# INF3580/4580 - Semantic Technologies - Spring 2018

Lecture 6: Introduction to Reasoning with RDF

Leif Harald Karlsen

20th February 2018



DEPARTMENT OF INFORMATICS



University of Oslo

# Mandatory exercises

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- Exercises mostly from this week's lecture, but one from next week's lecture, Reasoning with Jena.

# Today's Plan

Inference rules

2 RDFS Basics

Open world semantics

### Outline

- Inference rules
- 2 RDFS Basics

Open world semantics

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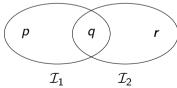
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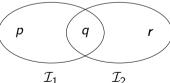


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  - this is not good.

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Syntactic reasoning easier to understand and use than model semantics

• we will show that first.

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Where  $\models$  is the entailment relation,  $\vdash$  is the inference relation. We write  $\Gamma \vdash P$  if we can deduce P from the assumptions  $\Gamma$ .

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- complete wrt the semantics, if (II) holds.

# Inference rules in propositional logic

(Part of) Natural dedcution calclulus for propositional logic:

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$$\frac{(A \wedge B)}{A} \wedge E_I \qquad \frac{(A \wedge B)}{B} \wedge E_r \qquad \frac{A}{(A \wedge B)} \wedge I$$

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may be read as an instruction;

• "If  $P_1, \ldots, P_n$  are all in the store, add P to the store."

### Outline

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- and (for our purposes) a subset of OWL.

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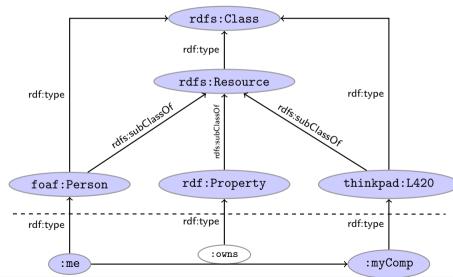
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  - rdfs:subClassOf: Class inclusion.
  - rdfs:subPropertyOf: Property inclusion.

### Example



#### Intuition: Classes as Sets

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| RDFS                  | Set Theory              |
|-----------------------|-------------------------|
| A rdf:type rdfs:Class | A is a set of resources |
| x rdf:type $A$        | $x \in A$               |
| A rdfs:subClassOf $B$ | $A\subseteq B$          |

RDFS supports three principal kinds of reasoning pattern:

I. Type propagation:

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  - "The 2CV is a car, and all cars are motorised vehicles, so..."
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  - "Steve lectures at Ifi, and anyone who does so is employed by Ifi, so. . . "

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# Set Theory Analogy

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A rdfs:subClassOf B . x rdf:type A . x rdf:type B . 
$$\underline{A \subseteq B \quad x \in A}$$

• Reflexivity of sub-class relation

$$A$$
 is a set  $A \subseteq A$ 

# Set Theory Analogy

Members of subclasses

$$A \subseteq B \qquad x \in A$$
$$x \in B$$

Reflexivity of sub-class relation

• Transitivity of sub-class relation

A rdfs:subClassOf B . B rdfs:subClassOf C . A rdfs:subClassOf C . 
$$\frac{A \subseteq B \quad B \subseteq C}{A \subset C}$$

## RDFS/RDF knowledge base:

ex:Vertebrate rdf:type rdfs:Class .

```
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(rdfs11)

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    ex:Mammal rdfs:subClassOf ex:Mammal . (rdfs10)
      (... and also for the other classes)
```

# A typical taxonomy

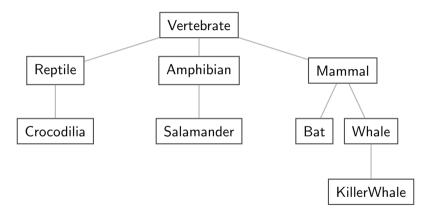


Figure: A typical taxonomy

• A set is a subset of many other sets:

$$\{2,3\} \subseteq \{1,2,3\} \quad \{2,3\} \subseteq \{2,3,4\} \quad \{2,3\} \subseteq \mathbb{N} \quad \{2,3\} \subseteq \mathbb{P}$$

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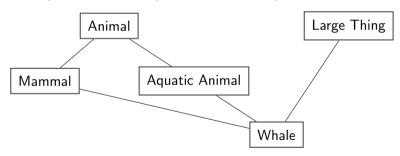
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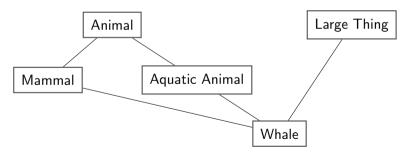


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• This is usually not called a *taxonomy*, but it's no problem for RDFS.

