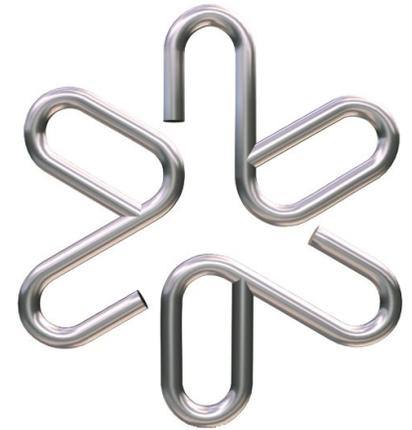


# Física do Calor (4300159)



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## **B05**

### Energia Interna de um Gas Ideal

## Provinha (3/4)

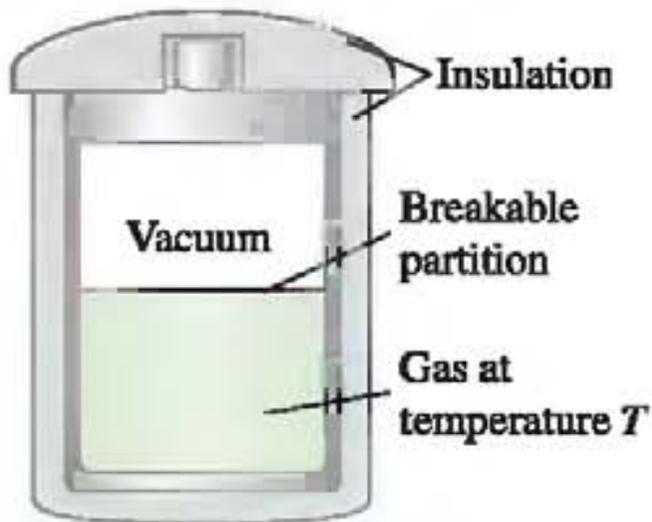
9.5 Um mol de um gás ideal, contido num recipiente munido de um pistão móvel, inicialmente a  $20\text{ }^{\circ}\text{C}$ , se expande isotermicamente até que seu volume aumenta de 50%. A seguir, é contraído, mantendo a pressão constante, até voltar ao volume inicial. Finalmente, é aquecido, a volume constante, até voltar à temperatura inicial, (a) Desenhe o diagrama  $P$ - $V$  associado; (b) Calcule o trabalho total realizado pelo gás nesse processo.

Data	Programa do curso
August 9	Temperatura e escalas
August 12	Expansão Térmica
August 16	Calorimetria
August 19	Condução, convecção Radiação (Corpo Humano)
August 23	Equação de Estado
August 26	Propriedades moleculares da Matéria
August 30	<b>(Aula de Exercícios e Revisão)</b>
September 2	Aula Modelo do Gas Ideal
September 6	Feriado
September 9	Feriado
September 13	<u>Prova 3 1/4 - Temperatura e Calor</u> - Capacidade Térmica
September 16	Velocidade molecular (Corpo Humano)
September 20	<b>(Aula de Exercícios e Revisão)</b>
September 23	<u>Prova 3 2/4 - Propriedades da Matéria</u> - Aula Fases da matéria
September 27	Prova 1: Temperatura, Calor e Propriedades da Matéria
September 30	Calor e trabalho
October 4	A primeira lei da Termodinâmica
October 7	Processos termodinâmicos
October 11	Semana de Ensino (IFUSP)
October 14	Semana de Ensino (IFUSP)
October 18	Termodinâmica do Gas Ideal
October 21	<b>(Aula de Exercícios e Revisão)</b>
October 25	<u>Prova 3 3/4 - Primeira Lei da Termodinâmica</u> - Aula Processos adiabaticos
October 28	Processos reversíveis e irreversíveis (Corpo Humano)
November 1	Maquinas térmicas, Ciclo de Otto e Refrigerador (Corpo Humano)
November 4	Segunda Lei da Termodinâmica
November 8	Ciclo de Carnot
November 11	<b>(Aula de Exercícios e Revisão)</b>
November 15	Feriado
November 18	Entropia Micro estados
November 22	<u>Prova 3 4/4 - Segunda Lei da Termodinâmica</u> - Aula Micro estados
November 25	Prova 2: Primeira e Segunda Lei da Termodinâmica
November 29	Prova Sub

