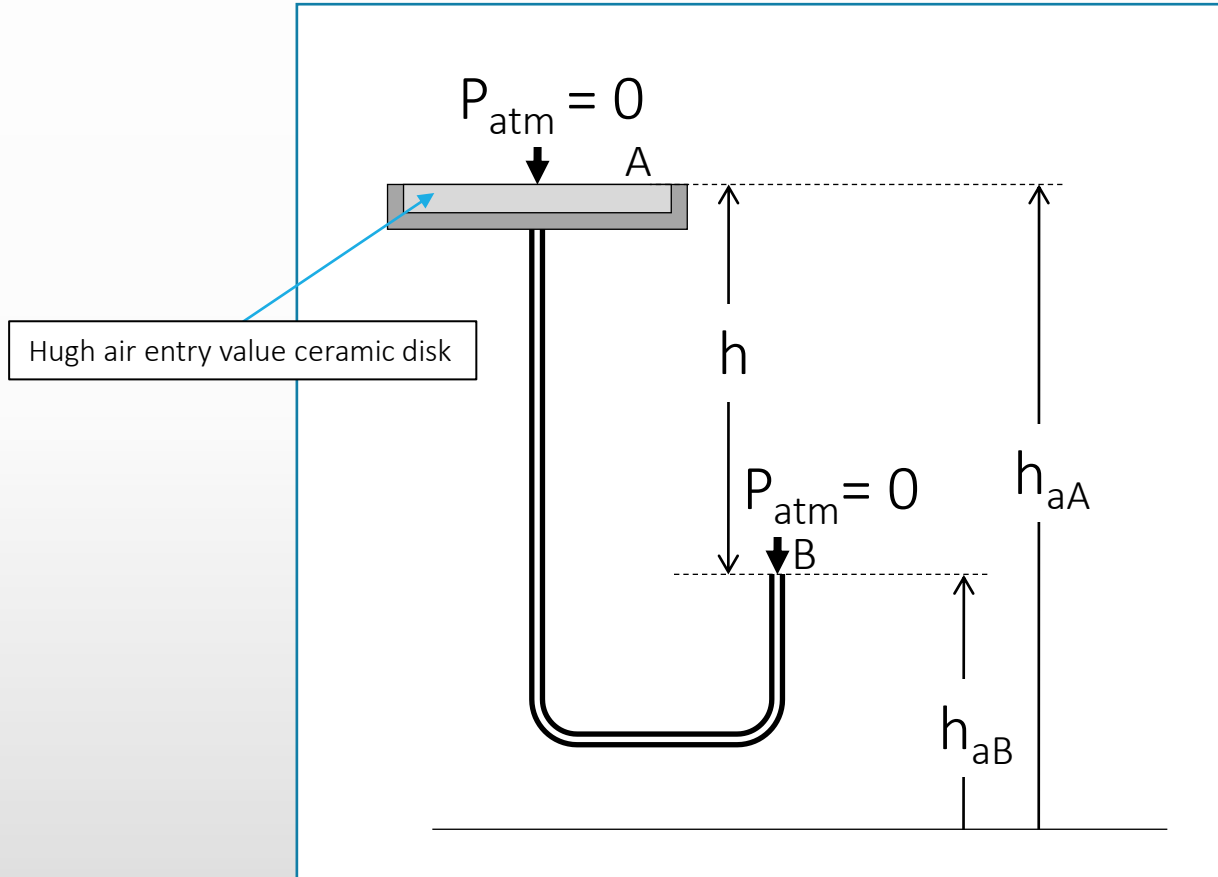
Hydraulic Potentials





Suction Plate

Working principle

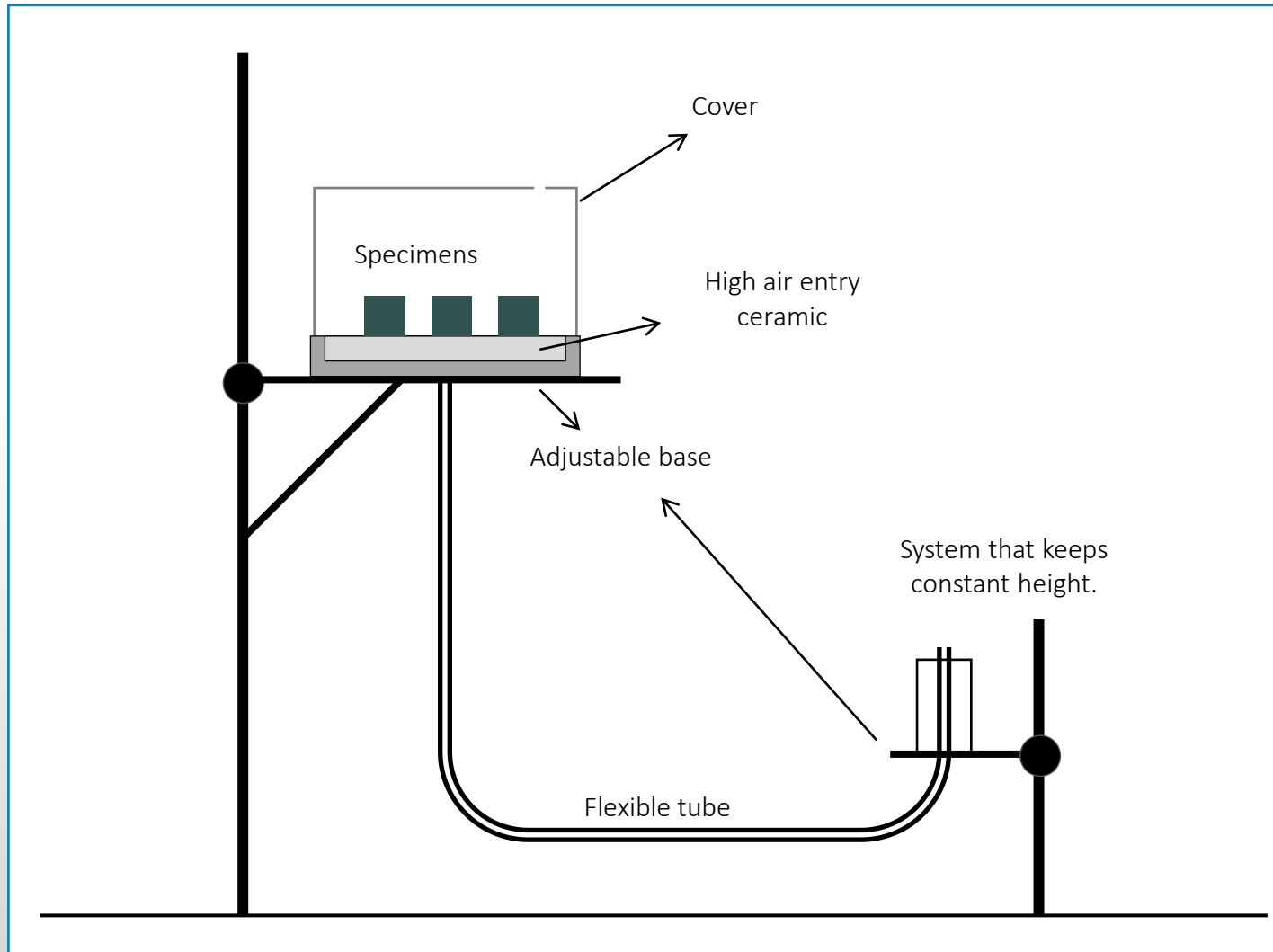


$$suction = h * \gamma_w$$

The suction applied by the difference in height (h) is not enough to desaturate the ceramic.

