

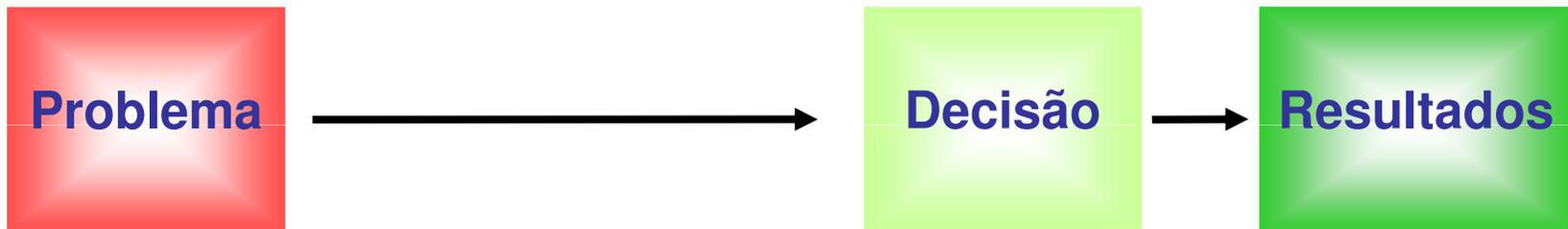
FIG. 1.5 – *Les deux grandes familles de modèles.*

# O que é um Modelo?

**Modelo** *s.* Uma descrição esquemática de um sistema, teoria ou fenômeno que contabiliza as suas propriedades conhecidas ou inferidas, e pode ser utilizada para estudos mais aprofundados das suas características.

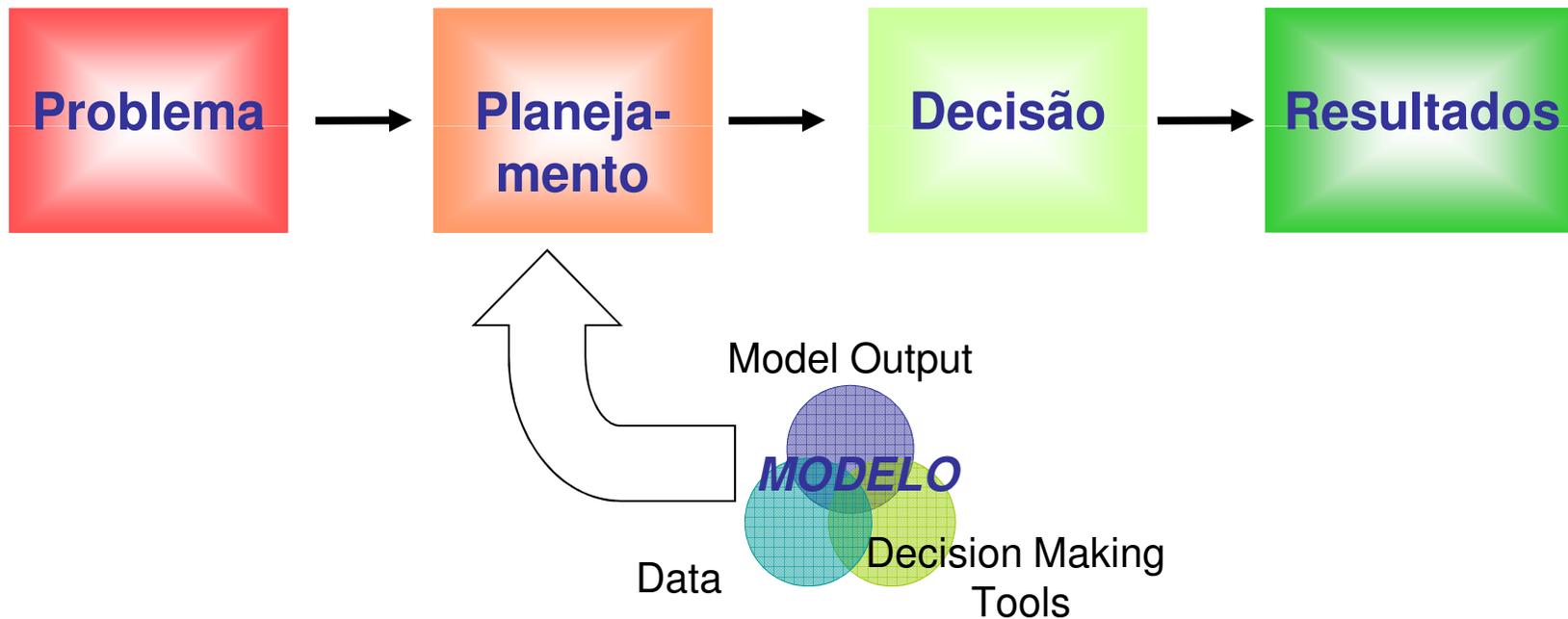
*-The American Heritage® Dictionary of the English Language: Fourth Edition. 2000.*