# Processos Isolados

$$\Delta U = 0 \quad \text{e} \quad Q = W = 0$$

**19.17** The partition is broken (or removed) to start the free expansion of gas into the vacuum region.



$T$  também é constante

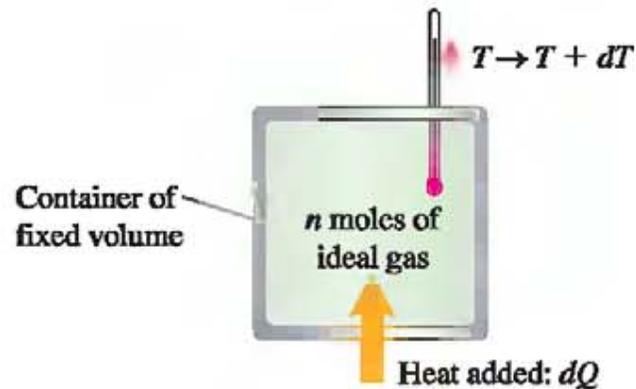
A energia interna de um gas ideal depende APENAS da temperatura, independe da pressão e volume

Para gases não ideais a temperatura muda durante expansão livre  
 $U$  depende de energia potencial e cinética

# Capacidade térmica de um gas ideal

**19.18** Measuring the molar heat capacity of an ideal gas (a) at constant volume and (b) at constant pressure.

(a) Constant volume:  $dQ = nC_V dT$



Porque eles seriam diferentes?

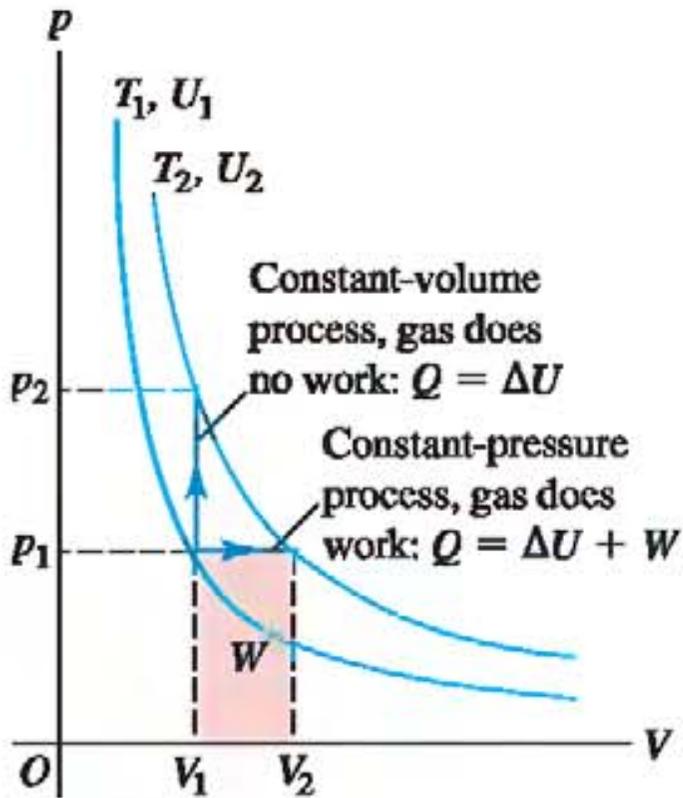
Volume constante

Sistema não realiza trabalho

$$Q = \Delta U$$

$$C_p > C_V$$

**19.19** Raising the temperature of an ideal gas from  $T_1$  to  $T_2$  by a constant-volume or a constant-pressure process. For an ideal gas,  $U$  depends only on  $T$ , so  $\Delta U$  is the same for both processes. But for the constant-pressure process, more heat  $Q$  must be added to both increase  $U$  and do work  $W$ . Hence  $C_p > C_v$ .



