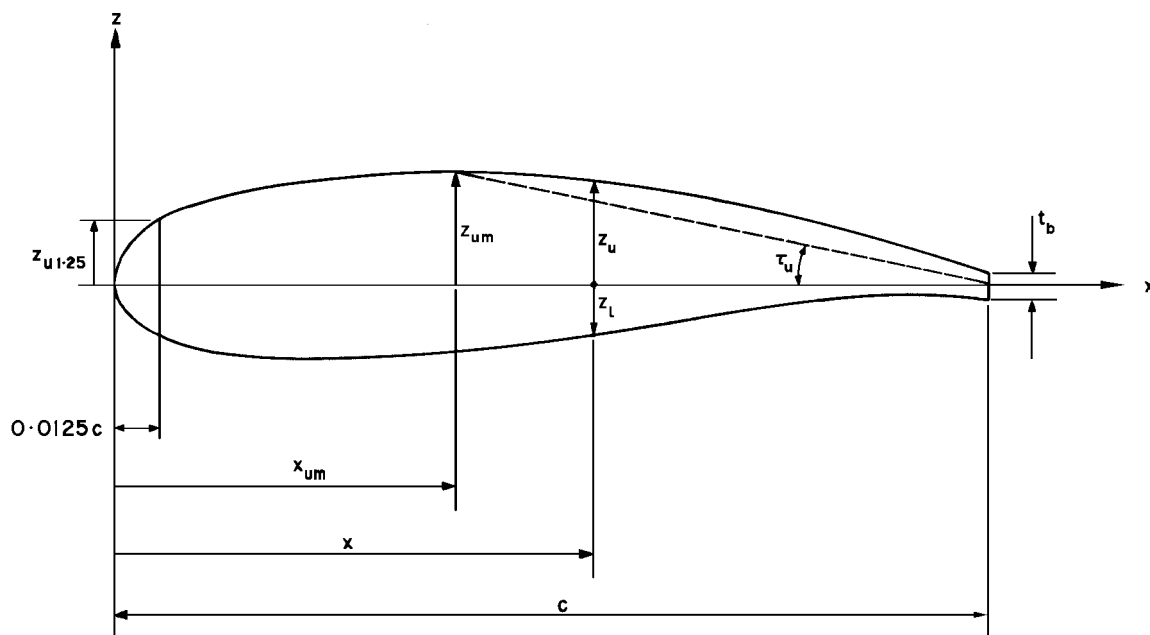


# AEROFOIL MAXIMUM LIFT COEFFICIENT FOR MACH NUMBERS UP TO 0.4

## 1. NOTATION AND UNITS

		<i>SI</i>	<i>British</i>
$(a_1)_0$	slope of lift coefficient curve with incidence for aerofoil in incompressible flow	$\text{rad}^{-1}$	$\text{rad}^{-1}$
$B_i$	coefficients used in estimation of $\alpha_0$ with $i = 1$ to 14 in Equation (5.1)	rad	rad
$C_{Lm}$	maximum lift coefficient of aerofoil		
$C_{L0}$	lift coefficient at zero incidence, Equation (5.3)		
$\Delta C_L$	increment in lift coefficient (see Section 2.2)		
$c$	aerofoil chord	m	ft
$F_1, F_2$	parameters in Equation (7.1)		
$F_M$	factor for effect of Mach number on $C_{Lm}$ (Equation (7.1))		
$F_S$	factor on $C_{Lm}$ for modern aerofoils in Figure 5		
$M$	free-stream Mach number		
$R_c$	Reynolds number based on free-stream conditions and aerofoil chord		
$t$	maximum thickness of aerofoil	m	ft
$t_b$	trailing-edge base thickness (see Sketch 1.1)	m	ft
$x$	chordwise distance measured from aerofoil leading edge, positive rearwards	m	ft
$x_{um}$	value of $x$ at which $z_{um}$ occurs (see Sketch 1.1)	m	ft
$z$	aerofoil ordinate measured normal to chord, positive upwards (see Sketch 1.1)	m	ft
$z_{ci}$	aerofoil camber ordinate with $i = 1$ to 14 in Equation (5.1)	m	ft
$z_l$	lower-surface ordinate (see Sketch 1.1)	m	ft

$z_l(x/c)$	lower-surface ordinate at $x/c$	m	ft
$z_u$	upper-surface ordinate (see Sketch 1.1)	m	ft
$z_{um}$	maximum upper-surface ordinate (see Sketch 1.1)	m	ft
$z_u(x/c)$	upper-surface ordinate at $x/c$	m	ft
$z_{u1.25}$	upper-surface ordinate at $x/c = 0.0125$	m	ft
$\alpha$	incidence	rad	rad
$\alpha_0$	zero-lift incidence, Equation (5.1)	rad	rad
$\tau_u$	aerofoil upper-surface angle defined by Equation (3.1), see also Sketch 1.1	rad	rad



Sketch 1.1 Aerofoil geometry

## 2. INTRODUCTION

At low speeds the two-dimensional flow over an aerofoil normally remains attached at small incidences and the increase of lift with incidence is effectively linear, so that the lift coefficient at any incidence is given by the product of the lift-curve slope,  $(a_1)_0$ , and the incidence from zero lift,  $(\alpha - \alpha_0)$ . The variation of lift with incidence remains essentially linear until the onset of flow separation at a particular incidence, which is dependent on the free-stream conditions and aerofoil geometry. Further increase in incidence results in greater extents of flow separation and reduction in the slope of the lift-incidence curve until the total lift coefficient of the aerofoil reaches a maximum value  $(C_{Lm})$  and the aerofoil stalls. At still higher incidences the lift is reduced, perhaps catastrophically.

