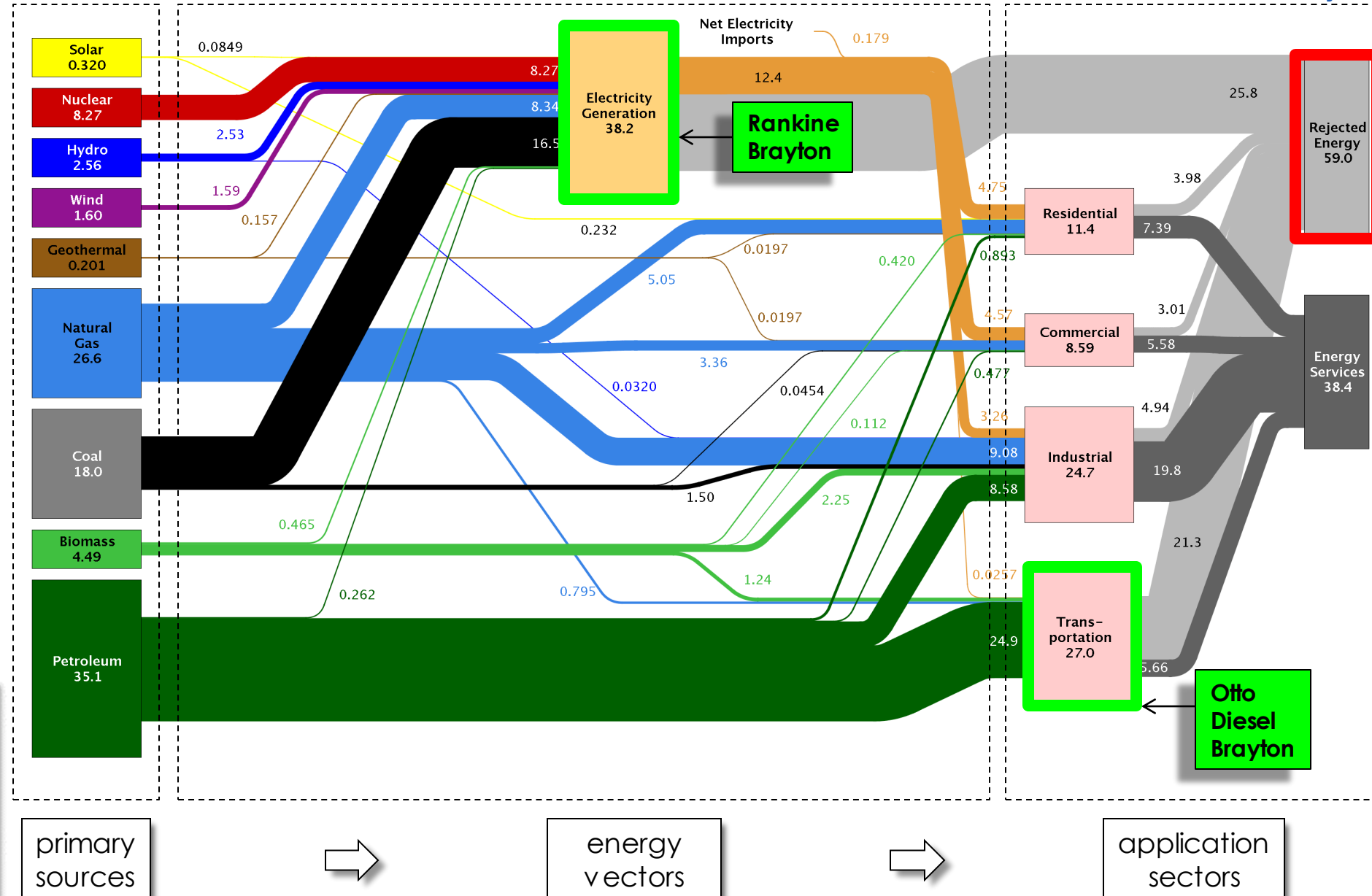
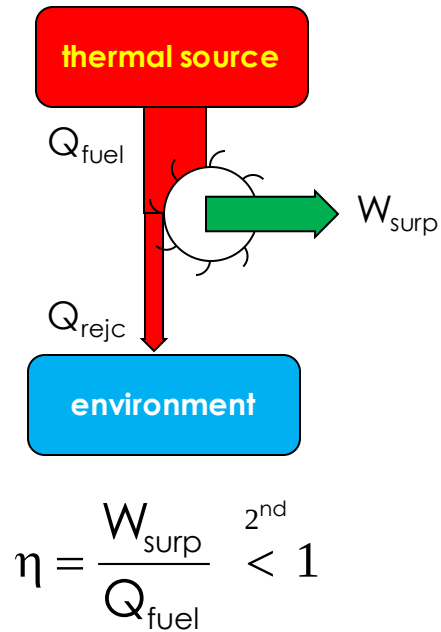


EXERGY ANALYSIS: integrating the 1st and 2nd laws of thermodynamics

Prof. Paulo Seleglim Jr.
Universidade de São Paulo



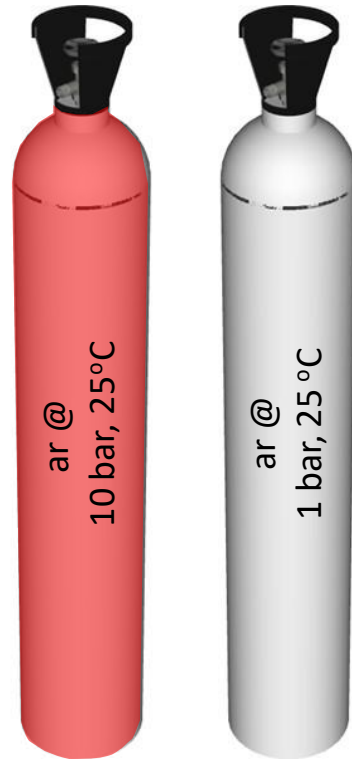
Estimated U.S. Energy Use in 2013: ~97.4 Quads



Sankey Diagram

How to maximize the conversion efficiency of an energy vector to useful energy ? (electricity, kinetic energy, etc.)



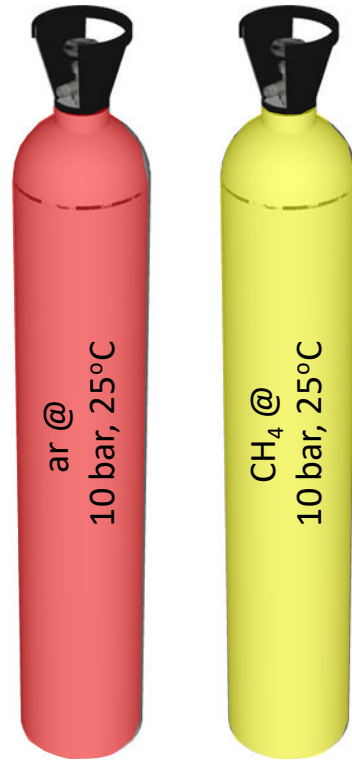


From which of these two systems is it possible to “generate” the greatest amount of mechanical work ?



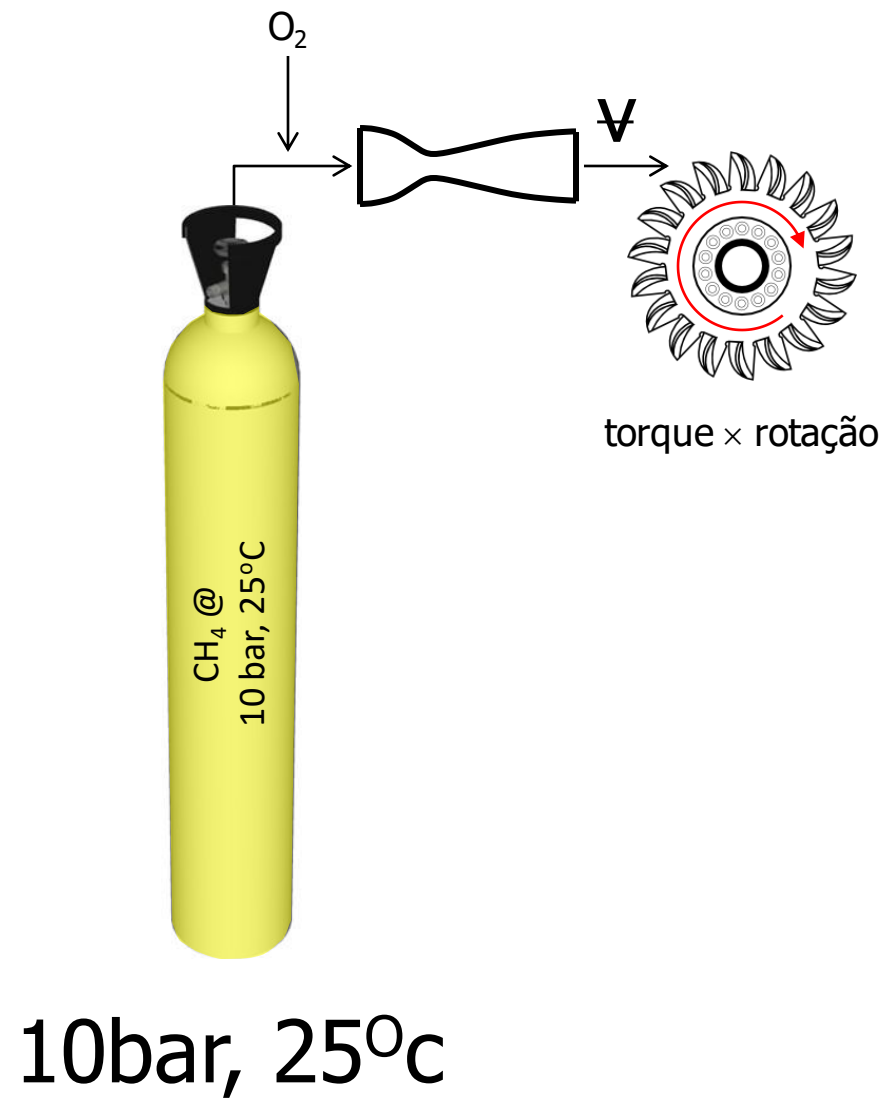


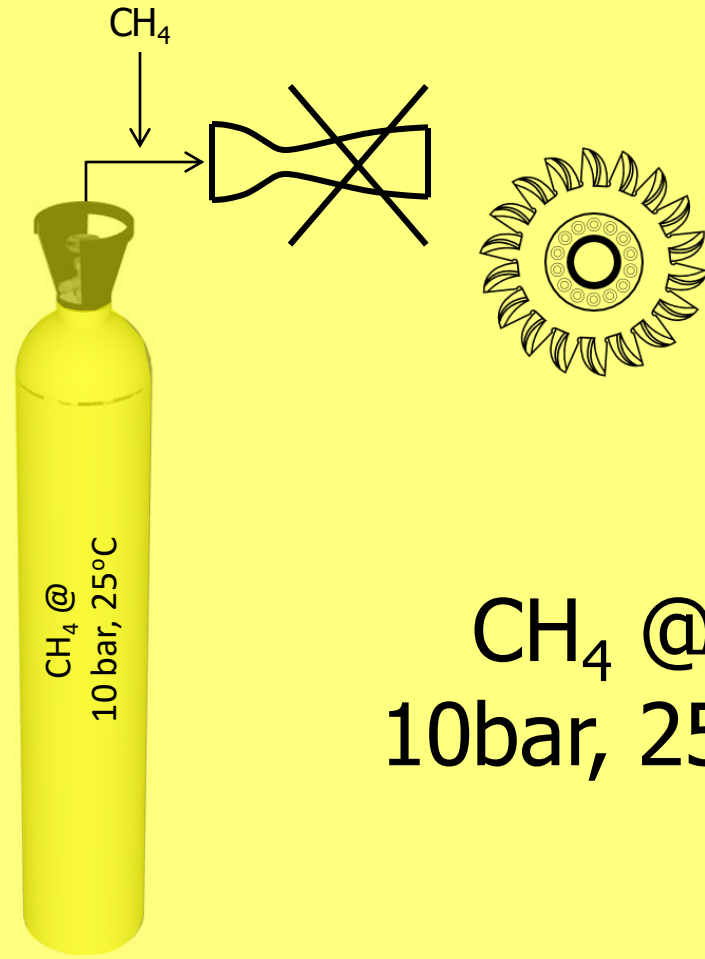
ar @
10bar, 25°C



10bar, 25°C

From which of these
two systems is it
possible to
“generate” the
greatest amount of
mechanical work ?





CH_4 @
10bar, 25°C

10bar, 25°C

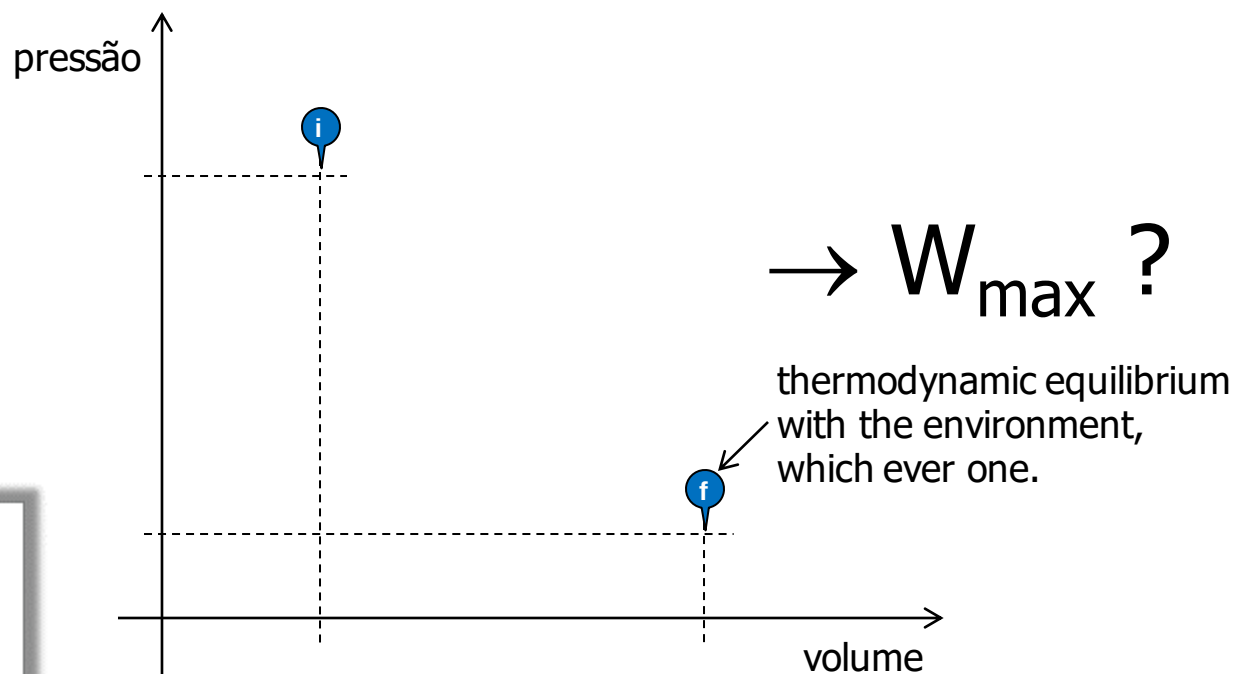
CONCLUSION:

the capacity to generate work is a **COMBINED** property of the thermodynamic state of the system (P and T) and the environment !



Nicolas Léonard Sadi Carnot
em 1824, aos vinte anos de idade

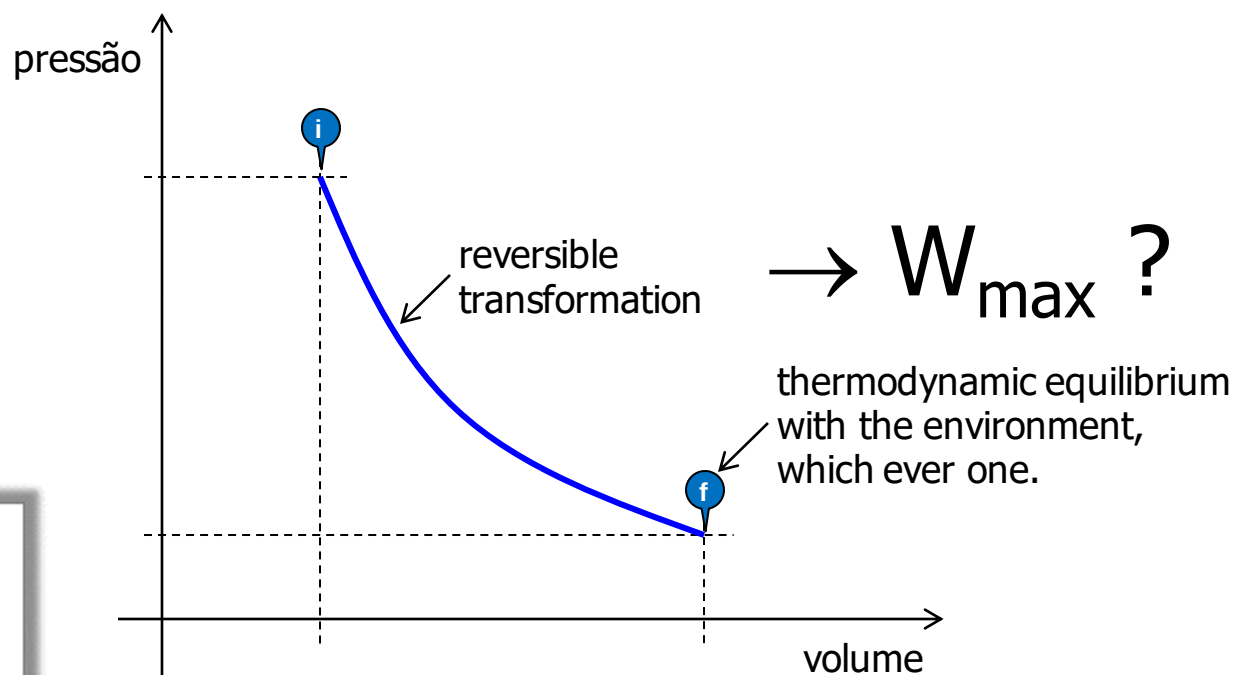
The maximum amount of work (mechanical energy) that one can obtain from a system is obtained by bringing it to equilibrium with the environment through a reversible transformation...





Nicolas Léonard Sadi Carnot
em 1824, aos vinte anos de idade

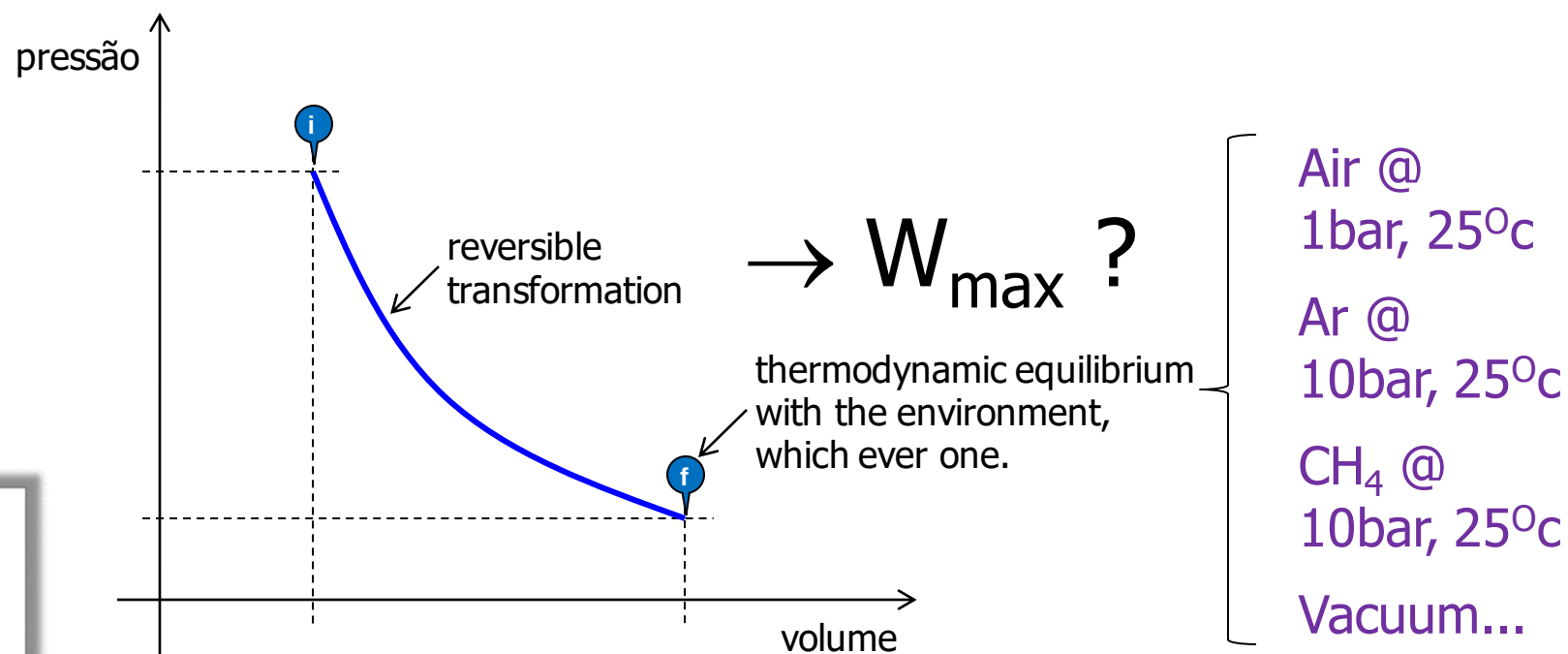
The maximum amount of work (mechanical energy) that one can obtain from a system is obtained by bringing it to equilibrium with the environment through a reversible transformation...





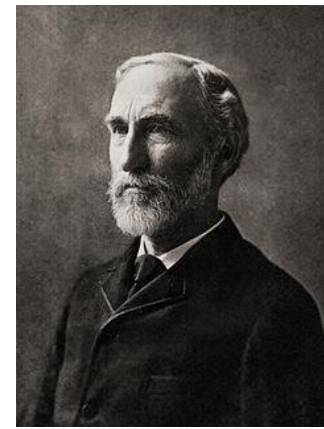
Nicolas Léonard Sadi Carnot
em 1824, aos vinte anos de idade

The maximum amount of work (mechanical energy) that one can obtain from a system is obtained by bringing it to equilibrium with the environment through a reversible transformation...



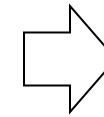
DEFINITIONS

“Useful work potential”: is the maximum amount of mechanical energy that one can obtain from a system, the difference being inevitably lost to the environment due to the implications of the 2nd law.



