



QFL5931/MPT6009 – Química Verde

Análise de Ciclo de Vida – Aula 2

Prof. Dr. Leandro H. Andrade (leandroh@iq.usp.br)

Prof. Dr. Reinaldo C. Bazito (bazito@iq.usp.br)

Prof. Dr. Renato S. Freire (rsfreire@iq.usp.br)

Estudo de Caso

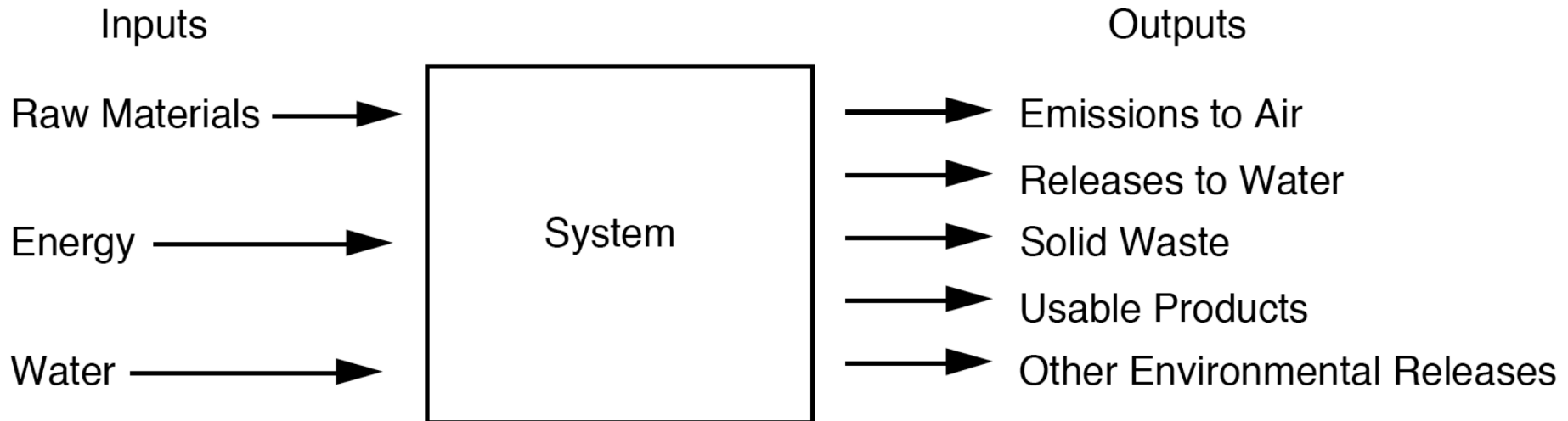
Saco de papel vs. Saco de Plástico



97

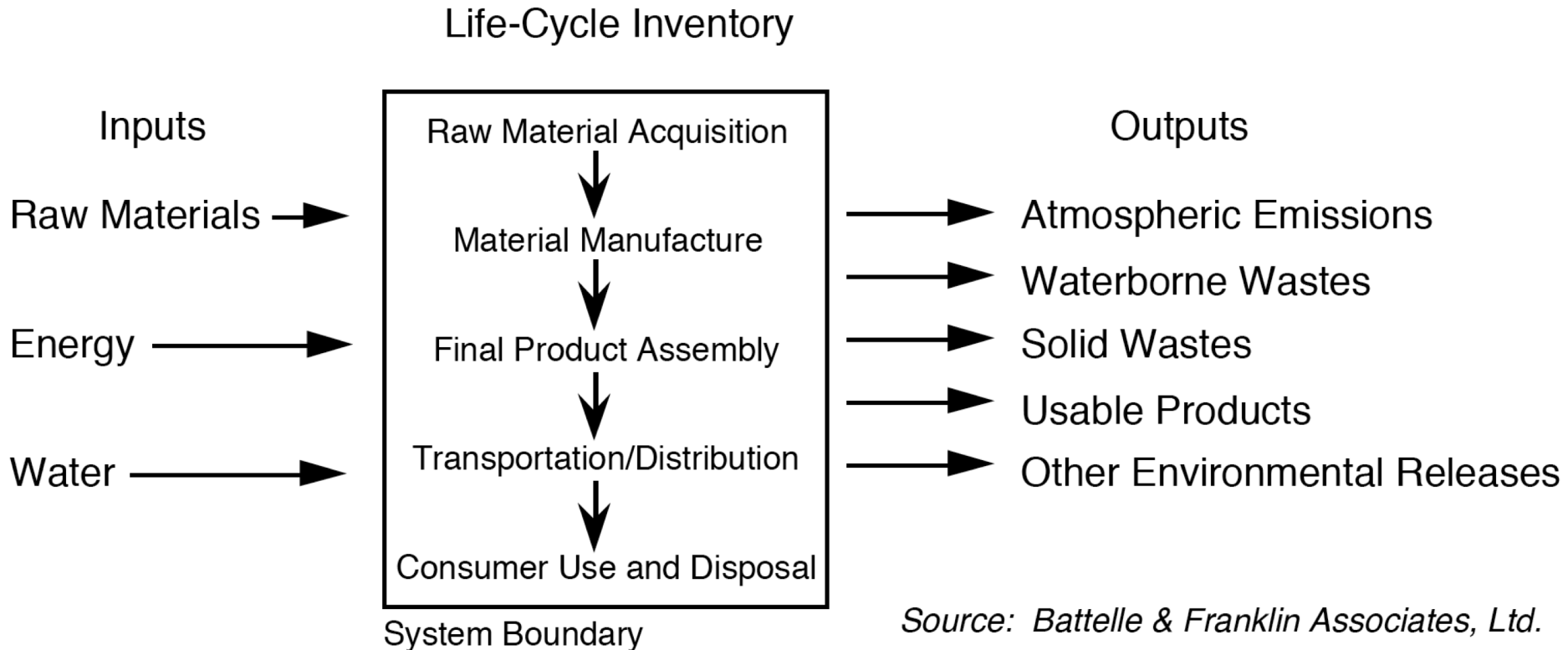
Análise de Inventário

Entradas e Saídas de um Sistema:



