

Revisão: Propriedades elétricas

- Metais
- Semicondutores

Ver: (cap. 42 – Fundamentos de Física – Halliday, Resnick, Walker, vol. 4 – 6ª. Ed.)

Classificar os sólidos, do ponto de vista elétrico, de acordo com três propriedades básicas:

Concentração (densidade) de portadores de carga n definida como o número de portadores de carga por unidade de volume (unidades: m^{-3})

Coefficiente de temperatura da resistividade α definido pela relação:

$$\frac{1}{\rho} \frac{d\rho}{dT} = \alpha \quad (\text{unidades: } K^{-1})$$

	Cobre	Silício
Densidade de Portadores de Carga (m^{-3})	9×10^{28}	1×10^{16}
Coefficiente de Temperatura da Resistividade (K^{-1})	$+ 4 \times 10^{-3}$	$- 70 \times 10^{-3}$

Resistividade ρ à temperatura ambiente [unidades: ohm-metro ($\Omega \cdot m$)]

Substância	Resistividade ($\Omega \cdot m$)
Cobre	1.7×10^{-8}
Ouro	2.3×10^{-8}
Alumínio	2.8×10^{-8}
Grafite	6×10^{-6}
Germânio (puro)	4.7×10^{-1}
Silício (puro)	2.1×10^3
Vidro	10^{10}
Mica	10^{15}
Diamante	10^{16}

Fermi energy

The energies available from ordinary thermal or electrical processes are a very tiny fraction of the Fermi energy.

Since all available energy levels are filled, electrons cannot interact with anything unless it is capable of raising them all the way to the Fermi level.

Band energy levels fill up to Fermi level at $T = 0K$

$E_F = 7 \text{ eV}$ for copper
 $kT = 0.026 \text{ eV}$ at 300K
 $eE = 0.00004 \text{ eV}$ for 100 volts on 1m wire.

$$KE_{avg} = \left[\frac{1}{2} m v^2 \right] = \frac{3}{2} kT$$

$\rho(E) = \frac{8\sqrt{2}\pi m^{3/2}}{h^3} \sqrt{E}$
 $\rho(E)$ = electron density of states

- The Fermi energy is the maximum energy occupied by an electron at 0K. By the Pauli exclusion principle, we know that the electrons will fill all available energy levels, and the top of that "Fermi sea" of electrons is called the Fermi energy or Fermi level. One of the remarkable things about the Fermi energy is how large it is compared to the energies which electrons could gain by ordinary physical interactions with their environment.
- The amount of energy available as a result of the temperature of the material is on the order of the average thermal energy, for which $kT = .026 \text{ eV}$ at 300K is a representative number. This is very small compared to the Fermi energy of 7 eV for copper. This tells us that that thermal energy can interact with only a tiny fraction of the electrons (roughly $.026/7$ or about 0.4% of the energy range), since the overwhelming majority of the electrons are separated from the top of the Fermi sea by much more than thermal energy. This correlates well with the observation that electrons do not contribute significantly to the specific heat of solids at ordinary temperatures. Only at very low temperatures does the electron specific heat become significant.

METAIS

Diagrama de Bandas

E_F
 $E = 0$ } Banda Parcialmente Preenchida

- E_F = nível de Fermi = energia de Fermi → definido para $T = 0 \text{ K}$
- elétrons que ocupam banda parcialmente preenchida → elétrons de valência
- Cobre:
 $E_F = 7,0 \text{ eV}$, $v_F = 0,0052 c = 1,6 \times 10^6 \text{ m/s}$ (vel. dos elétrons no nível de Fermi)

para $T = 0 \text{ K}$

O que acontece se aumentarmos a temperatura??

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Energia Térmica (kT)

- Elétrons próximos ao nível de Fermi irão para níveis vagos acima do nível de Fermi continuarão aprisionados nesta banda
- Distribuição de elétrons não difere muito da distribuição no zero absoluto
- *Energia Térmica = kT energia cedida ao elétron através do aumento de temperatura*
- (k = constante de Boltzman = $8,62 \times 10^{-5}$ eV/K)
- T=1000 K (727 °C) kT = 0,086 eV
- Pouca alteração na energia do elétron

Condução elétrica num metal: Resistividade ρ

- Expressão baseada no modelo de elétrons livres (gás de elétrons) – elétrons de condução
- Aplica-se um campo elétrico E \Rightarrow força F aplicada em cada elétron $F = -eE$
 - Tempo $\Delta t \Rightarrow$ aumento de Δv na velocidade dos elétrons de condução no sentido $-E$
 - \Rightarrow variação na energia dos elétrons
 - \Rightarrow ocupam outros níveis vagos
 - Velocidade dos elétrons não cresce sem limites
 - \Rightarrow colisões com vibrações térmicas da rede limita a velocidade
 - \Rightarrow chega a um valor constante \Rightarrow corrente constante
 - \Rightarrow tempo para que isto ocorra: **tempo de relaxação τ**
- $$\rho = \frac{m}{ne^2\tau}$$
- m = massa do elétron; e = carga do elétron;
n = concentração de portadores de cargas
(nº de elétrons de condução por volume.)

METAIS: como varia a resistividade com o aumento da temperatura?

$$\rho = \frac{m}{ne^2\tau}$$

- Concentração de portadores de carga (n) não aumenta muito, por causa dos processos de colisão;
- Tempo de relaxação τ diminui bastante com o aumento no número de colisões, mais rápido se chega a uma corrente constante.

ρ AUMENTA com a temperatura

$$\frac{1}{\rho} \frac{d\rho}{dT} = \alpha \quad \alpha = \text{coeficiente de temperatura da resistividade é POSITIVO!}$$

Como se calcula o número de elétrons de condução (N_{ec}) num sólido?

$$N_{ec} = N_{\text{átomos}} \times N_{\text{elétrons de valência/átomo}}$$

$$n = \frac{N_{ec}}{\text{volume da amostra}}$$

$$n = \frac{N_{\text{átomos}} \times N_{\text{elétrons de valência/átomo}}}{\text{volume da amostra}}$$

Concentração de portadores de carga

$$N_{\text{átomos}} = \frac{M_{\text{amostra}}}{\text{massa atômica}} = \frac{\text{massa específica} \times \text{volume}}{\text{massa atômica}}$$

$$\text{massa atômica} = \frac{\text{massa molar}}{N_A}$$

$$N_A = 6,02 \times 10^{23} \text{ mol}^{-1}$$

Estudo Quantitativo da Eletricidade num Metal

- 1) Contagem de Estados Quânticos:
para 1 átomo: $2(2l + 1)$
para N átomos num sólido: ??
- 2) Contagem dos Estados em $T = 0$ K
- 3) Cálculo da Energia de Fermi
- 4) Contagem dos Estados em $T > 0$ K

1) Contagem de estados quânticos:

N átomos: método estatístico

Em vez de perguntarmos: "qual a energia do estado? "

Perguntamos: "quantos estados (por unidade de volume) tem energia entre E e E + dE? "

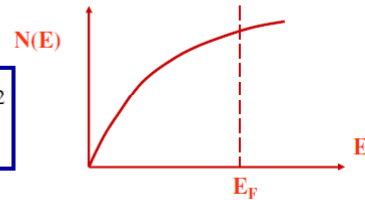
- ❖ Um cristal com 10^{23} átomos origina um número muito grande de níveis de energia. Muitos dos quais são degenerados (= Energia)
- ❖ A densidade de estados $N(E)$ é a medida de estados disponíveis com a mesma energia, por unidade de volume

Densidades de Estados

$$N(E) = \frac{8\pi}{h^3} (2m^3 E)^{1/2}$$

Densidade de Estados

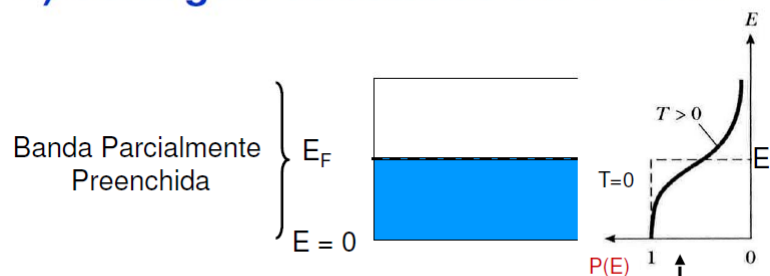
$$N(E) = \frac{8\pi}{h^3} (2m^3 E)^{1/2}$$



Não depende da forma, tamanho e material da amostra

É função apenas da energia!!

2) Contagem de estados em T = 0 K:



- até nível de Fermi, todos os estados estão ocupados (mais baixa energia)
- acima do nível de Fermi, todos os estados estão vazios
- ESTATÍSTICA: peso para cada estado de energia

$P(E) \Rightarrow$ função probabilidade \rightarrow = 1 certeza que o estado está ocupado
 \rightarrow = 0 certeza que o estado está vazio

Densidade de Ocupação de Estados

Nº de estados ocupados por unidade de volume $\rightarrow N_o(E) = N(E) P(E)$

Nº de estados não ocupados por unidade de volume (densidade de estados) $N(E) = \frac{8\pi}{h^3} (2m^3 E)^{1/2}$

Probabilidade de ocupação de um estado $P(E) \begin{cases} = 1 \\ = 0 \end{cases}$

$n = \int_0^{E_F} N_o(E) dE = \int_0^{E_F} N(E) P(E) dE$

$n = N^\circ$ de elétrons de condução por unidade de volume num metal $\rightarrow n = \int_0^{E_F} N(E) dE$

Em T = 0 K os elétrons de condução ocupam todos os estados de energia até o nível de Fermi

3) Cálculo da Energia de Fermi

$$n = \int_0^{E_F} N(E) dE = \int_0^{E_F} \frac{8\pi}{h^3} (2m^3 E)^{1/2} dE = \frac{8\pi}{h^3} (2m^3)^{1/2} \left[\frac{E^{3/2}}{3/2} \right]_0^{E_F}$$

$$n = \frac{16\pi}{3h^3} (2m^3)^{1/2} E_F^{3/2}$$

isolando E_F , temos: $A = 3,65 \times 10^{-19} (m^2 eV)$

$$E_F = \left(\frac{3}{16\sqrt{2}\pi} \right)^{2/3} \frac{h^2}{m} n^{2/3} = \frac{0,121 \cdot h^2}{m} n^{2/3} = A n^{2/3}$$

massa do elétron

Sabendo n (n° de elétrons de condução por volume) calcula-se E_F

4) Contagem de estados para $T > 0$ K

Como fica a função probabilidade $P(E)$?

Temos a distribuição de probabilidades de Fermi-Dirac que representa a probabilidade de ocupação de um estado de com energia E .

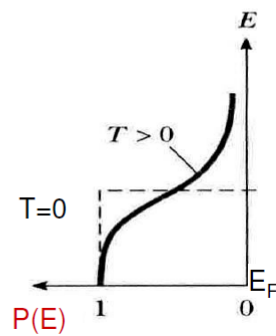
$$P(E) = \frac{1}{e^{(E-E_F)/kT} + 1}$$

Em $T = 0$ K temos:

$$\left\{ \begin{array}{l} \text{para } E < E_F \Rightarrow (E - E_F)/kT \Rightarrow -\infty \\ \quad \Rightarrow e^{-\infty} = 0 \Rightarrow P(E) = 1 \\ \text{para } E > E_F \Rightarrow (E - E_F)/kT \Rightarrow +\infty \\ \quad \Rightarrow e^{+\infty} = \infty \Rightarrow P(E) = 0 \end{array} \right.$$

4) Contagem de estados para $T > 0$ K

$$P(E) = \frac{1}{e^{(E-E_F)/kT} + 1}$$

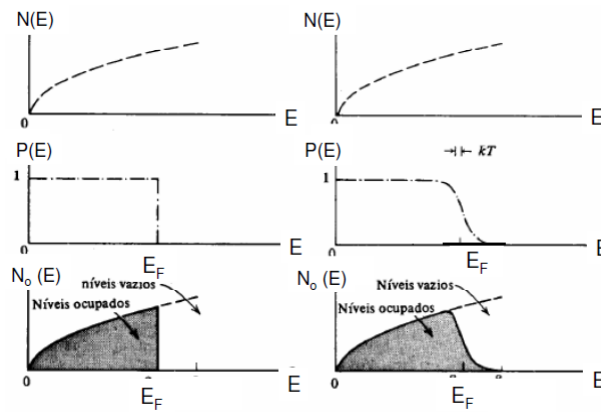


$$n = \int_0^E N_o(E) dE = \int_0^E N(E) P(E) dE$$

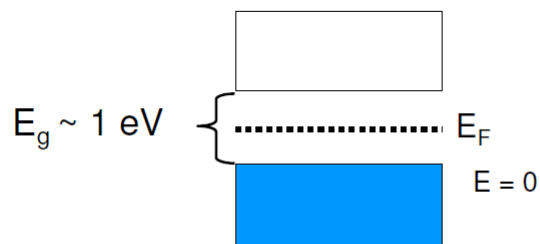
Comparando ocupação de estados para:

T = 0 K

T > 0 K



SEMICONDUCTORES



Elétron pode saltar da banda de valência para a banda de condução por simples agitação térmica

Concentração de portadores de carga:

Para metais: elétrons de condução (= n^o de elétrons de valência por átomo)

$$n_{Cu} = 9 \times 10^{28} \text{ (m}^{-3}\text{) em temperatura ambiente}$$

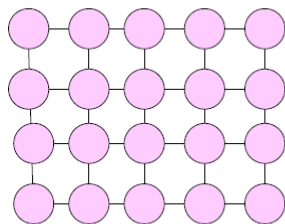
Para semicondutores: portadores de carga surgem apenas por agitação térmica

Elétrons saltam da banda de valência para a banda de condução, gerando

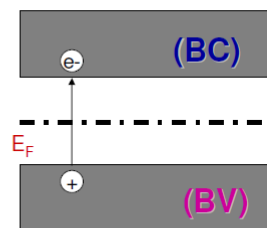
espaços vazios na banda de valência

BURACOS

Semicondutor Intrínseco



○ = Si



$$N(\text{buracos}) = N(\text{elétrons})$$

2 tipos de portadores de carga:

Elétrons na banda de condução (BC)

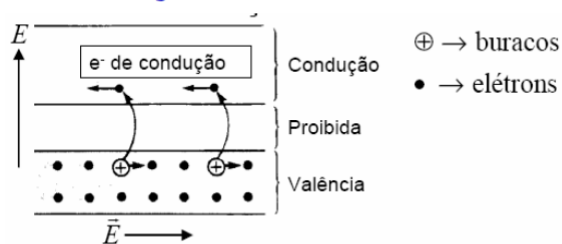
Buracos na banda de valência (BV)

Semiconductors

B	C	N	O
Al	Si	P	S
Ga	Ge	As	Se
In	Sn	Sb	Te

http://worldwatts.com/silicon_semiconductor.html

Condução elétrica em semicondutores:



Um campo elétrico aplicado a um semicondutor produz condução elétrica devido ao movimento dos e^- na banda de condução, bem como dos buracos na banda de valência. No caso dos buracos, o movimento também se deve aos e^- , que, devido ao campo, ocupam sucessivamente a vacância deixada pelo e^- promovido à banda de condução, fazendo com que a vacância se desloque no sentido oposto.

SEMICONDUCTORES: como varia a resistividade com o aumento da temperatura?

$$\rho = \frac{m}{ne^2\tau}$$

- Concentração de portadores de carga (n) aumenta rapidamente com a temperatura (elétrons e buracos);
- Tempo de relaxação τ tem uma diminuição pequena frente ao aumento de (n)

ρ DIMINUI com a temperatura

$$\frac{1}{\rho} \frac{d\rho}{dT} = \alpha \quad \alpha = \text{coeficiente de temperatura da resistividade é NEGATIVO!}$$

$$\alpha_{Si} = -70 \times 10^{-3} \text{ K}^{-1}$$

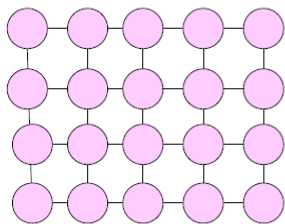
RESUMO:

Propriedade	Metais (M)	Semicondutores (S)	Observações
Portadores de carga (n)	Elétrons de condução	Elétrons + Buracos	$n_M > n_S$
Resistividade $\rho = \frac{m}{ne^2\tau}$	Pequena	Grande	$\rho_M < \rho_S$
Coeficiente de temperatura da resistividade $\frac{1}{\rho} \frac{d\rho}{dT} = \alpha$	$\frac{d\rho}{dT} > 0 \Rightarrow \alpha > 0$ • τ diminui com T • n independe de T	$\frac{d\rho}{dT} < 0 \Rightarrow \alpha < 0$ • τ diminui pouco comparado ao aumento de n com T • n aumenta de T	$\alpha_M > 0$ $\alpha_S < 0$

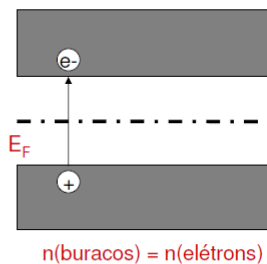
Dopagem de Semicondutores

Objetivo: aumentar a condutividade do SC pela adição de uma pequena quantidade de outro material, denominado de **dopante**

Semicondutor Intrínseco

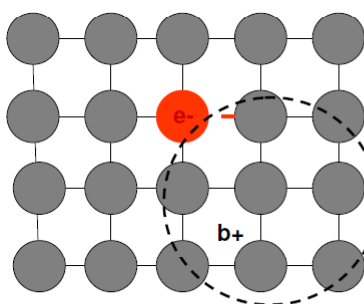


= Si Valência do Si +4

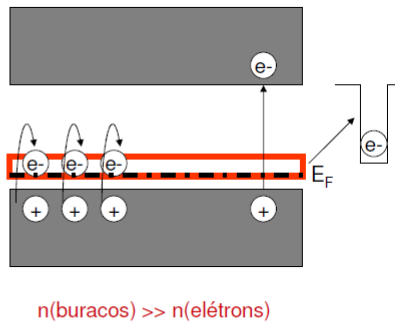


Semicondutor Extrínseco Tipo p (positivo): Portadores majoritários: buracos (BV)

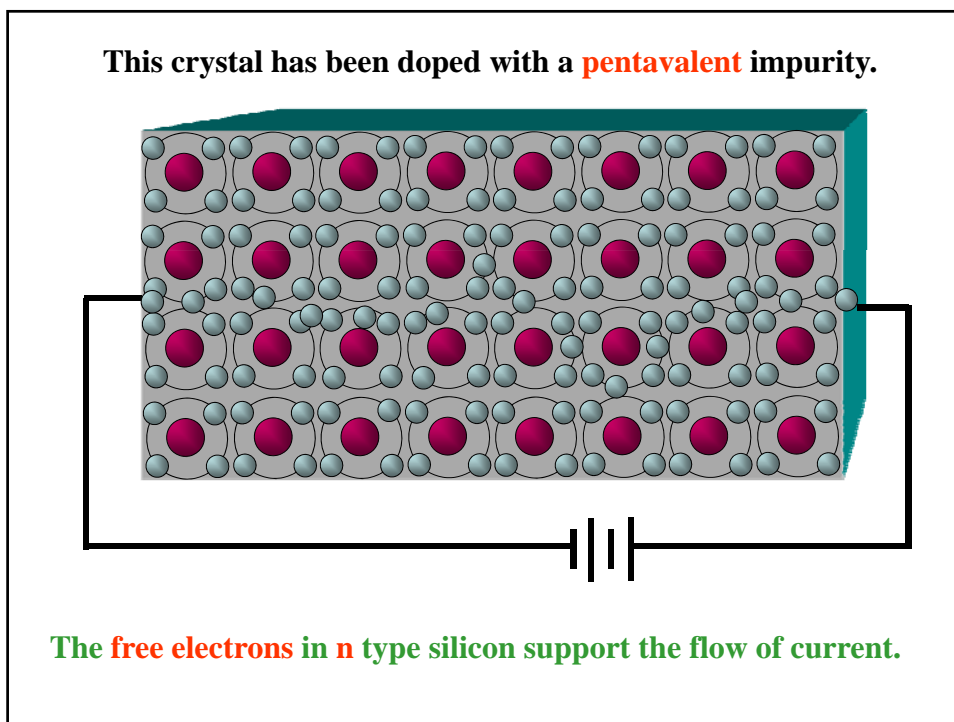
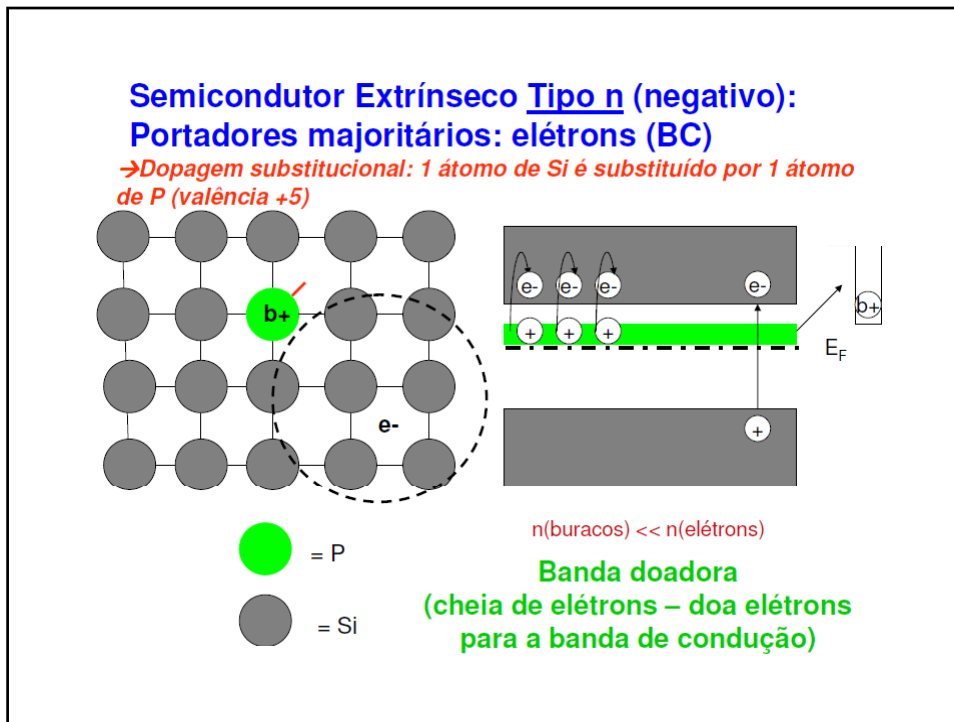
→Dopagem substitucional: 1 átomo de Si é substituído por um átomo de B (valência +3)



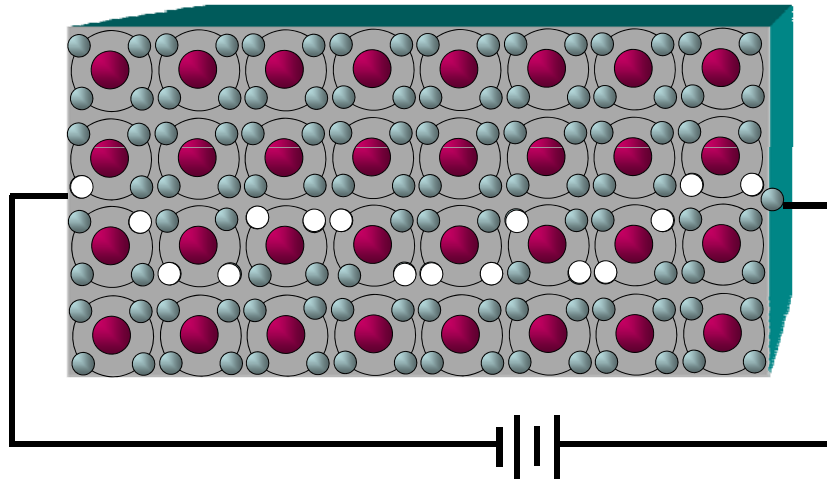
= B
 = Si



Banda receptora (vazia)
(recebe elétrons da banda de valência)



This crystal has been doped with a **trivalent** impurity.

