

## DATA VISUALIZATION BASICS

Multidimensional Projections and  
Similarity Trees/  
Text / other applications

Rosane Minghim  
2019-2

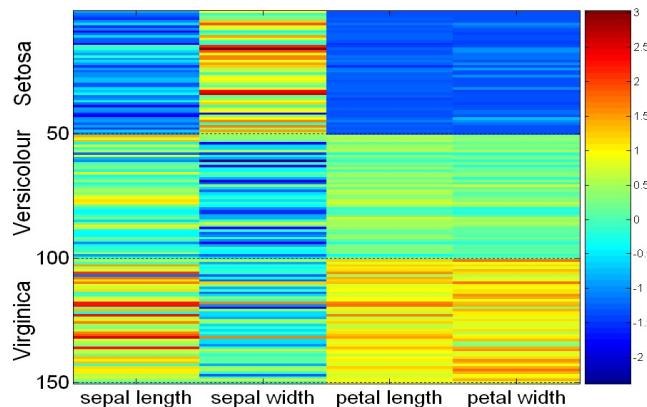
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Multidimensional Visualization  
Projections/Multidimensional Projections  
Document Collections  
Image Collections

- Visualization
- Visual Mining and Visual Analysis
- Projections
- Examples:
  - Text and Images

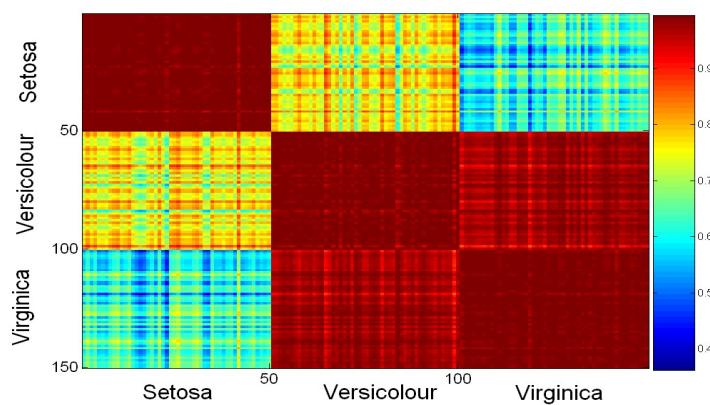
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## Data Matrix



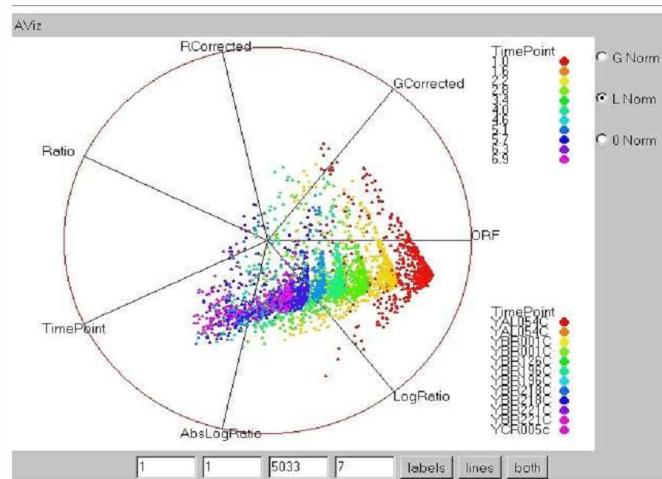
4

## Correlation Matrix

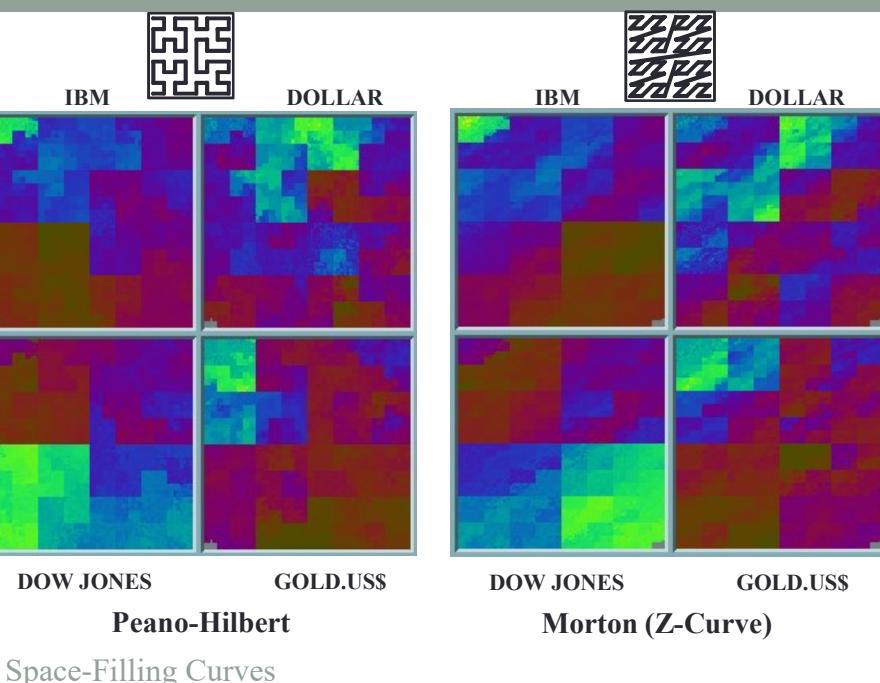


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## RadViz

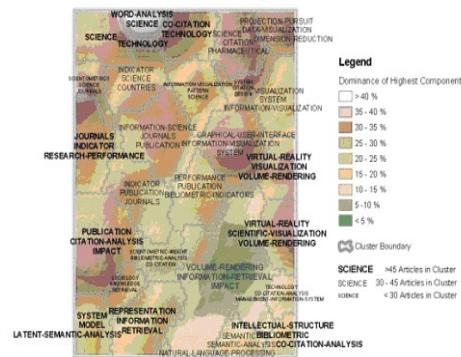


6



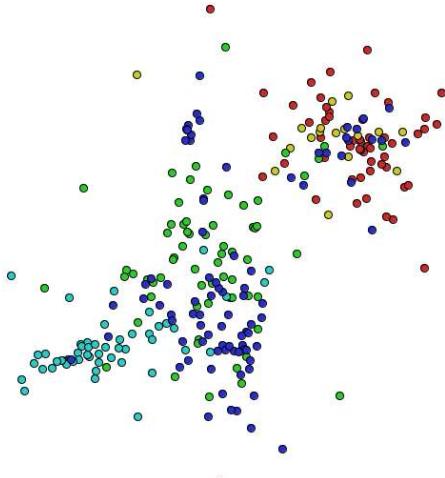
## SOM based

- Self-Organization Maps (SOMs) cartográficos (ex. Skurpin 2002)



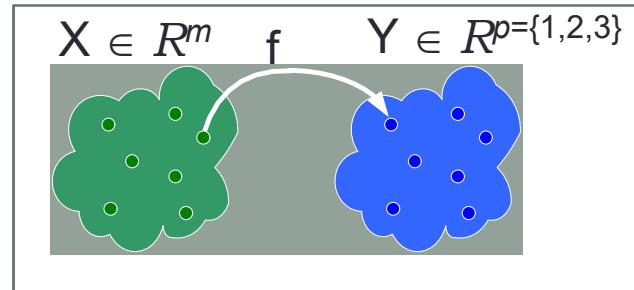
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Mapeamento para o plano permitindo a exploração.  
Ex: Patents **surgery**, **drugs**, **molecular bio**



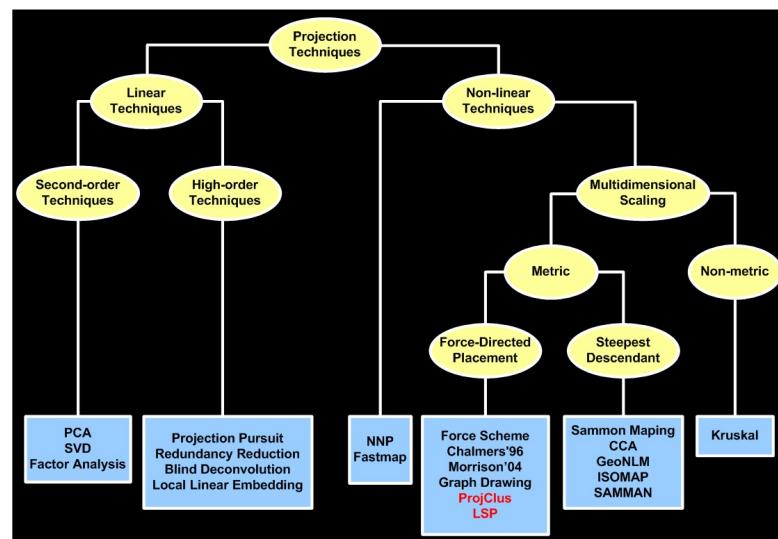
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## Projection Techniques



- $\delta: x_i, x_j \rightarrow R, x_i, x_j \in X$
- $d: y_i, y_j \rightarrow R, y_i, y_j \in Y$
- $f: X \rightarrow Y, |\delta(x_i, x_j) - d(f(x_i), f(x_j))| \approx 0, \forall x_i, x_j \in X$

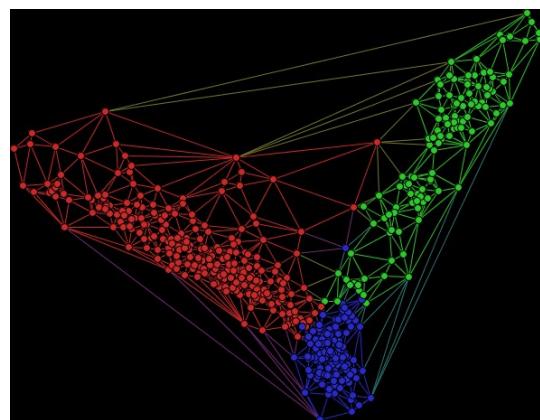
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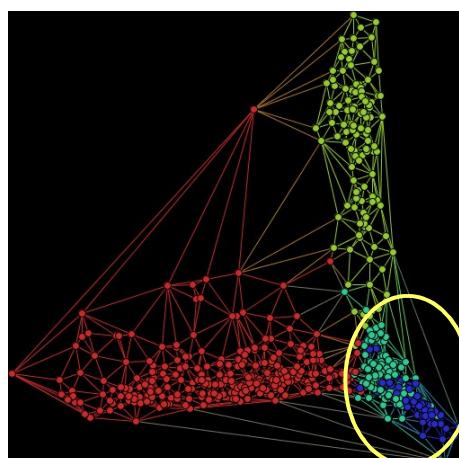
## Problems PCA

390 dimensions



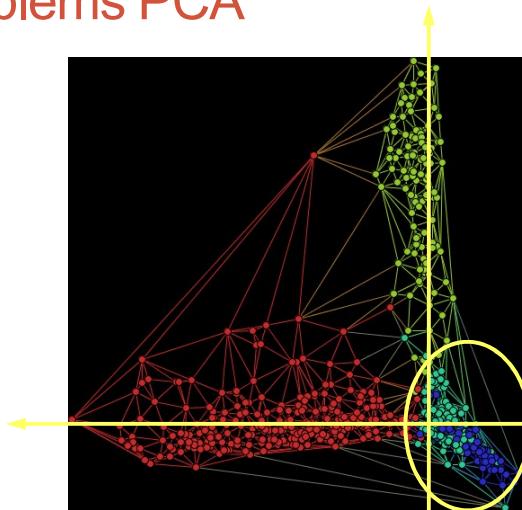
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## Problems PCA



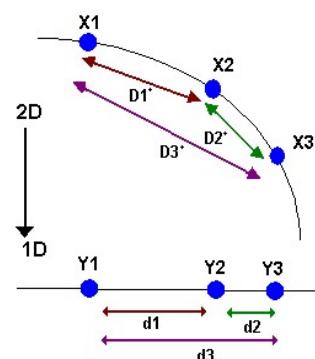
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## Problems PCA



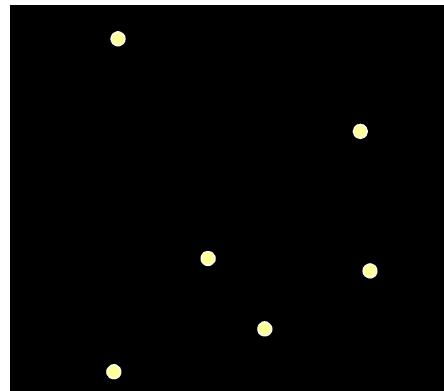
## Ex: Sammon Mapping

- Let  $\mathbf{X}$  be the points in the original space  $\mathbb{R}^n$ , we apply a distance measure  $d_{ij}^*$  between  $X_i$  and  $X_j$ , and find  $\mathbf{Y}$ , the projected point, ex.  $\mathbb{R}^2$  and  $d_{ij}$  the Euclidean distance between them.
- Sammon's method applies an error function to measure the target.