## 2.1 Types of Stall

There are various types of stall related to where the flow separations occur on the aerofoil. The types of stall can be classified as follows.

- (i) Trailing-edge stall, resulting from a trailing-edge flow separation which moves forward with increasing incidence.
- (ii) Leading-edge stall, resulting from a sudden separation of the laminar boundary layer near the leading edge, due to the bursting of a small bubble, which generally occurs without subsequent flow reattachment.
- (iii) Thin-aerofoil stall, which is due to a leading-edge separation reattaching to form a separation bubble. The reattachment point moves progressively aft with increasing incidence.
- (iv) A combined trailing-edge and leading-edge stall.

Further details of these types of stall and the effect on the aerofoil force characteristics can be found in Derivations 4 and 7, and Reference 22.

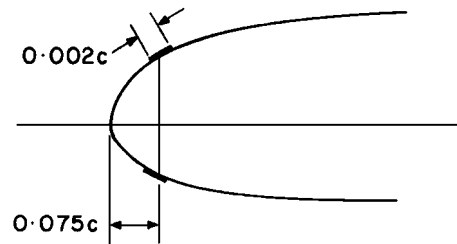
For low speeds, and for aerodynamically smooth aerofoils, the type of stall has been found (Derivation 4) to depend on the Reynolds number and the value of the upper-surface ordinate of the aerofoil at the 0.0125 chord location,  $z_{u1.25}$  (see Sketch 1.1).

For the correlation of aerofoil maximum lift coefficient it has been found necessary to consider the aerofoils in only two groups, those with  $z_{u1.25}/c < 0.017$  and those with  $z_{u1.25}/c \geq 0.017$ . These groups can be considered to contain aerofoils with predominantly leading-edge and trailing-edge stalls, respectively. Accordingly, the experimental values of  $C_{Lm}$  for the two groups have been correlated using leading-edge and trailing-edge geometrical parameters, respectively.

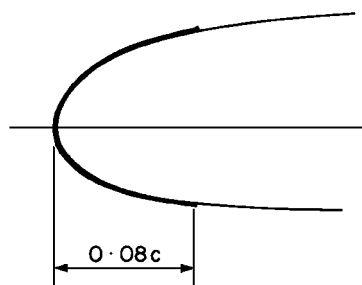
## 2.2 Scope of the Item

The main parameters that influence  $C_{Lm}$  are aerofoil geometry, surface condition (*i.e.* smooth or rough), Reynolds number and Mach number. Maximum lift coefficients are presented in terms of incremental lift coefficients,  $\Delta C_L$ , added to the lift coefficient at zero incidence,  $C_{L0}$ , which is useful in its own right as a measure of the effect of camber on lift. This approach was adopted to account for the main influence of aerofoil camber on maximum lift so that data for cambered and symmetrical aerofoils could be considered together. Procedures for obtaining  $\Delta C_L$  are given in Sections 3 and 4 for aerofoils with smooth and rough leading edges, while the procedure for obtaining  $C_{L0}$  is given in Section 5 and requires a detailed knowledge of the aerofoil geometry.

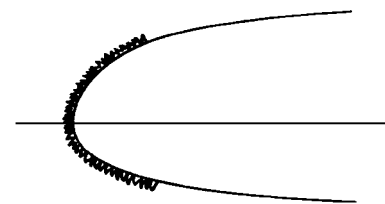
For the purposes of this Item a smooth aerofoil is defined as one with either no leading-edge roughness (*i.e.* natural boundary-layer transition) or with a small band of minimum roughness just sufficient to fix transition. This is the common practice for present day wind-tunnel tests; NASA, for example, use roughness boundary layer trips as illustrated in Sketch 2.1. A rough leading edge can be considered as similar to that obtained with ice formation or similar to that corresponding to the extent and size of roughness grains commonly used to fix boundary-layer transition in wind-tunnel tests of aerofoils at NACA some years ago, see Sketch 2.2a. Thus the data of Section 4, compared to those of Section 3, can be used as an indication of the loss in  $C_{Lm}$  due to ice formation.



**Sketch 2.1** Small-grain roughness for fixing boundary-layer transition in NASA tests (typically 0.0042 inch carborundum grains for a 24 inch chord model)



**Sketch 2.2a**



**Sketch 2.2b**

- (a) Large-grain roughness for fixing boundary-layer transition in NACA tests (typically 0.011 inch carborundum grains for a 24 inch chord model, covering 5 to 10 per cent of treated surface area)

- (b) Ice formation

A factor is given in Section 6 that has to be applied for modern, rear-loaded, aerofoils which terminate with a small trailing-edge base thickness and incorporate large rear camber as illustrated in Sketch 1.1. Finally, the effect of Mach number on  $C_{Lm}$ , for  $M \leq 0.4$ , is obtained from Section 7.

To apply the method presented in this Item various aerofoil geometrical parameters are required that are defined with respect to the aerofoil chord line. For the purposes of this Item the chord line is defined as the straight line connecting the leading and trailing edges. For an aerofoil with a finite base thickness the trailing-edge point is taken as the mid-thickness point. The leading edge is defined as that unique point at which a circle centred at the trailing-edge point is tangential to the aerofoil.

