

Lista de Exercícios 6

1) Calcule cada uma das integrais abaixo pelo método dos resíduos:

$$(1) \int_0^\infty \frac{x^2}{1+x^4} dx$$

$$(2) \int_0^\infty \frac{x \operatorname{sen}(x)}{(x^2+1)(x^2+4)} dx$$

$$(3) \int_{-\pi}^\pi \frac{\cos(\theta)}{5+4\cos(\theta)} d\theta$$

$$(4) \int_0^\infty \frac{\ln(x)}{x^2+1} dx$$

$$(5) \int_0^\infty \frac{\operatorname{sen}(tx)\operatorname{sen}(ax)}{x^2+b^2}, a \geq 0, b > 0$$

$$(6) \int_0^\pi \operatorname{sen}^{2n}(x) dx, n = 1, 2, 3, \dots$$

$$(7) \int_{-\infty}^\infty \frac{\exp(kx)}{1+\exp(x)}, 0 < k < 1$$

$$(8) \int_{-\infty}^\infty \frac{\cos(x)}{\pi^2-4x^2} dx$$

$$(9) \int_0^\infty \frac{\operatorname{sen}^2(x)}{x^2} dx$$

$$(10) \int_0^\infty \frac{\ln(x)}{(x^2+1)^2} dx$$

Respostas

$$1) \pi/(2\sqrt{2})$$

$$(2) \pi(1 - 1/e)/(6e)$$

$$(3) -\pi/3$$

$$(4) 0$$

$$(5) \left(\frac{\pi}{4b}\right)[\exp(-b|t-a|) - \exp(-b|t+a|)]$$

$$(6) \pi(2n)!/(2^n n!)^2$$

$$(7) \pi/\operatorname{sen}(k\pi)$$

$$(8) 1/2$$

$$(9) \pi/2$$

$$(10) -\pi/4$$