

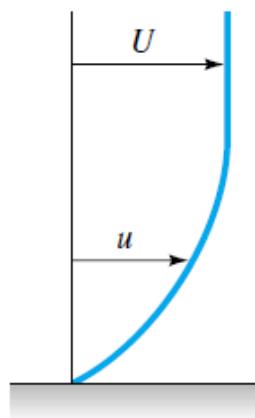
# **Fenômenos de Transporte I**

Fluid Mechanics – 4th ed. -Frank M. White

## **ESCOAMENTO EXTERNO**

# EFEITO DO GRADIENTE DE PRESSÃO NO PERFIL DE VELOCIDADES

Fluid Mechanics – 4th ed. -Frank M. White

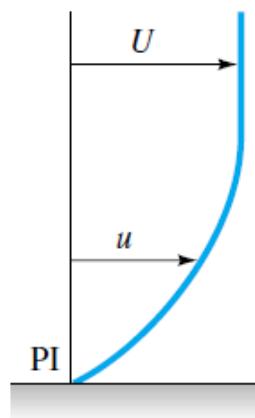


(a) Favorable gradient:

$$\frac{dU}{dx} > 0$$

$$\frac{dp}{dx} < 0$$

No separation,  
PI inside wall

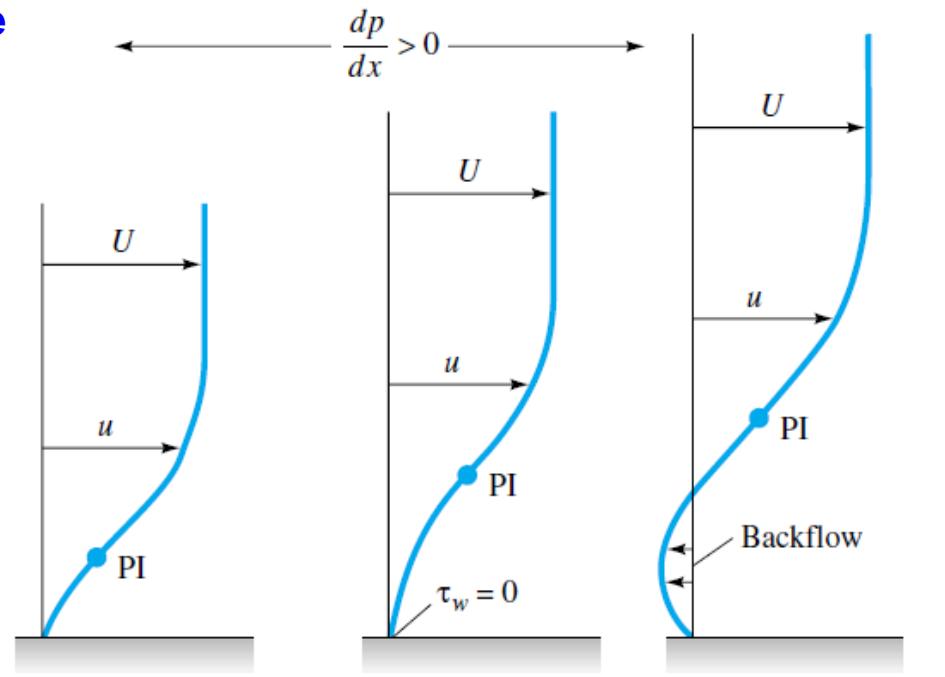


(b) Zero gradient:

$$\frac{dU}{dx} = 0$$

$$\frac{dp}{dx} = 0$$

No separation,  
PI at wall



(c) Weak adverse gradient:

$$\frac{dU}{dx} < 0$$

$$\frac{dp}{dx} > 0$$

No separation,  
PI in the flow

(d) Critical adverse gradient:

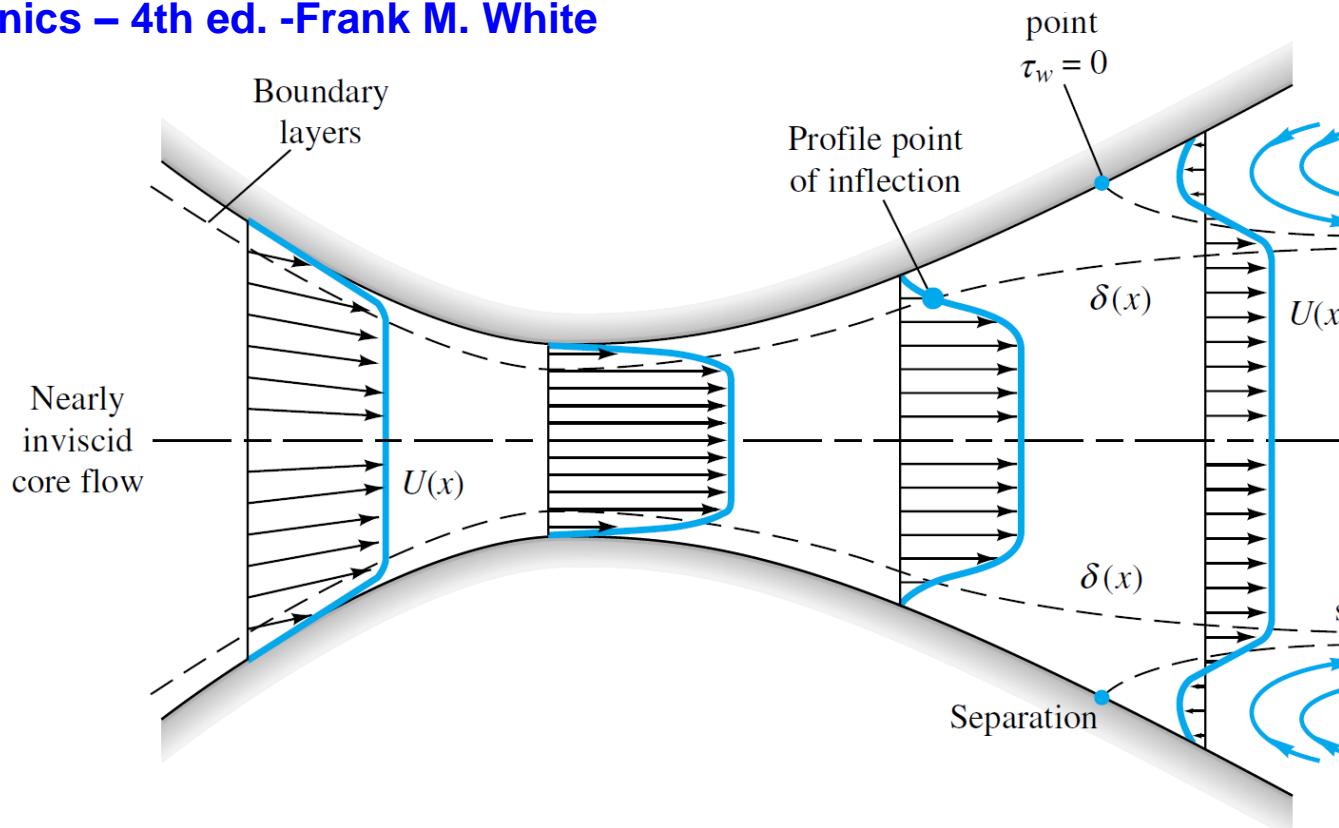
Zero slope  
at the wall:  
*Separation*

(e) Excessive adverse gradient:

Backflow  
at the wall:  
Separated  
flow region

# EFEITO DO GRADIENTE DE PRESSÃO NO PERFIL DE VELOCIDADES

Fluid Mechanics – 4th ed. -Frank M. White



Nozzle:  
Decreasing  
pressure  
and area

Increasing  
velocity

Favorable  
gradient

Throat:  
Constant  
pressure  
and area

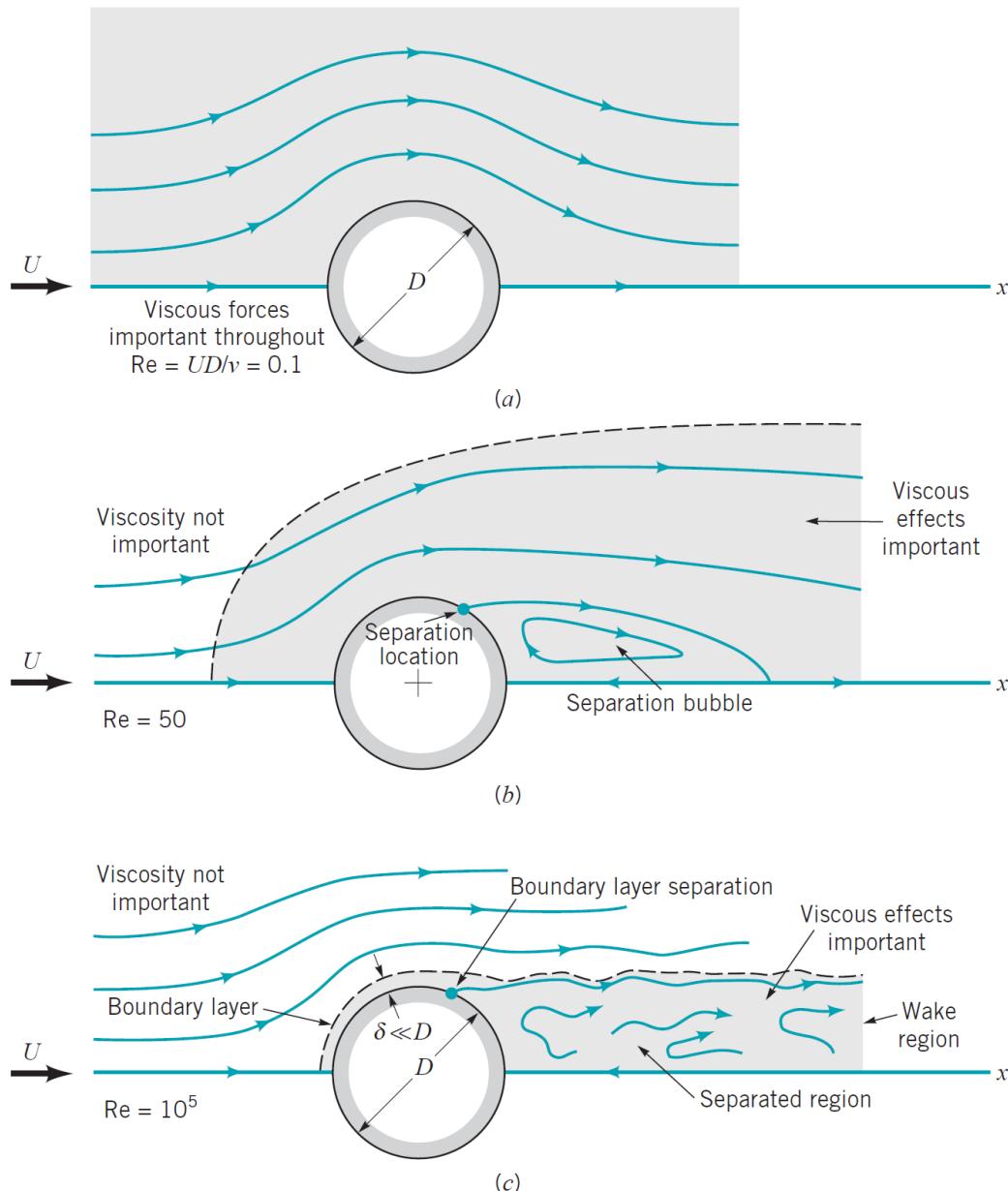
Velocity  
constant

Zero  
gradient

Diffuser:  
Increasing pressure  
and area

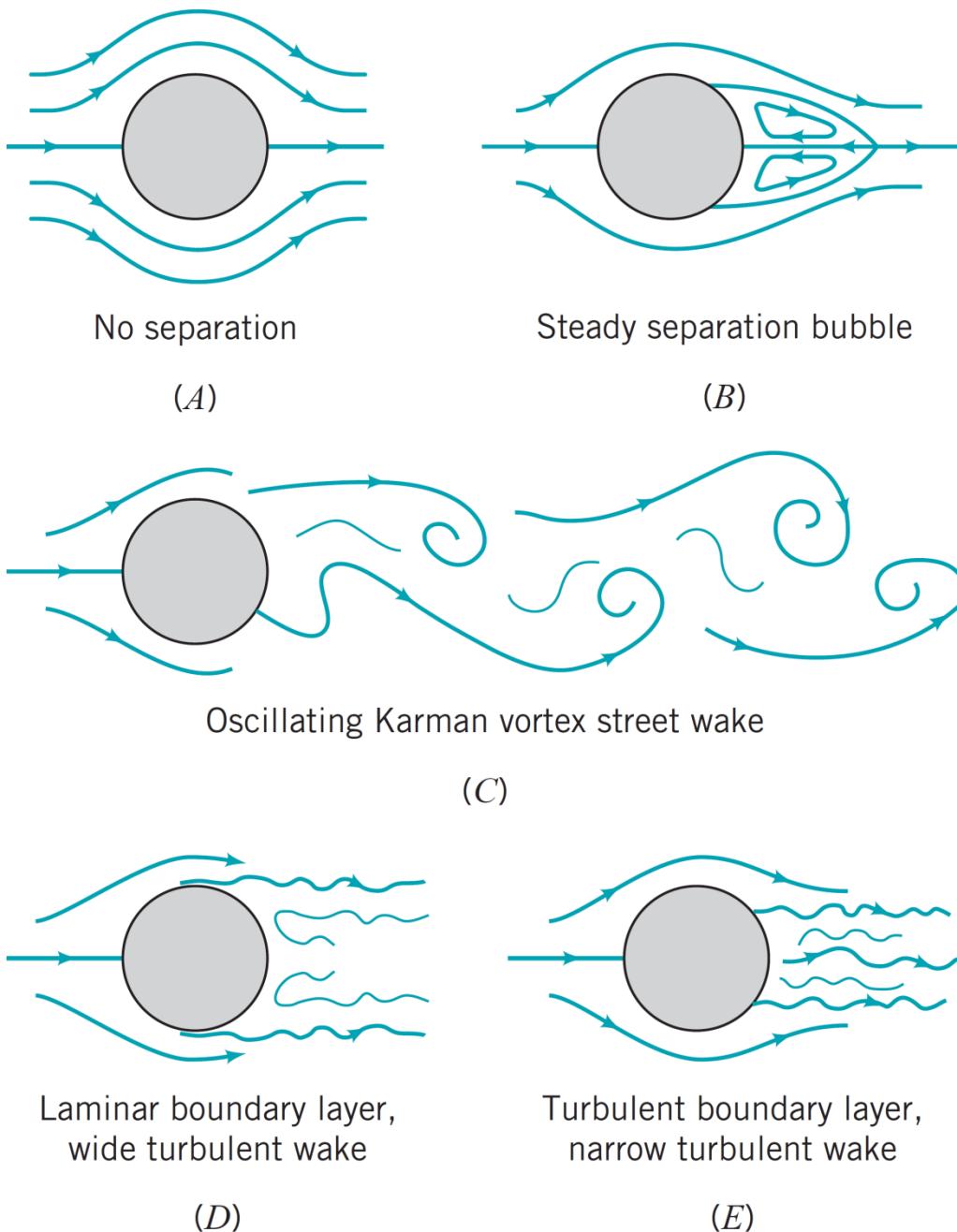
Decreasing velocity

Adverse gradient  
(boundary layer thickens)



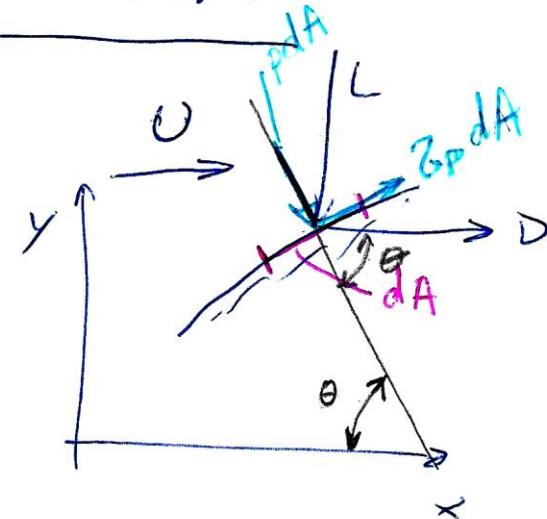
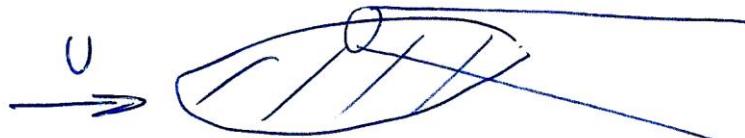
**FIGURE 9.6** Character of the steady, viscous flow past a circular cylinder: (a) low Reynolds number flow, (b) moderate Reynolds number flow, (c) large Reynolds number flow.

**FIGURE 9.21** (a) Drag coefficient as a function of Reynolds number for a smooth circular cylinder and a smooth sphere. (b) Typical flow patterns for flow past a circular cylinder at various Reynolds numbers as indicated in (a).