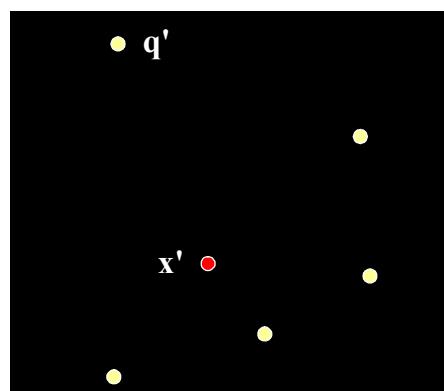
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## Force Based Point Placement



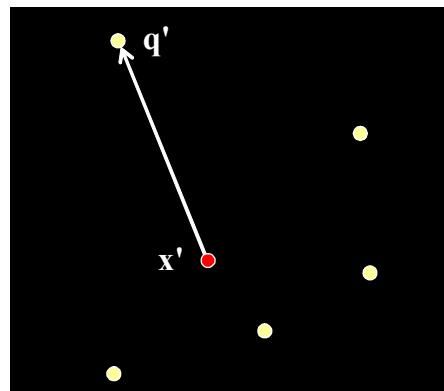
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## Force Scheme [Tejada et al., 2003]



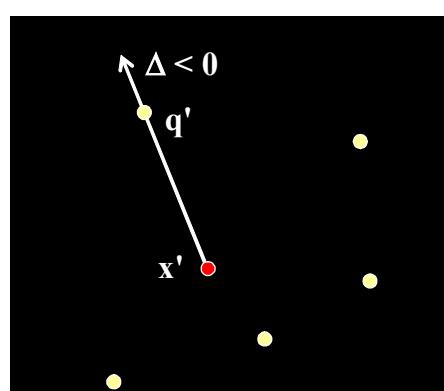
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## Force Scheme [Tejada et al., 2003]



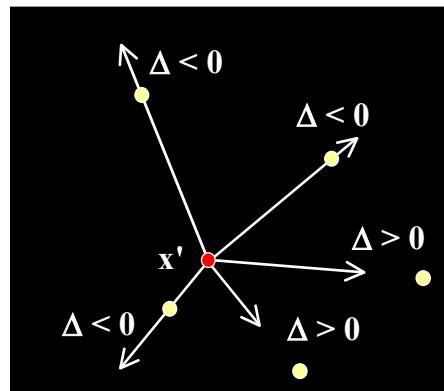
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## Force Scheme [Tejada et al., 2003]



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## Force Scheme [Tejada et al., 2003]



## Force Scheme [Tejada et al., 2003]

1. Map each point  $X$  to the plane (fastmap, nnp, etc.)
2. For each projected point  $x$ 
  1. For each projected point  $q' \neq x'$ 
    1. Compute the vector  $v$  of  $\langle x' \text{ to } q' \rangle$
    2. Move  $q'$  in direction of  $v$ , one fraction of  $\Delta$
$$\Delta = \frac{\delta(x, q) - \delta_{\min}}{\delta_{\max} - \delta_{\min}} - d(x', q')$$
  3. Normalize the coordinates between  $[0,1]$

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## LSP [Paulovich et al., 2006/2008]

- Least-Square Projection (LSP)
- Core idea: project a sub-set of points and interpolate the rest.
- Interpolation seeks to preserve the neighborhood between points.
- Each point is mapped within the convex hull of its neighbors.

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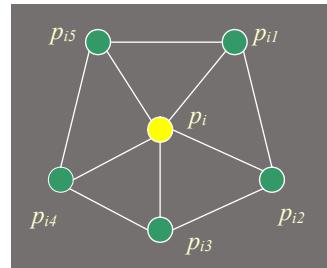
## LSP [Paulovich et al., 2006/2008]

- Three main steps:
  1. Select a subset of points(control points) and Project these in  $R^p$
  2. Determine the neighborhood of points
  3. Create a linear system whose answers are the Cartesian coordinates of points  $p_i$  in  $R^p$

## LSP: Laplacian Matrix

- Let  $V_i = \{p_{i1}, \dots, p_{ik}\}$  be the neighborhood of a point  $p_i$  and  $c_i$  the coordinates of  $p_i$  in  $\mathbb{R}^p$

$$c_i - \frac{1}{ki} \sum_{p_j \in V_i} c_j = 0$$



- Each  $p_i$  will be the centroid of points in  $V_i$

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## LSP: Laplacian Matrix

$$Lx_1=0, Lx_2=0, \dots, Lx_p=0$$

where  $x_1, x_2, \dots, x_p$  are vectors containing the Cartesian coordinates of the points

and  $L$  is the matrix defined by:

$$L_{ij} = \begin{cases} 1 & i = j \\ -\frac{1}{ki} & p_j \in V_i \\ 0 & otherwise \end{cases}$$

$$\boxed{L} = \boxed{\begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{pmatrix}} = \boxed{\begin{pmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{pmatrix}}$$

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## LSP: Adding control points

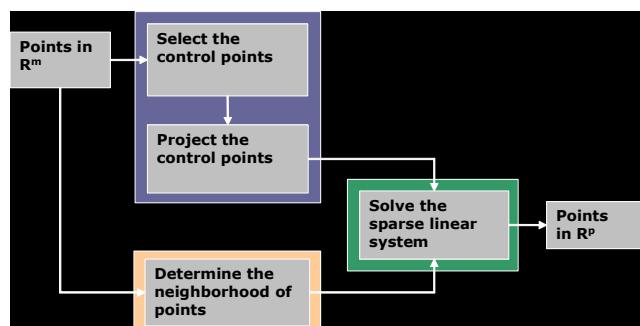
$$A = \begin{pmatrix} L \\ C \end{pmatrix} \quad C_{ij} = \begin{cases} 1 & p_j \text{ is a control point} \\ 0 & \text{otherwise} \end{cases}$$

$$b_i = \begin{cases} 0 & i \leq n \\ x_{p_{c_i}} & n < i \leq n + nc \end{cases}$$

$$\begin{pmatrix} & & & & \\ & & & & \\ & & L & & \\ & & & & \\ & 0 & 1 & 0 & \cdots & 0 \\ & 0 & \cdots & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ c_1 \\ c_2 \end{pmatrix}$$

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## LSP: Overview



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## LSP: Exemplo de Sistema

$$v_1 = \{p_3 p_4 p_6\}$$

$$v_2 = \{p_5 p_4 p_6\}$$

$$v_3 = \{p_1 p_5 p_6\}$$

$$v_4 = \{p_1 p_6\}$$

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$$v_6 = \{p_1 p_2 p_4 p_5\}$$

$$L = \begin{bmatrix} 1 & 0 & -1/3 & -1/3 & 0 & -1/3 \\ 0 & 1 & 0 & -1/3 & -1/3 & -1/3 \\ -1/3 & 0 & 1 & 0 & -1/3 & -1/3 \\ -1/2 & 0 & 0 & 1 & 0 & -1/2 \\ 0 & -1/3 & -1/3 & 0 & 1 & -1/3 \\ -1/4 & -1/4 & 0 & -1/4 & -1/4 & 1 \end{bmatrix}$$

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$$pc = \{p_3 p_6\}$$

L

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L

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## LSP: Solving the system

- It is necessary to solve  $Ax = b$
- The system is solved by using least squares

$$\|Ax - b\|^2$$

- The analytical solution is

$$A^T A x = A^T b \Rightarrow x = (A^T A)^{-1} A^T b$$

- $A^T A$  is symmetric and sparse and can be solved using the factorization of Cholesky

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## Choosing the Control Points

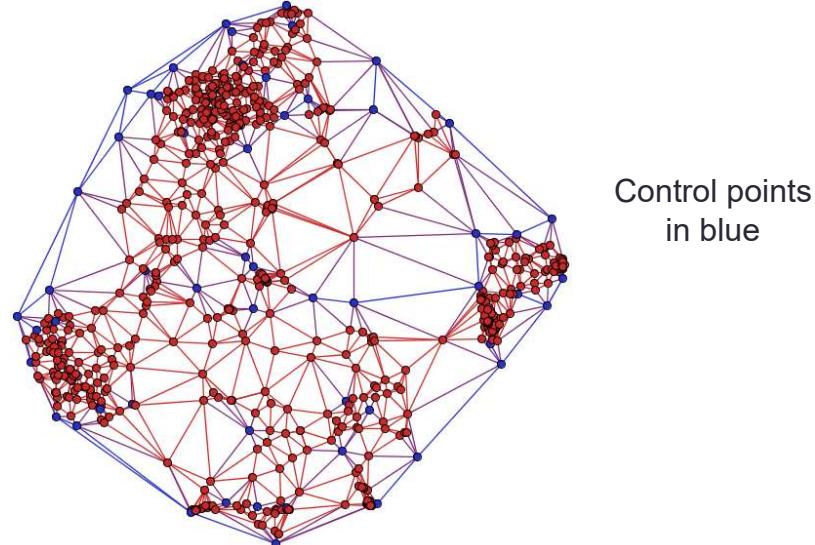
- In order to select the control points
  - the space  $R^m$  is split into  $nc$  clusters using k-medoids.
  - the control points are the medoids of each cluster

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## Choosing the Control Points

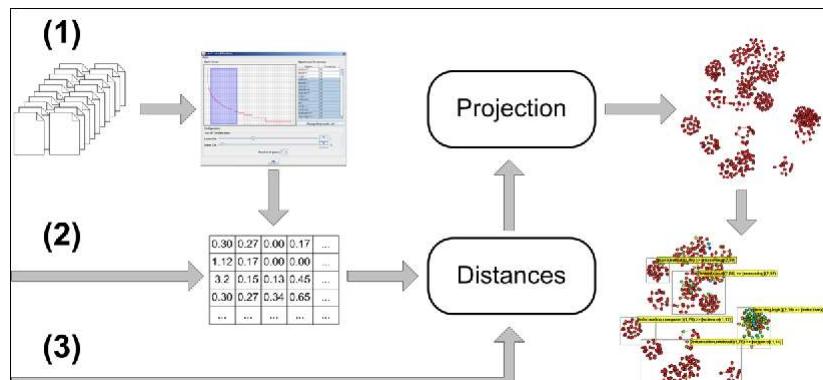
- Once the control points are chosen, these points are projected onto  $R^d$  through a fast dimensionality reduction method
  - Fast Projection (Fastmap or NNP)
  - Force Placement

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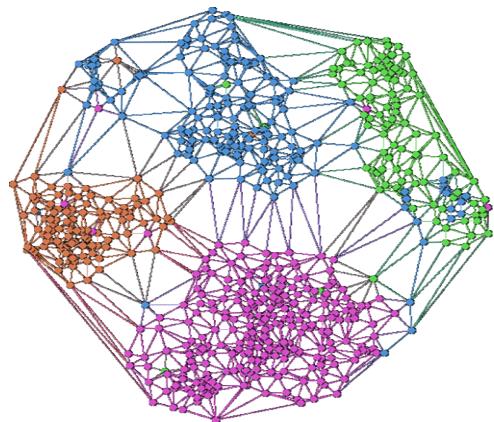
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## Content – based by Projections



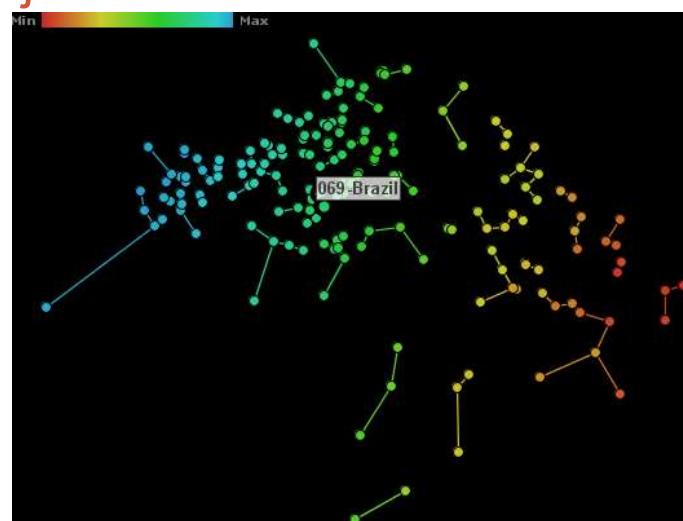
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## Projection



