



UNIVERSIDADE DE SÃO PAULO
ESCOLA SUPERIOR DE AGRICULTURA
“LUIZ DE QUEIROZ”
DEPARTAMENTO DE GENÉTICA
LGN5825 Genética e Melhoramento de Espécies Alógamas



Hybrids between lines

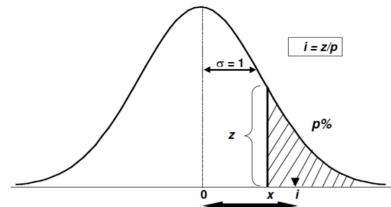
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Piracicaba, April 20th, 2018

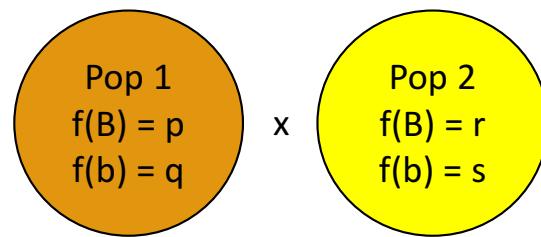
Hybrids

- Cross between two **divergent** but **complementary** lines
- Normally, they belong to different heterotic groups
- Why hybrids?
 - *Combine traits that are in different parents*
 - *Take advantage of heterosis*
 - *Uniformity*
 - *Just the best genotype (single-cross)*
 - *Market seed control*



Types of Hybrids

- SC- Single-cross – A x B
- TWC - Three-way cross - (A x A') x B
- DC - Double-Cross - (A x A') x (B x B')
- Predictions by Jenkins



$$TWC_{(12)3} = \frac{(SC_{13} + SC_{23})}{2} \quad DC_{(12)(34)} = \frac{(SC_{13} + SC_{23} + SC_{14} + SC_{24})}{4}$$

- Heterozygous, “homogeneous”, and high technology
- Number of hybrids (based on the groups)
- $N_{SC} = NL_1(NL_1-1) x NL_2$
- $N_{SC} = NL_1(NL_1-1)/2 x NL_2$
- $N_{SC} = NL_1(NL_1-1)/2 x NL_2(NL_2-1)/2$

Predicting hybrids

- TC - Three-way cross - $(A \times A') \times B$

Parents	Gametes	Possible TWC	GV
$SC_{12} AaBb$ $(AABB \times aabb)$	AB Ab aB ab	AABb	$u + \alpha_A + d_{Bb}$
		AAbb	$u + \alpha_A - \alpha_b$
L3 AAbb	Ab	AaBb	$u + d_{Aa} + d_{Bb}$
		Aabb	$u + d_{Aa} - \alpha_b$
Mean		$u + \frac{1}{2} (\alpha_A - \alpha_b + d_{Aa} + d_{Bb})$	

SC non-parents	Genotype	GV
SC_{13}	AABb	$u + \alpha_A + d_{Bb}$
SC_{23}	Aabb	$u + d_{Aa} - \alpha_b$
Mean		$u + \frac{1}{2} (\alpha_A - \alpha_b + d_{Aa} + d_{Bb})$

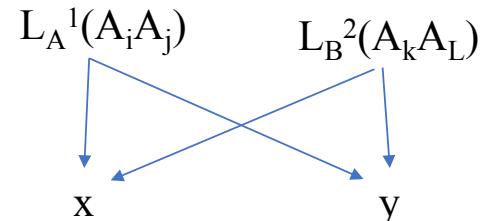
Covariance and response to selection in hybrids

- $\text{COV}_g(X_{ij(12)}, Y_{ij(12)}) = f_{xy1}Va_{12} + f_{xy2}Va_{21} + u_{xy12}Vd_{12}$
- $f_{xy1} = \frac{1}{2} [P(x_i^1 \equiv y_i^1)]$
- $f_{xy2} = \frac{1}{2} [P(x_j^2 \equiv y_j^2)]$
- $u_{xy12} = P(x_i^1 \equiv y_i^1) = P(x_j^2 \equiv y_j^2) = P(x_i^1 \equiv y_i^1; x_j^2 \equiv y_j^2)$
- As they different populations, the latter can be reduced to
- $u_{xy12} = 2f_{xy1}Va_{12} + 2f_{xy2}Va_{21}$
- Single-cross
- $f_{xy1} = \frac{1}{2} [P(x \equiv y \equiv A_i) + P(x \equiv y \equiv A_j) + 2.P(x \equiv y \equiv A_j \equiv A_i)]$