# EJERCIMIENTO Sobre CON AER. INÉ NJO

Aerostato sustentado.



$$dF_x = p dA (\cos \theta) + \frac{1}{2} \rho dA \sin \theta$$

$$dF_y = - (p dA) \sin \theta + \frac{1}{2} \rho dA \cos \theta$$

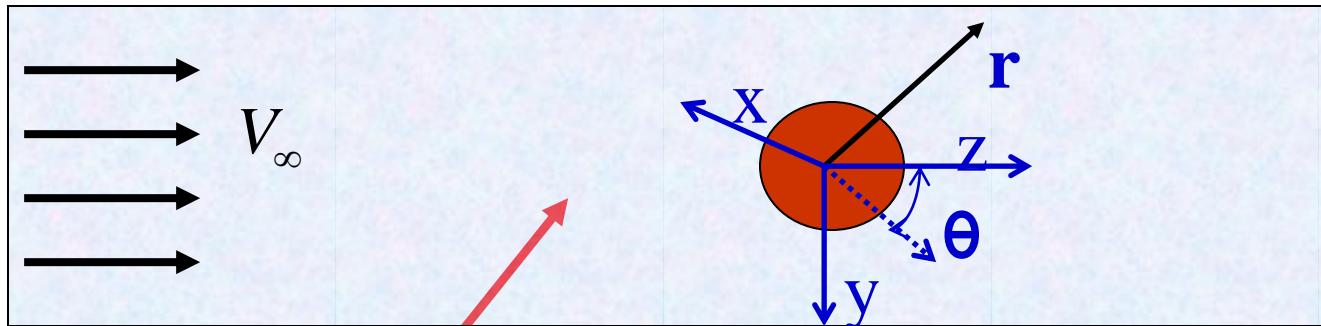
$$D = \int dF_x = \int p \sin \theta dA + \int \frac{1}{2} \rho \sin \theta dA$$

$$L = \int dF_y = - \int p \cos \theta dA + \int \frac{1}{2} \rho \cos \theta dA$$

$$C_L = \frac{L}{\frac{1}{2} \rho U^2 A} \quad \text{e} \quad C_D = \frac{D}{\frac{1}{2} \rho U^2 A}$$

Areas características. Normalmente se usa área frontal  
(1:e) a área proyectada.

# ”Lei” de Stokes – Meio Contínuo



Fluido => Equação de Navier-Stokes – pressão e velocidades

$$\rho \left( \frac{\partial \vec{V}}{\partial t} + \vec{V} \cdot \nabla \vec{V} \right) = \nabla P + \mu \nabla^2 \vec{V}$$

Regime permanente       $\text{Re} \ll 1$

•Cond. de contorno:

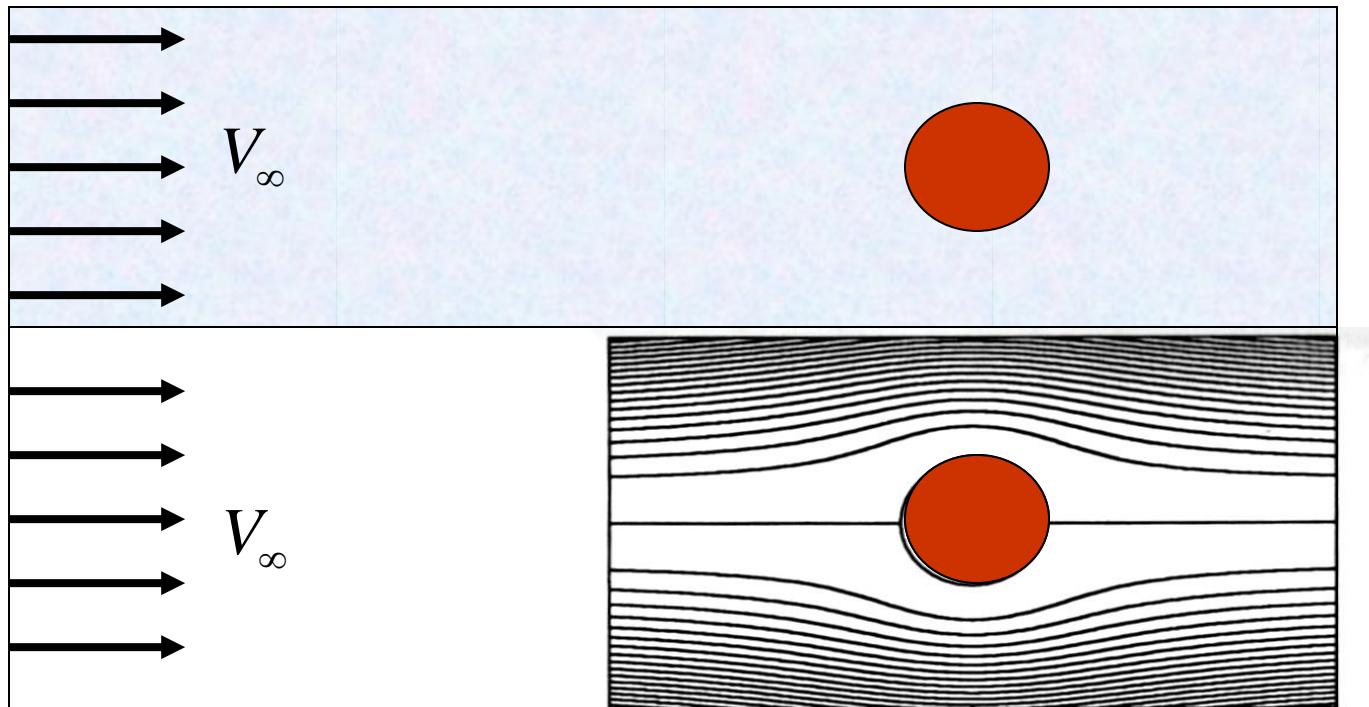
$$\begin{cases} r \rightarrow \infty, \vec{V} = V_\infty \\ r = R_p, \vec{V} = 0 \\ r \rightarrow \infty, p = p_0 \end{cases}$$

$$p = p_0 - \frac{3\mu V_\infty}{2R_p} \left( \frac{R_p}{r} \right)^2 \cos \theta$$

$$V_r = V_\infty \cos \theta \left[ 1 - \frac{3}{2} \left( \frac{R_p}{r} \right) + \frac{1}{2} \left( \frac{R_p}{r} \right)^3 \right]$$

$$V_\theta = -V_\infty \sin \theta \left[ 1 - \frac{3}{4} \left( \frac{R_p}{r} \right) - \frac{1}{4} \left( \frac{R_p}{r} \right)^3 \right]$$

## ”Lei” de Stokes – $\text{Re} < 1$

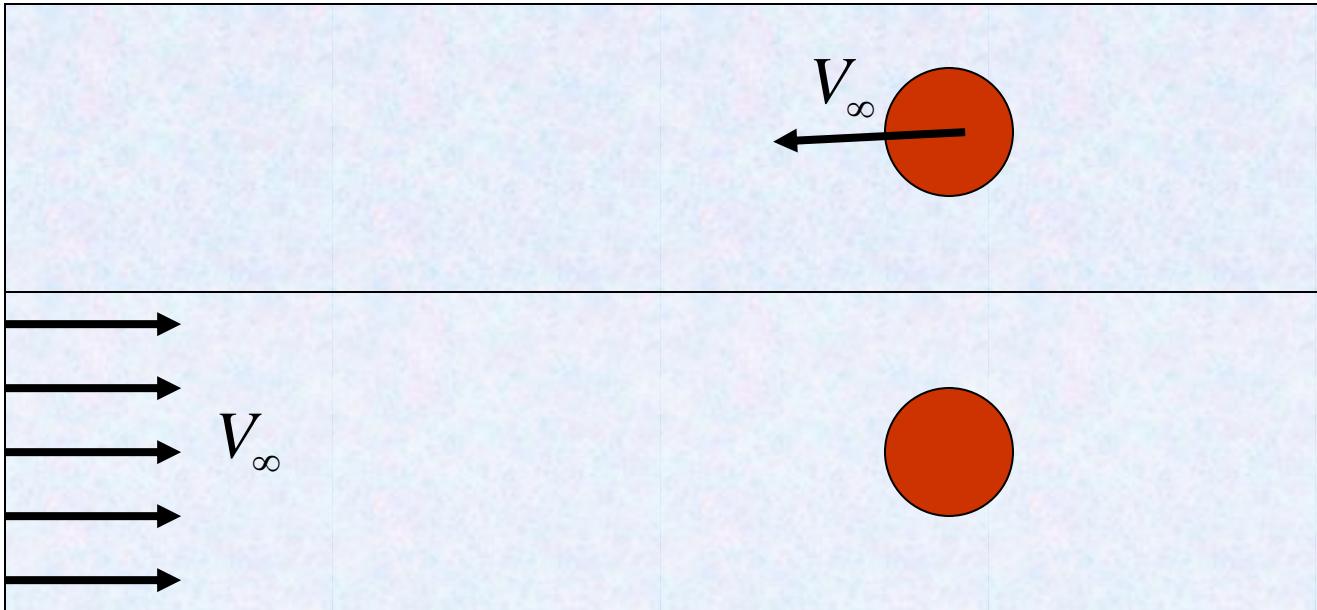


$$p = p_0 - \frac{3\mu V_\infty}{2R_p} \left( \frac{R_p}{r} \right)^2 \cos \theta$$

$$V_r = V_\infty \cos \theta \left[ 1 - \frac{3}{2} \left( \frac{R_p}{r} \right) + \frac{1}{2} \left( \frac{R_p}{r} \right)^3 \right]$$