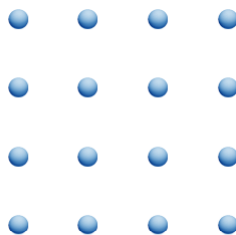


The **holes** in p type silicon contribute to the current.

Note that the hole current direction is opposite to electron current so the electrical current is in the same direction

Supercondutividade

- Supercondutividade - é uma propriedade física, de característica intrínseca de certos materiais, quando resfriados a temperaturas extremamente baixas, tendem a conduzir corrente elétrica sem resistência nem perdas.



Walther Meissner e Robert Ochsenfeld concluíram que supercondutores quando colocados imersos em um campo magnético externo e resfriados abaixo da sua temperatura de transição, tendem a ejetar todo o campo magnético aplicado. Esse fenômeno é chamado de Efeito Meissner, mas não se resume apenas na ejeção do campo magnético por parte do supercondutor, pois na verdade o campo externo tende a penetrar o supercondutor mas apenas até uma certa profundidade definida por um parâmetro λ , denominado parâmetro de penetração de London, decaindo exponencialmente a zero na maior parte do material supercondutor. O efeito Meissner é uma característica primordial da supercondutividade, e para a maioria dos supercondutores λ é da ordem de 100 nm.

Nanotubos de Carbono

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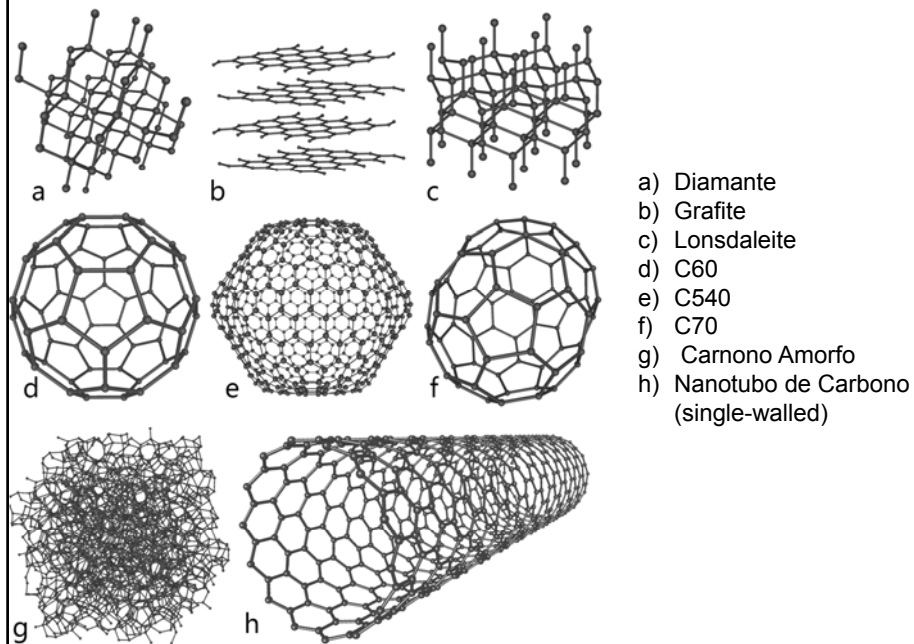
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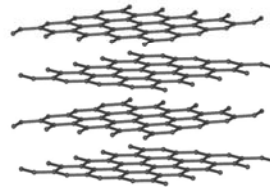
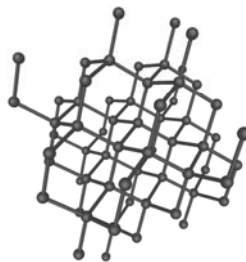
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Estruturas de Carbono



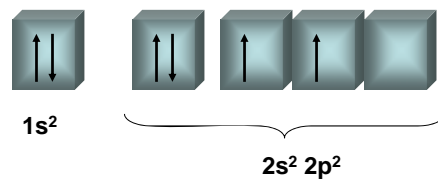
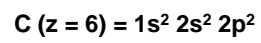
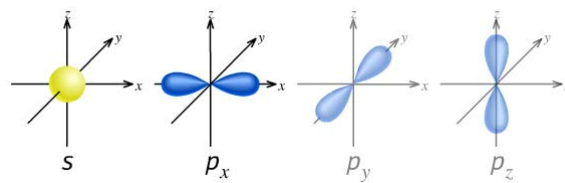
Estruturas de Carbono

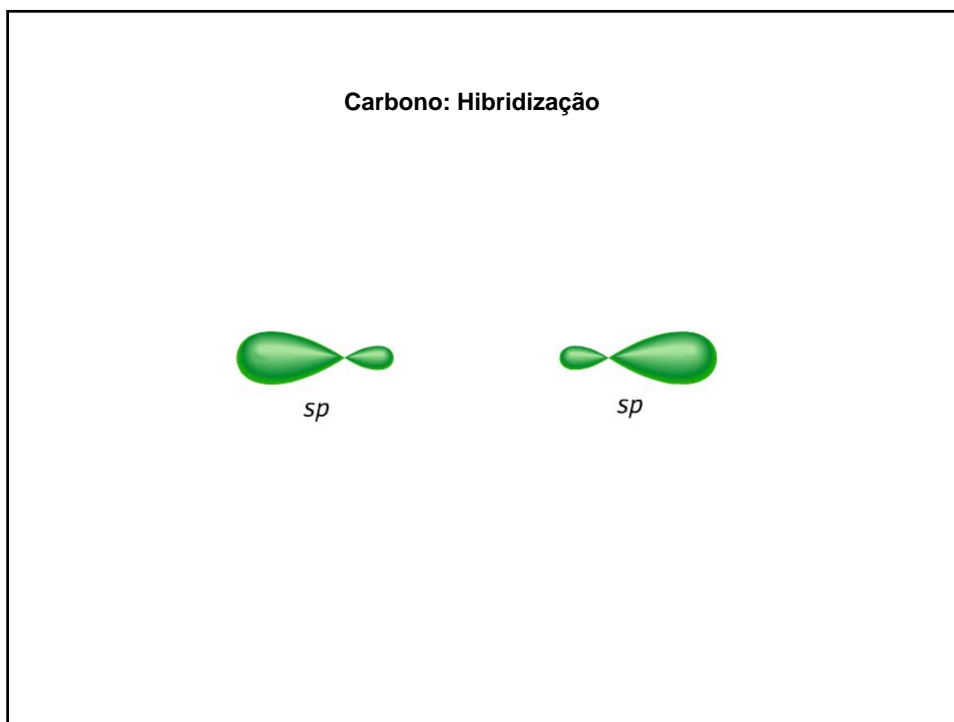
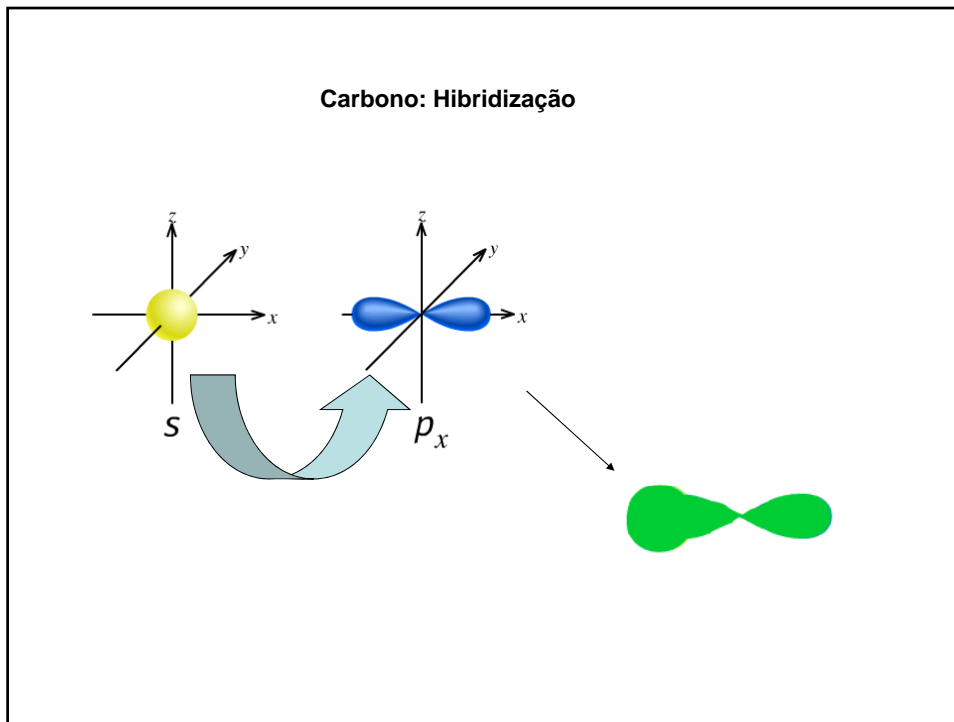
Alotropia

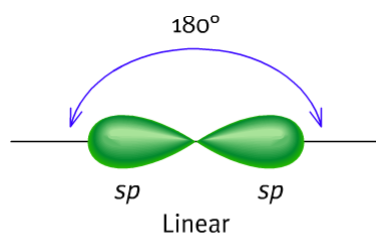
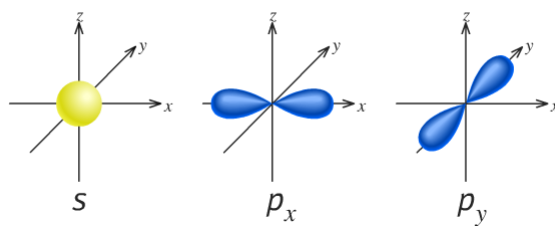


Carbono: Hibridização

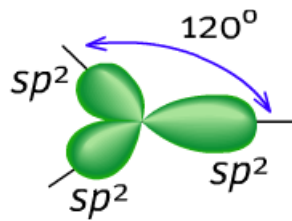
- ✓ **Hibridização:** formação de orbitais híbridos.
- ✓ **subníveis atômicos:** s e p se misturam formando orbitais híbridos sp, sp² e sp³.
- ✓ **Sobreposição de orbitais semipreenchidos**
- ✓ Explica a formação de algumas **ligações** e disposição **geométrica**

Carbono: Hibridização**Carbono: Hibridização**



Carbono: Hibridização**Carbono: Hibridização**

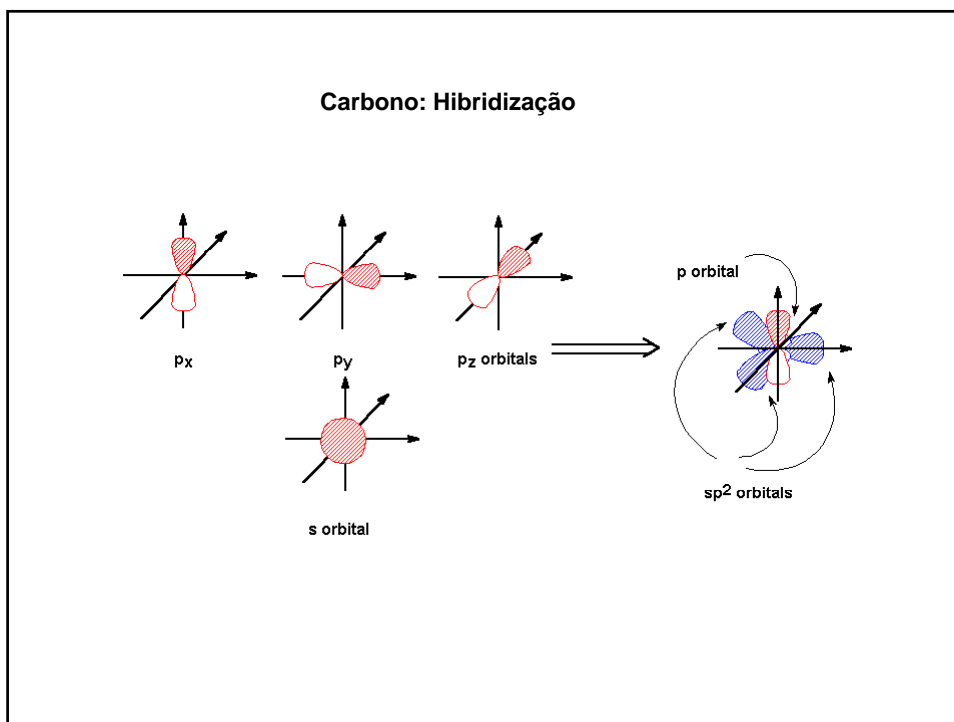
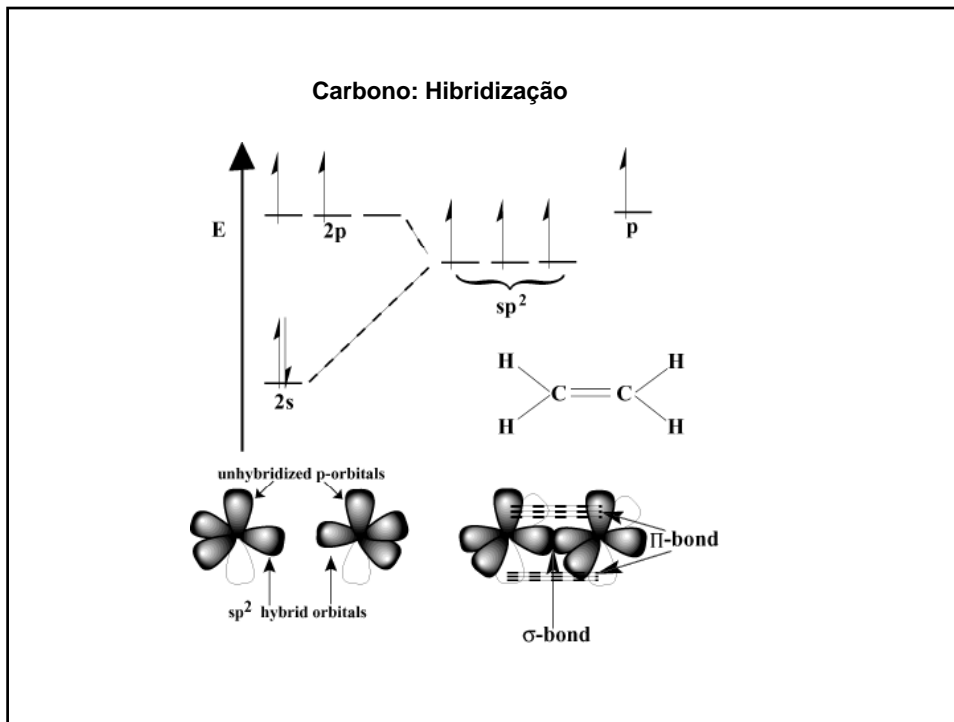
Carbono: Hibridização

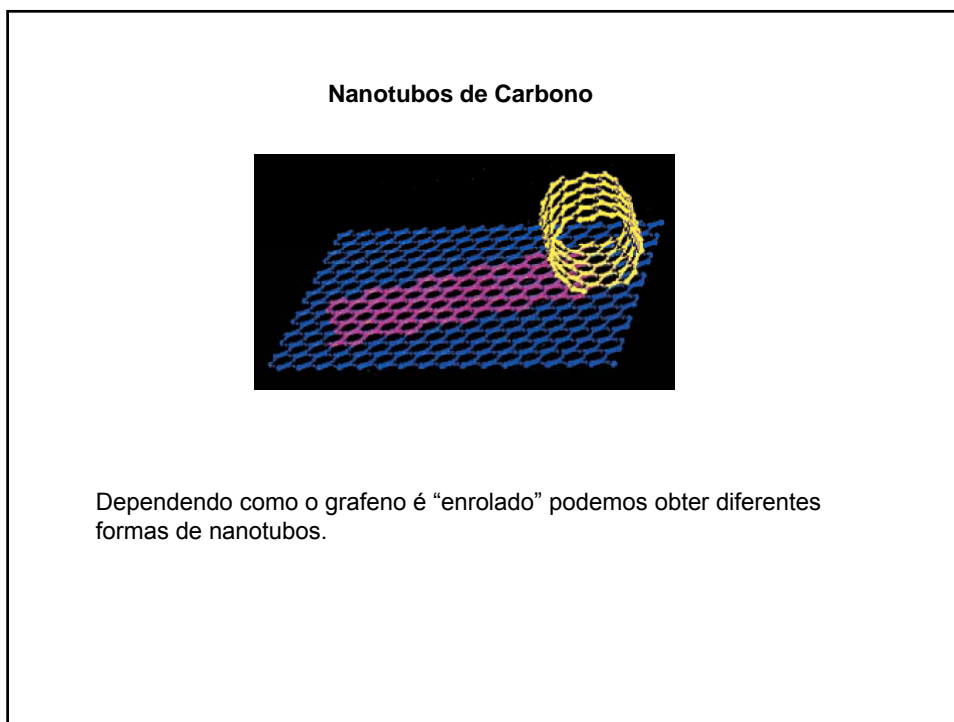
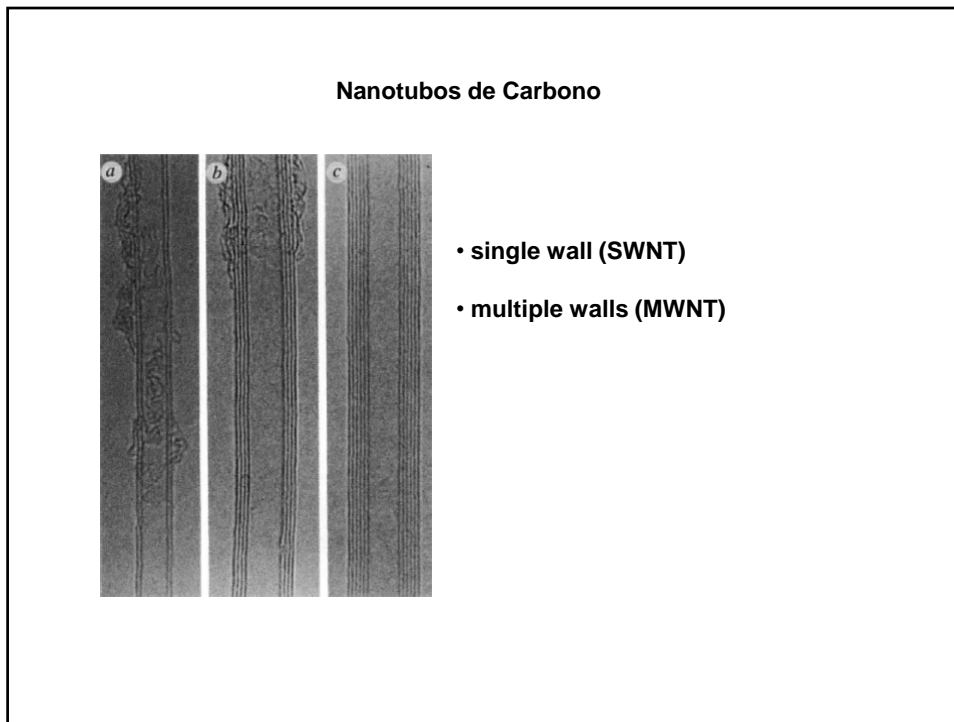


Trigonal Planar

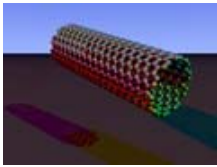
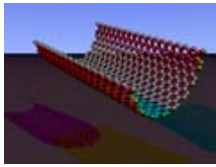
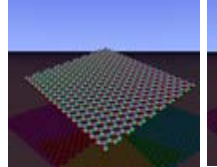
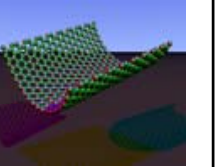
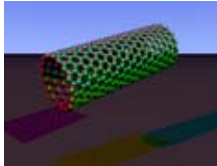
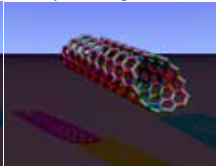
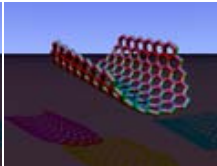
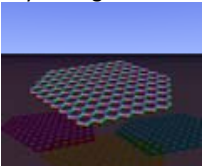
Hibridização