The aerofoil maximum lift coefficient is obtained as follows:

$$C_{Lm} = (C_{L0} + \Delta C_L) F_S F_M \quad (2.1)$$

in which the increment  $\Delta C_L$  is obtained from Section 3 or 4 and  $C_{L0}$  is obtained from Section 5. For modern aerofoils the factor  $F_S$  is obtained from Section 6 while for conventional sections  $F_S = 1.0$ . The factor  $F_M$ , obtained from Section 7, allows for the effect of Mach number up to 0.4. For  $M \leq 0.1$ ,  $F_M = 1.0$ .

A Fortran computer program for the method of this Item is available in ESDUpac A9315, see Item No. 93015 (Reference 23).

### 3. LIFT COEFFICIENT INCREMENT FOR AEROFOILS WITH SMOOTH LEADING EDGES

For aerofoils with smooth leading edges the lift coefficient increment,  $\Delta C_L$ , in Equation (2.1) is obtained from Figure 1 or 2.

For aerofoils with  $z_{u1.25}/c < 0.017$  Figure 1 gives  $\Delta C_L$  as a function of  $z_{u1.25}/c$  and Reynolds number,  $R_c$ . For  $z_{u1.25}/c \geq 0.017$  Figure 2 gives  $\Delta C_L$  as a function of  $\tan \tau_u$  and Reynolds number,  $R_c$ . The quantity  $\tau_u$  is the angle between the chord line and a line drawn from the maximum upper-surface ordinate to the trailing-edge point (see Sketch 1.1) given by

$$\tan \tau_u = (z_{um}/c)/(1 - x_{um}/c). \quad (3.1)$$

Figures 1 and 2 were obtained from measured data given in Derivations 2, 3, 5 to 8, 10 to 15, 17 to 20 which covered the ranges of parameters given in Table 3.1

**TABLE 3.1**  
**Ranges of Parameters for Tests on**  
**Aerofoils with Smooth Leading Edges**

<i>Parameter</i>	<i>Range</i>
$t/c$	0.06 to 0.24
$z_{u1.25}/c$	0.0069 to 0.0563
$\tan \tau_u$	0.0429 to 0.2249
$R_c \times 10^{-6}$	0.7 to 9.0
$M$	0.09 to 0.47

#### 4. LIFT COEFFICIENT INCREMENT FOR AEROFOILS WITH ROUGH LEADING EDGES

The data for aerofoils with rough leading edges are presented in a manner identical to those of Section 3 for aerofoils with smooth leading edges.

For aerofoils with  $z_{u1.25}/c < 0.017$  Figure 3 gives  $\Delta C_L$  as a function of  $z_{u1.25}/c$  for  $R_c = 6 \times 10^6$ . The single Reynolds number reflects the limited test data available for these aerofoils. For  $z_{u1.25}/c \geq 0.017$  Figure 4 gives  $\Delta C_L$  as a function of  $\tan \tau_u$  and  $R_c$ .

Figures 3 and 4 were obtained from measured data given in Derivations 2, 5 and 6, which covered the ranges of parameters given in Table 4.1. The aerofoils tested had leading-edge roughness as shown in Sketch 2.2a. Data presented in Derivation 9 reveal a loss in  $C_{Lm}$  due to simulated ice formation similar to that obtained due to leading-edge roughness. It is therefore considered that the data of Figures 3 and 4 can be used to indicate the loss of  $C_{Lm}$  due to ice formation by comparison with the corresponding values for smooth aerofoils obtained from Figures 1 and 2.

**TABLE 4.1**  
**Ranges of Parameters for Tests on**  
**Aerofoils with Rough Leading Edges**

<i>Parameter</i>	<i>Range</i>
$t/c$	0.06 to 0.24
$z_{u1.25}/c$	0.0069 to 0.0563
$\tan \tau_u$	0.0429 to 0.2249
$R_c \times 10^{-6}$	0.7 to 6.0
$M$	0.09 to 0.15

## 5. LIFT COEFFICIENT AT ZERO INCIDENCE

The coefficient  $C_{L0}$  for use in Equation (2.1) is obtained by combining the lift-curve slope,  $(a_1)_0$ , for incompressible flow obtained from Item No. Aero W 01.01.05 (Reference 21) with the zero-lift angle,  $\alpha_0$ , obtained by use of Pankhurst's method in Derivation 1,

$$\alpha_0 = -\frac{\pi}{90} \sum_{i=1}^{14} (B_i z_{ci}/c), \quad (5.1)$$

where  $z_{ci} = [z_u(x_i/c) + z_l(x_i/c)] / 2.$  (5.2)

The coefficients  $B_i$  are specified in Table 5.1 for the required values of  $x_i/c$ .

**TABLE 5.1**  
**Coefficients  $B_i$  in Equation (5.1)**

$i$	$x_i/c$	$B_i$	$i$	$x_i/c$	$B_i$
1*	0	1.45	8	0.50	3.67
2	0.025	2.11	9	0.60	4.69
3	0.05	1.56	10	0.70	6.72
4	0.10	2.41	11	0.80	11.75
5	0.20	2.94	12	0.90	21.72
6	0.30	2.88	13	0.95	99.85
7	0.40	3.13	14*	1.0	-164.88

\* Note that for the present definition of chord line the terms  $i = 1$  and 14 do not contribute to  $\alpha_0$ .