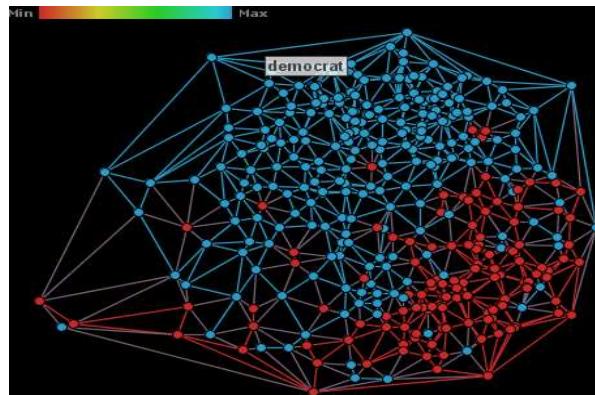
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## Projection: HDI



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## Projection: Voting



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## Stochastic Neighborhood Embedding sne and t-sne

- Distance in original space

$$p_{j|i} = \frac{\exp(-\|x_i - x_j\|^2 / 2\sigma_i^2)}{\sum_{k \neq i} \exp(-\|x_i - x_k\|^2 / 2\sigma_i^2)},$$

- Distance in projected space

$$q_{j|i} = \frac{\exp(-\|y_i - y_j\|^2)}{\sum_{k \neq i} \exp(-\|y_i - y_k\|^2)}$$

- Cost function

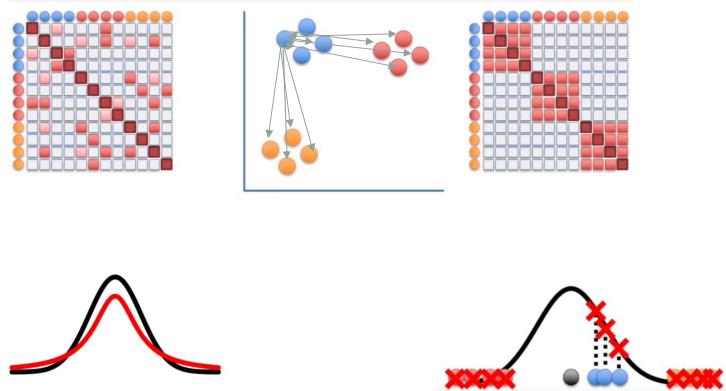
$$C = \sum_i KL(P_i || Q_i) = \sum_i \sum_j p_{j|i} \log \frac{p_{j|i}}{q_{j|i}}$$

- Non-gaussian neighborhoods: t-sne

L.J.P. van der Maaten and G.E. Hinton. **Visualizing High-Dimensional Data Using t-SNE**. *Journal of Machine Learning Research* 9(Nov):2579-2605, 2008

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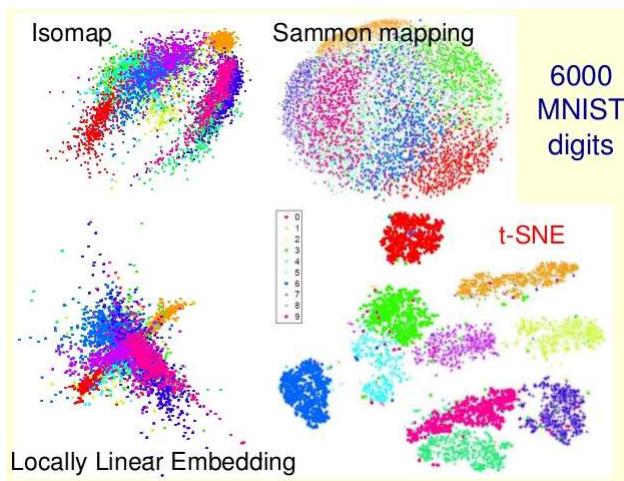
## Stochastic Neighborhood Embedding sne and t-sne



Source: StatQuest (adapted)

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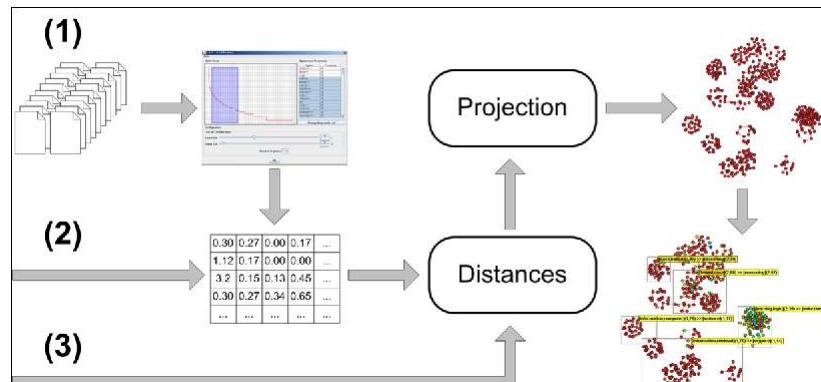
## T-sne Examples



Source: <https://www.slideshare.net/xuyangela/an-introduction-to-tsne>

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## Visualization by Projections



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## The case of document collections

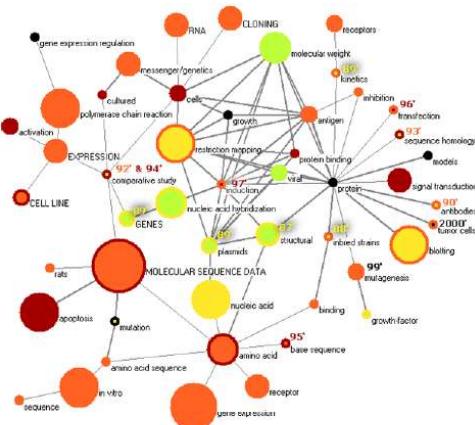
- Applications
  - Teaching/Research
  - Search
  - Investigation
  
- Patents
- Medical reports
- News

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- Maps of text Collections
- Based on Relationships (Borner & Chen)
  - Co-authorship, co-citation
- Based on Content
  - Similarity and Grouping
  - Common underlying subject
  - → Topics

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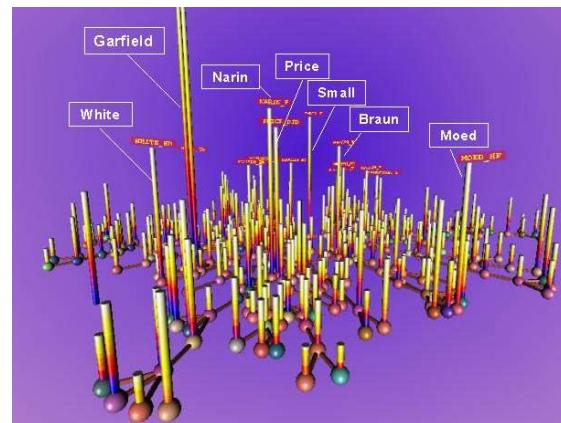
## Relationships : Topic Busts and co-word



(Mane and Borner)  
2004

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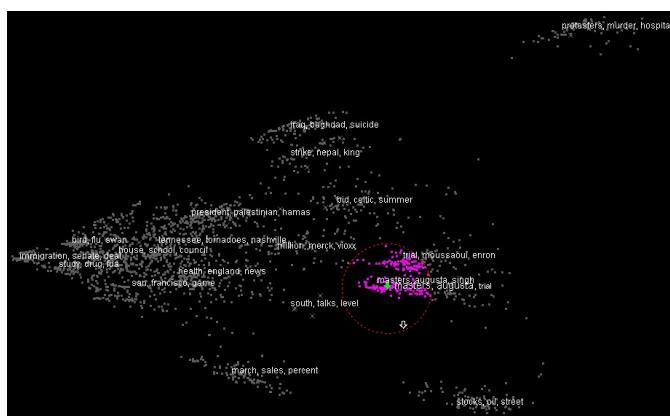
## Relationships : Citation and Co-citation



(Borner)  
(2003)

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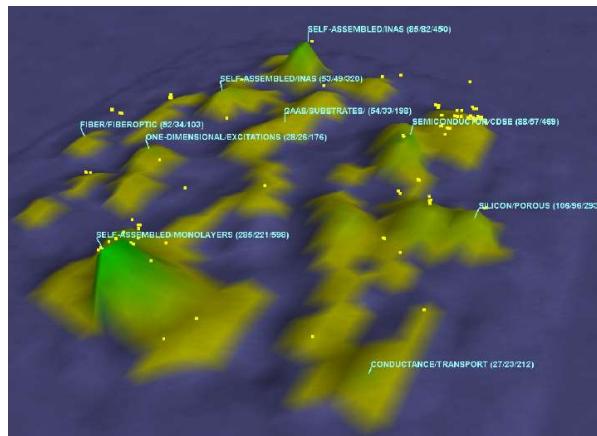
## Content - based



(Dimensional  
Reduction)  
News flash  
IN-SPIRE  
(PNL)

## VxInsight

- Sandia National Laboratories, mountain metaphor (Boyack et al., 2002).



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## Text Preprocessing

1. Stopwords elimination
2. Extraction of words radicals (stemming)
3. Creation of n-grams
4. Frequency count and Luhn's lower cut (n-grams appearing less than x times are ignored)
5. Weighting process (*term-frequency inverse document-frequency - (tfidf)*)

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## Result is a Vector Model

- Attributes: terms (n-grams)
- Value: term weight
- Table Data

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## Vector Representation – term weighting

- tf – term frequency
- tfidf –  $tf \times idf = tf \times \text{inverse document frequency}$

$$w_{ik} = tf_{ik} \times \log \left( \frac{N}{n_k} \right)$$

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## Vector Representation

	term <sub>1</sub>	term <sub>2</sub>	term <sub>3</sub>	term <sub>4</sub>	...	term <sub>m</sub>
Doc <sub>1</sub>	0.92	0.62	0.92	0.10	...	0.67
Doc <sub>2</sub>	0.13	0.11	1.00	0.34	...	0.33
Doc <sub>3</sub>	0.52	0.00	0.00	0.44	...	0.77
...	...	...	...	...	...	...
Doc <sub>n</sub>	0.02	0.12	0.22	0.92	...	0.00

70

## Vector Representation – Similarity calculation

### EUCLIDEAN

$$sim_{i,j} = \sqrt{(w_{i,1} - w_{j,1})^2 + \dots + (w_{i,k} - w_{j,k})^2}$$

### MANHATTAN

$$sim_{i,j} = |w_{i,1} - w_{j,1}| + \dots + |w_{i,k} - w_{j,k}|$$

### COSINE

$$sim_{i,j} = \frac{(w_{i,1} \times w_{j,1}) + \dots + (w_{i,k} \times w_{j,k})}{\sqrt{(w_{i,1}^2 + \dots + w_{i,k}^2) \times (w_{j,1}^2 + \dots + w_{j,k}^2)}}$$

71

## Vector Representation – distance calculation

$$dis(doc_i, doc_j) = \sqrt{2 * (1 - sim(doc_i, doc_j))}$$

$$sim(doc_i, doc_j) = \frac{doc_i \times doc_j}{\|doc_i\| * \|doc_j\|}$$

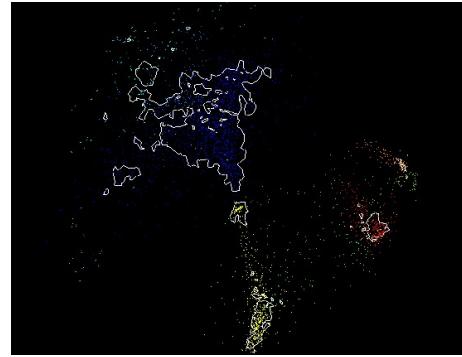
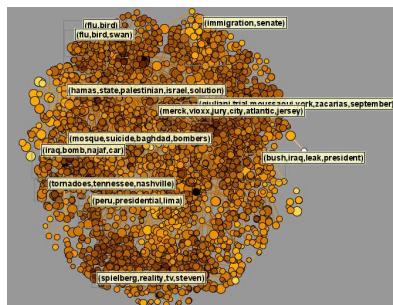
73

## Alternatives to Vector Representation

- Similarity Calculation text against text
  - Word2Vec, Doc2Vec (see <https://www.tensorflow.org/tutorials/representation/word2vec>)
  - Ex: NCD Normalized Compression Distance
    - Approximation of Kolmogorov Complexity
    - Ver: G. P. Telles, R. Minghim, and F. V. Paulovich. 2007. Visual Analytics: Normalized compression distance for visual analysis of document collections. *Comput. Graph.*, 31, 3 (June 2007), 327-337. DOI=<http://dx.doi.org/10.1016/j.cag.2007.01.024>
  - Editing distance
    - Dice's coefficient
    - Matching's coefficient
    - Overlap's coefficient
    - Qgram Distance
    - Ver: Frizzi San Roman Salazar. Um estudo sobre o papel de medidas de similaridade na visualização de coleções de documentos. 2012. Dissertação (Mestrado em Ciências da Computação e Matemática Computacional) - Instituto de Ciências Matemáticas e de Computação, Fundação de Amparo à Pesquisa do Estado de São Paulo. Orientador: Maria Cristina Ferreira de Oliveira.