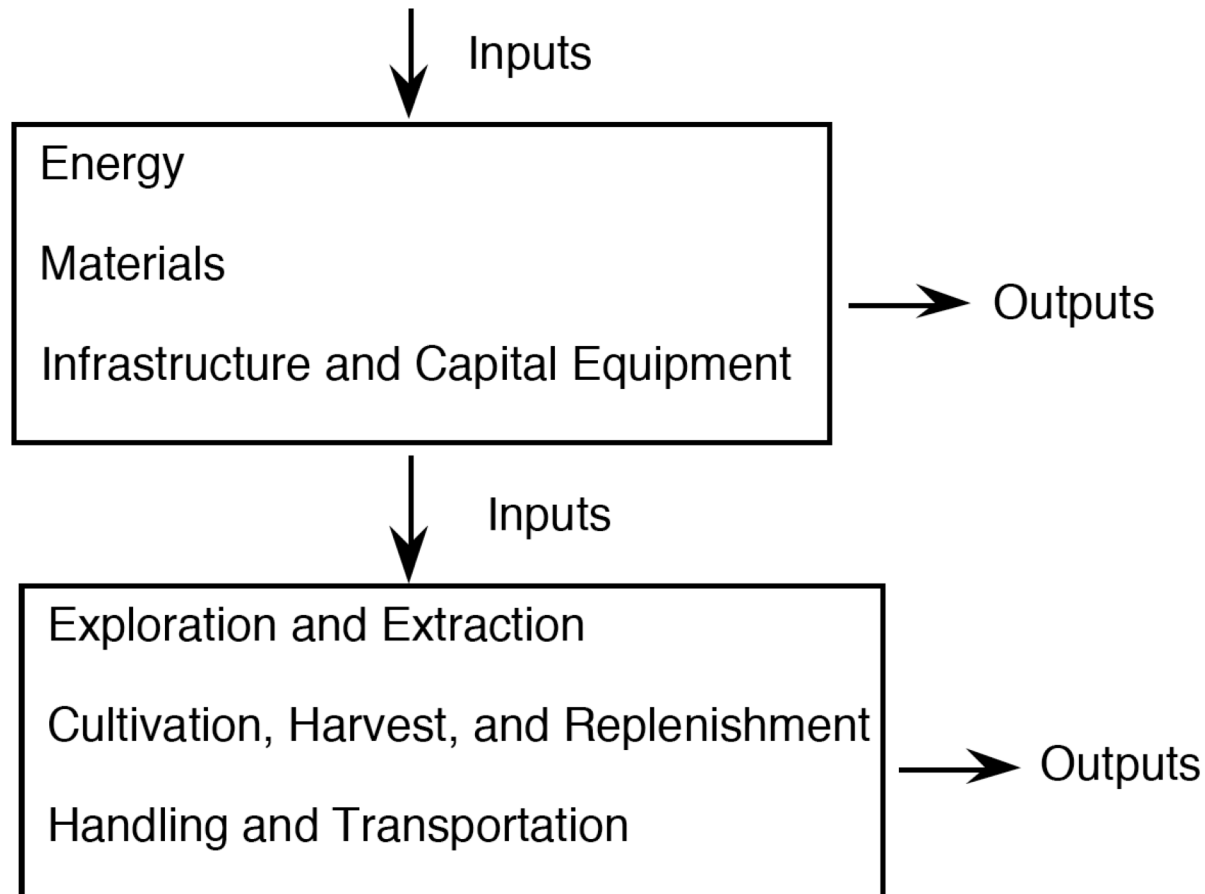
Análise de Inventário

Definindo as Fronteiras do Sistema:



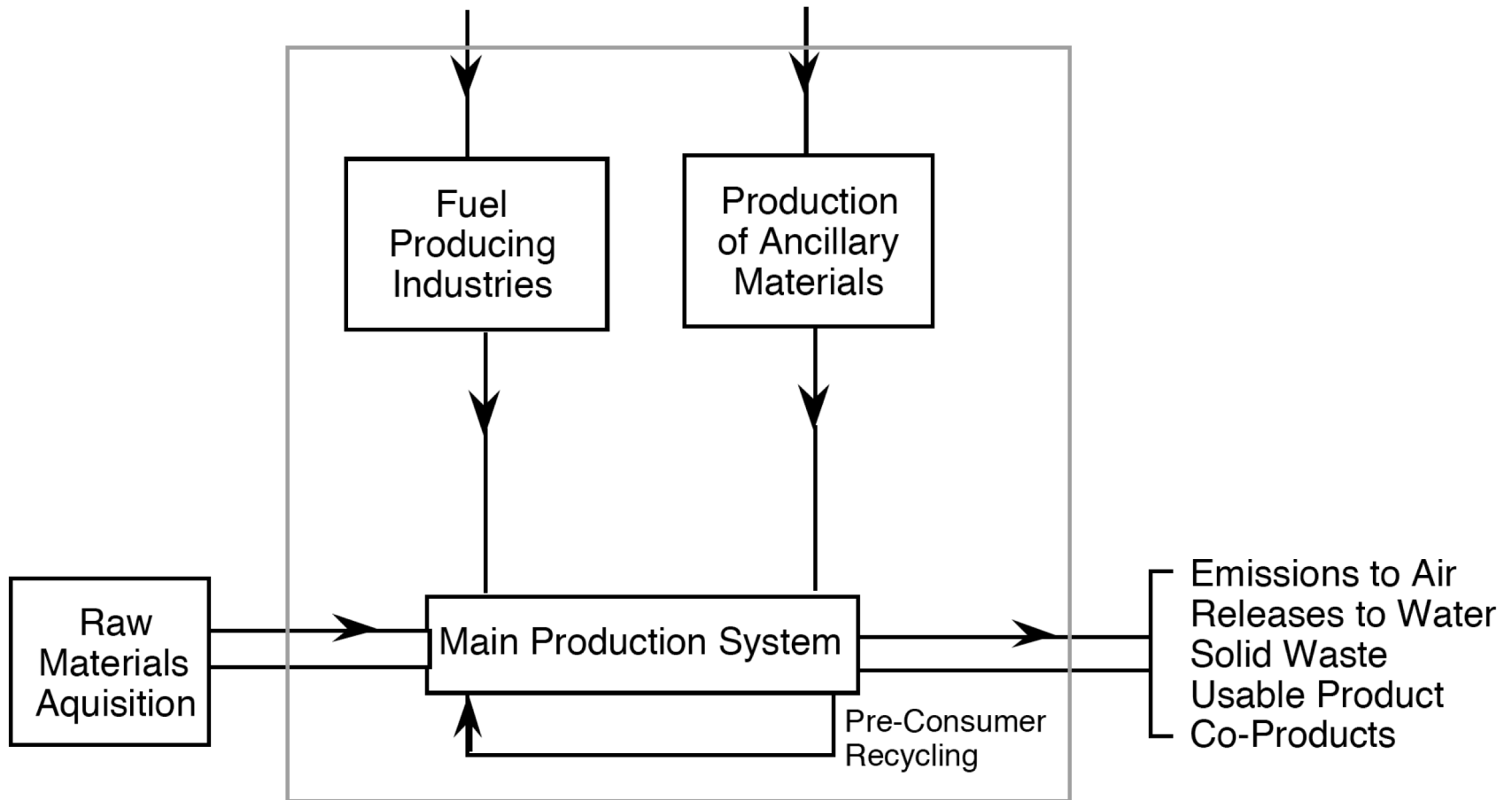
Análise de Inventário

Subsistema de Aquisição de Matéria-Prima:



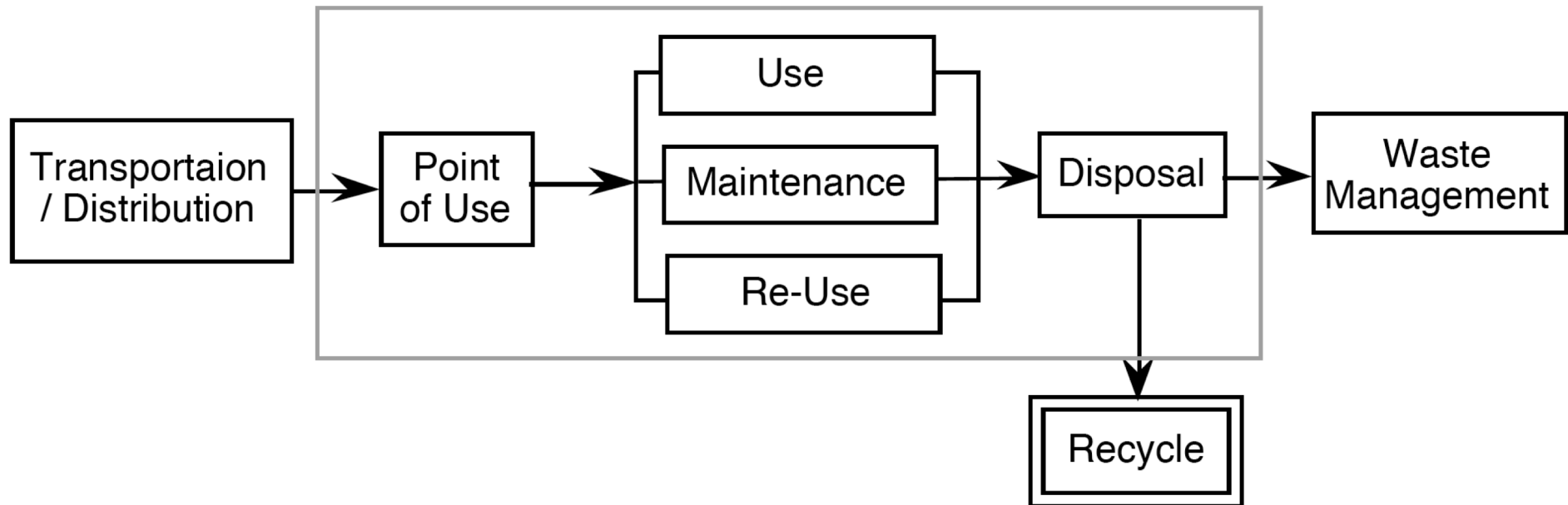
Análise de Inventário

Subsistema de Manufatura e Fabricação:



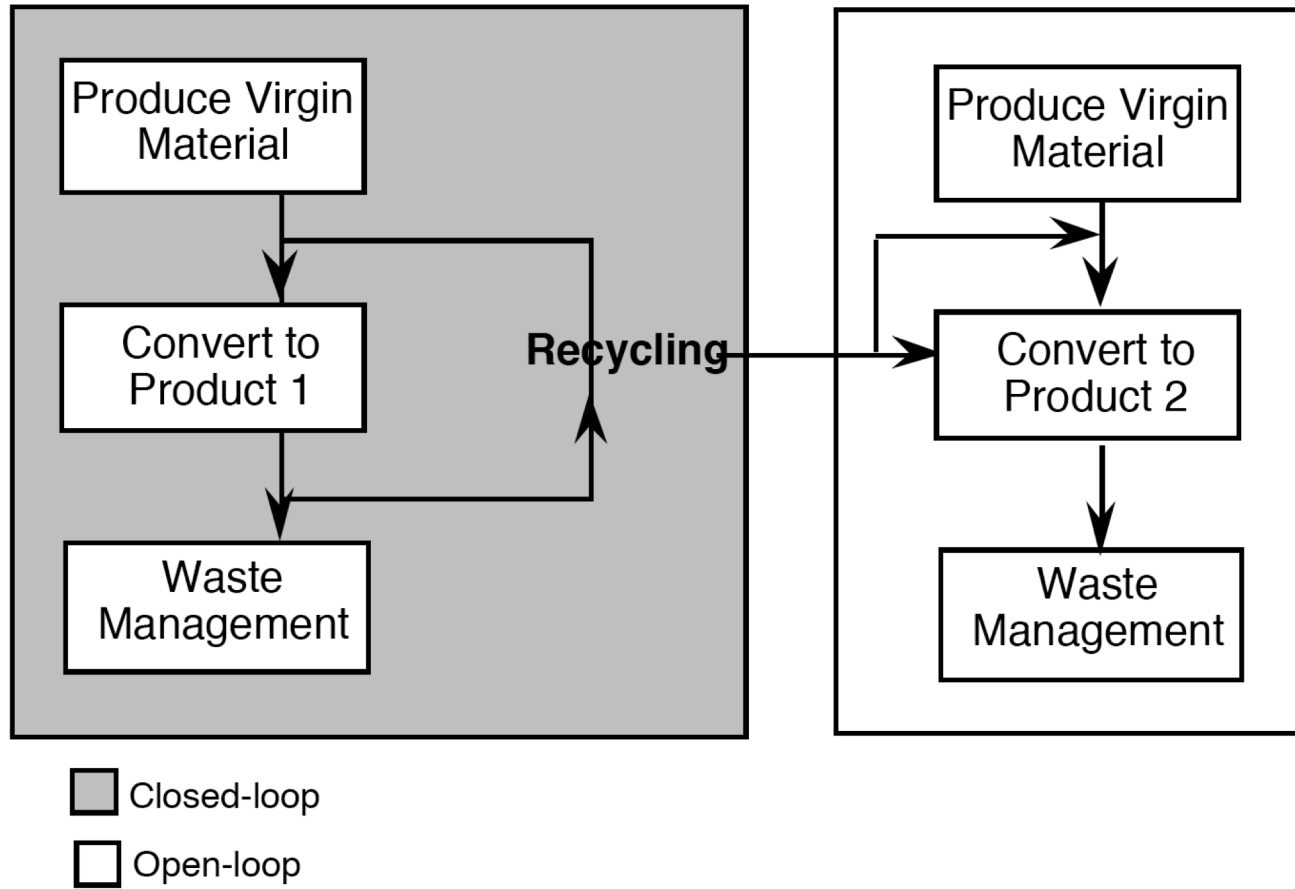
Análise de Inventário

Subsistema de Uso/Descarte pelo Consumidor:



Análise de Inventário

Subsistema de Reciclagem:



ACV em Química

- Escopo e Definição das Fronteiras do Sistema
- Impactos da Produção e Utilização
- Quantificação das Entradas e Saídas de Produtos Químicos/Reações
- Propriedades das “Entradas e Saídas” de Produtos Químicos/Reações
- “Economia” da Reação
- Requerimentos Regulatórios

Incorporation of Pollution Prevention Principles Into Chemical Science Education

[Jonathan W. Greene](#)

Center for Sustainable Systems – Umich

<http://www.umich.edu/~nppcpub/resources/compendia/CHEMpdfs/>

ACV em Química

Propriedades:

TABLE 4: Physical and Chemical Properties of Chemicals and Chemical Reactions

CHEMICALS

Form (solid/liquid/gas)

Density

Deactivation Rate (catalysts)

Melting Point

Boiling Point

Vapor Pressure

Lower Explosive Limit (LEL)

Upper Explosive Limit (UEL)

Speciation (ions, compounds, radicals)

Partition Coefficient (Log K_{OW})

Persistence (T_{1/2})

Water Solubility

Bioaccumulation Factor (chem.
concentraion in biota or water)

Freezing Point

CHEMICAL REACTIONS

Activation Energy (ΔH = exo/endermthermic)

Net Temperature

Net Pressure

pH

Reaction Time/Reactor Time

Selectivity

Atom Economy

Percent Conversion of Reactants

Reaction Yield

Batch/Continuous

ACV em Química

Propriedades:

TABLE 5: Health and Physical Hazards Associated with Chemicals (60)