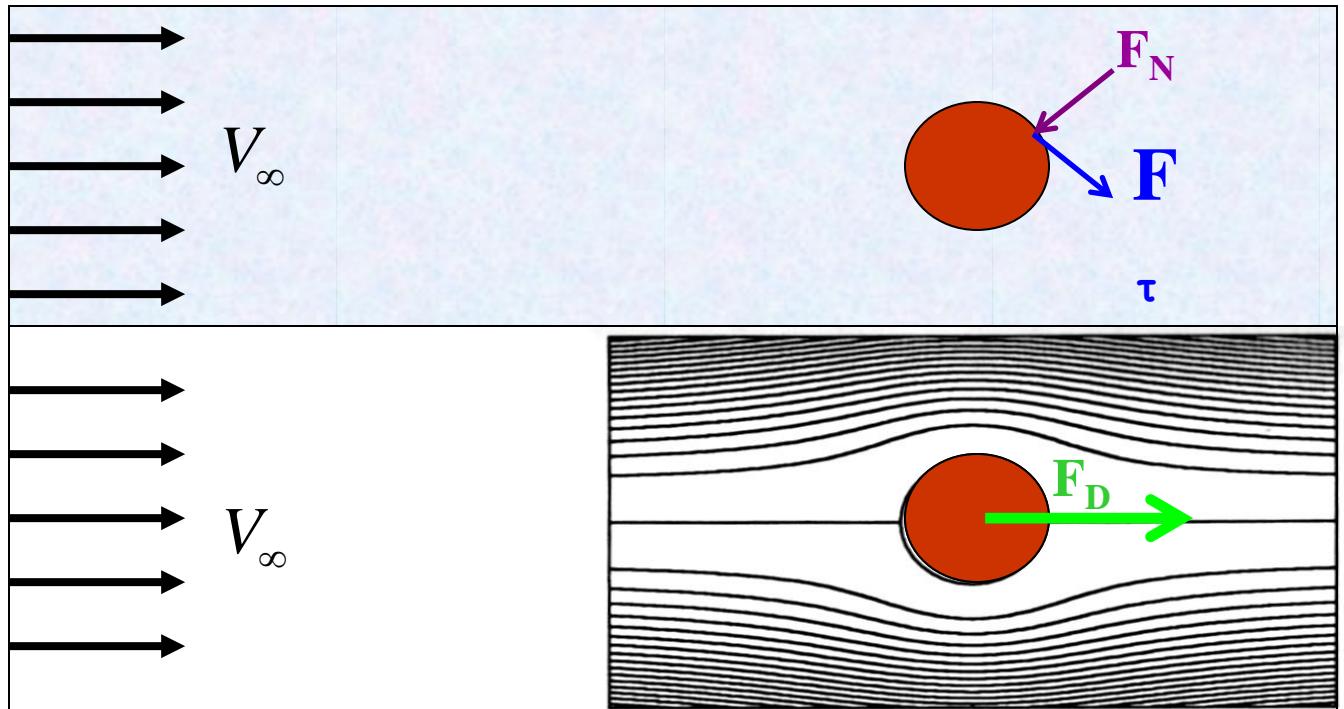
$$V_\theta = -V_\infty \sin \theta \left[ 1 - \frac{3}{4} \left( \frac{R_p}{r} \right) - \frac{1}{4} \left( \frac{R_p}{r} \right)^3 \right]$$

## ”Lei” de Stokes – Meio Contínuo



- Regime permanente
- Meio infinito
- Termos convectivos desconsiderados =>  
 $\text{Re} \ll 1$
- Fluido newtoniano
- Escoamento incompressível

## ”Lei” de Stokes – Força de Arraste (Drag)



$$p = p_0 - \frac{3\mu V_\infty}{2R_P} \cos \theta$$

$$F_n = \int^A -p d\vec{A} = 2\pi\mu V_\infty R_P$$

+

$$\tau = \frac{3\mu V_\infty}{2R_P} \left( \frac{R_P}{r} \right)^4 \sin \theta$$

$$F_\tau = \int^A \tau d\vec{A} = 4\pi\mu V_\infty R_P$$

$$F_D = 6\pi\mu V_\infty R_P$$

# Força de Arraste – Equacionamento Geral Coeficiente de Arrasto - CD

$$C_D = \frac{F_D / A_P}{\rho V_\infty^2 / 2}$$

$$\Rightarrow F_D = \frac{1}{2} C_D A_P \rho V_\infty^2 = \frac{1}{8} \pi C_D \rho D_P^2 V_\infty^2$$