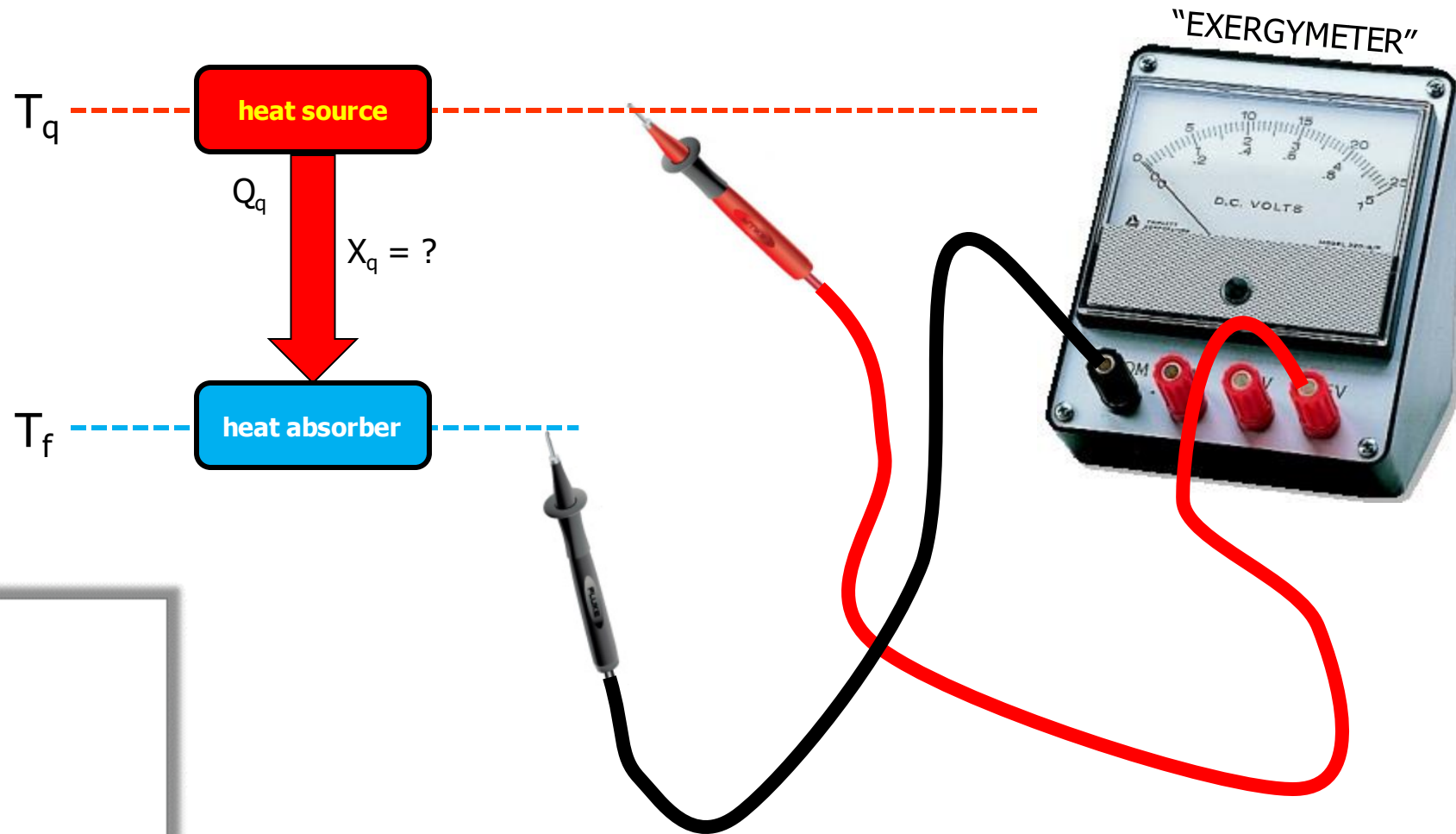
J. Willard Gibbs

EXERGY

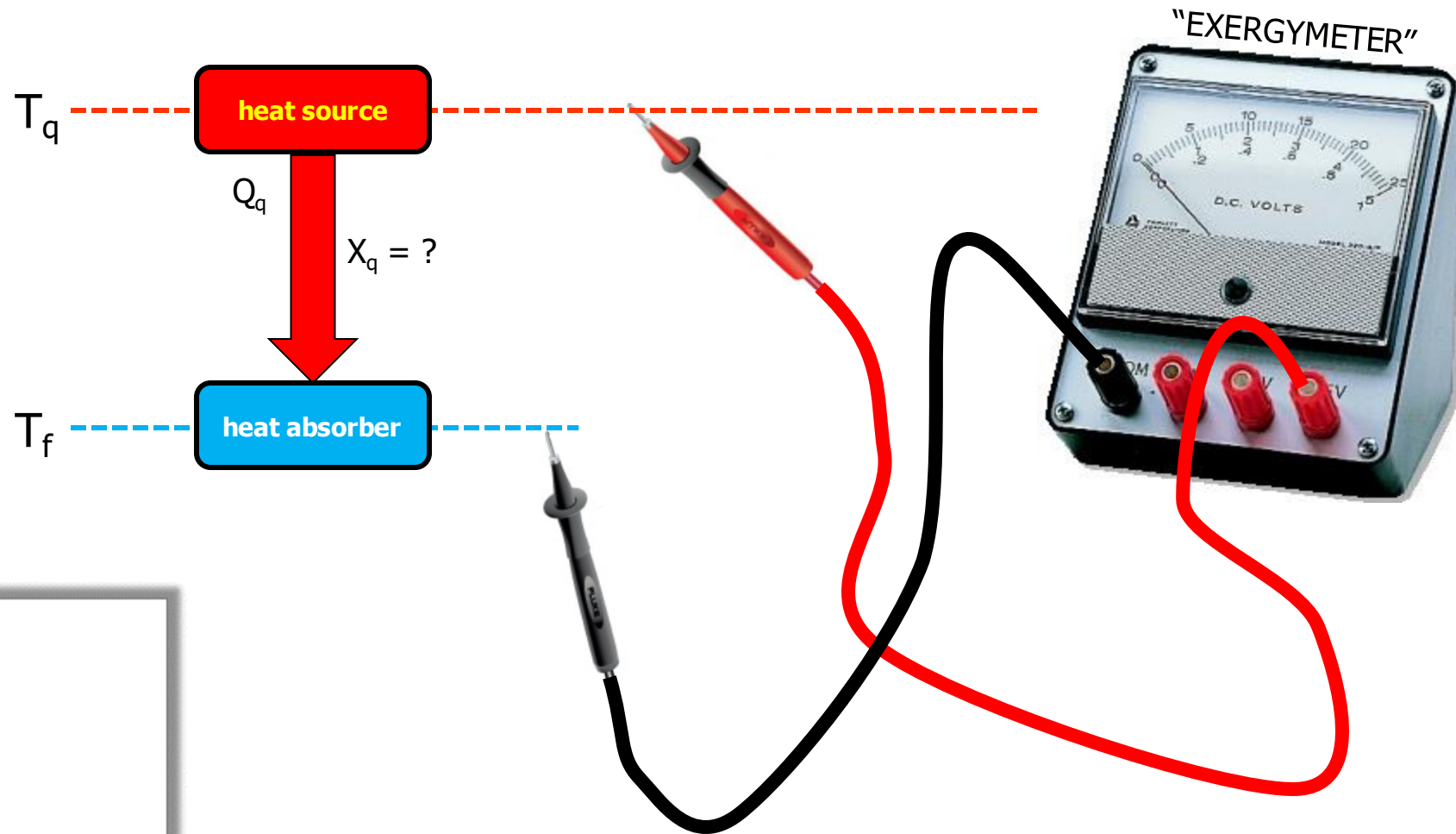


Available energy
Exergetic energy
Availability
Reversible work
Etc.

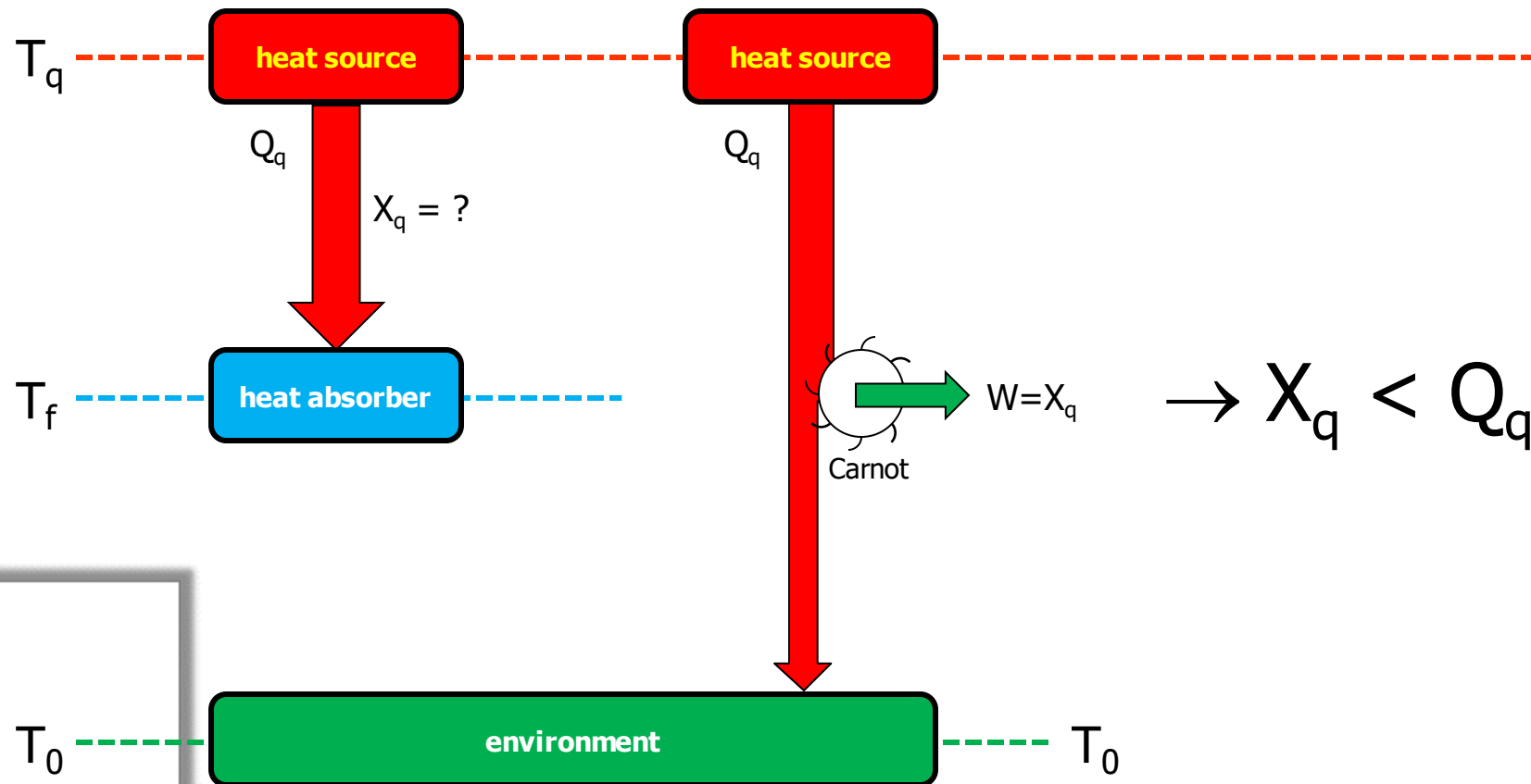
Exergy associated with the heat supplied by a thermal source...



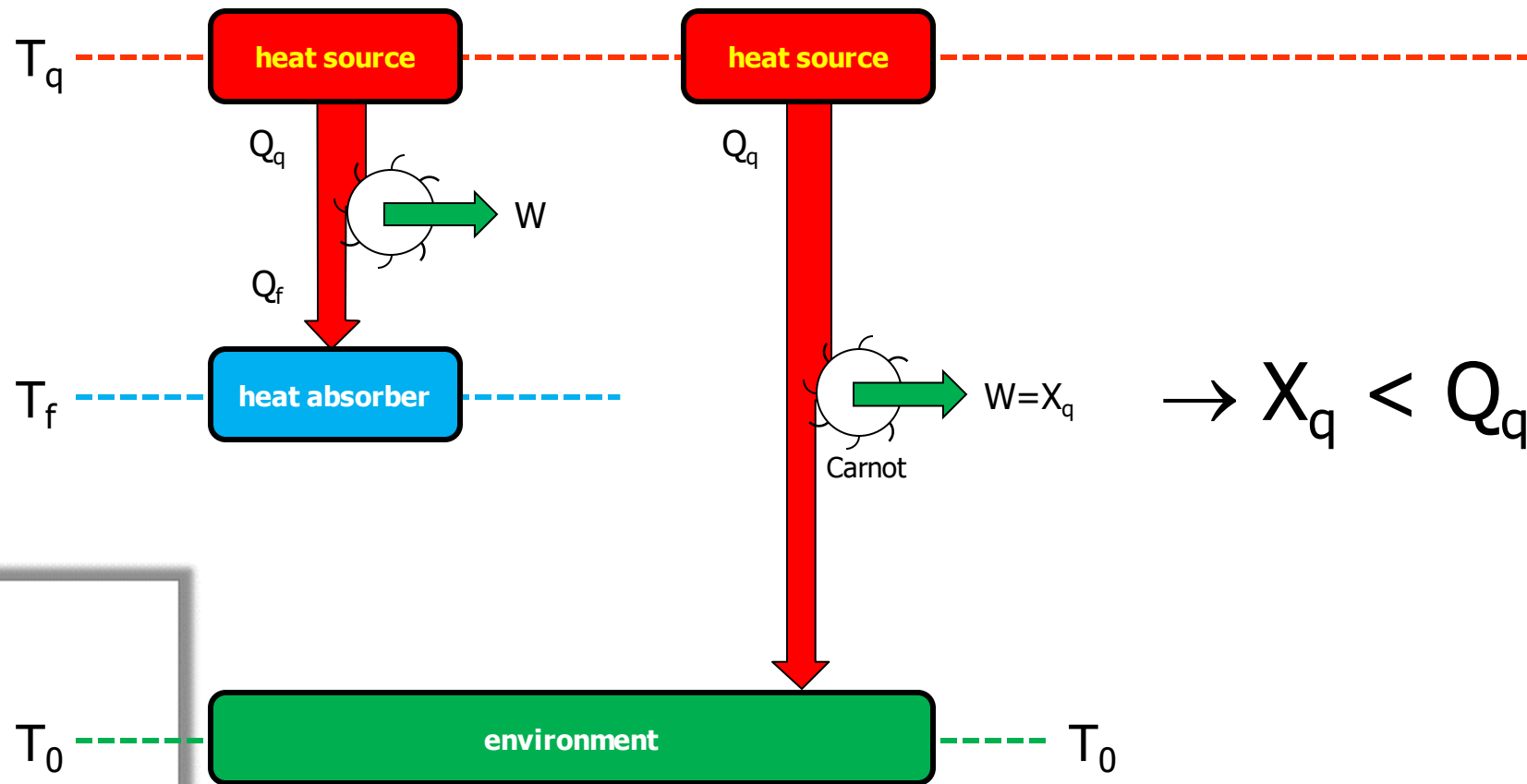
Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



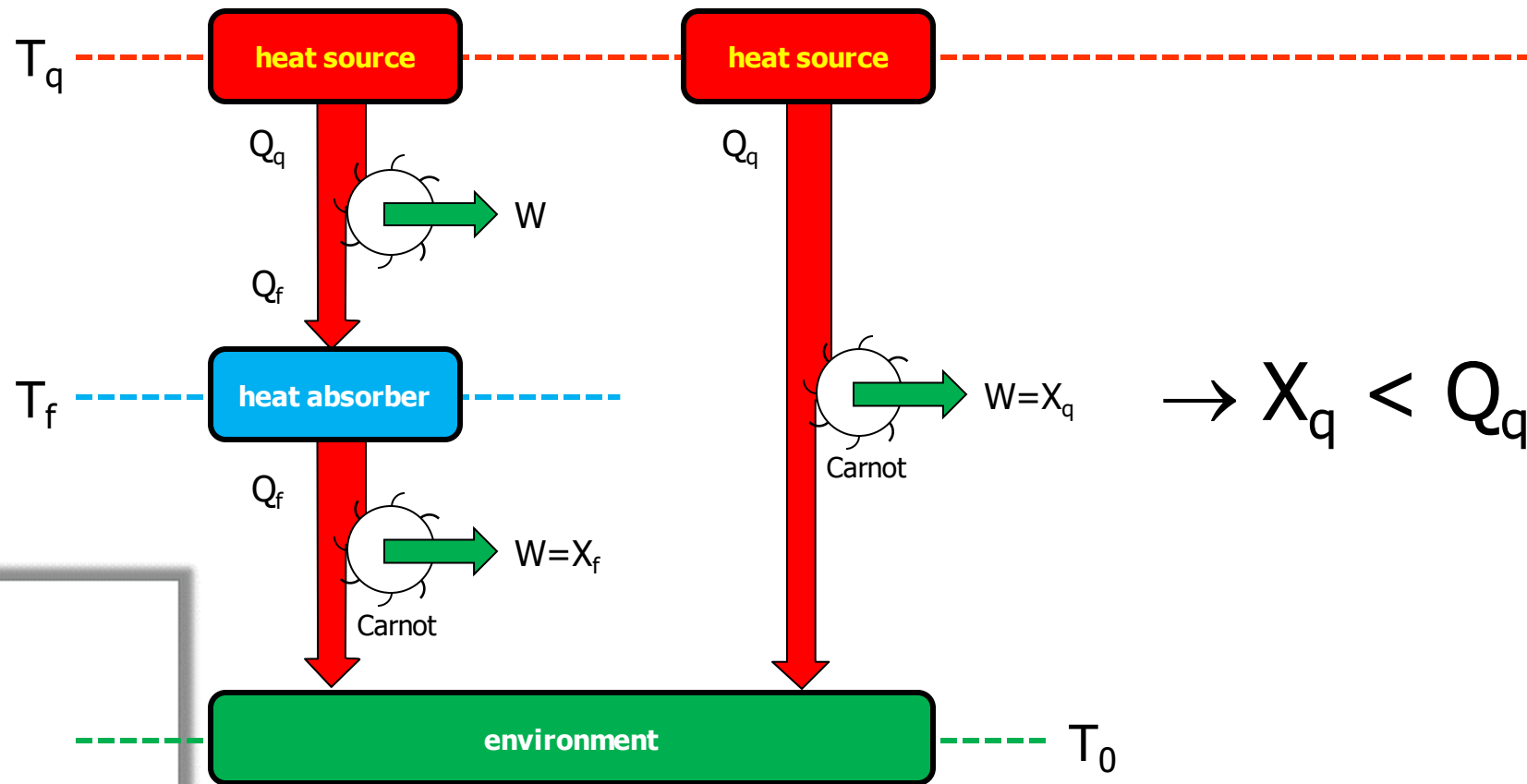
Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



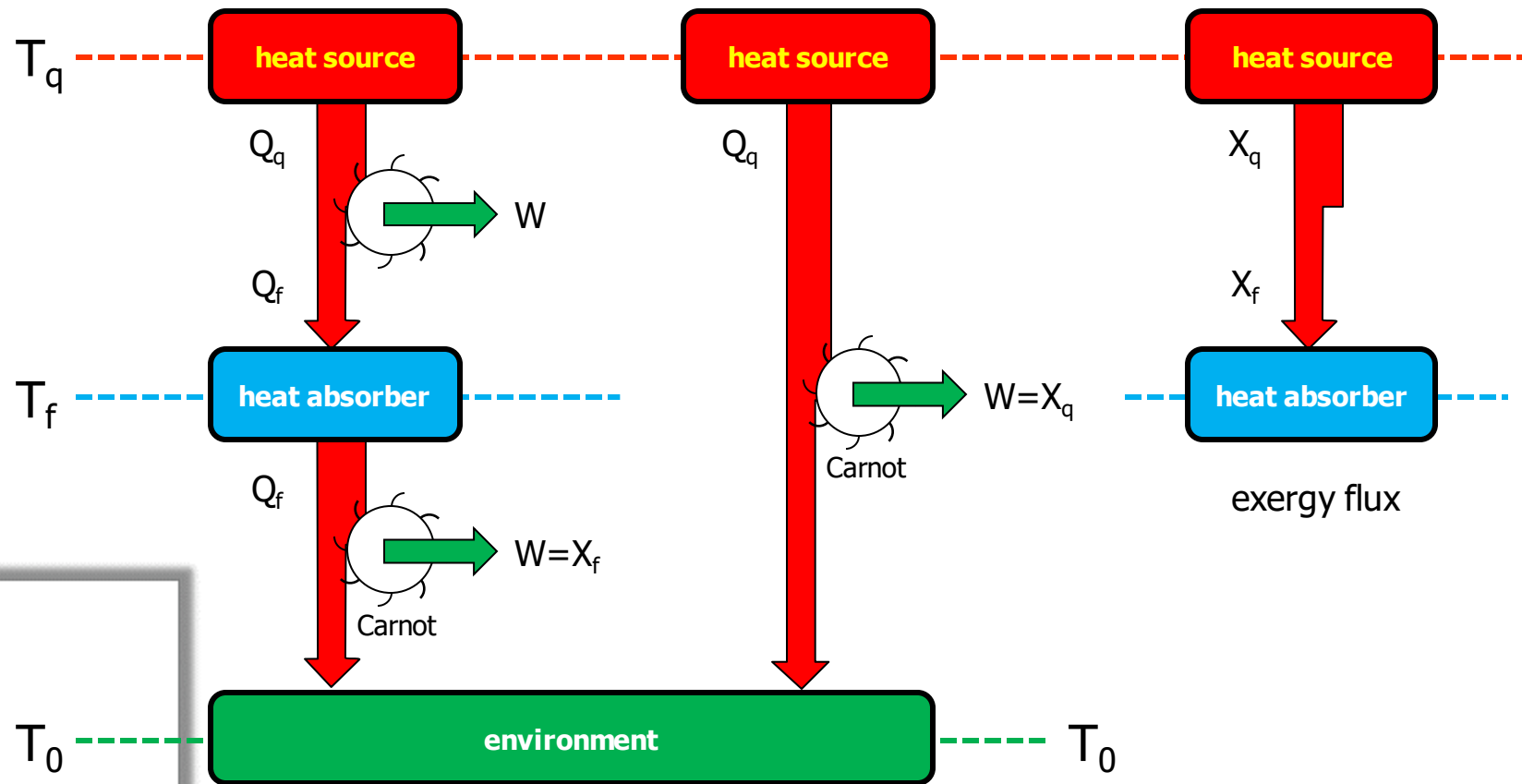
Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



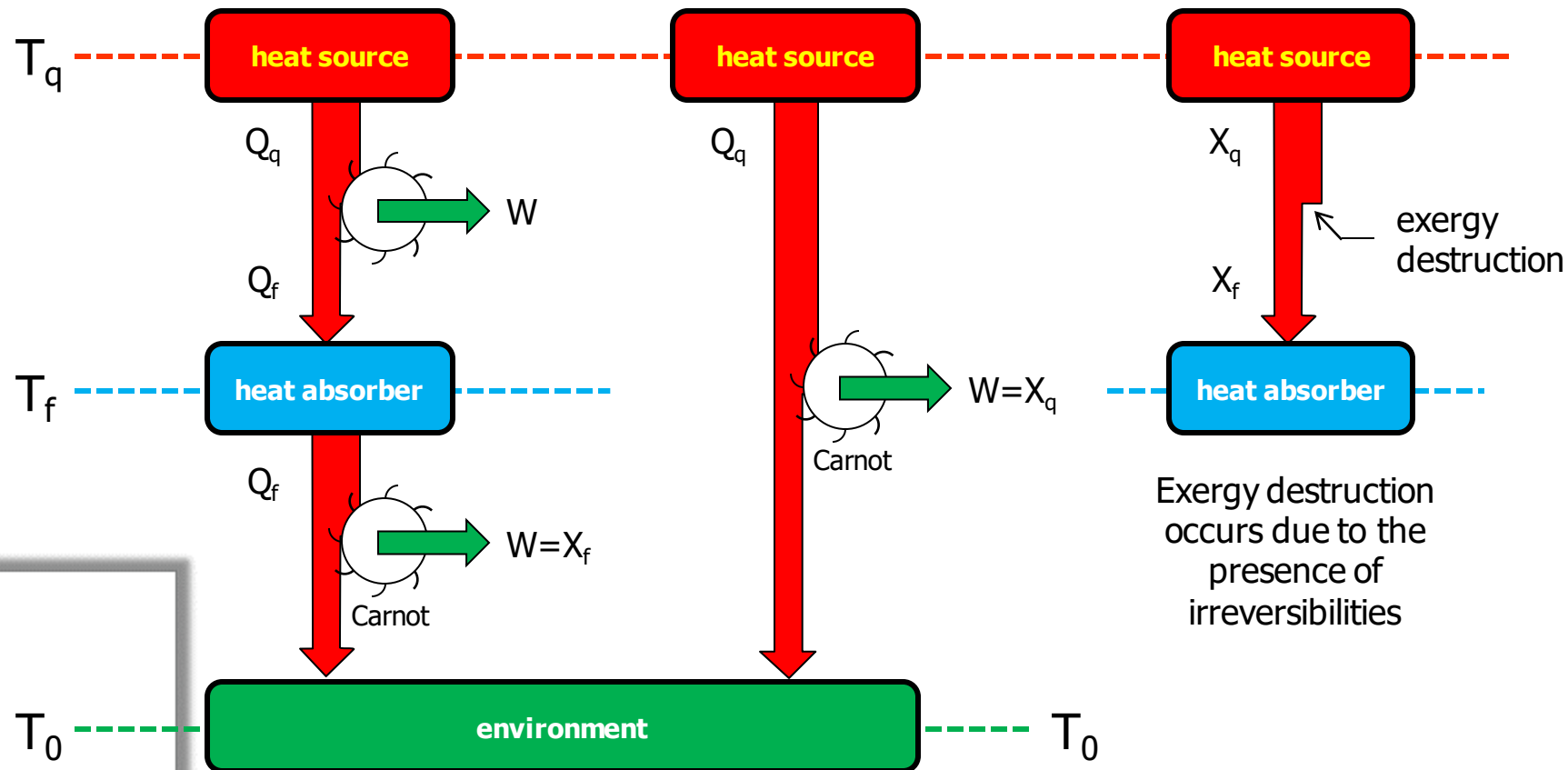
Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



