

Fundamental Physics and Gravitational Waves

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USP, June 3rd 2020

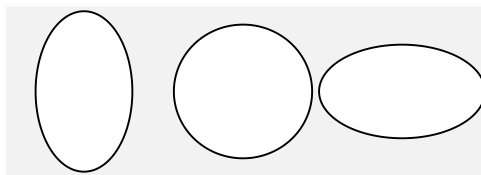
GW basics in 1 slide

Gauged fixed metric perturbations $h_{\mu\nu}$ after discarding $h_{0\mu}$ components, which are not radiative $\rightarrow$ **transverse** waves

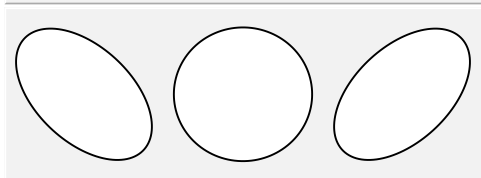
$$h_{ij} = \begin{pmatrix} h_+ & h_\times & 0 \\ h_\times & -h_+ & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

2 pol. state like any mass-less particle

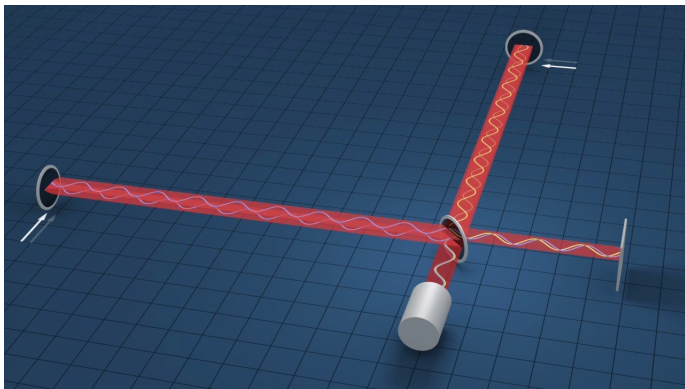
h_+



$h_\times$



LIGO and Virgo: very precise rulers



Robert Hurt (Caltech)

Light intensity $\propto$ light travel difference in perpendicular arms

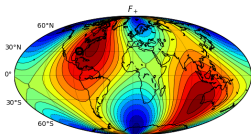
Effective optical path increased by factor $N \sim 500$ via Fabry-Perot cavities

Phase shift $\Delta\phi \sim 10^{-8}$ can be measured $\sim 2\pi N\Delta L/\lambda \rightarrow \Delta L \sim 10^{-15}/N \text{ m}$

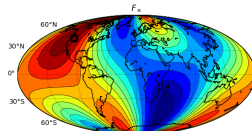
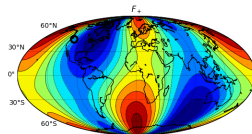
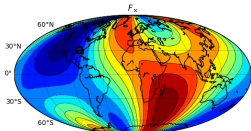
Almost omnidirectional detectors

Detectors measure h_{det} : linear combination $F_+ h_+ + F_\times h_\times$

$-1 \ 0 \ 1$
 F_+



$F_\times$



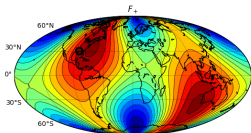
$h_{+, \times}$ depend on source

pattern functions $F_{+, \times}$ depend on orientation source/detector

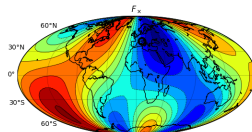
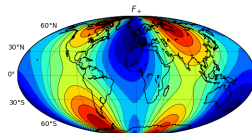
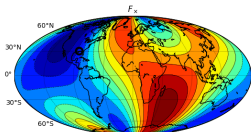
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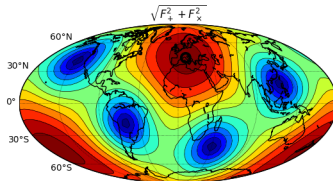
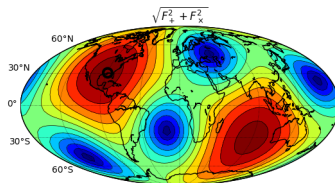
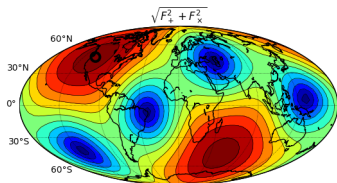
$F_\times$



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Pattern functions: $\sqrt{F_+^2 + F_-^2}$



The LIGO and Virgo observatories



- Observation run **O1** Sept '15 - Jan '16
~ 130 days, with 49.6 days of actual data, PRX (2016) 4, 041014, **2 detectors**, 3BBH
- **O2** Dec. '16 – Jul'17 **2 det's** + Aug '17 **3 det's**
3(+4) BBH + **1BNS** in **double** (**triple**) coinc.
- **O3a**: **3 detectors**, Apr 2nd - Oct 1st 2019
- **O3b**: Nov 1st – Mar/2020