Hence, the lift coefficient at zero incidence ( $\alpha = 0$ ) is given by

$$C_{L0} = -\alpha_0(a_1)_0. \quad (5.3)$$

Comparison with measured data in Derivations 2, 5, 8, 10 to 13, and 15 to 20 has shown this to be an adequate first approximation to  $C_{L0}$  and it is the method that must be used in the evaluation of  $C_{Lm}$  by Equation (2.1) in order to maintain the integrity of the original correlation. However, the issue of more recent Items, based on use of the VGK CFD code in the Transonic Aerodynamics Sub-series, means that the methods of Item Nos 72024, 97020 and 98011 (References 24 to 26), taken together, allow a more accurate evaluation of  $C_{L0}$  for use elsewhere. However, it may be noted that the difference in prediction is small in magnitude and of little consequence in the estimation of  $C_{Lm}$ .

## 6. FACTOR ON MAXIMUM LIFT COEFFICIENT FOR MODERN AEROFOILS

Analysis of measured data has revealed that modern, rear-loaded, aerofoils, which terminate with a small trailing-edge base and incorporate large rear camber, have a higher  $C_{Lm}$  than conventional aerofoils with the same  $z_{u1.25}/c$  and  $\tan \tau_u$ .

The factor,  $F_S$ , for use in Equation (2.1), is obtained from Figure 5 as a function of  $R_c$  and is applied only for modern aerofoils. For conventional aerofoils  $F_S = 1.0$ . Figure 5, which was obtained by an analysis of data from Derivations 8, 11 to 13, 15, and 17 to 20, should be used with caution for aerofoils that differ significantly from those used in its derivation, which cover the ranges of geometry given in Table 6.1.

**TABLE 6.1**  
**Geometrical Ranges for Data Used to Derive Figure 5**

<i>Parameter</i>	<i>Range</i>
$t/c$	0.13 to 0.21
$z_{u1.25}/c$	0.024 to 0.0383
$\tan \tau_u$	0.117 to 0.207
$t_b/c$	0.005 to 0.009
$[z_u(0.9) - z_l(0.9)]/z_u(0.9)$	0.64 to 1.14

Here,  $t_b$  is the trailing-edge base thickness (see Sketch 1.1) and  $[z_u(0.9) - z_l(0.9)]/z_u(0.9)$  is a measure of the amount of rear camber.

## 7. MACH NUMBER FACTOR ON MAXIMUM LIFT COEFFICIENT

As Mach number increases there is a noticeable reduction in  $C_{Lm}$ . This reduction is more marked for aerofoils with smaller leading-edge radii, which have increased leading-edge peak suction.

The Mach number factor,  $F_M$ , is given by

$$F_M = 1 - F_1 F_2, \quad (7.1)$$

where  $F_1$  is given in Figure 6 as a function of  $M$ , and  $F_2$  is given in Figure 7 as a function of the parameter  $[z_u(0.05) - z_u(0.01)]/c$ .

The parameters  $F_1$  and  $F_2$  are based on data from Derivations 7, 8, 10 to 12, 15, 16, and 18 to 20.



## 8. ACCURACY

The accuracy of the method presented in this Item can be assessed from a comparison of measured and estimated values of  $C_{Lm}$ . The data for comparison have been considered in groups corresponding to aerofoil type and surface condition and the standard deviations for each group are presented in Tables 8.1 to 8.5 below, which include the number of data points for each Reynolds number.

**TABLE 8.1**  
**NACA Conventional Symmetric Aerofoils – Smooth Leading Edge**

$R_c$	Standard Deviation	Number of Data Points
$1 \times 10^6$	0.065	2
$2 \times 10^6$	0.055	2
$3 \times 10^6$	0.068	27
$6 \times 10^6$	0.047	27
$9 \times 10^6$	0.061	27
All $R_c$	0.059	85

**TABLE 8.2**  
**NACA Conventional Cambered Aerofoils – Smooth Leading Edge**

$R_c$	Standard Deviation	Number of Data Points
$1 \times 10^6$	0.095	11
$2 \times 10^6$	0.098	14
$3 \times 10^6$	0.085	64
$6 \times 10^6$	0.086	68
$9 \times 10^6$	0.076	63
All $R_c$	0.084	220

**TABLE 8.3**  
**NASA Modern Cambered Aerofoils – Smooth Leading Edge**  
**(including cases with minimum roughness, Sketch 2.1)**

$R_c$	Standard Deviation	Number of Data Points
$2 \times 10^6$	0.081	18
$3 \times 10^6$	0.085	18
$6 \times 10^6$	0.091	18
$9 \times 10^6$	0.080	16
All $R_c$	0.084	70

**TABLE 8.4**  
**NACA Conventional Symmetric Aerofoils – Rough Leading Edge**  
(Sketch [2.2a](#))

$R_c$	<i>Standard Deviation</i>	<i>Number of Data Points</i>
$1 \times 10^6$	0.045	2
$2 \times 10^6$	0.081	2
$6 \times 10^6$	0.082	27
All $R_c$	0.080	31

**TABLE 8.5**  
**NACA Conventional Cambered Aerofoils – Rough Leading Edge**  
(Sketch [2.2a](#))

$R_c$	<i>Standard Deviation</i>	<i>Number of Data Points</i>
$1 \times 10^6$	0.051	10
$2 \times 10^6$	0.051	10
$6 \times 10^6$	0.096	67
All $R_c$	0.088	87

## 9. DERIVATION AND REFERENCES

### 9.1 Derivation

The Derivation lists selected sources that have assisted in the preparation of this Item.