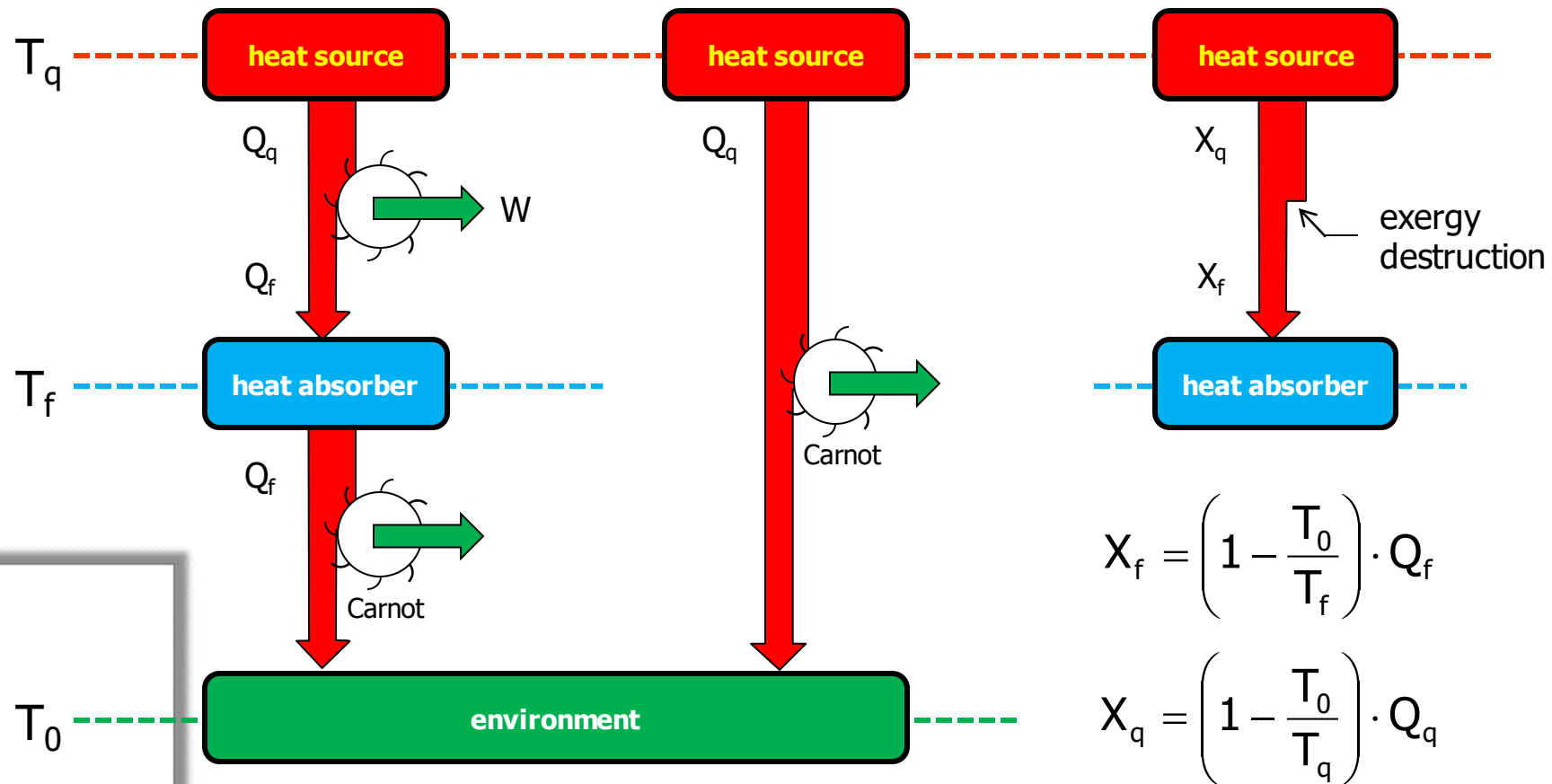
Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



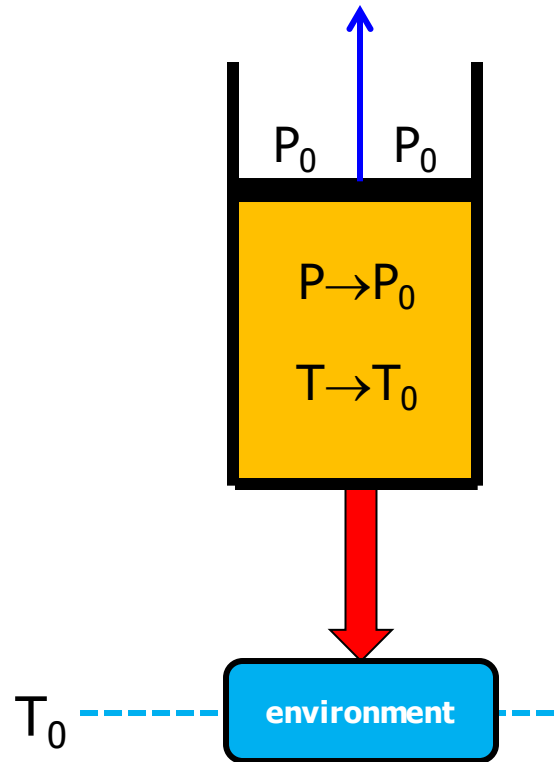
Exergy associated with the heat supplied by a thermal source...
is equal to the work produced by a reversible cycle operating
between the thermal reservoirs and the environment



Closed system analysis

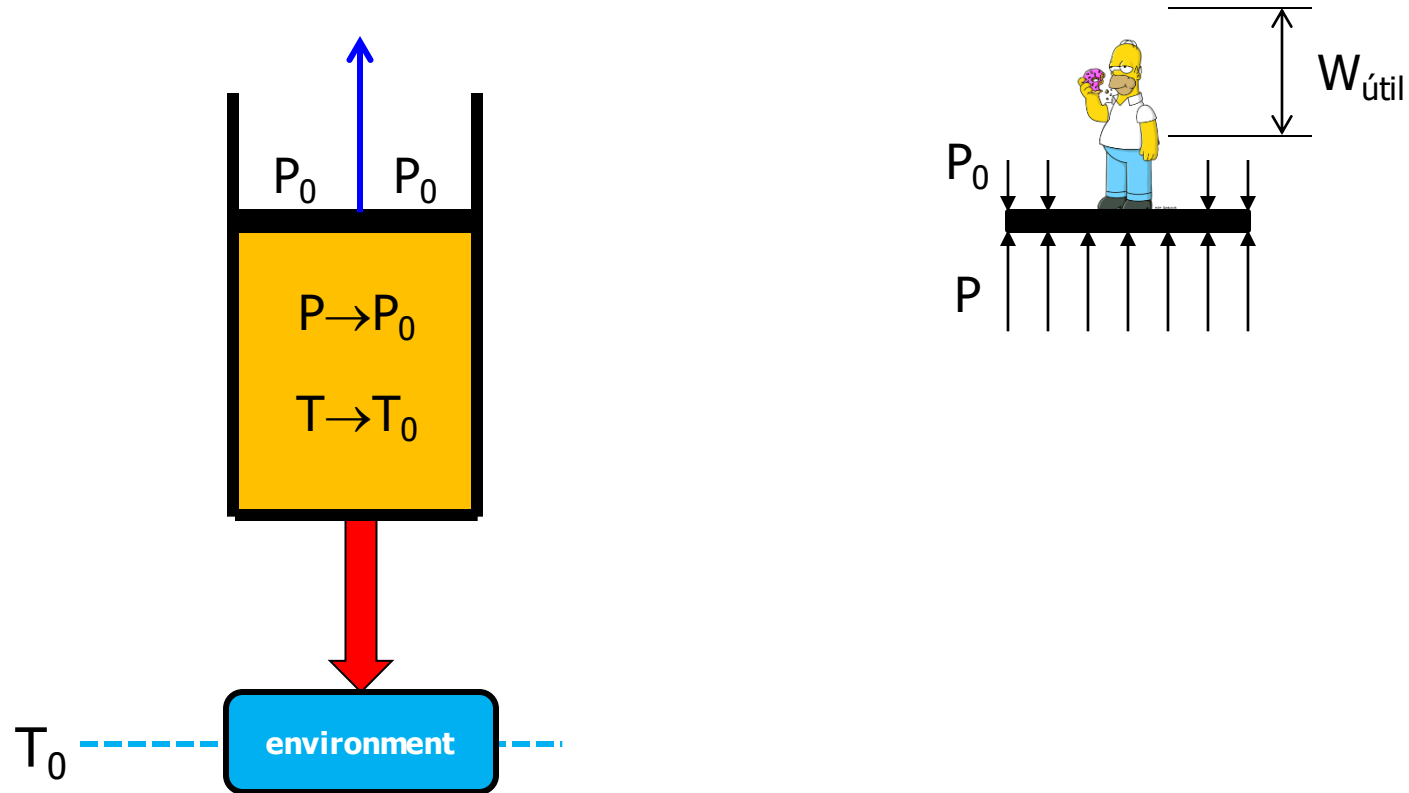


Variation of the amount of exergy in a closed system

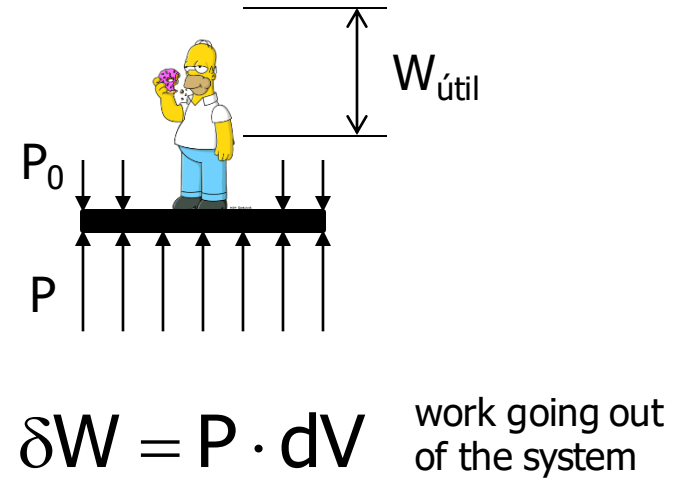
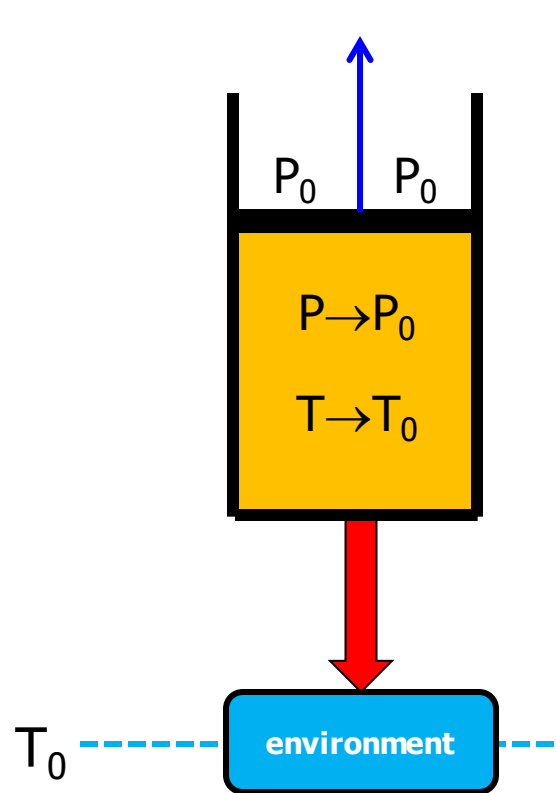


Expansion of the system with exportation of mechanical work until it reaches the equilibrium with the environment...

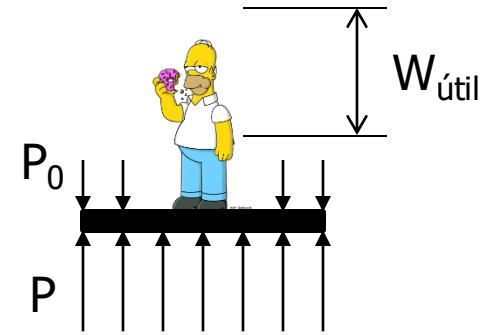
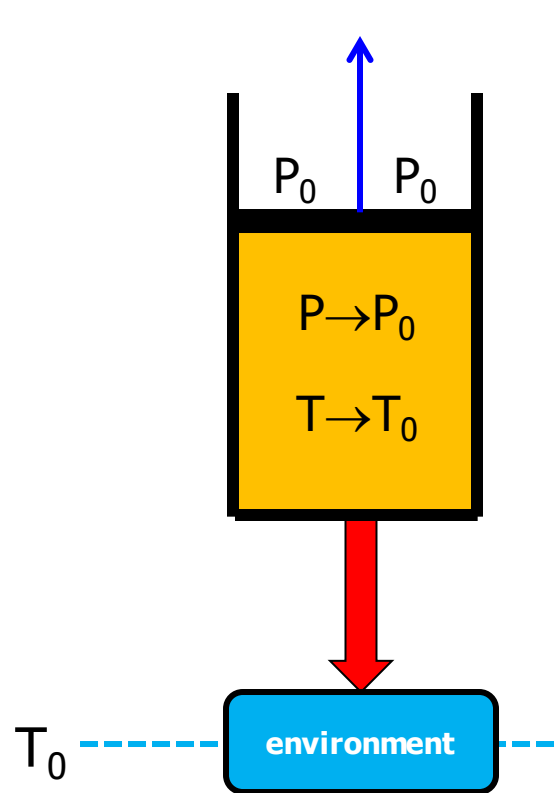
Variation of the amount of exergy in a closed system



Variation of the amount of exergy in a closed system



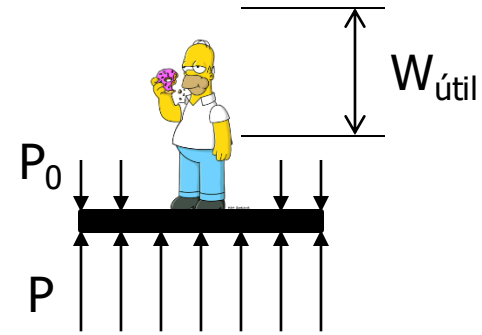
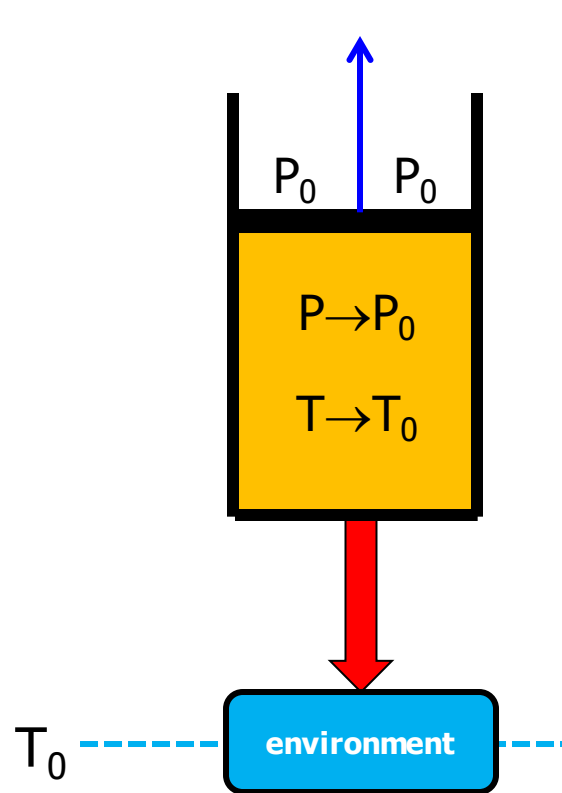
Variation of the amount of exergy in a closed system



$$\delta W = P \cdot dV$$

$$\delta W = (P - P_0) \cdot dV + P_0 \cdot dV$$

Variation of the amount of exergy in a closed system

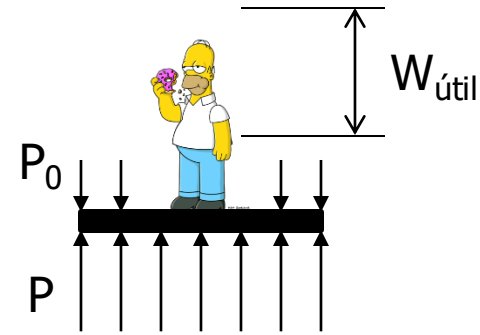
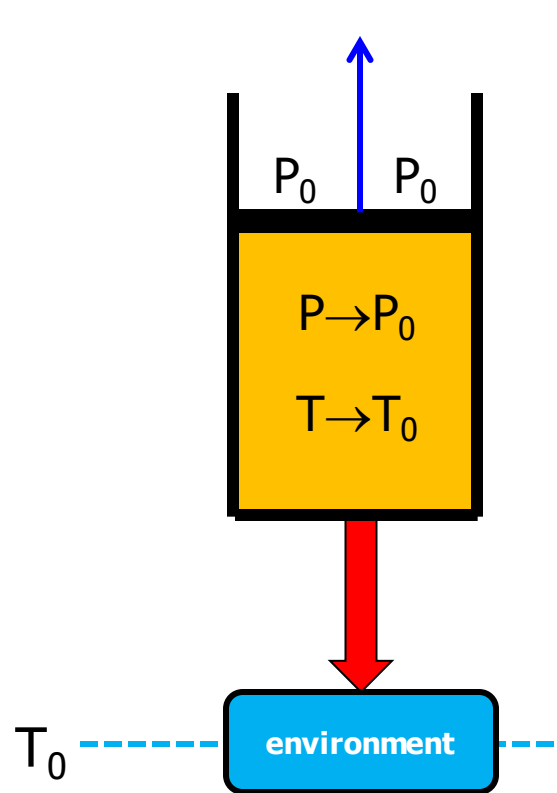


$$\delta W = P \cdot dV$$

$$\delta W = (P - P_0) \cdot dV + P_0 \cdot dV$$

$$\delta W = \delta W_{\text{útil}} + P_0 \cdot dV$$

Variation of the amount of exergy in a closed system



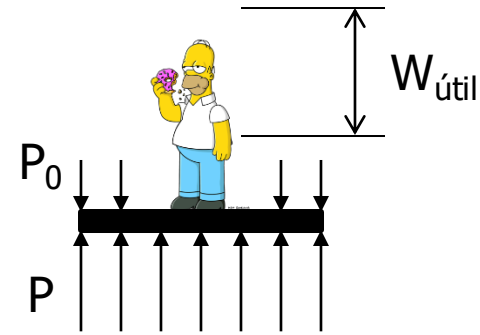
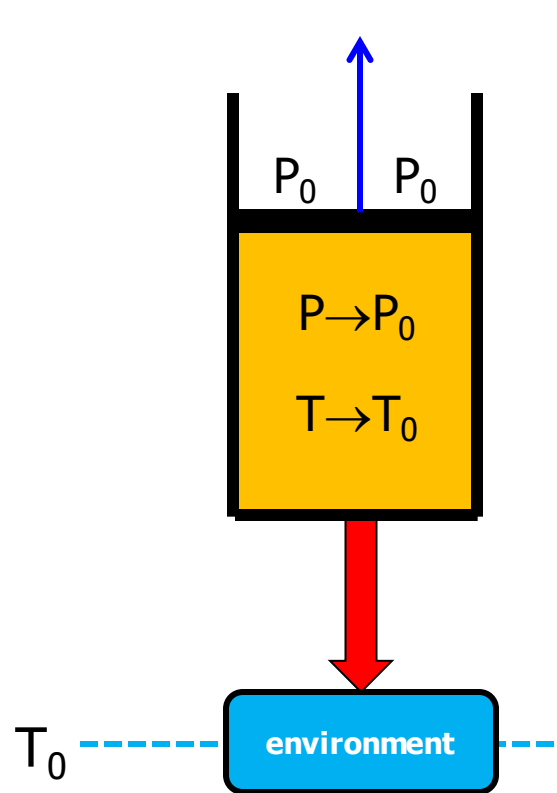
$$\delta W = P \cdot dV$$

$$\delta W = (P - P_0) \cdot dV + P_0 \cdot dV$$

$$\delta W = \delta W_{\text{util}} + P_0 \cdot dV$$

$$W = W_{\text{util}} + \int P_0 \cdot dV$$

Variation of the amount of exergy in a closed system



$$\delta W = P \cdot dV$$

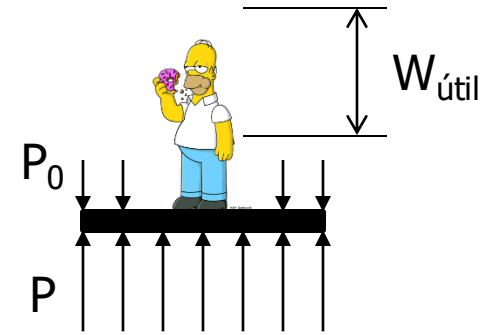
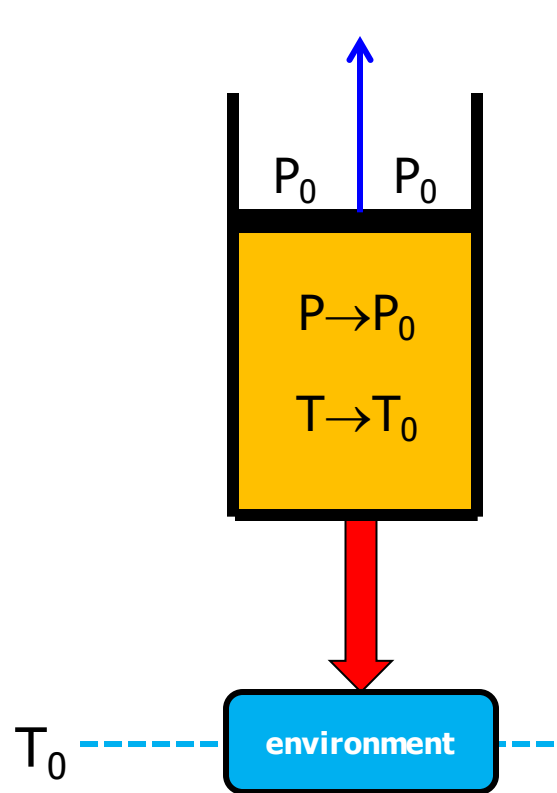
$$\delta W = (P - P_0) \cdot dV + P_0 \cdot dV$$

$$\delta W = \delta W_{\text{útil}} + P_0 \cdot dV$$

$$W = W_{\text{útil}} + \int P_0 \cdot dV$$

$$W = W_{\text{útil}} + P_0 \cdot (V_2 - V_1)$$

Variation of the amount of exergy in a closed system



$$\delta W = P \cdot dV$$

$$\delta W = (P - P_0) \cdot dV + P_0 \cdot dV$$

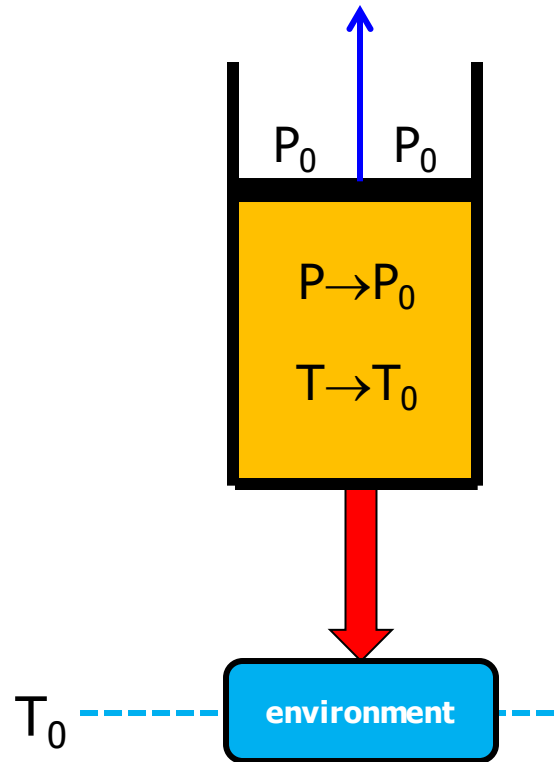
$$\delta W = \delta W_{\text{util}} + P_0 \cdot dV$$