In April 2020 Japanese KAGRA joined the network, in 202? Indian INDIGO will join the collab-

Wave generation: localized sources

Einstein formula relates h_{ij} to the source quadrupole moment Q_{ij}

$$Q_{ij} = \int d^3x \rho \left(x_i x_j - \frac{1}{3} \delta_{ij} x^2 \right), \quad v^2 \simeq G_N M / r, \quad \eta \equiv m_1 m_2 / M^2$$

$$h_{ij} \sim g(\theta_{LN}) \frac{2G_N}{D} \frac{d^2 Q_{ij}}{dt^2} \simeq \frac{2G_N \eta M v^2}{D} \cos(2\phi(t))$$

$$f = 2\text{kHz} \left(\frac{r}{30\text{Km}} \right)^{-3/2} \left(\frac{M}{3M_\odot} \right)^{1/2} < f_{\text{Max}} \simeq 12\text{kHz} \left(\frac{M}{3M_\odot} \right)^{-1}$$

$$v = 0.3 \left(\frac{f}{1\text{kHz}} \right)^{1/3} \left(\frac{M}{M_\odot} \right)^{1/3} < \frac{1}{\sqrt{6}}$$

Geometric factor $g(\theta_{LN})$ takes account of transversality projection (angular momentum L of the binary, observation direction N)

$$h_+ \sim \frac{1 + \cos^2(\theta_{LN})}{2} \eta \frac{M v^2}{D} \cos \phi(t_s / M, \eta, S_i^2 / m_i^4, \dots)$$

$$h_\times \sim \cos(\theta_{LN}) \eta \frac{M v^2}{D} \sin \phi(t_s / M, \eta, \dots)$$

Amplitudes of 2 polarizations modulated by θ_{LN} ($h \nearrow$ for $\theta_{LN} \searrow 0$), never both vanishing unlike dipolar motion for the electromagnetic case

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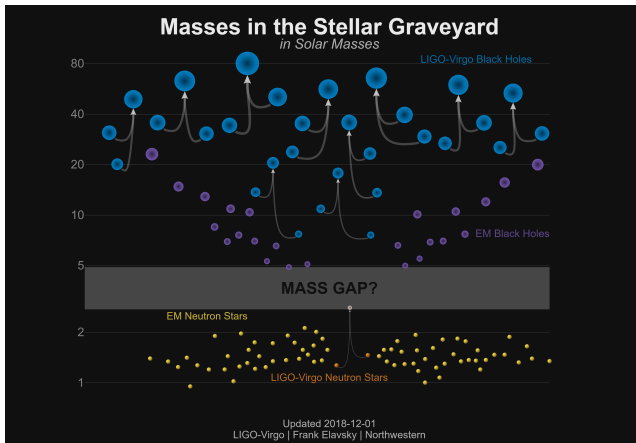
$$h_+ \sim \frac{1 + \cos^2(\theta_{LN})}{2} \eta \frac{M v^2}{d_L} \cos \phi(t_0 / \mathcal{M}, \eta, S_i^2 / m_i^4, \dots)$$

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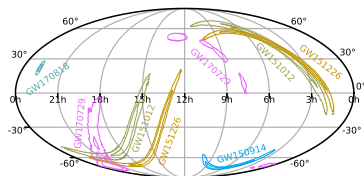
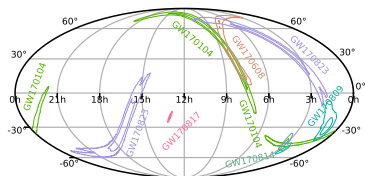
h sensitive to red-shifted masses $M \rightarrow M(1+z) \equiv \mathcal{M}$

Binary systems and compact detected so far



- 1 GW190412: sistema mais assimétrico: $m_1/m_2 \sim 3$, massa total $\sim 40M_{\odot}$
- 2 GW190425: novo sistema binário de estrela de nêutrons

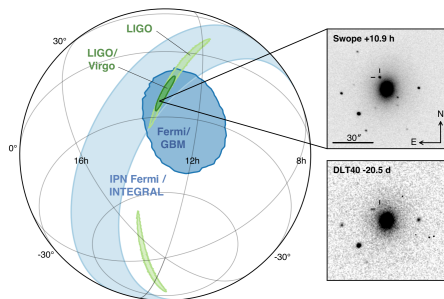
Sky localization



Distances between 40 e $\sim 2800 \text{ Mpc}$ ($\pm 20\%$), (our galaxy size $\sim 30 \text{ kpc}$)