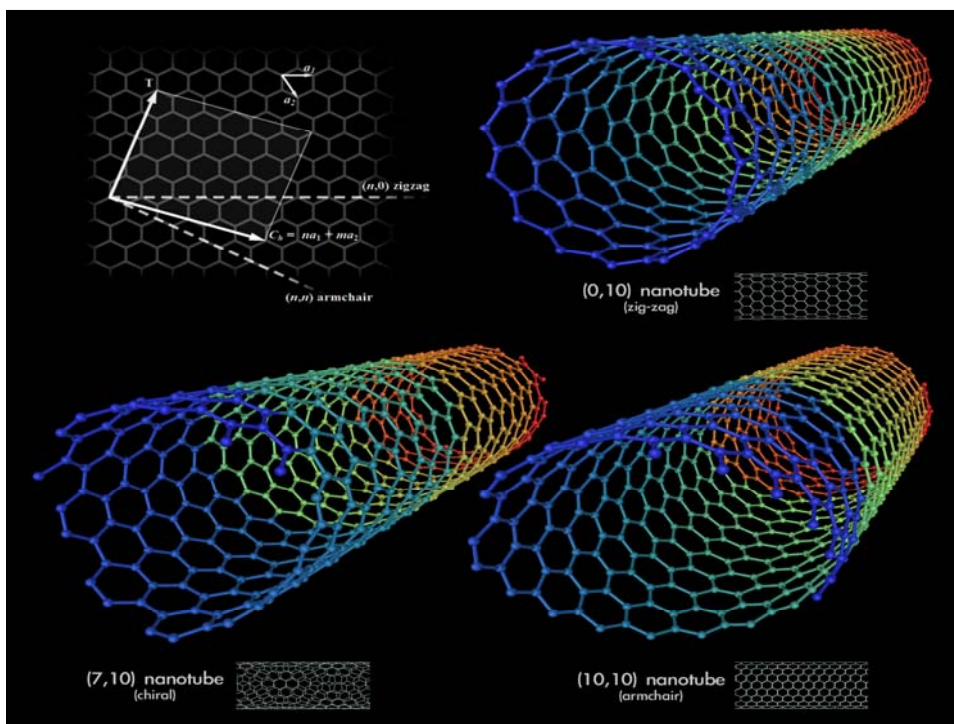
Pure atomic orbitals of central atom	Hybridization of the central atom	Number of hybrid orbitals	Shape of hybrid orbitals
s,p	sp	2	Linear 180°
s,p,p	sp^2	3	Trigonal Planar 120°
s,p,p,p	sp^3	4	Tetrahedral $109,5^\circ$
s,p,p,p,d	sp^3d	5	Trigonal Bipyramidal 90° 120°
s,p,p,p,d,d	sp^3d^2	6	Octahedral 90°

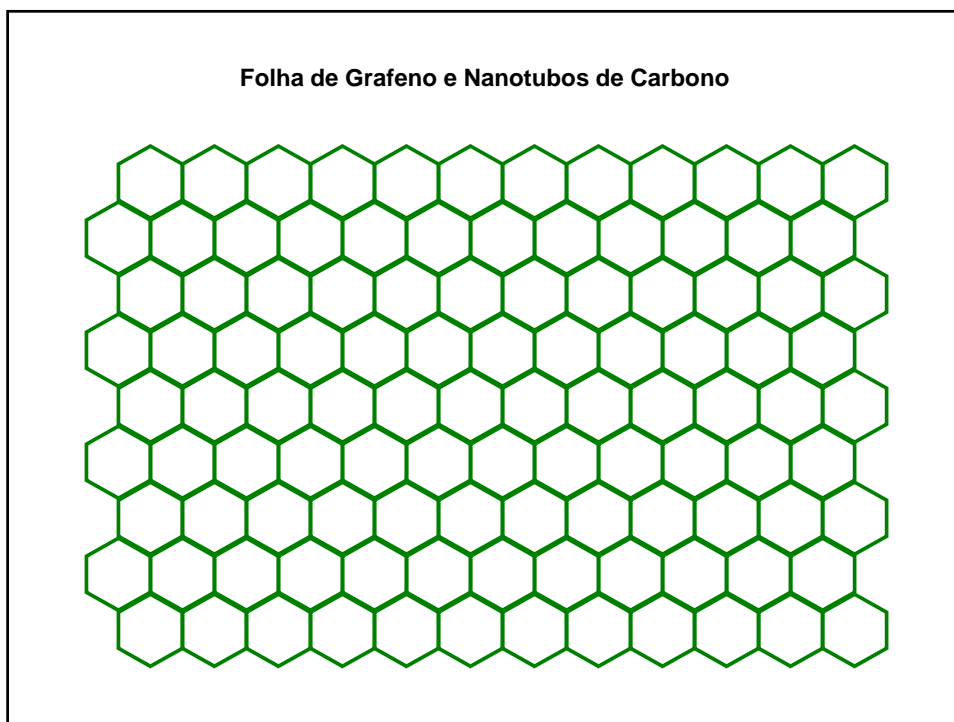
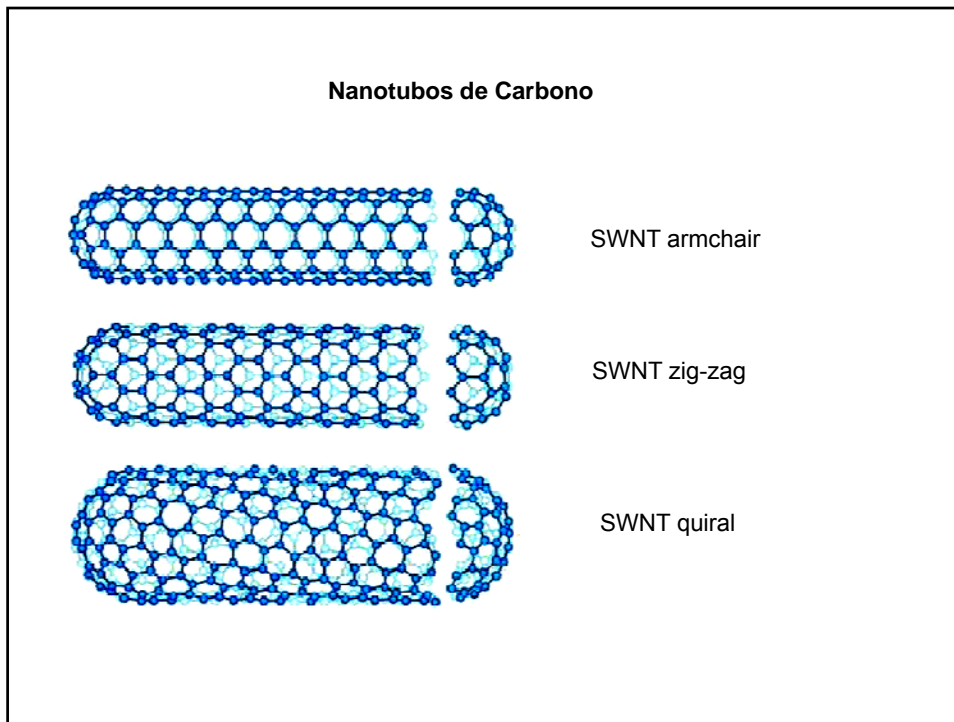


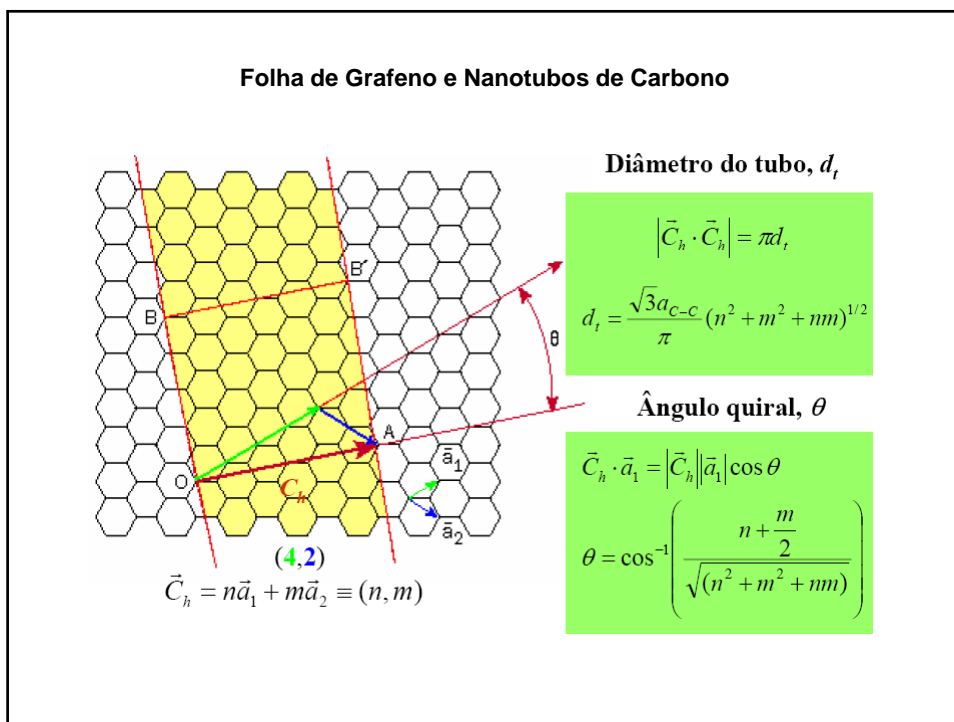
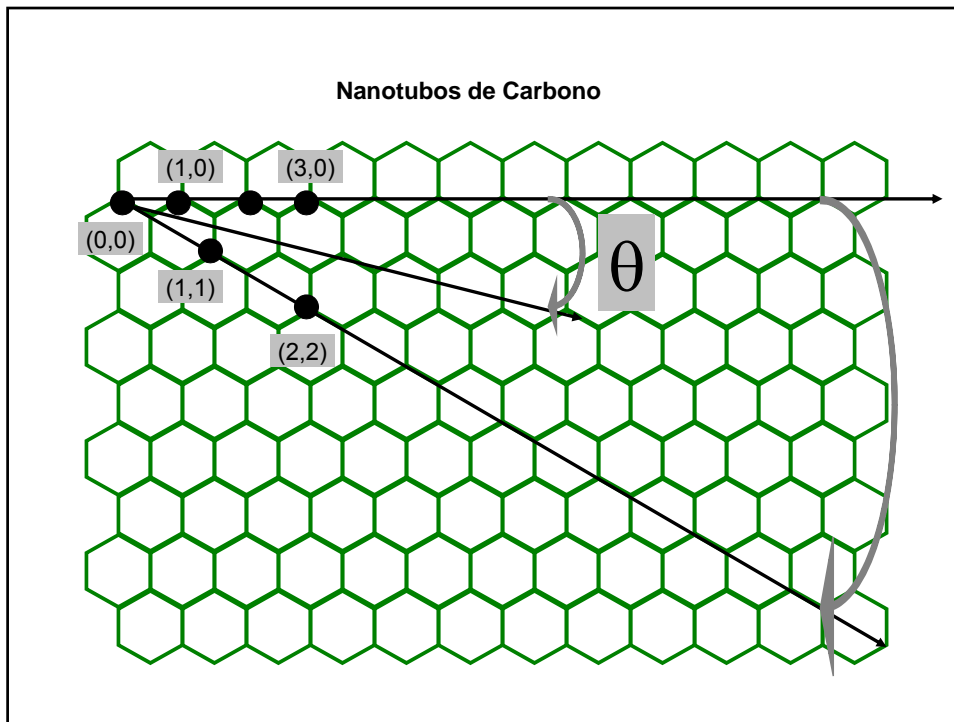


Single-Wall Nanotubes [SWNTs](#)

			
Armchair (n,n)	The chiral vector is bent, while the translation vector stays straight	Zigzag $(n,0)$	Graphene nanoribbon
			
Zigzag $(n,0)$	Chiral (n,m)	n and m can be counted at the end of the tube	Graphene nanoribbon







Folha de Grafeno e Nanotubos de Carbono

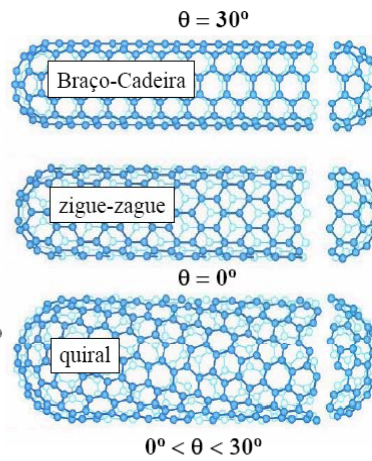
$$\theta = \cos^{-1} \left(\frac{n + \frac{m}{2}}{\sqrt{n^2 + m^2 + nm}} \right)$$

$$i) m = 0$$

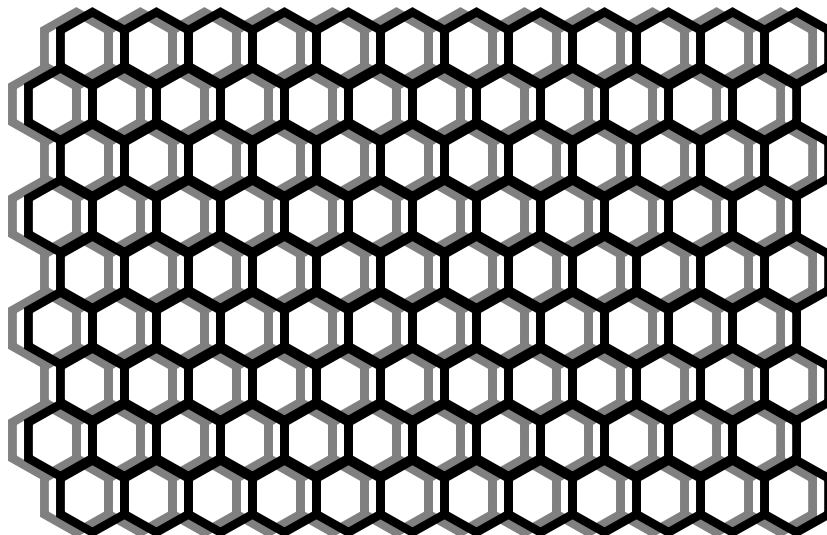
$$\theta = \cos^{-1} \left(\frac{n}{\sqrt{n^2}} \right) \Rightarrow \theta = 0^\circ$$

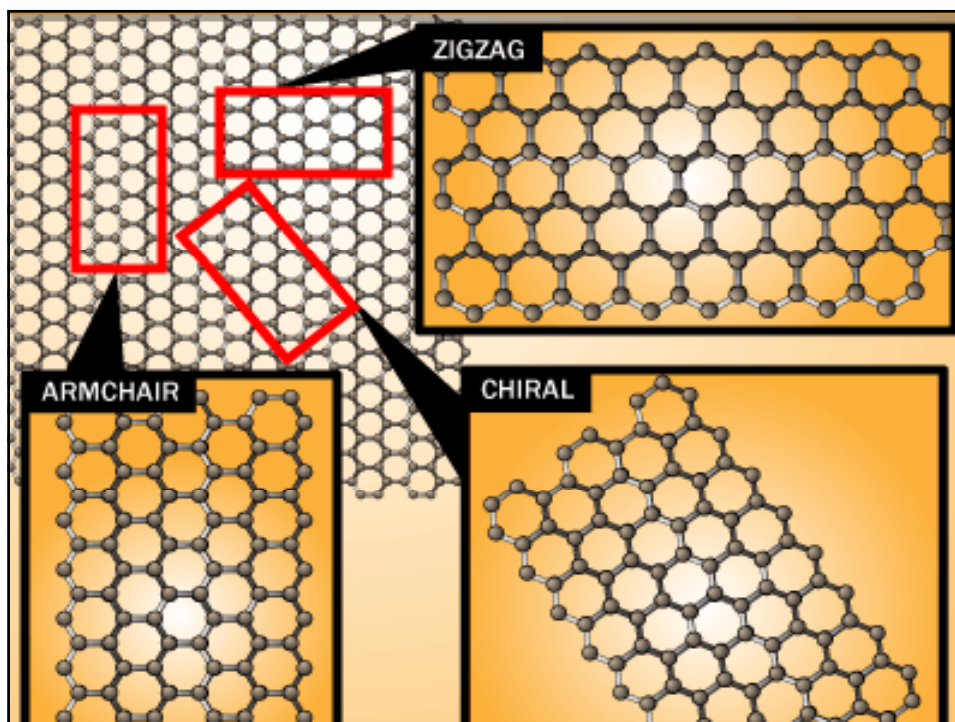
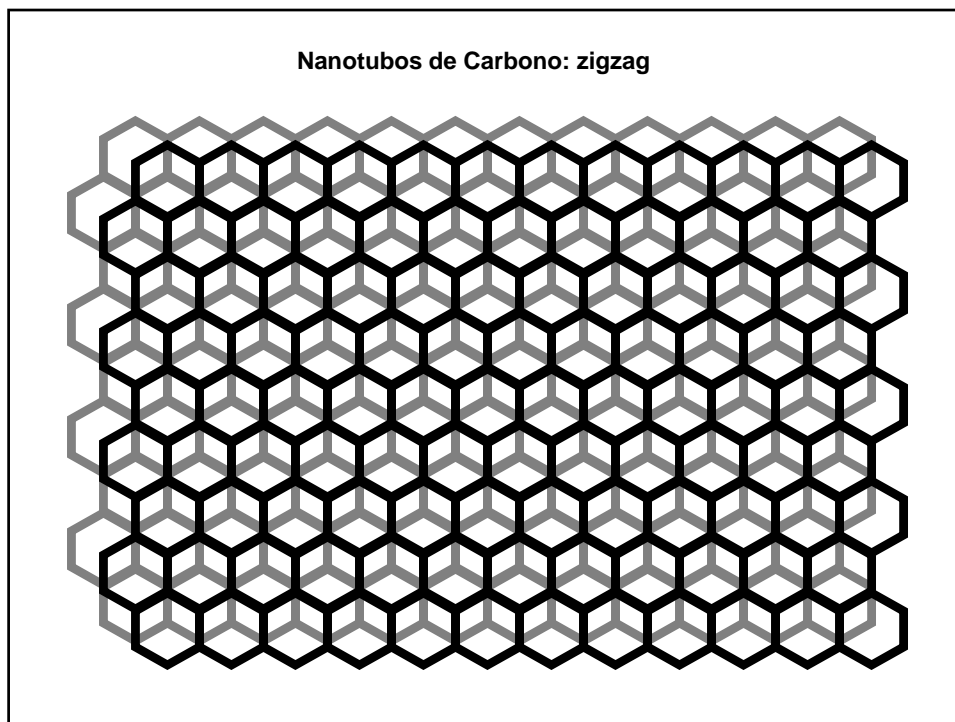
$$ii) n = m$$

$$\theta = \cos^{-1} \left(\frac{3n/2}{\sqrt{3n^2}} \right) = \cos^{-1} \left(\frac{\sqrt{3}}{2} \right) \rightarrow \theta = 30^\circ$$



Nanotubos de Carbono: Armchair





Nanotubos de Carbono

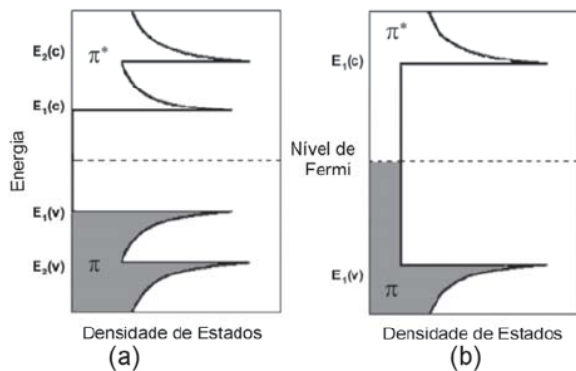
Ângulo quiral

$$\theta = \arctan\left(\frac{-\sqrt{3}m}{2n+m}\right), 0 \leq \theta \leq 30^\circ$$

Nanotubos de Carbono

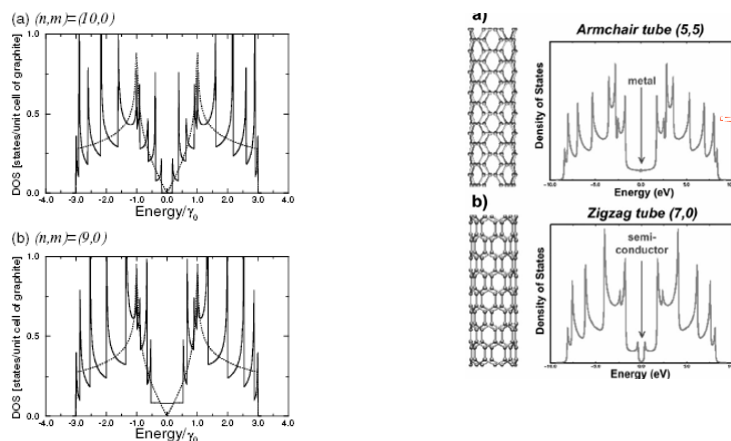
- ✓ armchair: caráter metálico
- ✓ $n-m = 3k \rightarrow$ semicondutores \rightarrow baixo band gap
- ✓ SWNT com diâmetro entre 0,6 e 1,6 apresentam band gap entre 0,4 e 1,0eV
- ✓ MWNT apresentam interação fraca entre os tubos: van der Waals

Nanotubos de Carbono: Propriedades



Densidade de estados eletrônicos para SWNTs semicondutores (a) e metálicos (b). Os estados preenchidos (orbitais π) estão localizados abaixo do nível de Fermi e os estados vazios (orbitais π^*) acima do nível de Fermi

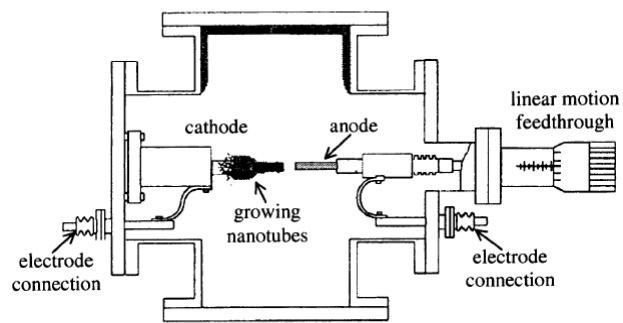
Nanotubos de Carbono: Propriedades



Electronic 1D density of states per unit cell of a 2D graphene sheet for two $(n,0)$ zigzag nanotubes: (a) the $(10,0)$ nanotube which has semiconducting behaviour, (b) the $(9,0)$ nanotube which has metallic behaviour. Also shown in the figure is the density of states for the 2D graphene sheet (dotted line)

Fonte: SAITO, R., DRESSELHAUS, G., and DRESSELHAUS, M. S., 1993, J. appl. Phys., 73, 494.