$$W = W_{\text{util}} + \int P_0 \cdot dV$$

$$W = W_{\text{util}} + P_0 \cdot (V_2 - V_1)$$

$$W = W_{\text{util}} + W_{\text{env}}$$

Variation of the amount of exergy in a closed system

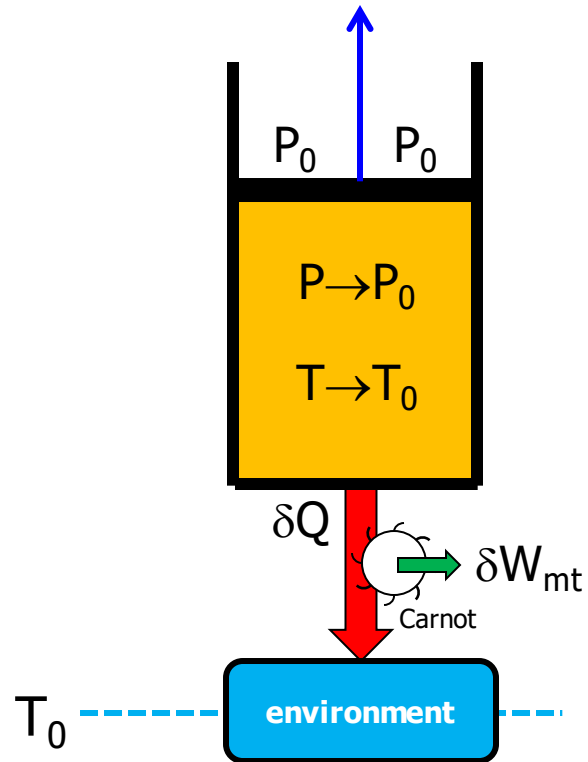


$$\delta W = \delta W_{\text{util}} + P_0 \cdot dV$$



$$\delta Q|_{\text{rev}} \stackrel{\text{def}}{=} T \cdot dS$$

Variation of the amount of exergy in a closed system

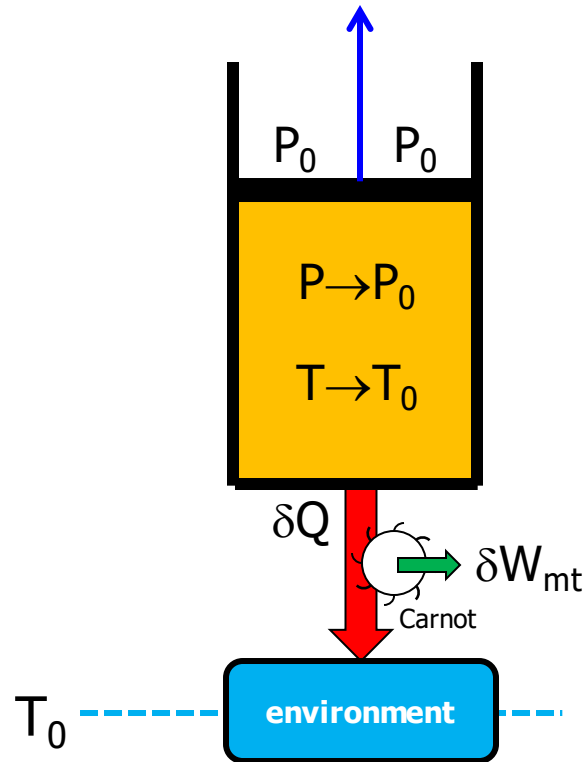


$$\delta W = \delta W_{\text{útil}} + P_0 \cdot dV$$



$$\delta Q \Big|_{\text{rev}} \stackrel{\text{def}}{=} T \cdot dS$$

Variation of the amount of exergy in a closed system



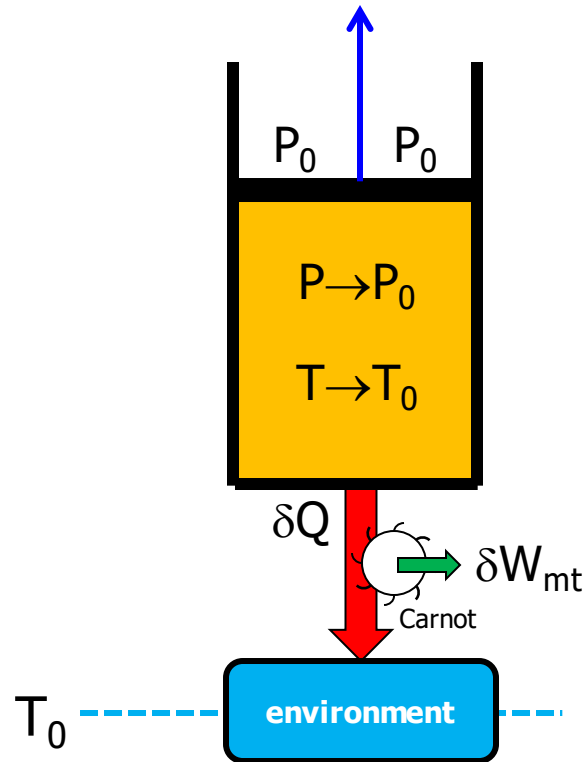
$$\delta W = \delta W_{\text{util}} + P_0 \cdot dV$$



$$\delta Q|_{\text{rev}} \stackrel{\text{def}}{=} T \cdot dS$$

$$\delta W_{\text{mt}} = \left(1 - \frac{T_0}{T} \right) \cdot \delta Q$$

Variation of the amount of exergy in a closed system



$$\delta W = \delta W_{\text{útil}} + P_0 \cdot dV$$

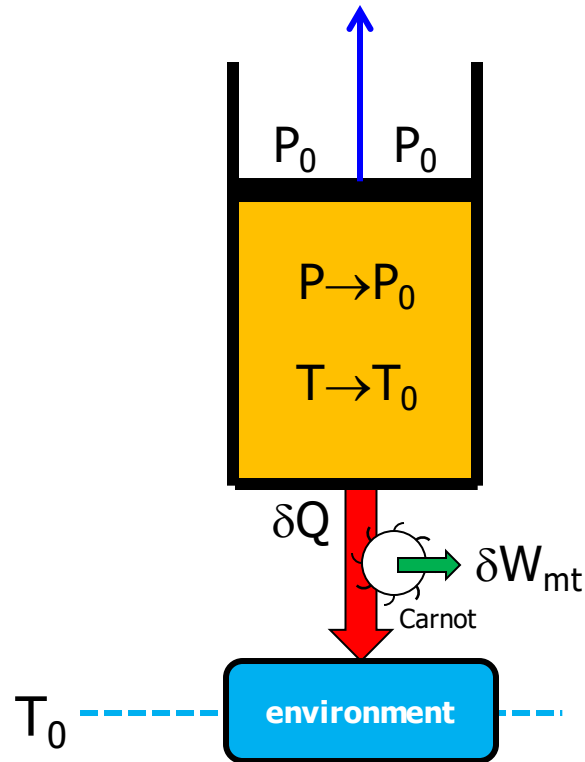


$$\delta Q|_{\text{rev}} \stackrel{\text{def}}{=} T \cdot dS$$

$$\delta W_{\text{mt}} = \left(1 - \frac{T_0}{T} \right) \cdot \delta Q$$

$$\delta Q = \delta W_{\text{mt}} + \delta Q_{\text{env}} = \delta W_{\text{mt}} + T_0 \cdot ds$$

Variation of the amount of exergy in a closed system



$$\delta W = \delta W_{\text{útil}} + P_0 \cdot dV$$



$$\delta Q|_{\text{rev}} \stackrel{\text{def}}{=} T \cdot dS$$

$$\delta W_{\text{mt}} = \left(1 - \frac{T_0}{T} \right) \cdot \delta Q$$

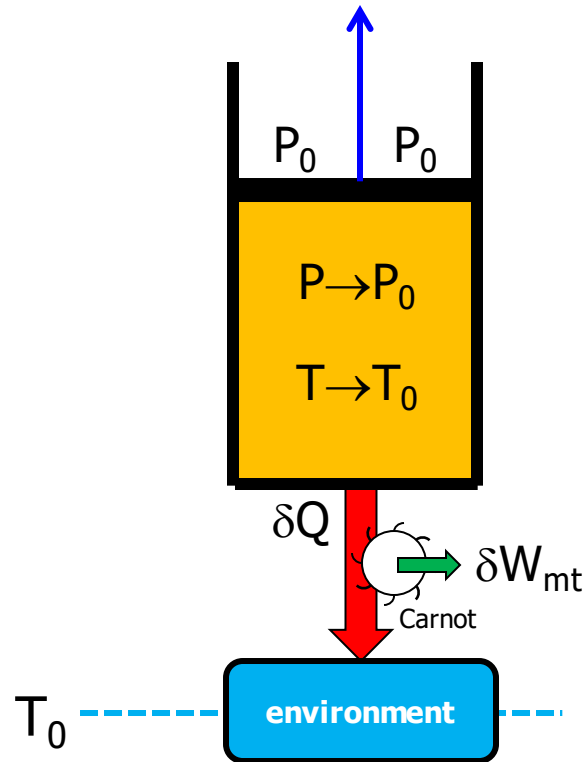
$$\delta Q = \delta W_{\text{mt}} + \delta Q_{\text{env}} = \delta W_{\text{mt}} + T_0 \cdot ds$$

$$dU = -\delta Q - \delta W$$



heat going out
of the system

Variation of the amount of exergy in a closed system



$$\delta W = \delta W_{\text{util}} + P_0 \cdot dV$$



$$\delta Q \Big|_{\text{rev}} \stackrel{\text{def}}{=} T \cdot dS$$

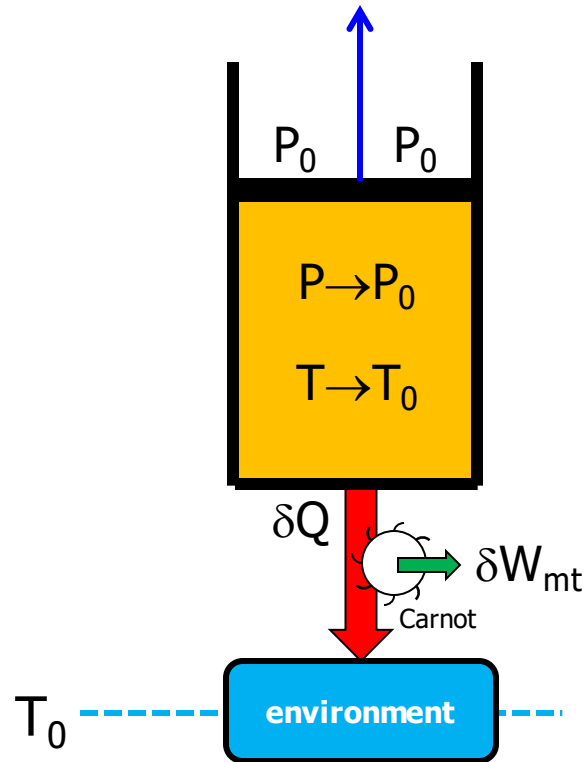
$$\delta W_{\text{mt}} = \left(1 - \frac{T_0}{T} \right) \cdot \delta Q$$

$$\delta Q = \delta W_{\text{mt}} + \delta Q_{\text{env}} = \delta W_{\text{mt}} + T_0 \cdot ds$$

$$dU = -\delta Q - \delta W$$

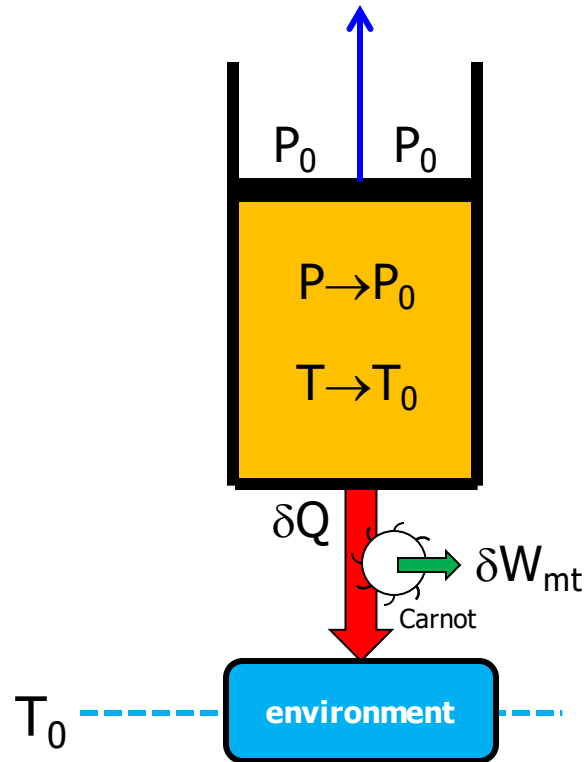
$$dU = -(\delta W_{\text{mt}} + T_0 dS) - (\delta W_{\text{util}} + P_0 dV)$$

Variation of the amount of exergy in a closed system



$$\Rightarrow dU = -(\delta W_{mt} + T_0 dS) - (\delta W_{util} + P_0 dV)$$

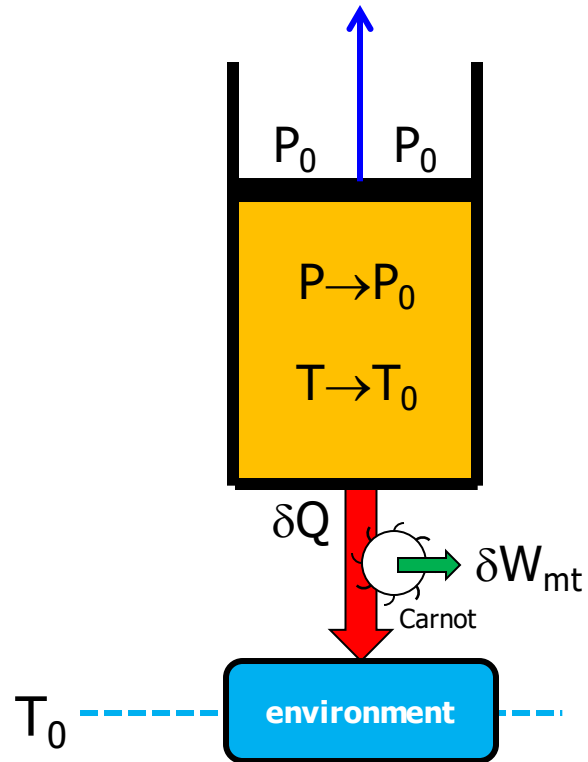
Variation of the amount of exergy in a closed system



$$\Rightarrow dU = -(\delta W_{mt} + T_0 dS) - (\delta W_{\acute{u}til} + P_0 dV)$$

$$\delta W_{\acute{u}til \text{ total}} = \delta W_{mt} + \delta W_{\acute{u}til}$$

Variation of the amount of exergy in a closed system

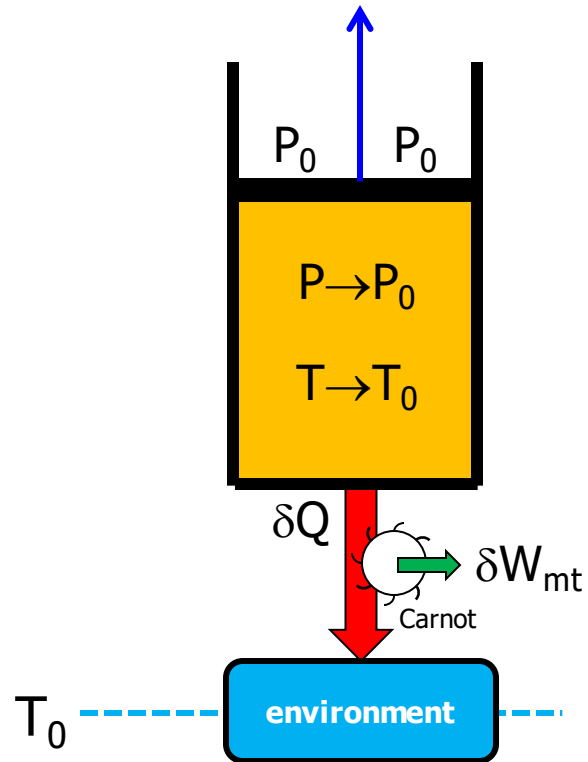


$$\Rightarrow dU = -(\delta W_{mt} + T_0 dS) - (\delta W_{\acute{u}til} + P_0 dV)$$

$$\delta W_{\acute{u}til\ total} = \delta W_{mt} + \delta W_{\acute{u}til}$$

$$\delta W_{\acute{u}til\ total} = -dU - P_0 dV - T_0 dS$$

Variation of the amount of exergy in a closed system



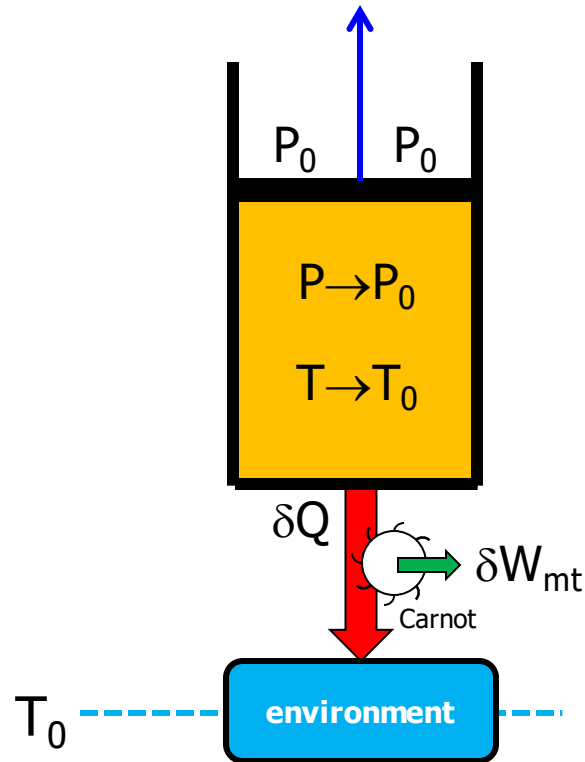
$$\Rightarrow dU = -(\delta W_{mt} + T_0 dS) - (\delta W_{util} + P_0 dV)$$

$$\delta W_{util\ total} = \delta W_{mt} + \delta W_{util}$$

$$\delta W_{util\ total} = -dU - P_0 dV - T_0 dS$$

$$\int_{inicial}^0 \delta W_{util\ total} = \dots$$

Variation of the amount of exergy in a closed system



$$\Rightarrow dU = -(\delta W_{mt} + T_0 dS) - (\delta W_{util} + P_0 dV)$$

$$\delta W_{util\ total} = \delta W_{mt} + \delta W_{util}$$

$$\delta W_{util\ total} = -dU - P_0 dV - T_0 dS$$

$$\int_{inicial}^0 \delta W_{util\ total} = \dots$$

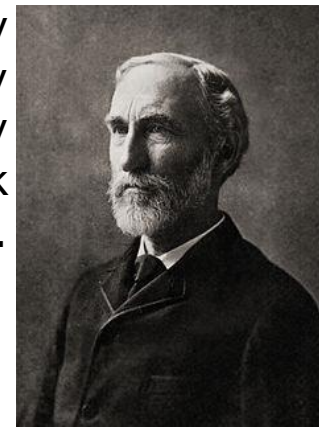
$$\Rightarrow W_{util\ total} = (U - U_0) + P_0 (V - V_0) - T_0 (S - S_0)$$

DEFINITIONS

Exergy...

$$X \stackrel{\text{def}}{=} (U - U_0) + P_0(V - V_0) - T_0(S - S_0)$$

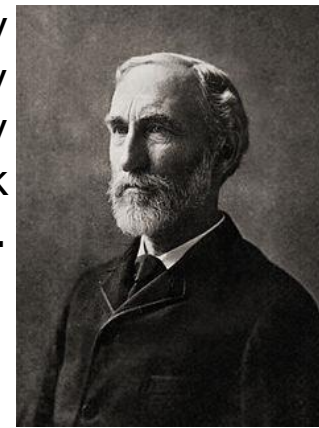
Available energy
Exergetic energy
Availability
Reversible work
Etc.



J. Willard Gibbs

DEFINITIONS

Available energy
Exergetic energy
Availability
Reversible work
Etc.



J. Willard Gibbs

Exergy...

$$X^{\text{def}} = (U - U_0) + P_0(V - V_0) - T_0(S - S_0)$$

accounts the influence of the environment

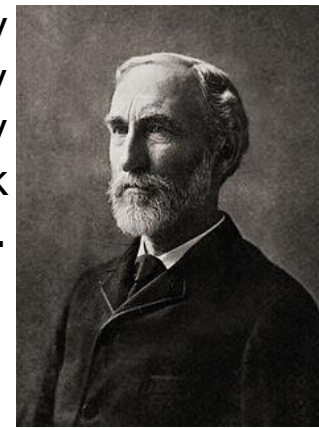
properties of the system
when in equilibrium with
the environment

DEFINITIONS

Exergy...

$$X \stackrel{\text{def}}{=} \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}}$$

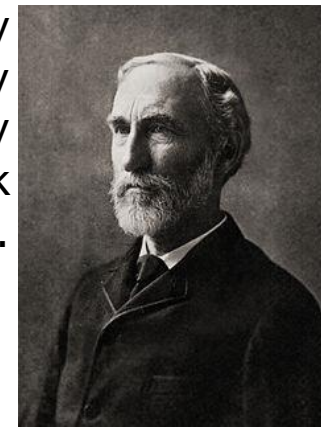
Available energy
Exergetic energy
Availability
Reversible work
Etc.



J. Willard Gibbs

DEFINITIONS

Available energy
Exergetic energy
Availability
Reversible work
Etc.



J. Willard Gibbs

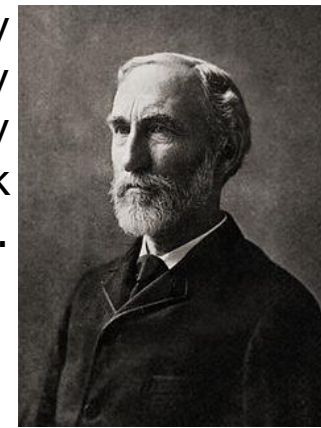
Exergy...

$$X^{\text{def}} = \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}}$$

$$X^{\text{def}} = \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}} + \underbrace{EP + EC}_{\text{mechanical exergy}}$$

DEFINITIONS

Available energy
Exergetic energy
Availability
Reversible work
Etc.