$$Re = \frac{\rho V_\infty D_P}{\mu} < 1$$



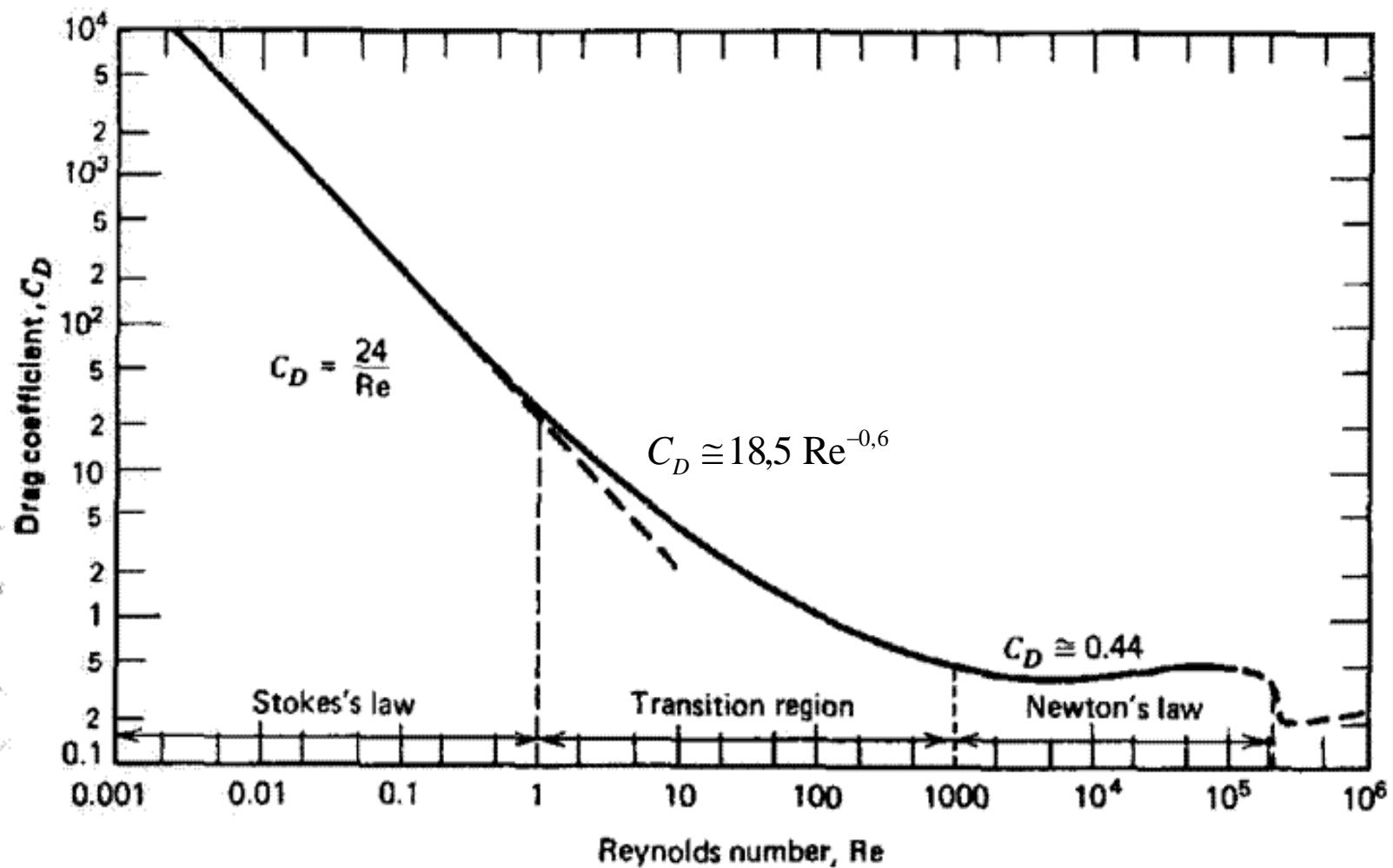
$$F_D = 6\pi\mu V_\infty R_P$$



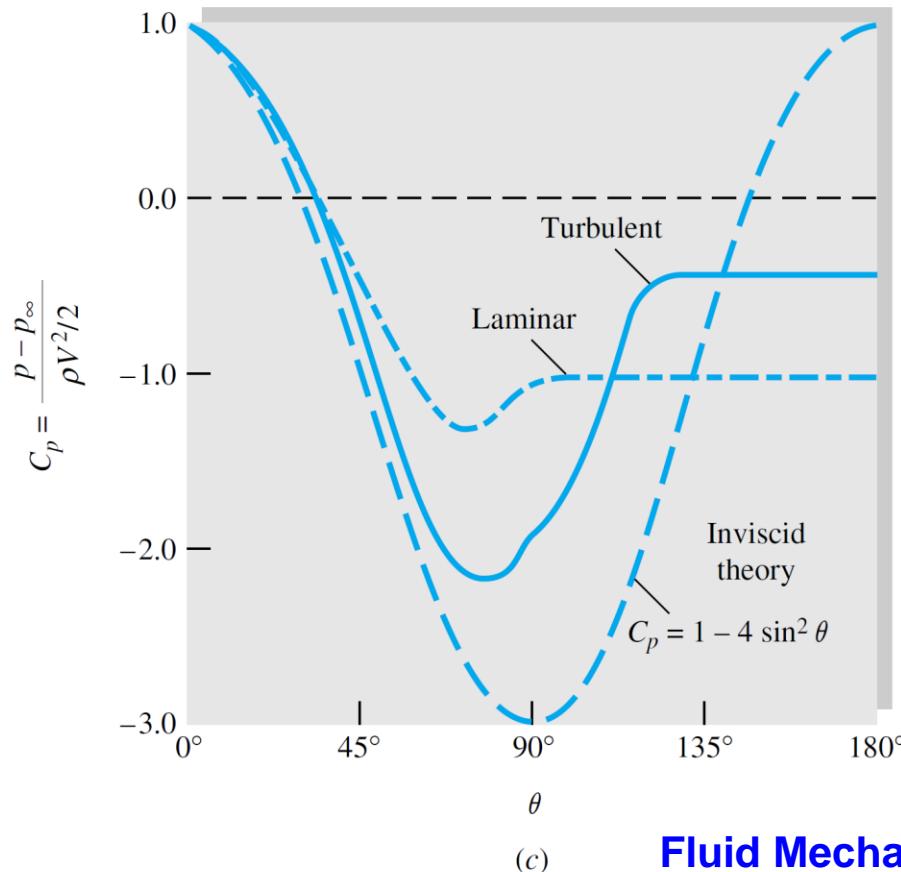
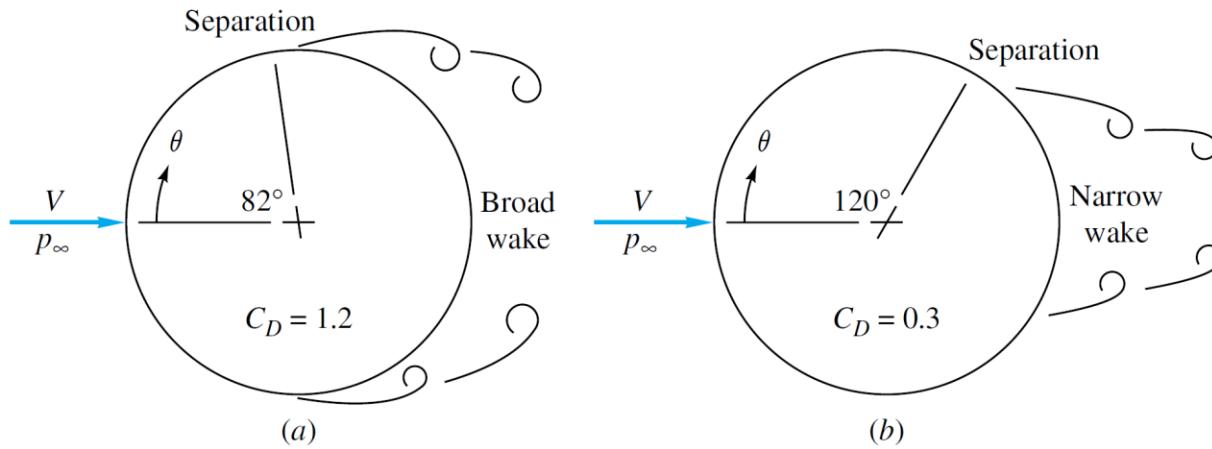
$$C_D = 24 / Re$$

$C_D$	$Re$
$24 / Re$	$Re < 1$
$18,5 Re^{-0,6}$	$1 < Re < 10^3$
0,44	$10^3 < Re < 10^5$

## ”Lei” de Stokes – Força de Arraste (Drag)

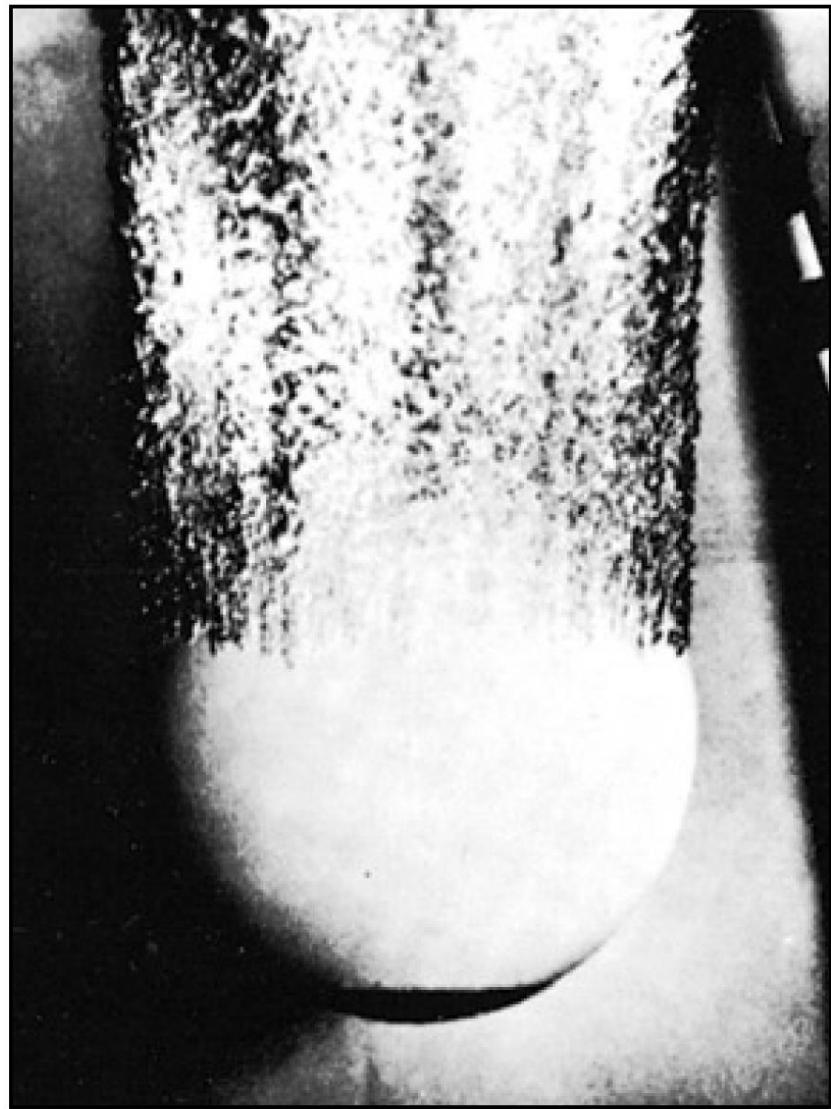


**FIGURE 3.1** Drag coefficient versus Reynolds number for spheres.





(a)



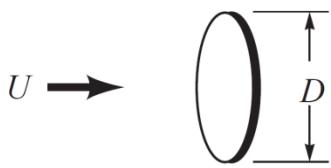
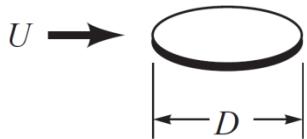
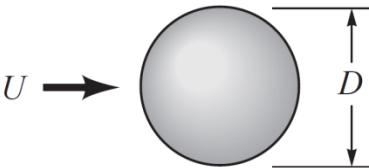
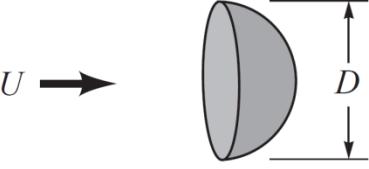
(b)

Strong differences in laminar and turbulent separation on an 8.5-in bowling ball entering water at 25 ft/s:  
(a) smooth ball, laminar boundary layer; (b) same entry, turbulent flow induced by patch of nose-sand<sub>14</sub> roughness.