Suction Plate

Working principle



Suction Plate

Procedures

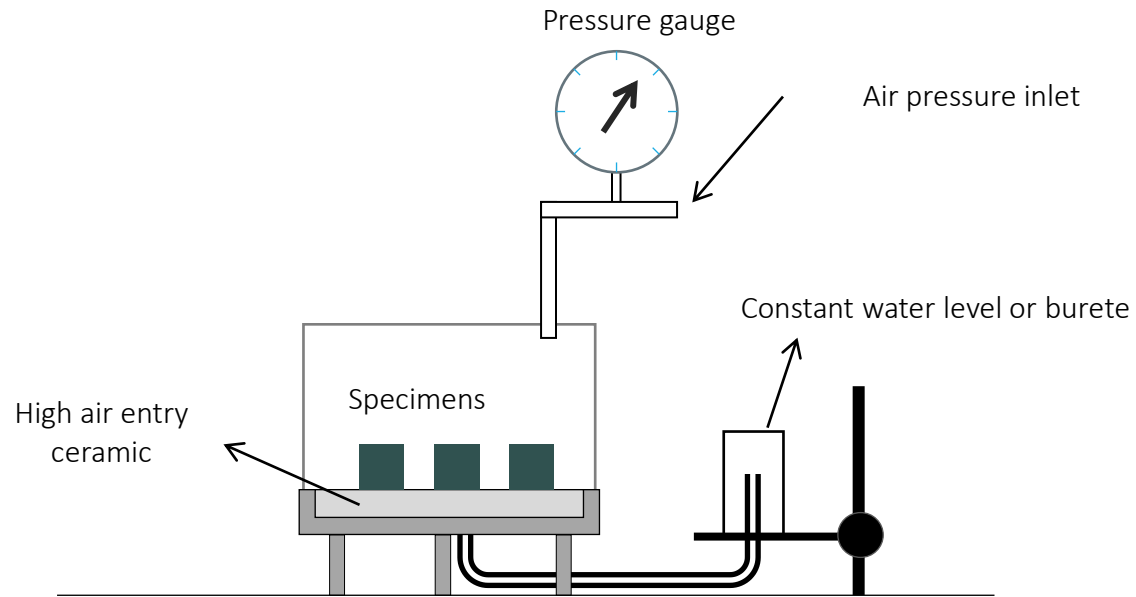
- The system should be saturated to eliminate any visible bubble.
- The ceramic should be saturated over night under pure water using a high vacuum pump.
- The use of hot water (above 35°) improve the saturation.
- The specimens can be undisturbed, compacted or remoulded.
- Volume of the specimen should be determined in order to be able to calculate volume based parameters
- Specimen is placed on the top of the ceramic taking care to have a intimate contact between soil water and ceramic water.
- In case the contact is not good a filter paper or silica should be used to improve the contact.
- The middle of the specimen and the output level of the system should be placed at the same level.
- After the specimen is placed water can added in the surrounding of the mould. Eventually water can be added from the top.
- The initial saturation procedure may take few days.
- After the saturation equilibrium the specimen is weighted and its volume determined.
- After that the differential height is increased.
- The choice of heights (suctions) depends on the soil type.
- The procedure is repeated for each increase in height.
- If the soil is not going to be used for another test (e.g. pressure plate or filter paper), the sample should be placed in the over after weighting and determining its volume.
- With the dry weight of the specimen water content and any volume based parameter can be obtained.

Pressure Plate

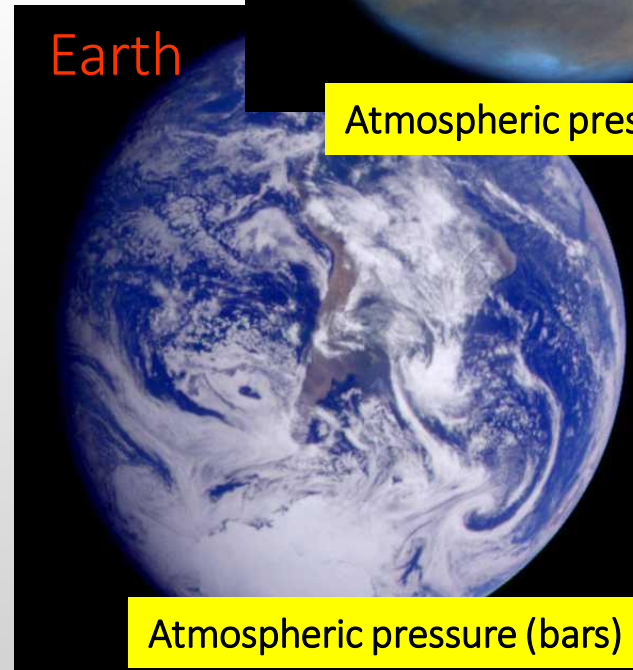
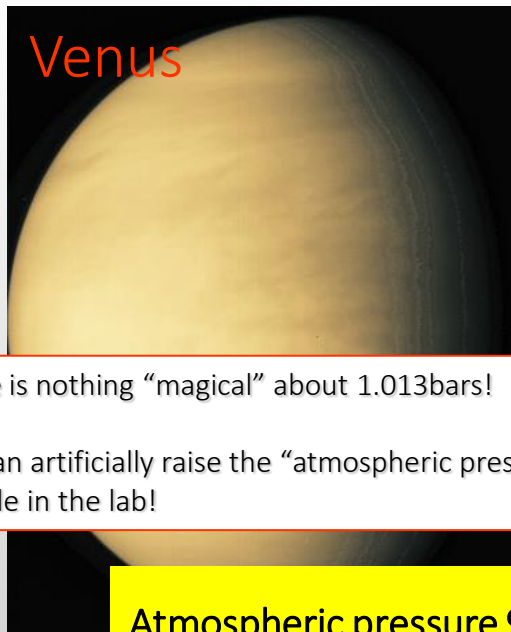
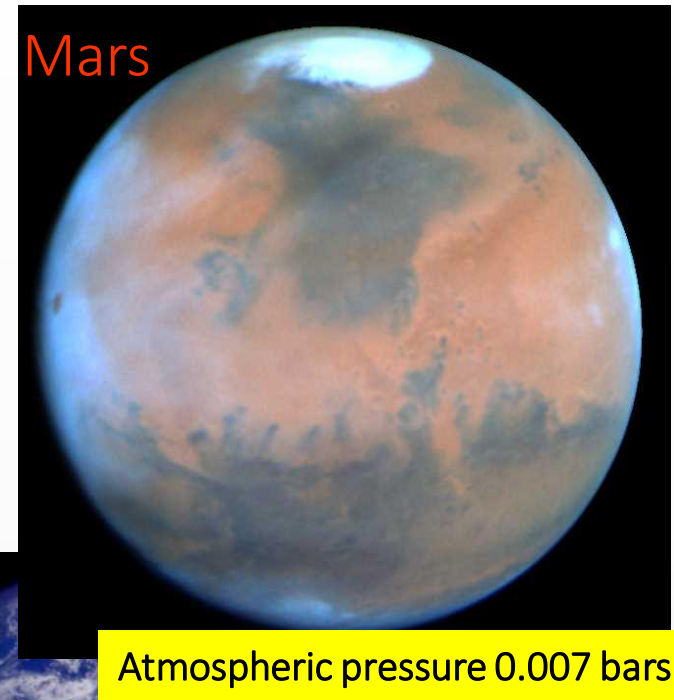
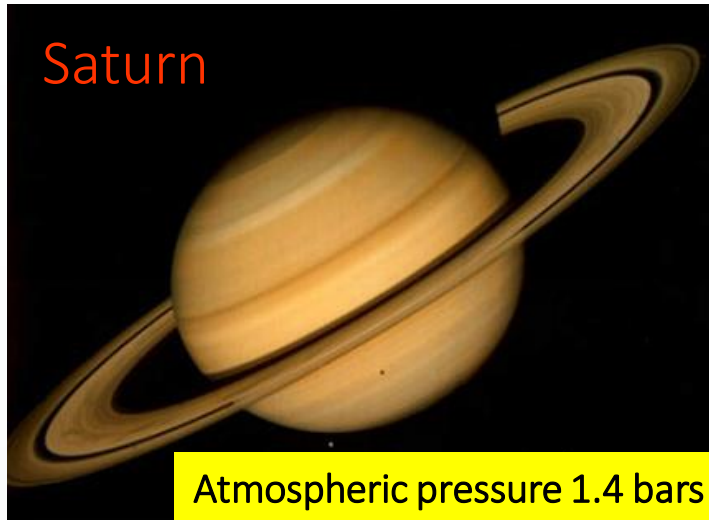
Axis translation technique