J. Willard Gibbs

Exergy...

$$X^{\text{def}} = \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}}$$

$$X^{\text{def}} = \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}} + \underbrace{EP + EC}_{\text{mechanical exergy}}$$

$$X^{\text{def}} = \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}} + \underbrace{EP + EC}_{\text{mechanical exergy}} + \underbrace{EQ}_{\text{chemical exergy}}$$

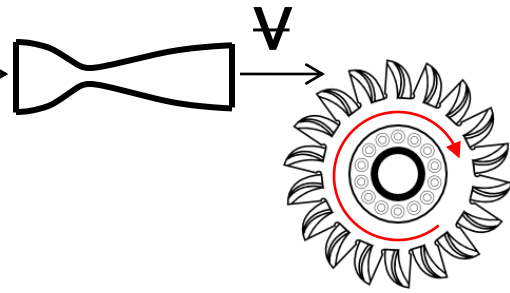
Ar @
10bar, 25°C

CH₄ @
10bar, 25°C



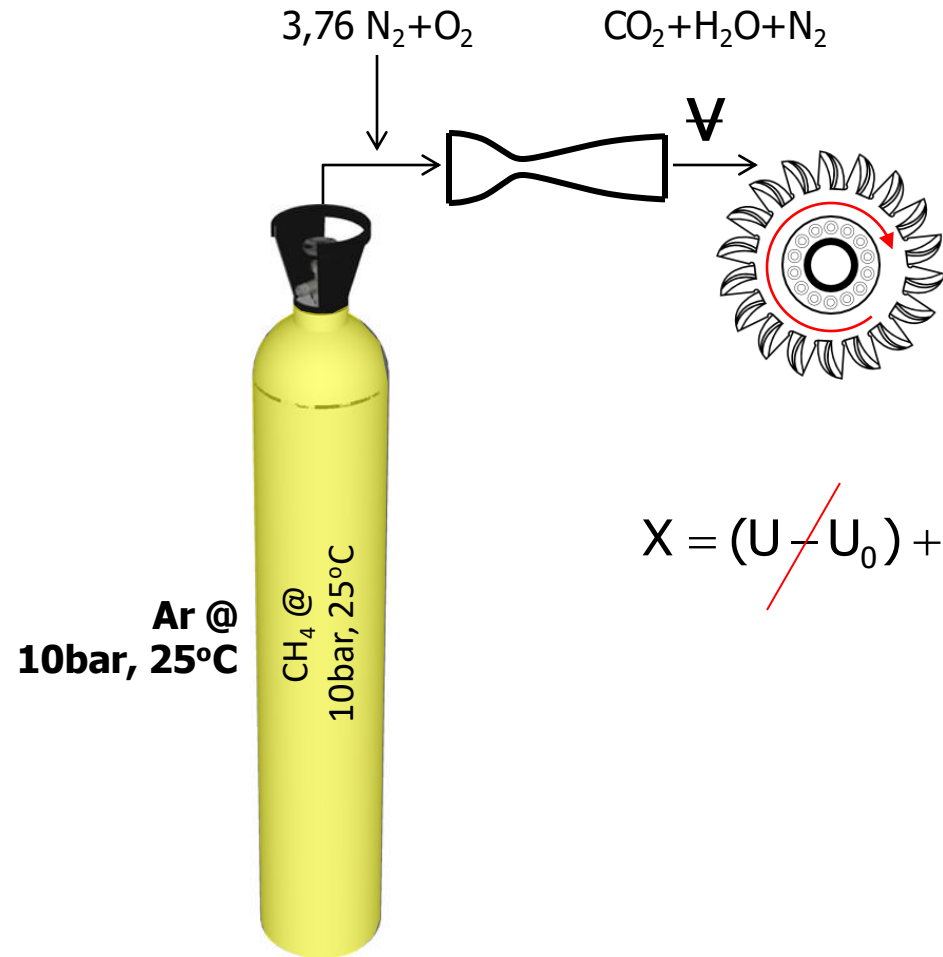
3,76 N₂+O₂

CO₂+H₂O+N₂



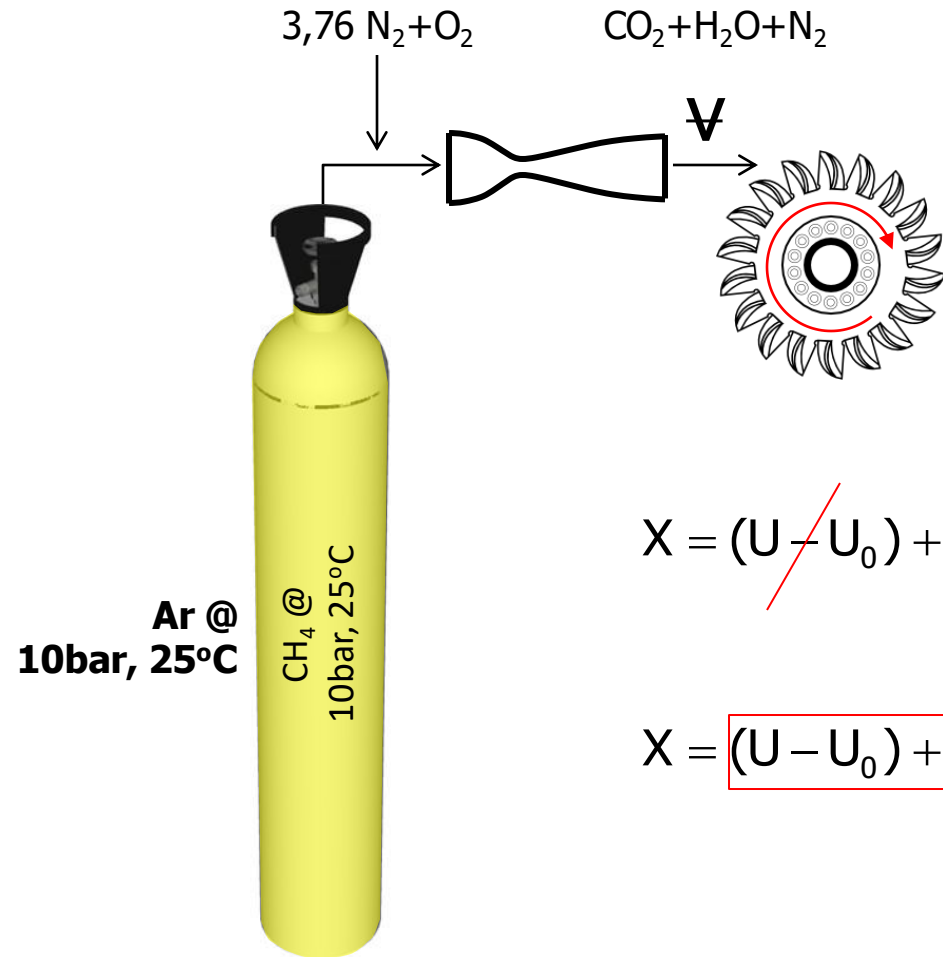
Chemical exergy is the maximum amount of work when its constituents are chemically transformed to those of the environment

$$X = (U - U_0) + P_0(V - V_0) - T_0(S - S_0) + EP + EC + EQ$$



Chemical exergy is the maximum amount of work when its constituents are chemically transformed to those of the environment

$$X = (\cancel{U - U_0}) + P_0(\cancel{V - V_0}) - T_0(\cancel{S - S_0}) + \cancel{EP} + \cancel{EC} + EQ$$

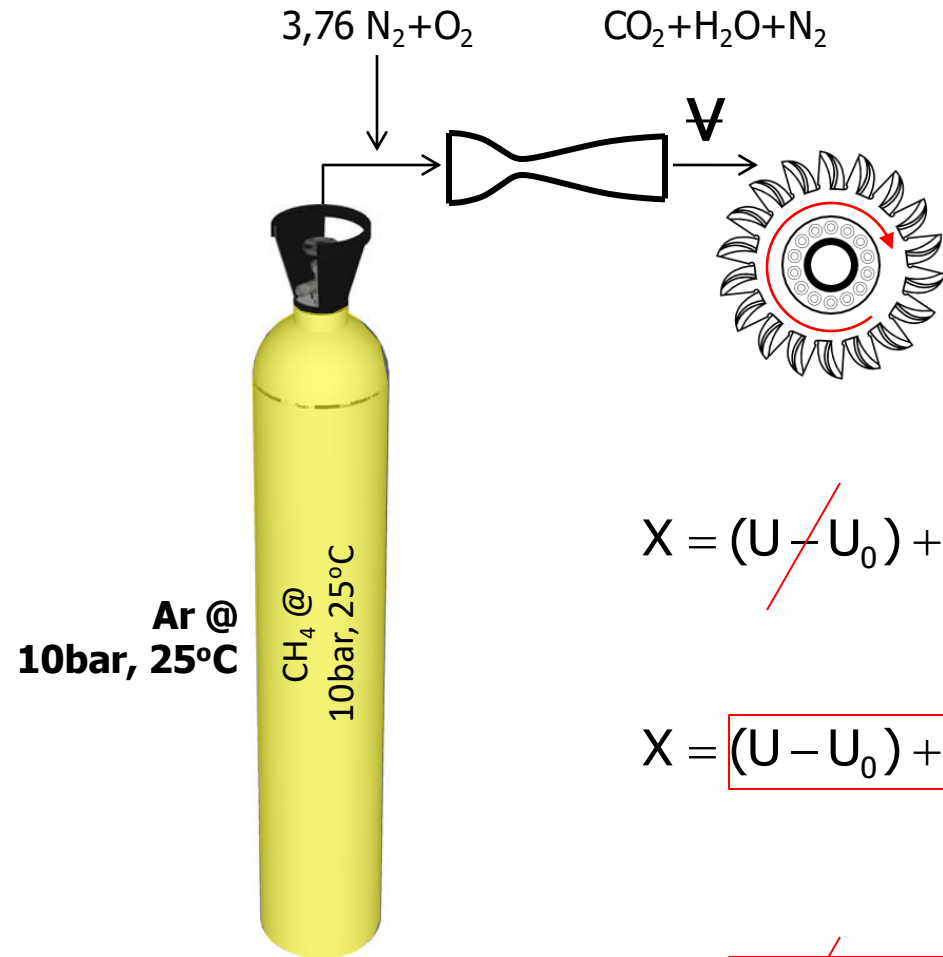


Chemical exergy is the maximum amount of work when its constituents are chemically transformed to those of the environment

$$X = (\cancel{U - U_0}) + P_0(\cancel{V - V_0}) - T_0(\cancel{S - S_0}) + \cancel{EP} + \cancel{EC} + EQ$$

$$X = \boxed{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)} + \cancel{EP} + \cancel{EC} + \boxed{EQ}$$

A red arrow points from the box around EQ to the box around the first three terms, indicating that the sum of these terms is also part of the exergy calculation.



Chemical exergy is the maximum amount of work when its constituents are chemically transformed to those of the environment

$$X = (\cancel{U - U_0}) + P_0(\cancel{V - V_0}) - T_0(\cancel{S - S_0}) + \cancel{EP} + \cancel{EC} + EQ$$

$$X = \boxed{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)} + \cancel{EP} + \cancel{EC} + \boxed{EQ}$$

A red arrow points from the boxed term to the boxed EQ term, indicating that the first three terms are grouped together as chemical exergy.

$$X = \boxed{(\cancel{U - U_0}) + P_0(\cancel{V - V_0}) - T_0(\cancel{S - S_0})} + \cancel{EP} + \boxed{EC} + \cancel{EQ}$$

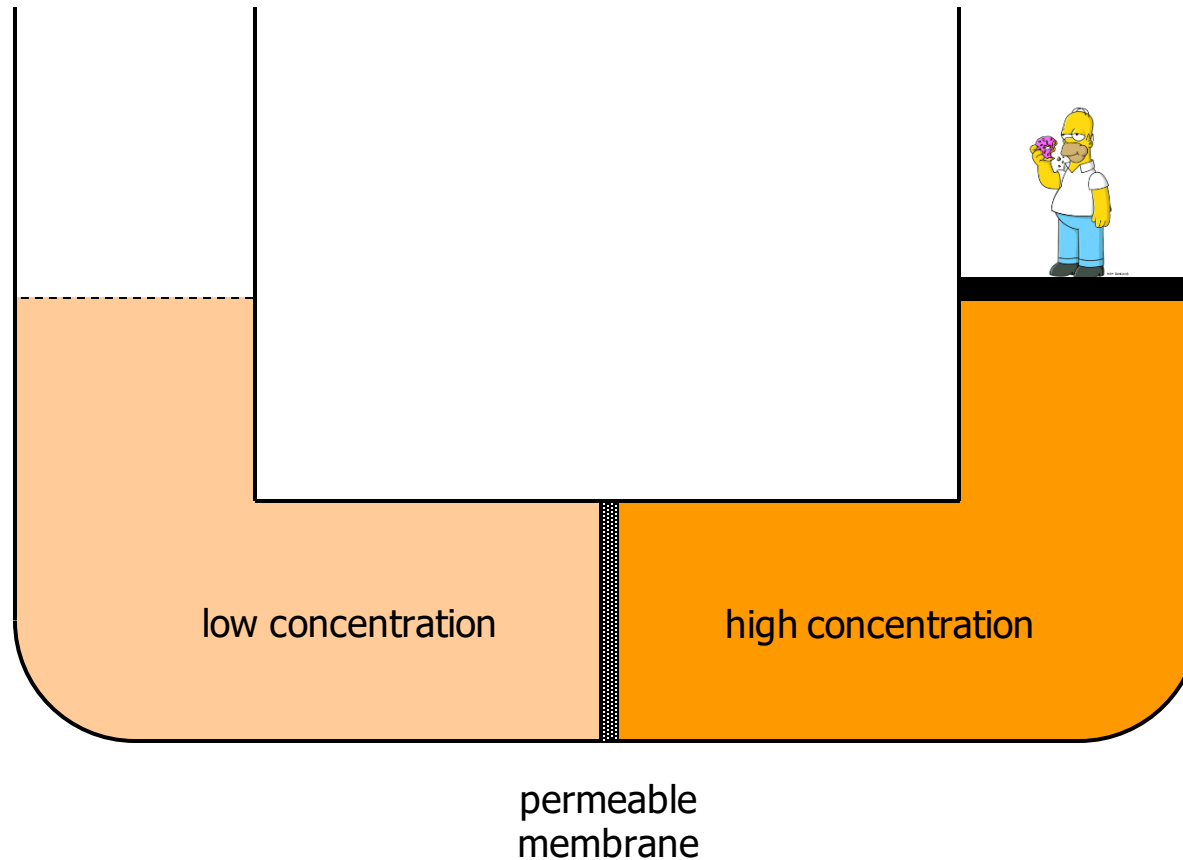
A red arrow points from the boxed term to the boxed EC term, indicating that the first three terms are grouped together as physical exergy.



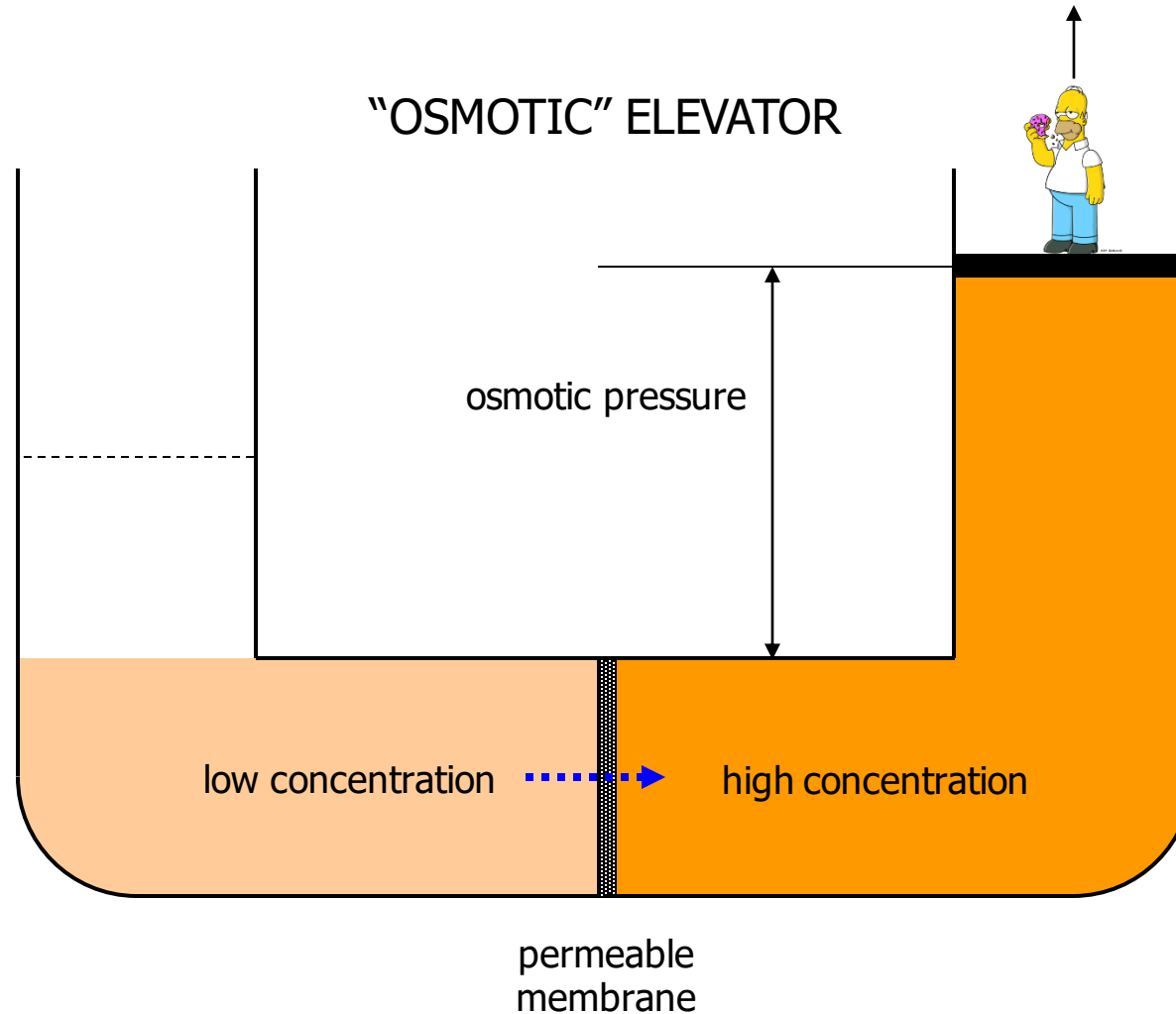
The potential to generate work (organized energy) exists when there are differences between the system and the environment. Those differences may be in terms of thermodynamic properties, chemical composition...

Potential to generate work from differences in chemical composition

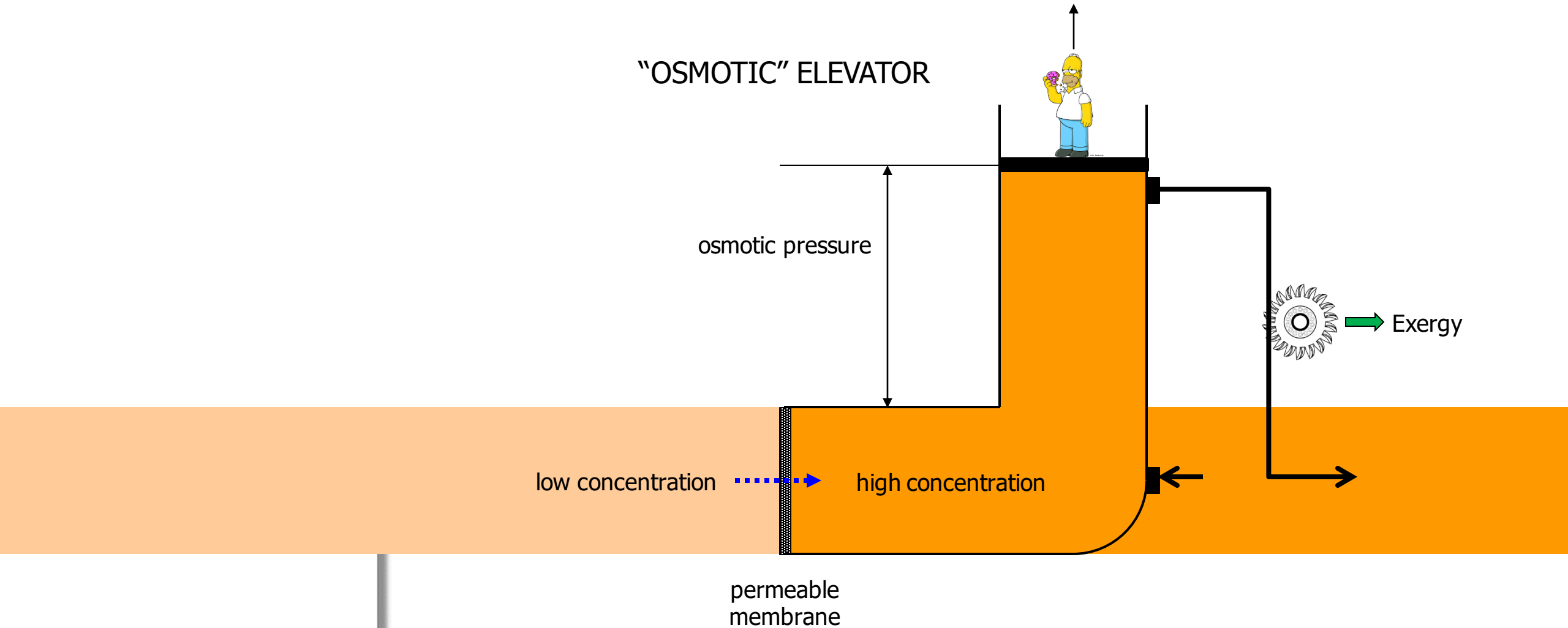
"OSMOTIC" ELEVATOR



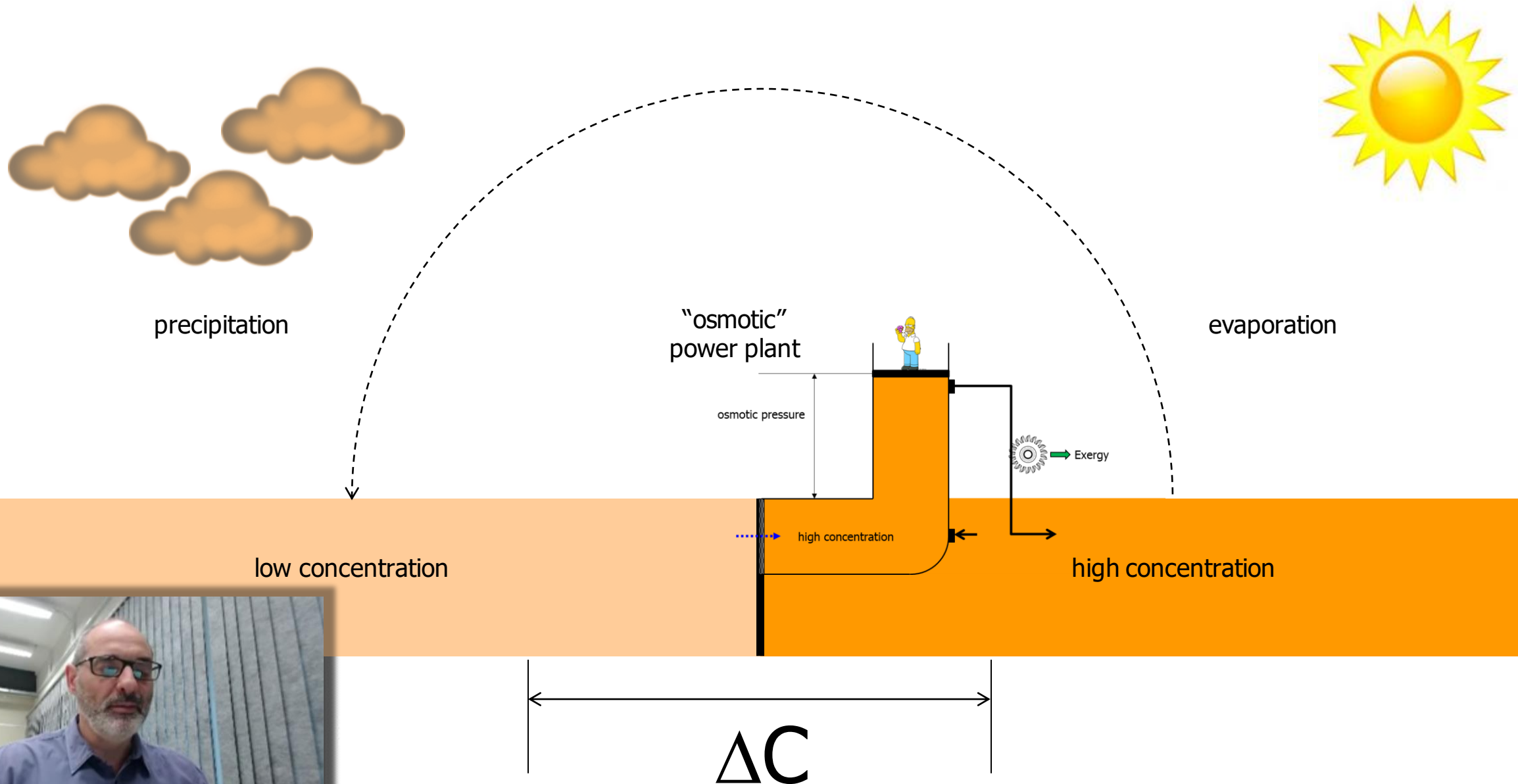
Potential to generate work from differences in chemical composition