PHYSICAL HAZARDS

Fire Hazards

combustible liquid

flammable aerosols

flammable gases

flammable liquids

flammable solids

oxidizers

pyrophoric materials

Other Physical Hazards

water reactive materials

compressed gases

explosives

shock-sensitive chemicals

heat-sensitive chemicals

unstable materials

HEALTH HAZARDS³

Acute

irritants G31

cutaneous hazards

toxic agents

highly toxic agents

eye hazards

blood/hematopoietic agents

Chronic

sensitizers

carcinogens

reproductive toxins

hepatotoxins

nephrotoxins

neurotoxins

pulmonary toxins

ACV em Química

Propriedades:

TABLE 6: Statutory Terminology that Applies to Chemicals and Reaction Residuals

<u>STATUTE</u>	<u>TERMINOLOGY</u>
Resource Conservation and Recovery Act	Hazardous Waste, Solid Waste
Atomic Energy Act	Nuclear Waste
Comprehensive Environmental Response, Compensation, and Liability Act	Hazardous Substance (reportable quantity chemicals, metals)
Clean Air Act	Hazardous Air Pollutants, Criteria Pollutants
Clean Water Act	Waste Water, Water Pollutants

ACV em Química

Propriedades:

TABLE 7: Renewable and Non-renewable Reaction Feedstock and Energy Sources (10)

	RENEWABLE	NON-RENEWABLE
FEEDSTOCKS	Biomass (agriculture-based, forests)	Petroleum, Minerals, Ores, & Metals
ENERGY	Solar Wind Geothermal Hydroelectric Biomass (e.g., wood, crop/animal wastes, or glucose-based ethanol / methanol fuels) Combustion of landfill methane Combustion of solid and hazardous wastes	Fossil Fuels Nuclear

ACV em Química

Propriedades:

TABLE 8: Ecological Impacts Associated with Renewable Feedstock and Energy Sources (10, 16)

CONSTRUCTION OF HYDROELECTRIC DAMS

- Loss of critical habitats and endangered flora and fauna, alteration of aquatic habitats
- Alteration in sediment and ground/surface water flows
- Displacement of human populations and loss of historical artifacts

BIO-BASED FUEL/FEEDSTOCK SOURCES

- Deforestation and land-clearing , topsoil erosion, loss of critical habitats & species diversity
- Surface and groundwater contamination from excessive pesticide and fertilizer applications

SOLAR POWER

- Hazardous materials (metals) utilized in batteries for long-term energy storage

HAZARDOUS AND SOLID WASTE COMBUSTION

- Air pollution associated with combustion and processing of fuels
 - Ash and other residual solid wastes have concentrated toxicity
 - Combustion and processing of inert materials may result in conversion to highly toxic species (i.e., dioxin and derivatives)
-

ACV em Química

“Economia” da Reação:

TABLE 9: Reaction Costing Framework Based on ABC/M and TCA Principles (14)

USUAL PRODUCTION COSTS

Capitol Costs

- Buildings
- Production Equip.
- Pollution Control Equip.

Production Costs

- Residual Mgmt. / Disposal
- Utilities
- Raw Materials
- Misc. Supplies
- Labor

Production Revenue

- Desired Rxn Product
- Rxn Co-products
- Recycled Residuals
- Managed Residuals

HIDDEN & LESS-TANGIBLE COSTS & BENEFITS

Capitol Costs

- Emission-monitoring equip.
- Safety/control technology
- Personal protective equip.

Expenses

- Closure/post-closure care
- Reporting & recordkeeping
- Monitoring/Testing
- Planning/studies/modeling
- Medical surveillance
- Worker Training
- Insurance and material use taxes
- Facility and product labeling
- Research and Development

Benefits

- Green marketing
- Corporate image
- Consumer loyalty

ACV em Química

“Economia” da Reação:

LIABILITY COSTS⁷

- Legal staff or consultants
- Penalties and fines
- Workplace injury
- Customer injury due to product malfunction (product liability lawsuits)
- Future liabilities from contamination of production and residual disposals
 - soil and waste removal , treatment
 - ground water removal and treatment
 - personal injury to surrounding community (health care, insurance ramifications)
 - economic loss, real property damage
 - natural resource damage
- Bans and taxes on chemicals and chemically based products
 - fines for non-compliance
 - capitol expenses for re-tooling of production equipment
 - research and development to identify alternatives

ACV em Química

Requerimentos Regulatórios:

TABLE 10: Federal Laws for Consideration in Chemical Production and Utilization (10, 14, 63)

<u>STATUTE</u>	<u>MEDIA/AREA OF REGULATION</u>
Clean Air Act ⁸	Air pollution discharges(point/non-point source; mobile/stationary sources)
Clean Water Act	Water pollution discharges (industrial, agricultural, municipal sources; stationary/mobile sources)
Safe Drinking Water Act	Sets health based standards for levels of contaminants in water delivered to users of public water supplies
Comprehensive Environmental Response, Compensation, and Liability Act	Allocates federal and state authority to clean up industrial sites contaminated with chemicals
Federal Insecticide, Fungicide, and Rodenticide Act	Regulates sale, labeling, and testing of pesticides, herbicides, fungicides, and rodenticides
Occupational Safety and Health Act	Regulates safety and health of workers in the occupational environment
Resource Conservation and Recovery Act	Generation, storage and disposal of solid and hazardous waste
Toxic Substances Control Act	Production, use, distribution of new chemicals into industrial and consumer markets
Mining Safety and Health Act	Regulates all aspects of mining activities in U.S.
Pollution Prevention Act	Establishes a national policy for P2
National Environmental Policy Act	Requires all applicable federally funded projects to undergo an environmental impact assessment prior to initiation

Estudo de Caso

Anticongelantes: etilenoglicol vs. propilenoglicol

<u><i>PG-BASED ANTIFREEZE</i></u>	<u><i>% OF TOTAL</i></u>
Water	3.20
Propylene Glycol	94.00
Sodium Hydroxide	0.20
Sodium Nitrate	0.30
Sodium Silicate	0.29
Sodium Tetraborate	2.01

<u><i>EG-BASED ANTIFREEZE</i></u>	<u><i>% OF TOTAL</i></u>
Water	2.20
Ethylene Glycol	96.20
Sodium Hydroxide	0.22
Sodium Nitrate	0.15
Sodium Silicate	0.23
Sodium Tetraborate	0.70
Sodium Orthophosphate	0.30

Incorporation of Pollution Prevention Principles Into Chemical Science Education

[Jonathan W. Greene](#)

Center for Sustainable Systems - UMich

<http://www.umich.edu/~nppcpub/resources/compendia/CHEMpdfs/>

Escopo: EUA

PG PRODUCTION	Hydrolysis of Propylene Oxide (PO) in Water
EG PRODUCTION	Hydrolysis of Ethylene Oxide (EO) in Water
PO PRODUCTION	Weighted Average of Chlorohydrination, Isobutane Hydroperoxidation, and Ethylbenzene Hydroperoxidation
EO PRODUCTION	Catalytic Oxidation of Ethylene

Figure 4: Summary of Production Processes of EG- and PG-Based Antifreeze Solutions