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| RDFS                              | Set Theory                   |
|-----------------------------------|------------------------------|
| r rdf:type rdf:Property           | r is a relation on resources |
| x r y                             | $\langle x,y \rangle \in r$  |
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And suppose we wish to integrate S and T under a common scheme,

for instance Dublin Core.

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```
:writer rdf:type rdf:Property .
:author rdf:type rdf:Property .
:author rdfs:subPropertyOf dcterms:creator .
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And Facts:
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    ex:hamsun :author ex:sult .
```

### Infer:

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- Legacy applications that use e.g. author can operate unmodified.

Large organizations (e.g. universities) offer different kinds of contracts;

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- :recSchol (receives scholarship from).

# Organising the properties

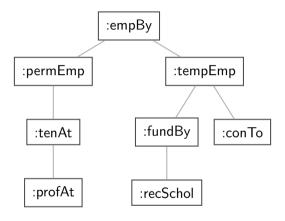


Figure: A hierarchy of employment relations

## Organising the properties

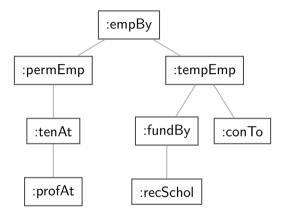


Figure: A hierarchy of employment relations

• Note: doesn't have to be tree-shaped.

## Querying the inferred model

#### Formalising the tree:

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:profAt rdf:type rdfs:Property .
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..... and so forth.
```

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#### Given a data set such as:

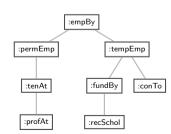
```
:Arild :profAt :UiO .

:Audun :fundBy :UiO .

:Steve :conTo :OLF .

:Trond :recSchol :BI .

:Jenny :tenAt :SSB .
```



#### cont.

#### We may now query on different levels of abstraction :

### Temporary employees

```
SELECT ?emp WHERE {?emp :tempEmp \_:x .} \rightarrow Audun, Steve, Trond
```

#### cont.

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→ Audun, Steve, Trond
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```

#### cont.

### We may now query on different levels of abstraction :

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```
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Arild, Jenny
```

#### All employees

```
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```

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Triggered by combinations of

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• rdfs:range

Triggered by combinations of

- rdfs:range
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  - therefore an application of p suffices to type that resource.

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- The *domain* of R is the set of all x with  $xR \cdots$ :

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• The range of R is the set of all y with  $\cdots R y$ :

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• Example:

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### Set intuitions for rdfs:domain and rdfs:range

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| Set Theory                        |
|-----------------------------------|
| $domr\subseteq A$                 |
| $\operatorname{rg} r \subseteq B$ |
|                                   |

## Set intuitions for rdfs:domain and rdfs:range

• If an rdfs:Class is like a set of resources and an rdf:Property is like a relation on resources...

| RDFS            | Set Theory                        |
|-----------------|-----------------------------------|
| r rdfs:domain A | $domr\subseteq A$                 |
| r rdfs:range B  | $\operatorname{rg} r \subseteq B$ |

Rules:

$$\frac{\text{dom } p \subseteq A \qquad \langle x, y \rangle \in p}{x \in A}$$

$$\frac{\text{rg } p \subseteq B \qquad \langle x, y \rangle \in p}{y \in B}$$

Suppose we have a class hierarchy that includes:

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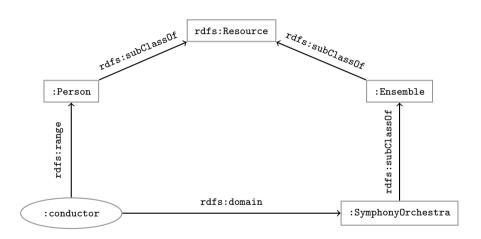
:conductor rdfs:range :Person .