Por definição:

$$dQ = nC_v dt$$

Todavia (Primeira Lei):

$$dQ = dU + dW$$

como:  $dW = 0$

$$dU = nC_v dt$$

$dU$  depende apenas de  $T$

Por definição:

$$dQ = nC_p dt$$

$$dW = p dV$$

$$dW = nRT$$

$$p_1 V = nRT$$

$$V = \frac{1}{p_1} nRT$$

$$dV = \frac{1}{p_1} nR dT$$

$$nC_p dT = dU + nR dT$$

$$nC_p dT = nC_v dT + nR dT$$

$$C_p = C_v + R$$

**Table 19.1** Molar Heat Capacities of Gases at Low Pressure

Type of Gas	Gas	$C_v$ (J/mol·K)	$C_p$ (J/mol·K)	$C_p - C_v$ (J/mol·K)	$\gamma = C_p/C_v$
Monatomic	He	12.47	20.78	8.31	1.67
	Ar	12.47	20.78	8.31	1.67
Diatomic	H <sub>2</sub>	20.42	28.74	8.32	1.41
	N <sub>2</sub>	20.76	29.07	8.31	1.40
	O <sub>2</sub>	20.85	29.17	8.31	1.40
	CO	20.85	29.16	8.31	1.40
Polyatomic	CO <sub>2</sub>	28.46	36.94	8.48	1.30
	SO <sub>2</sub>	31.39	40.37	8.98	1.29
	H <sub>2</sub> S	25.95	34.60	8.65	1.33

# Processos Adiabáticos

Ou o sistema está isolado ou é rápido o suficiente para não sair ou entrar calor

$$Q = 0 \quad \Delta U = -W$$

Para qualquer processo, seja o processo adiabático ou não:

$$dU = nC_v dt$$

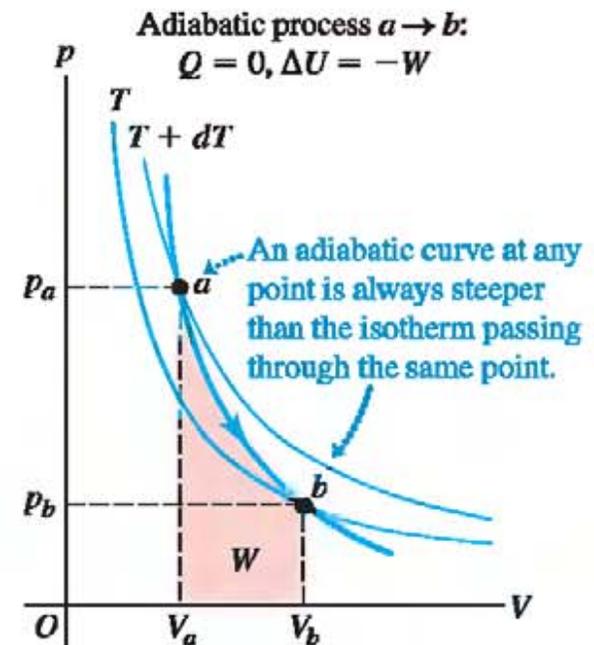
$$dW = p dV$$

Para um processo adiabático

$$dU = -dW$$

$$-p dV = nC_v dT$$

**19.20** A  $pV$ -diagram of an adiabatic ( $Q = 0$ ) process for an ideal gas. As the gas expands from  $V_a$  to  $V_b$ , it does positive work  $W$  on its environment, its internal energy decreases ( $\Delta U = -W < 0$ ), and its temperature drops from  $T + dT$  to  $T$ . (An adiabatic process is also shown in Fig. 19.16.)