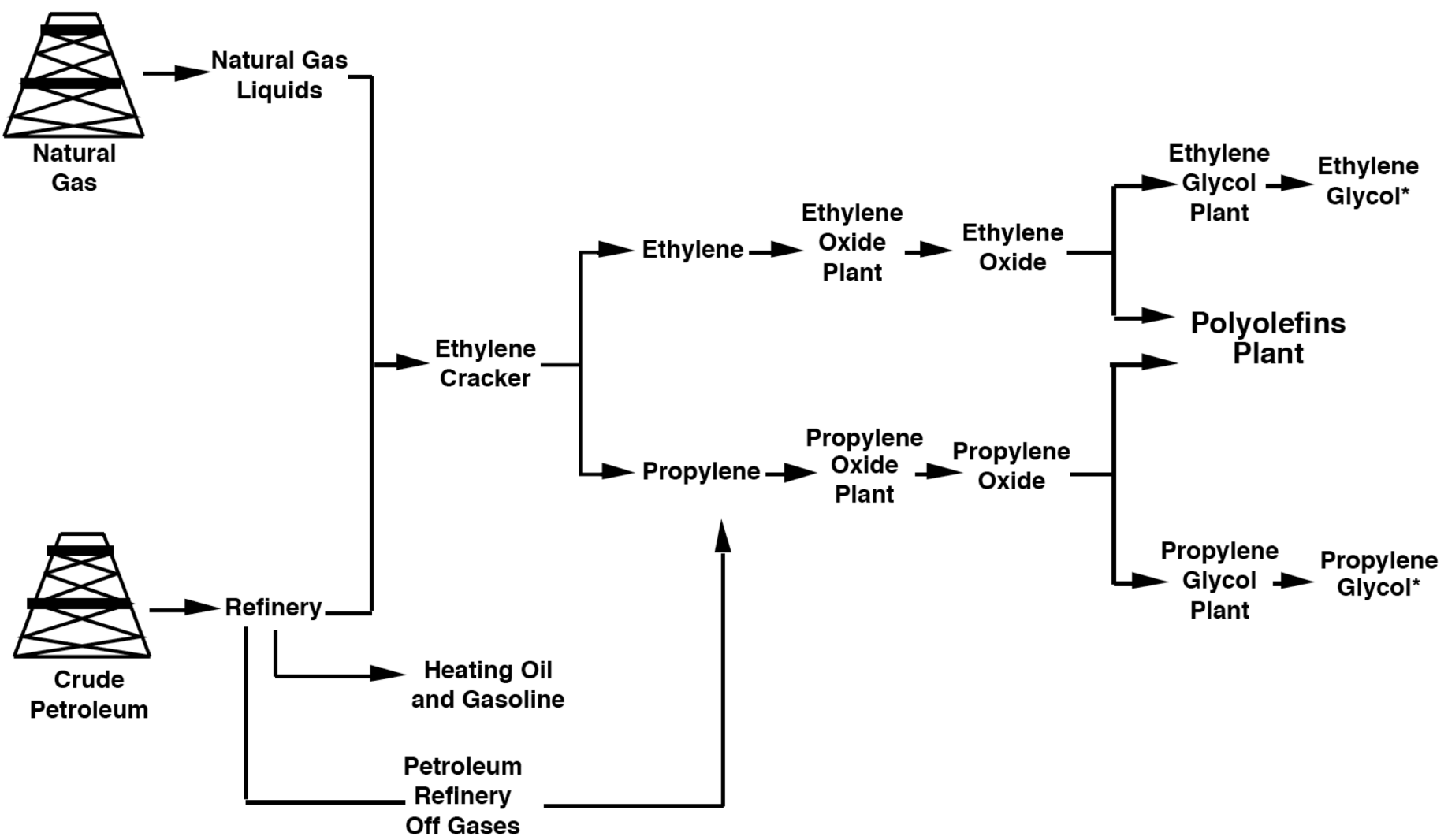


TABLE 11: Component Weights for EG- and PG-based Antifreeze Product and Packaging System (55)

	EG (lbs/10 ³ gallons)	PG (lbs/10 ³ gallons)
<i>Feedstocks and other Reaction Inputs</i>		
Ethylene	14,590.00 to 31,265.00	—
Ethylene Oxide	2,751.00	—
Silver Catalyst	n/a	—
Molydenum Catalyst	—	n/a
Isobutane	—	34,394.00
tert-butyl hydroperoxide	—	6,405.00
Propylene Oxide	—	3,241.00
Propylene	—	29,891.00
Methyl Tert-butyl Ether (co-product)	—	n/a
<i>Antifreeze Product</i>		
Ethylene Glycol	4,274.00	—
Propylene Glycol	—	4,316.00
Sodium Tetraborate	31.10	92.80
Sodium Silicate	10.20	13.30
Sodium Nitrate	6.70	13.80
Sodium Orthophosphate	13.30	—
Sodium Hydroxide	9.80	9.60
Water	95.90	147.00
<i>Water Added by Consumer</i>	4,442.00	4,072.00
<i>Primary Packaging</i>		
HDPE Containers	162.00	171.80
Polypropylene Cap	5.10	5.37
Bleached Paperboard Cap Liner	0.77	0.80
Aluminum Foil & HDPE Film Safety Seal	0.11	0.12
<i>Tertiary Packaging</i>		
Corrugated Cardboard	166.60	176.20
LDPE Stretchwrap	2.00	2.10

TABLE 12: Energy (Btu) Requirements for Production and Utilization of 1,000 gallons of EG- and PG-Based Antifreeze Solutions (55)

	Process	Transportation	Material Resource	WTE Credit	Total
EG	63.2	3.9	65.9	(4.6)	128.5
PG	119.6	5.7	69.0	(4.6)	189.7

TABLE 13: Energy (Btu) Requirements for Components of EG- and PG-Based Antifreeze Product and Packaging Systems (55)

	EG Energy	% Total	PG Energy	% Total
Glycol Production	114.6 Btu	86.1	175.2 Btu	90.2
Formulation Chemicals	0.5	0.3	0.8	0.4
Antifreeze Formulation	5.4	4.0	5.0	2.6
Primary Packaging	6.5	4.9	6.9	3.6
Tertiary Packaging	2.6	2.0	2.8	1.4
Disposition	3.5	2.7	3.6	1.8
Total	133.1 Btu		194.2 Btu	

Note: • All numbers expressed in terms of 10⁶ Btu
• Dilution ratios are 50% water / 50% EG product, 47% water / 53% PG product

TABLE 14: Energy Sources Associated with Production and Utilization of 1,000 Gallons of EG- and PG-Based Antifreeze Solutions (56)

	Natural Gas	Oil	Coal	Hydro	Nuclear	Wood	Other	Total
EG	86.6	29.8	10.8	0.61	4.3	0.96	0.074	133.1 Btu
PG	113.8	44.7	24.5	1.25	8.8	1.02	0.15	194.2 Btu

Note:

- All numbers expressed in terms of 10⁶ Btu
- Dilution ratios are 50% water / 50% EG product, 47% water / 53% PG product
- Data account for portion of electricity generated at manufacturing facilities & sold to grid

TABLE 15: Solid Waste Associated with Production and Utilization of 1,000 Gallons of EG- and PG-Based Antifreeze Solutions (56)