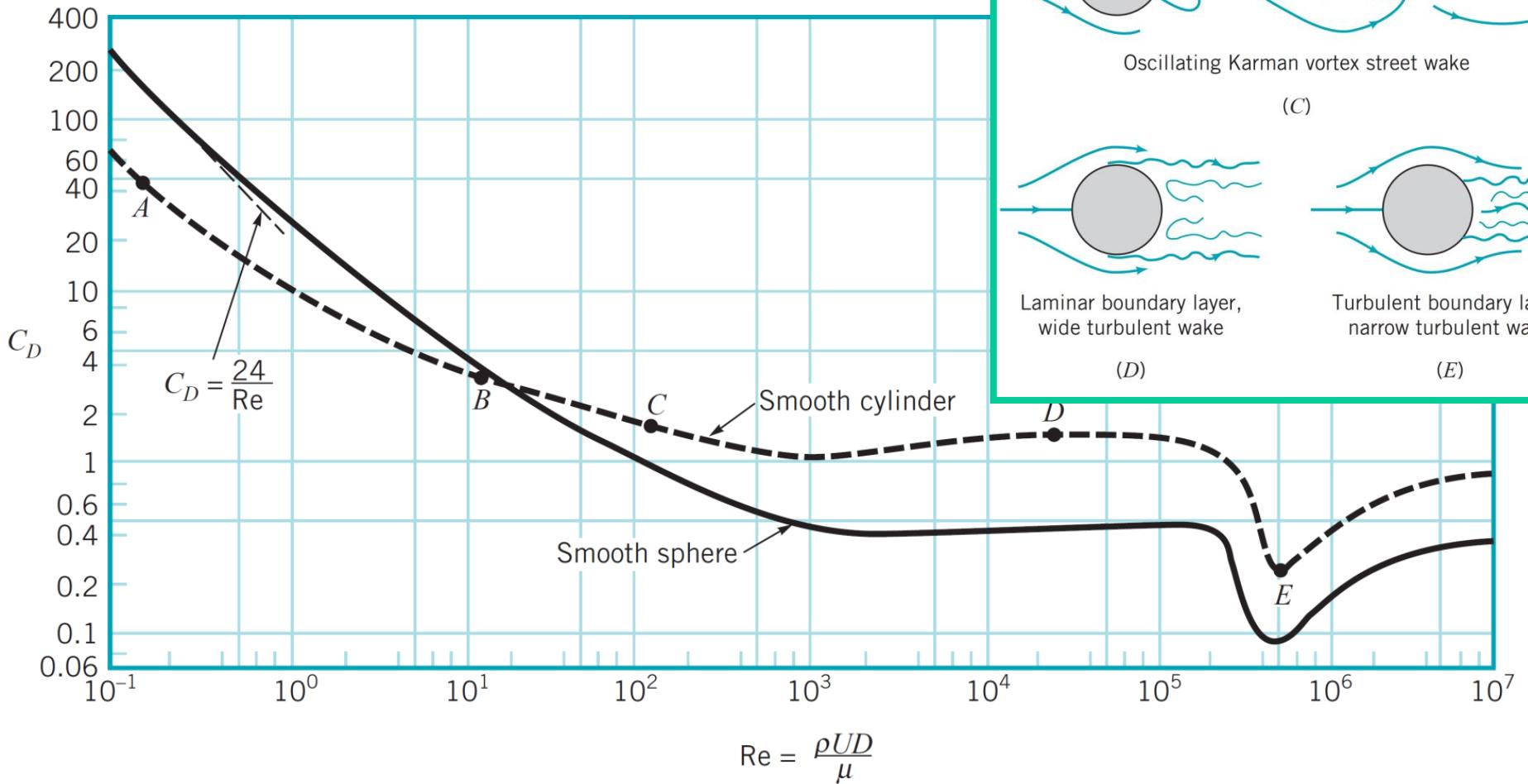
(U.S. Navy photograph, Ordnance Test Station, Pasadena Annex.)

# Coeficientes de Arrasto

$$C_D = \mathcal{D}/(\rho U^2 A/2)$$

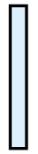
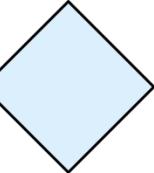
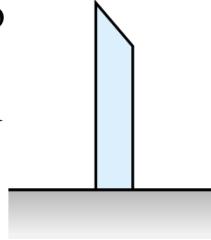
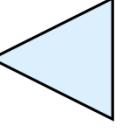
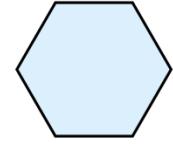
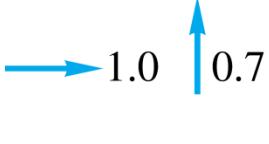
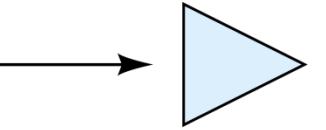
Object	(for $\text{Re} \lesssim 1$ )	$C_D$
a. Circular disk normal to flow	$20.4/\text{Re}$	
		
b. Circular disk parallel to flow	$13.6/\text{Re}$	
		
c. Sphere		$24.0/\text{Re}$
		
d. Hemisphere		$22.2/\text{Re}$
		

# Coeficientes de Arrasto: cilindro e esfera



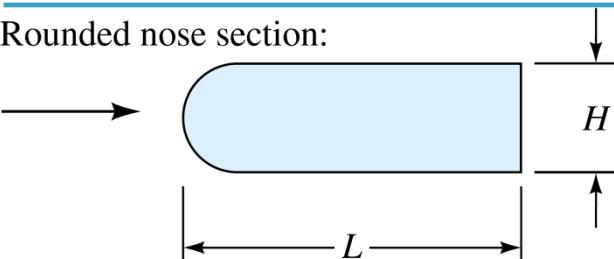
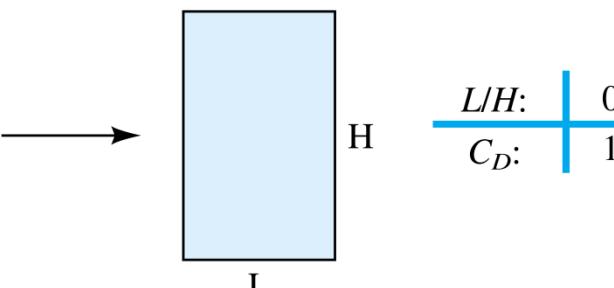
# Coeficientes de Arrasto

Table 7.2 Drag of Two-Dimensional Bodies at  $\text{Re} \geq 10^4$

Shape	$C_D$ based on frontal area	Shape	$C_D$ based on frontal area	Shape	$C_D$ based on frontal area
Square cylinder:		Half-cylinder:		Plate:	
 2.1	 1.2	 2.0			
 1.6	 1.7	 1.4			
Half tube:		Equilateral triangle:		Hexagon:	
 1.2	 1.6		2.0	 1.0 0.7	
 2.3	 2.0				

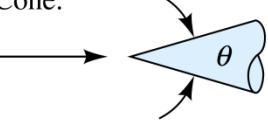
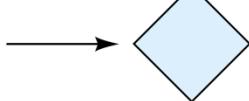
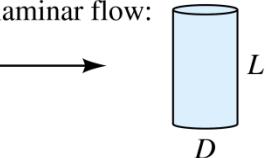
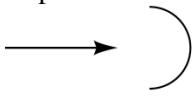
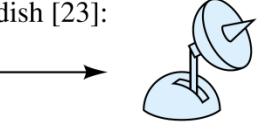
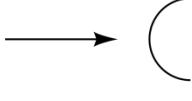
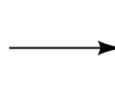
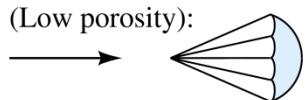
# Coeficientes de Arrasto