Image by Leo Singer, <http://www.ligo.org>

- GW trigger on Aug 17th, 2017, ended at 12h 41' 04.4" UTC, first in in LIGO Hanford, then confirmed as a triple coincidence $\rightarrow$ localized in an area of $\sim 28 \text{ deg}^2$
- GRB trigger from Fermi-GBM 1.7" after
- first optical image 10.87 hr afterwards by One-Meter Two Hemisphere team with Swope telescope at Las Campanas Observatory in Chile
- X obtained by the X-Ray Telescope on Swift after 14.9 h (NuSTAR 16.8 h)
- radio ($\sim 3,6 \text{ GHz}$) by VLA 16 days after GW event



LIGO/Virgo & Partner Astronomy groups, *Astrophys.J.* 848 (2017) no.2, L12

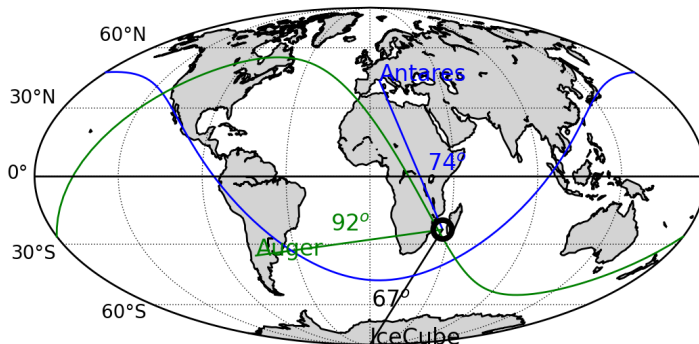
An example of the optical image



Transient Optical Robotic Observatory of the South

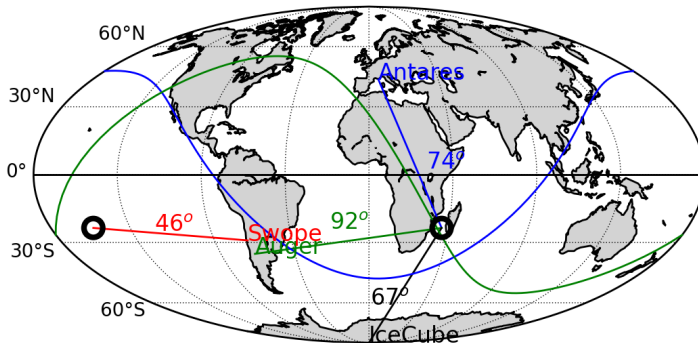


GW170817 and ν detectors



Potential ν s down-going for Antares and IceCube, grazing for Auger

GW170817 and ν detectors



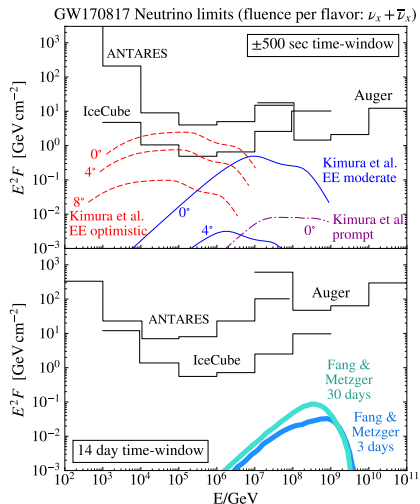
Potential ν s down-going for Antares and IceCube, grazing for Auger
Source location at optical detection

ANTARES and IceCube look for ν

IceCube and ANTARES looked for $\mu - \nu$ at ± 500 sec, observation for 2 weeks

no detection

Pierre Auger for $> 10^{17}$ eV, grazing good for τ production at 10^{18} eV

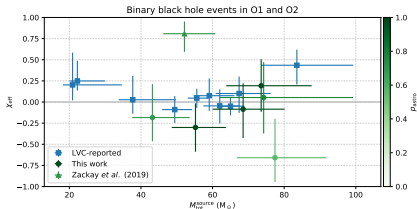


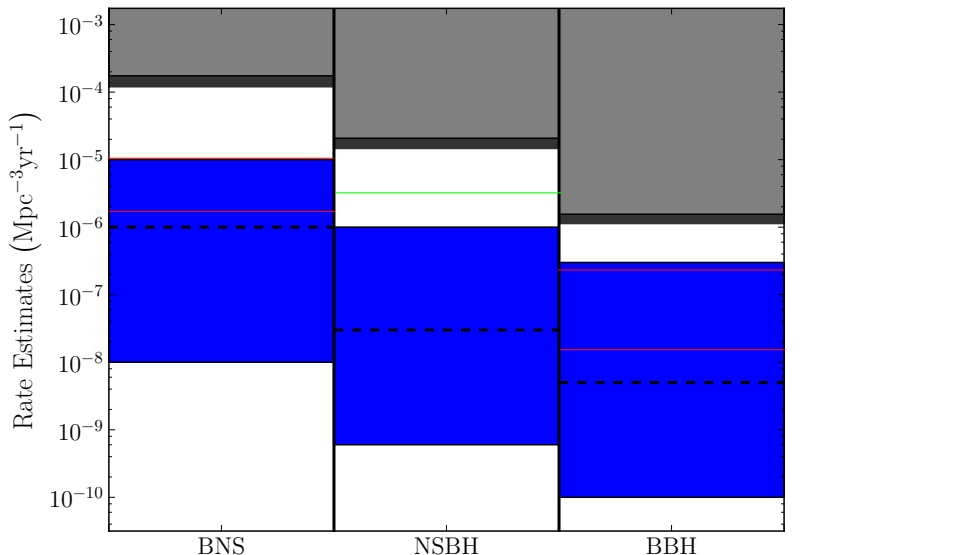
LIGO/Virgo, ANTARES, ICECUBE and Pierre Auger, *Astrophys.J.* 850 '17 2, L35

