

# PESQUISA OPERACIONAL I

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# MODELOS DE TRANSPORTE

- definir se uma determinada carga deve ser transportada
- identificação do destino final da carga a ser transportada
- seleção do veículo e/ou modalidade de transporte a serem utilizados
- identificação da melhor rota a ser seguida



FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	120
2	15	10	12	80
3	3	9	10	80
CAP.	150	70	60	280

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	120
2	15	10	12	80
3	3	9	10	80
CAP.	150	70	60	<b>280</b>

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	120
2	15	10	12	80
3	3	9	10	<del>80</del> 0
	80	---	---	
CAP.	<del>150</del> 70	70	60	

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	<del>120</del> 50
		70		
2	15	10	12	80
		---		
3	3	9	10	<del>80</del> 0
	80	---	---	
CAP.	<del>150</del> 70	<del>70</del> 0	60	

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8 ---	5 70	6 50	<del>120</del> <del>50</del> 0
2	15	10 ---	12	80
3	3 80	9 ---	10 ---	<del>80</del> 0
CAP.	<del>150</del> 70	<del>70</del> 0	<del>60</del> 10	

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8 ---	5 70	6 50	<del>120</del> <del>50</del> 0
2	15	10 ---	12 10	<del>80</del> 70
3	3 80	9 ---	10 ---	<del>80</del> 0
CAP.	<del>150</del> 70	<del>70</del> 0	<del>60</del> <del>10</del> 0	



FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	<del>120</del> <del>50</del> 0
	---	70	50	
2	15	10	12	<del>80</del> <del>70</del> 0
	70	---	10	
3	3	9	10	<del>80</del> 0
	80	---	---	
CAP.	<del>150</del> <del>70</del> 0	<del>70</del> 0	<del>60</del> <del>10</del> 0	

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8 ---	5 70	6 50	120
2	15 70	10 ---	12 10	80
3	3 80	9 ---	10 ---	80
CAP.	150	70	60	280

$$C = \$ 2.060,00$$

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	120
2	15	10	12	80
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CAP.	150	70	60	280

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2	15	10	12	<del>80</del> 10
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1	8	5	6	120
		---		
2	15	10	12	<del>80</del> <del>10</del> 0
	---	70	10	
3	3	9	10	80
		---		
CAP.	150	<del>70</del> 0	<del>60</del> 50	

FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	120
		---		
2	15	10	12	<del>80</del> <del>10</del> 0
	---	70	10	
3	3	9	10	<del>80</del> 0
	80	---	---	
CAP.	<del>150</del> 70	<del>70</del> 0	<del>60</del> 50	