$$\quad \quad \quad \frac{1}{2} \quad \frac{1}{2} \quad \quad \quad \frac{1}{2} \quad \frac{1}{2} \quad \quad \quad \frac{1}{2} \quad \frac{1}{2} \quad F$$
- $f_{xy1} = \frac{1}{2} [\frac{1}{4} + \frac{1}{4} + 2.\frac{1}{4}.F] = \frac{1}{4}(1+F)$
- $f_{xy2} = \frac{1}{2} [P(x \equiv y \equiv A_k) + P(x \equiv y \equiv A_L) + 2.P(x \equiv y \equiv A_k \equiv A_L)] = \frac{1}{4}(1+F)$
- $u_{xy12} = 2f_{xy1}Va_{12} + 2f_{xy2}Va_{21} = 2.\frac{1}{4}(1+F) + 2.\frac{1}{4}(1+F) = \frac{1}{4}(1+F)^2$
- $\text{COV}_{gSC12} = \frac{1}{4}(1+F)[Va_{12} + Va_{21}] + \frac{1}{4}(1+F)^2Vd_{12}$

$$RS = \frac{i}{\sigma_P} COV_G(x, y)$$

$$RS = \frac{i}{\sigma_P} \sigma_H^2$$

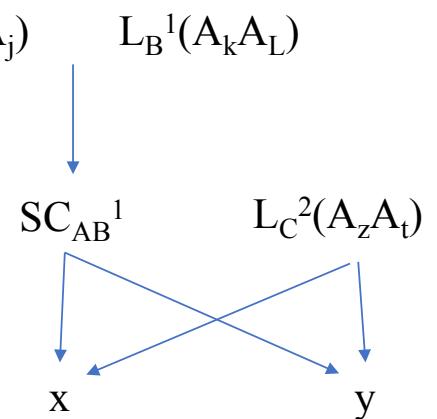


Covariance and response to selection in hybrids

- $\text{COV}_{gSC12} = \frac{1}{4}(1+F)[Va_{12} + Va_{21}] + \frac{1}{4}(1+F)^2Vd_{12}$
- Thus, for SC between S_1 lines ($F = 0 = \text{parents } F$)
- $\text{COV}_{gSC12} = \frac{1}{4}(1+0)[Va_{12} + Va_{21}] + \frac{1}{4}(1+0)^2Vd_{12}$
- $\text{COV}_{gSC12} = \frac{1}{4}[Va_{12} + Va_{21}] + \frac{1}{4}Vd_{12}$
- and for SC between inbred lines ($F=1$)
- $\text{COV}_{gSC12} = \frac{1}{4}(1+1)[Va_{12} + Va_{21}] + \frac{1}{4}(1+1)^2Vd_{12}$
- $\text{COV}_{gSC12} = \frac{1}{2}[Va_{12} + Va_{21}] + Vd_{12}$
- The latter takes advantage of all the dominance and additive genetic variability
- Therefore, there is no VG within hybrids, just among them

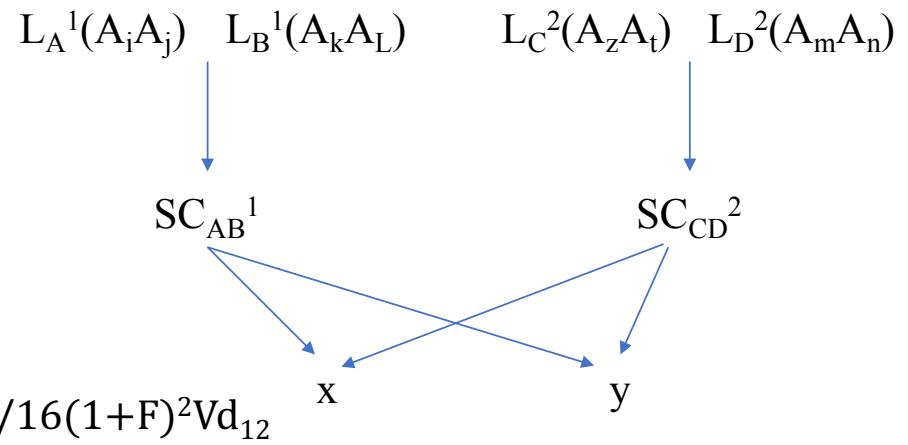
Covariance and response to selection in hybrids