Event	Primary mass (M_{sun})	Secondary mass (M_{sun})	Effective inspiral spin	chirp mass (M_{sun})	Final spin	Final mass (M_{sun})	Luminosity distance (Mpc)	Sky localization (deg ²)
GW150914	35.6 ^{+4.8} _{-3.0}	30.6 ^{+3.0} _{-4.4}	-0.01 ^{+0.12} _{-0.13}	28.6 ^{+1.0} _{-1.5}	0.69 ^{+0.03} _{-0.04}	63.1 ^{+3.3} _{-3.0}	430 ⁺¹³⁰ ₋₁₇₀	179
GW151012	23.3 ^{+14.0} _{-5.5}	13.6 ^{+4.1} _{-4.8}	0.04 ^{+0.28} _{-0.19}	15.2 ^{+2.0} _{-1.1}	0.67 ^{+0.13} _{-0.11}	35.7 ^{+9.9} _{-3.8}	1060 ⁺⁵⁴⁰ ₋₄₈₀	1555
GW151226	13.7 ^{+8.8} _{-3.2}	7.7 ^{+2.2} _{-2.6}	0.18 ^{+0.20} _{-0.12}	8.9 ^{+0.3} _{-0.3}	0.74 ^{+0.07} _{-0.03}	20.5 ^{+0.4} _{-1.5}	440 ⁺¹⁸⁰ ₋₁₉₀	1033
GW170104	31.0 ^{+7.2} _{-5.6}	20.1 ^{+4.9} _{-4.5}	-0.04 ^{+0.17} _{-0.20}	21.5 ^{+2.1} _{-1.7}	0.66 ^{+0.08} _{-0.10}	49.1 ^{+5.2} _{-3.9}	960 ⁺⁴³⁰ ₋₄₁₀	924
GW170608	10.9 ^{+5.3} _{-1.7}	7.6 ^{+1.3} _{-2.1}	0.03 ^{+0.19} _{-0.07}	7.9 ^{+0.2} _{-0.2}	0.69 ^{+0.04} _{-0.04}	17.8 ^{+3.2} _{-0.7}	320 ⁺¹²⁰ ₋₁₁₀	396
GW170729	50.6 ^{+10.6} _{-10.2}	34.3 ^{+9.1} _{-10.1}	0.36 ^{+0.21} _{-0.25}	35.7 ^{+6.5} _{-4.7}	0.81 ^{+0.07} _{-0.13}	80.3 ^{+14.6} _{-10.2}	2750 ⁺¹³⁵⁰ ₋₁₃₂₀	1033
GW170809	35.2 ^{+8.3} _{-0.0}	23.8 ^{+5.2} _{-5.1}	0.07 ^{+0.10} _{-0.10}	25.0 ^{+2.1} _{-1.6}	0.70 ^{+0.08} _{-0.09}	56.4 ^{+5.2} _{-3.7}	990 ⁺³²⁰ ₋₃₈₀	340
GW170814	30.7 ^{+5.7} _{-3.0}	25.3 ^{+2.9} _{-4.1}	0.07 ^{+0.12} _{-0.11}	24.2 ^{+1.4} _{-1.1}	0.72 ^{+0.07} _{-0.05}	53.4 ^{+3.2} _{-2.4}	580 ⁺¹⁶⁰ ₋₂₁₀	87
GW170817	1.46 ^{+0.12} _{-0.10}	1.27 ^{+0.09} _{-0.09}	0.00 ^{+0.02} _{-0.01}	1.186 ^{+0.001} _{-0.001}	≤ 0.89	≤ 2.8	40 ⁺¹⁰ ₋₁₀	16
GW170818	35.5 ^{+7.5} _{-4.7}	26.8 ^{+4.3} _{-5.2}	-0.09 ^{+0.18} _{-0.21}	26.7 ^{+2.1} _{-1.7}	0.67 ^{+0.07} _{-0.08}	59.8 ^{+4.8} _{-3.8}	1020 ⁺⁴³⁰ ₋₃₉₀	39
GW170823	39.6 ^{+10.0} _{-6.6}	29.4 ^{+6.3} _{-7.1}	0.08 ^{+0.20} _{-0.22}	29.3 ^{+4.2} _{-3.2}	0.71 ^{+0.08} _{-0.10}	65.6 ^{+9.4} _{-6.6}	1850 ⁺⁸⁴⁰ ₋₈₄₀	1651