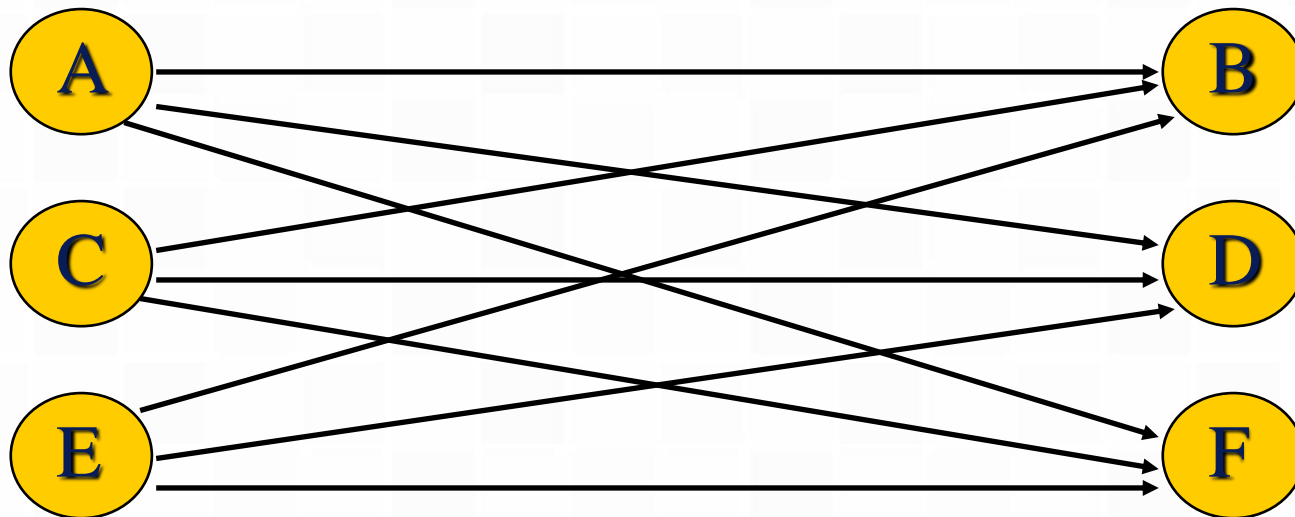
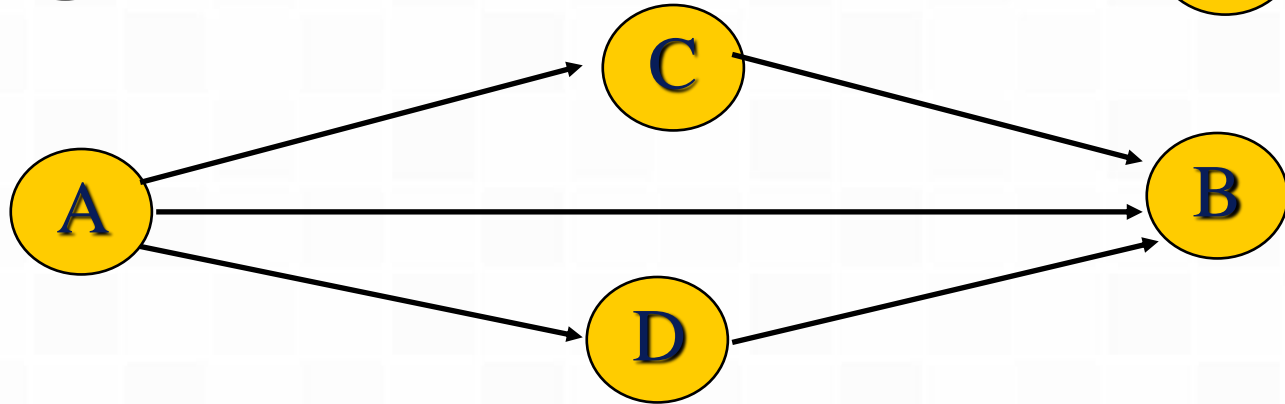
FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8	5	6	<del>120</del> 70
		---	50	
2	15	10	12	<del>80</del> <del>10</del> 0
	---	70	10	
3	3	9	10	<del>80</del> 0
	80	---	---	
CAP.	<del>150</del> 70	<del>70</del> 0	<del>60</del> <del>50</del> 0	



FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8 70	5 ---	6 50	<del>120</del> <del>70</del> 0
2	15 ---	10 70	12 10	<del>80</del> <del>10</del> 0
3	3 80	9 ---	10 ---	<del>80</del> 0
CAP.	<del>150</del> <del>70</del> 0	<del>70</del> 0	<del>60</del> <del>50</del> 0	

