

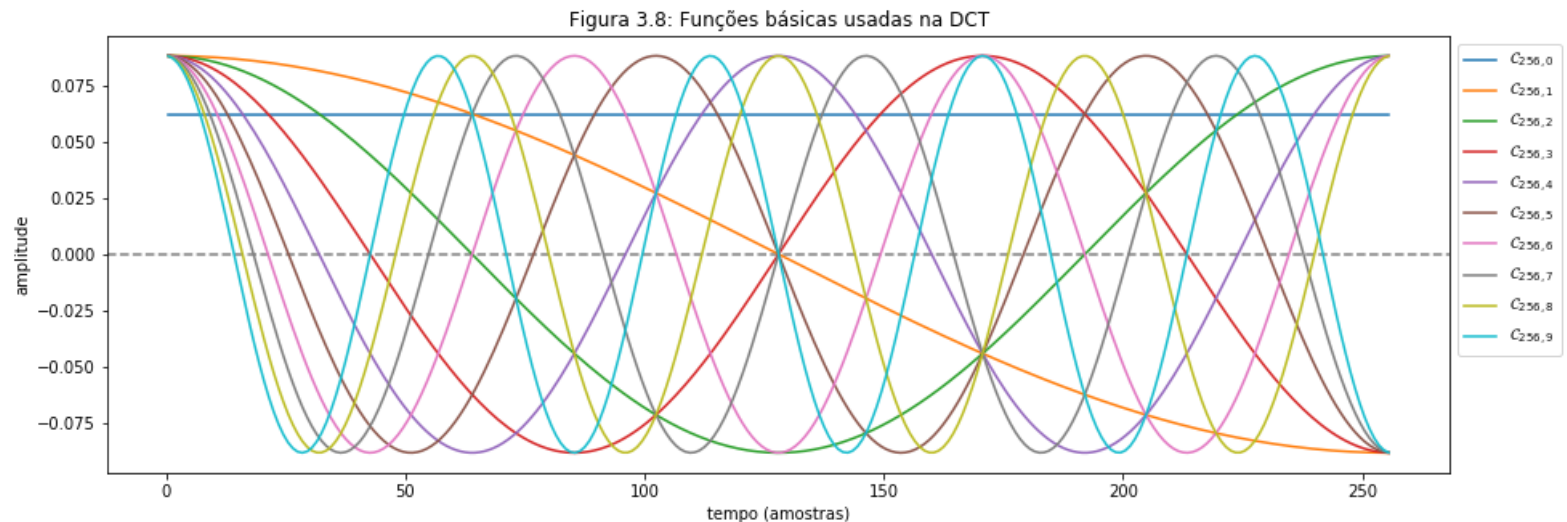
**MAC0317/MAC5920**

**Introdução ao Processamento de Sinais Digitais**

**Seção 3.5: Propriedades da DCT**

## Seção 3.5.2: Domínio da frequência para a DCT

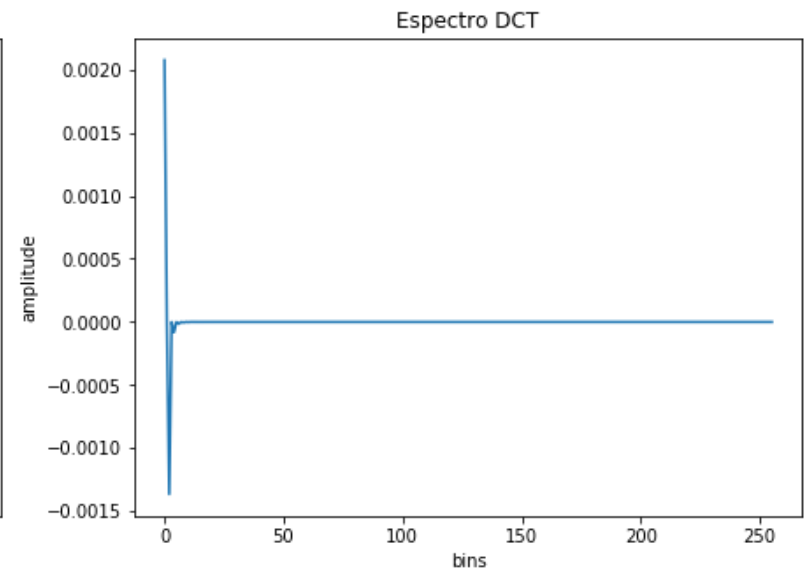
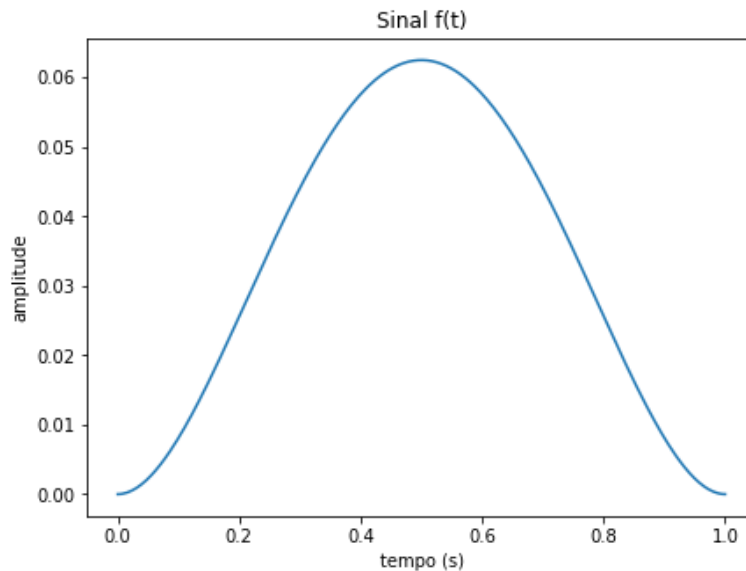
```
In [19]: N=256; t = np.arange(0.5,N,1); plt.figure(figsize=(15,5))
plt.title(r'Funções básicas da DCT  $\mathcal{C}_{256,k}$   $0 \leq k < 9$ ')
plt.xlabel('tempo (amostras)'); plt.ylabel('amplitude')