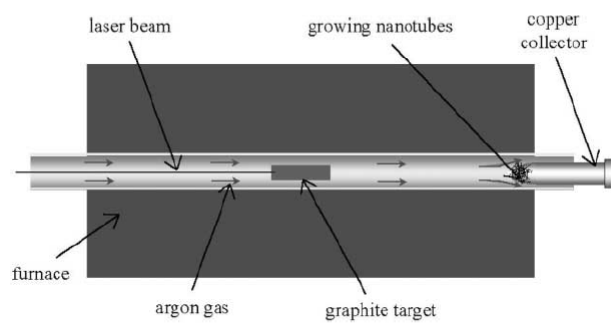
Síntese de Nanotubos de Carbono



Schematic illustration of the arc-discharge technique

Fonte: E.T. Thostenson et al. / Composites Science and Technology 61 (2001) 1899–1912

Síntese de Nanotubos de Carbono

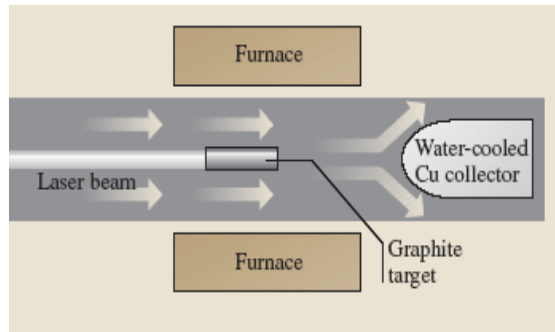


Schematic of the laser ablation process

Fonte: E.T. Thostenson et al. / Composites Science and Technology 61 (2001) 1899–1912

Synthesis of Carbon Nanotube

1 Laser Ablation – Experimental Devices

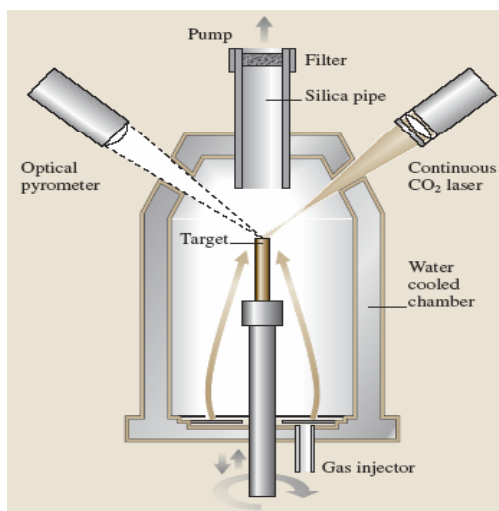


- graphite pellet containing the catalyst put in an inert gas filled quartz tube;
- oven maintained at a temperature of 1,200 °C;
- energy of the laser beam focused on the pellet;
- vaporize and sublime the graphite

Sketch of an early laser vaporization apparatus

The carbon species are there after deposited as soot in different regions: water-cooled copper collector, quartz tube walls.

2 Synthesis with CO₂ laser

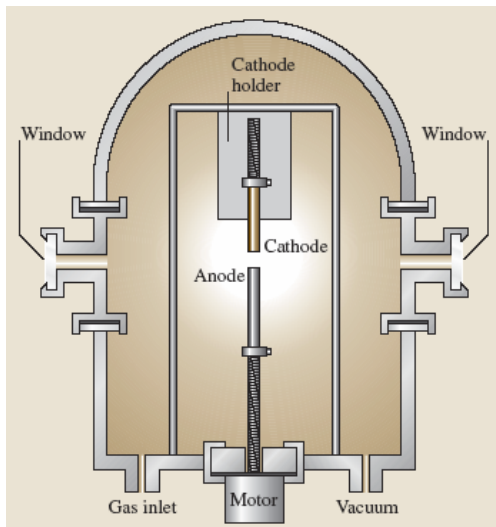


Vaporization of a target at a fixed temperature by a continuous CO₂ laser beam ($\lambda = 10.6\mu\text{m}$). The power can be varied from 100W to 1,600 W.

The synthesis yield is controlled by three parameters: the cooling rate of the medium where the active, secondary catalyst particles are formed, the residence time, and the temperature (in the 1,000–2,100K range) at which SWNTs nucleate and grow.

Fig. 3.10 Sketch of a synthesis reactor with a continuous CO₂ laser device

3 Electric-Arc Method – Experimental Devices



After the triggering of the arc between two electrodes, a **plasma is formed** consisting of the **mixture** of **carbon vapor**, the rare **inert gas** (helium or argon), and the vapors of **catalysts**.

The vaporization is the consequence of the **energy transfer** from the arc to the **anode** made of graphite doped with catalysts.

Sketch of an **electric arc reactor**. It consists of a cylinder of about 30 cm in diameter and about 1m in height.

Nanotubos de Carbono: Funcionalização

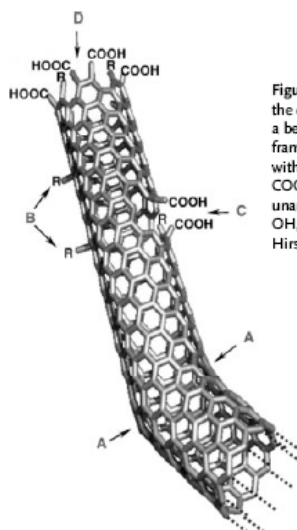
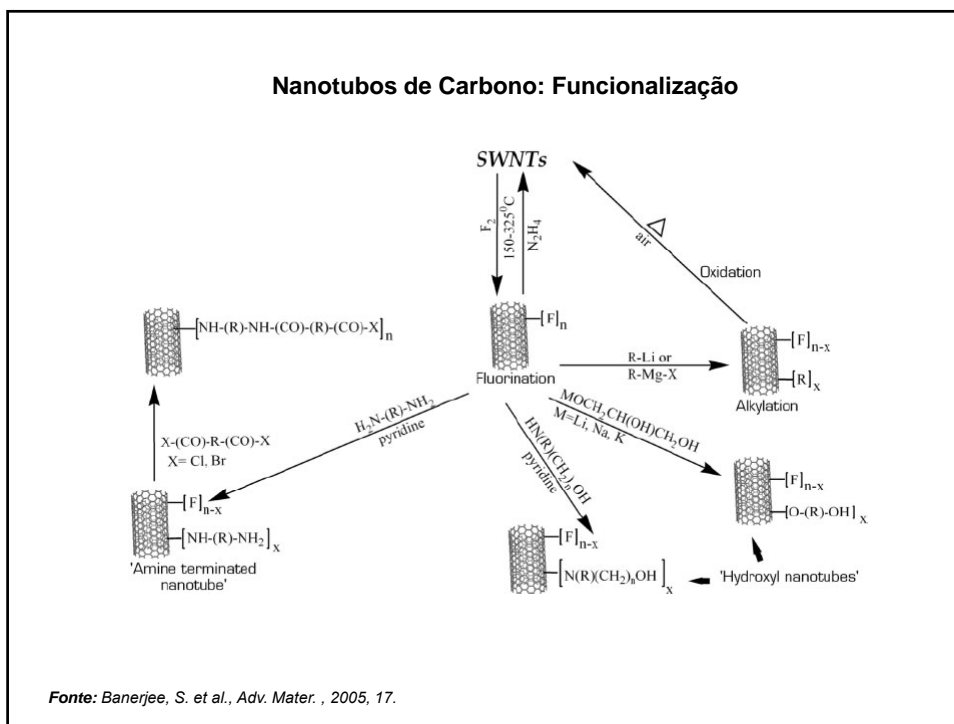
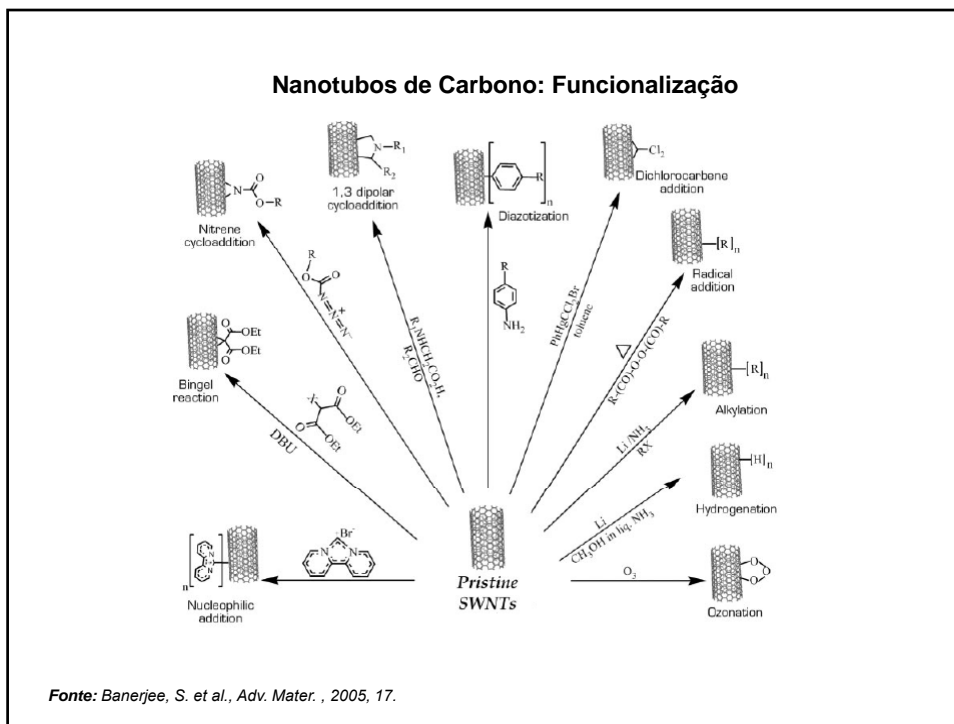


Figure 1. Typical defects in a SWNT. A) Five- or seven-membered rings in the carbon framework, instead of the normal six-membered ring, leads to a bend in the tube. B) sp^3 -hybridized defects (R=H and OH). C) Carbon framework damaged by oxidative conditions, which leaves a hole lined with $-COOH$ groups. D) Open end of the SWNT, terminated with $-COOH$ groups. Besides carboxy termini, the existence of which has been unambiguously demonstrated, other terminal groups such as $-NO_2$, $-OH$, $-H$, and $=O$ are possible. Reprinted with permission from A. Hirsch, *Angew. Chem. Int. Ed.* 2002, 41, 1853. Copyright 2002 Wiley-VCH.

Fonte: Banerjee, S. et al., *Adv. Mater.*, 2005, 17.



Espectroscopia Raman

Quando uma molécula é irradiada, a energia pode ser transmitida, absorvida, ou espalhada. A espectroscopia Raman é baseada na detecção da luz espalhada.

No espalhamento Rayleigh (*elástico*), a interação da molécula com o fóton não provoca mudanças nos níveis de energia vibracional e/ou rotacional da molécula. *Assim as frequências da luz incidente e espalhada são as mesmas.*

O efeito Raman pode ser explicado pela colisão *não-elástica* entre o fóton incidente e a molécula. Isto muda os níveis das energias vibracional e/ou rotacional da molécula por um incremento ($\pm \Delta E$). Pela lei de conservação de energia, isto significa que as energias dos ftons Incidente e espalhado serão diferentes, ou seja $\nu_{\text{incidente}} \neq \nu_{\text{espalhada}}$. Se a molécula absorve energia, ΔE é positiva, $\nu_{\text{incidente}} > \nu_{\text{espalhada}}$, estas são as *linhas Stokes* do espectro (regra de Stokes de fluorescência, $\nu_{\text{incidente}} > \nu_{\text{fluorescência}}$). Se a molécula perde energia, ΔE é negativa, $\nu_{\text{incidente}} < \nu_{\text{espalhada}}$, *linhas anti Stokes* do espectro.

Raman Spectroscopy: Some Sources

General Principles and Instrumentation:

Principles of Instrumental Analysis, by Douglas A. Skoog, F. James Holler, Timothy A. Nieman

Inorganic:

Infrared and Raman Spectra of Inorganic and Coordination Compounds : Theory and Applications in Inorganic Chemistry (Volume A) by Kazuo Nakamoto

Infrared and Raman Spectra of Inorganic and Coordination Compounds : Applications in Coordination, Organometallic, and Bioinorganic Chemistry (Volume B) by Kazuo Nakamoto

Organic:

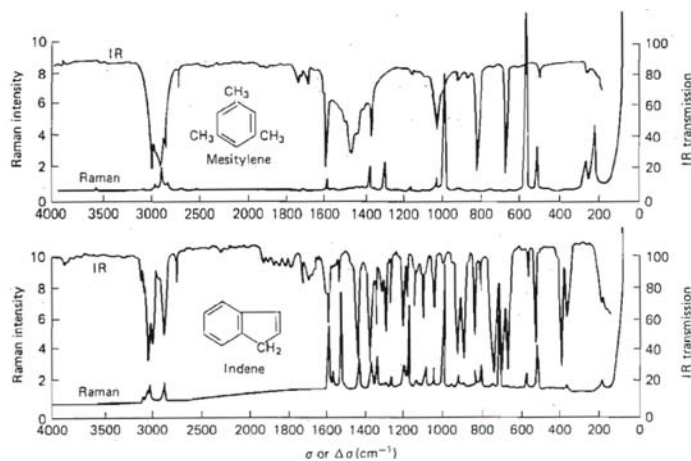
The Handbook of Infrared and Raman Characteristic Frequencies of Organic Molecules by Daimay Lin-Vien, et al

Raman Spectroscopy: Overview

- A vibrational spectroscopy
 - IR and Raman are the most common vibrational spectroscopies for assessing molecular motion and fingerprinting species
 - Based on **inelastic** scattering of a monochromatic excitation source
 - Routine energy range: 200 - 4000 cm^{-1}
- Complementary selection rules to IR spectroscopy
 - Selection rules dictate which molecular vibrations are probed
 - Some vibrational modes are both IR and Raman active
- Great for many real-world samples
 - Minimal sample preparation (gas, liquid, solid)
 - Compatible with wet samples and normal ambient
 - Achilles Heal is sample fluorescence

Raman Spectroscopy: General

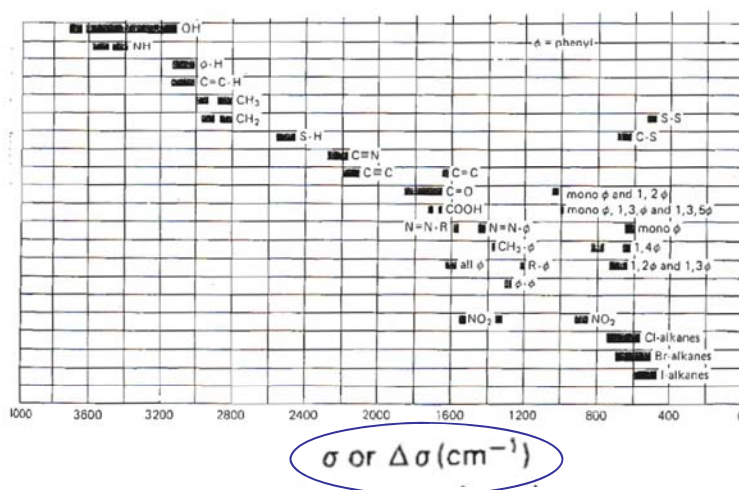
- IR and Raman are both useful for Fingerprinting



- Symmetry dictates which are active in Raman and IR

Raman Spectroscopy: General

- Group assignments identify characteristic vibrational energy



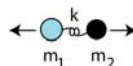
Raman Spectroscopy: Classical Treatment

- Number of peaks related to degrees of freedom

$$DoF = 3N - 6 \text{ (bent) or } 3N - 5 \text{ (linear) for } N \text{ atoms}$$

- Energy related to harmonic oscillator

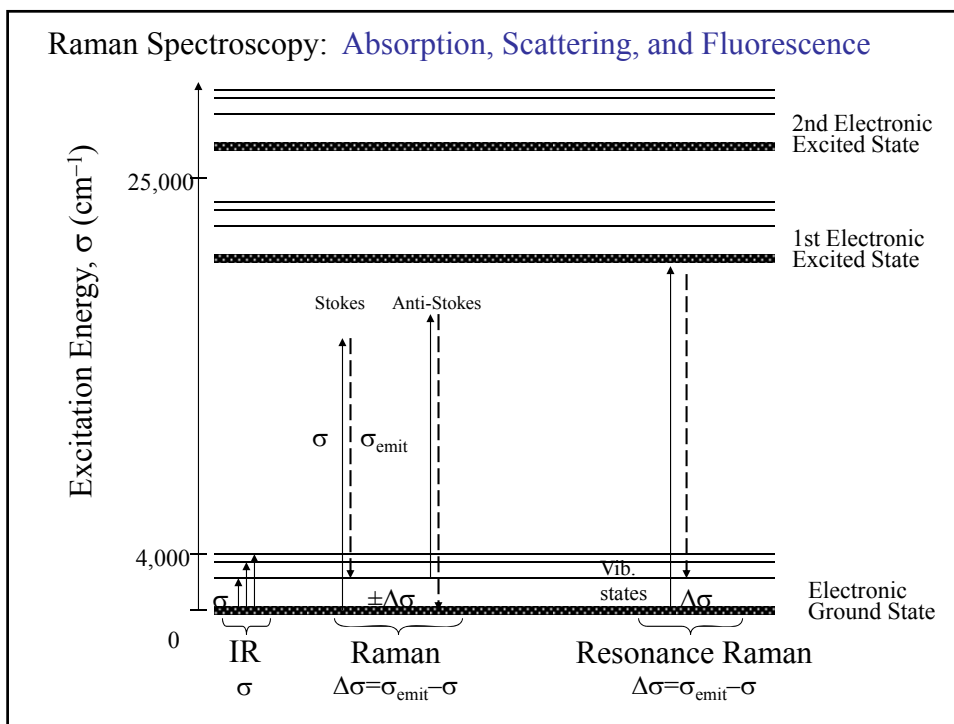
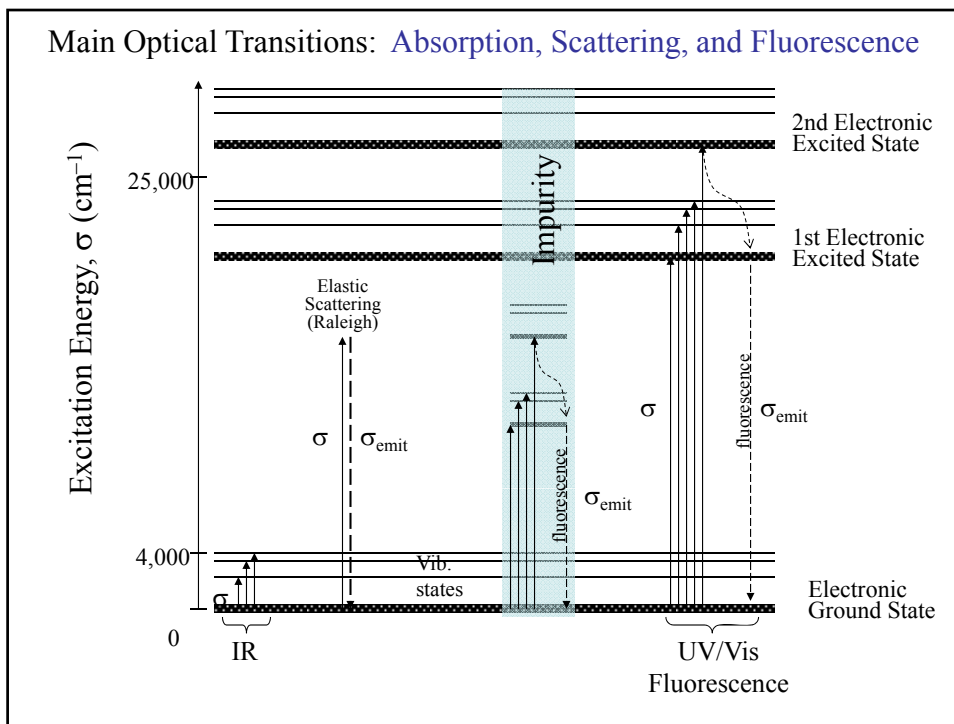
$$\sigma \text{ or } \Delta\sigma = \frac{c}{2\pi} \sqrt{\frac{k(m_1+m_2)}{m_1 m_2}}$$