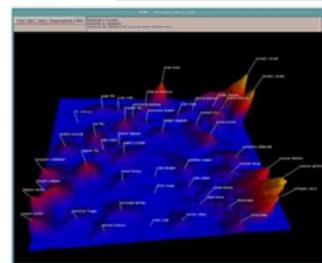
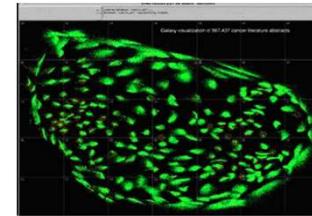
75

## Visual representations: graphs, surfaces, volumes, triangulations



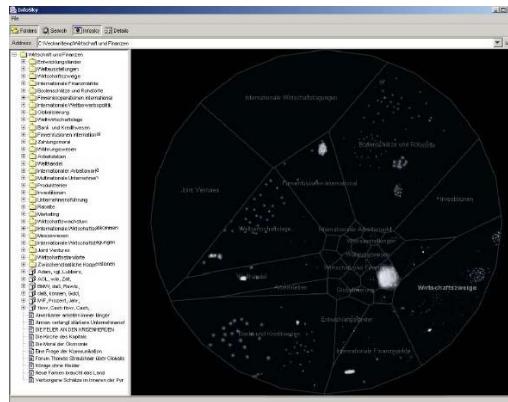
## IN-SPIRE

- Spatial Paradigm for Information Retrieval - Pacific Northwest National Laboratories
- Two Visualization Metaphors:
  - Galaxies – dimensional reduction
  - Themescape

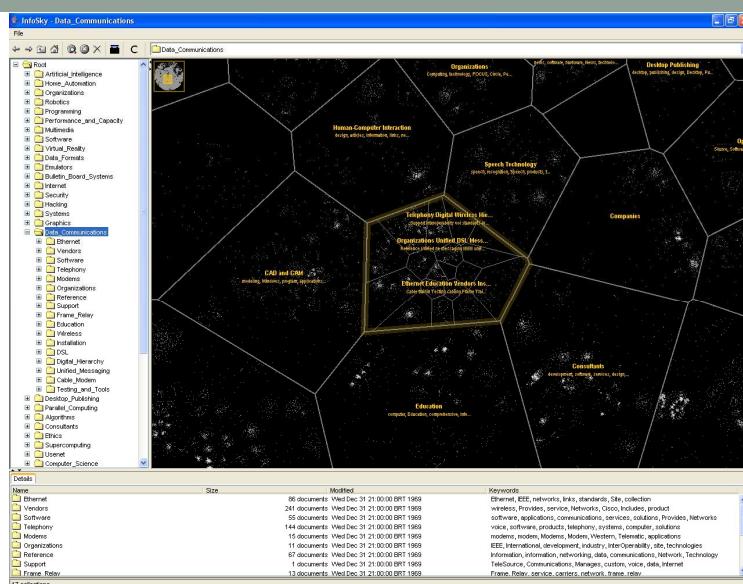


## InfoSky

Granitzer (Granitzer et al., 2004) also employs galaxy metaphor



80

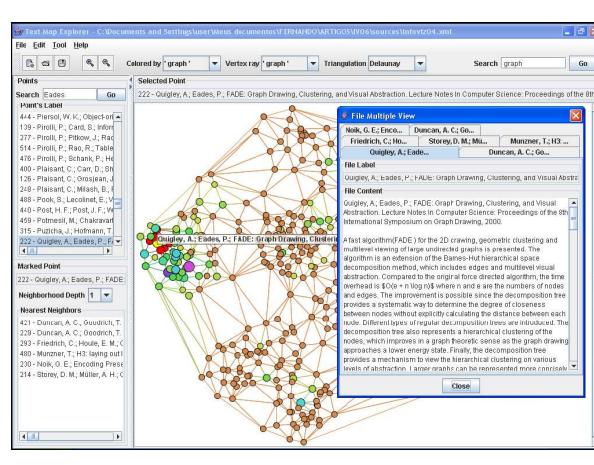


[http://en.know-center.at/forschung/wissenserschliessung/downloads\\_demos/infosky\\_demo](http://en.know-center.at/forschung/wissenserschliessung/downloads_demos/infosky_demo)

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## Projection Explorer (PEx)

- Projection and Point placement
- Precision
- Graphs and surfaces (Super Spider)



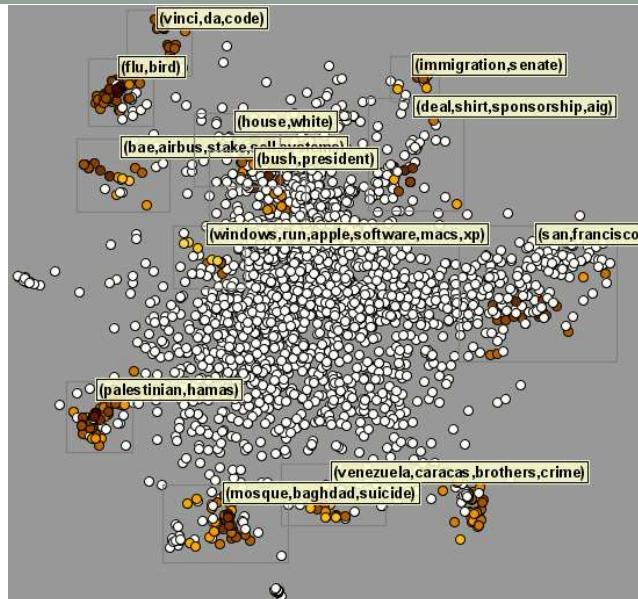
83

## Mapping Text Collections via Projections and Point Placement

- Positioning and labeling



84

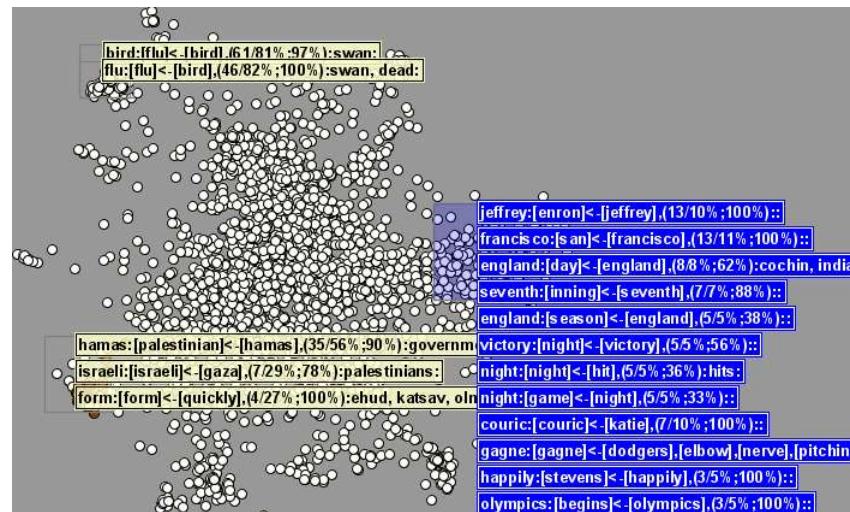


85

- Detailing topics



86

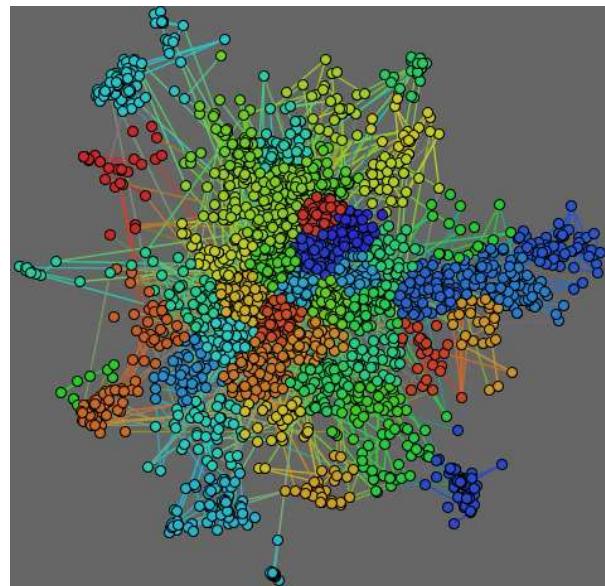


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- Finding Relationships



88

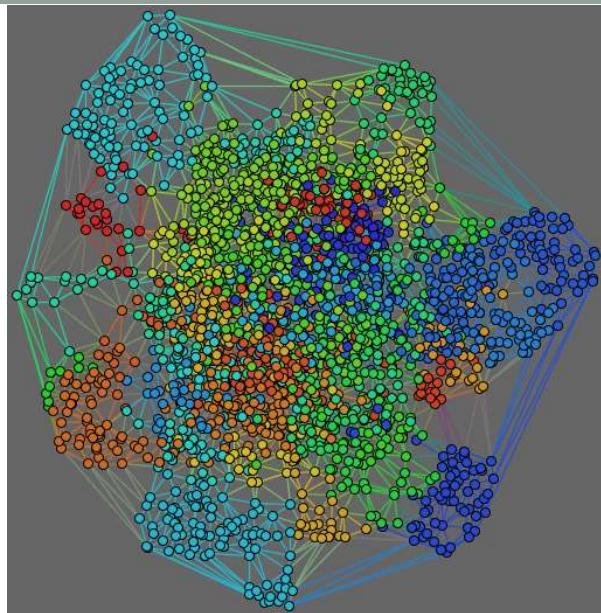


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- Building a mesh



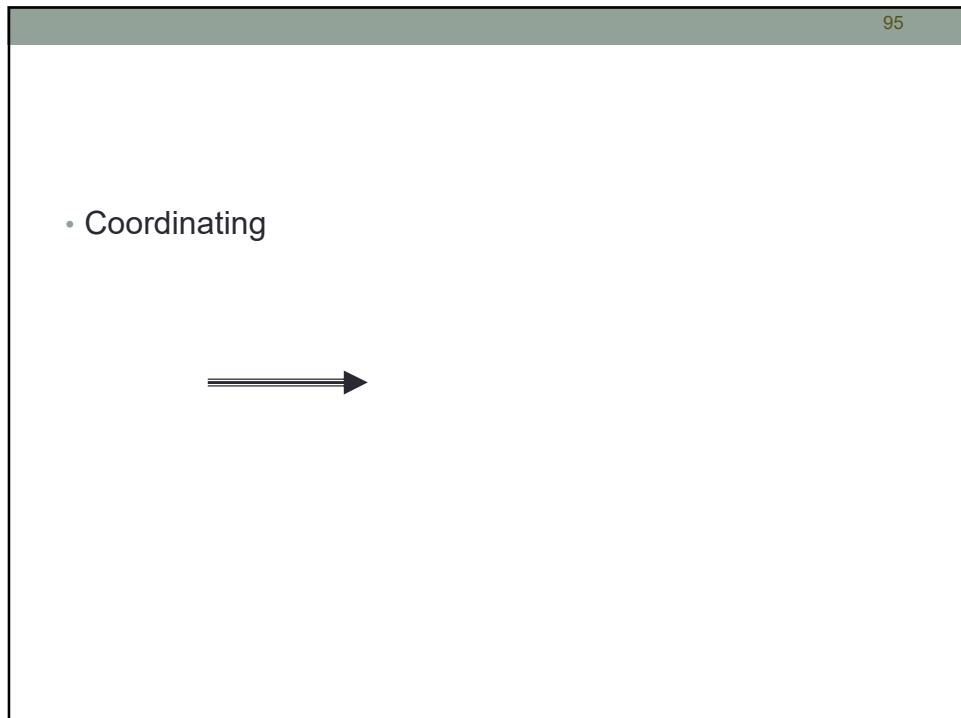
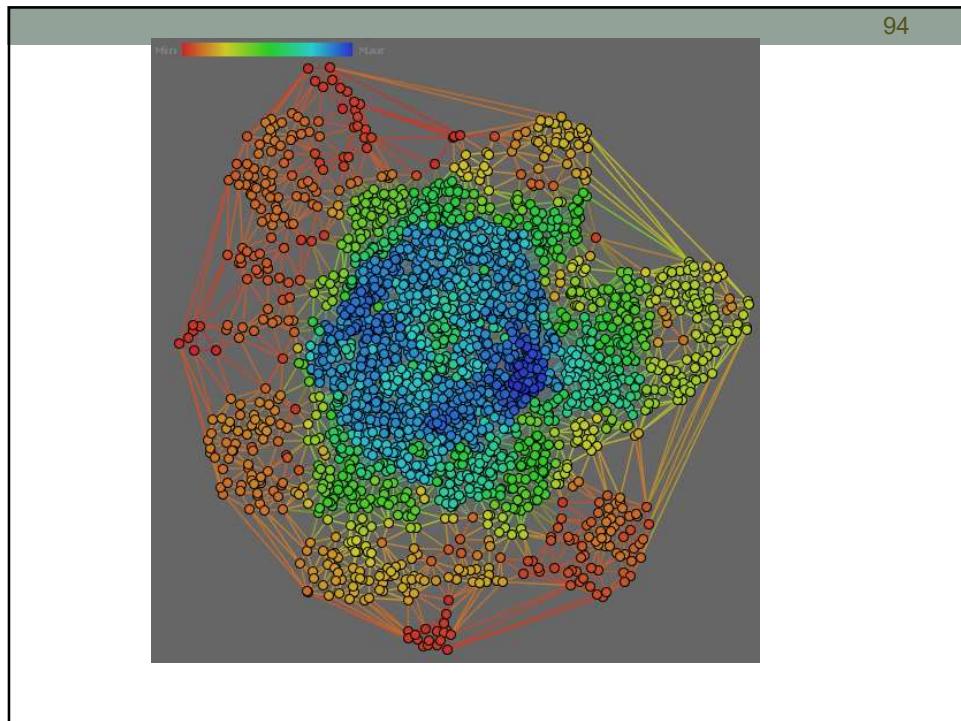
92



