



LISTA EXERCÍCIOS - DERIVADAS

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Assunto referente: Diferenciabilidade de função de uma variável

- P. 346 $y = \frac{a + \sqrt{x}}{a - \sqrt{x}}$
- P. 347 $F(r) = \sqrt{\frac{1+r}{1-r}}$
- P. 348 $y = \sqrt{\frac{1+x^2}{1-x^2}}$
- P. 349 $y = \sqrt{4 + \frac{1}{x}}$
- P. 350 $y = \sqrt{\frac{x^2 - 5}{10 - x^2}}$
- P. 351 $y = \frac{1}{t - \frac{1}{t}}$
- P. 352 $y = \sqrt{\left(\frac{1-x}{1+x}\right)^2}$
- P. 353 $y = \sqrt{1 + \sqrt{x}}$
- P. 354 $y = \frac{2t^2 - 1}{3t^3} \cdot \sqrt{t^2 + 1}$
- P. 355 $y = \frac{\sqrt{a-x} + \sqrt{a+x}}{\sqrt{a-x} - \sqrt{a+x}}$
- P. 356 $f(x) = \cotg x$
- P. 357 $f(x) = \sec x$
- P. 358 $f(x) = \operatorname{cosec} x$
- P. 359 $y = 5 \operatorname{sen} x + 3 \operatorname{cos} x$
- P. 360 $y = \operatorname{tg} x - \cotg x$
- P. 361 $y = \frac{\operatorname{sen} x + \operatorname{cos} x}{\operatorname{sen} x - \operatorname{cos} x}$
- P. 362 $y = 2t \cdot \operatorname{sen} t - (t^2 - 2) \operatorname{cos} t$
- P. 363 $y = x \cdot \cotg x$
- P. 364 $y = \frac{\operatorname{sen} x}{x}$
- P. 365 $y = 2 \cdot \operatorname{cos}^3 x$
- P. 366 $y = 5 \cdot \operatorname{tg}^4 x$
- P. 367 $y = \operatorname{sen}^3 x$
- P. 368 $y = \operatorname{sen}(x^3)$
- P. 369 $y = 2 \cdot \operatorname{sen}(x - 2)$
- P. 370 $y = \operatorname{sen} 3x$
- P. 371 $y = \operatorname{sen} x^3$
- P. 372 $y = \operatorname{cos} 2x$
- P. 373 $y = 2 \cdot \operatorname{cos}(2x - 1)$
- P. 374 $y = \sqrt{\operatorname{sen} x}$
- P. 375 $y = \operatorname{sen} \sqrt{x}$
- P. 376 $y = 3 \cdot \operatorname{tg} 2x$
- P. 377 $y = \operatorname{tg}(2x^2 - x + 3)$
- P. 378 $y = \operatorname{sen}^4 2x$
- P. 379 $y = \operatorname{cos}^3 2x$
- P. 380 $y = \operatorname{sen}(\operatorname{cos} x)$
- P. 381 $y = \operatorname{tg}(\operatorname{sen} x)$
- P. 382 $y = \frac{\operatorname{sen} 2x}{1 + \operatorname{cos} 2x}$
- P. 383 $y = a^{3x}$
- P. 384 $y = e^{2x}$
- P. 385 $y = e^x - e^{-x}$
- P. 386 $y = 2^{\operatorname{tg} x}$



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P.387 $y = 3^{\text{sen } x + \cos x}$