# Processos Adiabáticos

$$-pdV = nC_v dT$$

$$p = nRT/V$$

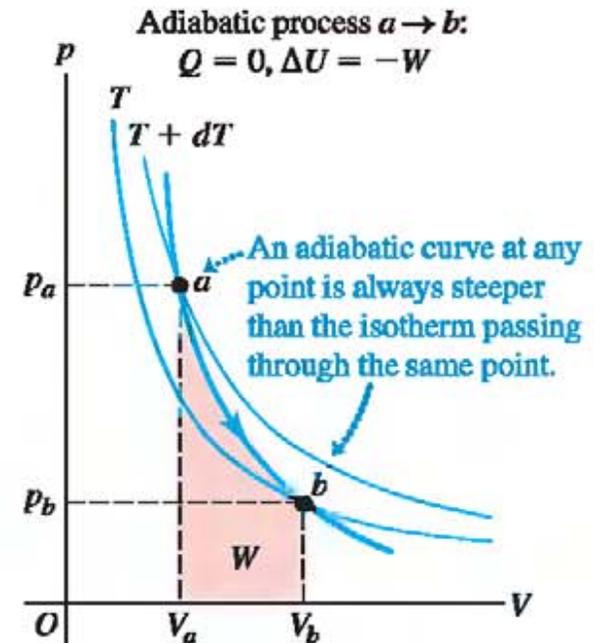
$$nC_v dT = -\frac{nRT}{V} dV$$

$$\frac{dT}{T} + \frac{R}{C_v} \frac{dV}{V} = 0$$

$$\frac{R}{C_v} = \frac{C_p - C_v}{C_v} = \frac{C_p}{C_v} - 1 = \gamma - 1$$

$$\frac{dT}{T} + (\gamma - 1) \frac{dV}{V} = 0$$

**19.20** A  $pV$ -diagram of an adiabatic ( $Q = 0$ ) process for an ideal gas. As the gas expands from  $V_a$  to  $V_b$ , it does positive work  $W$  on its environment, its internal energy decreases ( $\Delta U = -W < 0$ ), and its temperature drops from  $T + dT$  to  $T$ . (An adiabatic process is also shown in Fig. 19.16.)



# Processos Adiabáticos

$$\frac{dT}{T} + (\gamma - 1) \frac{dV}{V} = 0$$

$\gamma$  é sempre maior que 1,  $(\gamma - 1) > 0$

se  $dV > 0$ , isso implica  $dT < 0$

se  $dV < 0$ , isso implica  $dT > 0$

$$\int \frac{dT}{T} + \int (\gamma - 1) \frac{dV}{V} = 0$$

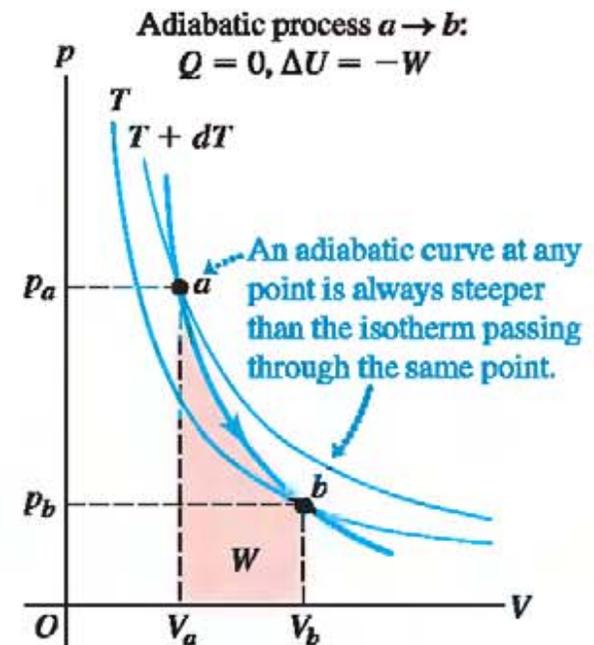
$$\ln T + (\gamma - 1) \ln V = \text{constante}$$