- Three-way cross
- $f_{xy1} = \frac{1}{2} [P(x \equiv y \equiv A_i) + P(x \equiv y \equiv A_j) + 2.P(x \equiv y \equiv A_j \equiv A_j) + \frac{1}{4} \frac{1}{4} + \frac{1}{4} \frac{1}{4} + \frac{1}{4} \frac{1}{4} F]$
- $+ P(x \equiv y \equiv A_k) + P(x \equiv y \equiv A_L) + 2.P(x \equiv y \equiv A_K \equiv A_L)]$
- $f_{xy1} = \frac{1}{2} [1/16 + 1/16 + 2.1/16.F + 1/16 + 1/16 + 2.1/16.F] = \frac{1}{8}(1+F)$
- $f_{xy2} = \frac{1}{2} [P(x \equiv y \equiv A_z) + P(x \equiv y \equiv A_t) + 2.P(x \equiv y \equiv A_z \equiv A_t)]$
- $f_{xy2} = \frac{1}{2} [\frac{1}{4} + \frac{1}{4} + 2.\frac{1}{4}.F] = \frac{1}{4}(1+F)$
- $u_{xy12} = 2f_{xy1}Va_{12} + 2f_{xy2}Va_{21} = 2.1/8(1+F) + 2.\frac{1}{4}(1+F) = \frac{1}{8}(1+F)^2$
- $COV_{gTWC(12)3} = 1/8(1+F)Va_{12} + 1/4(1+F)Va_{21} + 1/8(1+F)^2Vd_{12}$
- TWC between S_1 lines ($F = 0 = \text{parents } F$)
- $COV_{gTWC(12)3} = 1/8Va_{12} + 1/4Va_{21} + 1/8Vd_{12}$
- TWC between inbred lines ($F=1$)
- $COV_{gTWC(12)3} = 1/4Va_{12} + 1/2Va_{21} + 1/2Vd_{12}$



Covariance and response to selection in hybrids

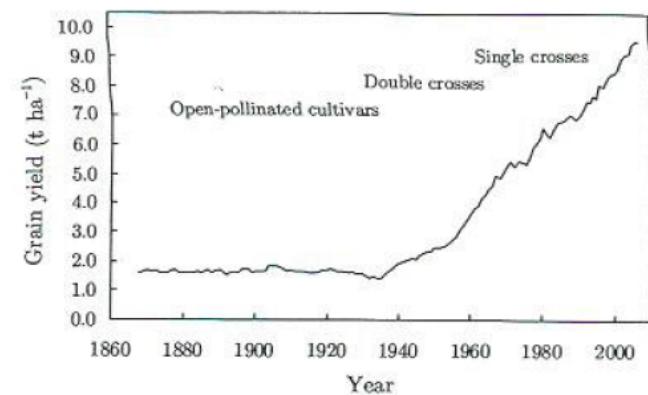
- Double-cross
- $f_{xy1} = 1/8(1+F)$
- $f_{xy2} = 1/8(1+F)$
- $u_{xy12} = 1/16(1+F)^2$
- $\text{COV}_{gDC(12)(34)} = 1/8(1+F)Va_{12} + 1/8(1+F)Va_{21} + 1/16(1+F)^2Vd_{12}$
- DC between S_1 lines ($F = 0 = \text{parents } F$)
- $\text{COV}_{gDC(12)(34)} = 1/8Va_{12} + 1/8Va_{21} + 1/16Vd_{12}$
- DC between inbred lines ($F=1$)
- $\text{COV}_{gDC(12)(34)} = 1/4Va_{12} + 1/4Va_{21} + 1/4 Vd_{12}$



Comparison among cultivars

Hybrid	Vg (among)			Vg (within)		
	V _a ₁₂	V _a ₂₁	V _d ₁₂	V _a ₁₂	V _a ₂₁	V _d ₁₂
SC	1/2	1/2	1	0	0	0
TWC	1/4	1/2	1/2	1/4	0	1/2
DC	1/4	1/4	1/4	1/4	1/4	3/4

Cost, yield, heterosis, homogeneity, and technology



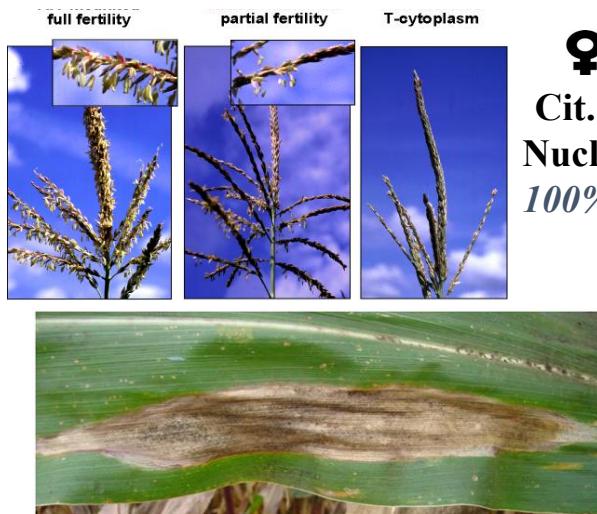
Obtaining hybrids

- SC – ratio **male:female** 1:2 to 1:3 (**3 field of crosses**)
- TWC - 1:2 to 1:3 (**5 fields**)
- DC - 1:6 (**7 fields**)
- Seed cost x Yield
- *Female parent*
- How can we avoid contaminations?
- Coincidence of flowering dates
- Remove the tassels
- Distance of **300m** between fields
- Time interval between fields - **20 to 30 days**



Male-sterility

Double-Cross



Single-cross

DC (12)(34)

Cit. sterile

$\frac{1}{2}$ fertile $\frac{1}{2}$ sterile