plt.axhline(y=0.0, color='gray', linestyle='--', ms=1)
for k in range(10):
    plt.plot(t, m.sqrt((1+(k>0))/N)*np.cos(m.pi*k*t/N), label=r" $\mathcal{C}_{256, %d}$ " % k)
plt.title("Figura 3.8: Funções básicas usadas na DCT")
plt.legend(loc='upper left', bbox_to_anchor=(1, 1))
plt.show()
```



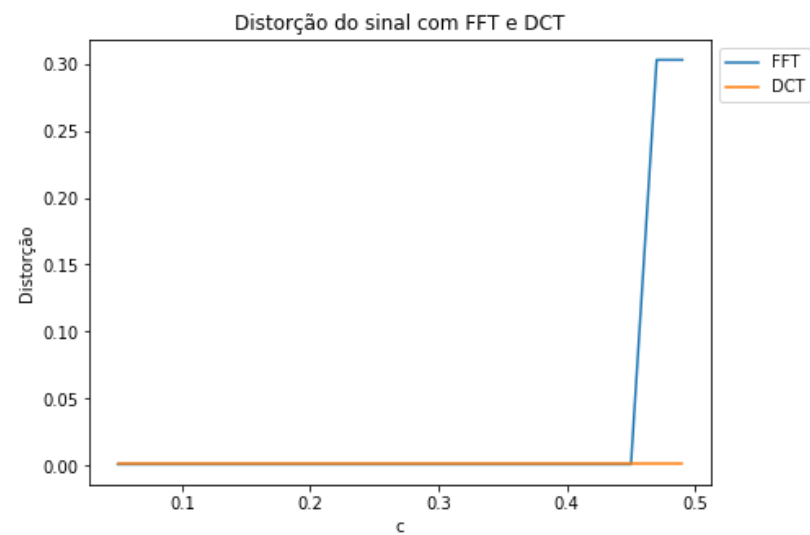
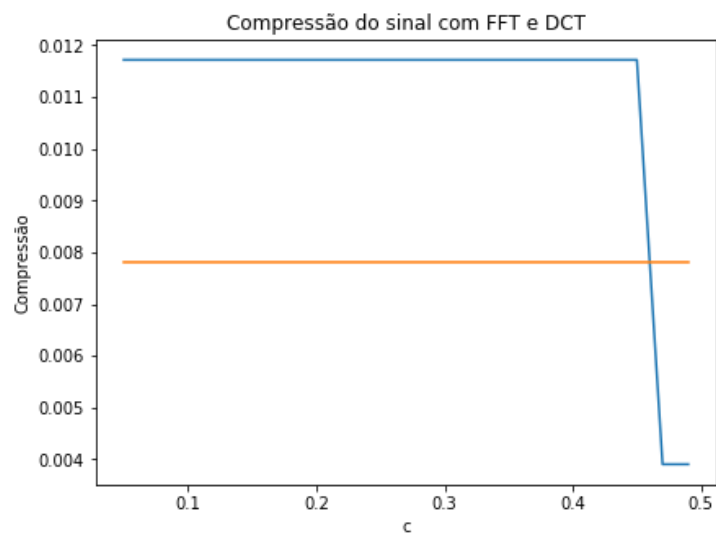
### **Seção 3.5.3 - Repetição dos exemplos anteriores usando DCT ao invés de DFT**