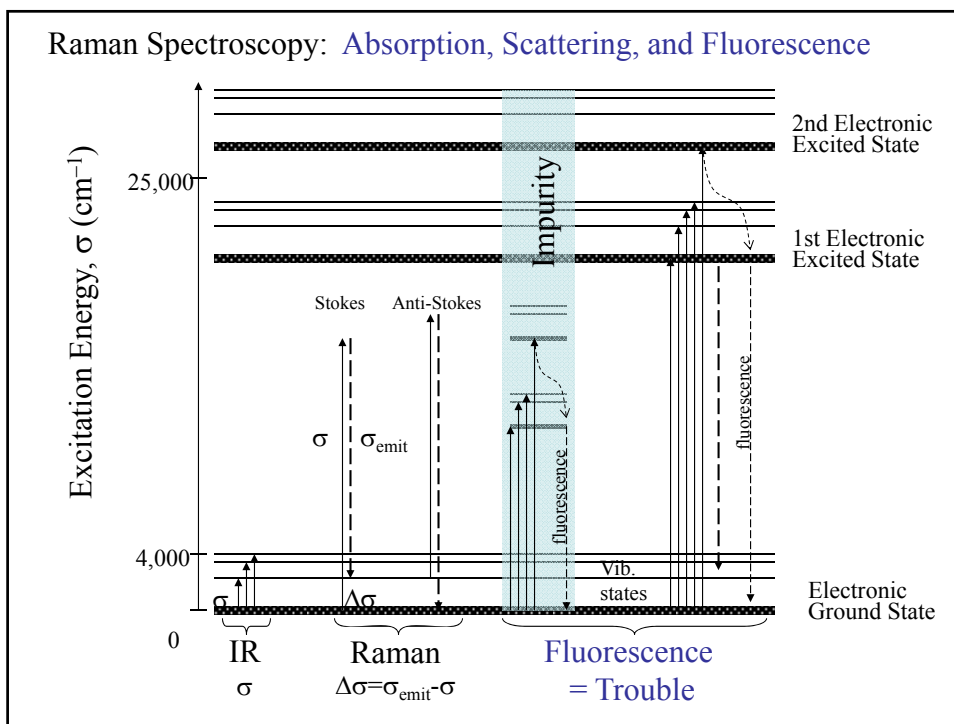
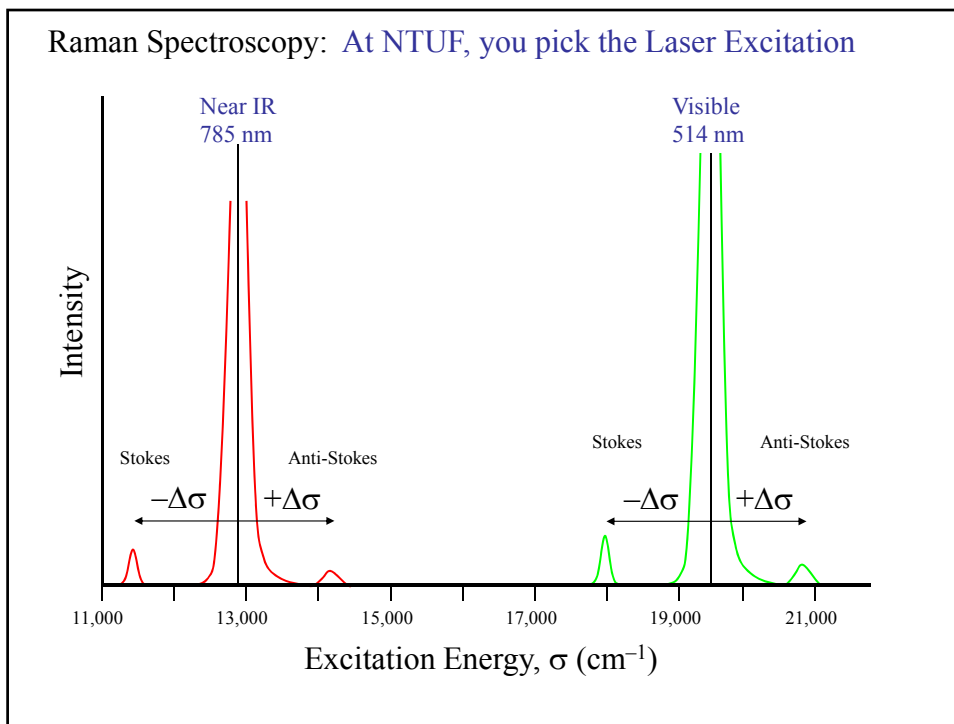


- Selection rules related to symmetry

Rule of thumb: symmetric=Raman active, asymmetric=IR active

CO ₂	H ₂ O
<p>Raman: 1335 cm⁻¹</p>	<p>Raman + IR: 3657 cm⁻¹</p> <p>Raman + IR: 3756 cm⁻¹</p> <p>+ IR: 1594 cm⁻¹</p>
<p>IR: 2349 cm⁻¹</p>	
<p>IR: 667 cm⁻¹</p>	





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Raman spectroscopy of carbon nanotubes

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^bFrancis Bitter Magnet Lab, MIT, Cambridge, MA 02139, USA

^cDepartment of Physics, Tohoku University, and CREST, JST, Sendai 980-8578, Japan

^dDepto. de Física, Universidade Federal de Minas Gerais, Belo Horizonte - MG 30123-970, Brazil

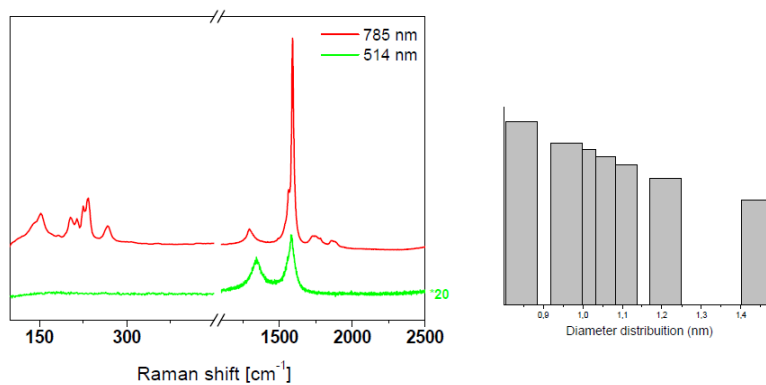
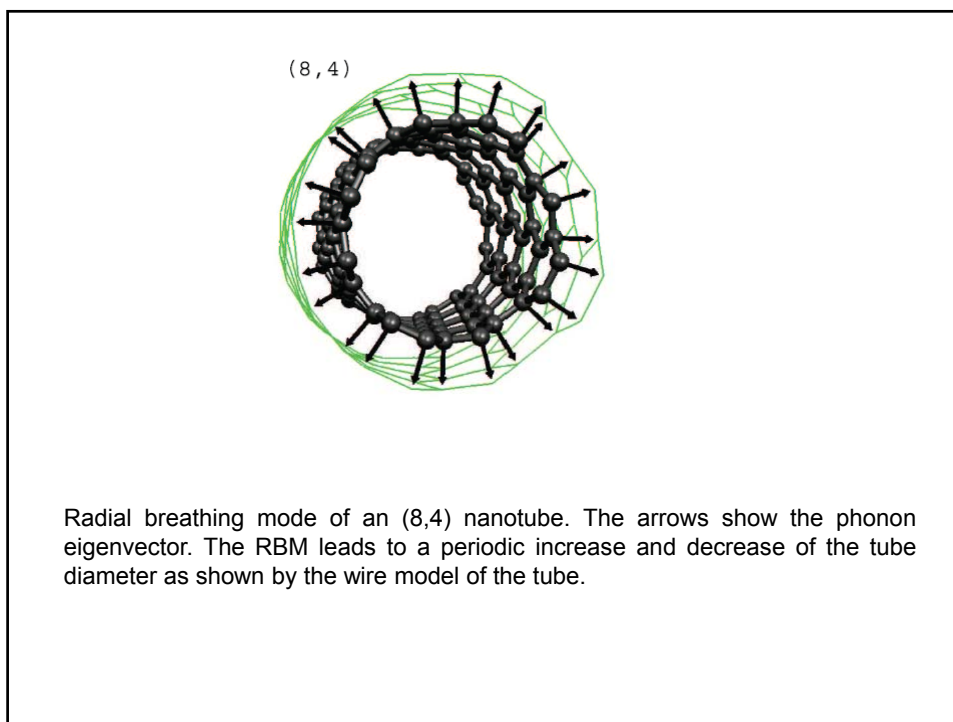
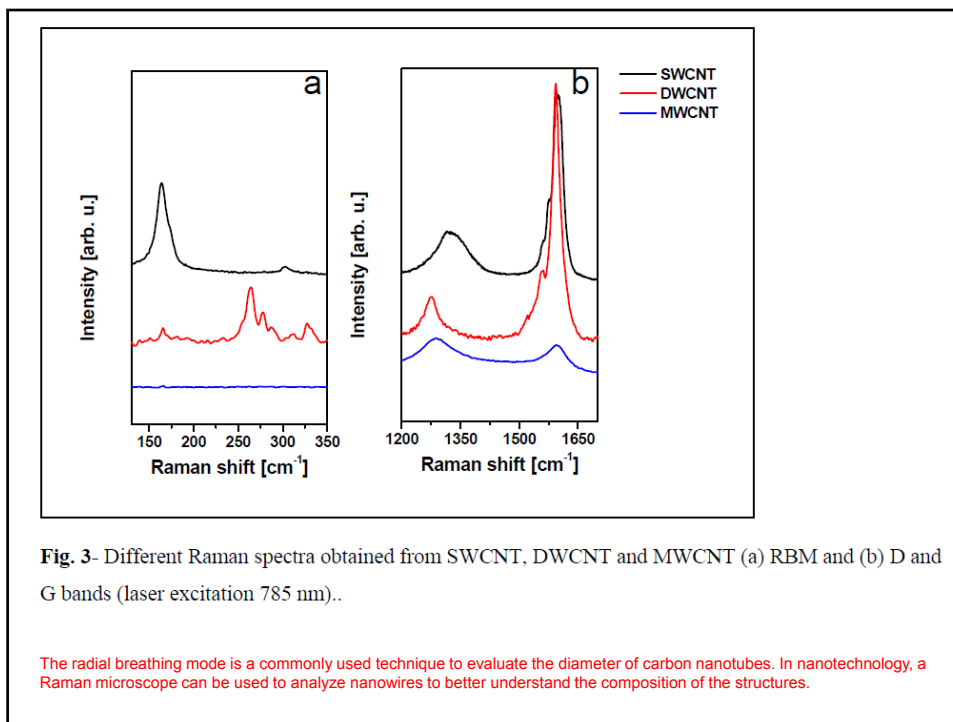
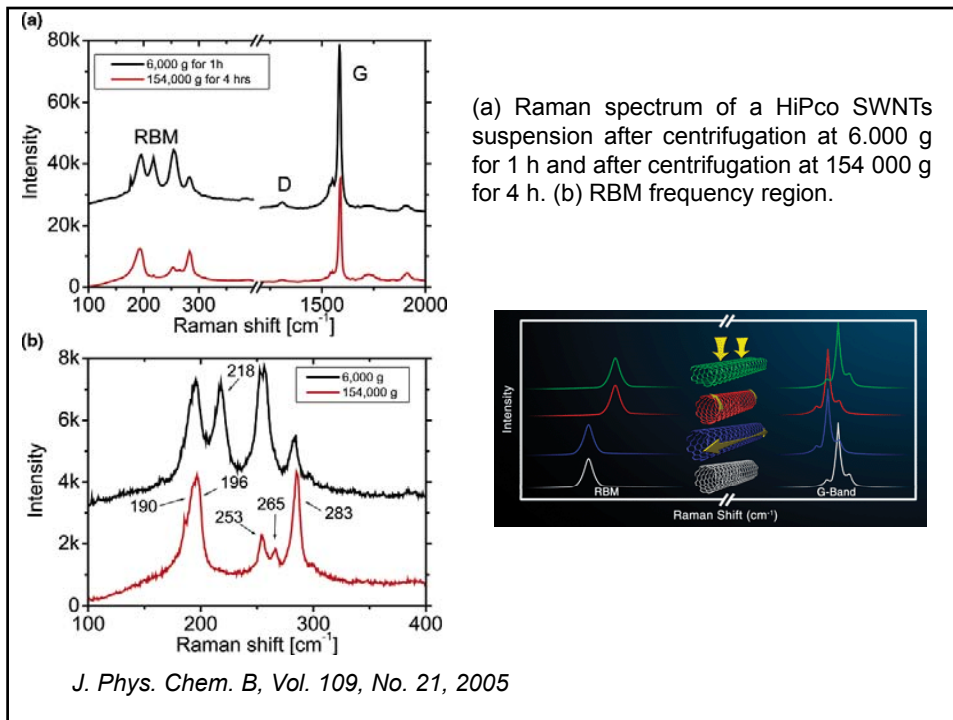


Fig. 1- (a) Different Raman spectra of SWCNT obtained from red laser (785 nm) and green laser (514 nm), (b) and its diameter distribution.





Grafeno

- Graphene is an allotrope of carbon. In this material, carbon atoms are arranged in a regular hexagonal pattern. Graphene can be described as a one-atom thick layer of the mineral graphite, (many layers of graphene stacked together effectively form crystalline flake graphite). Amongst its other well-publicised superlative properties, it is very light, with a 1-square-meter sheet weighing only 0.77 milligrams.
- The Nobel Prize in Physics for 2010 was awarded to Andre Geim and Konstantin Novoselov at the University of Manchester "for groundbreaking experiments regarding the two-dimensional material graphene". In 2013, graphene researchers led by Prof. Jari Kinaret from Sweden's Chalmers University of Technology, secured a €1 billion grant from the European Union to be used for further research into development of potential applications of graphene

Brief history of graphene

The term graphene first appeared in 1987 to describe single sheets of graphite as one of the constituents of [graphite intercalation compounds](#) (GICs). Larger graphene molecules or sheets (so that they can be considered as true isolated 2D crystals) cannot be grown even in principle. In the 1930s, Landau and Peierls (and Mermin, later) showed thermodynamics prevented 2-d crystals in free state, an article in Physics Today reads:

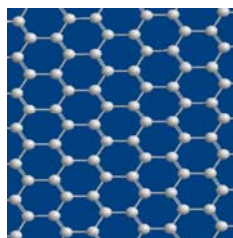
"Fundamental forces place seemingly insurmountable barriers in the way of creating [2D crystals] ... Nascent 2D crystallites try to minimize their surface energy and inevitably morph into one of the rich variety of stable 3D structures that occur in soot. But there is a way around the problem. Interactions with 3D structures stabilize 2D crystals during growth. So one can make 2D crystals sandwiched between or placed on top of the atomic planes of a bulk crystal. In that respect, graphene already exists within graphite ... One can then hope to fool Nature and extract single-atom-thick crystallites at a low enough temperature that they remain in the quenched state prescribed by the original higher-temperature 3D growth."

In **2004**: Andre Geim and Kostya Novoselov at Manchester University managed to extract single-atom-thick crystallites (graphene) from bulk graphite: Pulled out graphene layers from graphite and transferred them onto thin silicon dioxide on a silicon wafer in a process sometimes called micromechanical cleavage or, simply, the Scotch tape technique. Since 2004, an explosion in the investigation of graphene in term of synthesis, characterization, properties as well as specific potential application were reported.

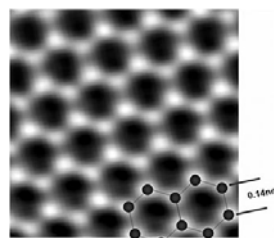
Introduction to graphene

Graphene is a one-atom-thick planar sheet of *sp²-bonded carbon* atoms that are densely packed in a honeycomb crystal lattice

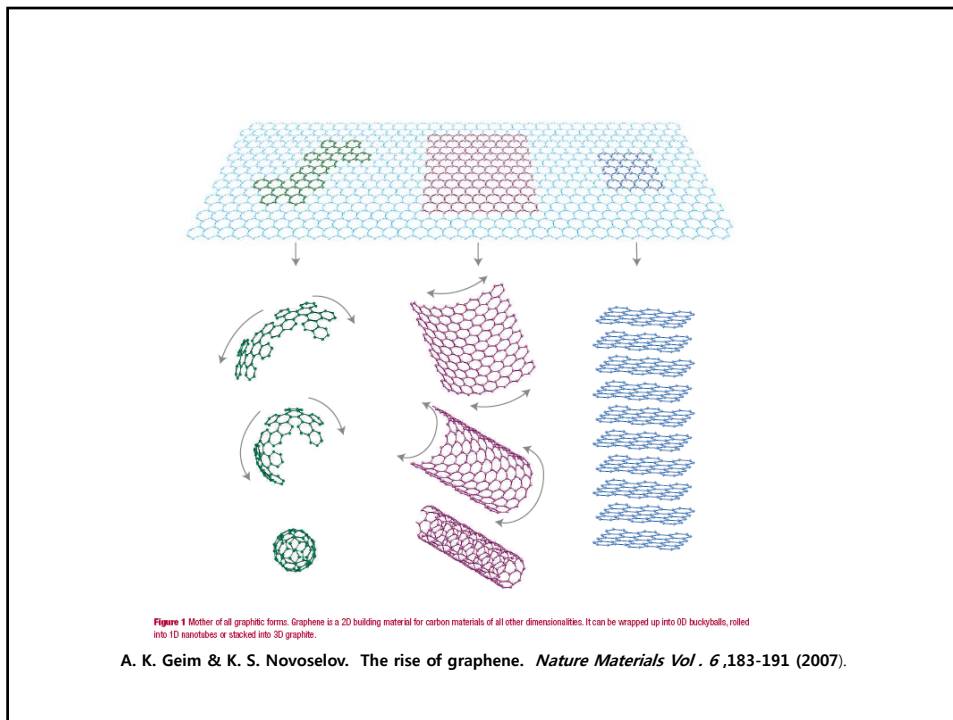
The name 'graphene' comes from [graphite](#) + *-ene* = graphene



Molecular structure of graphene



High resolution transmission electron microscope images (TEM) of graphene



Properties of graphene

- Electronic properties
- Thermal properties
- Mechanical properties
- Optical properties
- Relativistic charge carriers
- Anomalous quantum Hall effect

Electronic properties

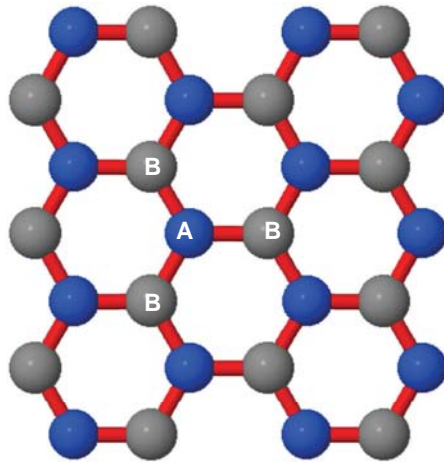
- High electron mobility (at room temperature $\sim 200.000 \text{ cm}^2/(\text{V}\cdot\text{s})$, ex. Si at RT $\sim 1400 \text{ cm}^2/(\text{V}\cdot\text{s})$, carbon nanotube: $\sim 100.000 \text{ cm}^2/(\text{V}\cdot\text{s})$, organic semiconductors (polymer, oligomer): $<10 \text{ cm}^2/(\text{V}\cdot\text{s})$)

$$\mathbf{v}_d = \mu \mathbf{E}$$

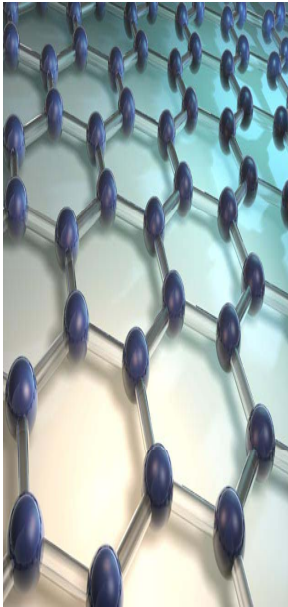
Where v_d is the drift velocity in m/s (SI units)
 \mathbf{E} is the applied electric field in V/m (SI)
 μ is the mobility in $\text{m}^2/(\text{V}\cdot\text{s})$, in SI units.

- Resistivity of the graphene sheet $\sim 10^{-6} \Omega\cdot\text{cm}$, less than the resistivity of silver (Ag), the lowest resistivity substance known at room temperature (electrical resistivity is also the inverse of the conductivity σ (*sigma*), of the material, or

$$\rho = \frac{1}{\sigma}$$

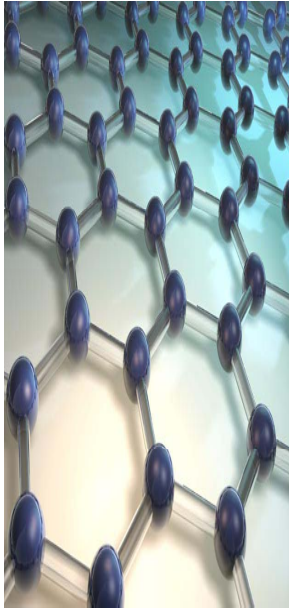


Triangular sublattices of graphene. Each atom in one sublattice (A) has 3 nearest neighbors in sublattice (B) and viceversa.