	<i>Industrial Solid Waste</i>		<i>Fuel</i>		<i>Post-Consumer Solid Waste</i>		<i>Total Solid Waste</i>	
	<i>Process</i>							
	(lbs)	(ft ³)	(lbs)	(ft ³)	(lbs)	(ft ³)	(lbs)	(ft ³)
EG	95	1.9	388	7.8	232	13.9	715	23.6
PG	346	6.9	831	16.6	246	14.7	1424	38.3

NOTE:

- Dilution ratios are 50% water / 50% EG product, 47% water / 53% PG product
- 55% of corrugated containers are recycled; 19% of unrecycled packaging materials are combusted and 81% landfilled
- 94% of combustion of unrecyclable solid waste occurs at WTE facilities
- Data accounts for hazardous waste production but does not identify quantities

TABLE 16: Industrial Atmospheric Emissions Associated with Production of 1,000 Gallons of EG- and PG-Based Antifreeze Solutions⁸ (55)

	<i>Process EG (lbs.)</i>	<i>Process PG (lbs.)</i>	<i>Fuel EG (lbs.)</i>	<i>Fuel PG (lbs.)</i>	<i>Total EG (lbs.)</i>	<i>Total PG (lbs.)</i>
acid	—	0.2	—	—	—	0.2
aldehydes *	0.033	0.034	0.26	0.035	0.29	0.39
ammonia	0.015	0.23	0.035	0.068	0.05	0.3
carbon dioxide *	2186	739	9313	17,609	11,499	18,348
carbon monoxide *	1.04	1.09	17.4	26.9	18.5	28
chlorine * ^	8.7E-05	0.0052	—	—	8.7E-05	0.0052
ethylbenzene	—	4.2	—	—	—	4.2
ethylene glycol #	7.29	—	—	—	7.29	—
ethylene oxide #	1.31	—	—	—	1.31	—
hydrocarbons	73.8	92.5	38	66.2	112	159
hydrogen fluoride	1.5E-04	1.6E-04	—	—	1.5E-04	1.6E-04
isobutane	—	6.75	—	—	—	6.75
kerosene *	—	—	8.87E-04	0.0018	8.8E-04	0.0018
lead ^	0.0012	0.0013	2.7E-04	5.1E-04	0.0015	0.0018
mercury * ^	3.7E-06	0.0014	—	—	3.7E-06	0.0014
methane	2.09	—	0.11	0.19	2.19	0.19
nitrogen oxides *	3.42	3.59	37.8	69.7	41.2	73.3
odorous sulfur	0.0051	0.054	—	—	0.0051	0.0054
other organics *	0.072	0.073	3.09	3.25	3.16	3.33
particulates *	1.45	1.39	11.5	25.4	13.0	26.8
propylene \$	—	0.92	—	—	—	0.92
propylene chlorohydrin\$	—	0.034	—	—	—	0.034
propylene oxide \$	—	2.07	—	—	—	2.07
sulfur oxides *	4.17	4.37	30.7	66.9	34.8	71.3

* Emission results from acquisition and fuel combustion; mat’ls w/o designation were process-related wastes

^ Emission results from production of sodium hydroxide and chlorine utilized in paper manufacturing

Emission results from EG process only

\$ Emission results from PG process only

TABLE 17: Industrial Waterborne Emissions Associated with Production of 1,000 Gallons of EG- and PG-Based Antifreeze Solutions (55)

	<i>Process EG (lbs.)</i>	<i>Process PG (lbs.)</i>	<i>Fuel EG (lbs.)</i>	<i>Fuel PG (lbs.)</i>	<i>Total EG (lbs.)</i>	<i>Total PG (lbs.)</i>
acid*	0.37 lbs	44.2 lbs	2.03 lbs	4.53 lbs	2.40 lbs	48.7 lbs
ammonia	0.0015	0.0016	–	–	0.0015	0.0016
biological oxygen demand	0.56	0.59	0.035	0.068	0.60	0.66
chromium	1.4E-04	1.5E-04	–	–	1.4E-04	1.5E-04
chemical oxygen demand	0.63	0.66	0.098	0.19	0.73	0.85
cyanide	1.6E-06	1.6E-06	–	–	1.6E-06	1.6E-06
dissolved solids *	9.56	19.6	13.9	25	23.5	44.6
fluorides	8.5E-05	9.0E-05	–	–	8.5E-05	9.0E-05
herbicides !	1.7E05	1.8E-05	–	–	1.7E-05	1.8E-05
hydrocarbons ##	–	4.07	–	–	–	4.07
iron *	4.1E-06	4.4E-06	1.6	3.3	1.6	3.30
lead ^	5.5E-09	2.1E-06	–	–	5.5E-09	2.1E-06
mercury ^	1.0E-08	3.8E-06	–	–	1.0E-08	3.8E-06
metal ion *	3.5E-05	3.8E-05	0.51	1.14	0.51	1.14
nickel	5.5E-09	2.1E-06	–	–	5.5E-09	2.1E-06
nitrogen !	0.002	0.002	–	–	0.0020	0.0021
oil	0.23	0.024	0.018	0.034	0.25	0.27
pesticide !	8.6E-06	9.1E-06	–	–	8.6E-06	9.1E-06
phenol*	7.7E-05	5.87	0.0089	0.017	0.0089	5.89
phosphates	0.019	0.02	–	–	0.019	0.020
sodium hydroxide	–	6.27	–	–	–	6.27
sulfides	0.17	0.18	0.0089	0.017	0.18	0.19
sulfuric acid *	–	–	0.019	0.039	0.019	0.039
suspended solids	2.26	0.75	0.053	0.1	2.31	0.85
zinc	0.0031	0.0032	–	–	0.0031	0.0032

Figure 5: Post-Production End Use, Waste Management, and Recycling Scenarios for EG- and PG-Based Spent Antifreeze Solutions