# Porque usamos modelos?



# Porque usamos modelos?

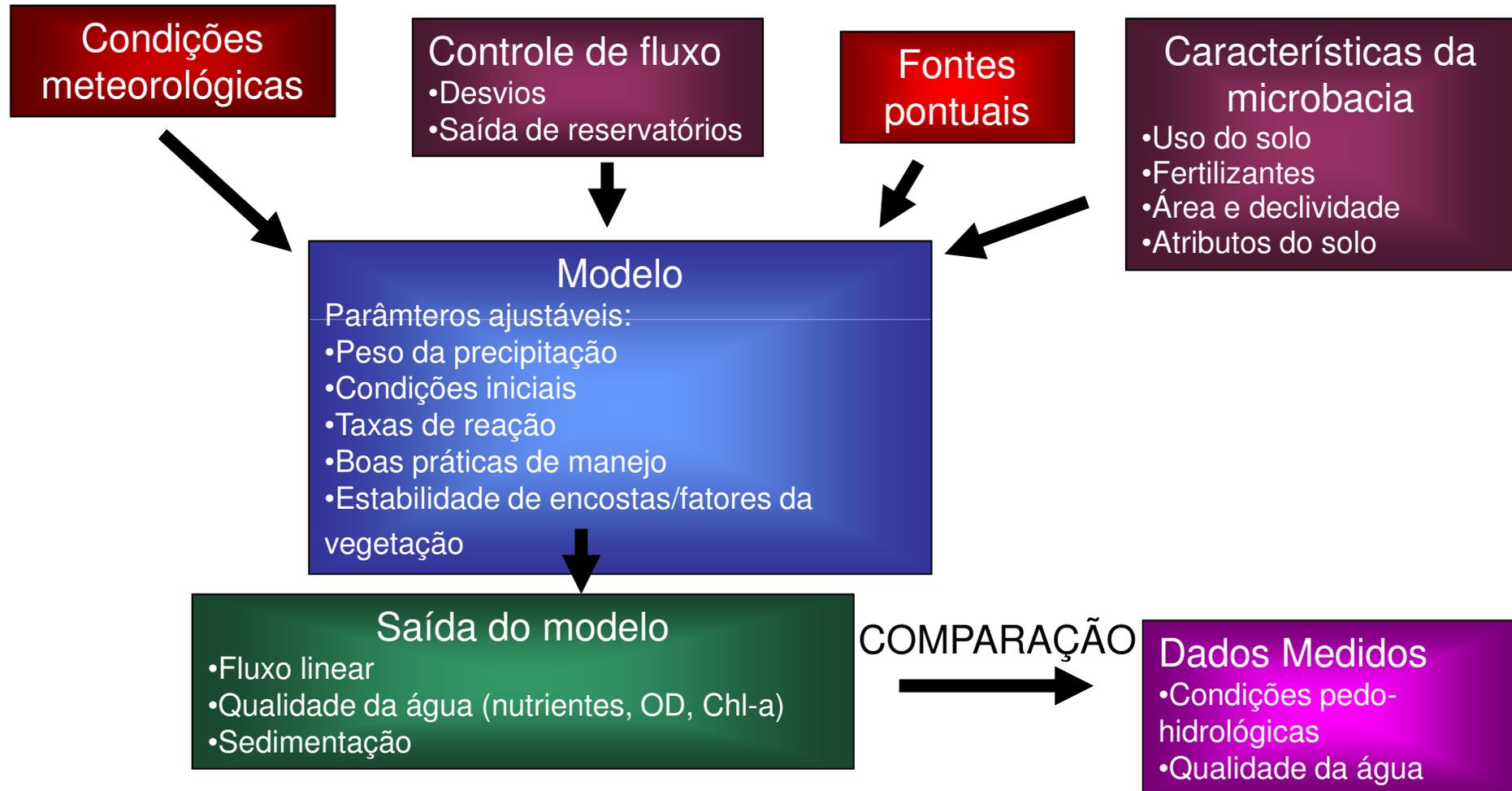
- Modelo ajuda a responder “E se?”