<https://www.gw-openscience.org/catalog/>

See however Princeton's group
results
arXiv:1904.07214





Astrophysical predictions, upper limit from S5/6/O1 and observation from O1/O2

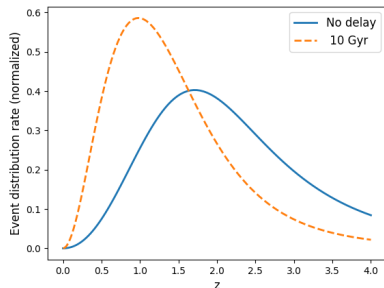
LIGO/Virgo CQG ('10) 27 173001, PRX ('16), APJ (2016), PRL 119 ('17)

Ongoing O3: towards measuring merger distribution

At <https://gracedb.ligo.org/superevents/public/O3>

summary of **candidate** detections from O3a+b:

1 BNS+1BBH+53(+1) candidate events, ~ 10 of which possibly involving at least a NS



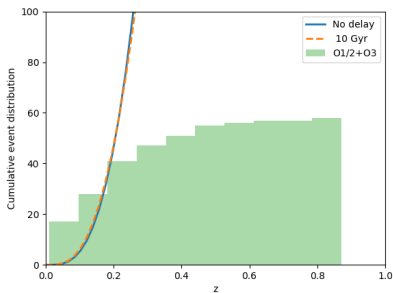
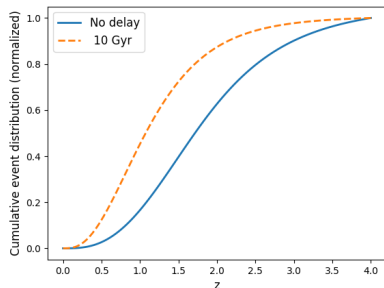
Expected merger distribution from Star Formation Rate (—) or SFR+Poissonian distributed delay (---)

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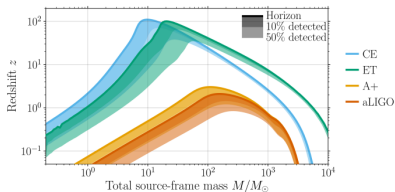
Future with ET and LISA looks very loud

Future 3rd generation detectors (Einstein Telescope, Cosmic Explorer)/space telescope LISA will detect CBC signals with $\text{SNR } 10 - 10^2$, with few golden events with $\text{SNR} \sim 10^3$.

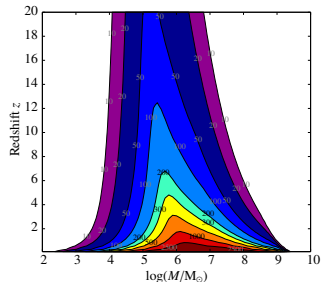
Templates few % accurate OK for characterising a source with $\text{SNR } O(10)$ (typical for LIGO/Virgo)

for $\text{SNR} \sim 10^3$ residual after extracting that source will have $\text{SNR} \sim O(10)$

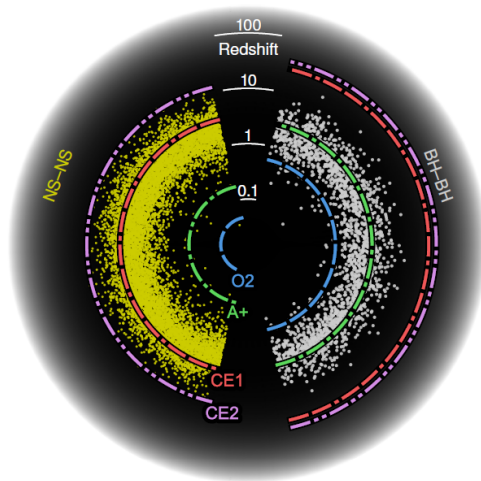
- 1) biasing parameter estimation
- 2) contaminating the extraction of additional sources.



from arXiv:1902.09485



How many more?



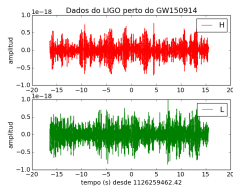
New lines of research

- Precision gravity
- General Relativity tests in strong gravity
- “Hairiness” of black holes
- Universe expansion history (standard sirens)
- Phase transitions in the Early Universe
- Black hole mass function
- How binary systems form and how frequent are they? (star formation rate)
- Fate of a massive star
- Probe the the interior of a neutron star
- Understand the life of a pulsar and its evolution
- Dark matter and Gravitational Waves (modification of compact object and/or their environment)
- Data analysis challenges for signals with $SNR \sim 100$
- Central Core of Galaxies, Massive Black Holes and their role in Galaxy Formation
- Multi-messenger astronomy