93

- Coloring by degree of proximity



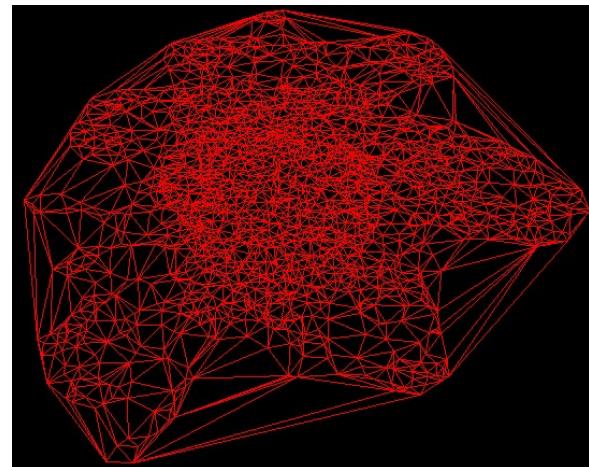
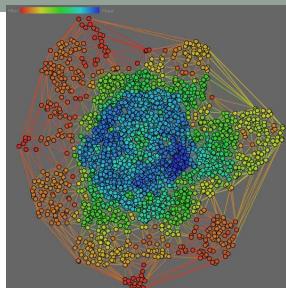


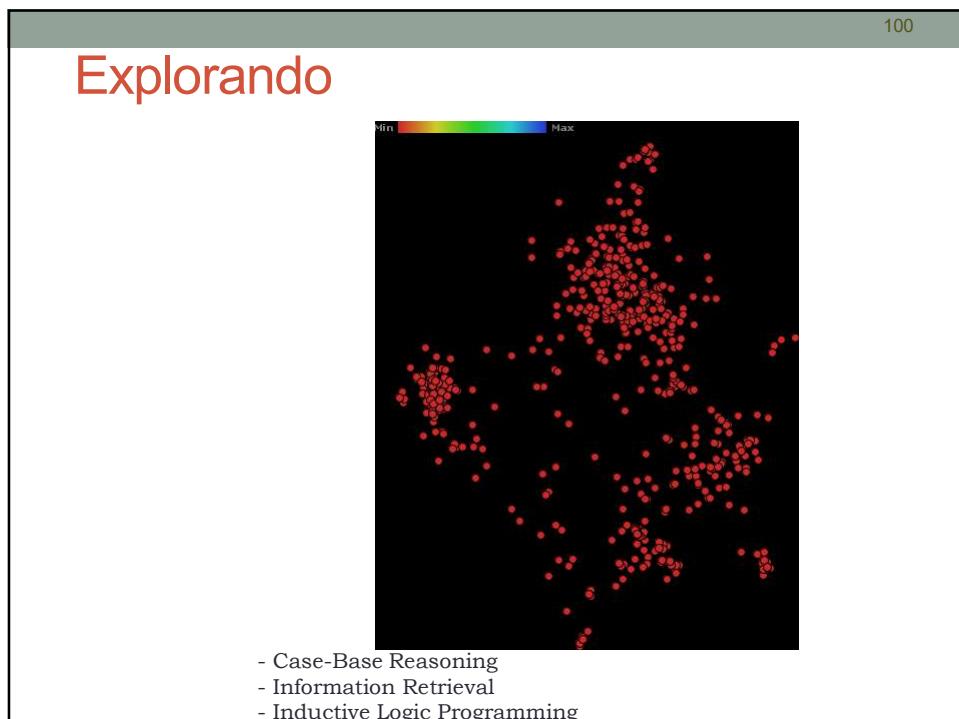
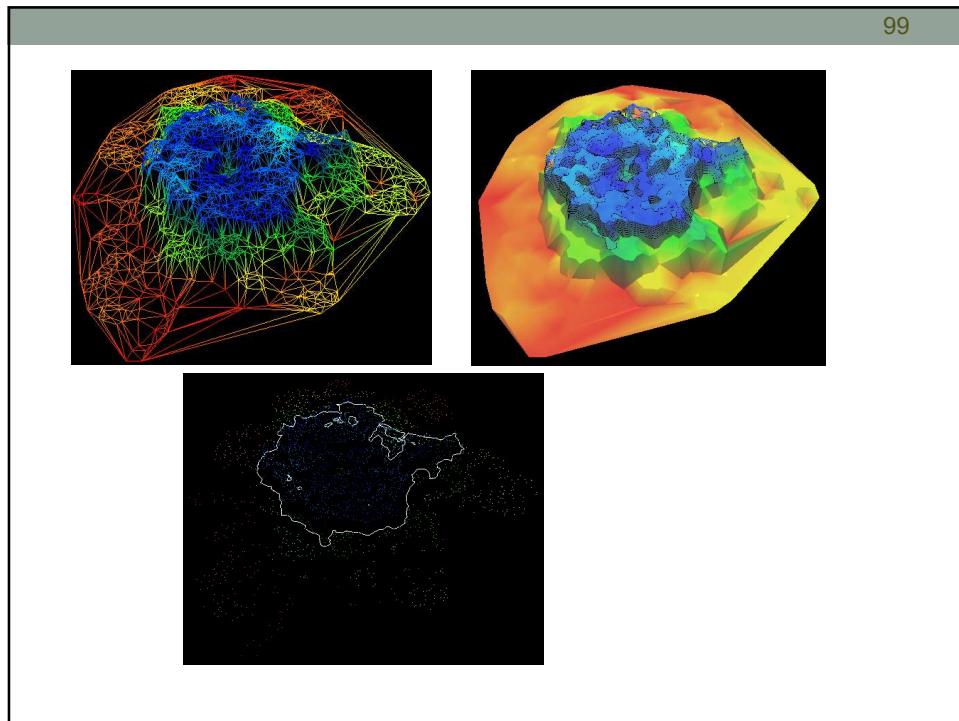
97

- Building a Surface



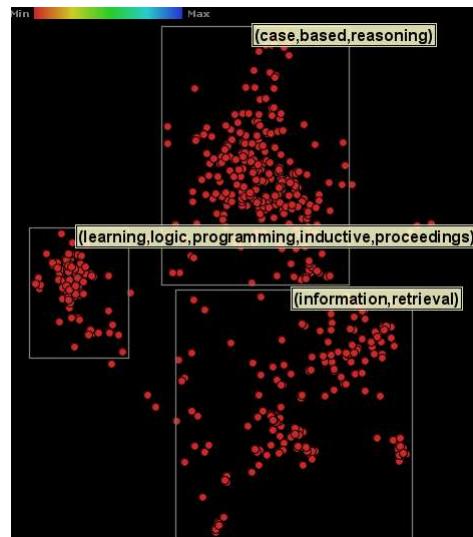
98



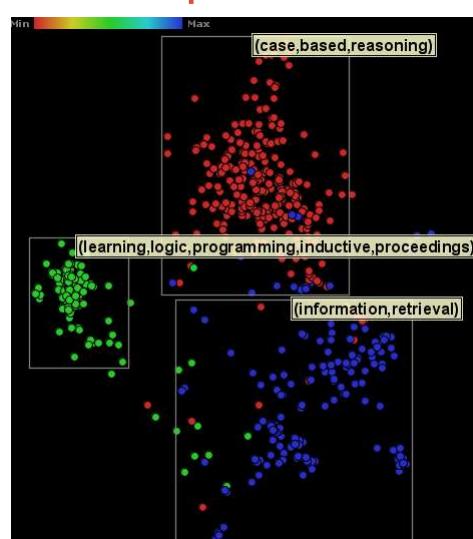


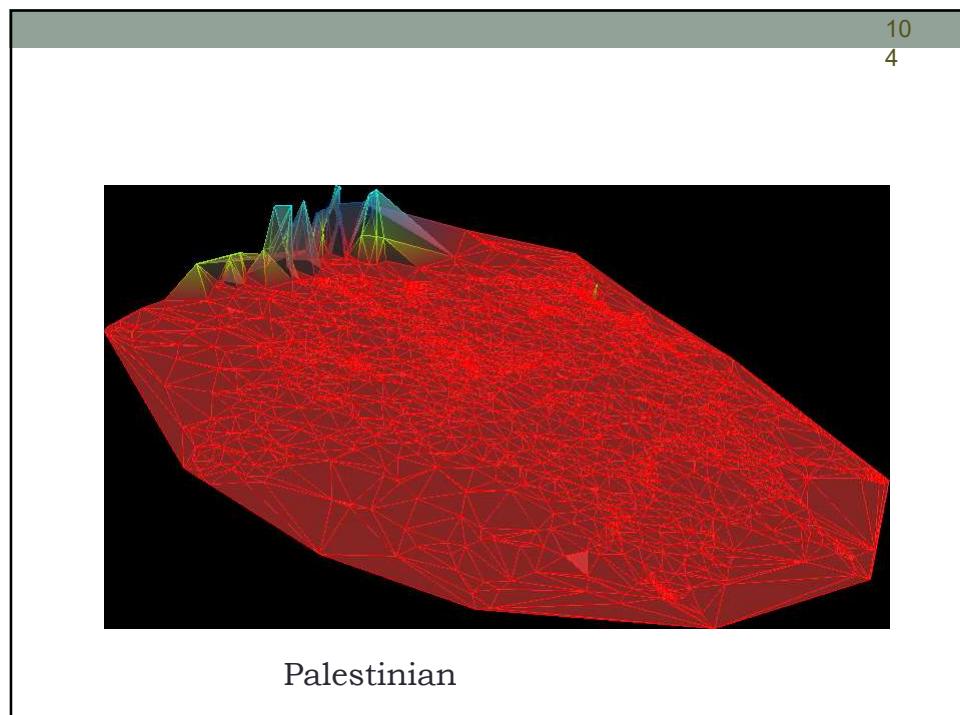
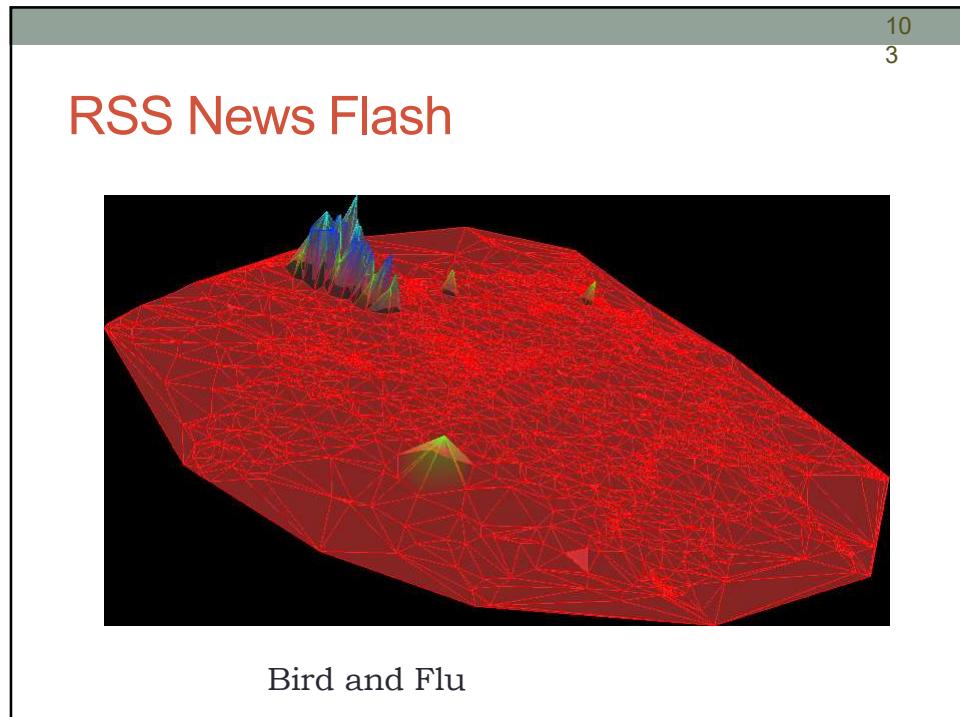
10  
1