Pressure Plate



The Axis-Translation Technique

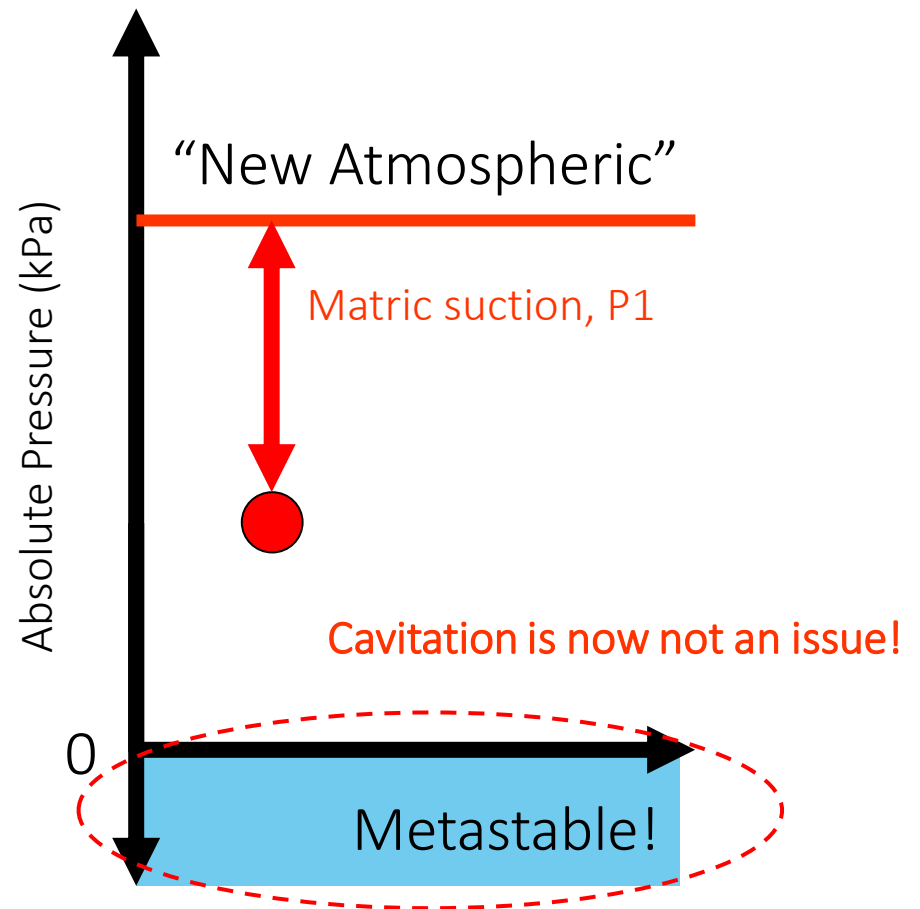
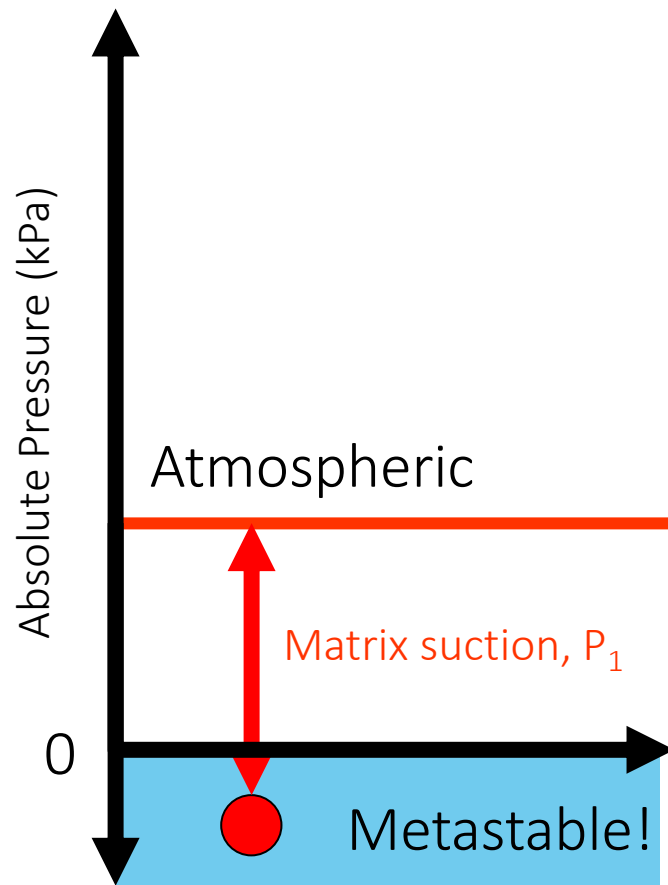


There is nothing “magical” about 1.013bars!

We can artificially raise the “atmospheric pressure” of a sample in the lab!

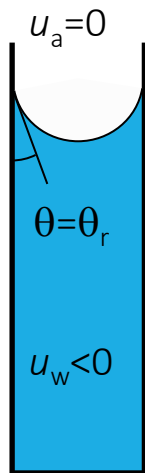


The Axis-Translation Technique

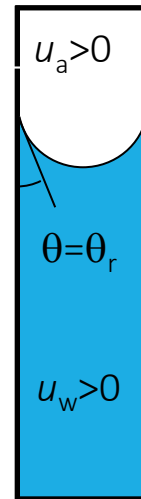


The Axis-Translation Technique

Conceptual justification



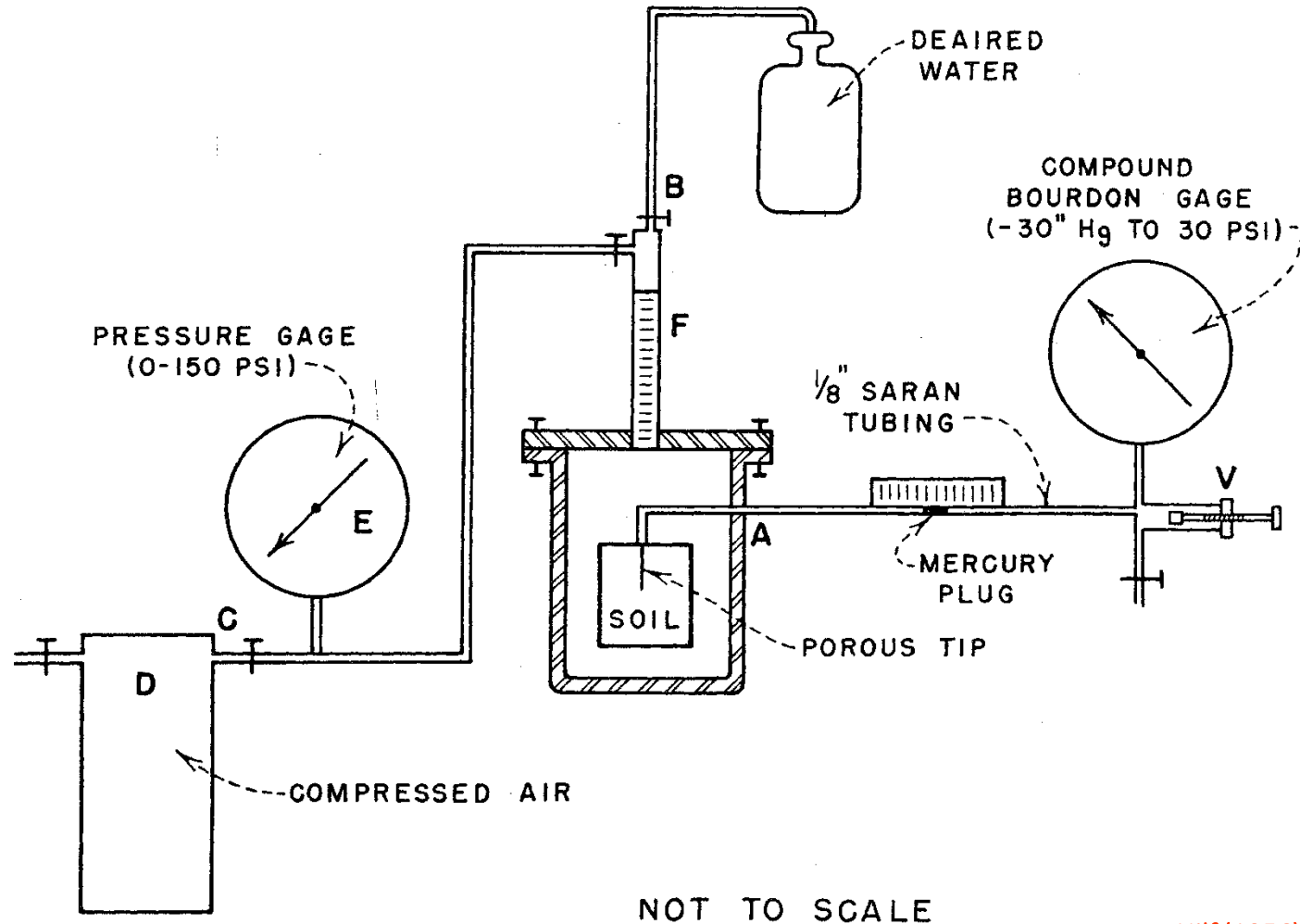
$$u_w - u_a = -2T \cos \theta_r / r$$



$$u_w - u_a = -2T \cos \theta_r / r$$

For **incompressible liquid**, an increase in air pressure does not alter the meniscus curvature and, hence, the difference $u_w - u_a$