Properties

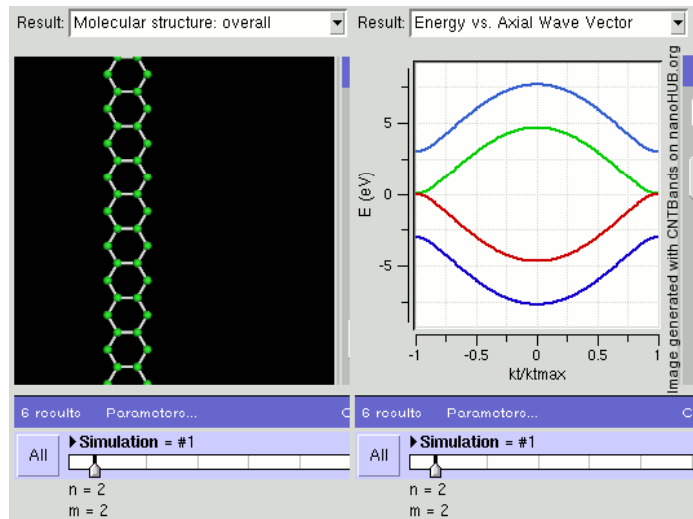
- Electronic
- Optical
- Excitonic
- Thermal
- Mechanical
- Spin transport
- Anomalous quantum Hall effect



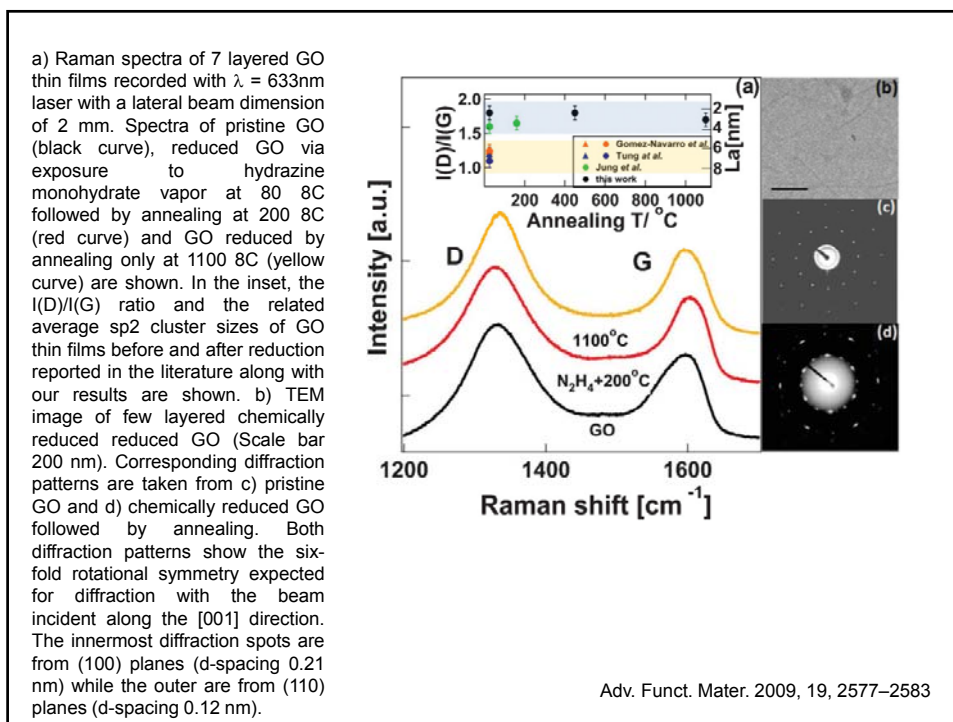
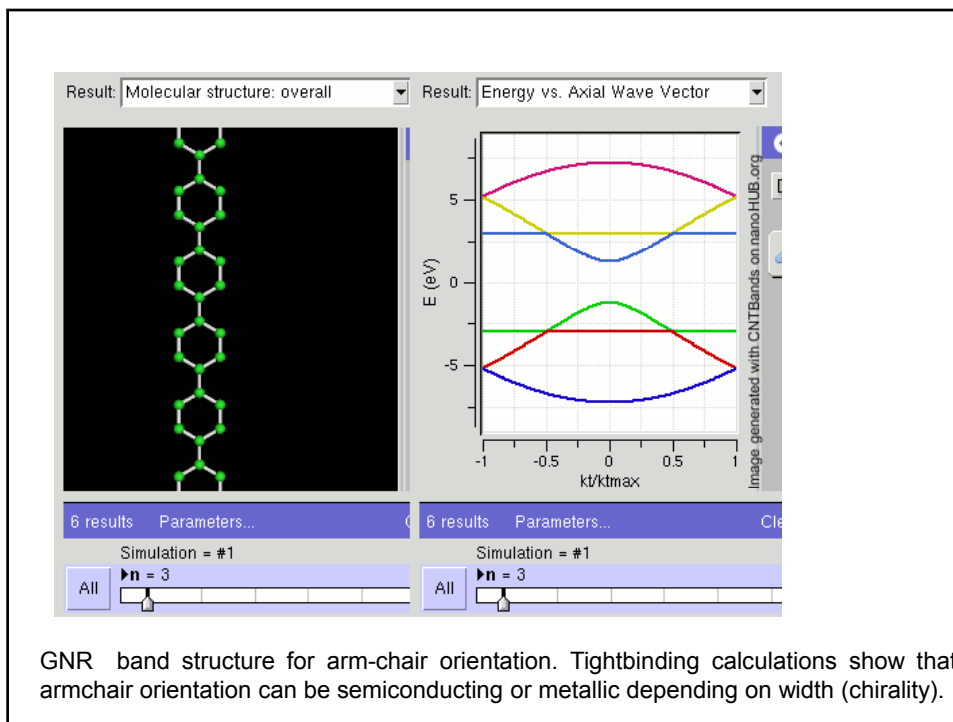
Electronic

- Intrinsic graphene is a semi-metal or zero-gap semiconductor
- remarkably high electron mobility at room temperature, with reported values in excess of $15,000 \text{ cm}^2 \cdot \text{V}^{-1} \cdot \text{s}^{-1}$.
- Fermi velocity $v_F \sim 10^6 \text{ m/s}$
- resistivity of the graphene sheet would be $10^{-6} \Omega \cdot \text{cm}$. This is less than the resistivity of silver, the **lowest resistivity substance known at room temperature!**

Electronic



GNR band structure for zig-zag orientation. Tightbinding calculations show that zigzag orientation is always metallic.

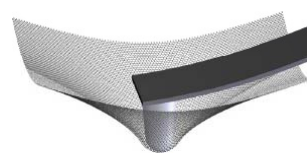


Material	Electrical Conductivity (S·m ⁻¹)	Notes
Graphene	~ 10 ⁸	
Silver	63.0 × 10 ⁶	Best electrical conductor of any known metal
Copper	59.6 × 10 ⁶	Commonly used in electrical wire applications due to very good conductivity and price compared to silver.
Annealed Copper	58.0 × 10 ⁶	Referred to as 100% IACS or International Annealed Copper Standard. The unit for expressing the conductivity of nonmagnetic materials by testing using the eddy-current method. Generally used for temper and alloy verification of aluminium.
Gold	45.2 × 10 ⁶	Gold is commonly used in electrical contacts because it does not easily corrode.
Aluminium	37.8 × 10 ⁶	Commonly used for high voltage electricity distribution cables [citation needed]
Sea water	4.8	Corresponds to an average salinity of 35 g/kg at 20 °C. [1]
Drinking water	0.0005 to 0.05	This value range is typical of high quality drinking water and not an indicator of water quality
Deionized water	5.5 × 10 ⁻⁶	Conductivity is lowest with monoatomic gases present; changes to 1.2 × 10 ⁻⁴ upon complete de-gassing, or to 7.5 × 10 ⁻⁵ upon equilibration to the atmosphere due to dissolved CO ₂ . [2]
Jet A-1 Kerosene	50 to 450 × 10 ⁻¹²	[3]
n-hexane	100 × 10 ⁻¹²	
Air	0.3 to 0.8 × 10 ⁻¹⁴	

Properties of graphene

Mechanical properties

- High Young's modulus (~1,100 Gpa)
- High fracture strength (125 Gpa)

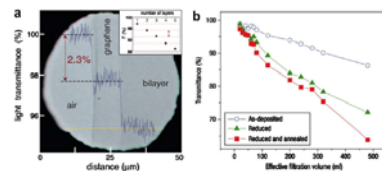


A representation of a diamond tip with a two nanometer radius indenting into a single atomic sheet of graphene (*Science*, **321** (5887): 385)

- Graphene is as the strongest material ever measured, some 200 times stronger than structural steel

Optical properties

- Monolayer graphene absorbs $\pi\alpha \approx 2.3\%$ of white light (97.7 % transmittance), where α is the fine-structure constant.



Preparation and characterization graphene

Preparation methods

Top-down approach (From graphite)

- Micromechanical exfoliation of graphite (Scotch tape or peel-off method)
- Creation of colloidal suspensions from **graphite oxide** or graphite intercalation compounds (GICs)

Bottom up approach (from carbon precursors)

- By chemical vapour deposition (CVD) of hydrocarbon
- By epitaxial growth on electrically insulating surfaces such as SiC
- Total Organic Synthesis

Table 1 – Advantages and disadvantages for techniques currently used to produce graphene.

	Advantages	Disadvantages
Mechanical exfoliation	Low cost and easy No special equipment needed, SiO ₂ thickness is tuned for better contrast	Serendipitous Uneven films Labor intensive (not suitable for large-scale production)
Epitaxial growth	Most even films (of any method) Large scale area	Difficult control of morphology and adsorption energy High-temperature process
Graphene oxide	Straightforward up-scaling Versatile handling of the suspension Rapid process	Fragile stability of the colloidal dispersion Reduction to graphene is only partial

Ref: Carbon, 48, 2127–2150 (2010)

Characterization methods

Scanning Probe
Microscopy (SPM):

Raman
Spectroscopy

Transmission electron
Microscopy (TEM)

X-ray diffraction
(XRD)

- Atomic force microscopes (AFMs)
- Scanning tunneling microscopy (STM)

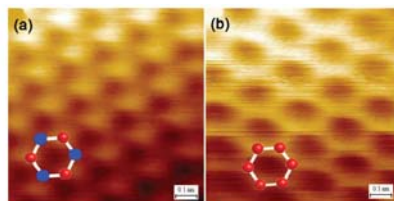
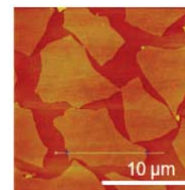
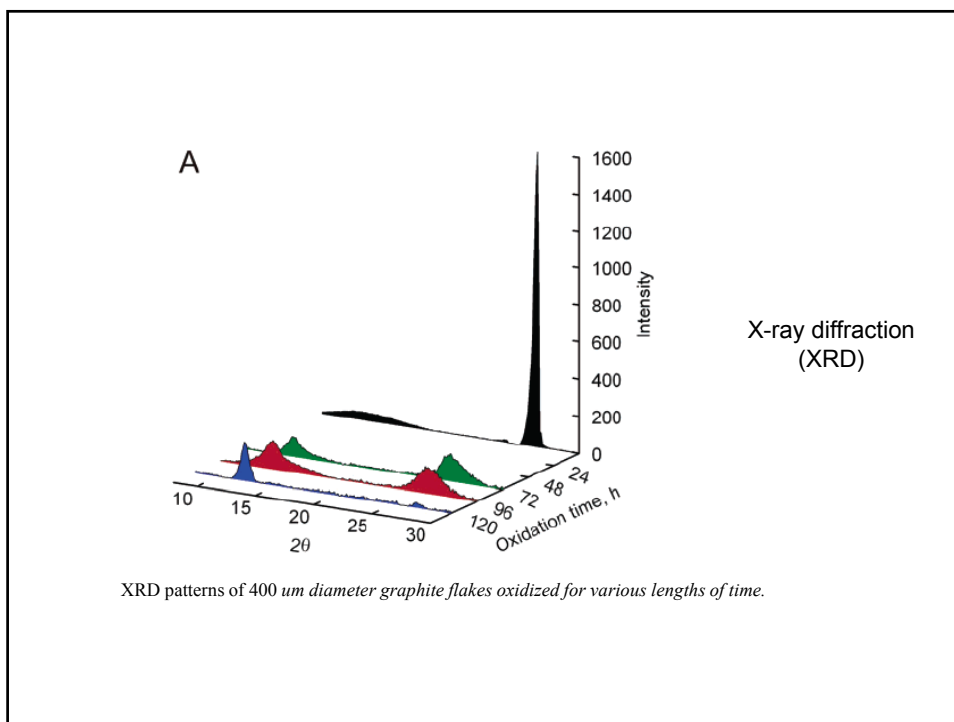
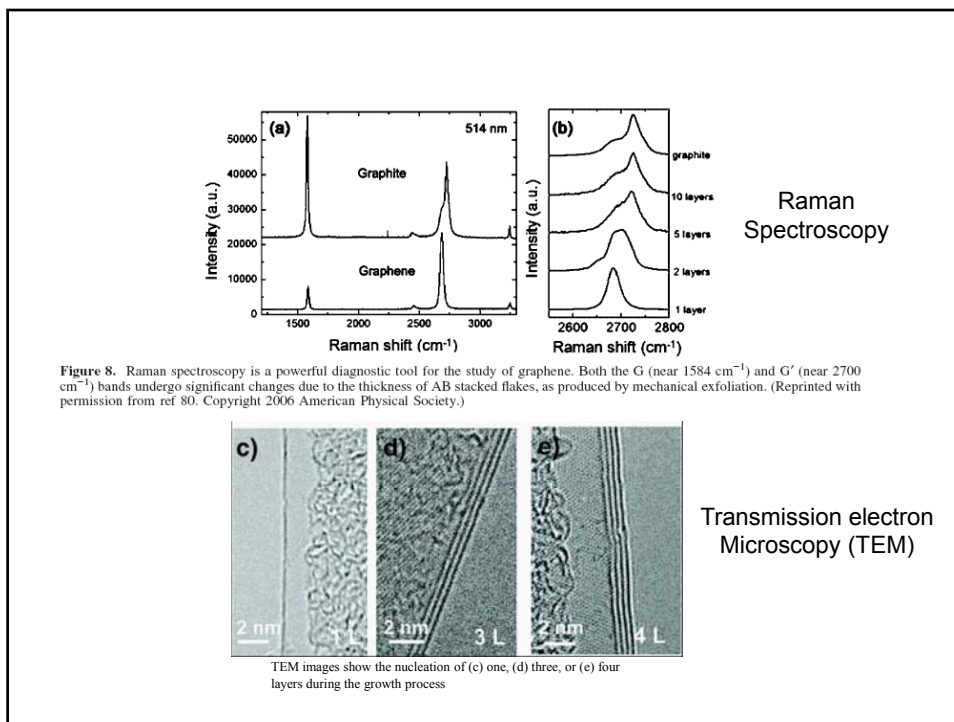


Figure 7. (a) STM image of graphite showing only the three carbons that eclipse a neighbor in the sheet directly below. (b) In contrast, all six carbons are equivalent and thus visible in mechanically exfoliated single-layer graphene. (Reprinted with permission from ref 79. Copyright 2007 PNAS.)



Atomic force microscopy images of a graphene oxide film deposited by Langmuir-Blodgett assembly



Preparation methods and discussions

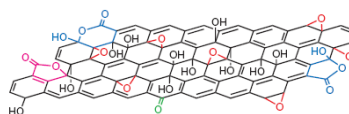
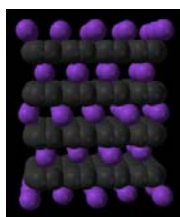
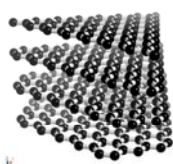


Top-down approach
(From graphite)

Direct exfoliation of
graphite

Graphite intercalation compound

Graphite oxide method



Nature nanotechnology, vol 4, APRIL (2009)

Table 1 | Comparison of a set of chemical approaches to produce colloidal suspensions of CMG sheets

Ref.	Starting materials	Dispersible solvents	Concentration (mg ml ⁻¹)	Lateral size	Thickness (nm)
34	GO/MH	Water	1	—	—
36	GO/MH	Water	0.5	Several hundred nm	-1
39	GO/MH	Water	0.1	—	-1.7
40	GO/MH	Water	7	Several hundred nm	-1
42	GO/H	Water/methanol, acetone, acetonitrile mixed solvents	3-4	Several hundred nm	-1.2
45	GO/MH	DMF, NMP, DMSO, HMPA	1	~560 nm	-1
46	GO/H	Water, acetone, ethanol, 1-propanol, ethylene glycol, DMSO, DMF, NMP, pyridine, THF	0.5	100-1,000 nm	1.0-1.4
49	GO/O	DMF, THF, CCl ₄ , DCE	0.5	—	0.5-2.5
50	Graphite fluoride	DCB, MC, THF	0.002-0.54	1,600 nm	-0.95
51	GO/S	DMF, DMAc, NMP	1	Several hundred nm	1.8-2.2
52	GO/MH	Hydrazine	1.5	Up to 20 μm x 40 μm	-0.6
54	GO/S	THF	<0.48	—	1-2
55, 56, 10	GO/S	NMP, DMF, DCB, THF, nitromethane	0.1	100-2,500 nm	1.1-3.5 (ave. 1.75)
57	GO/H	Ethanol	1	Several hundred nm	-2
59	Graphite powder	NMP, DMAc, GBL, DMEU	0.01	Several μm	1-5
60	GIC	NMP	0.15	Several hundred nm	-0.35
61	EG	DCE	0.0005	Nanoribbon (width <10 nm)	1-1.8
62	EG	DMF	—	~250 nm	-1
63	EG	Water, DMF, DMSO	0.015-0.020	Several hundred nm to a few μm	2-3 (2-3 layers of graphene)
64	Graphite rod	DMF, DMSO, NMP	1	500-700 nm	-1.1

GO, graphite oxide; MH, modified Hummers method; H, Hummers method; O, their own method; S, Staudenmaier method; EG, expandable graphite; GIC, graphite intercalation compound; DMF, dimethylformamide; DMAc, N,N-dimethylacetamide; DMSO, dimethylsulphoxide; NMP, N-methylpyrrolidone; THF, tetrahydrofuran; MC, dichloromethane; DCE, 1,2-dichloroethane; DCB, 1,2-dichlorobenzene; HMPA, hexamethylphosphoramide; GBL, γ-butyrolactone; DMEU, 1,3-dimethyl-2-imidazolidinone.

Direct exfoliation of graphite

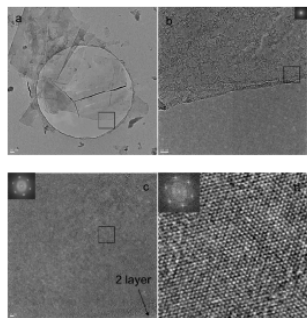


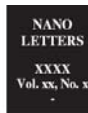
Figure 1. TEM images of single layer graphene from HOPG dispersion showing (a) monolayer and few layer of graphene stacked with smaller flakes; (b) selected edge region from (a); (c) selected area from (b) with FFT inset; (d) HRTEM of boxed region in (c) showing lattice fringes with FFT inset.

High-Yield Organic Dispersions of Unfunctionalized Graphene

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Richard E. Smalley Institute for Nanoscale Science and Technology and Department of Chemistry, Rice University, Houston, Texas 77005

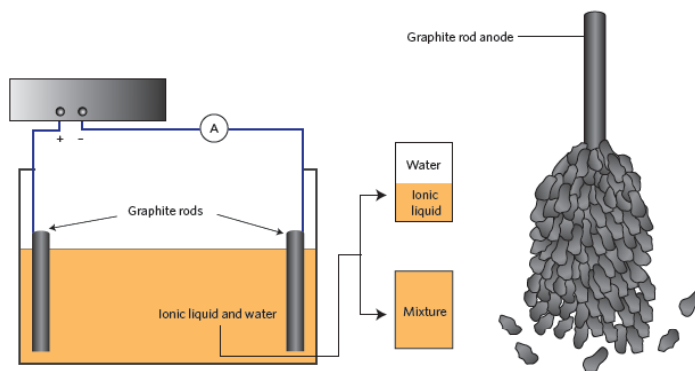
Received May 20, 2009; Revised Manuscript Received July 12, 2009



We demonstrate herein a simple, high-yield method of producing homogeneous dispersions of graphene nanosheets in ortho-dichlorobenzene (ODCB) from various graphite materials. The advantage of our method lies in its high yield, its simplicity, and its avoidance of harsh oxidation chemistry.

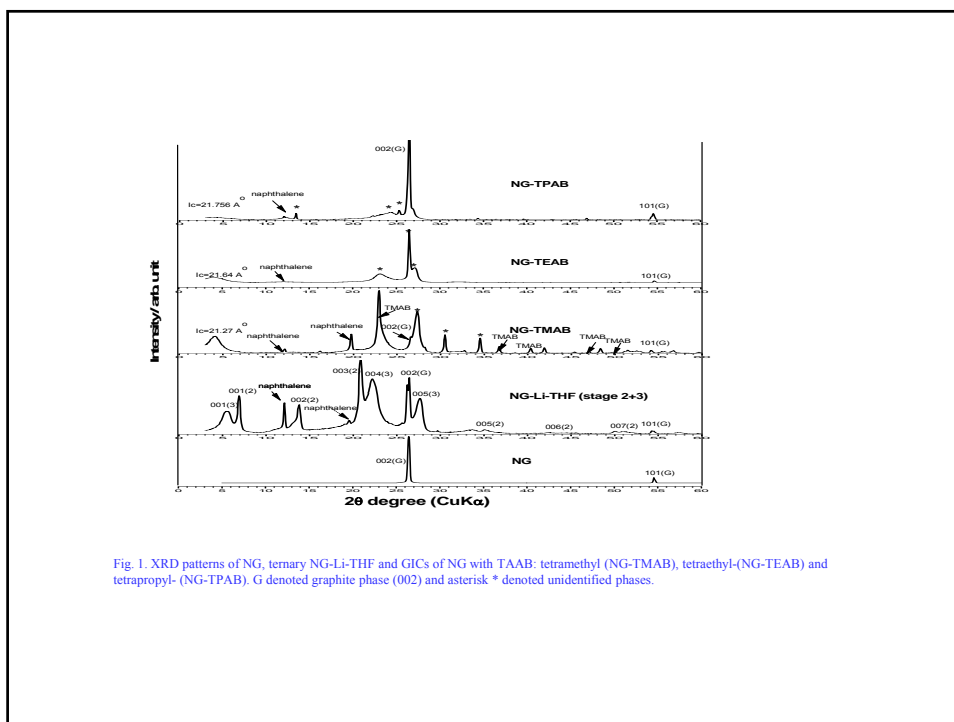
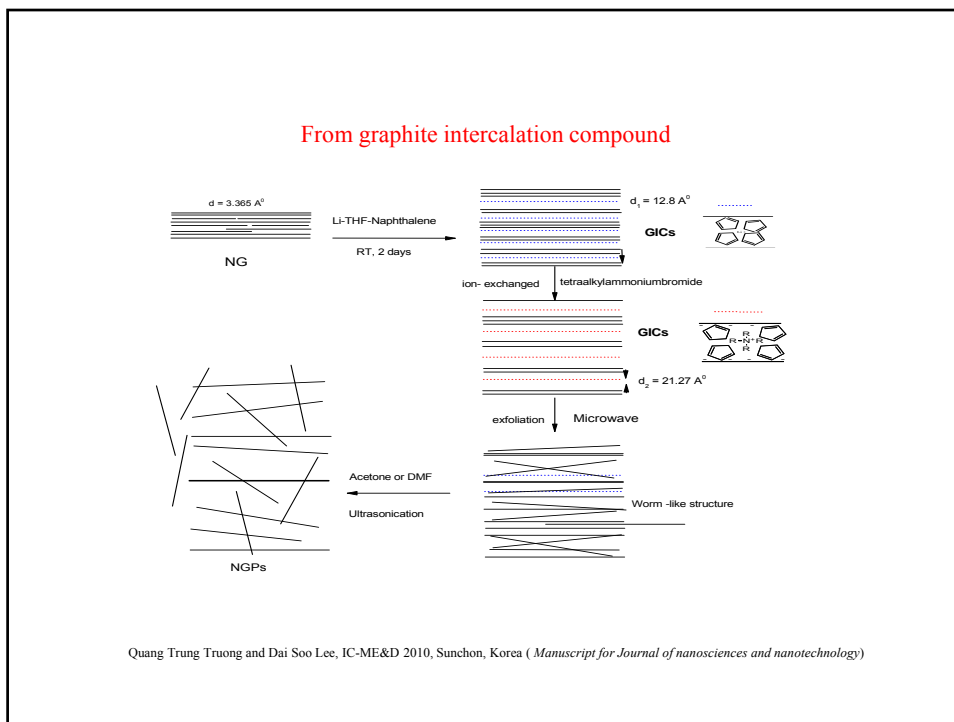
Dispersions of microcrystalline synthetic graphite have a concentration of 0.03 mg mL⁻¹. Dispersions of expanded graphite and HOPG are less concentrated (0.02 mg mL⁻¹).