## Exemplo 1: Função $f(t) = (t - t^2)^2$

```
In [21]: t = np.linspace(0, 1, 256)
f = (t - t**2) **2
X = plot_func_dct(t,f)
```

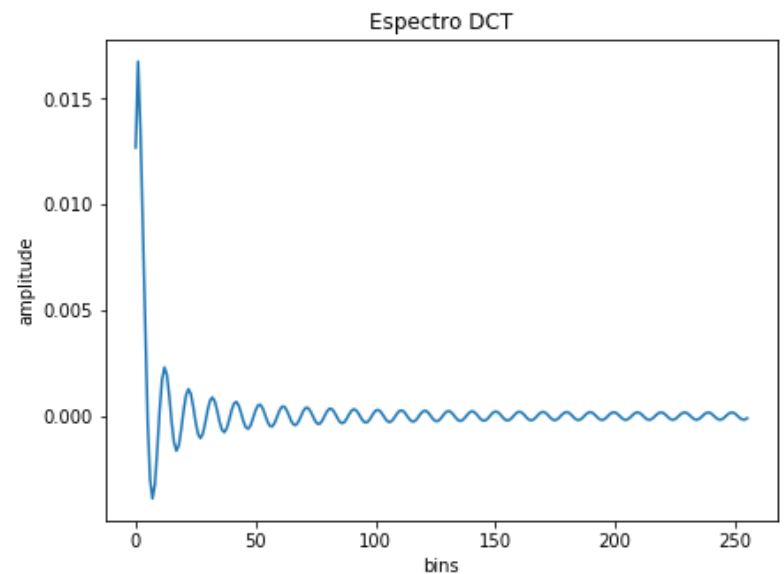
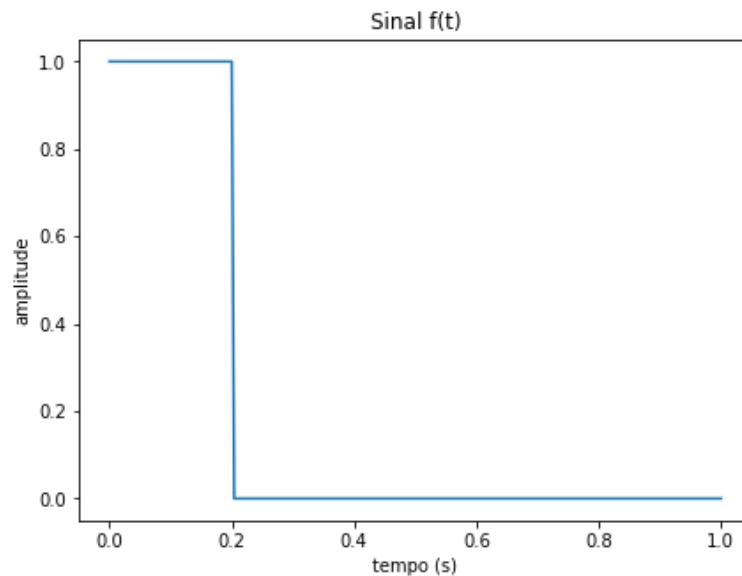