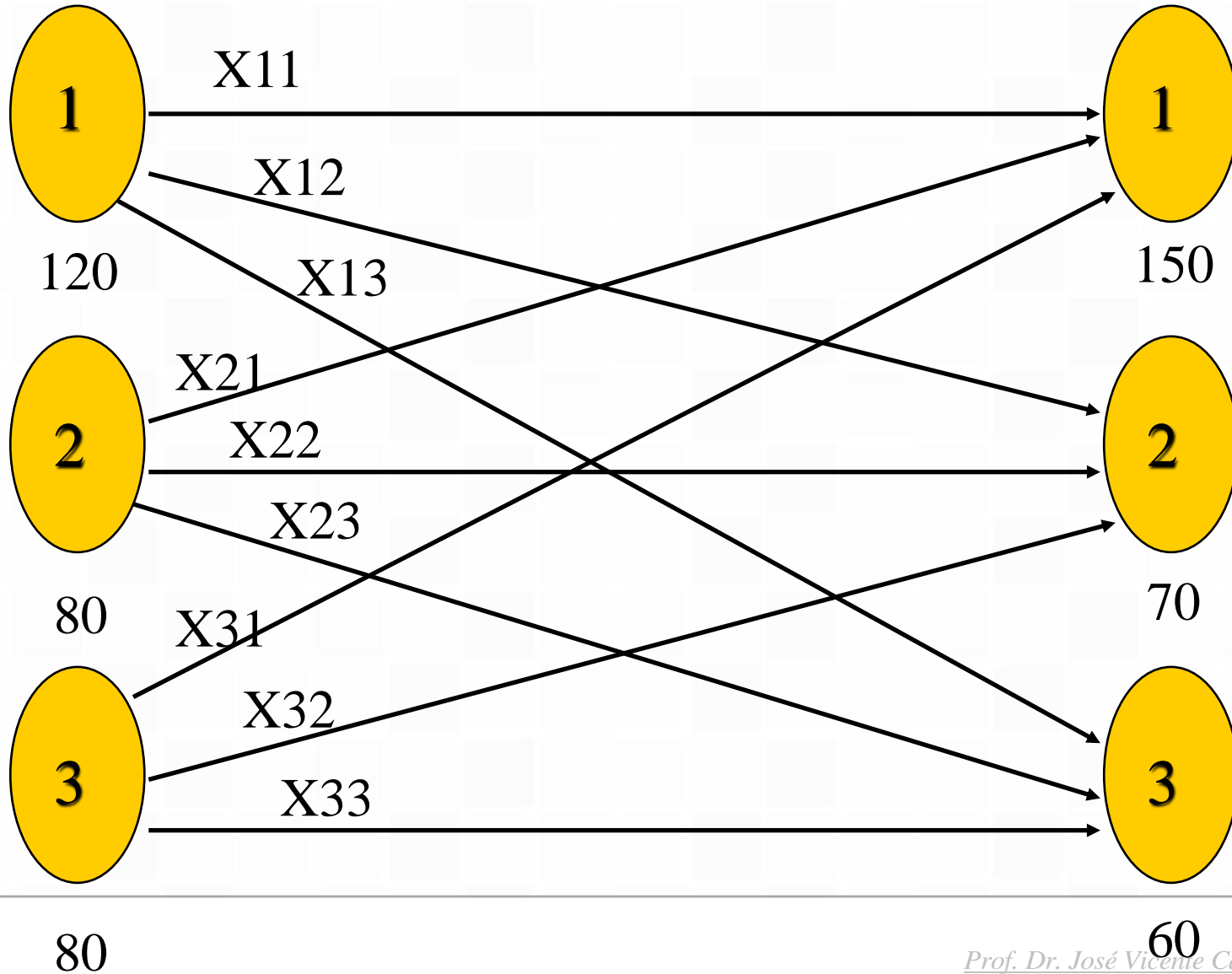
FÁB.	DEPÓSITO			PROD.
	1	2	3	
1	8 70	5 -----	6 50	120
2	15 -----	10 70	12 10	80
3	3 80	9 -----	10 -----	80
CAP.	150	70	60	280

$$C = \$ 1.920,00$$



FÁBRICA

DEPÓSITO



Assim sendo, tem-se:

$$\text{Min } 8X_{11} + 5X_{12} + 6X_{13} + 15X_{21} + 10X_{22} + 12X_{23} + 3X_{31} + 9X_{32} + 10X_{33}$$