Potential to generate work from differences in chemical composition

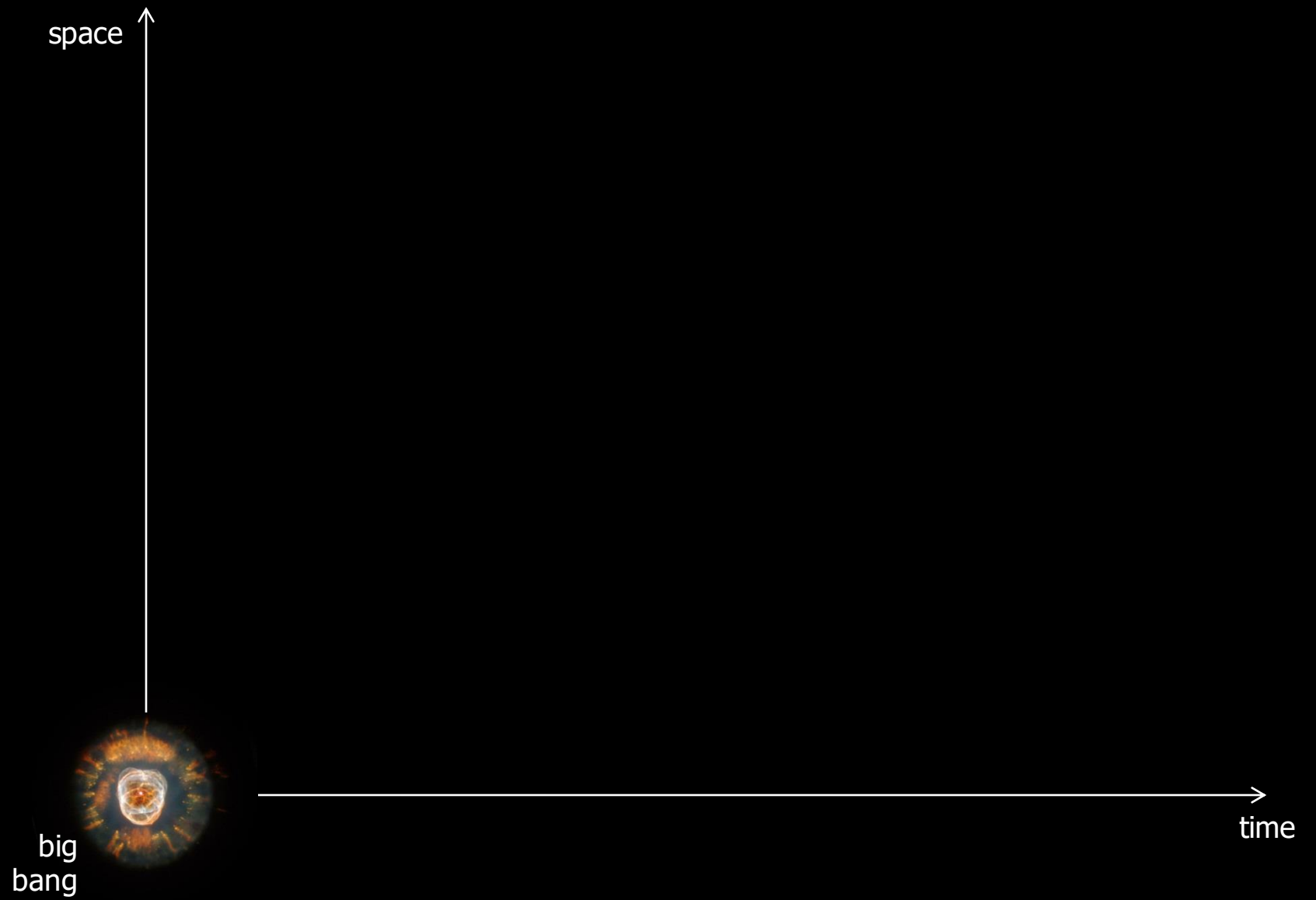


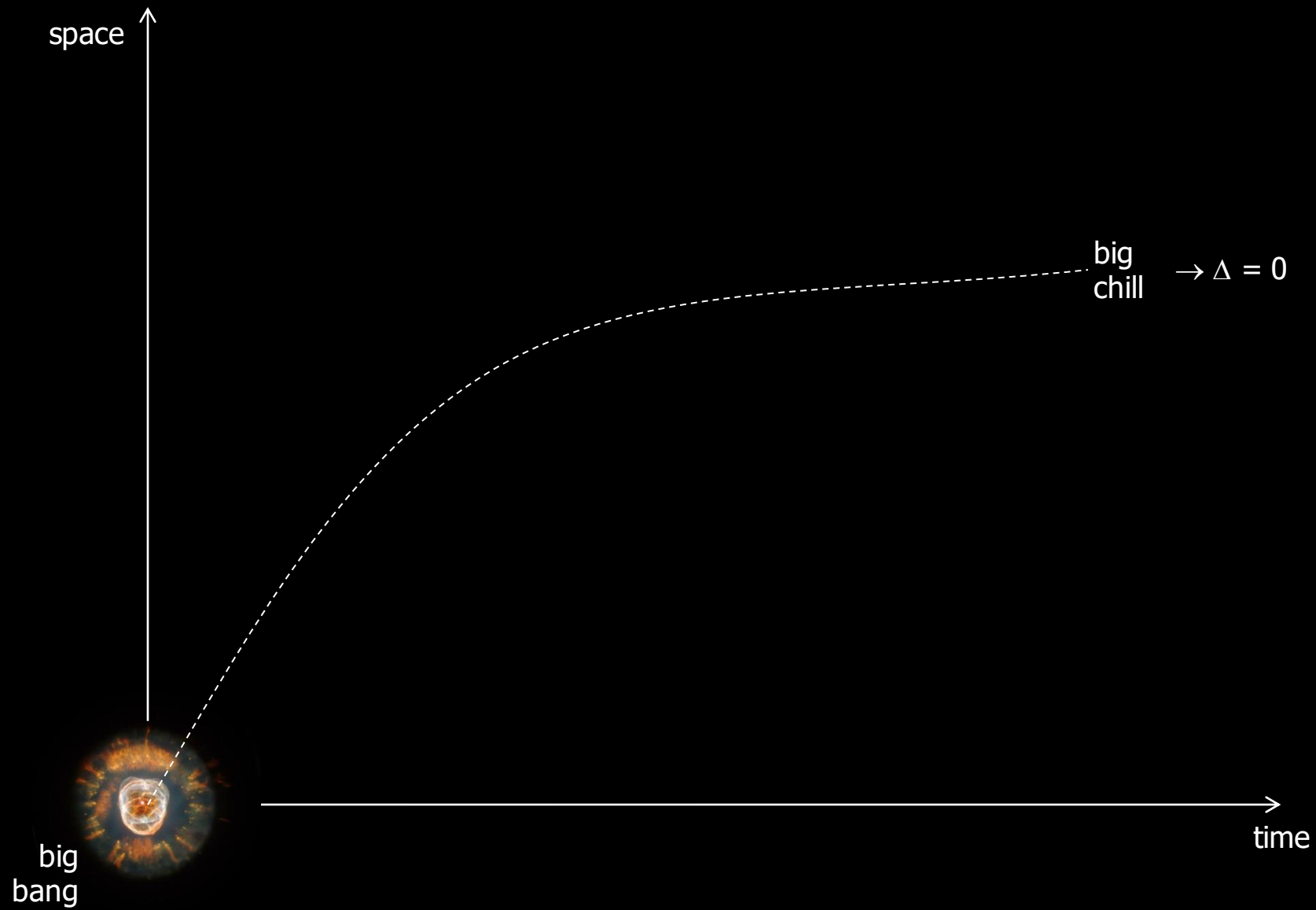
Potential to generate work from differences in chemical composition

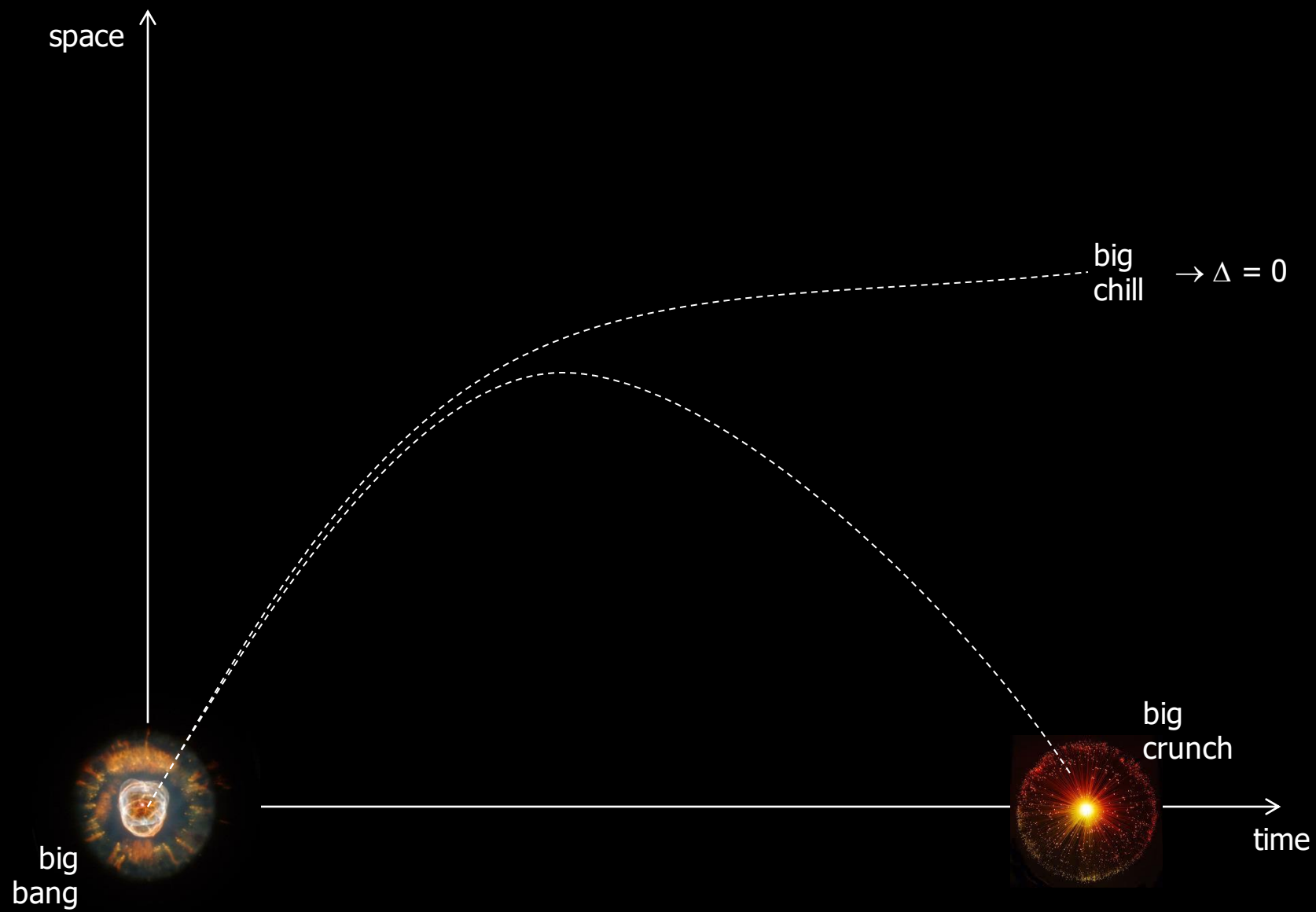


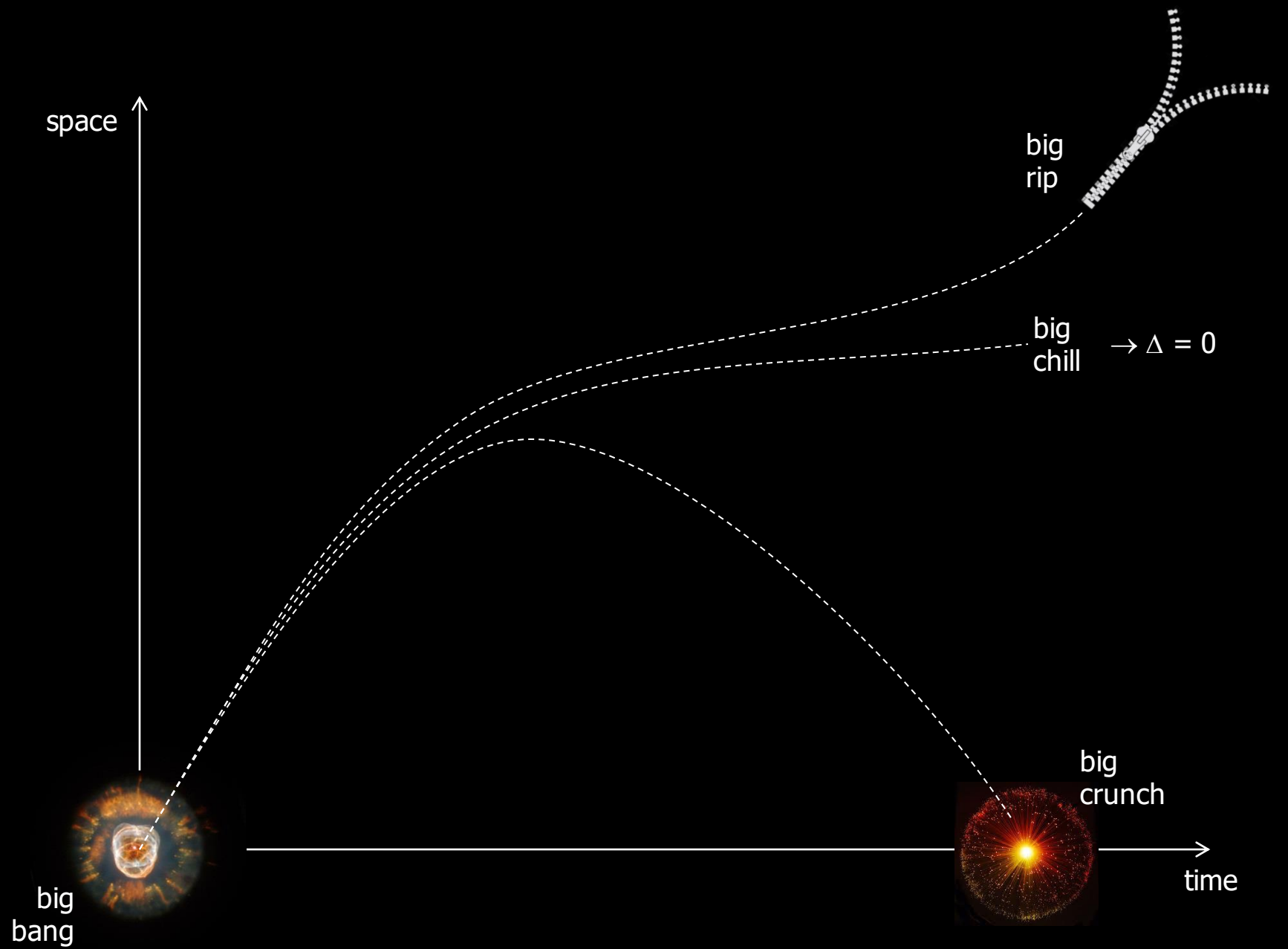


But if exergy can only be destroyed,
this means the total exergy of the
universe is decreasing and that all
differences tend to equalize,
pressures and temperatures become
the same, differences in chemical
composition disappear...





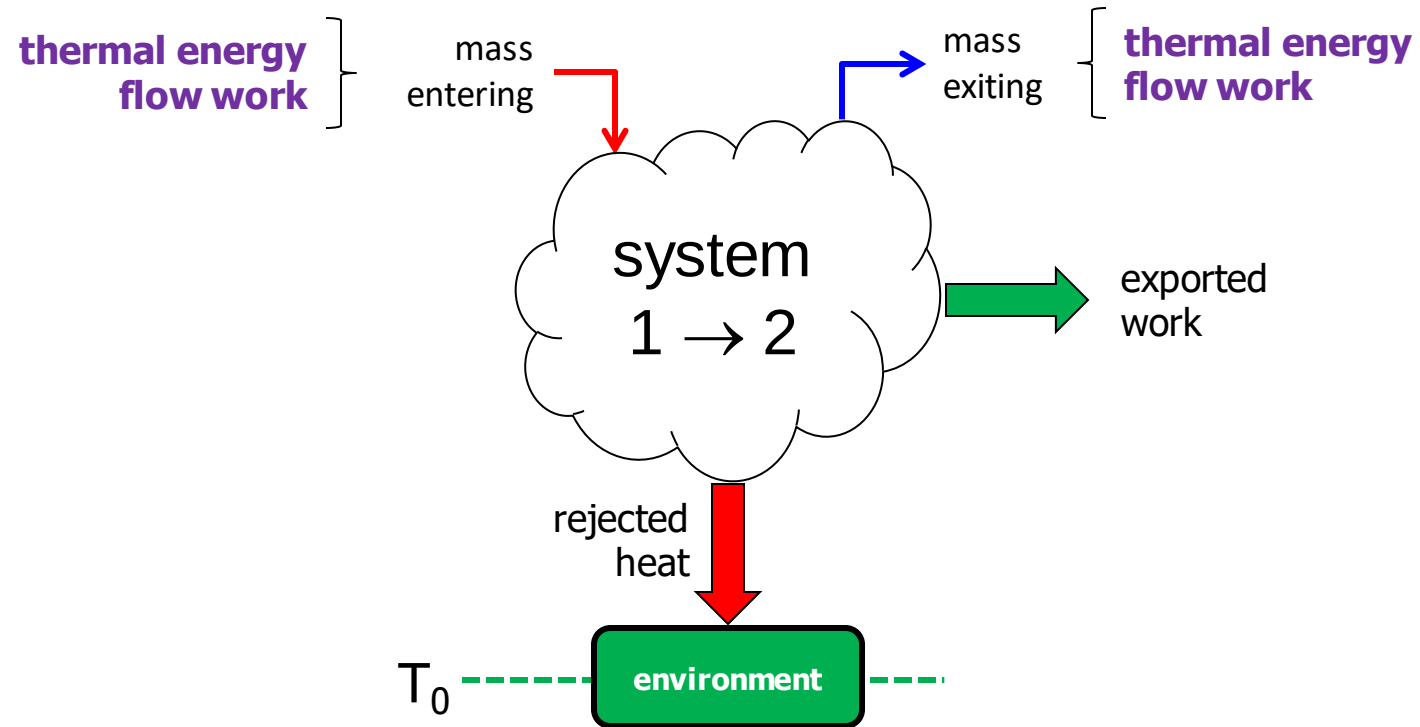




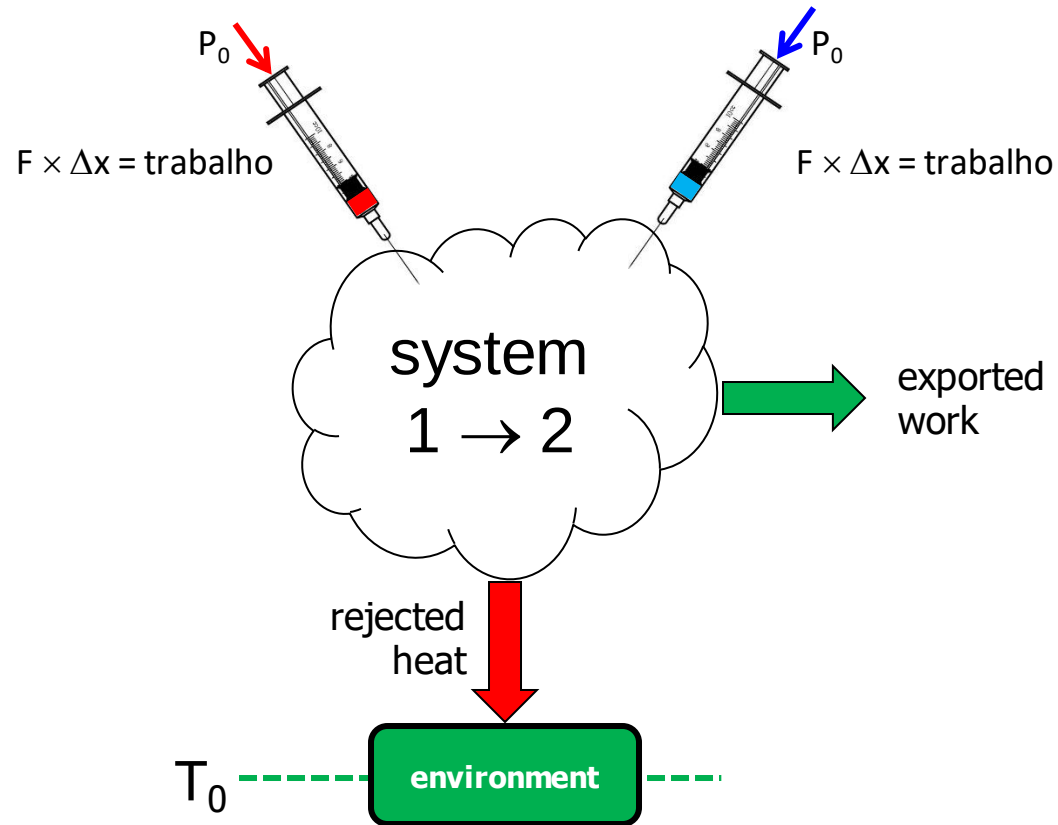
Open system analysis



Flow exergy and exergy flux of an open system



Flow exergy and exergy flux of an open system



$$W_{\text{fluxo}} = (P \cdot A) \cdot \Delta x = P \cdot V$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

$$X = X_{\text{sist. fechado}} + X_{\text{fluxo}}$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

$$X = \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{exergia termodinâmica}} + \underbrace{(P - P_0)V}_{\text{exergia de fluxo}}$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

$$X = (U - U_0) + \cancel{P_0(V - V_0)} - T_0(S - S_0) + \cancel{(P - P_0)V}$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

$$X = (U - U_0) + \cancel{P_0(V - V_0)} - T_0(S - S_0) + \cancel{(P - P_0)V}$$

$$X = (H - H_0) - T_0(S - S_0)$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

$$X = (U - U_0) + \cancel{P_0(V - V_0)} - T_0(S - S_0) + \cancel{(P - P_0)V}$$

$$X = (H - H_0) - T_0(S - S_0)$$

$$X = (H - H_0) - T_0(S - S_0) + EP + EC + EQ$$

$$W_{\text{fluxo}} = P \cdot (A \cdot \Delta x) = P \cdot V$$

$$X_{\text{fluxo}} = P \cdot V - P_0 \cdot V = (P - P_0) \cdot V$$

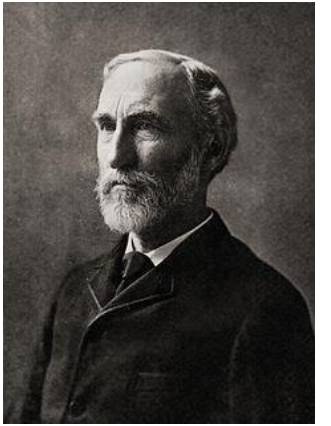
$$X = (U - U_0) + \cancel{P_0(V - V_0)} - T_0(S - S_0) + \cancel{(P - P_0)V}$$

$$X = (H - H_0) - T_0(S - S_0)$$

$$X = (H - H_0) - T_0(S - S_0) + EP + EC + EQ$$

$$x = (h - h_0) - T_0(s - s_0) + ep + ec + eq$$

second law efficiency
rational efficiency
etc.

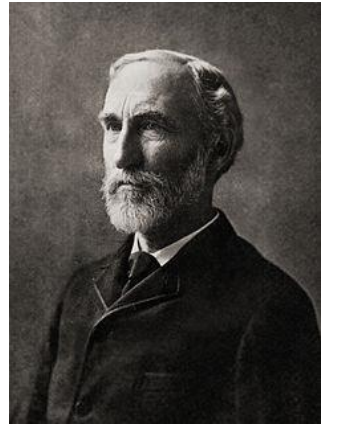


J. Willard Gibbs

DEFINITIONS

Exergetic efficiency is the ratio of the 1st law efficiency of a thermal cycle to the efficiency of a reversible cycle operating between the same temperatures

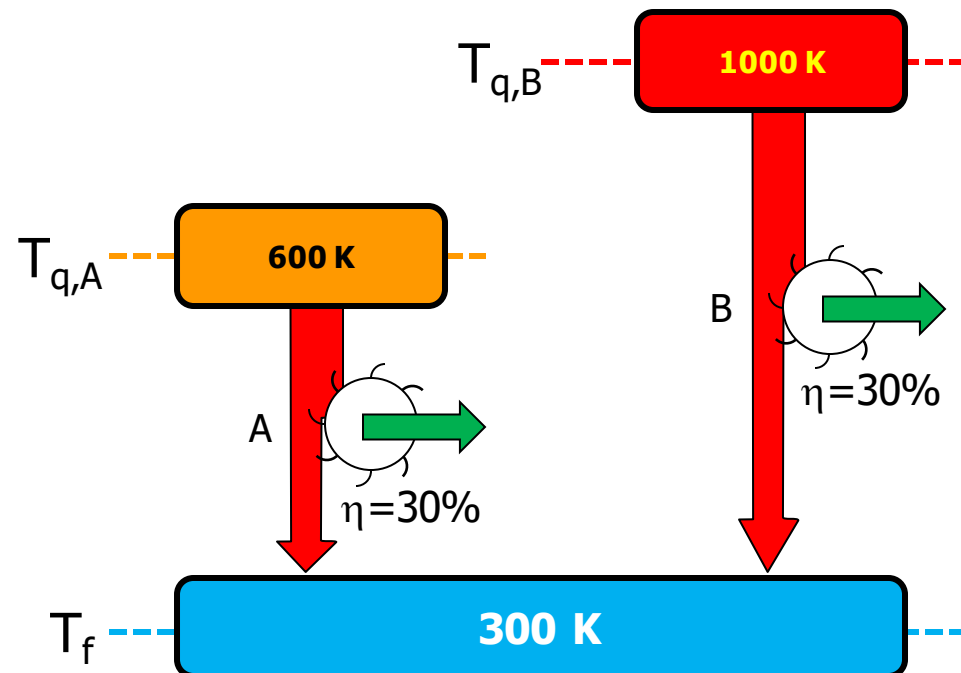
second law efficiency
rational efficiency
etc.