$$\ln T + \ln V^{\gamma-1} = \text{constante}$$

$$\ln(TV^{\gamma-1}) = \text{constante}$$

$$TV^{\gamma-1} = \text{constante}$$

**19.20** A  $pV$ -diagram of an adiabatic ( $Q = 0$ ) process for an ideal gas. As the gas expands from  $V_a$  to  $V_b$ , it does positive work  $W$  on its environment, its internal energy decreases ( $\Delta U = -W < 0$ ), and its temperature drops from  $T + dT$  to  $T$ . (An adiabatic process is also shown in Fig. 19.16.)





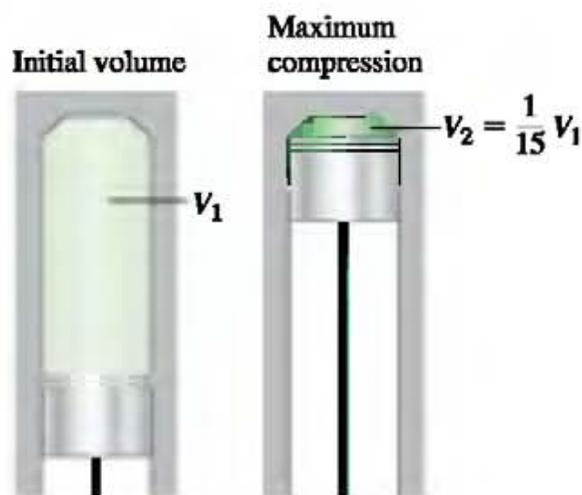
### Example 19.7 Adiabatic compression in a diesel engine

The compression ratio of a diesel engine is 15 to 1; this means that air in the cylinders is compressed to  $\frac{1}{15}$  of its initial volume (Fig. 19.21). If the initial pressure is  $1.01 \times 10^5$  Pa and the initial temperature is  $27^\circ\text{C}$  (300 K), find the final pressure and the temperature after compression. Air is mostly a mixture of diatomic oxygen and nitrogen; treat it as an ideal gas with  $\gamma = 1.40$ .

#### SOLUTION

**IDENTIFY:** Since this problem involves the adiabatic compression of an ideal gas, we can use the ideas of this section.

**19.21** Adiabatic compression of air in a cylinder of a diesel engine.



**SET UP:** We are given the initial pressure  $p_1 = 1.01 \times 10^5$  Pa and the initial temperature  $T_1 = 300$  K, and we are told that the ratio of initial and final volumes is  $V_1/V_2 = 15$ . We can find the final temperature  $T_2$  using Eq. (19.22) and the final pressure  $p_2$  using Eq. (19.24).

**EXECUTE:** From Eq. (19.22),

$$T_2 = T_1 \left( \frac{V_1}{V_2} \right)^{\gamma-1} = (300 \text{ K}) (15)^{0.40} = 886 \text{ K} = 613^\circ\text{C}$$

From Eq. (19.24),

$$\begin{aligned} p_2 &= p_1 \left( \frac{V_1}{V_2} \right)^\gamma = (1.01 \times 10^5 \text{ Pa}) (15)^{1.40} \\ &= 44.8 \times 10^5 \text{ Pa} = 44 \text{ atm} \end{aligned}$$