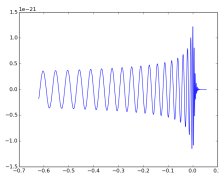
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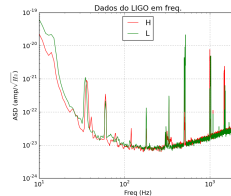
The importance of theoretical modeling



$\times$



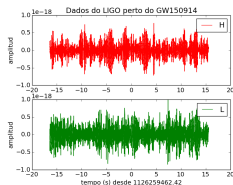
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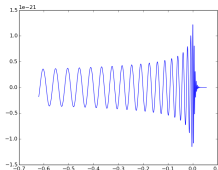
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The importance of theoretical modeling

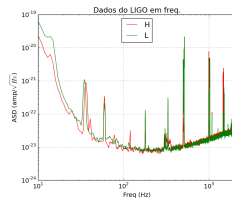
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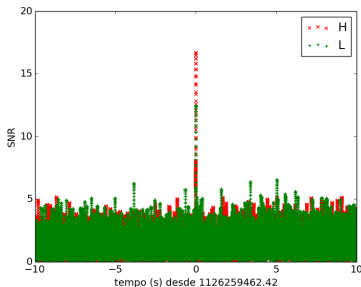
$\times$



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$=$



Data from <https://losc.ligo.org/events/GW150914/>

Fundamental GR: inspiral analytic model

Inspiral $h = A \cos(\phi(t)) \quad \frac{\dot{A}}{A} \ll \dot{\phi}$

Virial relation:

$$v \equiv (G_N M \pi f_{GW})^{1/3} \quad \eta = \frac{m_1 m_2}{(m_1 + m_2)^2}$$

$$\begin{aligned} E(v) &= -\frac{1}{2} \eta M v^2 (1 + \#(\eta, S_i/m_i^2) v^2 + \#(\eta, S_i/m_i^2) v^4 + \dots) \\ P(v) \equiv -\frac{dE}{dt} &= \frac{32}{5 G_N} v^{10} (1 + \#(\eta, S_i/m_i^2) v^2 + \#(\eta, S_i/m_i^2) v^3 + \dots) \end{aligned}$$

$E(v)(P(v))$ known up to 3(3.5)PN

$$\begin{aligned} \frac{1}{2\pi} \phi(T) &= \frac{1}{2\pi} \int^T \omega(t) dt = - \int^{v(T)} \frac{\omega(v) dE/dv}{P(v)} dv \\ &\sim \int (1 + \#(\eta, S_i/m_i^2) v^2 + \dots + \#(\eta, S_i/m_i^2) v^6 + \dots) \frac{dv}{v^6} \end{aligned}$$

Fundamental GR: inspiral analytic model

Inspiral $h = A \cos(\phi(t)) \quad \frac{\dot{A}}{A} \ll \dot{\phi}$

Virial relation:

$$v \equiv (G_N M \pi f_{GW})^{1/3} \quad \eta = \frac{m_1 m_2}{(m_1 + m_2)^2}$$

$$\begin{aligned} E(v) &= -\frac{1}{2} \eta M v^2 (1 + \#(\eta, S_i/m_i^2) v^2 + \#(\eta, S_i/m_i^2) v^4 + \dots) \\ P(v) \equiv -\frac{dE}{dt} &= \frac{32}{5 G_N} v^{10} (1 + \#(\eta, S_i/m_i^2) v^2 + \#(\eta, S_i/m_i^2) v^3 + \dots) \end{aligned}$$

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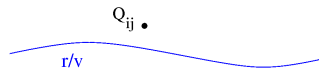
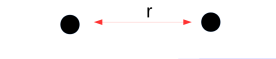
PN Coefficients (tidal $\sim v^{10}$)

PN approximation to General Relativity

Small expansion parameter v , related to metric perturbation $v^2 \sim \frac{G_N M}{r}$

Near zone, $D \sim r$

Far zone, $D \gtrsim \lambda = r/v$

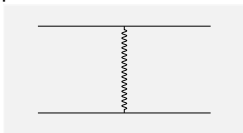


Describe **conservative** dynamics

conservative + **dissipative**

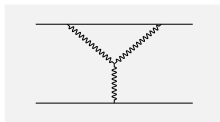
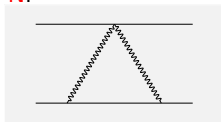
EFT framework pioneered by W. Goldberger and I. Rothstein, PRD '06

Newtonian potential:

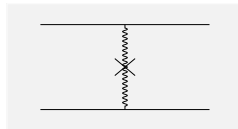
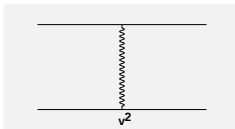
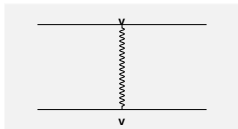


$$S_{\text{eff}} \sim \int dt \frac{G_N m_1 m_2}{r} \sim L$$

At 1PN:



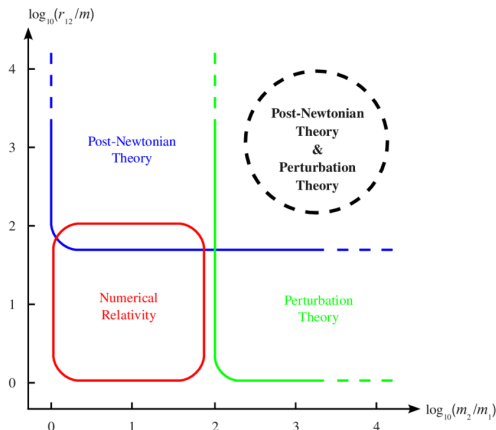
$$S_{\text{eff}} = \int dt \frac{G_N^2 m_1^2 m_2}{r^2} \sim L v^2$$



$$V_{1PN} = -\frac{Gm_1m_2}{2r} \left[1 - \frac{G_N m_1}{2r} + \frac{3}{2}(v_1^2) - \frac{7}{2}v_1v_2 - \frac{1}{2}v_1\hat{r}v_2\hat{r} \right] +$$

$1 \leftrightarrow 2$

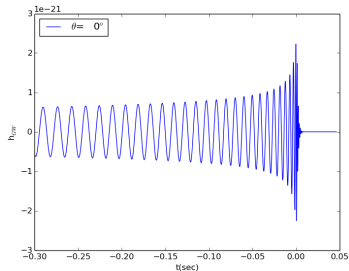
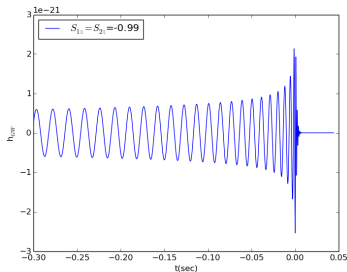
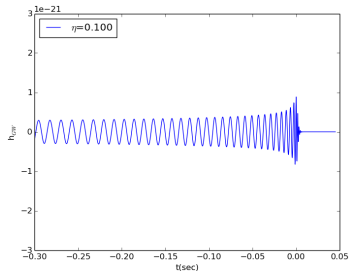
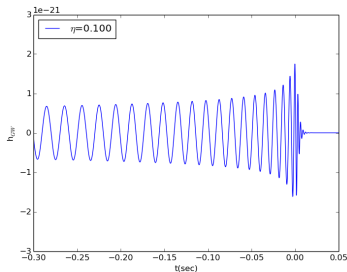
Different approximation methods



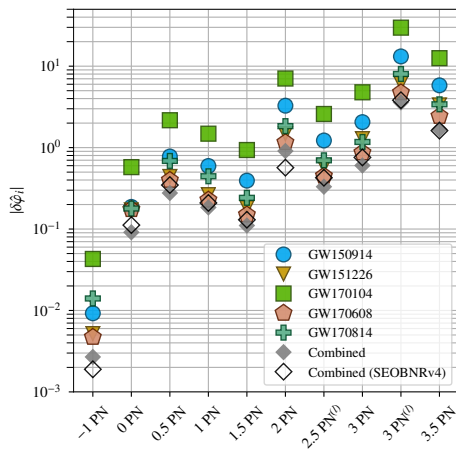
(Blanchet et al. arXiv:1007.2614)

Numerical relativity solutions are expensive for large separation (large orbital scale) and large mass ratios (long dynamical evolution time)

Looking for sources fingerprints



Testing the PN series with O1/2

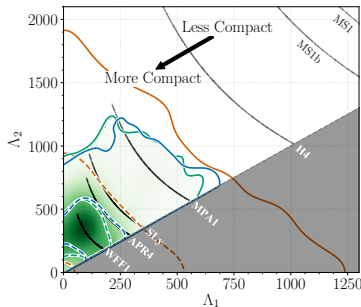


Precision in measuring the PN coefficients $\sim 100\%$: one cannot both **measure the astro parameters** and **test GR** with same detection! Unique probe of high PN-orders

Fundamental physics of Neutron stars

Tidal deformability $\Lambda \simeq R^{-5} Q_{ab} / (\partial_a \partial_b U_{\text{tidal}})$ depends on Equation of State

Determination of $\Lambda_{1,2}$
(assuming same EoS for 1,2)



Shading Common EoS for 2 bodies and constrain for $m_{\text{max}} > 1.97 M_{\odot}$
Lines 50%, 90% countours, No minimum m_{max} , independent EoSs