sujeito a

$$\text{FAB1) } X_{11} + X_{12} + X_{13} = 120$$

$$\text{FAB2) } X_{21} + X_{22} + X_{23} = 80$$

$$\text{FAB3) } X_{31} + X_{32} + X_{33} = 80$$

$$\text{DEP1) } X_{11} + X_{21} + X_{31} = 150$$

$$\text{DEP2) } X_{12} + X_{22} + X_{32} = 70$$

$$\text{DEP3) } X_{13} + X_{23} + X_{33} = 60$$

$$X_{11}, X_{12}, X_{13}, X_{21}, X_{22}, X_{23}, X_{31}, X_{32}, X_{33} \geq 0$$

$$\text{Min } Z = \sum_{i=1}^m \sum_{j=1}^n c_{ij} x_{ij}$$

*sujeito a*

$$\sum_{j=1}^n x_{ij} \leq s_i \quad , \quad \text{para } i = 1, \dots, m$$

$$\sum_{i=1}^m x_{ij} \geq d_j \quad , \quad \text{para } j = 1, \dots, n$$

$$x_{ij} \geq 0 \quad , \quad \text{para } i = 1, \dots, m \quad \text{e} \quad j = 1, \dots, n$$

onde:  $c_{ij}$  = custo do transporte entre  $i$  e  $j$ ;

$x_{ij}$  = quantidade a ser movimentada de  $i$  até  $j$ ;

$s_i$  = quantidade ofertada em  $i$ ;

$d_j$  = quantidade demandada em  $j$ .

UTILIZE O SOFTWARE  
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What'sBest! lets you build linear, nonlinear, and integer models in Excel. Models are easy to build and understand using standard

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LINGO is a comprehensive tool designed to help you build and solve linear, optimization models quickly, easily, and efficiently.

### LINDO API

LINDO API creates optimization applications. It allows you to plug the power of the LINDO solver right into customized



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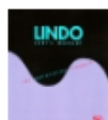
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LINGO is a comprehensive tool designed to help you build and solve linear, nonlinear, and integer optimization models quickly, easily, and efficiently. LINGO includes a powerful modeling language, a full-featured environment for building and editing problems, the ability to read and write to Excel and databases, and a set of fast built-in solvers.