# Tipos de Modelos de Erosão

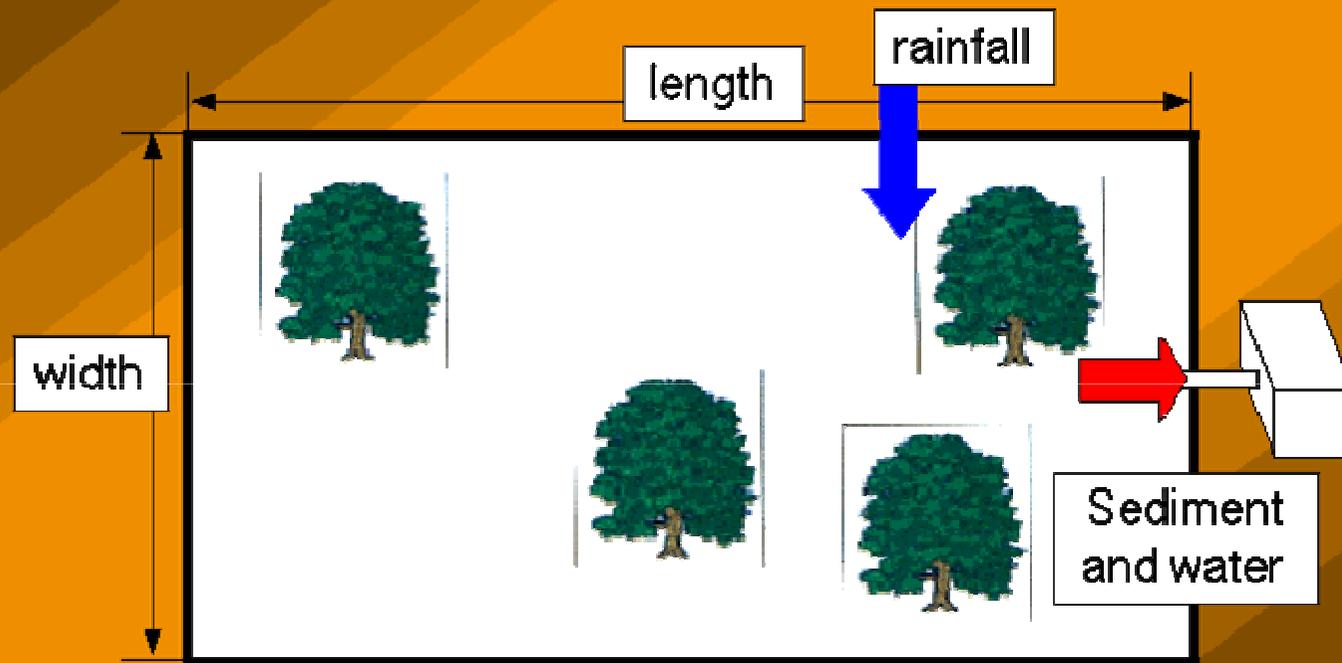
- **Avaliação dos Balanços de Massa**
  - Cálculos simplificados, planilhas de cálculo
  - Baixo custo, fácil de implementar, partem de suposições simplificadas
- **Ferramentas baseadas em SIGs**
  - Relacionar modelos de balanço de massa simples a bases de SIG
  - Produzir mapas ressaltando regiões das microbacias de alta sensibilidade
- **Modelos Matemáticos**
  - Ferramentas complexas utilizando equações diferenciais para descrever processos físicos
  - Rigoroso, baseado em processos físicos, fornecem simulações dinâmicas de um sistema