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Suppose we have a class hierarchy that includes: :SymphonyOrchestra rdfs:subClassOf :Ensemble . and a property : conductor whose domain and range are: :conductor rdfs:domain :SymphonyOrchestra . :conductor rdfs:range :Person . Now, if we assert :OsloPhilharmonic :conductor :Petrenko . we may infer:

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Suppose we have a class hierarchy that includes:
    :SymphonyOrchestra rdfs:subClassOf :Ensemble .
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    :conductor rdfs:domain :SymphonyOrchestra .
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Now, if we assert
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we may infer:
    :OsloPhilharmonic rdf:type :SymphonyOrchestra .
    :OsloPhilharmonic rdf:type:Ensemble .
    :Petrenko rdf:type :Person .
```

#### Conductors and ensembles



#### Consider once more the dataset:

```
:Arild :profAt :UiO .
:Audun :fundBy :UiO .
:Steve :conTo :OLF .
:Trond :recSchol :BI .
:Jenny :tenAt :SSB .
```

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and suppose we wish to filter out everyone but the freelancers:

• State that only freelancers :conTo an organisation,

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```
:Freelancer rdf:type rdfs:Class .
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:Freelancer rdf:type rdfs:Class .
:conTo rdfs:domain :Freelancer .
```

## Finding the freelancers

The class of freelancers is generated by the rdfs2 rule,

```
:Steve :conTo rdfs:domain :Freelancer . :Steve :conTo :OLF . :Steve rdf:type :Freelancer
```

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## Finding the freelancers

The class of freelancers is generated by the rdfs2 rule,

```
:conTo rdfs:domain :Freelancer . :Steve :conTo :OLF . rdfs2
```

and may be used as a type in SPARQL (reasoner presupposed):

```
Finding the freelancers

SELECT ?freelancer WHERE {
    ?freelancer rdf:type :Freelancer .
}
```

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• Only classes have subclasses:

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• ... (another 30 or so)

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- In OWL, there are some simplification which make this superfluous.

## Writing proofs

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## Outline

1 Inference rules

2 RDFS Basics

Open world semantics

Recall that RDF Schema was conceived of as a schema language for RDF.

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```
\verb|:isRecordedBy rdfs:range : Orchestra|.\\
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This is the most important difference between relational DBs and RDF.

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  - For instance, the two triples

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• (It is not possible to in RDFS to say that ex: Smoker and ex:nonSmoker are disjoint).

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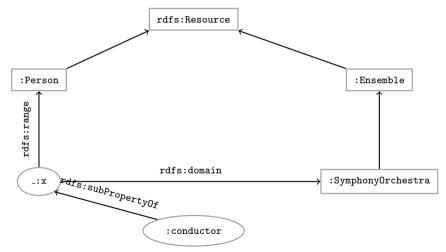
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### Therefore,

- RDFS supports no reasoning services that require consistency-checking.
- If consistency-checks are needed, one must turn to OWL.
- More about that in a few weeks.

## A conspicuous non-pattern

Suppose we elaborate on our music example in the following way:



#### That is:

- We make :conductor a subproperty of \_:x,
- \_:x is a generic relation between people and orchestras,
- to be used whenever we want the associated restrictions.

We would then want to be able to reason as follows (names abbreviated):

1 :Oslo :cond :Abadi . - P

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- 3 :Oslo \_:x :Abadi . − rdfs7, 1, 2
- 4 \_:x rdfs:domain :Person . P
- 3 :Abadi rdfs:type :Person . rdfs2, 3, 4

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### Nevertheless,

- this really is a semantically valid inference,
- thus the RDFS rules are incomplete wrt. RDFS semantics.
- There are also other cases where the RDFS rules are not sufficient for deriving all entailed triples (e.g. deriving domains and ranges), more on this in three weeks.

## Assessing the situation

RDFS reasoners usually implement only the standardised incomplete rules, so

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# Assessing the situation

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• they do not guarantee complete reasoning.

### Better therefore;

- if all you need is the three RDFS reasoning patterns,
- to use OWL and OWL reasoners instead.

### Unless, of course

- you need to talk about properties and classes as objects,
- that is, you need the meta-modelling facilities of RDFS,
- but people rarely do.

• We have seen that by modelling knowledge using the URIs in the RDF and RDFS vocabularies (e.g. rdf:type, rdfs:subClassOf, rdfs:range), the computer can derive new triples, that follows from our original triples.

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- OWL will also allow us to express more complex statements and use more complex types of reasoning.

That's it for today!

Remember the oblig!