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## 10. EXAMPLES

### 10.1 Example 1

The maximum lift coefficient is to be estimated for a two-dimensional NACA 65-210 aerofoil section with a smooth leading edge. Estimates are required for Reynolds numbers of 3, 6 and  $9 \times 10^6$  at a Mach number of 0.10. For the aerofoil it can be assumed that the trailing-edge angle,  $\tau$ , is zero and that boundary layer transition occurs at  $0.3c$ .

The required aerofoil surface ordinates have the following values.

**TABLE 10.1**

$x/c$	$z_u/c$	$z_l/c$	$x/c$	$z_u/c$	$z_l/c$
0	0	0	0.50	0.0592	-0.0371
0.01	0.012	-0.010	0.60	0.0522	-0.0308
0.0125	0.013	-0.0105	0.70	0.0413	-0.0218
0.025	0.018	-0.014	0.80	0.0278	-0.0119
0.05	0.025	-0.019	0.90	0.0133	-0.0029
0.10	0.036	-0.025	0.95	0.0062	0.0001
0.20	0.0495	-0.0334	0.99	0.00124	0.00002
0.30	0.0570	-0.0379	1.0	0	0
0.40	0.0607	-0.0392			

The procedure is first to calculate, from Section 5, the lift coefficient at zero incidence,  $C_{L0}$ , then to calculate the lift coefficient increment,  $\Delta C_L$ , from Section 3. The values of  $C_{Lm}$  are then obtained from Equation (2.1) with factors  $F_S = 1.0$  for a conventional aerofoil section and  $F_M = 1.0$  for  $M = 0.1$ .

The calculations are carried out using the following steps.

- (i) From Equation (5.1), Table 5.1 and Table 10.1 the zero-lift angle is calculated as

$$\alpha_0 = -0.0274 \text{ rad.}$$

- (ii) From use of Reference 21 the values of  $(a_1)_0$  are calculated.

- (iii) The lift coefficient at zero incidence,  $C_{L0}$ , is calculated from Equation (5.3).

- (iv) From Table 10.1  $z_{u1.25}/c = 0.013$  and  $\Delta C_L$  is obtained from Figure 1.

- (v) Finally, the values of  $C_{Lm}$  are evaluated using Equation (2.1) which, with  $F_S = 1$  and  $F_M = 1.0$ , simplifies to

$$C_{Lm} = C_{L0} + \Delta C_L.$$

The results of the calculations are summarised in Table 10.2.

TABLE 10.2

$R_c$	$3 \times 10^6$	$6 \times 10^6$	$9 \times 10^6$
$(a_1)_0$	5.89	6.01	6.06
$C_{L0}$	0.161	0.164	0.166
$\Delta C_L$	1.122	1.194	1.234
$C_{Lm}$	1.28	1.36	1.40

## 10.2 Example 2

The effect of coarse surface roughness or ice formation over the leading edge on the maximum lift coefficient is to be estimated for the aerofoil of Example 1.

The Reynolds number is  $6 \times 10^6$  and the Mach number is 0.1.

It can be assumed that the roughness shifts the boundary layer transition forward to the leading edge.

From Example 1,  $C_{Lm} = 1.36$  for the aerofoil with a smooth leading edge.

For the aerofoil with a rough leading edge the procedure of Example 1 is followed but with the lift increment,  $\Delta C_L$ , being obtained from Figure 3.

In this case with  $z_{u1.25}/c = 0.013$  the value of  $\Delta C_L$  is 0.886. Also, the effect of the shift in boundary layer transition gives a slightly reduced  $C_{L0}$  value of 0.163.

$$\begin{aligned}
 \text{Thus, } C_{Lm} &= C_{L0} + \Delta C_L \\
 &= 0.163 + 0.886 \\
 &= 1.05.
 \end{aligned}$$

The loss in  $C_{Lm}$  due to coarse leading-edge roughness or ice formation is given by

$$\Delta C_{Lm} = 1.36 - 1.05 = 0.31.$$

### 10.3 Example 3

The effect of Mach number on the maximum lift coefficient is to be estimated for the aerofoil used in Example 1 with a smooth leading edge. Estimates are required for Mach numbers up to 0.4 at a Reynolds number of  $6 \times 10^6$ .

The values of  $C_{Lm}$  are estimated using Equation (2.1) which, with  $F_S = 1.0$ , simplifies to

$$C_{Lm} = (C_{L0} + \Delta C_L) F_M.$$

From Example 1,  $(C_{L0} + \Delta C_L) = 1.36$ .

The factor  $F_M$  is obtained from Equation (7.1), *i.e.*

$$F_M = 1 - F_1 F_2,$$

in which  $F_1$  is found from Figure 6 and  $F_2$ , from Figure 7, corresponds to