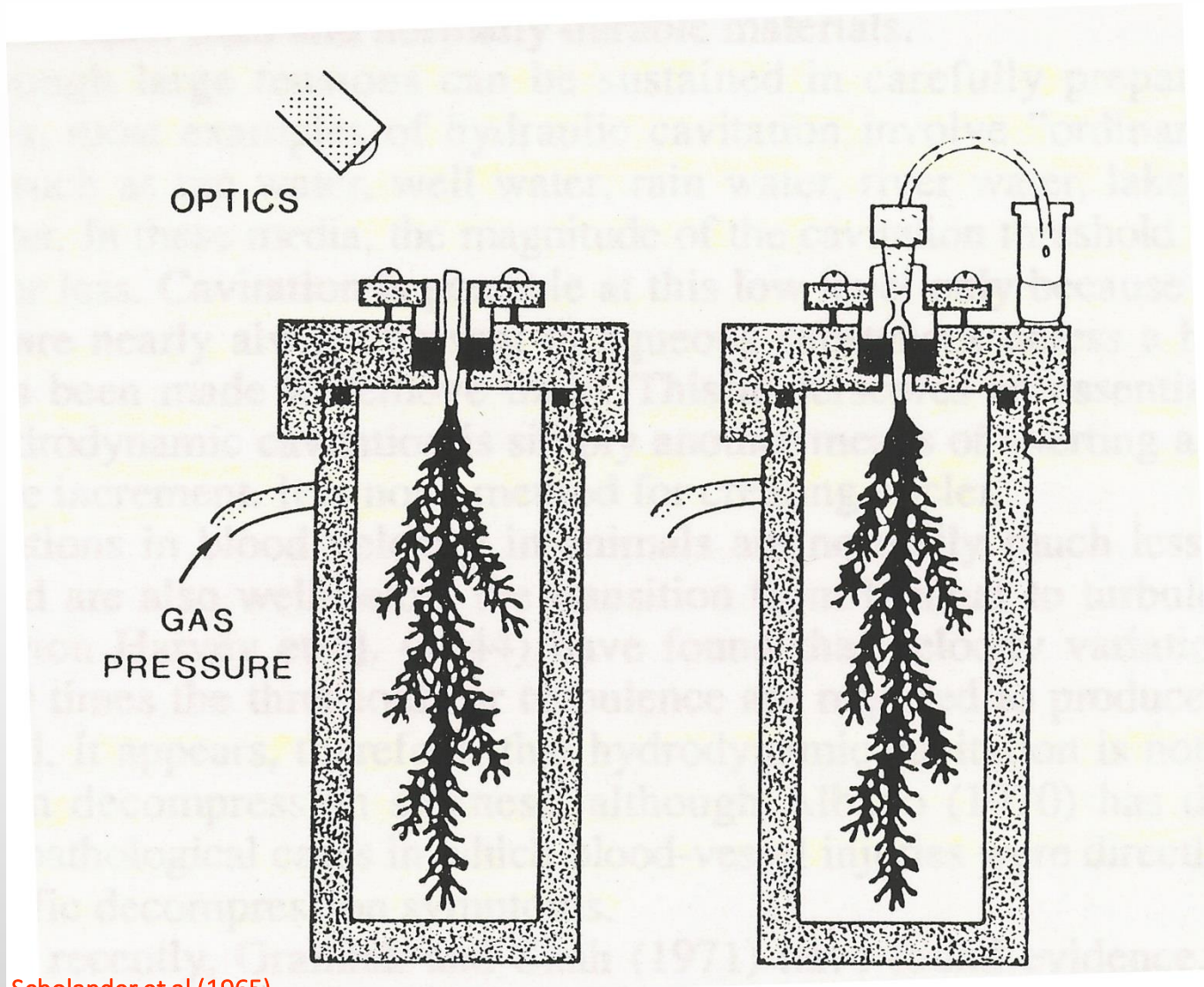
The Axis-Translation Technique



Hilf (1956)

