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FLS-6183  
Métodos Quantitativos de Pesquisa II  
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Lab 1

Review of Hypothesis Tests  
Difference of means test vs. coefficient test in a bivariate regression model

Answer Key

Part I. Univariate Hypothesis Test Review

- 1) Please summarize the hypothesis test (univariate) on  $y$  as described in the lab? After running the hypothesis test, what can we conclude?

$H_0: y=0.5$

$H_a: y \text{ does not equal } 0.5$  (two-tailed hypothesis test)

$$Pr(|T| > |t|) = 0.0000$$

*We can reject the null hypothesis that  $y=0.5$  with 99% confidence.*

*Have students draw the Student  $t$ -distribution and illustrate the null hypothesis.*

Part II. Bivariate Hypothesis Test Review

- 1) First, let's carry out a hypothesis test where the dependent variable,  $y$ , is a continuous variable ( $y$ ) which differs between two groups with a difference of means test. Please summarize the result of the difference of means hypothesis test on  $y$ ? After running the hypothesis test, is there a difference in the mean conditional on  $x$ ?

$$H_0: x_1 - x_2 = 0$$

$$H_a: x_1 - x_2 \neq 0$$

$$Pr(|T| > |t|) = 0.0000$$

We can reject the null hypothesis that  $x_1 - x_2 = 0$  with 99% confidence.

- 2) Next, let's carry out the same test using a bivariate regression model. Please summarize the result of the difference of means hypothesis test on  $y$ ? After running the hypothesis test, is there a difference in the mean conditional on  $x$ ?

$$y = 0.84 + 2.25x + \varepsilon$$

If we look at the results of the null hypothesis that  $b=0$ , we can reject the null with 99% confidence.

- 3) Do you think there is a preferred method in this particular case for these type of data ( $y$ =continuous and  $x$ =dummy)?

*The methods are different, but the conclusion of the hypotheses tests are the same in this case because  $x$  is a categorical variable. This is a special case.*

*The regression model gives us further information than the difference of means test, but in this case that information has little value added for the inference we are seeking to make in this particular example.*

- 4) Are there any advantages of using a regression in this case? Please explain.

*A falta de linearidade entre as duas variáveis, dado que  $X$  é categórica, faz com que o teste de médias baste para verificar a relação entre ambas. Supondo uma variável  $X$  contínua, os valores da correlação dadas pelo coeficiente da regressão seriam muito mais valiosos.*