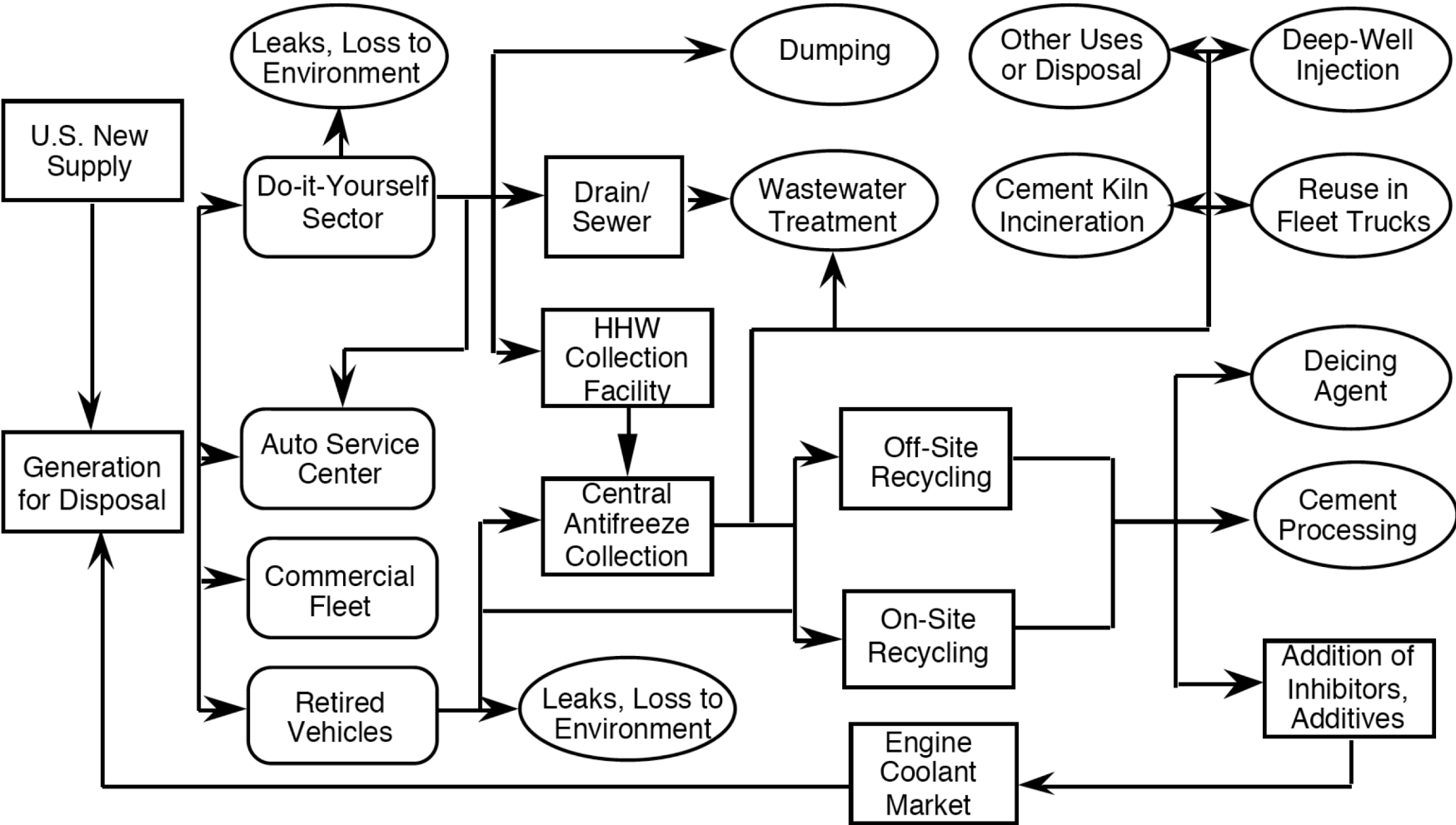


TABLE 18: Waterborne Wastes Generated by Improper Disposal of 1,000 gallons of EG- and PG-Based Antifreeze Solutions (55)

	lbs. EG*	lbs. PG*	lbs. PG**
Ethylene Glycol	1,665.000	0	0
Propylene Glycol	0	1,586.000	1,681.000
Sodium Hydroxide	3.810	3.540	3.710
Sodium Nitrate	2.420	5.060	5.400
Sodium Orthophosphate	5.190	0	0
Sodium Silicate	3.810	4.900	5.060
Sodium Tetraborate	12.100	34.100	36.100
Lead***	0.016	0.016	0.016
TOTAL	<u>1692.340</u>	<u>1,633.620</u>	<u>1,731.270</u>

Note: * Dilution ratio is 50% antifreeze product / 50% water
** Dilution ratio is 53% antifreeze product / 46% water
*** Lead is not present if antifreeze product is dumped in unused form

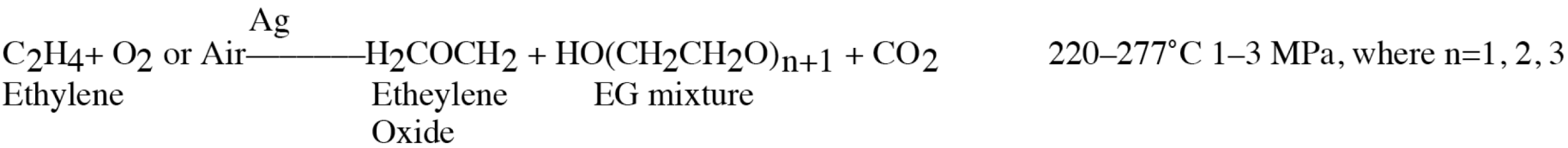
**TABLE 19: Physical and Chemical Properties of Feedstock Chemicals
 Used in Production of EG- and PG-Based Antifreeze Products
 (66, 67, 68, 69, 71)**

	<i>EG</i>	<i>PG</i>	<i>EO</i>	<i>PO</i>	<i>TBH</i>
<hr/>					
<i>REACTION PROPERTIES</i>					
Rxn Temperature (°C)	200	125–200	220–275	110–120	120–140
Rxn Pressure (MPa)	n/a	2	1–2.2	4	3.63–5.0
% Feedstock Conversion	n/a	n/a	7–15	98 (9%/pass)	48
% Selectivity	90	~ 90	80	80	50
<i>PRODUCT PROPERTIES</i>					
Boiling Point@101.3 kPa (°C)	197.6, 107*	187.9, 104.5*	10.8	34.23	n/a
Freezing Point (°C)*	-36.67	-33.33	n/a	n/a	n/a
Vapor Pressure (Pa)	300@65°C	11@20°C	145.6@20°C	58.8@20°C	n/a
LEL (vol %)	3.20	2.6	2.6	2.3	n/a
UEL (vol %)	53	n/a	100	36	n/a
Ignition Temperature (°C)	410	410	429	430	n/a
Flash Point (°C)	111	103	n/a	-37	n/a
<hr/>					

TABLE 20: Toxicity and Adverse Health Effects Associated With EG, PG, EO, and PO (66, 67, 68,69, 71)