Layout of apparatus for triaxial compression test with pore pressure measurement

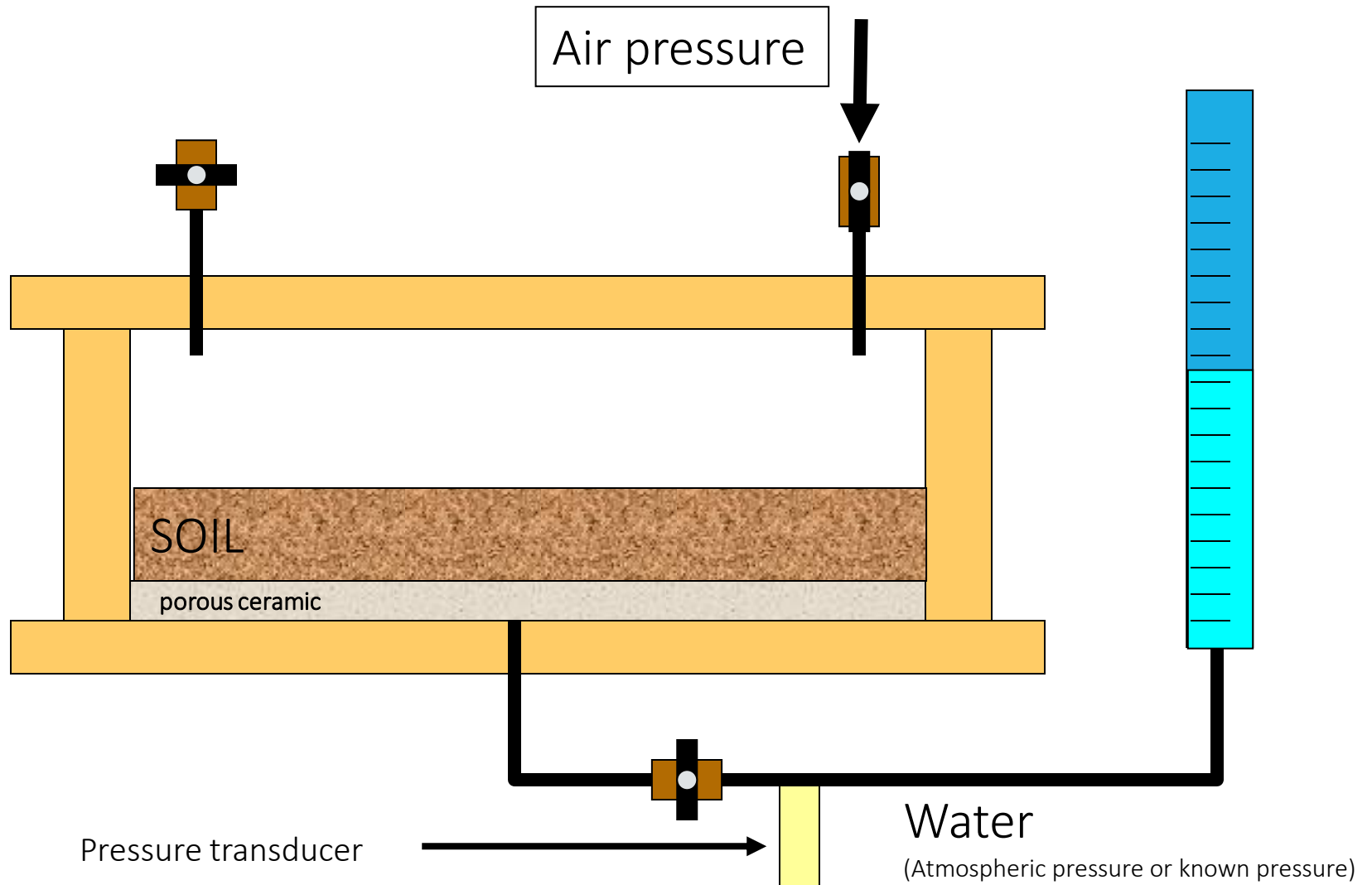
The Axis-Translation Technique



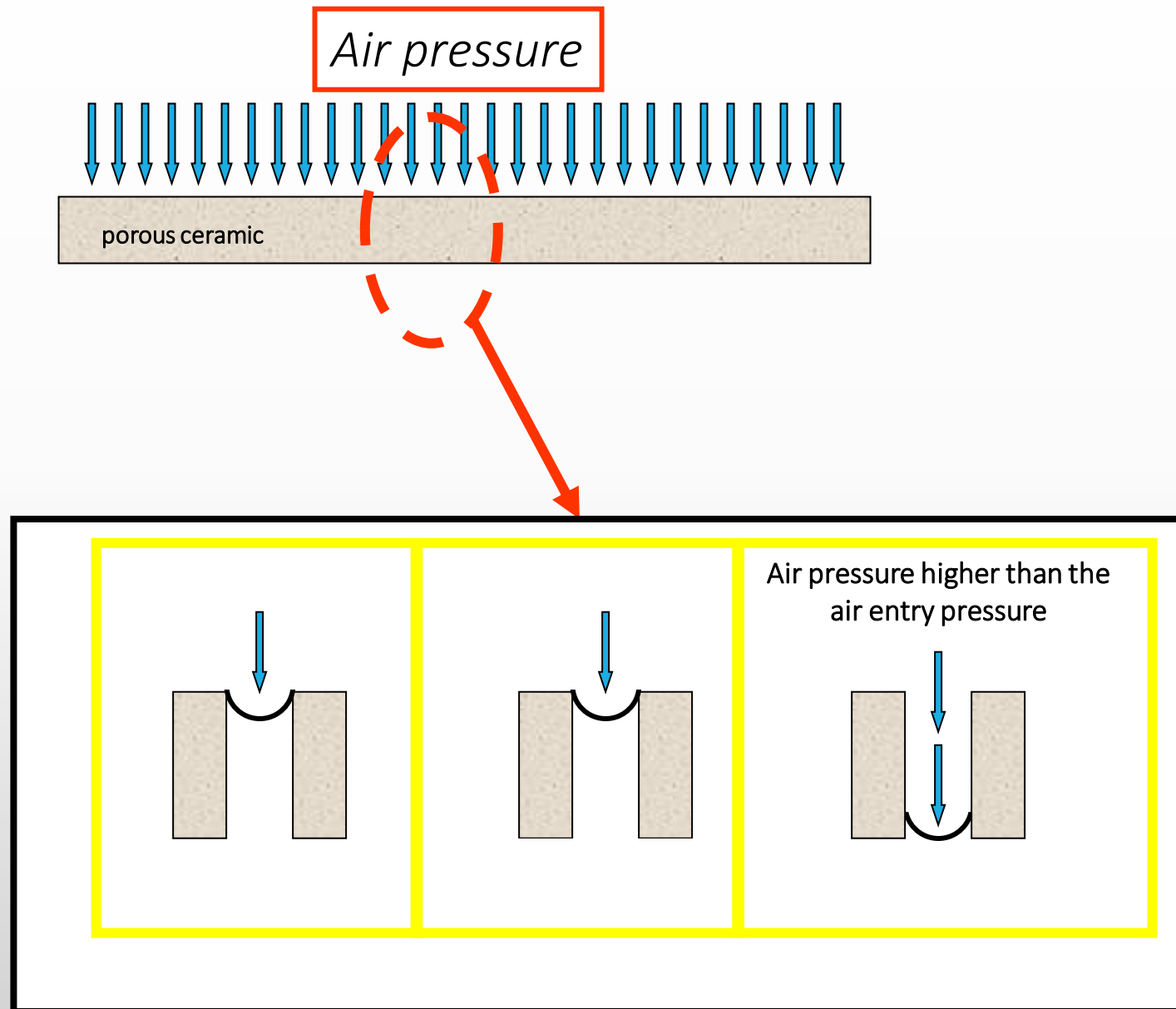
Scholander et al (1965)

Apparatus used to measure the internal tensile pressure in a twig severed from its stalk

The Axis-Translation Technique



The Axis-Translation Technique



Tensiometer versus Axis-Translation

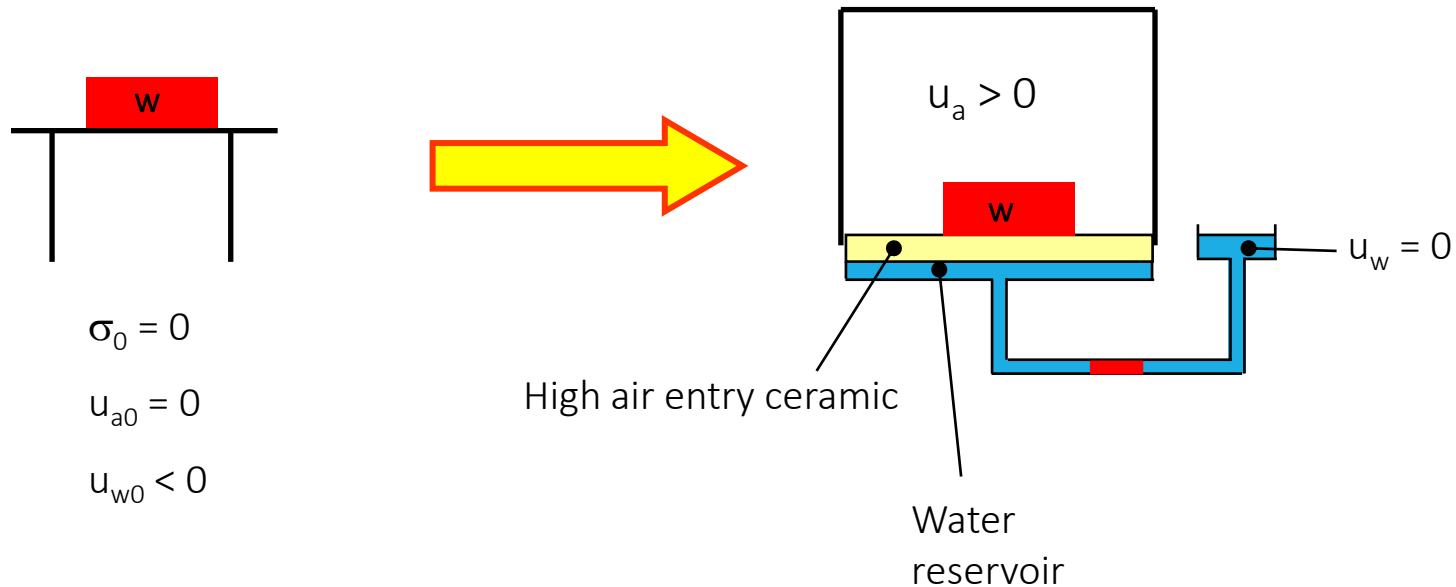
Similarities

- A pressure differential is measured across a high air entry ceramic
- Expansion of air cavities in the ceramic may also take place in axis-translation technique, but this problem is (probably?) negligible if the ceramic is adequately saturated
- Water pressure in the water reservoir may differ from pore-water pressure if the ceramic is not adequately saturated

Differences

- Water in axis-translation is NOT in a metastable state
- In axis-translation, relatively large air cavities in the ceramic may slowly expand (because of air diffusion) but there is not rapid expansion of cavitation nuclei.

Validity of Axis-Translation Technique



At the same water content, can we state that

$$u_{a0} - u_{w0} = u_a - u_w$$

and hence chamber air pressure u_a equals negative pressure $-u_{w0}$?