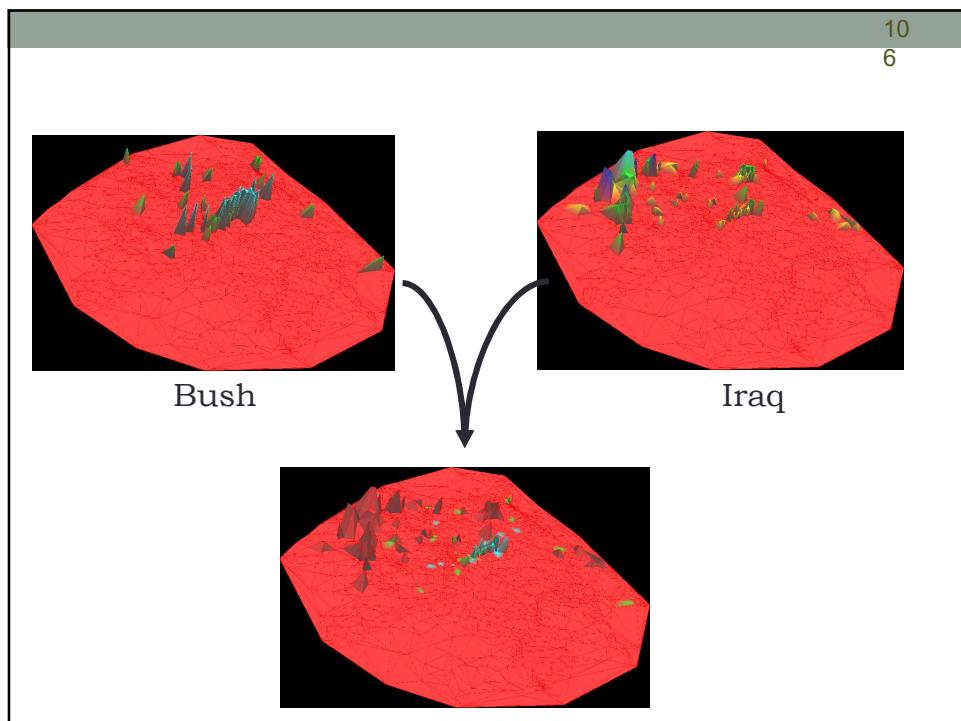
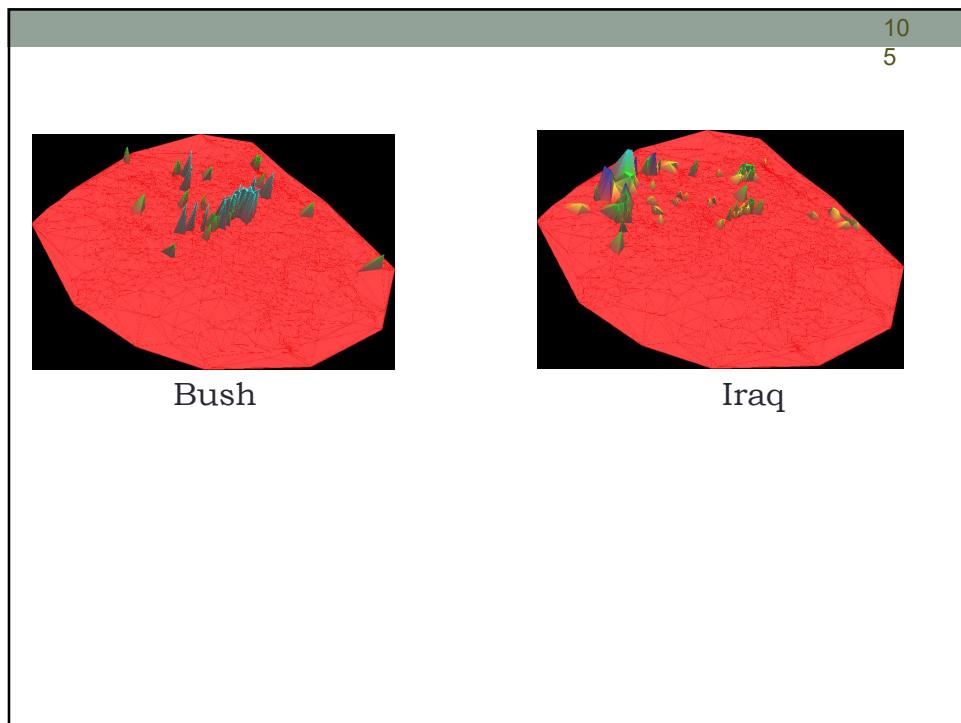
## Exemplos de Mapas

10  
2

## Exemplos de Mapas

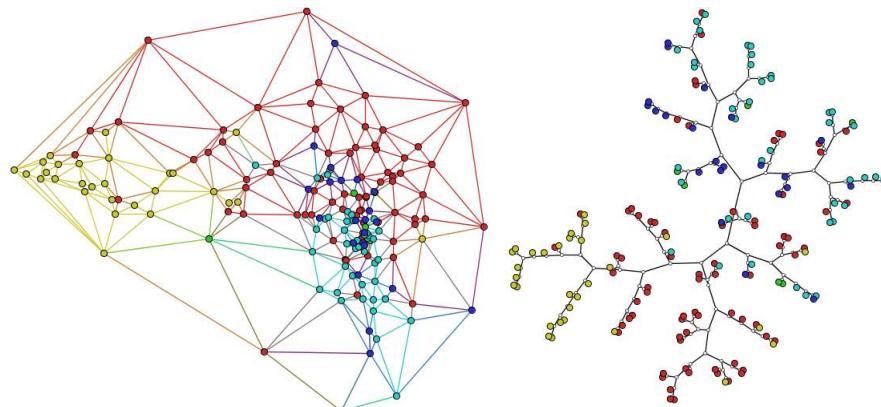






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## Further Example - patents

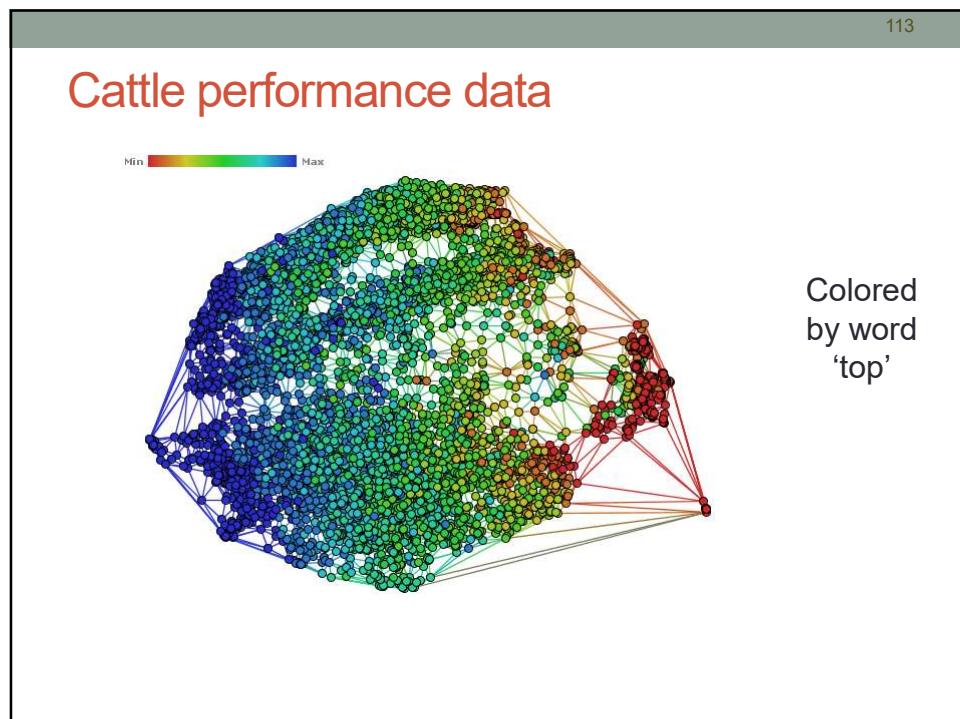
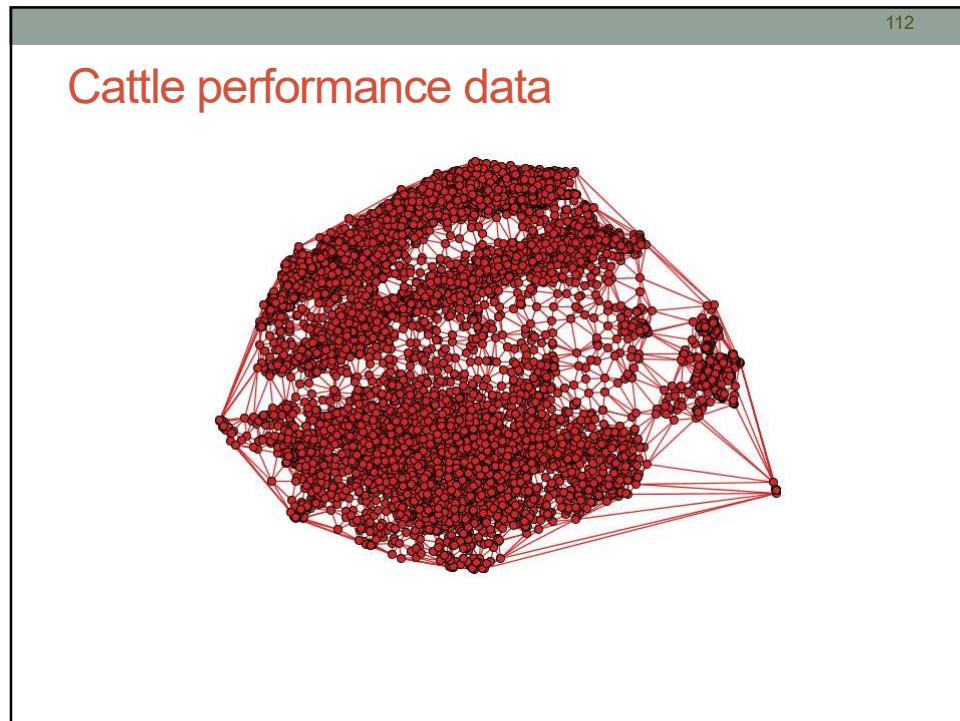


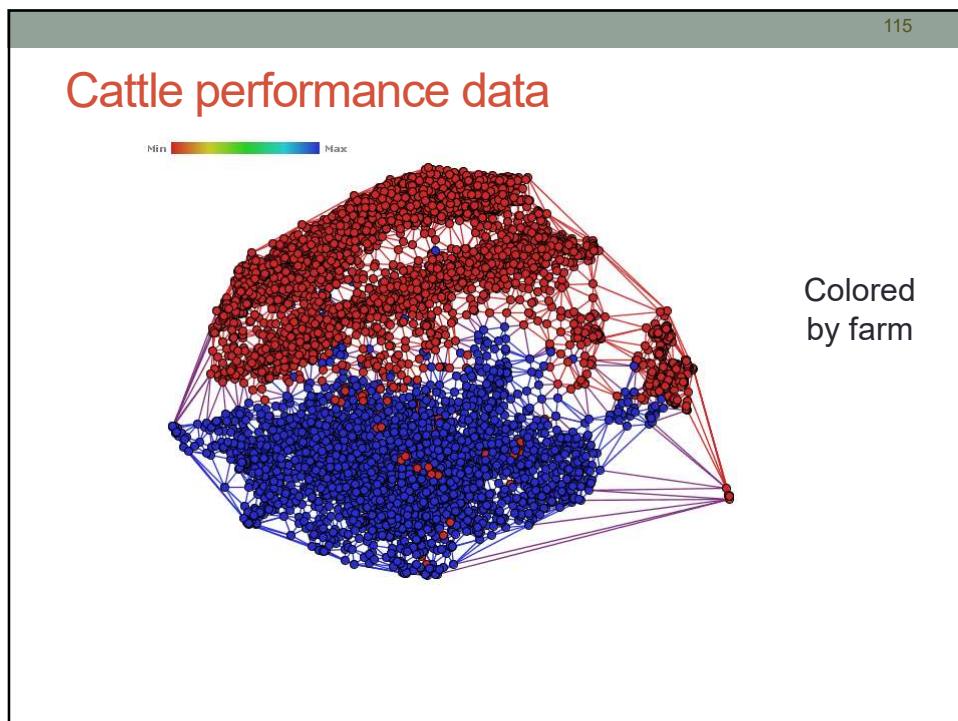
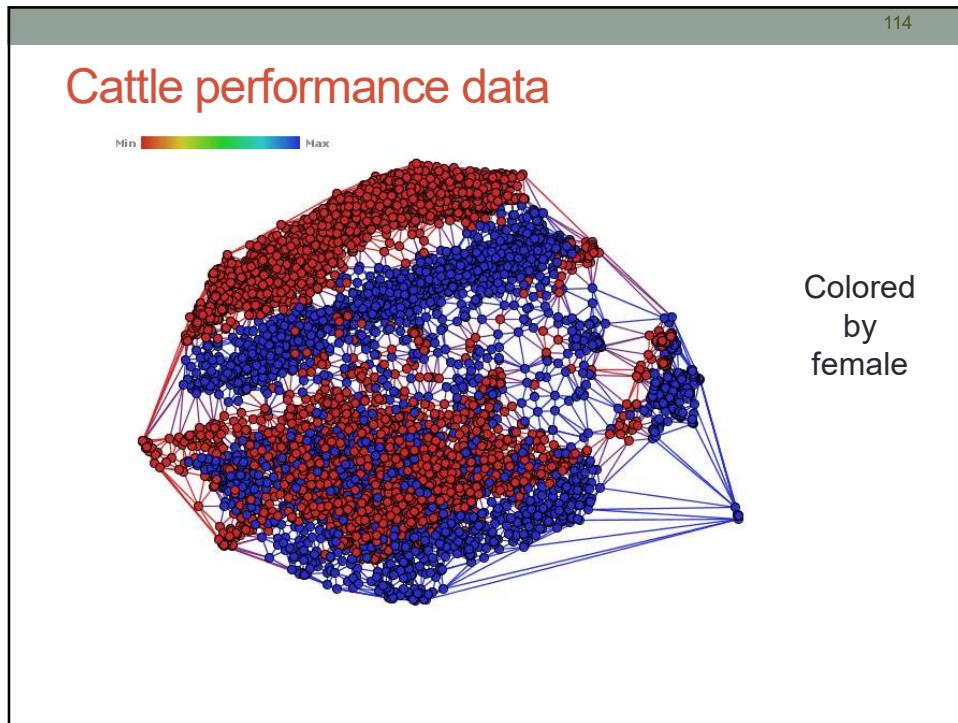
111