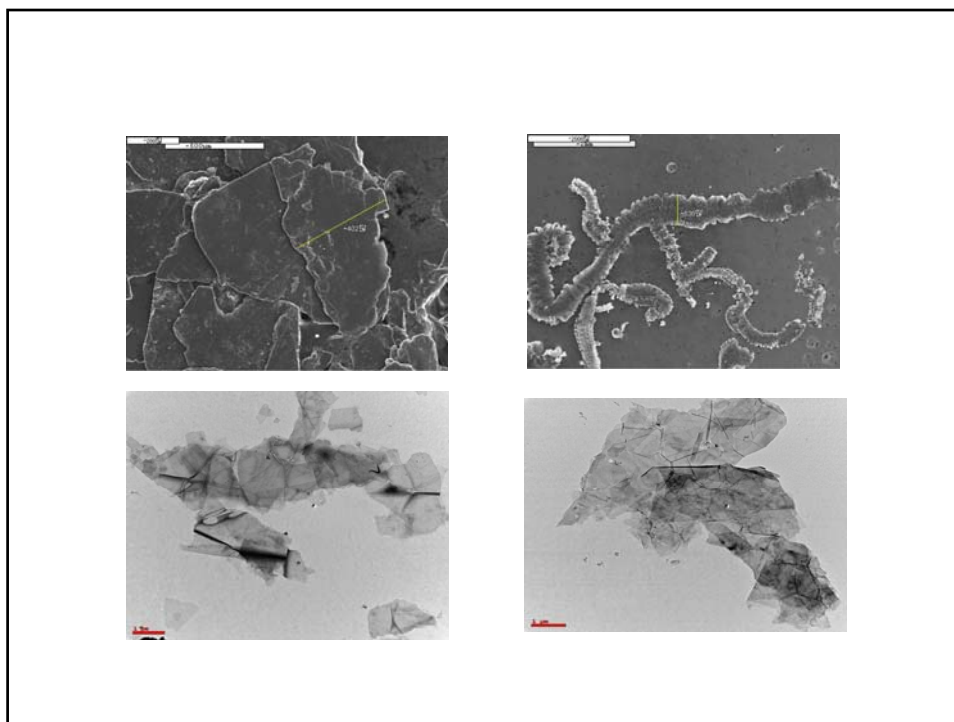
Direct exfoliation of graphite



Graphene sheets ionic-liquid-modified by electrochemistry using graphite electrodes.

Liu, N. *et al.* One-step ionic-liquid-assisted electrochemical synthesis of ionic-liquid-functionalized graphene sheets directly from graphite. *Adv. Funct. Mater.* **18**, 1518–1525 (2008).





Graphite intercalation compound

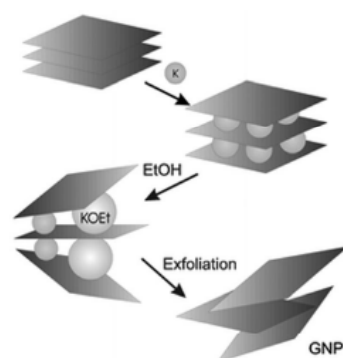
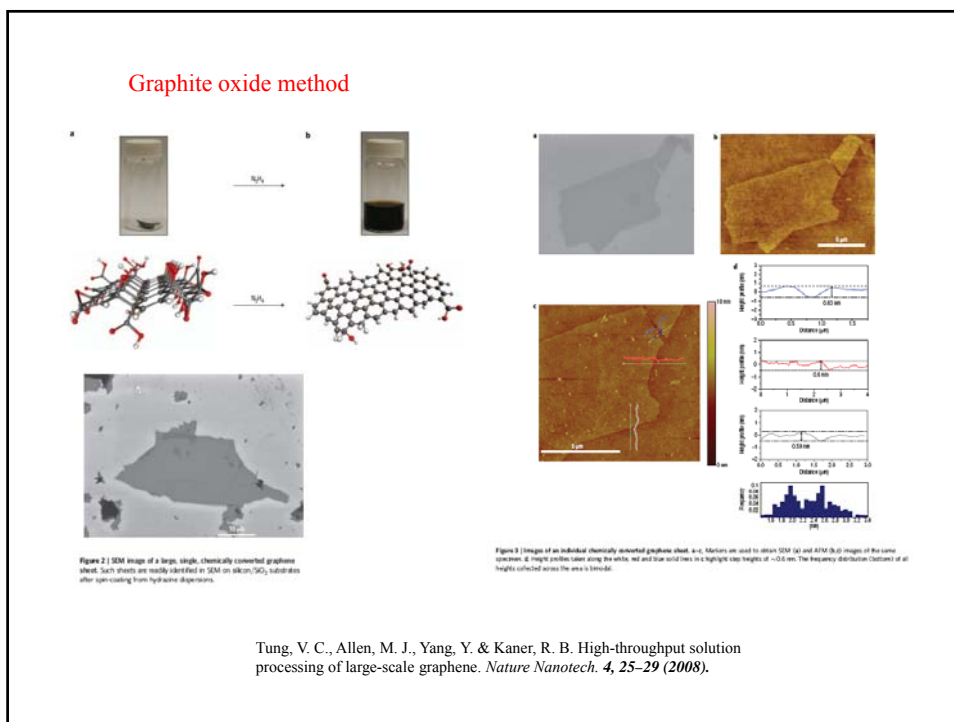
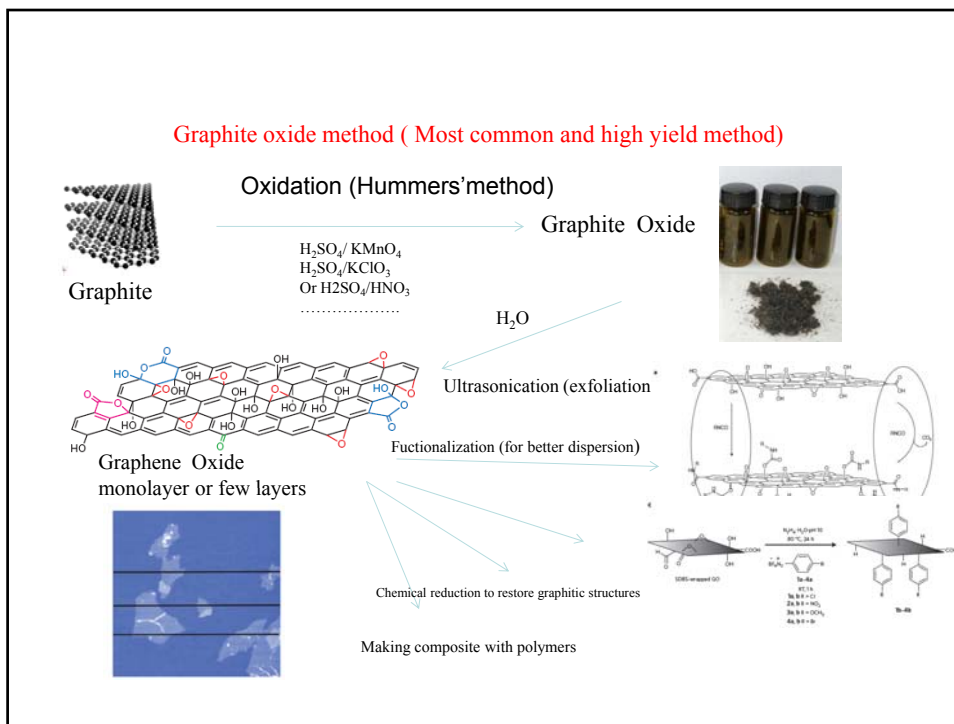
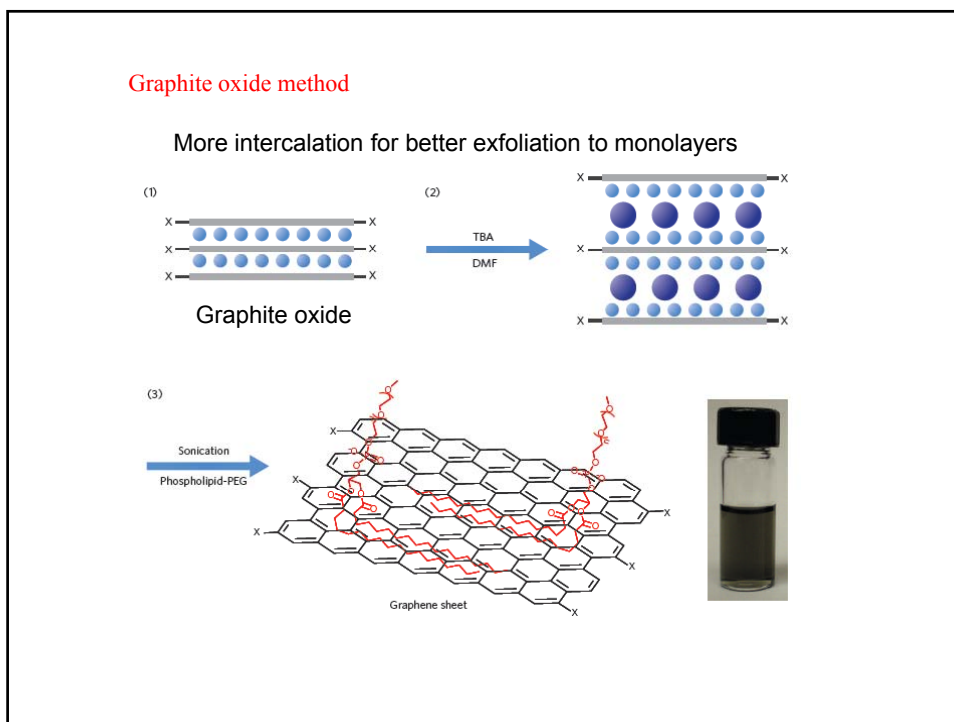
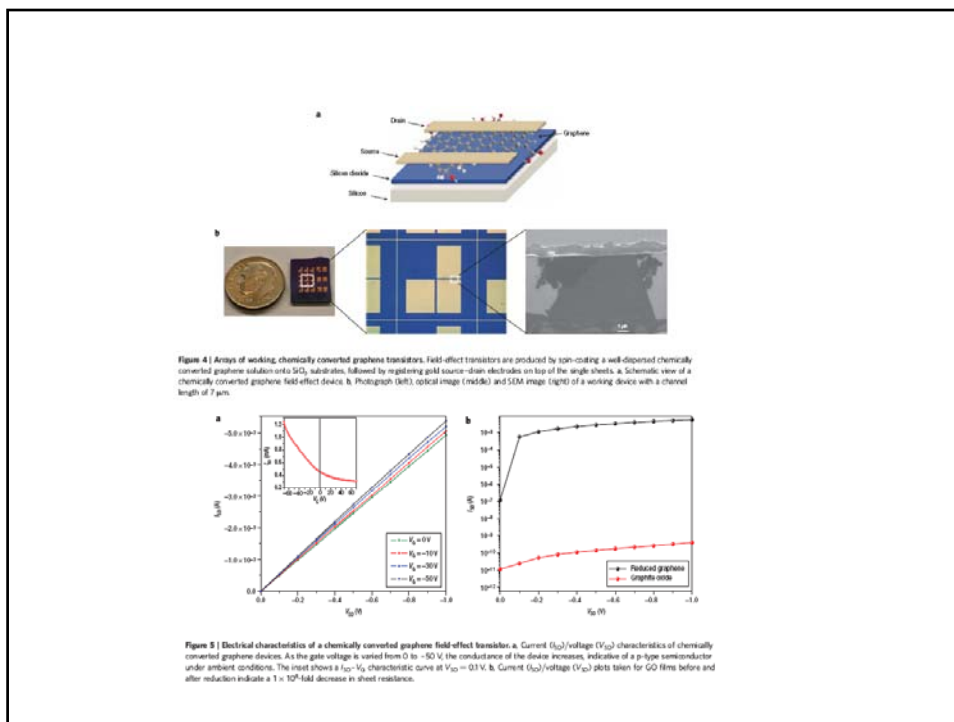


Figure 2. Schematic diagram showing the intercalation and exfoliation process to produce thin slabs of graphite. Potassium is inserted between the layers and reacted violently with alcohols. The exfoliated slabs are ~30 layers thick. (Reprinted with permission by The Royal Society of Chemistry from ref 60.)

J. Mater. Chem. **2005**, *15*, 974.



Tung, V. C., Allen, M. J., Yang, Y. & Kaner, R. B. High-throughput solution processing of large-scale graphene. *Nature Nanotech.* **4**, 25–29 (2008).



Bottom up approach (from carbon precursors)

Table 2 - Synoptic table of the graphene growth methods on both metals and carbides substrates. Acronyms are as follows: 1L, single layer coverage; ML, monolayer; T, temperature; STM, scanning tunneling microscopy; LEED, low-energy electron diffraction; AES, Auger electron spectroscopy; AFM, atomic force microscopy; PCIM, point-contact microscopy; XPS, X-ray photoemission spectroscopy; ARUPS, angle-resolved ultraviolet photo-electron spectroscopy; SELLFS, surface extended-energy-loss fine-structure; SEM, scanning electron microscopy; XPD, X-ray photoelectron diffraction; TDS, time-domain spectroscopy; LEIS, low-energy ion spectroscopy.

Substrate	Growth condition (gas, T, exposure)	Experimental technique	Edges	Comment ($a_c = 0.245$ nm)	Ref.		
Metals	Pt(111) Benzene (C_6H_6), T = 1000 K. 1-5L non-graphitic film; >5L full coverage	STM, LEED, AES	Hexagonal arrangement beyond edges		[83]		
		Ethylene (C_2H_4), T = 800 K. 5L exposure (if T > 1000 K: graphitic island)	LEED, STM	No clear hexagonal arrangement; No growth over the edges	$a_{Pt} = 0.278$ nm $a_{Metal} = 2.2$ nm	[55]	
	Ni(111)	HOPG on 1ML graphitic film	AFM, PCIM	Continuous film from upper terrace to lower terrace	0.738 nm < a < 2.1 nm	[239]	
		Chemical vapor deposition	LEED, XPS, ARUPS	Formation of large sheet		[240]	
Ni(110)	Carbon monoxide (CO), T = 600 K. 90000L exposure	SELLFS		Evidence of Fuchs-Klewer phonons	[87]		
Ru(001)	Ethylene (C_2H_4), T = 1270 K. T-dependent solubility gradient	LEEM, SEM, μ -Raman, AES, electrical	No growth "uphill" over the edges	$a_{Ru} = 0.271$ nm a = 0.145 nm (1st layer)	[56]		
Ir(111)	Ethylene (C_2H_4), T > 1100 K. 1L exposure	STM	Growth beyond both side of the edges	$a_{Ir} = 0.272$ nm	[86]		
Co(0001)	Acetylene (C_2H_2), T = 410 K. 0.6L-3.6L exposure	XPS, XPD, LEED, TDS, LEIS		$a_{Co} = 2.5$ nm K enhances the coverage of the surface	[242]		
Carbides	nH-SiC (n = 1, 2, ...) Si sublimation, T ~ 1670 K.	LEED, X-ray, STM	Formation of large continuous sheet over terraces		[69]		
		TiC(111)	Chemical Vapor Deposition on faceted surface, T = 1770 K	XPS, ARUPS, LEED	No edge-localized state	Growth on each facet	[78]
		TiC(410)	Chemical Vapor Deposition on platelets surface, T = 1770 K	XPS, ARUPS, LEED	No growth over the edges	Nanoribbon growth (~1-2 nm)	[78]
		TaC(111)	Ethylene (C_2H_4), T = 1570 K. 10000L exposure, T = 1270 K	AES, LEED, STM	Coverage is interrupted at terrace interface	a = 0.249 nm (1st layer) a = 0.247 nm (2nd layer)	[80]

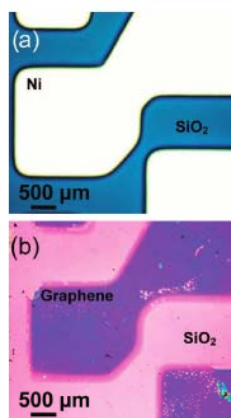


Fig. 5 - Nickel-grown graphene. (a) Optical image of a pre-patterned Ni film on SiO_2/Si . CVD graphene is grown on the surface of the Ni pattern. (b) Optical image of the grown graphene transferred intact from the Ni surface in (a) to another SiO_2/Si substrate. Reproduced with permission from Ref. [58]. Copyright 2009 American Chemical Society.

Total Organic Synthesis

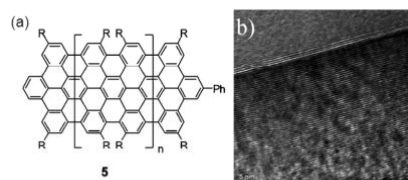
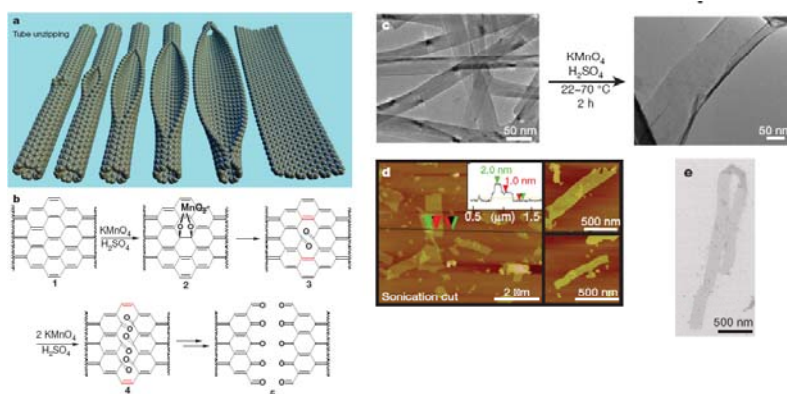


Figure 17. Polyacyclic aromatic hydrocarbons (PAHs) may offer a ground-up synthesis of graphene. (a) Chemical structure of PAHs and (b) TEM of a nanoribbon synthesized by Mullen. (Reprinted with permission from ref 35. Copyright 2008 American Chemical Society.)

Yang, X. Y.; Dou, X.; Rouhanipour, A.; Zhi, L. J.; Rader, H. J.; Mullen, K. *J. Am. Chem. Soc.* **2008**, *130*, 4216.

Graphene nanoribbons
(from carbon nanotube)

NATURE, Vol , 458, 16 , April (2009)

Potential application of graphene

- Single molecule gas detection
- Graphene transistors
- Integrated circuits
- Transparent conducting electrodes for the replacement of ITO
- Ultracapacitors
- Graphene biodevices
- Reinforcement for polymer nanocomposites:
Electrical, thermally conductive nanocomposites,
antistatic coating, transparent conductive
composites..ect

Electrical, thermally conductive nanocomposites

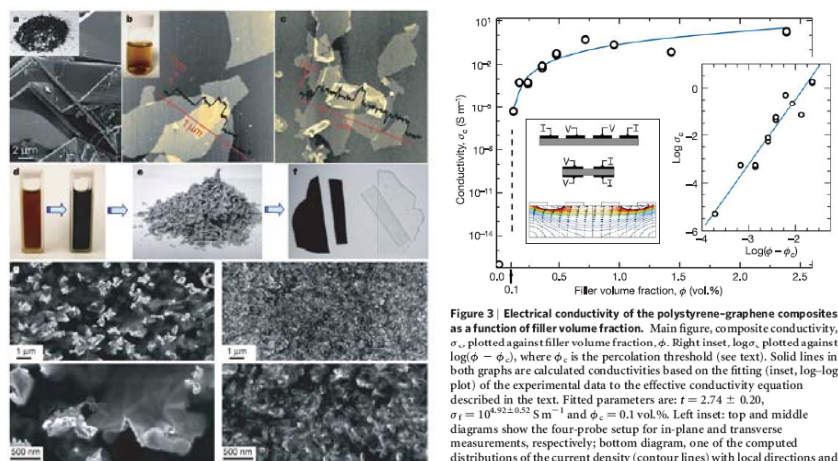
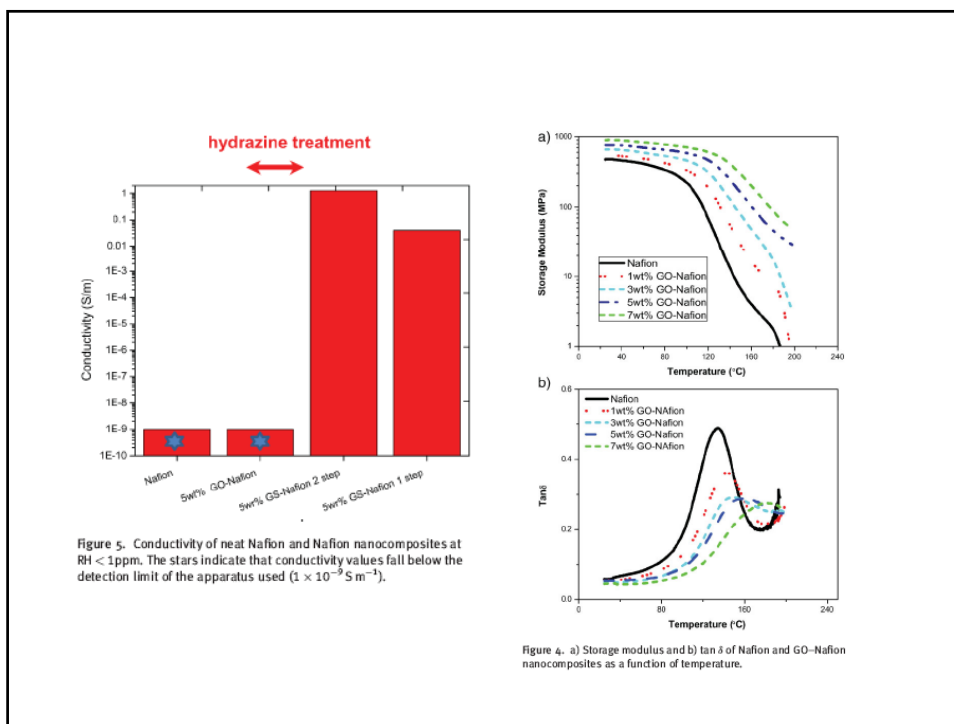
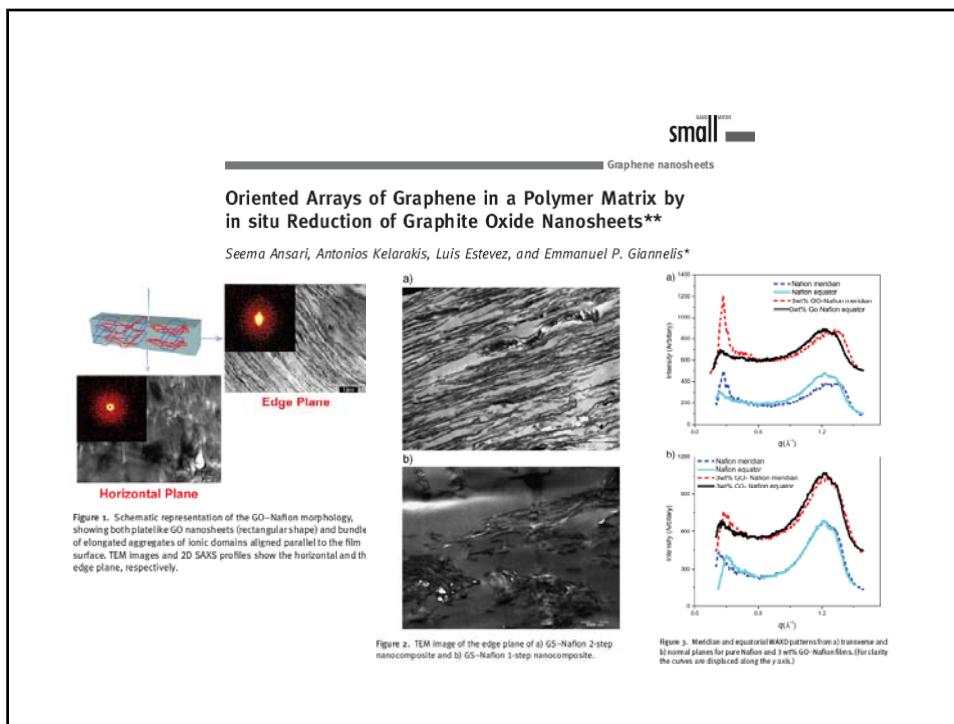
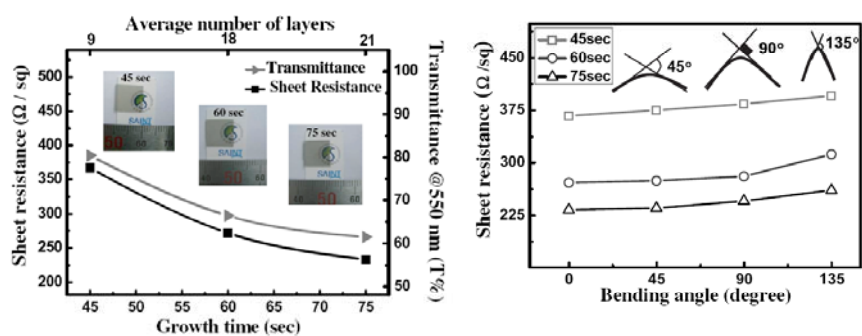