Validation of the Axis-Translation

Medium degree of saturation ($S_r < 0.85-0.9$)

- Bishop & Donald (1961)
- Bocking & Fredlund (1980)
- Tarantino, Mongiovi, and Bosco (2000)

High degree of saturation ($S_r > 0.85-0.9$)

- Fredlund & Morgenstern (1977) (data not really consistent)
- Tarantino and Mongiovi (2005) (one single test)

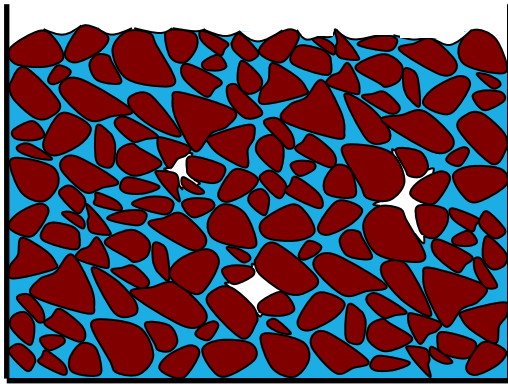
Is axis translation reliable at high degrees of saturation ?

Do we have clear and convincing experimental evidence ?

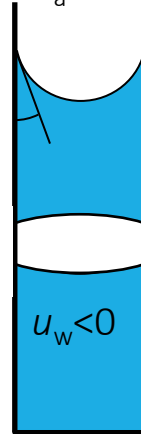
Conceptual limitation of Axis-Translation

$$0.85-0.90 < S_r < 1$$

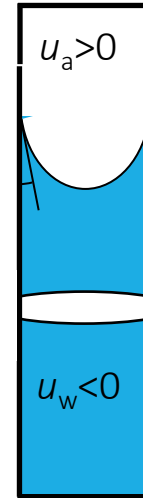
$$u_w < 0$$



$$u_a = 0$$



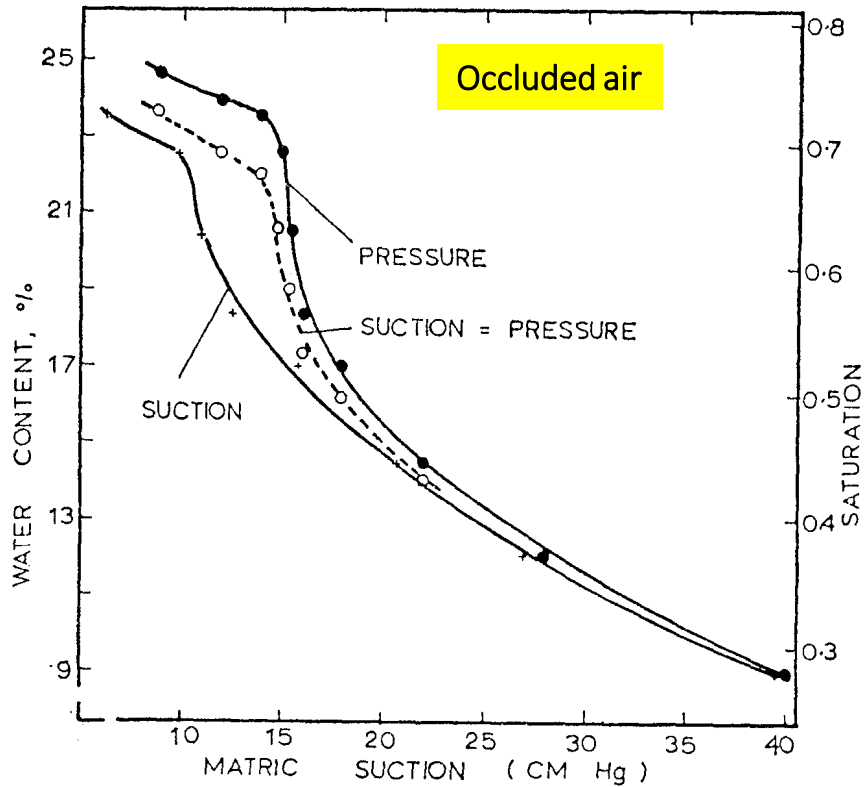
$$u_a > 0$$



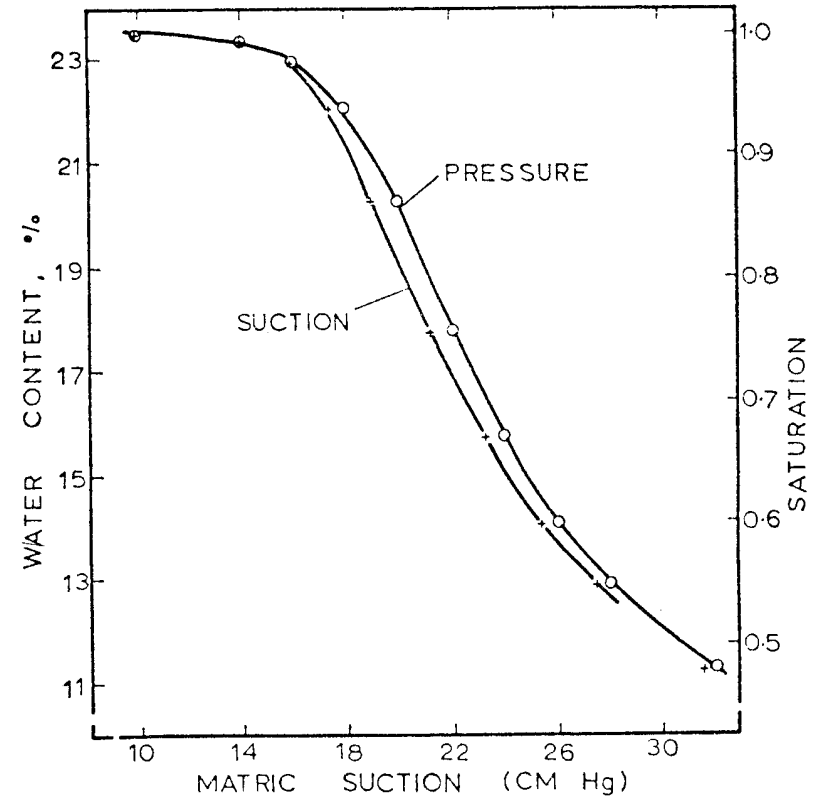
At high degree of saturation, we have to figure out a capillary tube with compressible liquid. The increase in air pressure increase the boundary meniscus curvature and, hence, the difference $u_w - u_a$