In [23]: `plot_threshold(f, c_max=0.5)`

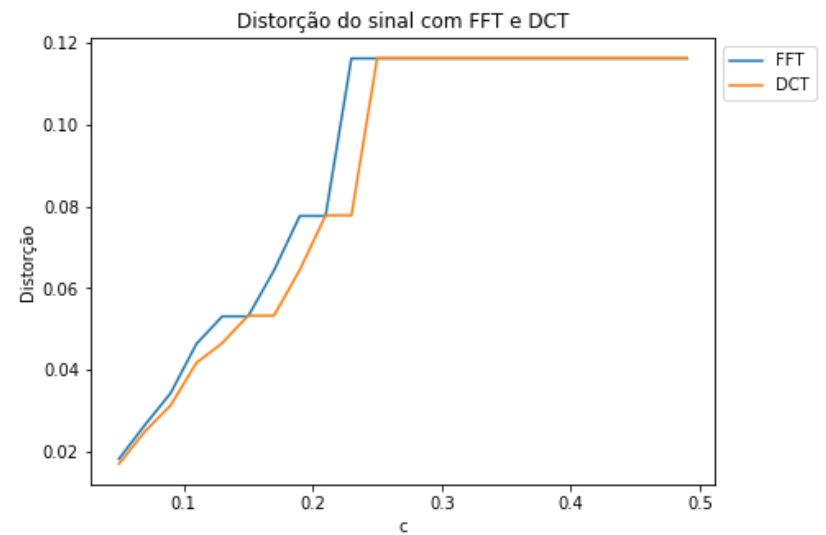
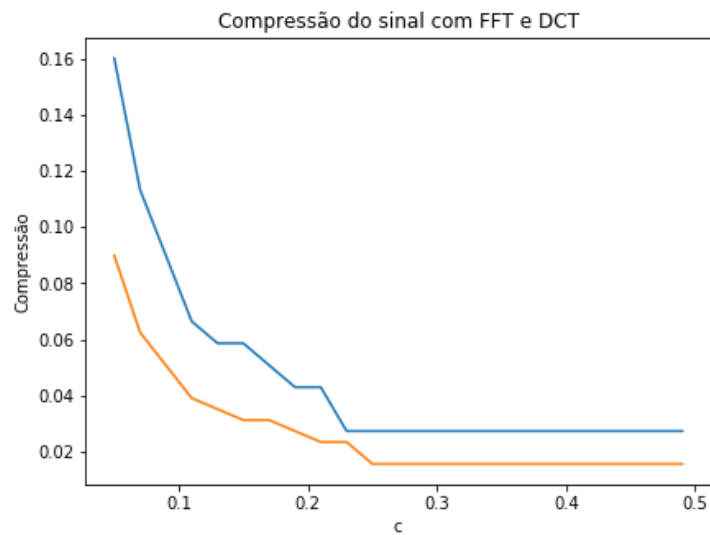


## Exemplo 2: Função degrau

```
In [24]: N = 256  
t = np.linspace(0, 1, N);  
f = np.zeros(N)  
f[0 : int(np.floor(0.2 * N+1))] += 1  
plot_func_dct(t,f)
```



In [25]: `plot_threshold(f, c_max=0.5)`



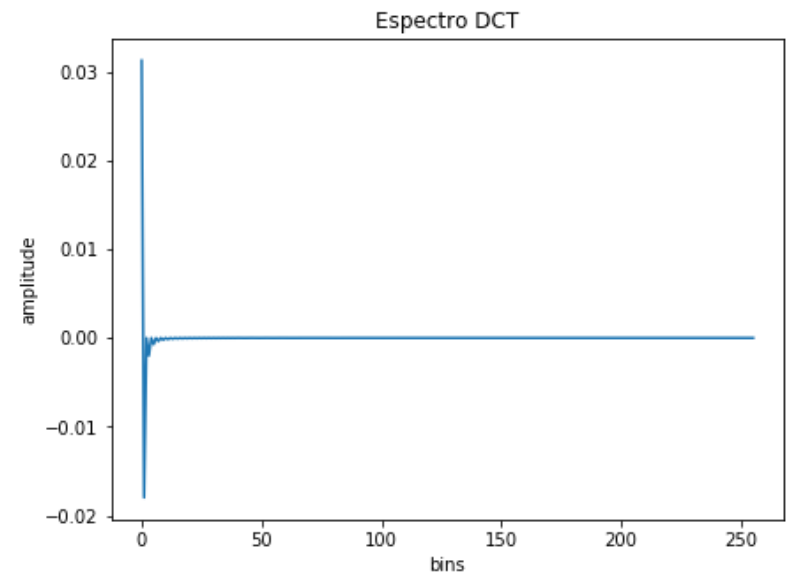
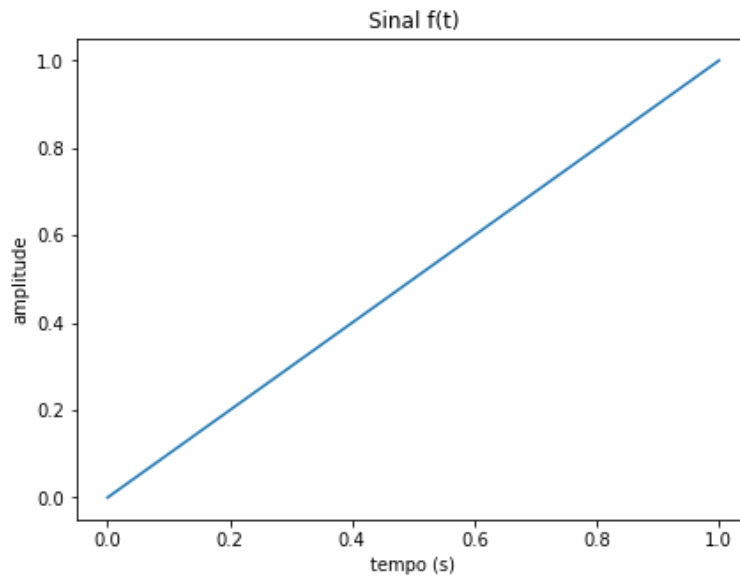
## Reconstrução da função degrau usando DCT (iterativo)

```
In [27]: # Cria o ambiente interativo
w = interactive(plt_sampled_signal, c=c,)
display(VBox([w.children[1], w.children[0]], layout=Layout(align_items='center'
)))
w.update()
```



