

4ª Lista

Colisão

1. Conservação do momento linear

a)

eixo X
 $P_i = P_f$
 $m \cdot u = M \cdot v \cdot \cos \theta$

eixo Y
 $P_i = P_f$
 $0 = m \cdot u + M \cdot v \cdot \sin \theta$

$$\begin{cases} m u = M v \cos \theta \\ m u = -M v \sin \theta \end{cases} \Rightarrow \theta = -30^\circ$$

b) Colisão Elástica: $\Delta E_c + \Delta E_p = 0$

$$\Rightarrow E_i = E_f \Rightarrow \frac{m u^2}{2} = \frac{m \left(\frac{u}{3}\right)^2}{2} + \frac{M v^2}{2}$$

$$\Rightarrow \frac{2 m u^2}{3} = M v^2 \quad (I)$$

elevar ao quadrado e somando

sendo

$$\begin{cases} m u = M v \cos \theta \\ m u = -M v \sin \theta \end{cases} \Rightarrow M^2 v^2 = \frac{4 m^2 u^2}{3}$$

utilizando I:

$$\begin{cases} M^2 v^2 = \frac{4 m^2 u^2}{3} \\ M v^2 = \frac{2 m u^2}{3} \end{cases} \Rightarrow \frac{M}{m} = 2$$

$$M v^2 = \frac{2m u^2}{3} \Rightarrow \theta = \frac{u}{\sqrt{3}} //$$

$$c) V_{CM}^i = V_{CM}^f$$

$$V_{CM} = \frac{m u + M \cdot 0}{M + m} = \frac{1}{3} u \hat{i}$$

$$\vec{V}_{Mf} = \left| \frac{u}{\sqrt{3}} \right| \cdot (\cos \theta \hat{i} + \sin \theta \hat{j}) = u \left(\frac{1}{2} \hat{i} - \frac{1}{2\sqrt{3}} \hat{j} \right)$$

\downarrow
 -30°

$$\vec{V}_{mf} = \left(\frac{u}{\sqrt{3}} \right) \hat{j}$$

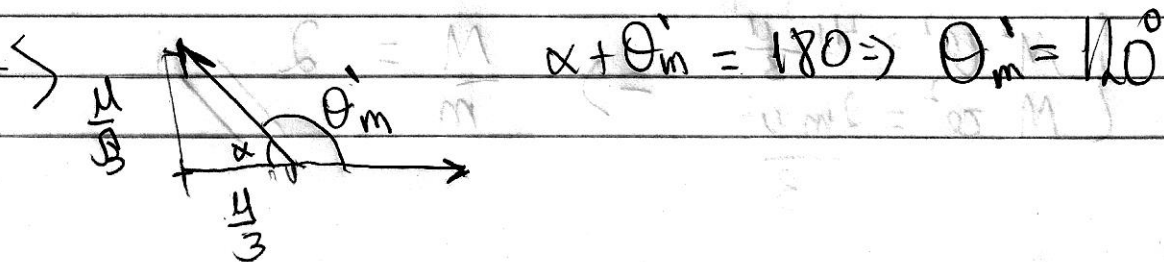
No referencial do CM:

$$\vec{V}'_{Mf} = \vec{V}_{Mf} - \vec{V}_{CM} = u \left(\frac{1}{6} \hat{i} - \frac{1}{2\sqrt{3}} \hat{j} \right)$$

$$\vec{V}'_{mf} = \vec{V}_{mf} - \vec{V}_{CM} = u \left(-\frac{1}{3} \hat{i} + \frac{1}{\sqrt{3}} \hat{j} \right)$$

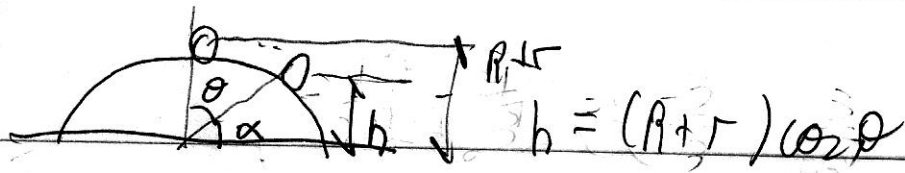
$$\tan \alpha = \frac{C.O.}{C.A.} = \frac{-\frac{1}{3}}{\frac{1}{2\sqrt{3}}} = -\frac{2}{\sqrt{3}} \Rightarrow \alpha = 60^\circ$$

$$\tan \theta'_m = \frac{C.O.}{C.A.} = \frac{-\frac{2}{\sqrt{3}}}{\frac{1}{6}} = -\frac{4}{\sqrt{3}} \Rightarrow \theta'_m = 30^\circ$$



$$v = \frac{a}{R}$$

$$v = \frac{v_{cm}}{R}$$



$$h = (R+r) \cos \theta$$

$$2.) \quad \text{A } F_{cp} = P \cos \theta \Rightarrow \frac{m v^2}{(R+r)} = mg \cos \theta \Rightarrow v$$

$$\Rightarrow v^2 = (R+r) g \cos \theta$$

Conservação de energia

$$E_i = E_f$$

$$mg(R+r) = mgh + \frac{m v^2}{2} + \frac{\omega^2 I}{2}$$

$$I = \frac{2}{5} m R^2$$

$$\Rightarrow \cos \theta = \frac{10}{17} \Rightarrow \theta = 54$$

$$b) \quad v = \sqrt{g \cos 54 (R+r)} = \sqrt{\frac{10g}{17} (R+r)}$$