Axis translation might overestimate suction at high degrees of saturation

The Axis-Translation Technique

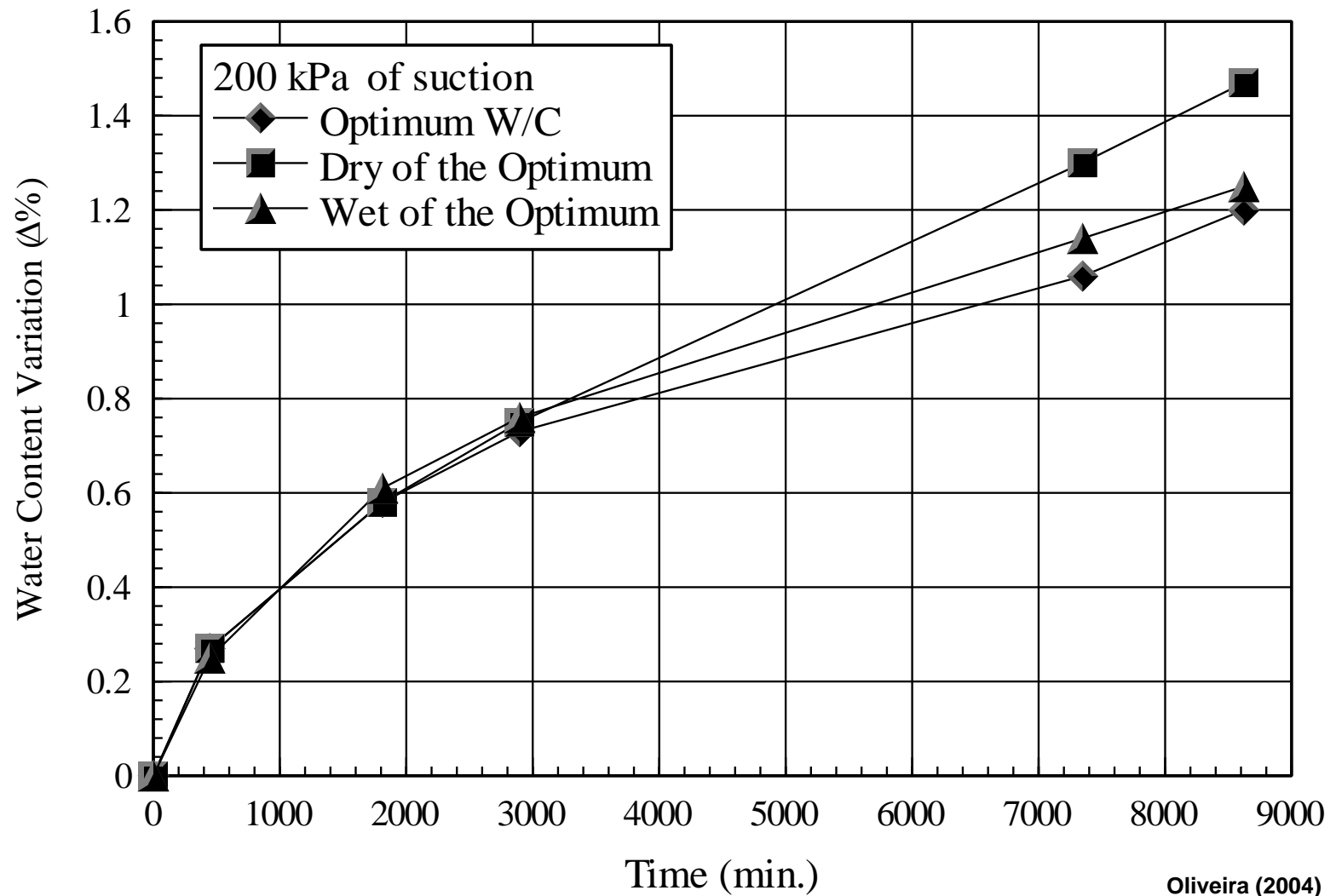


Soil-water retention curve for initially unsaturated coarse silt.



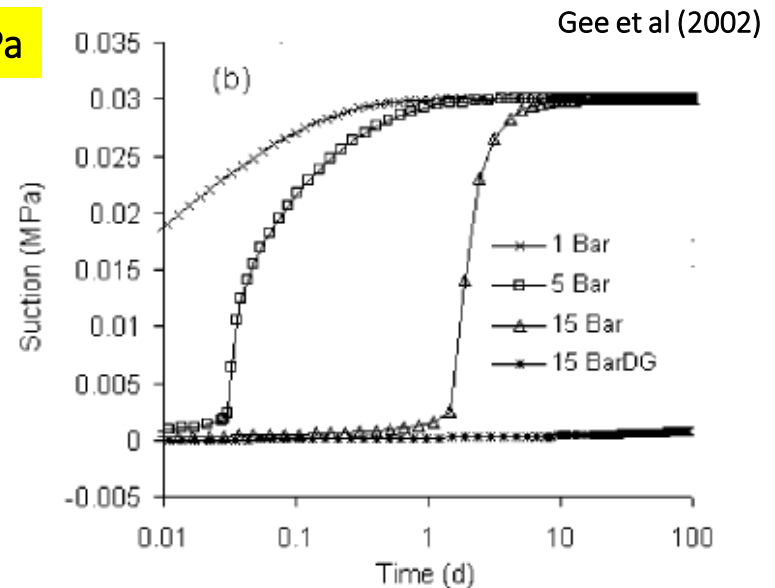
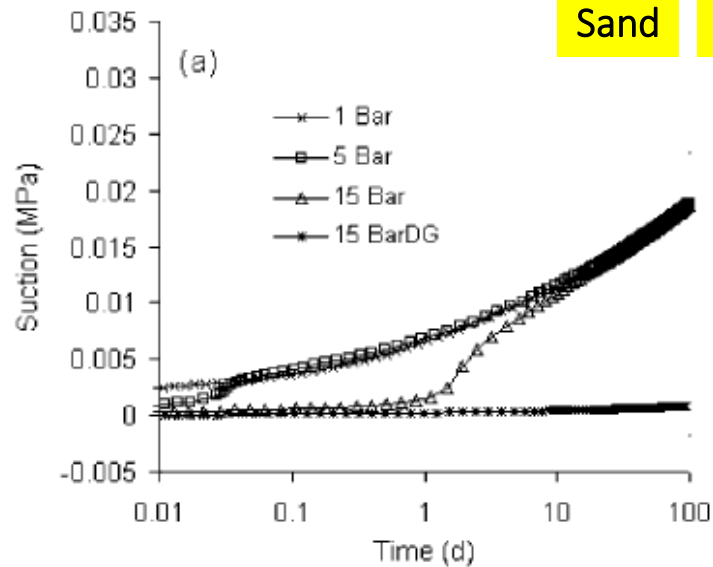
Soil-water retention curve for initially saturated coarse silt

The Axis-Translation Technique

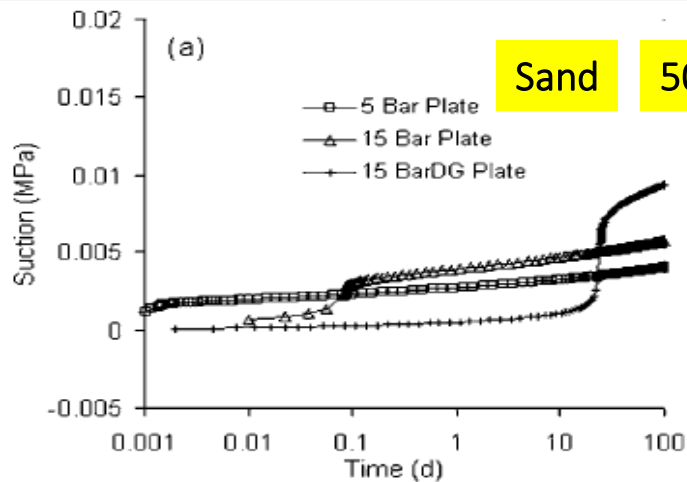


Soil water content change during axis translation

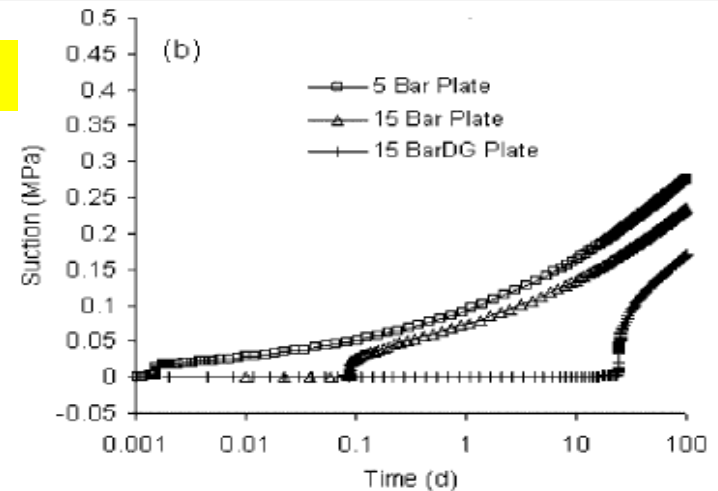
The Axis-Translation Technique



The 5 mm height (sample midpoint)