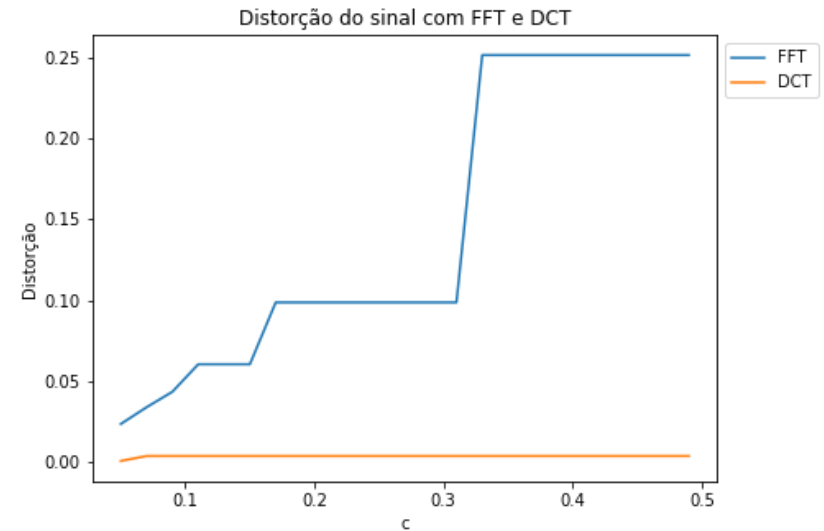
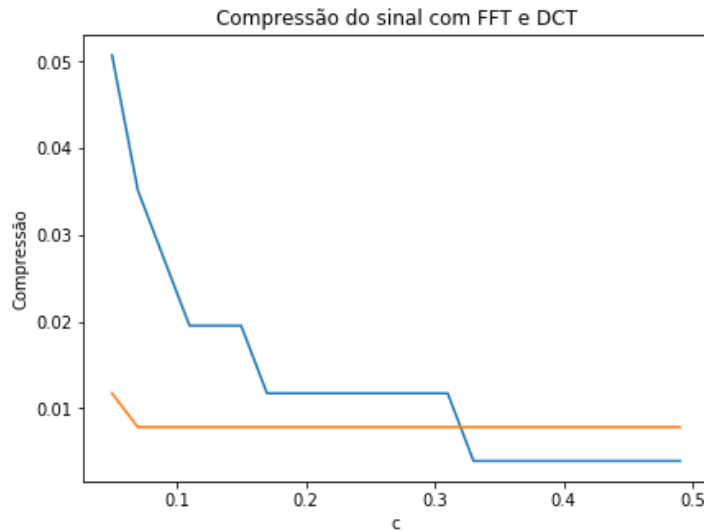
## Exemplo 3: Função $f(t) = t$

```
In [28]: N=256;  
t = np.linspace(0,1,N);  
f = t;  
plot_func_dct(t,f)
```



## Gráfico correspondente à Tabela 3.6 para $f(t) = t$

In [29]: `plot_threshold(f)`



## Reconstrução da função $f(t) = t$ usando DCT (iterativo)

```
In [31]: # Cria o ambiente interativo
w = interactive(plt_sampled_signal, c=c,)
display(VBox([w.children[1], w.children[0]], layout=Layout(align_items='center'
)))
w.update()
```

```

In [33]: X = np.fft.fft(f)
C1 = np.linspace(1e-8, 10 ** -0.3, 50)
P, D = comp_dist_list(f, C1, method='fft')
PC, DC = comp_dist_list(f, C1, method='dct')
plt.figure(figsize=(15, 5)); plt.plot(P, D, label='FFT'); plt.plot(PC, DC, label='DCT')
plt.title("$D(c)$ versus $P(c)$ na compressao de $f(t)=t$ usando FFT e DCT"); plt
.xlabel("$P(c)$"); plt.ylabel("$D(c)$"); plt.xlim([0, 0.5])
plt.legend(loc='upper left', bbox_to_anchor=(1, 1)); plt.show()

```