Figure 3 | Electrical conductivity of the polystyrene-graphene composites as a function of filler volume fraction. Main figure, composite conductivity, σ_c , plotted against filler volume fraction, ϕ . Right inset, $\log \sigma_c$ plotted against $\log(\phi - \phi_c)$, where ϕ_c is the percolation threshold (see text). Solid lines in both graphs are calculated conductivities based on the fitting (inset, log-log plot) of the experimental data to the effective conductivity equation described in the text. Fitted parameters are: $t = 2.74 \pm 0.20$, $\sigma_f = 10^{4.92 \pm 0.52} \text{ S m}^{-1}$ and $\phi_c = 0.1 \text{ vol.}\%$. Left inset: top and middle diagrams show the four-probe setup for in-plane and transverse measurements, respectively; bottom diagram, one of the computed distributions of the current density (contour lines) with local directions and magnitude (shown by arrows) in a specimen for the following conditions—the sample thickness is twice the electrode width and the gap between them, and the in-plane resistivity is 10 times lower than the transverse resistivity.

Nature, Vol. 442, 20, July (2006)



Transparent conducting electrodes

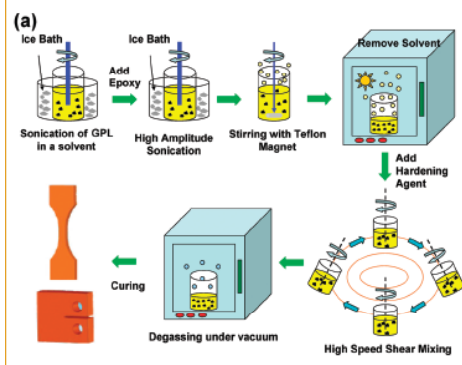


(a)

Table 1. Comparison of our results with other transparent conducting film properties of sheet resistance, transmittance, and thickness.

Transparent conducting film by	Sheet resistance (Ω/sq)	Transmittance (%)	Thickness (nm)	References
CVD graphene	367	80	~3	
	272	66	~6	
	233	62	~7	
HOPG (monolayer)	29.4	97.7	0.34	Nair ¹⁹
Reduced graphite-oxide	1800	65	10–11	Wang ¹³
	1900	90	8.1	Becerril ²⁰
Carbon nanotube	50	~68	40	Contreras ²¹
	30	~75	50	Wu ²²
	40–70	70–80	40–60	Geng ²³
	200	85	30	Rowell ²⁴

Reinforcement for polymer nanocomposites



ACS Nano, 2009, 3 (12), pp 3884–3890

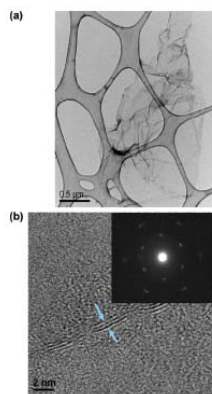


Figure 1. (a) TEM image of a GPL flake deposited on a standard TEM grid, and (b) HRTEM image of the edges of a GPL flake indicating the layered graphene platelet structure. The inset shows the measured electron diffraction pattern.

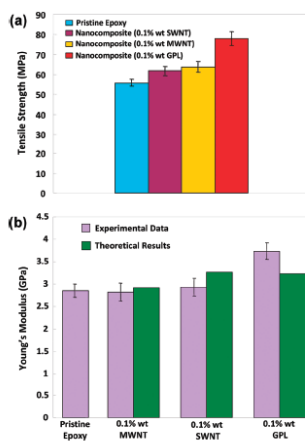
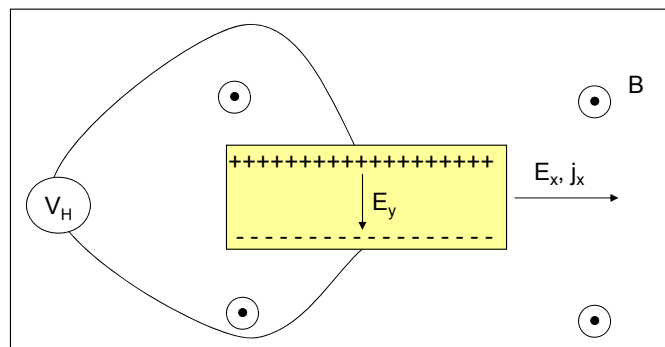


Figure 3. Uniaxial tensile testing. (a) Ultimate tensile strength for the baseline epoxy and GPL/epoxy, MWNT/epoxy, and SWNT/epoxy nanocomposites. The weight fraction of nanofillers for all of the nanocomposite samples tested was fixed at ~0.1%. (b) Young's modulus of nanocomposite samples with ~0.1% weight of GPL, ~0.1% weight of SWNT, and ~0.1% weight of MWNT is compared with the pristine (i.e., unfilled) epoxy matrix. Theoretical predictions using the Halpin–Tsai theory for the nanocomposite samples are also shown in the figure. The error in estimation of weight fraction for the various nanocomposite samples is estimated to be less than $\pm 0.002\%$.

Quantum Hall Effect

- Integral Quantum Hall effect can be accurately modeled as a non-interacting electron gas in a magnetic field
- The Fractional Quantum Hall effect involves composite fermion quasi-particles which are electrons with attached flux quanta

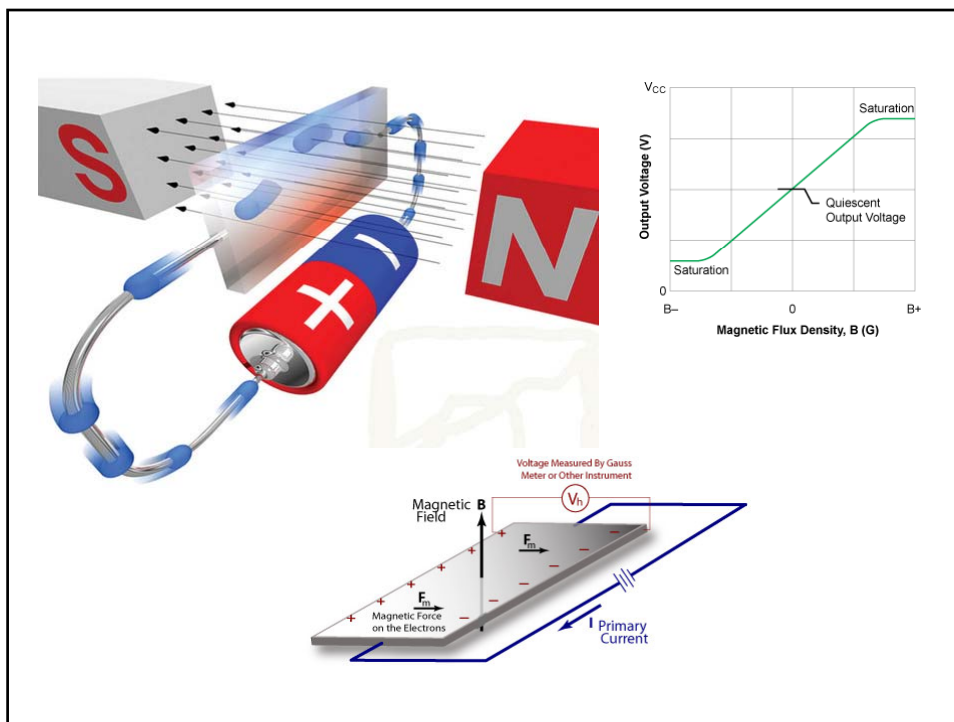
Classical Hall Effect



Experimental Values*

Metal	R_H ($-1/nec$)
Li	0.8
Na	1.2
Rb	1.0
Ag	1.3
Be	-0.2

$$E_y = -\left(\frac{1}{c} \times \mathbf{v} \times \mathbf{B}\right)_y \longrightarrow R_H = \frac{E_y}{j_x B} = \frac{1}{nec}$$

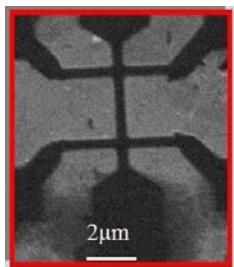


Integer QHE

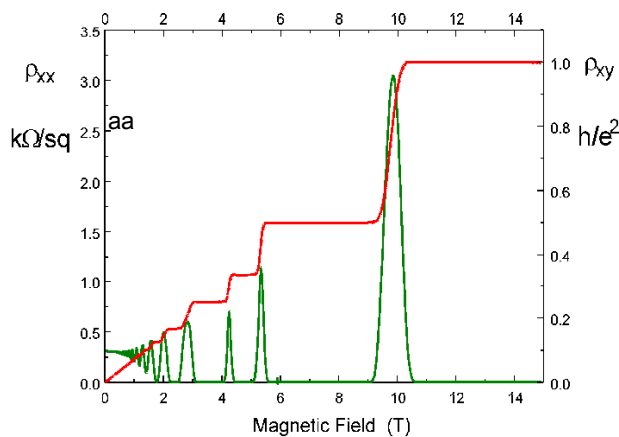
Discovered in 1980,

Nobel Prize awarded to von Klitzing in 1985

$$\rho = \begin{bmatrix} 0 & -h/e^2 \\ h/e^2 & 0 \end{bmatrix}$$



SEM image of a Hall bar*



Quantum Mechanical Description

$$\hat{H}\psi = E\psi = \frac{1}{2m} \left(\mathbf{p} - \frac{e}{c} \mathbf{r} A \right)^2 \psi \quad \text{Landau Gauge: } A = -By\hat{x}$$

$$= \frac{1}{2m} \left[(p_x - eBy)^2 + p_y^2 \right] \psi$$

$$\psi = e^{ik_x x} \phi(y) \longrightarrow H(e^{ik_x x} \phi) = \frac{\omega_c}{2} \left[-l^2 \partial_y^2 + \left(\frac{y}{l} - lk_x \right)^2 \right] e^{ik_x x} \phi = E e^{ik_x x} \phi$$

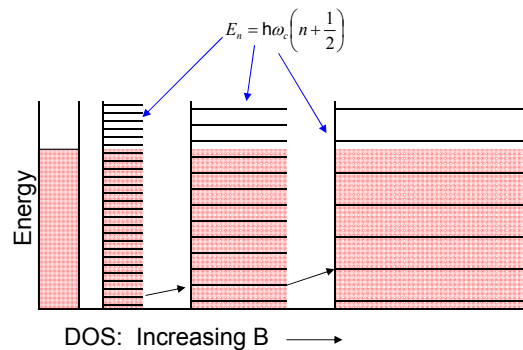
$$l \equiv \left(\frac{\hbar c}{eB} \right)^{1/2}, \quad \omega_c^2 = \frac{eB}{mc}$$

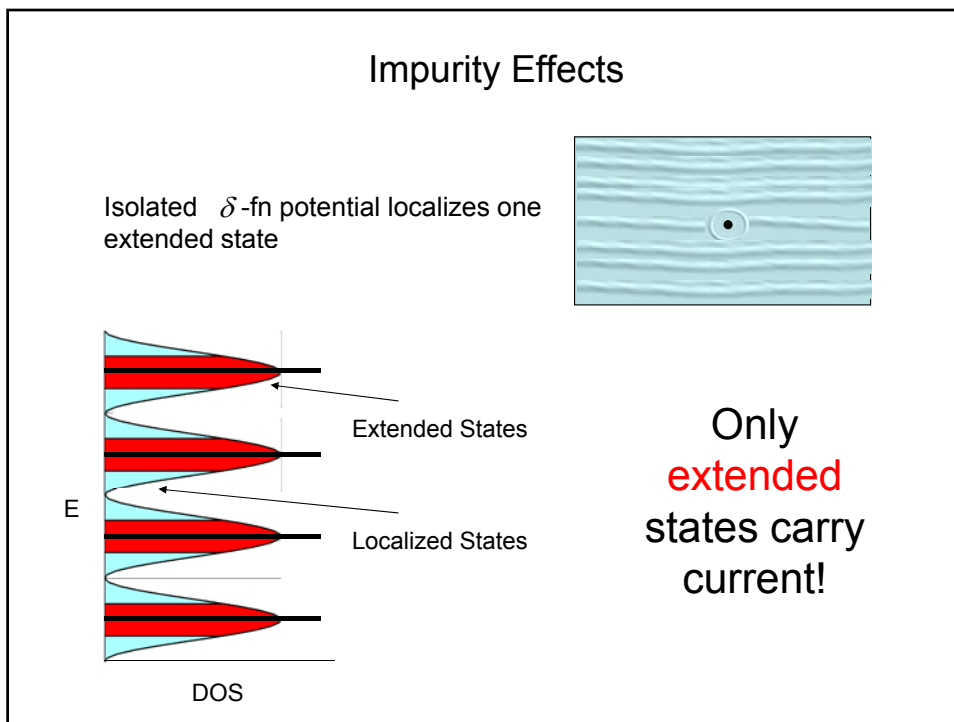
Degeneracy of Landau Levels

Each wavefunction is centered at $y = l^2 k_x$

$$0 < y < W \longrightarrow 0 < k_x < \frac{W}{l^2}, \quad k_x = \frac{2\pi}{L} n$$

$$0 < n < \frac{LW}{2\pi l^2}$$





The Laughlin Argument for the Integer Hall effect

Form a closed loop w/ Hall bar

$$j_x = -\frac{\partial \langle H \rangle}{\partial A_x} \rightarrow I_x = -\frac{d \langle H \rangle}{d \Phi}$$

Change the flux through the loop by one quanta: $\Delta \Phi = \Phi_0 = \frac{h}{e}$

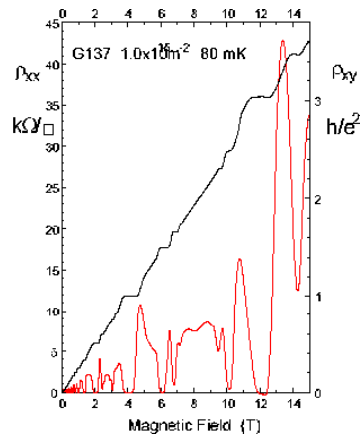
No change can take place in the bulk –
move one electron to the other edge

$$\Delta \langle H \rangle = -pe[V(W) - V(0)]$$

$$I_x = p \frac{e^2}{h} (V_y) \rightarrow \sigma_{xy} = p \frac{e^2}{h}$$

p must be an integer

Fractional QHE



Filling factor is a rational fraction

$$\sigma_{xy} = \nu \frac{e^2}{h}, \nu = \frac{p}{q}$$

Cannot be explained in terms of free electrons

Composite Fermion Picture

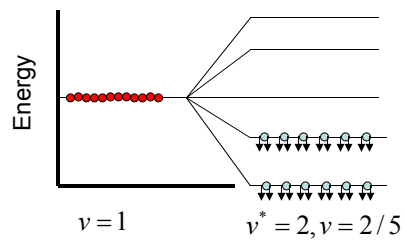
Electrons \longrightarrow IQHE
 Composite Fermions \longrightarrow FQHE

Fractional Hall effect encompasses states with filling factors: $\nu = \frac{\nu^*}{2p\nu^* \pm 1}$

Composite fermions can be viewed as electrons with attached flux quanta

$$\vec{B} \text{ is screened to } \vec{B}^* = \vec{B} - 2pe\Phi_0$$

Lowest Landau level splitting for composite fermions



$\nu=1$ lowest Landau Level splits into levels separated by $\hbar\omega_c^*$

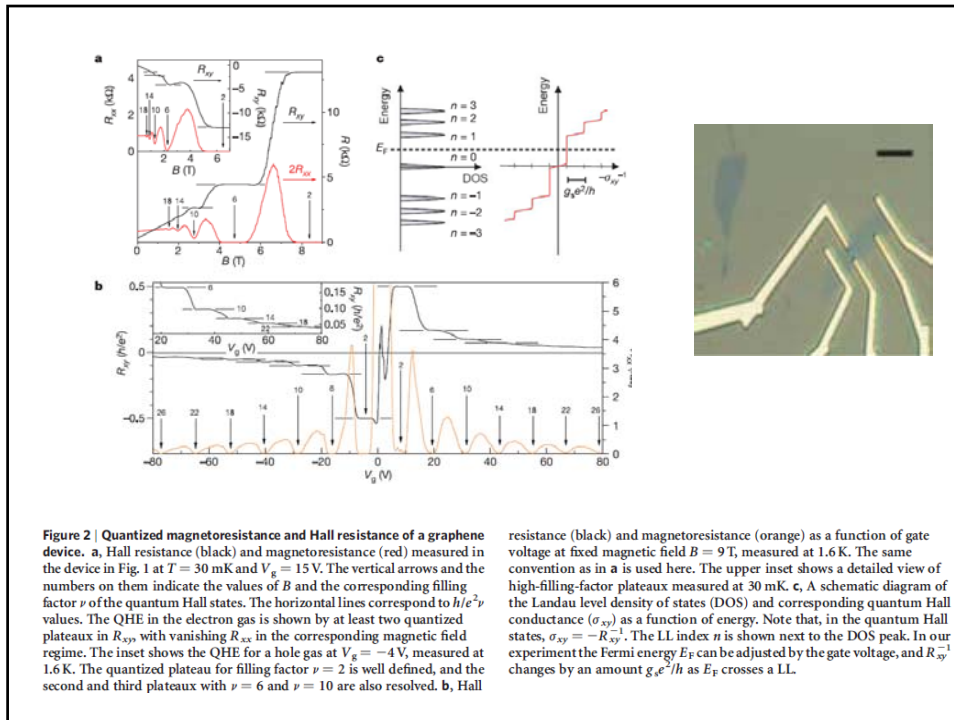
The fractional filling of **electrons** is really the integral filling of **composite fermions**

LETTERS

Experimental observation of the quantum Hall effect and Berry's phase in graphene

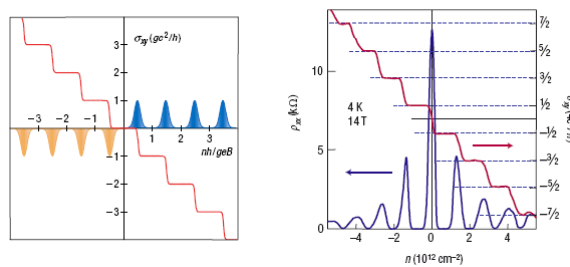
Yuanbo Zhang¹, Yan-Wen Tan¹, Horst L. Stormer^{1,2} & Philip Kim¹

http://www.youtube.com/watch?v=bHo6_jltfc8



Observation of the fractional quantum Hall effect in graphene

Kirill I. Bolotin, Fereshte Ghahari, Michael D. Shulman, Horst L. Stormer & Philip Kim
 Nature 462, 196–199 (2009)



Comparison between conventional and unconventional integer QHE. **(a)** Schematic illustration of the conventional integer QHE in 2D semiconductor systems by showing the Hall conductivity versus the carrier density, where orange and blue peaks represent the density of state of Landau levels. **(b)** The experimental measurements of the Hall conductivity and longitudinal resistivity versus the carrier density in graphene.

K. S. Novoselov, et al. Nature Physics **2**, 177 (2006).
 A. K. Geim, and K. S. Novoselov. Nature Materials **6**, 183 (2007)