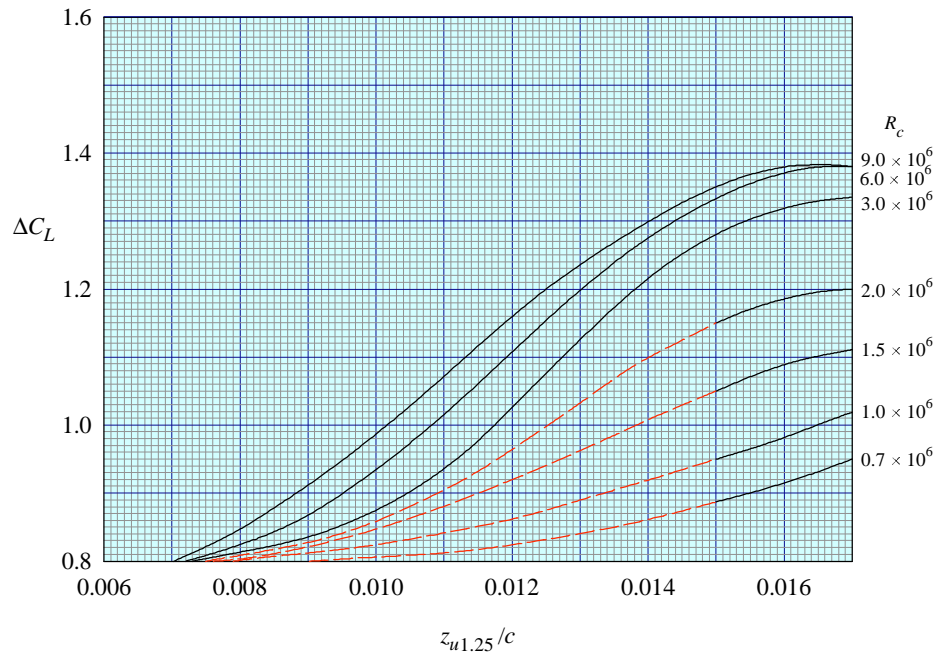
$$[z_u(0.05) - z_u(0.01)]/c = 0.013.$$

The calculations are tabulated in Table 10.3.

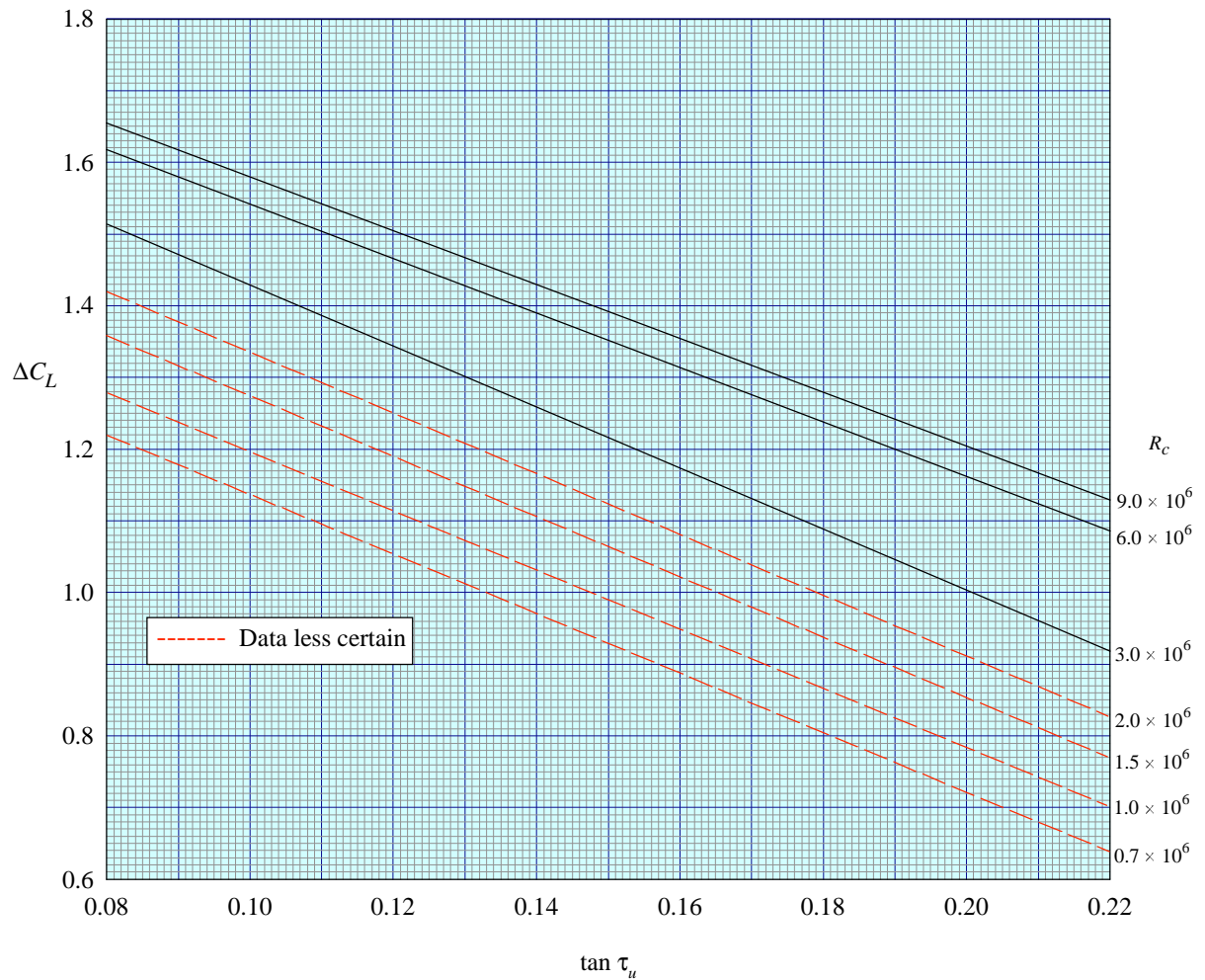
**TABLE 10.3**

$M$	0.1	0.2	0.3	0.4
$F_1$ (Figure 6)	0	0.036	0.100	0.141
$F_2$ (Figure 7)	2.07	2.07	2.07	2.07
$F_M$ (Equation (7.1))	1.0	0.925	0.793	0.708
$C_{Lm}$	1.36	1.26	1.08	0.96