P.388 $y = x^2 \cdot e^{ax}$

P.389 $y = x^n \cdot a^x$

P.390 $y = \log_e \sqrt{1 - x^2}$

P.391 $y = \log_e (x^2 + a)$

P.392 $y = \log_e (ax + b)$

P.393 $y = x \log_e x$

P.394 $y = \log_e \frac{a+x}{a-x}$

P.395 $y = \log_e (x + \sqrt{1+x^2})$

P.396 $P(y) = \log_e \sqrt{\frac{1+y}{1-y}}$

P.397 $y = \log_e \frac{\sqrt{x^2+1} - x}{\sqrt{x^2+1} + x}$

P.398 $y = \log_e (\log_e x)$

P.399 $y = x^7 \cdot \log_e x$

P.400 $y = (x-1) \cdot \log_e x$

P.401 $y = \frac{\log_e x}{x^2}$

P.402 $y = \frac{1}{x} + 2 \log_e x - \frac{\log_e x}{x}$

P.403 $y = x^3 \log_e x - \frac{x^3}{3}$

P.404 $y = \frac{\log_a x^2}{\log_a e} - \log_e x$

P.405 $f(t) = \log_e \cos t$

P.406 $y = \log_e \text{tg } x$

P.407 $y = \log_e \text{tg} \left(\frac{\pi}{4} + \frac{x}{2} \right)$

P.408 $y = \log_e \frac{1 + \text{tg} \frac{x}{2}}{1 - \text{tg} \frac{x}{2}}$

P.409 $y = (\log_e x) \cdot \cos x$

P.410 $y = \frac{\log_e x}{e^x}$

P.411 $y = \text{arc sen} \frac{x}{a}$

P.412 $y = \text{arc tg} \frac{2x}{1-x^2}$

P.413 $y = \text{arc tg } x + \text{arc cotg } x$

P.414 $y = x \cdot \text{arc sen } x$

P.415 $y = \frac{(1+x^2) \text{arc tg } x - x}{2}$

P.416 $y = \text{arc tg} \frac{x+a}{1-ax}$

P.417 $y = \text{arc cos} \sqrt{\frac{1+\cos x}{2}}$

P.418 $y = x\sqrt{a^2-x^2} + a^2 \text{arc sen} \frac{x}{a}$

P.419 $y = x^x$

P.420 $y = x \cdot e^x$

P.421 $y = x^{x^x}$

P.422 $y = x^{\text{tg } x}$

P.423 $y = \frac{1}{e^x + e^{-x}}$

P.424 $y = \frac{e^{ax}(a \cdot \cos bx + b \cdot \text{sen } bx)}{a^2 + b^2}$



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RESPOSTAS

$$P.346 \ y' = \frac{a}{\sqrt{x}(a - \sqrt{x})^2}$$

$$P.347 \ F'(r) = \frac{1}{(1-r)\sqrt{1-r^2}}$$

$$P.348 \ y' = \frac{2x}{(1-x^2)\sqrt{1-x^4}}$$

$$P.349 \ y' = -\frac{1}{2\sqrt{x^3}(4x+1)}$$

$$P.350 \ y' = \frac{5x}{\sqrt{(10-x^2)^3(x^2-5)}}$$

$$P.351 \ y' = -\frac{t^2+1}{(t^2-1)^2}$$

$$P.352 \ \begin{cases} y' = \frac{-2}{(1+x)^2} \text{ para } -1 < x < 1 \\ y' = \frac{2}{(1+x)^2} \text{ para } x < -1 \text{ ou } x > 1 \end{cases}$$

$$P.353 \ y' = \frac{1}{4\sqrt{x+x\sqrt{x}}}$$

$$P.354 \ y' = \frac{1}{t^4\sqrt{t^2+1}}$$

$$P.355 \ y' = \frac{1}{\sqrt{a^2-x^2} \cdot (a^2-\sqrt{a^2-x^2})}$$

$$P.356 \ f'(x) = -\operatorname{cosec}^2 x$$

$$P.357 \ f'(x) = \sec x \cdot \operatorname{tg} x$$

$$P.358 \ f'(x) = -\operatorname{cosec} x \operatorname{cotg} x$$

$$P.359 \ y' = 5 \cdot \cos x - 3 \cdot \operatorname{sen} x$$

$$P.360 \ y' = \sec^2 x + \operatorname{cosec}^2 x$$

$$P.361 \ y' = \frac{-2}{(\operatorname{sen} x - \cos x)^2}$$

$$P.362 \ y' = t^2 \cdot \operatorname{sen} t$$

$$P.363 \ y' = \operatorname{cotg} x - x \cdot \operatorname{cosec}^2 x$$

$$P.364 \ y' = \frac{x \cdot \cos x - \operatorname{sen} x}{x^2}$$

$$P.365 \ y' = -6 \cdot \cos^2 x \cdot \operatorname{sen} x$$

$$P.366 \ y' = 20 \cdot \operatorname{tg}^3 x \cdot \sec^2 x$$

$$P.367 \ y' = 3 \cdot \operatorname{sen}^2 x \cdot \cos x$$

$$P.368 \ y' = 3 \cdot x^2 \cdot \cos(x^3)$$

$$P.369 \ y' = 2 \cdot \cos(x-2)$$

$$P.370 \ y' = 3 \cdot \cos 3x$$

$$P.387 \ y' = 3^{\operatorname{sen} x + \cos x} \cdot (\cos x - \operatorname{sen} x) \cdot \log_e 3$$