J. Willard Gibbs

DEFINITIONS

Exergetic efficiency is the ratio of the 1st law efficiency of a thermal cycle to the efficiency of a reversible cycle operating between the same temperatures



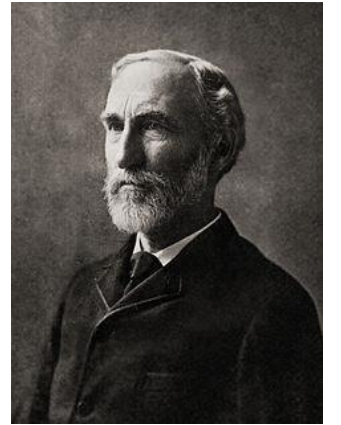
$$\eta_{2^{lei}}^{\text{def}} = \eta_{\text{term}} / \eta_{\text{rev}}$$

$$\eta_{\text{rev},A} = 1 - T_f / T_{q,A}$$

$$\eta_{2^{lei}} = 0,3 / (1 - 300 / 600)$$

$$\eta_{2^{lei}} = 0,60$$

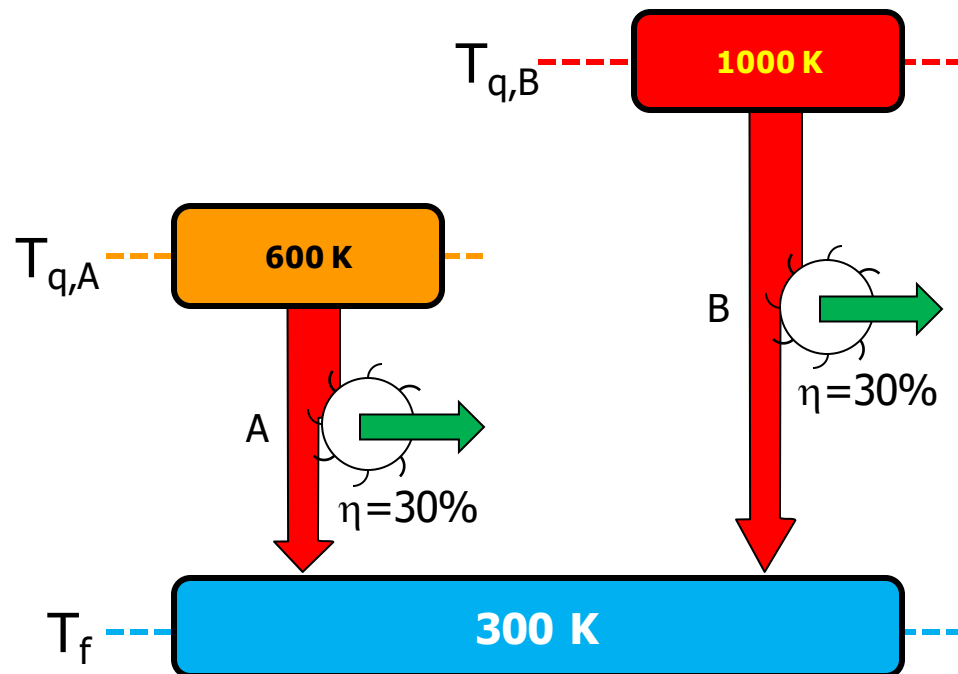
second law efficiency
rational efficiency
etc.



J. Willard Gibbs

DEFINITIONS

Exergetic efficiency is the ratio of the 1st law efficiency of a thermal cycle to the efficiency of a reversible cycle operating between the same temperatures

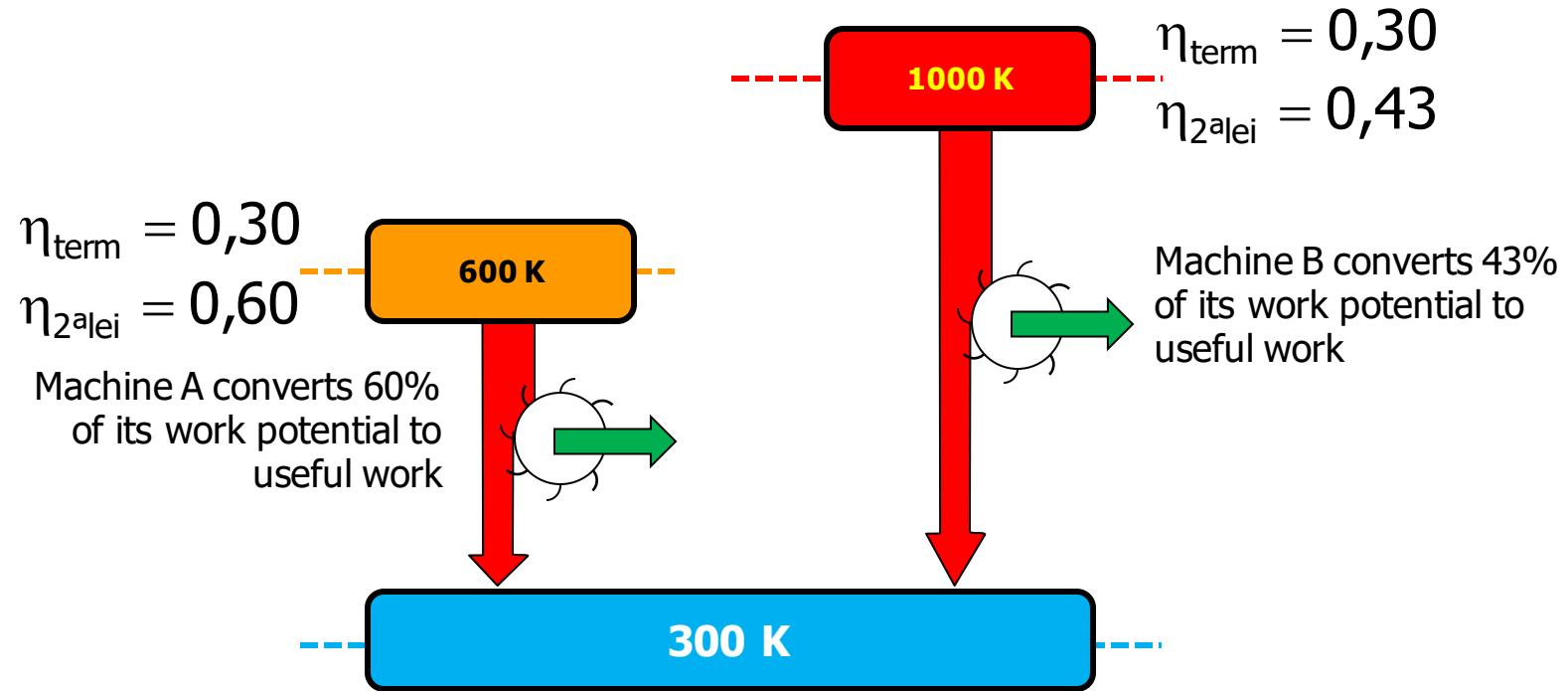


$$\eta_{2^{lei}}^{def} = \eta_{term} / \eta_{rev}$$

$$\eta_{rev,B} = 1 - T_f / T_{q,B}$$

$$\eta_{2^{lei}} = 0,3 / (1 - 300 / 1000)$$

$$\eta_{2^{lei}} = 0,43$$



$$\eta_{2^{\text{a}}\text{lei}} = \frac{W_{\text{útil}}}{W_{\text{rev}}} \Rightarrow \eta_{2^{\text{a}}\text{lei}} = \frac{\text{recovered exergy}}{\text{supplied exergy}} = 1 - \frac{\text{destroyed exergy}}{\text{supplied exergy}}$$

Exergy transfer mechanisms

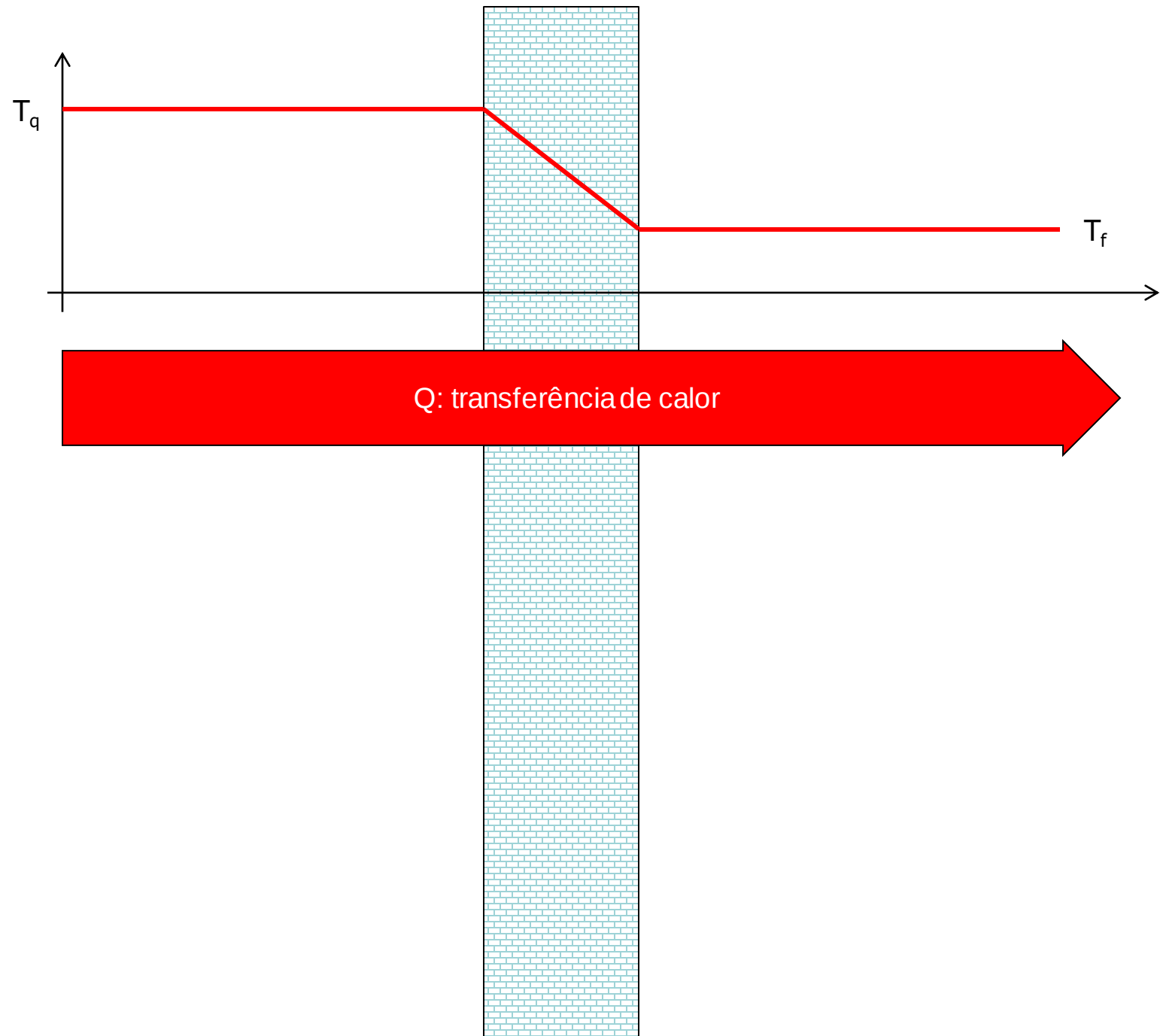
- Heat, work and mass flow

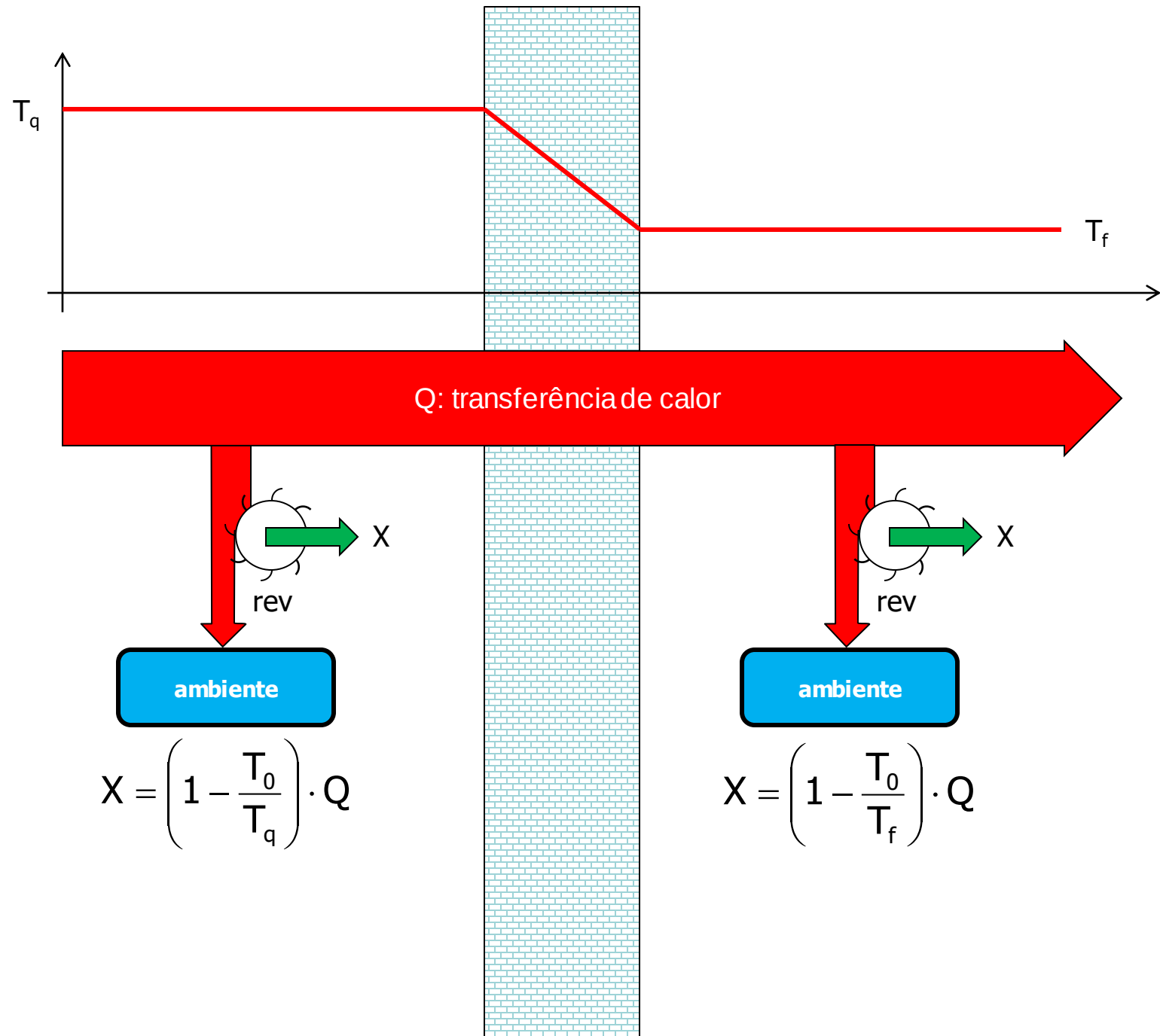
$$X \stackrel{\text{def}}{=} \underbrace{(U - U_0) + P_0(V - V_0) - T_0(S - S_0)}_{\text{thermodynamic exergy}} + \underbrace{EP}_{\text{mechanical exergy}} + \underbrace{EQ}_{\text{chemical exergy}}$$

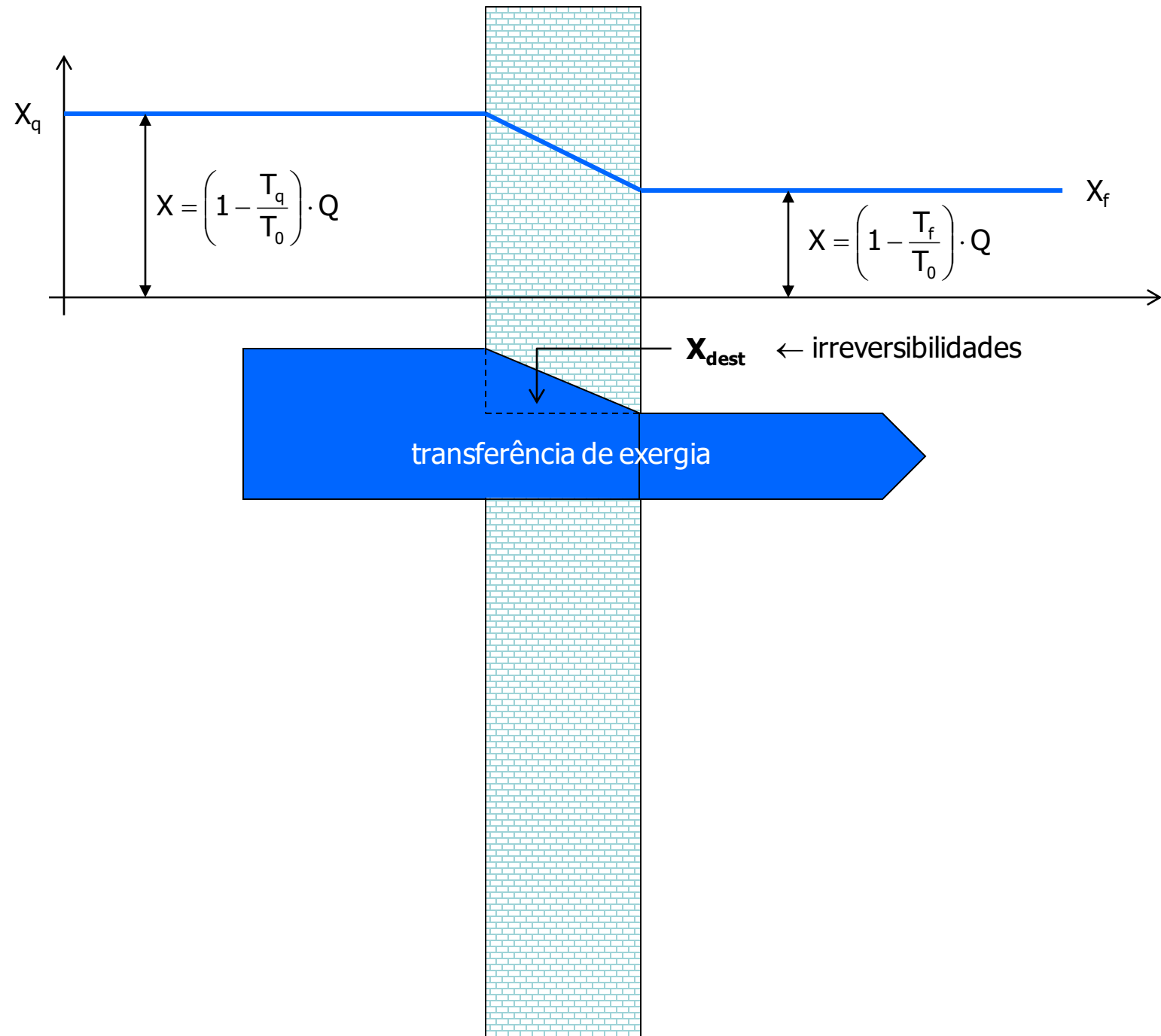
Exergy is a thermodynamic property, i.e. a state property

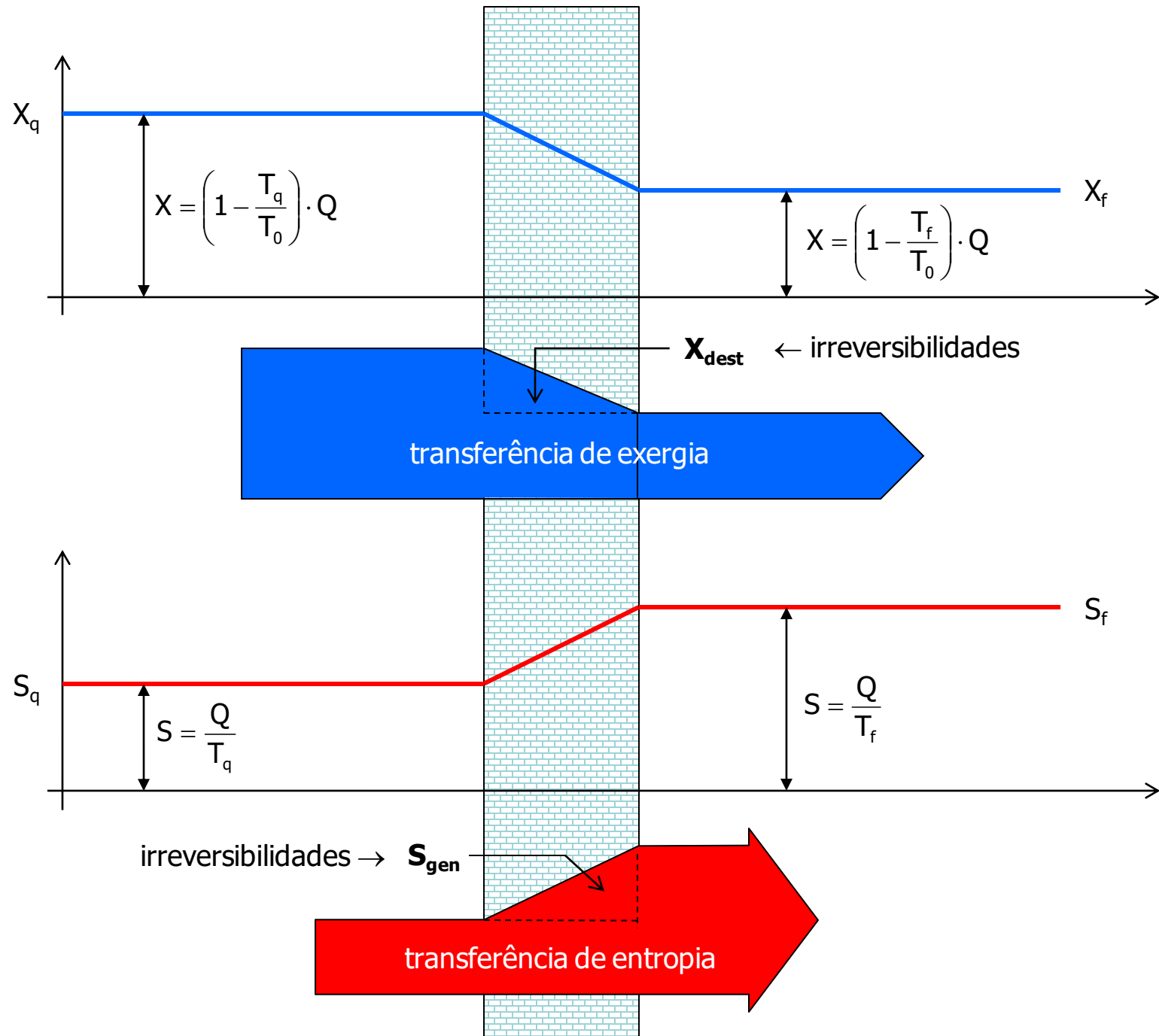
Exergy transfer through heat...