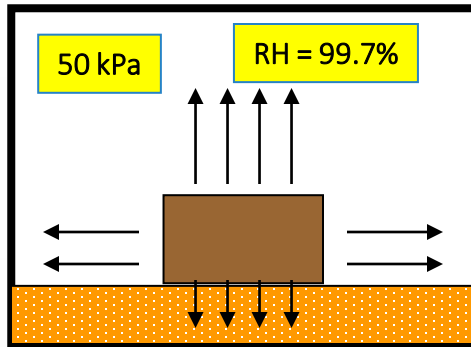


The soil-plate interface

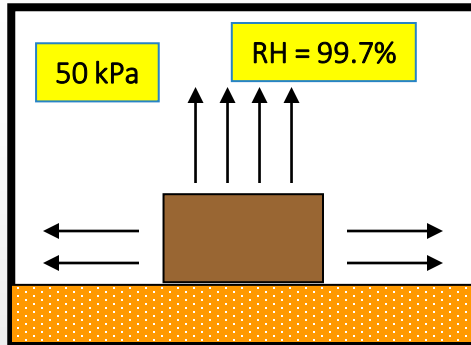


The Axis-Translation Technique

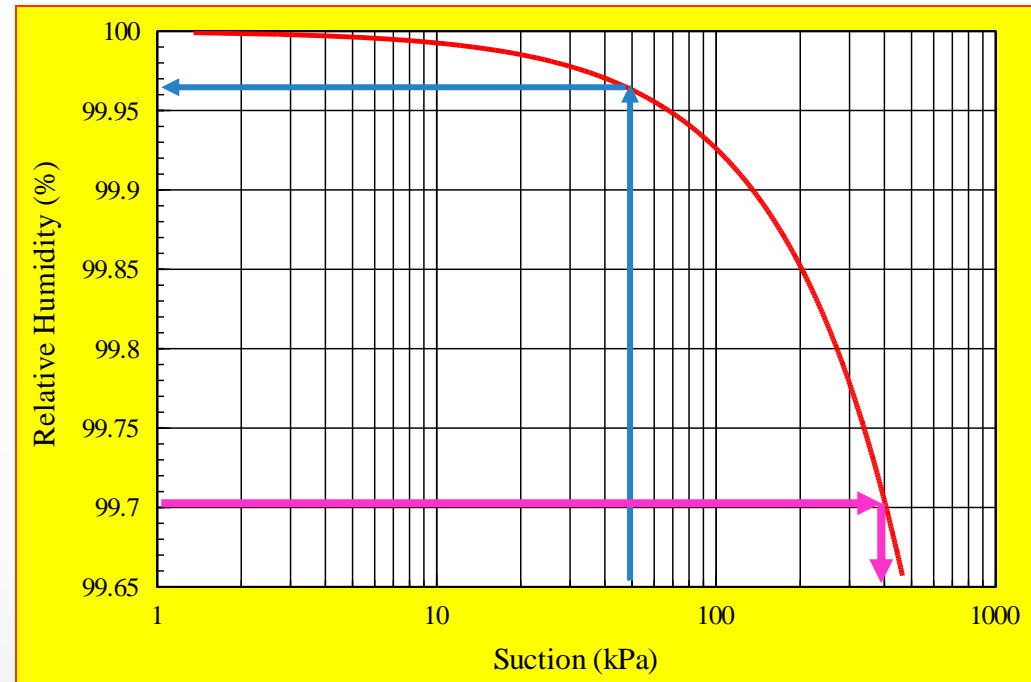
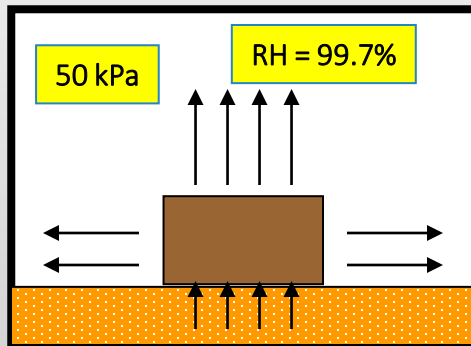
(a)



(b)

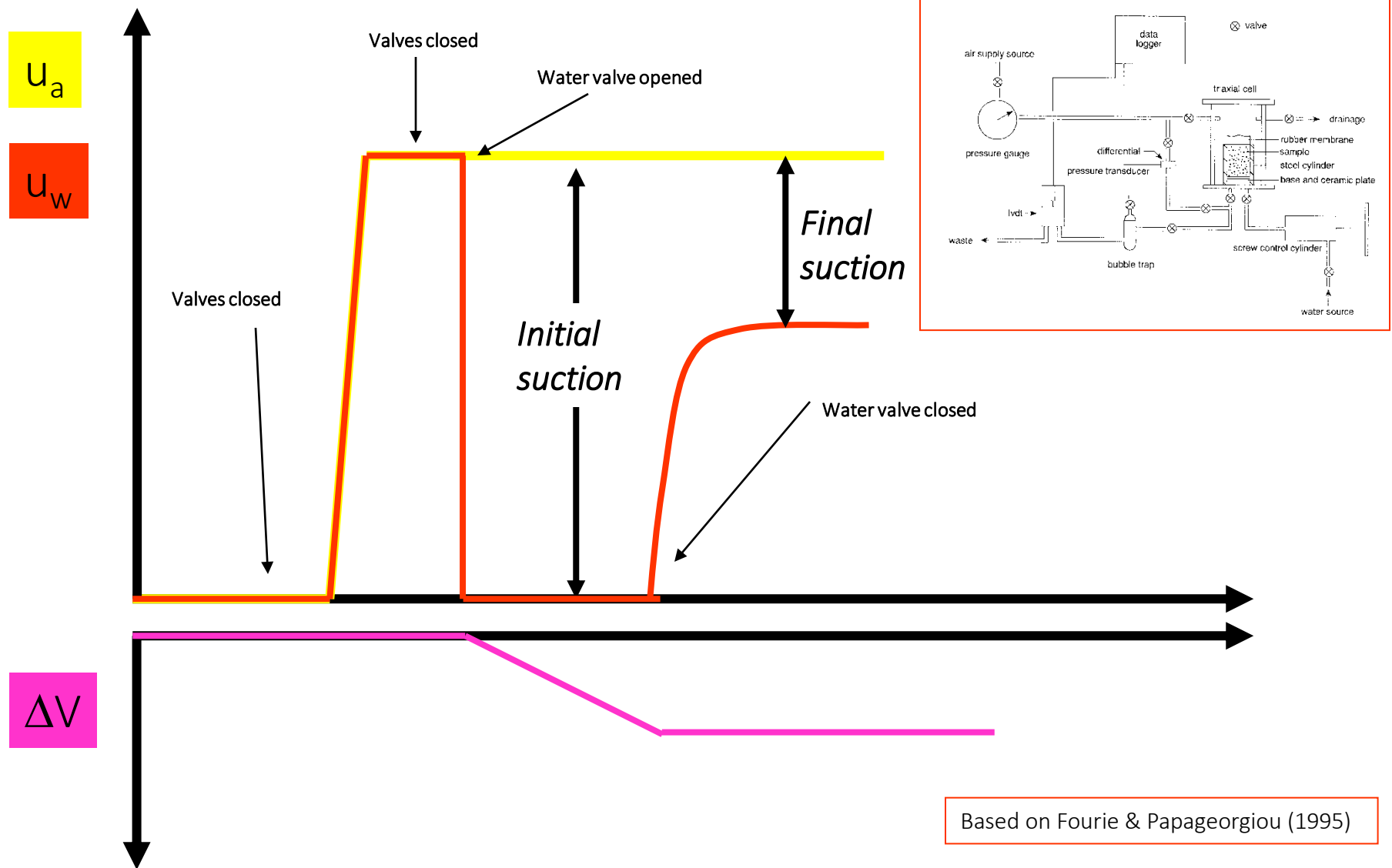


(c)



Relative humidity inside the chamber

The Axis-Translation Technique



Based on Fourie & Papageorgiou (1995)

Technique to reduce the equilibrium time

WATERMARK Sensors



TEROS 21





1. *In which situation the osmotic suction can affect the actual measurement of matrix suction?*
2. *Why an ordinary tensiometer can measure higher values of suction if the measurement is made in Santos in relation to São Paulo city?*
3. *What is the importance of the ceramic for a tensiometer and why it should have a high air entry value?*
4. *What level of suction you consider important for engineering purpose?*
5. *What kind of suction is induced when you place a soil sample out of contact with a salt solution in a closed environment?*
6. *Consider that a salt solution generate a RH that induces a suction of 700 kPa. If a filter paper is placed in contact with a specimen (with no salt in it) and another is placed out of contact, what value of suction you should expect from both filter papers?*
7. *When using a suction plate or a pressure plate the specimen is in contact with air. What is the influence of the RH of that air on the equilibrium of the system?*
8. *How can you generate suction for calibration of all sensors and equipment presented here?*