#### [Download LINDO API](#)

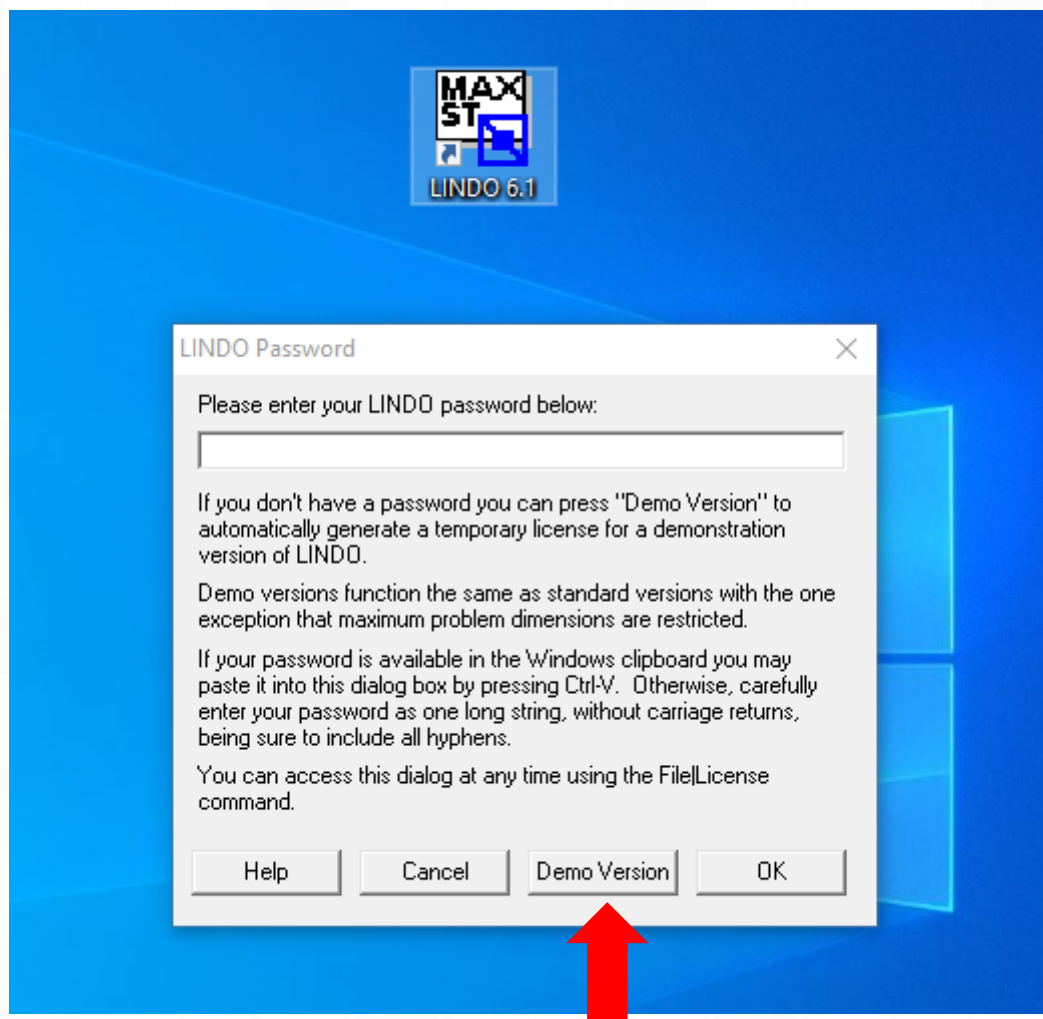
With the LINDO API, you can easily create your own optimization applications. It allows you to plug the power of the LINDO solver right into customized applications that you have written.



#### [Download Classic LINDO](#)

Classic LINDO's simple interface and straightforward model expression style make it easy to learn and use. Classic LINDO is appropriate for building and solving moderately sized linear and integer models.





## TELA DE ENTRADA DO SOFTWARE LINDO

The screenshot shows the LINDO software interface with the following content:

**LINDO**  
File Edit Solve Reports Window Help

**C:\PROJETOS\Cursos\AULALI-1\TRAN-P64.LTX**

MIN  $8X_{11} + 5X_{12} + 6X_{13} + 15X_{21} + 10X_{22} + 12X_{23} + 3X_{31} + 9X_{32} + 10X_{33}$   
ST  
 FAB1)  $X_{11} + X_{12} + X_{13} = 120$   
 FAB2)  $X_{21} + X_{22} + X_{23} = 80$   
 FAB3)  $X_{31} + X_{32} + X_{33} = 80$   
 DEP1)  $X_{11} + X_{21} + X_{31} = 150$   
 DEP2)  $X_{12} + X_{22} + X_{32} = 70$   
 DEP3)  $X_{13} + X_{23} + X_{33} = 60$

## TELA DE SAÍDA DO SOFTWARE LINDO

The screenshot shows the LINDO Reports Window with the following content:

**LINDO**  
File Edit Solve Reports Window Help

**Reports Window**

LP OPTIMUM FOUND AT STEP 6

OBJECTIVE FUNCTION VALUE

1) 1920.000

VARIABLE	VALUE	REDUCED COST
X11	70.000000	0.000000
X12	0.000000	1.000000
X13	50.000000	0.000000
X21	0.000000	1.000000
X22	70.000000	0.000000
X23	10.000000	0.000000
X31	80.000000	0.000000
X32	0.000000	10.000000
X33	0.000000	9.000000

ROW	SLACK OR SURPLUS	DUAL PRICES
FAB1)	0.000000	6.000000
FAB2)	0.000000	0.000000
FAB3)	0.000000	11.000000
DEP1)	0.000000	-14.000000
DEP2)	0.000000	-10.000000
DEP3)	0.000000	-12.000000