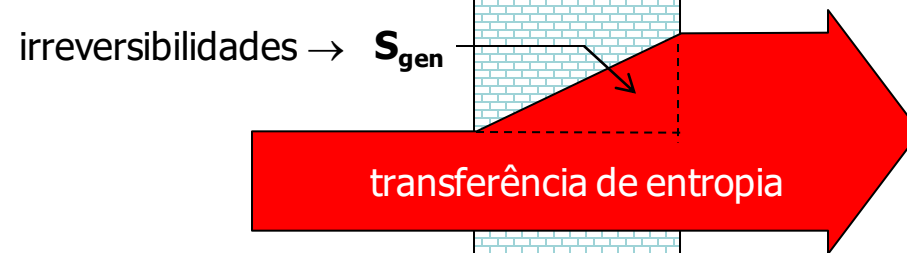
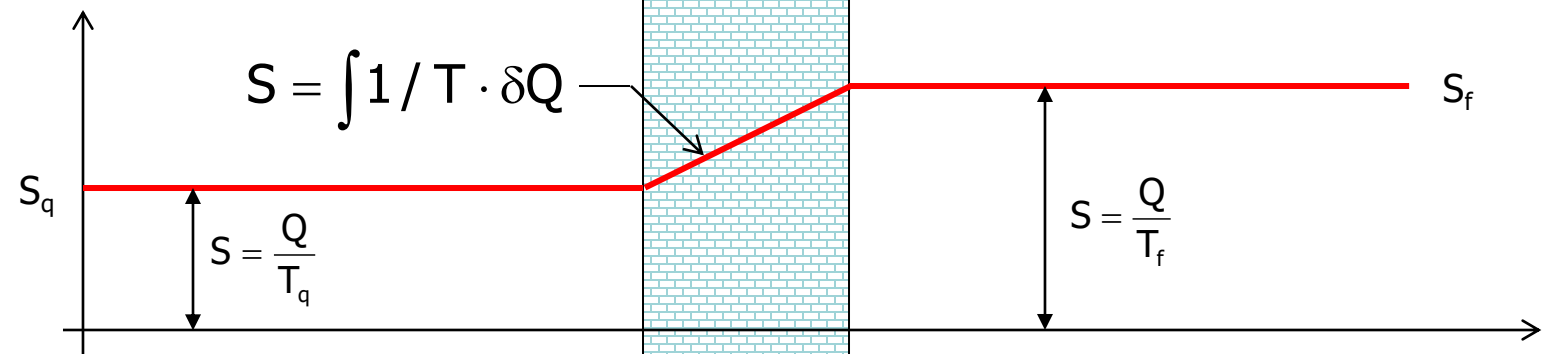
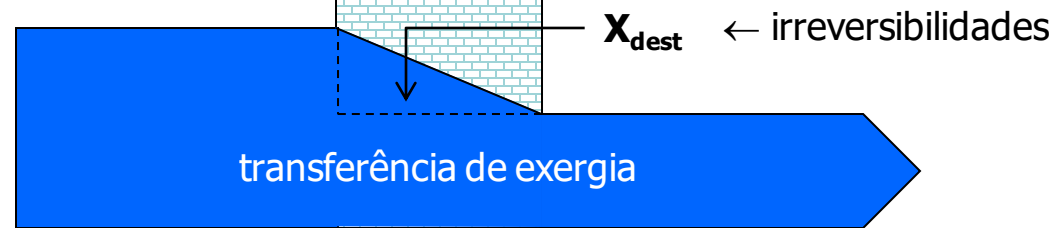
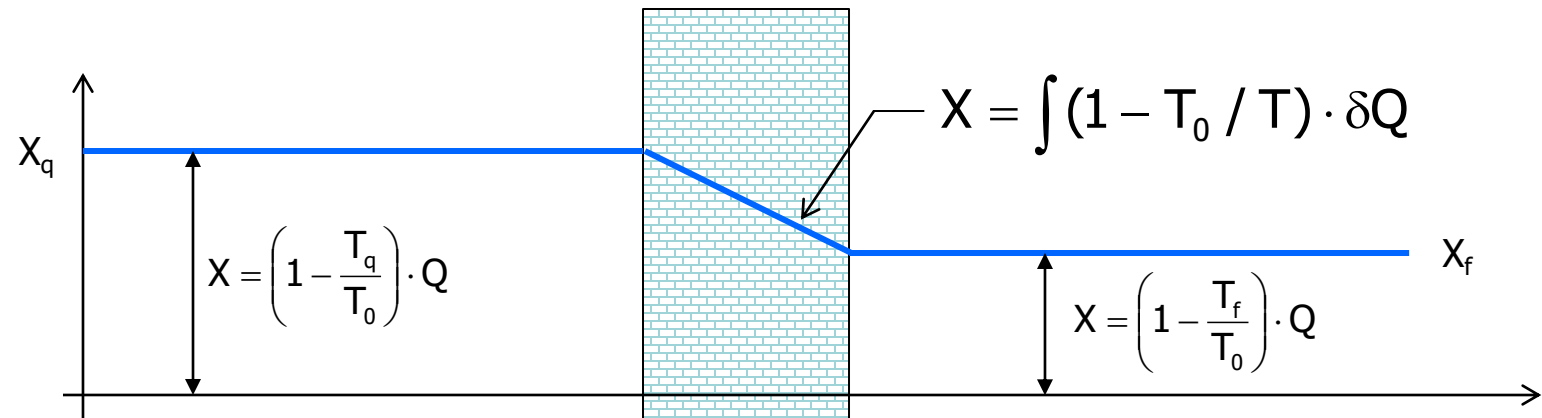








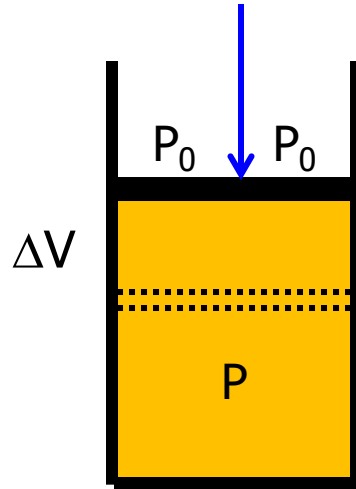




Exergy transfer through work...

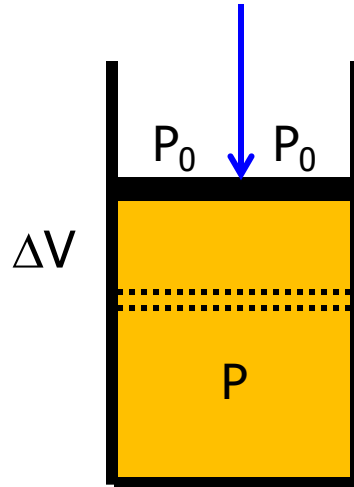


potential to generate useful work= exergy



$$X_{\text{work}} = W_{\text{boundary}} - W_{\text{neighborhood}}$$

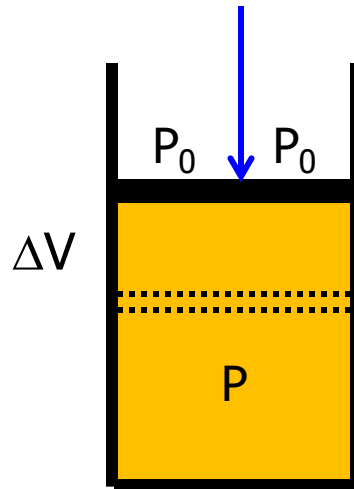
potential to generate useful work = exergy



$$X_{\text{work}} = W_{\text{boundary}} - W_{\text{neighborhood}}$$

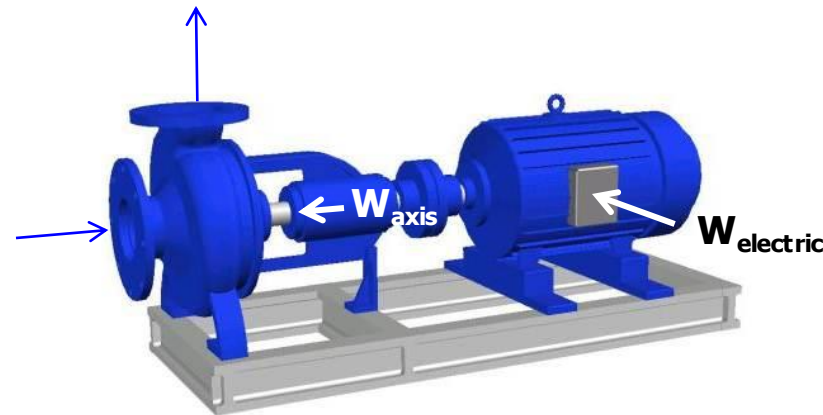
$\int P dV \quad \uparrow \quad \uparrow \quad P_0 \Delta V$

potential to generate useful work= exergy



$$X_{\text{work}} = W_{\text{boundary}} - W_{\text{neighborhood}}$$

$$\int P dV \quad \uparrow \quad \uparrow \quad P_0 \Delta V$$



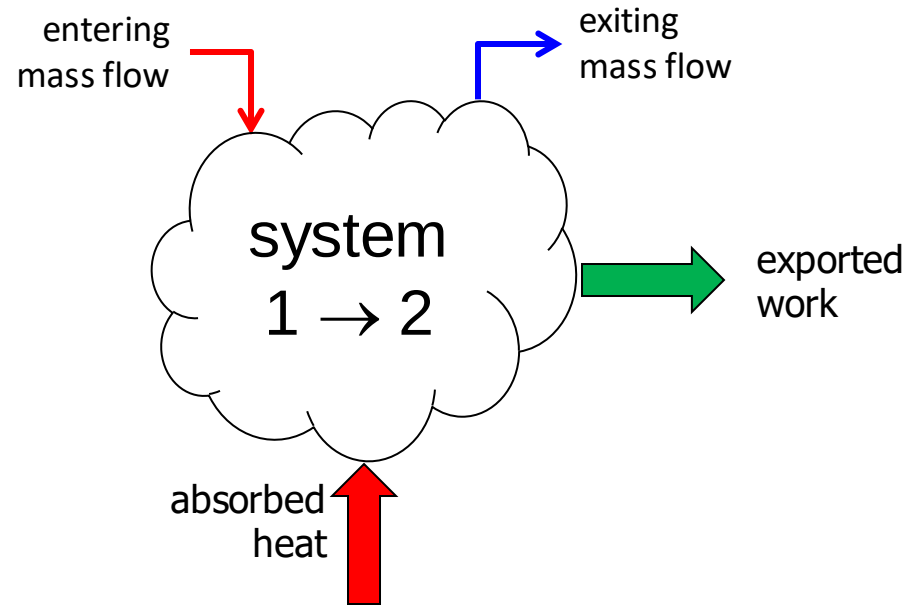
$$X_{\text{work}} = W_{\text{axis}}$$

$$X_{\text{work}} = W_{\text{electric}}$$

Exergy transfer through
mass flow...

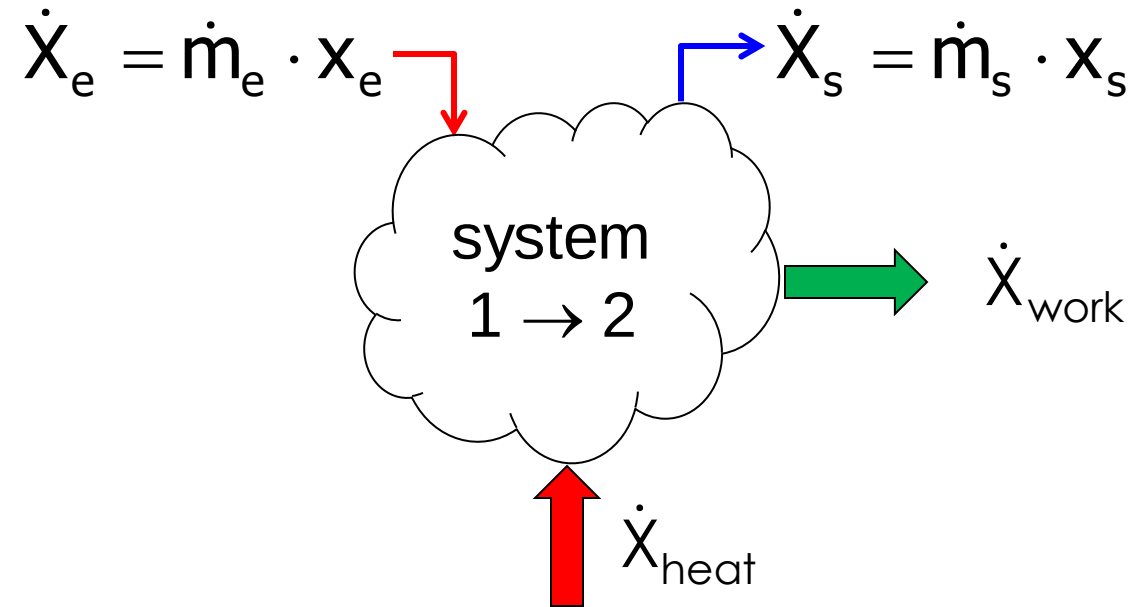


Mass contains exergy, energy, entropy, etc.



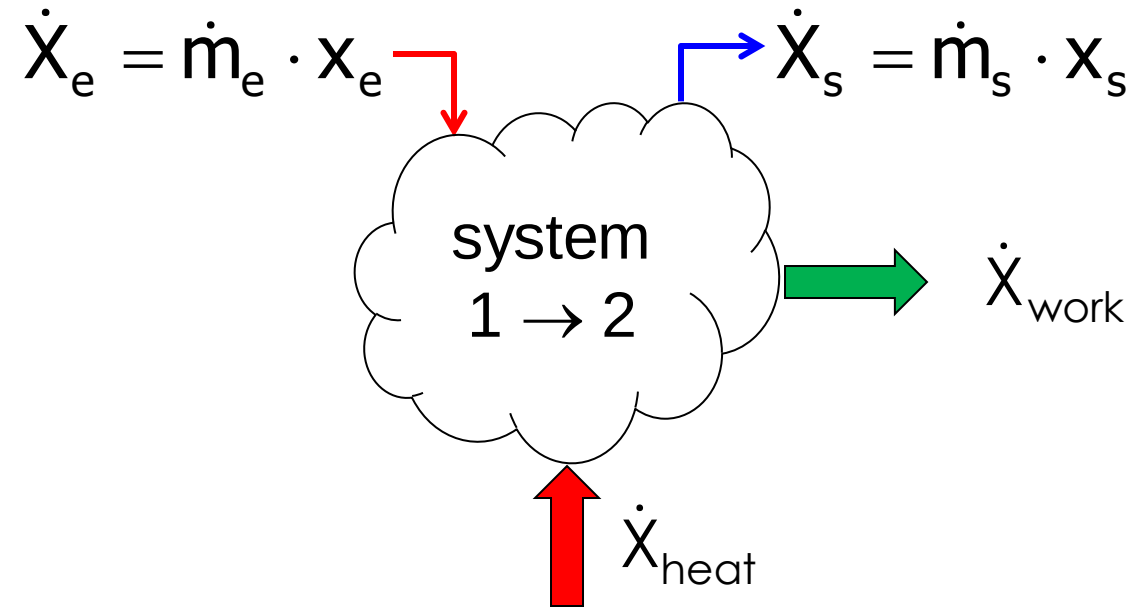
$$x = (h - h_0) - T_0(s - s_0) + ep + ec + eq$$

Mass contains exergy, energy, entropy, etc.



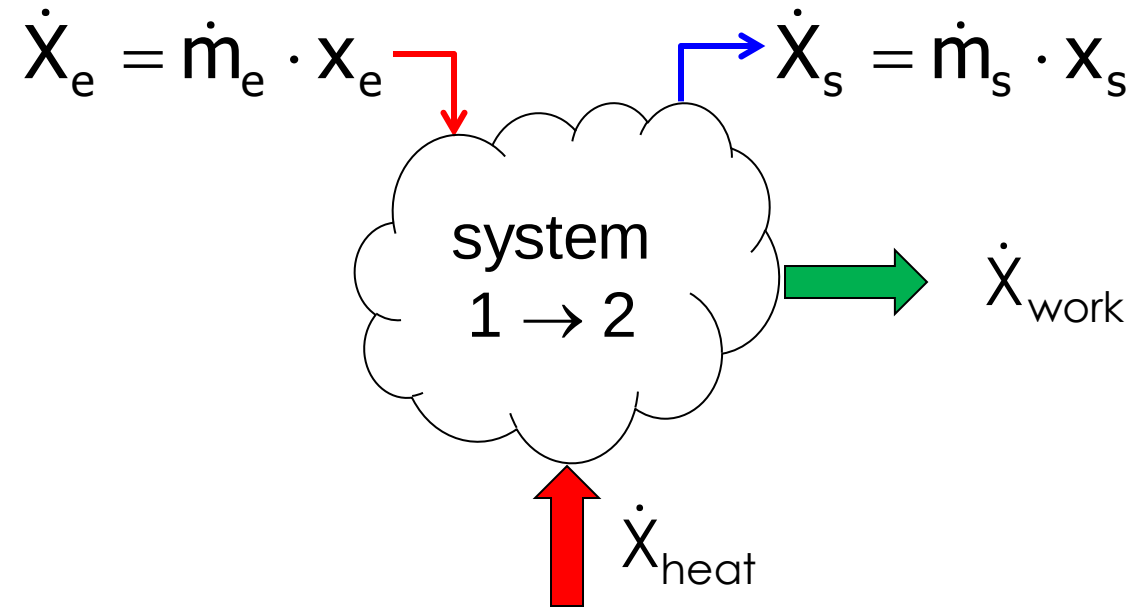
$$x = (h - h_0) - T_0(s - s_0) + ep + ec + eq$$

Mass contains exergy, energy, entropy, etc.



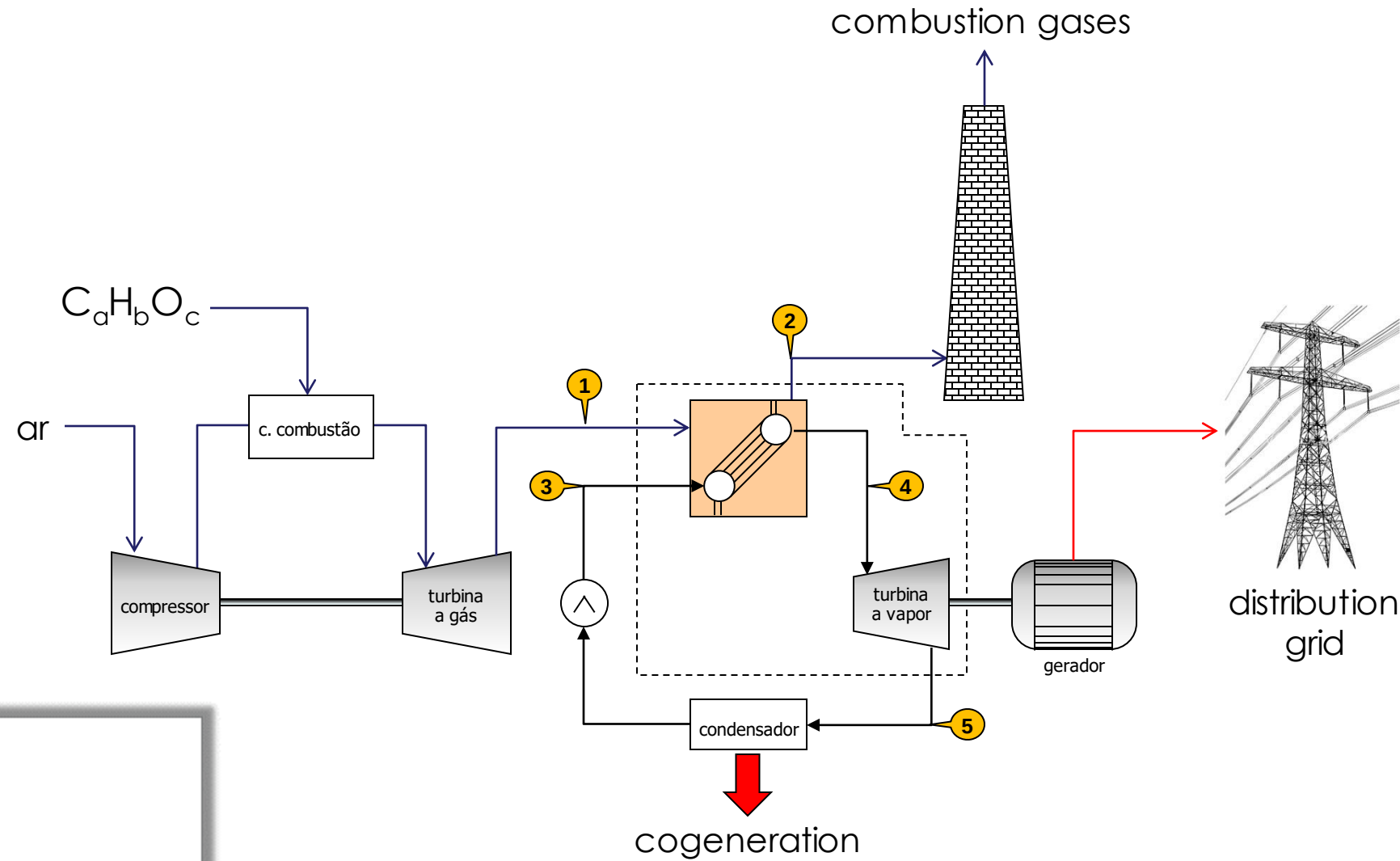
$$\dot{X}_{\text{heat}} - \dot{X}_{\text{work}} + \dot{X}_{e,\text{mflow}} - \dot{X}_{s,\text{mflow}} - \dot{X}_{\text{destroyed}} = dX_{\text{vc}} / dt$$

Mass contains exergy, energy, entropy, etc.



$$\sum \left(1 - \frac{T_0}{T_k} \right) \dot{Q}_k - \left(\dot{W} - P_0 \frac{dV_{vc}}{dt} \right) + \sum \dot{m}_e x_e - \sum \dot{m}_s x_s - \dot{X}_{\text{dest}} = \frac{dX_{vc}}{dt}$$

Exergetic analysis: combined cycle thermal power plant





Tutorial - Análise Exer... 

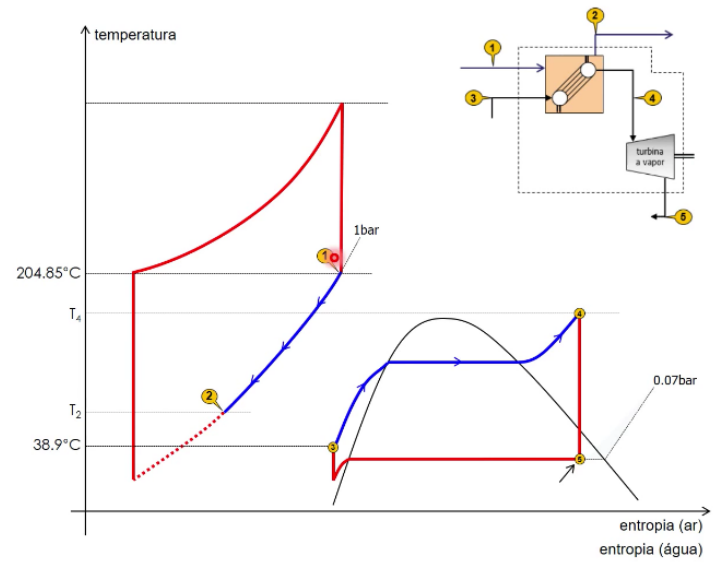
https://www.youtube.com/watch?v=TsIN7kNgx_s  Search      

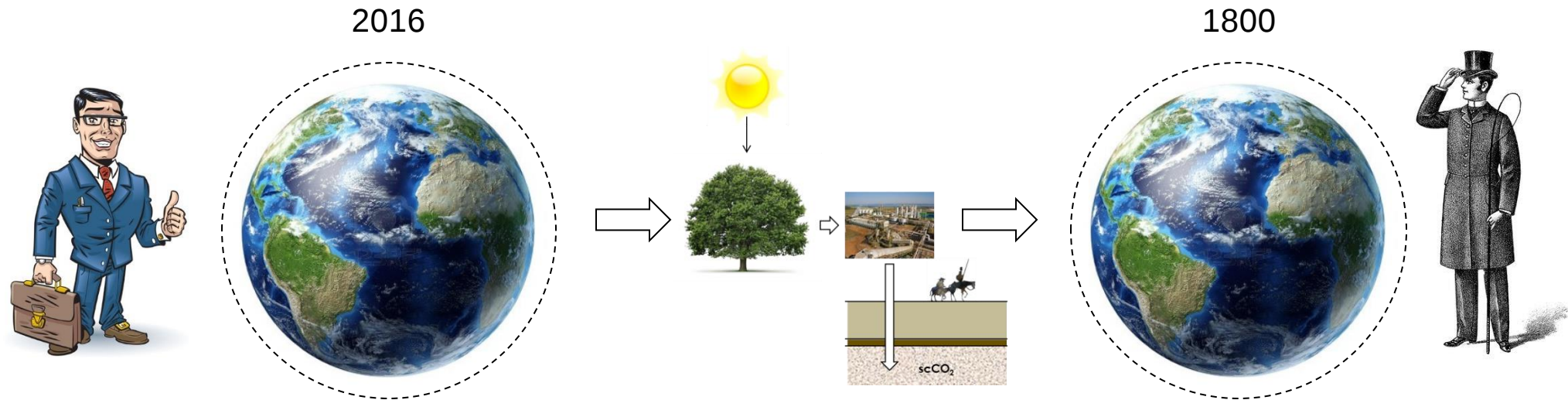
Gases de combustão (ar):
 $m = 69.78 \text{ kg/s}$
 $T_1 = 204.85^\circ\text{C}$
 $P_1 = 1 \text{ bar}$
 $P_2 = 1 \text{ bar}$

Fluido de trabalho (água):
 $m = 2.08 \text{ kg/s}$
 $T_3 = 38.9^\circ\text{C}$
 $P_3 = 2.75 \text{ bar}$
 $P_4 = 2.75 \text{ bar}$
 $P_5 = 0.07 \text{ bar}$
 $x_4 = 0.93 \text{ kg/kg}$

Caldeira regenerativa:
 $U = 2.5 \text{ kW/M}^2/\text{K}$
 $A = 40 \text{ m}^2$



Next classes: "Sun Powered CCS Industrial Plants"



How much exergy is necessary to reconstitute earth's atmosphere to its original constitution...
Exergetic analysis of separation processes...