## LIFT COEFFICIENT INCREMENT FOR AEROFOILS WITH SMOOTH LEADING EDGES



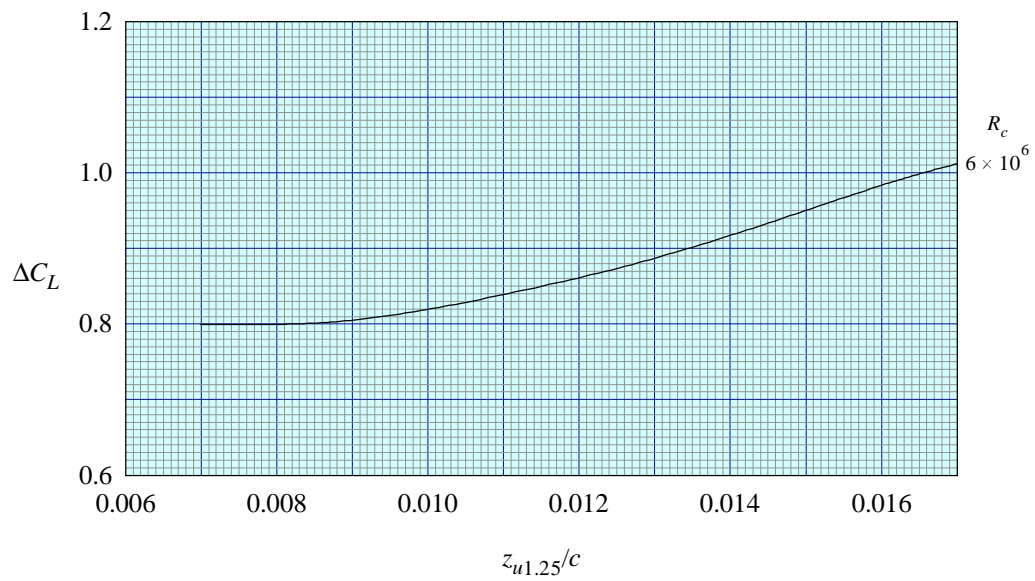
**FIGURE 1**  $z_{u1.25}/c < 0.017$



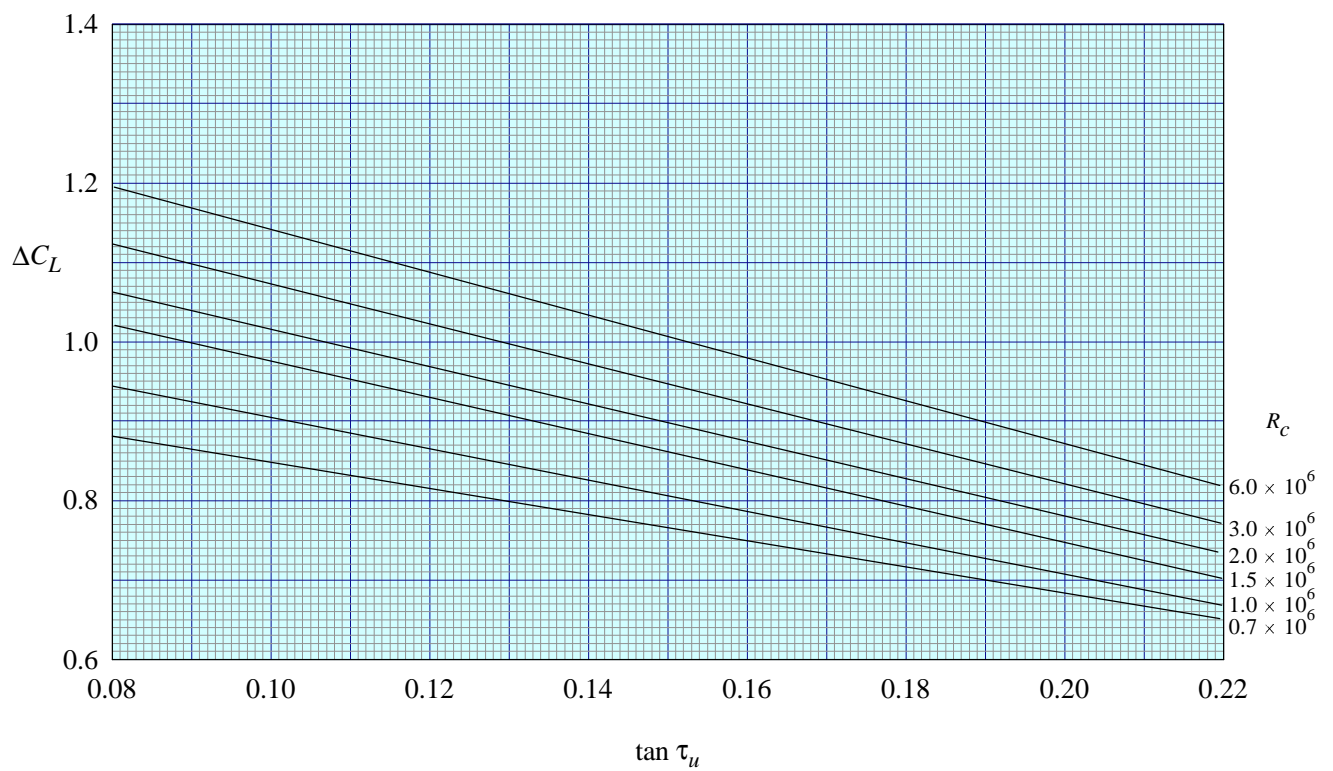
**FIGURE 2**  $z_{u1.25}/c \geq 0.017$



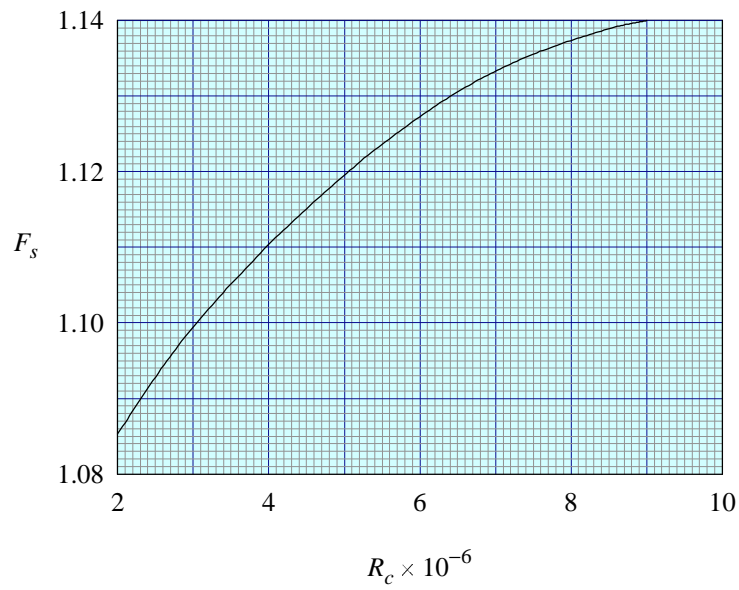
## LIFT COEFFICIENT INCREMENT FOR AEROFOILS WITH ROUGH LEADING EDGES



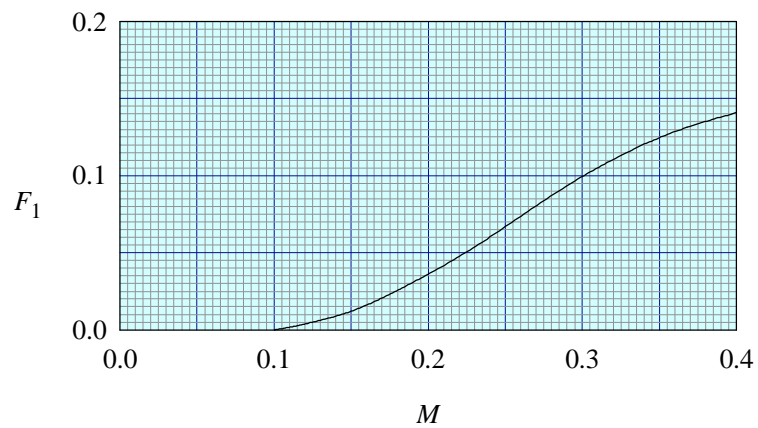
**FIGURE 3**  $z_{u1.25}/c < 0.017$



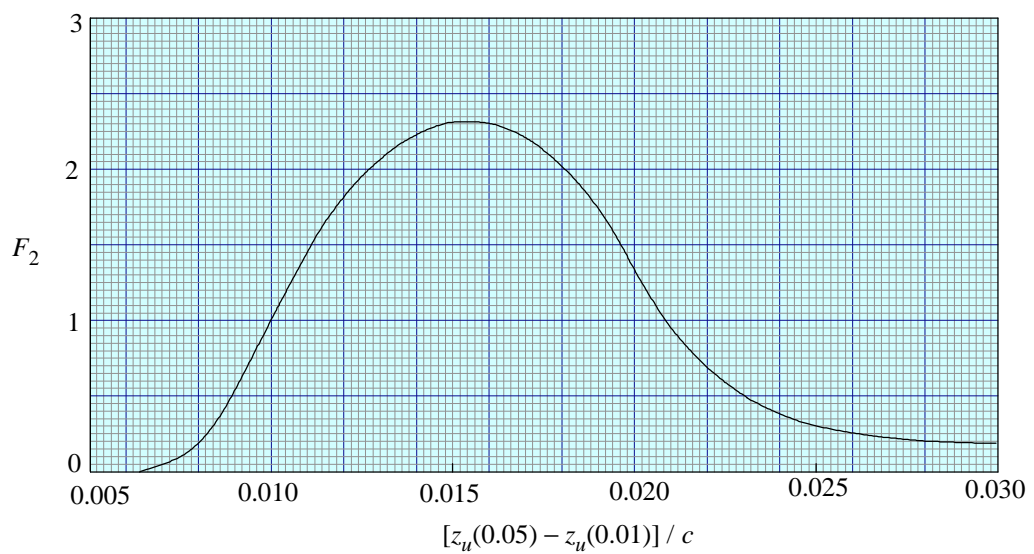
**FIGURE 4**  $z_{u1.25}/c \geq 0.017$



**FIGURE 5 FACTOR ON  $C_{Lm}$  FOR MODERN AEROFOILS**



**FIGURE 6 PARAMETER IN EQUATION (7.1)**



**FIGURE 7 PARAMETER IN EQUATION (7.1)**

## THE PREPARATION OF THIS DATA ITEM

The work on this particular Item, which supersedes Item No. Aero W.01.01.06, was monitored and guided by the Aerodynamics Committee, which first met in 1942 and now has the following membership:

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The technical work involved in the initial assesement of the available information and the construction and subsequent development of the Item was carried out under contract to ESDU by Mr C.D. Hollis and Mr R.G. Williams of British Aerospace plc, Aircraft Group, Bristol.