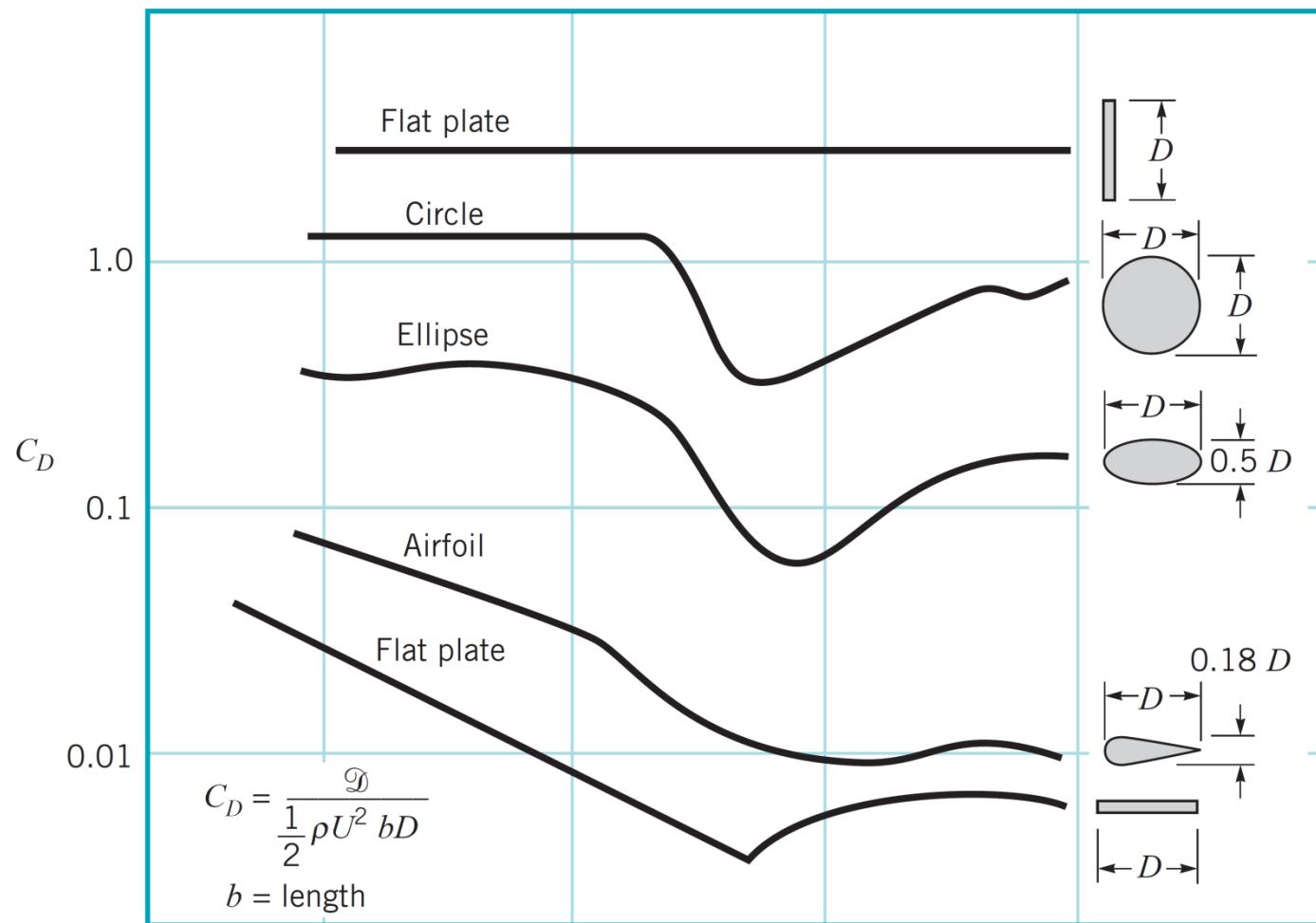
Table 7.2 Drag of Two-Dimensional Bodies at  $\text{Re} \geq 10^4$

Shape	$C_D$ based on frontal area															
Rounded nose section:																
Flat nose section																
Elliptical cylinder:	<table border="1"> <thead> <tr> <th><u>Laminar</u></th> <th><u>Turbulent</u></th> </tr> </thead> <tbody> <tr> <td>1.2</td> <td>0.3</td> </tr> <tr> <td>0.6</td> <td>0.2</td> </tr> <tr> <td>0.35</td> <td>0.15</td> </tr> <tr> <td>0.25</td> <td>0.1</td> </tr> </tbody> </table>						<u>Laminar</u>	<u>Turbulent</u>	1.2	0.3	0.6	0.2	0.35	0.15	0.25	0.1
<u>Laminar</u>	<u>Turbulent</u>															
1.2	0.3															
0.6	0.2															
0.35	0.15															
0.25	0.1															
1:1 $\longrightarrow$	0.5	1.16	1.0	2.0	4.0	6.0										
2:1 $\longrightarrow$	0.4	2.3	2.7	2.1	1.8	1.4										
4:1 $\longrightarrow$	0.7	0.90	1.2	2.0	2.5	3.0										
8:1 $\longrightarrow$	1.0	0.70	2.0	0.68	0.64	0.64										