LIGO/Virgo collaboration, arXiv:1805.11581

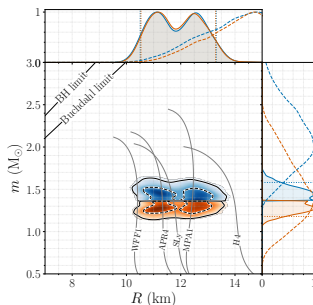
Fundamental physics of Neutron stars II

Parametrizing EoS with $\Gamma \equiv \frac{\epsilon+p}{p} \frac{dp}{d\epsilon}$, $\Gamma(x) = \exp(\sum_k \gamma_k x^k)$, $x \equiv \log \frac{p}{p_0}$

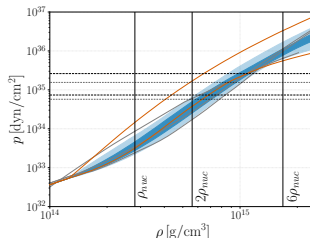
$\gamma_0 \in [0.2, 2], \gamma_1 \in [1.6, 1.7], \gamma_2 \in [0.6, 0.6], \gamma_3 \in [0.02, 0.02], \Gamma(p) \in [0.6, 4.5]$

L. Lindblom PRD 82, 103011 (2010)

Constraints on Mass vs- radius and p vs. rho



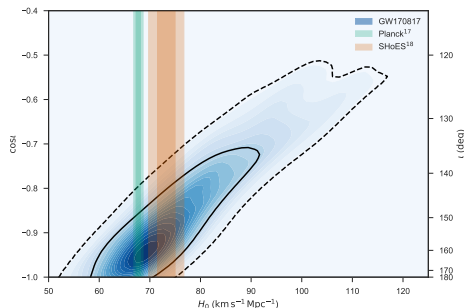
lighter, heavier



90% prior, posterior

LIGO/Virgo collaboration, arXiv:1805.11581

- From GWs only: luminosity distance
 $d_L \sim 40^{+8}_{-14} \text{ Mpc}$, viewing angle
 $\theta_{LN} > 125^\circ$
- Fixing d_L from info from EM location
 + Hubble relation $d_L H_0 = z$
 - Hubble constant from SuperNovae (SHoES)
 $148^\circ < \theta_{LN} < 166^\circ$
 Riess et al. ApJ 826, 56 '16
 - from Planck
 $157 < \theta_{LN} < 177^\circ$
 Planck A&A, 594, A13 '16
- GW almost coincident with EM
 $\Rightarrow \Delta v_{GW}/c \sim 10^{-15}$
 LIGO/Virgo, Fermi Gamma-Ray Burst Monitor, INTEGRAL Ap.J. 848 (2017) 2, L13



LIGO/Virgo Nature 551 '17 7678, 85

$$h''_{+,\times} + 2\frac{a'}{a}h'_{+,\times} + c_s^2 \nabla^2 h_{+,\times} = 0$$

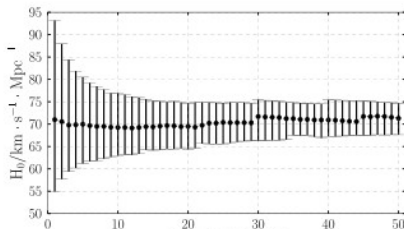
Determining H_0 without EM counterpart

Hubble law: $z = H_0 d_L$

D_L can be measured, z degenerate with M , however **if**

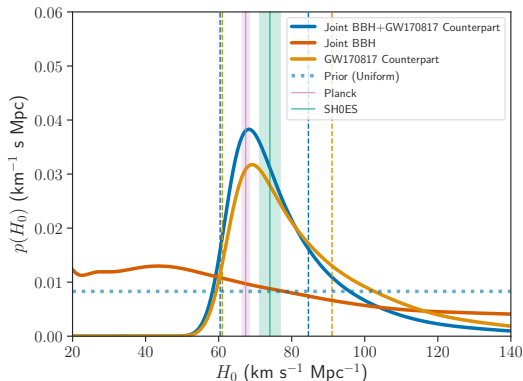
- the source in the sky has been localised (α, δ)
- GW sources are in the galaxy catalogue with known red-shift

$$P(z, D_L | c_i) = \int d\mathcal{M} d\vec{\theta} d\alpha d\delta P(D_L \mathcal{M}, \vec{\theta}, \alpha, \delta | c_i) \pi(z, |\alpha, \delta)$$



Schutz, Nature (1986)
323 310
W. Del Pozzo,
Phys.Rev.D86 (2012)
043011

Galaxy catalogs and H_0



sky localization from DES-Y1
(GW170814)
GWENS (GW170818)
GLADE (GW150914, GW151226,
GW170608)

LIGO/Virgo, arXiv:1908.06060

Conclusions (Actually just the beginning!)

- After the beginning of GW astronomy, we have witnessed the start of multi-messenger astronomy
- New era for Cosmology: H_0 from GWs! (and EM)
- New input for fundamental physics: test of gravity in the strong field at short scale, radiative gravity sector tested at large distances and soon **precision gravity** is going to be needed