$$P.388 \ y' = x \cdot e^{ax} \cdot (ax + 2)$$

$$P.389 \ y' = a^x \cdot x^{n-1} \cdot (x \cdot \log_e a + n)$$

$$P.371 \ y' = 3x^2 \cdot \cos x^3$$

$$P.372 \ y' = -2 \cdot \operatorname{sen} 2x$$

$$P.373 \ y' = -4 \cdot \operatorname{sen}(2x-1)$$

$$P.374 \ y' = \frac{\cos x}{2\sqrt{\operatorname{sen} x}}$$

$$P.375 \ y' = \frac{\cos \sqrt{x}}{2\sqrt{x}}$$

$$P.376 \ y' = 6 \cdot \sec^2 2x$$

$$P.377 \ y' = (4x-1) \cdot \sec^2(2x^2-x+3)$$

$$P.378 \ y' = 8 \cdot \operatorname{sen}^3 2x \cdot \cos 2x$$

$$P.379 \ y' = -6 \cdot \cos^2 2x \cdot \operatorname{sen} 2x$$

$$P.380 \ y' = -\operatorname{sen} x \cdot \cos(\cos x)$$

$$P.381 \ y' = \cos x \cdot \sec^2(\operatorname{sen} x)$$

$$P.382 \ y' = \sec^2 x$$

$$P.383 \ y' = 3 \cdot a^{3x} \cdot \log_e a$$

$$P.384 \ y' = 2 \cdot e^{2x}$$

$$P.385 \ y' = e^x + e^{-x}$$

$$P.386 \ y' = 2^{\operatorname{tg} x} \cdot \sec^2 x \cdot \log_e 2$$



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RESPOSTAS

$$P.390 \ y' = \frac{x}{x^2 - 1}$$

$$P.391 \ y' = \frac{2x}{x^2 + a}$$

$$P.392 \ y' = \frac{a}{ax + b}$$

$$P.393 \ y' = 1 + \log_e x$$

$$P.394 \ y' = \frac{2a}{a^2 - x^2}$$

$$P.395 \ y' = \frac{1}{\sqrt{1 + x^2}}$$

$$P.396 \ P'(y) = \frac{1}{1 - y^2}$$

$$P.397 \ y' = \frac{-2}{\sqrt{x^2 + 1}}$$

$$P.398 \ y' = \frac{1}{x \cdot \log_e x}$$

$$P.399 \ y' = x^6(7 \cdot \log_e x + 1)$$

$$P.400 \ y' = 1 - \frac{1}{x} + \log_e x$$

$$P.401 \ y' = \frac{1 - 2 \cdot \log_e x}{x^3}$$

$$P.402 \ y' = -\frac{1}{x^2} + \frac{2}{x} - \frac{1 - \log_e x}{x^2}$$

$$P.403 \ y' = 3x^2 \cdot \log_e x$$

$$P.404 \ y' = \frac{1}{x}$$

$$P.422 \ y' = x^{\operatorname{tg} x} \left(\sec^2 x \cdot \log_e x + \frac{\operatorname{tg} x}{x} \right)$$

$$P.405 \ f'(t) = -\operatorname{tg} t$$

$$P.406 \ y' = \sec x \cdot \operatorname{cosec} x$$

$$P.407 \ y' = \sec x$$

$$P.408 \ y' = \sec x$$

$$P.409 \ y' = \frac{\cos x}{x} - (\log_e x) \cdot \sin x$$

$$P.410 \ y' = \frac{1 - x \cdot \log_e x}{x \cdot e^x}$$

$$P.411 \ y' = \frac{1}{\sqrt{a^2 - x^2}}$$

$$P.412 \ y' = \frac{2}{1 + x^2}$$

$$P.413 \ y' = 0$$

$$P.414 \ y' = \operatorname{arc} \operatorname{sen} x + \frac{x}{\sqrt{1 - x^2}}$$

$$P.415 \ y' = x \cdot \operatorname{arc} \operatorname{tg} x$$

$$P.416 \ y' = \frac{1}{1 + x^2}$$

$$P.417 \ y' = \frac{1}{2}$$

$$P.418 \ y' = 2 \sqrt{a^2 - x^2}$$

$$P.419 \ y' = x^x \cdot (1 + \log_e x)$$

$$P.420 \ y' = e^x \cdot (1 + x)$$

$$P.421 \ y' = x^{x^x} \cdot x^x \cdot (\log_e x + \log_e^2 x + \frac{1}{x})$$

$$P.423 \ y' = \frac{e^{-x} - e^x}{(e^x + e^{-x})^2}$$

$$P.424 \ y' = e^{ax} \cdot \cos bx$$