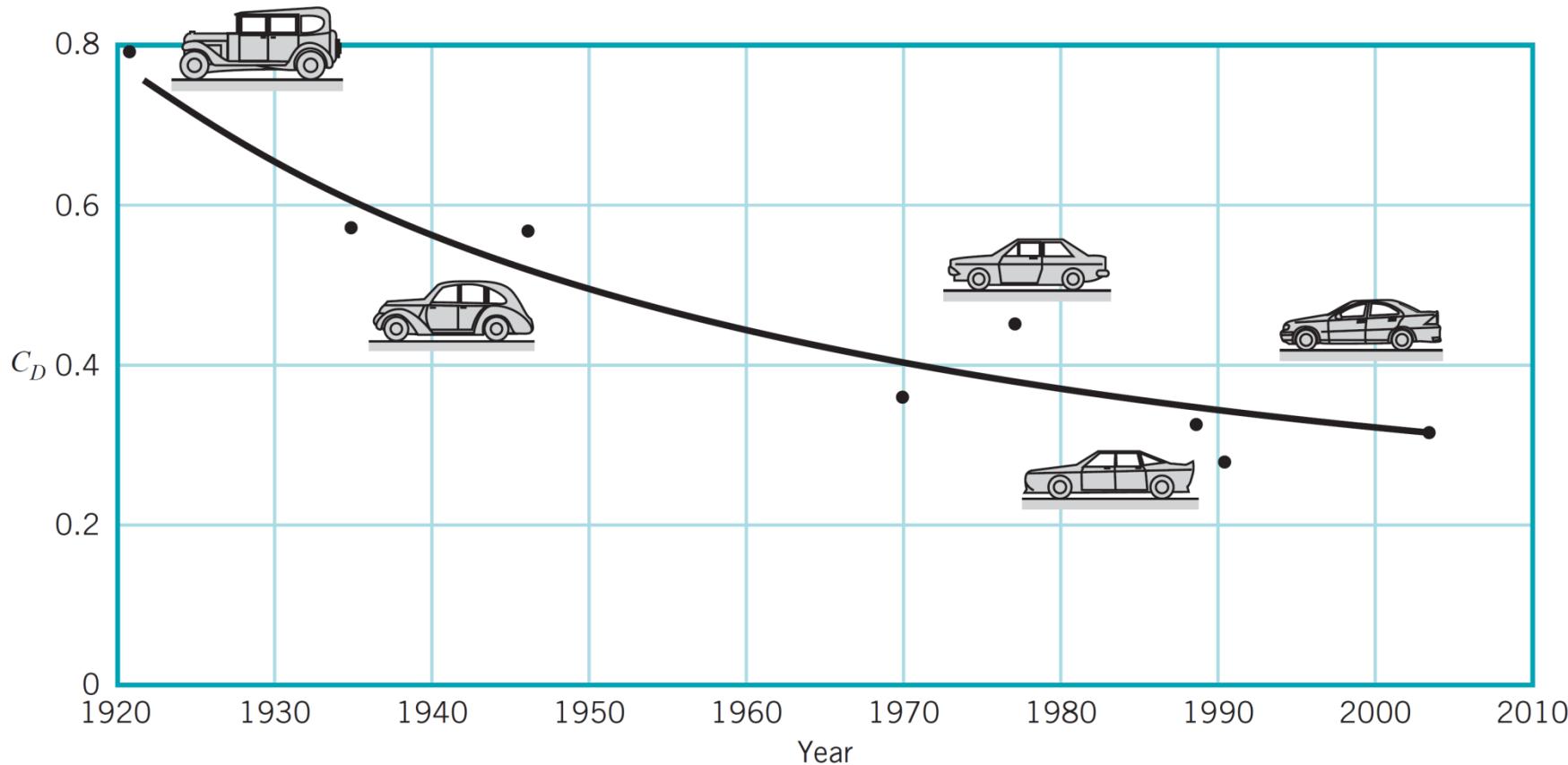
# Coeficientes de Arrasto

**Table 7.3** Drag of Three-Dimensional Bodies at  $\text{Re} \geq 10^4$

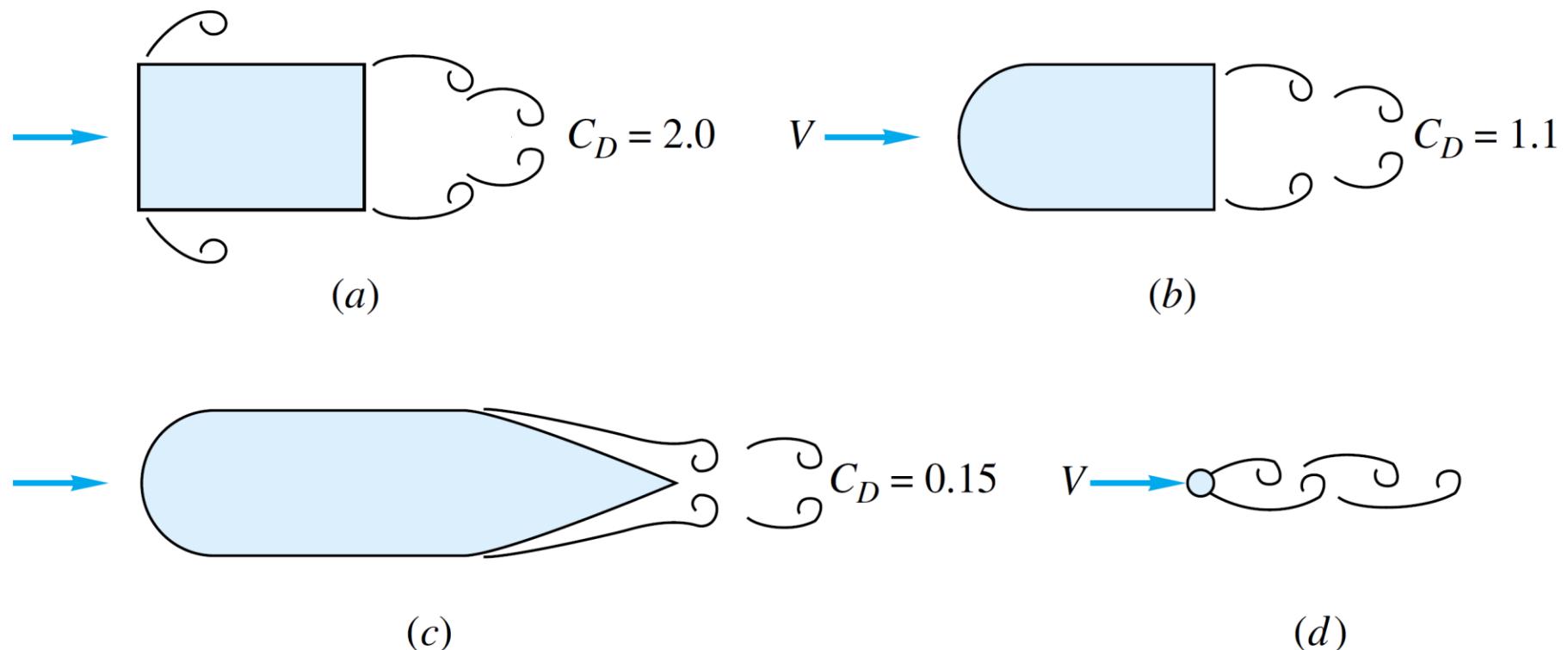
Body	$C_D$ based on frontal area	Body	$C_D$ based on frontal area																					
Cube: 	1.07	Cone: 	$\theta:$ <table border="1"> <tr> <td><math>\theta:</math></td> <td>10°</td> <td>20°</td> <td>30°</td> <td>40°</td> <td>60°</td> <td>75°</td> <td>90°</td> </tr> <tr> <td><math>C_D:</math></td> <td>0.30</td> <td>0.40</td> <td>0.55</td> <td>0.65</td> <td>0.80</td> <td>1.05</td> <td>1.15</td> </tr> </table>	$\theta:$	10°	20°	30°	40°	60°	75°	90°	$C_D:$	0.30	0.40	0.55	0.65	0.80	1.05	1.15					
$\theta:$	10°	20°	30°	40°	60°	75°	90°																	
$C_D:$	0.30	0.40	0.55	0.65	0.80	1.05	1.15																	
	0.81	Short cylinder, laminar flow: 	$L/D:$ <table border="1"> <tr> <td><math>L/D:</math></td> <td>1</td> <td>2</td> <td>3</td> <td>5</td> <td>10</td> <td>20</td> <td>40</td> <td><math>\infty</math></td> </tr> <tr> <td><math>C_D:</math></td> <td>0.64</td> <td>0.68</td> <td>0.72</td> <td>0.74</td> <td>0.82</td> <td>0.91</td> <td>0.98</td> <td>1.20</td> </tr> </table>	$L/D:$	1	2	3	5	10	20	40	$\infty$	$C_D:$	0.64	0.68	0.72	0.74	0.82	0.91	0.98	1.20			
$L/D:$	1	2	3	5	10	20	40	$\infty$																
$C_D:$	0.64	0.68	0.72	0.74	0.82	0.91	0.98	1.20																
Cup: 	1.4	Porous parabolic dish [23]: 	Porosity: <table border="1"> <tr> <td>Porosity:</td> <td>0</td> <td>0.1</td> <td>0.2</td> <td>0.3</td> <td>0.4</td> <td>0.5</td> </tr> <tr> <td><math>\leftarrow C_D:</math></td> <td>1.42</td> <td>1.33</td> <td>1.20</td> <td>1.05</td> <td>0.95</td> <td>0.82</td> </tr> <tr> <td><math>\rightarrow C_D:</math></td> <td>0.95</td> <td>0.92</td> <td>0.90</td> <td>0.86</td> <td>0.83</td> <td>0.80</td> </tr> </table>	Porosity:	0	0.1	0.2	0.3	0.4	0.5	$\leftarrow C_D:$	1.42	1.33	1.20	1.05	0.95	0.82	$\rightarrow C_D:$	0.95	0.92	0.90	0.86	0.83	0.80
Porosity:	0	0.1	0.2	0.3	0.4	0.5																		
$\leftarrow C_D:$	1.42	1.33	1.20	1.05	0.95	0.82																		
$\rightarrow C_D:$	0.95	0.92	0.90	0.86	0.83	0.80																		
	0.4	Average person: 	$C_D A \approx 9 \text{ ft}^2$ $C_D A \approx 1.2 \text{ ft}^2$																					
Disk: 	1.17	Pine and spruce trees [24]: 	$U, \text{ m/s:}$ <table border="1"> <tr> <td><math>U, \text{ m/s:}</math></td> <td>10</td> <td>20</td> <td>30</td> <td>40</td> </tr> <tr> <td><math>C_D:</math></td> <td>1.2 ± 0.2</td> <td>1.0 ± 0.2</td> <td>0.7 ± 0.2</td> <td>0.5 ± 0.2</td> </tr> </table>	$U, \text{ m/s:}$	10	20	30	40	$C_D:$	1.2 ± 0.2	1.0 ± 0.2	0.7 ± 0.2	0.5 ± 0.2											
$U, \text{ m/s:}$	10	20	30	40																				
$C_D:$	1.2 ± 0.2	1.0 ± 0.2	0.7 ± 0.2	0.5 ± 0.2																				
Parachute (Low porosity): 	1.2																							



$$Re = \frac{UD}{\nu}$$

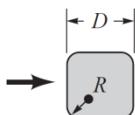
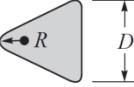
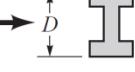
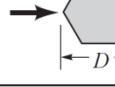
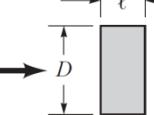


■ FIGURE 9.27 The historical trend of streamlining automobiles to reduce their aerodynamic drag and increase their miles per gallon (adapted from Ref. 5).



**Fig. 7.15** The importance of streamlining in reducing drag of a body ( $C_D$  based on frontal area):  
 (a) rectangular cylinder; (b)  
 rounded nose; (c) rounded nose and  
 streamlined sharp trailing edge; (d)  
 circular cylinder with the same  
 drag as case (c).

Fluid Mechanics – 4th ed. -Frank M. White

Shape	Reference area $A$ ( $b$ = length)	Drag coefficient $C_D = \frac{D}{\frac{1}{2} \rho U^2 A}$	Reynolds number $Re = \rho U D / \mu$	
	Square rod with rounded corners	$A = bD$	$R/D$ $C_D$ 0            2.2 0.02        2.0 0.17        1.2 0.33        1.0	$Re = 10^5$
	Rounded equilateral triangle	$A = bD$	$R/D$ $C_D$ 0            1.4    2.1 0.02        1.2    2.0 0.08        1.3    1.9 0.25        1.1    1.3	$Re = 10^5$
	Semicircular shell	$A = bD$	$\rightarrow$ 2.3 $\leftarrow$ 1.1	$Re = 2 \times 10^4$
	Semicircular cylinder	$A = bD$	$\rightarrow$ 2.15 $\leftarrow$ 1.15	$Re > 10^4$
	T-beam	$A = bD$	$\rightarrow$ 1.80 $\leftarrow$ 1.65	$Re > 10^4$
	I-beam	$A = bD$	2.05	$Re > 10^4$
	Angle	$A = bD$	$\rightarrow$ 1.98 $\leftarrow$ 1.82	$Re > 10^4$
	Hexagon	$A = bD$	1.0	$Re > 10^4$
	Rectangle	$A = bD$	$\ell/D$ $C_D$ ≤ 0.1    1.9 0.5        2.5 0.65       2.9 1.0        2.2 2.0        1.6 3.0        1.3	$Re = 10^5$

■ FIGURE 9.28 Typical drag coefficients for regular two-dimensional shapes.