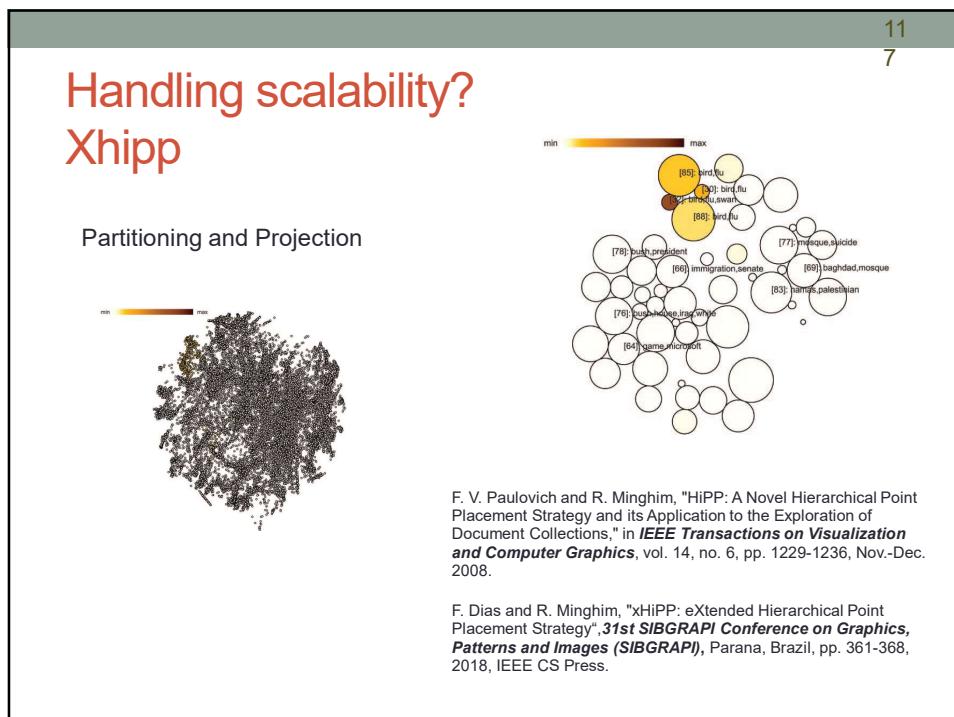
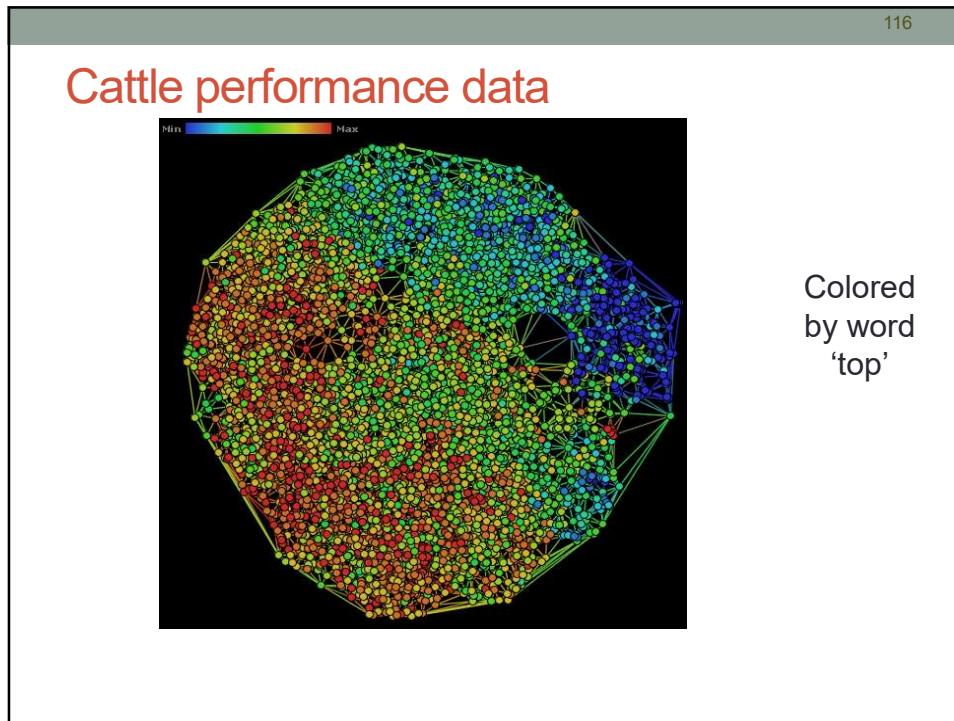
## Further Example

- Cattle performance data
  - Translated to text from categorical information, e.g.,
    - Ranges of weight to words such as:

```
{weight_below_fifty_percent;
  weight_between_fifty_seventy_five; etc..}
```
  - 9135 individuals

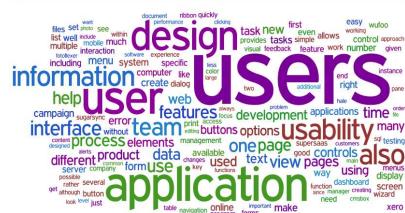






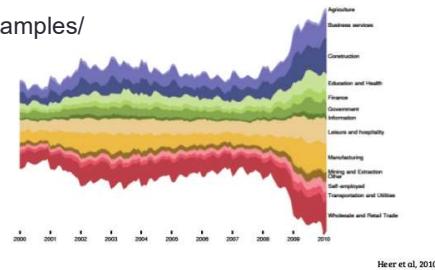
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## Tag-clouds and Theme River



Stacked graph  
aka Steam graph, Theme river

<https://www.nngroup.com/articles/tag-cloud-examples/>

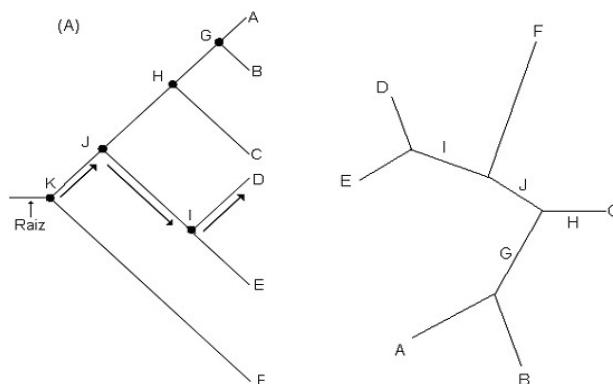


Heer et al, 2010

<http://complexdatavisualized.com/time-series-visualizations-an-overview/>

11  
9

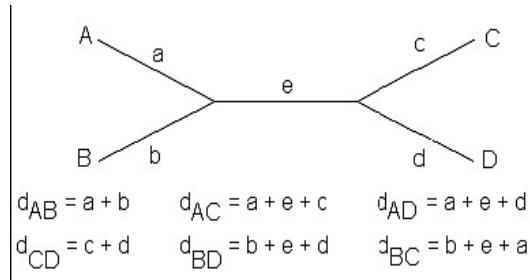
## Point Placement by Phylogenetic Tree Construction Algorithms (N-J Trees)



12  
0

## Point Placement by Phylogenetic Tree Construction Algorithms (N-J Trees)

$$d_{AB} + d_{CD} \leq \max(d_{AC} + d_{BD}, d_{AD} + d_{BC})$$

12  
1

## Algorithm Neighbor-joining

Input: distance matrix

1. Create a star tree for n objects.
2. Iteration
  1. Select a node pair (i,j) with smaller  $S_{ij}$  (branch size)

$$S_{ij} = \frac{1}{2(n-2)} \sum_{k=3}^N (D_{ik} + D_{jk}) + \frac{1}{2} D_{ij} + \frac{1}{n-2} \sum_{3 \leq m < n} D_{ij}$$

2. Combine nodes i and j in a new node and calculate the branch size of the new node.

$$L_{ix} = \frac{D_{ij} + D_{iz} - D_{jz}}{2} \quad L_{jx} = \frac{D_{ij} + D_{jz} - D_{iz}}{2}$$

12  
2

### Algorithm Neighbor-joining

3. Calculate new distance matrix, computing the new distances from the new node to the remaining nodes.

$$D_{(i-j),k} = \frac{(D_{ik} + D_{jk})}{2} \quad (3 \leq k \leq N)$$

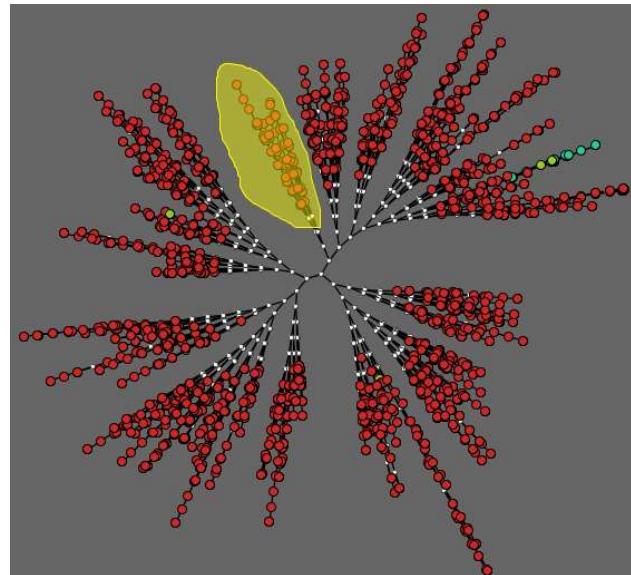
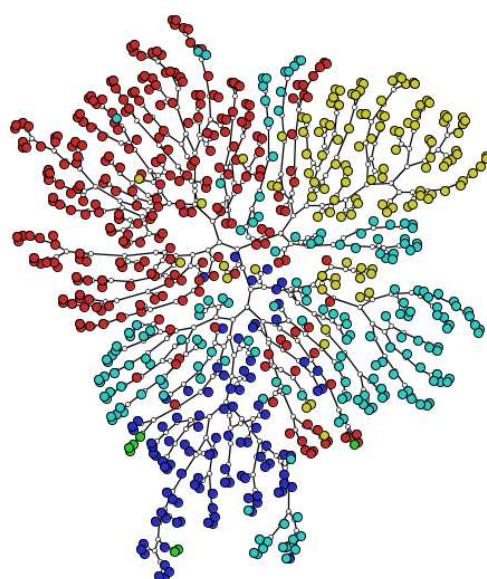
4. Eliminate previous nodes i and j
5. If n>2 then iterate again.