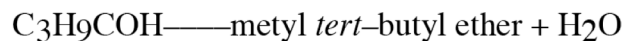
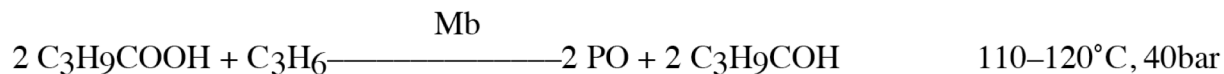
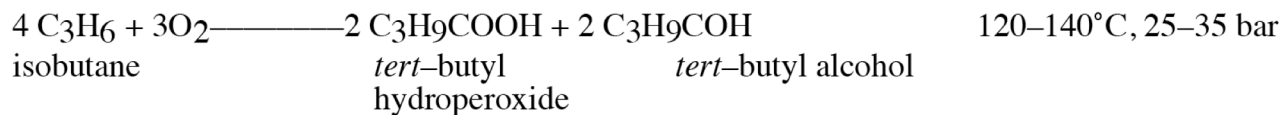
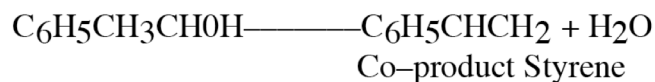
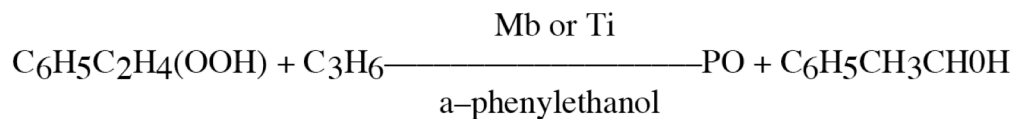
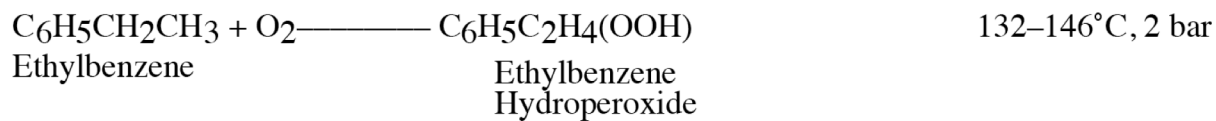
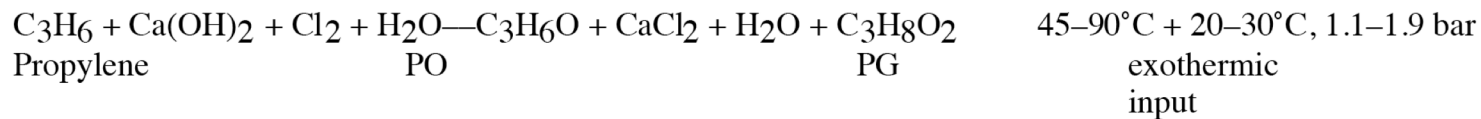
	EG	PG	EO	PO
Acute Health Effects	narcosis, kidney damage	little to none	headaches, nausea, vomiting, numbness	headache, skin and respiratory irritation
Acute Oral Toxicity (LD50)	1.56 g/Kg (adult)	20 g/Kg	0.33 g/Kg (adult)	300–1000 g/Kg (rats) (rats)
Chronic Health Effects	kidney damage	none reported	sensory-motor neuropathy	CNS depression
Lethal Dose (Adult)	0.1 L	1 L	n/a	n/a
Evidence of Teratogenicity	yes (mice, rats)	none reported (mice, rats, rabbits)	none reported in rats	none reported
Evidence of Carcinogenicity	none reported	none reported	yes\$	yes#

ETHYLENE GLYCOL



Detalhes - Reações

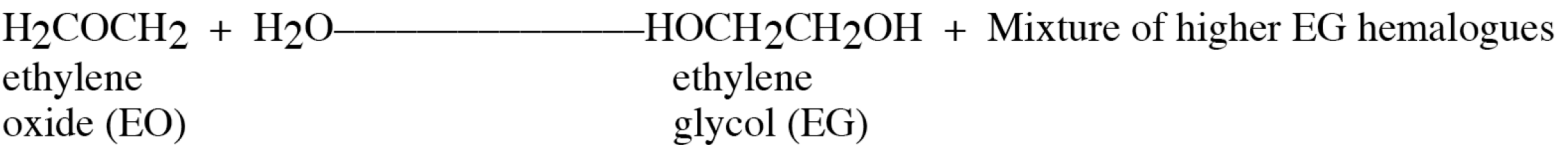
PROPYLENE GLYCOL



*15 molar excess of water produces mono, di-, and tri- PG in ratio of 100:10:1

ETHYLENE GLYCOL

- (1) Assumptions:
- 3,877 g (62.53 mols) of EG is goal based on FAL data
 - EG selectivity is 90%, 100% conversion of feedstocks



62.53 mols PO x 44 g/mol = 2751 g PO

- (2) Assumption:
- Oxidation with pure oxygen
 - 7% to 15% conversion of ethylene
 - 80% selectivity for PO

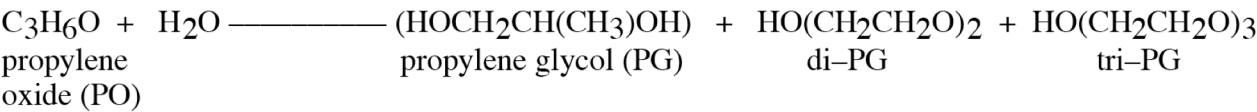


62.53 mols ethylene x 1/0.80 x 1/0.07 x 28 g ethylene/mol = **31,265 g ethylene @ 7% conversion**
62.53 mols ethylene x 1/0.80 x 1/0.15 x 28 g ethylene/mol = 14,590 g ethylene @ 15% conversion

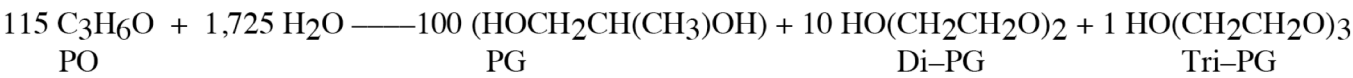
Detalhes -
Reações -
Estequiometria

PROPYLENE GLYCOL

- (1) Assumptions:
- 3694 g of PG is goal based on FAL data
 - isobutane hydroperoxidation is the production process
 - 15 molar excess of water produces mono, di, and tri PGs in a ratio of 100:10:1

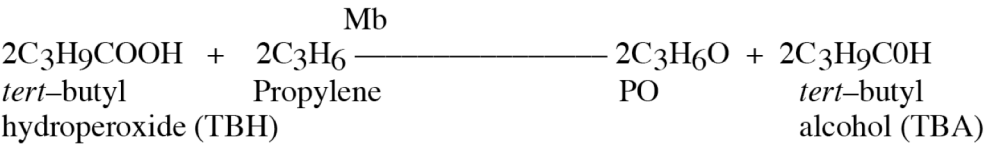


$$\begin{aligned} 346 \text{ total carbons} &= 100 \text{ (3 carbons in PG)} + 10 \text{ (4 carbons in di-PG)} + 1 \text{ (6 carbons in tri-PG)} \\ 346/3 &= 115 \end{aligned}$$



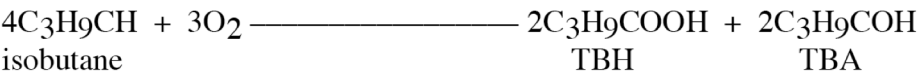
$$3,694 \text{ g PG} \times 1 \text{ mol}/76 \text{ g} \times 115 \text{ mol PO}/100 \text{ mol PG} \times 58 \text{ g PO}/\text{mol} = \mathbf{3241 \text{ g PO -or- 55.89 mols PO}}$$

- (2) Assumptions:
- Reactants dissolved in toluene
 - Molybdenum catalyst
 - Selectivity for PO is 80%
 - Propylene conversion is 98% with ten-fold excess of propylene



$$\begin{aligned} 55.8 \text{ mols PO} \times 1/0.80 \times 1/0.98 &= 71.17 \text{ mols TBH} \times 90 \text{ g/mol} = \mathbf{6,405 \text{ g TBH}} \\ 711.7 \text{ mols propylene} \times 42 \text{ g/mol} &= \mathbf{29,891 \text{ g propylene}} \end{aligned}$$

- (3) Assumptions:
- Isobutane generated from mixed butane fraction
 - 48% conversion of isobutane
 - 50% selectivity for TBH, 48% selectivity for TBA, 4% residual selectivity



$$\begin{aligned} 71.17 \text{ mols TBH} \times 1/0.48 \times 1/0.5 \times 4 \text{ mols isobutane}/2 \text{ mols TBH} &= \mathbf{593 \text{ mols Isobutane}} \\ 593 \text{ mols Isobutane} \times 90 \text{ g/mol} &= \mathbf{34, 394 \text{ g Isobutane; 65.5 mols TBA or 4845 g TBA}} \end{aligned}$$