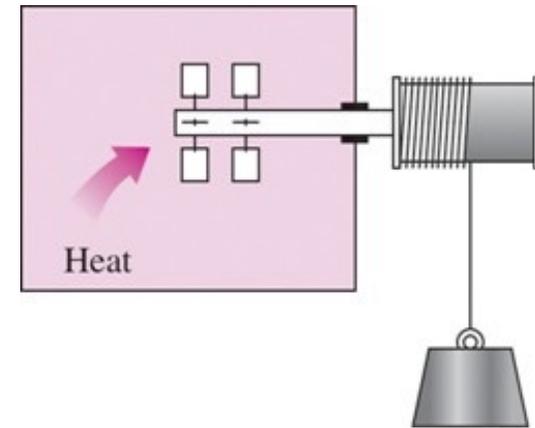
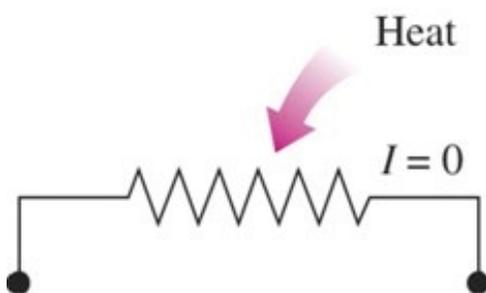
**EVALUATE:** If the compression had been isothermal, the final pressure would have been 15 atm, but because the temperature also increases during an adiabatic compression, the final pressure is much greater. When fuel is injected into the cylinders near the end of the compression stroke, the high temperature of the air attained during compression causes the fuel to ignite spontaneously without the need for spark plugs.

# Segunda Lei da Termodinâmica



Um copo de café nunca esquenta em um ambiente frio

Transferir calor para uma resistência não vai gerar eletricidade

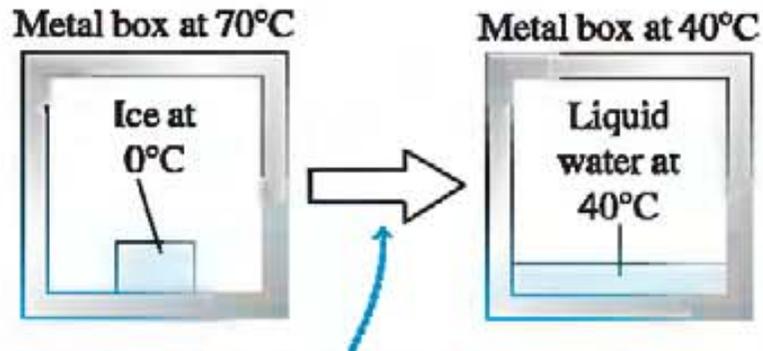


Transferir calor para uma roda com remos não vai fazer ela rodar

**Esses processos não podem ocorrer, mesmo que eles não violem a primeira lei da termodinâmica**

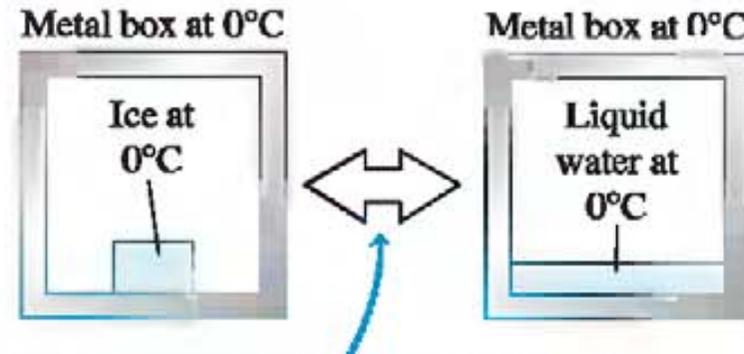
**Irreversibilidade!!!**

(a) A block of ice melts *irreversibly* when we place it in a hot ( $70^{\circ}\text{C}$ ) metal box.



Heat flows from the box into the ice and water, never the reverse.

(b) A block of ice at  $0^{\circ}\text{C}$  can be melted *reversibly* if we put it in a  $0^{\circ}\text{C}$  metal box.



By infinitesimally raising or lowering the temperature of the box, we can make heat flow into the ice to melt it or make heat flow out of the water to refreeze it.

Idealizado reversível, muito próximo ao equilíbrio termodinâmico