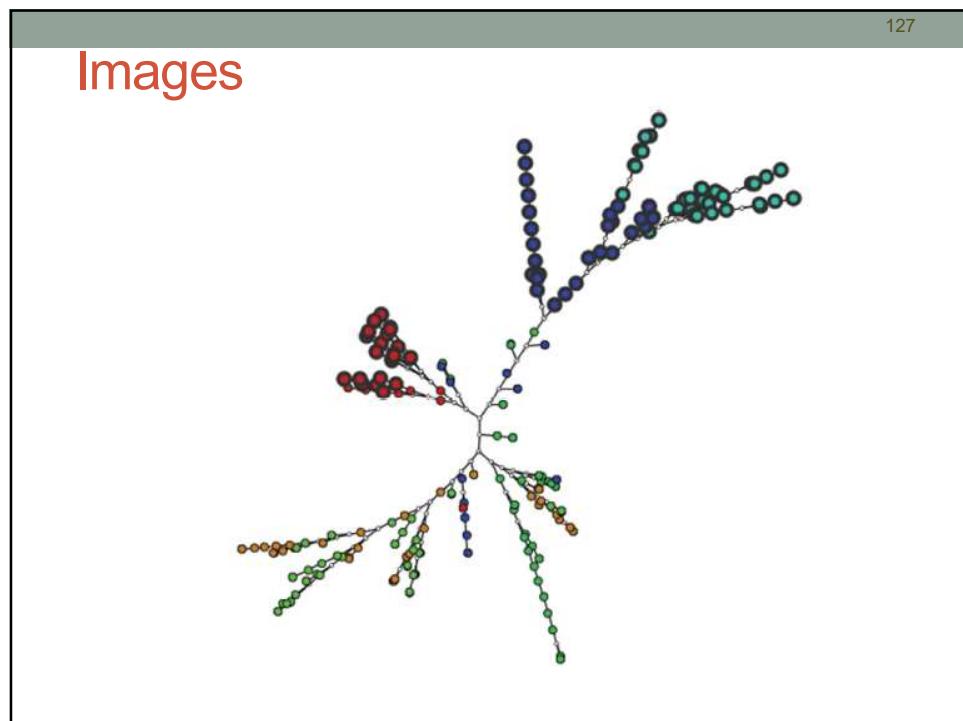
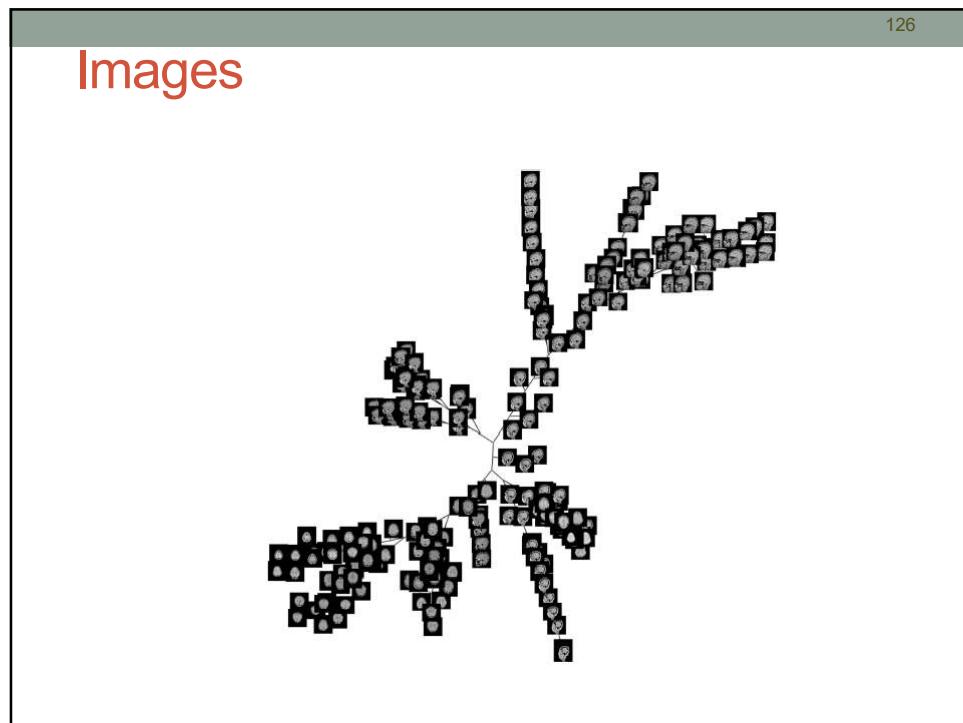
123

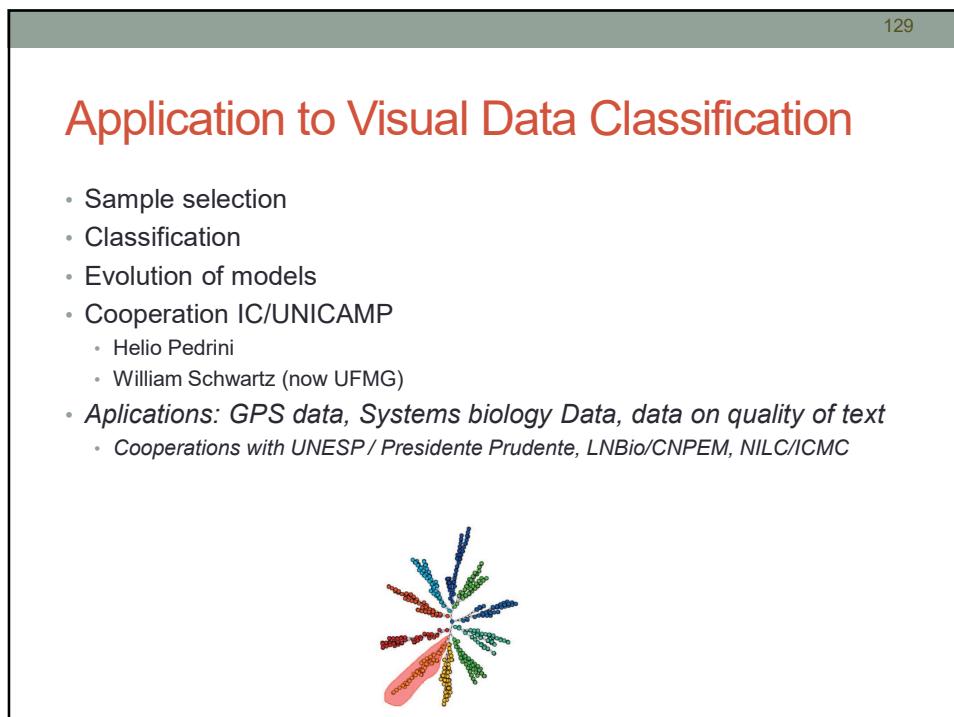
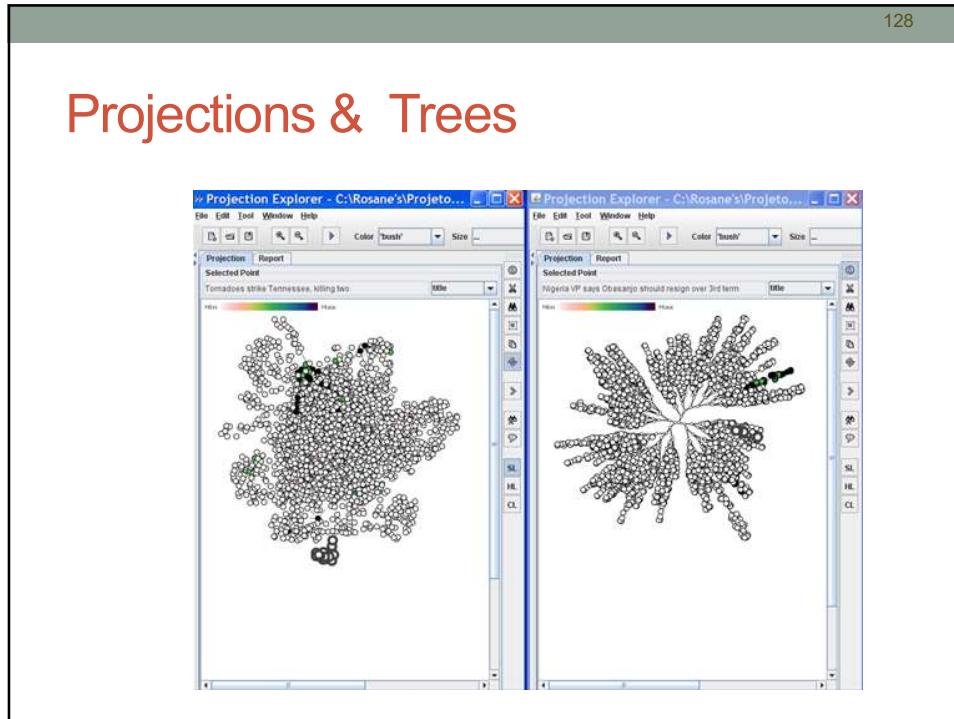
- Alternate view (N-J Tree)



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12  
5

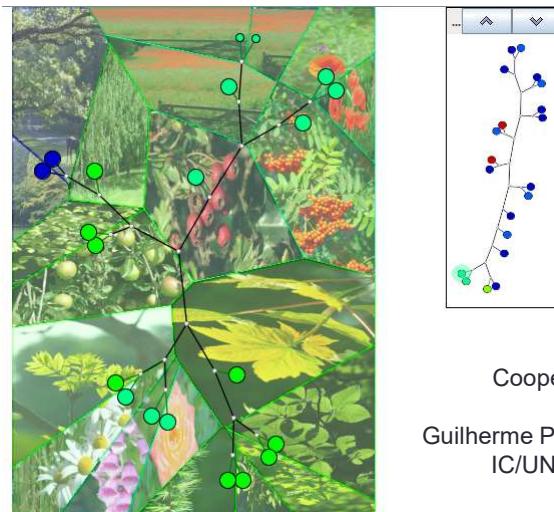




13  
0

## Scalability

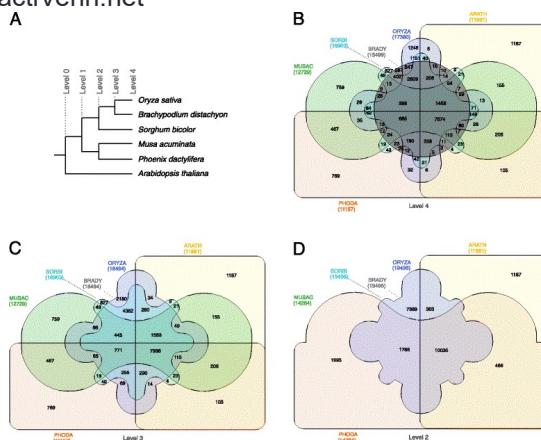
### The Visual Super Tree



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## Application: comparison of sets

- Cooperation ICMC/UNICAMP/LNBio (Campinas)/ Embrapa (Campinas)
- Fig.: Comparison of gene lists from different species
- [www.interactiVenn.net](http://www.interactiVenn.net)



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## Context: Visual Data Mining

- Definition [Ankerst 2000]
  - step in process of knowledge discovery / extraction (KDD)
  - utilizes visualization as communication channel between computer and user
  - to support identification of new and interpretable patterns

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## Homework 3

- Explore the data sets left in Moodle-USP using:
  - Visipipeline (After Sept 19th)
  - Any tool available (go fetch!!)
- For the news data set:
  - Mention 5 headlines of importance
  - Describe generally what happened regarding each one.
- Create or obtain a new text or image data set.
  - Format using .data or .dmat (and .zip, if text) for Visipipeline (see pex-manual for that)
  - Explore using both projections and trees.
  - Write and illustrate your findings in two pages.

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- Paulovich, F. V., Oliveira, M.C.F., Minghim, R. - The Projection Explorer: A Flexible Tool for Projection-based Multidimensional Visualization, IEEE Sibgrapi 2007, IEEE CS Press, Belo Horizonte, Brazil,pp. 27-34.
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- Carnielli, C.M.M; de Rossi, C.C.S; Granato, T.; Rivera, D. C; Domingues, R. R.; Pauletti, B. B.; Yokoo, S.; Heberle, H.; busso-lopes, ariane fidelis cervigne, nilva karla sawazaki-calone, iris meirelles, gabriela vaz marchi, fábio albuquerque telles, guilherme pimentel minghim, rosane ribeiro, ana carolina prado brandão, thais bianca de castro, gilberto gonzález-arriagada, wilfredo alejandro gomes, alexandre penteado, fabio santos-silva, alan roger lopes, márcio ajudarte rodrigues, priscila campioni , sundquist, elias salo, tuula da silva, sabrina daniela alaoui-jamali, moulay a. graner, edgard fox, jay w. coletta, ricardo della paes leme, adriana franco ; Combining discovery and targeted proteomics reveals a prognostic signature in oral cancer. Nature Communications, v.9, 3598, 2018.

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