# O que é um modelo de erosão?



# Quantificando a Erosão do Solo

## *Estimating Soil Erosion Rates with Study Plots*



*How would you calculate the "erosion rate"?*





Erosion Plot



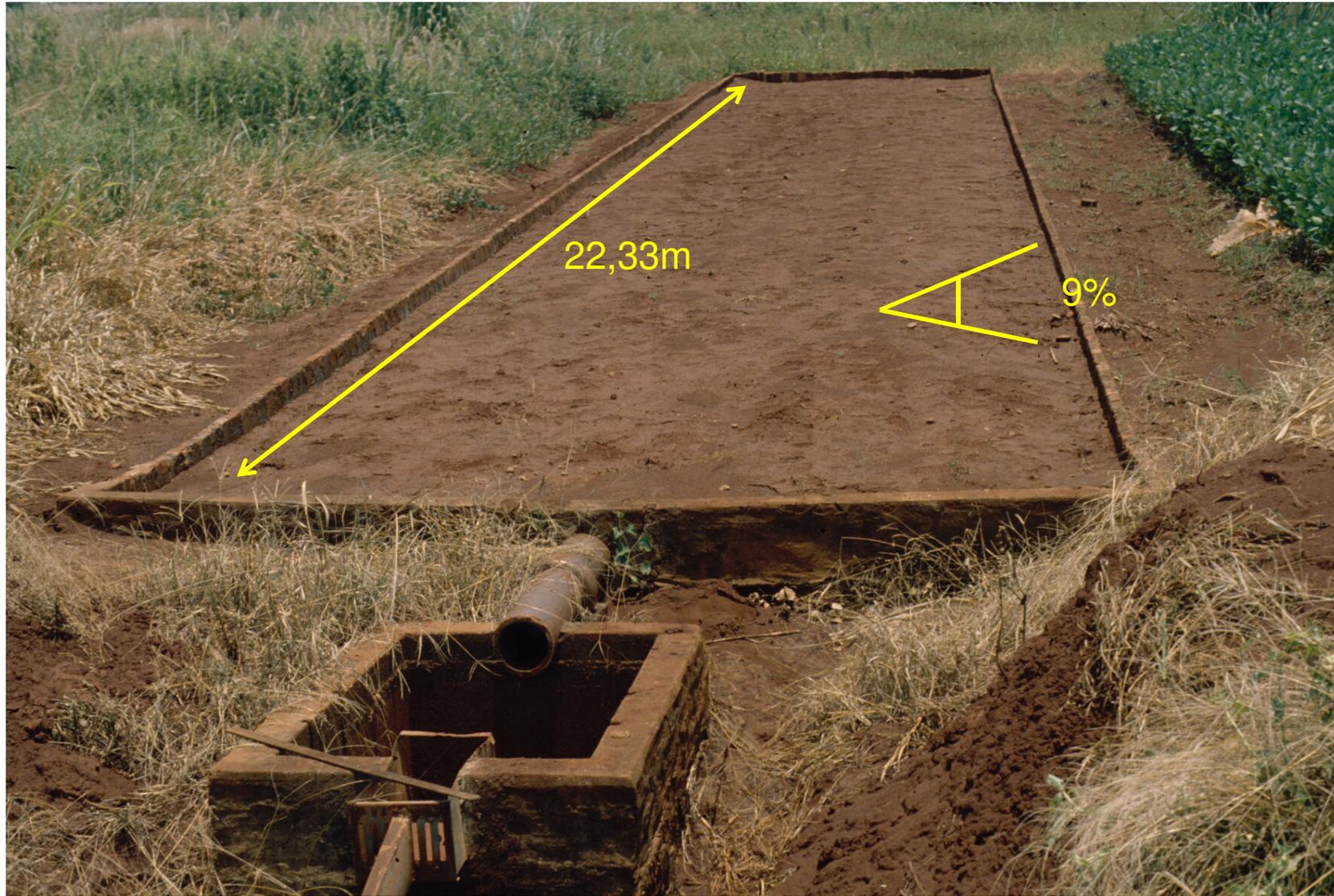
Sediment Collector

# Canteiro coletor USLE

- Comprimento 22,33m
- Declividade 9%
- Largura 4m.



## Canteiro coletor USLE (valor padrão)



# USLE

## Equação Universal de Perda de Solo

- ✦ Wischmeier, W.H. and D.D. Smith. 1978. Predicting rainfall erosion losses. USDA Agriculture Handbook 537, U.S. Department of Agriculture.

- Modelo Empírico:
  - Análise de observações
  - Procura caracterizar respostas destas informações
- Baseado:
  - Padrões de chuva, tipo de solo, topografia, sistema de cultivo e práticas conservacionistas.
- Prediz:
  - Taxas anuais de perda do solo de longo prazo
- Subrotinas em modelos como:
  - SWRRB (Williams, 1975), EPIC (Williams et al., 1980), ANSWERS (Beasley et al., 1980), AGNPS (Young et al., 1989)

## A equação:

$$A = R \times K \times LS \times C \times P$$

- A = perda do solo anual (tons/ha ano)
- R = índice de erosividade
- K = erodibilidade do solo
- L = comprimento de rampa
- S = declividade
- C = fator de cultivo/preparo
- P = fator práticas conservacionistas

## R (índice de erosividade)

- Índice de erosão (EI) para um evento:
  - Produto da energia cinética das gotas de chuva e a intensidade máxima em 30 minutos.
- Fator  $R = \sum EI$  num ano/100

$$A = \underline{R} \times K \times LS \times C \times P$$

## Rainfall erosivity map for Brazil

Alexandre Marco da Silva

Laboratório de Ecologia Isotópica-Centro de Energia Nuclear na Agricultura, Universidade de São Paulo (USP), Avenida Centenario, 303, 13.400-970, Piracicaba, São Paulo, Brazil

Received 5 February 2003; received in revised form 15 October 2003; accepted 24 November 2003

$x$  = índice mensal

$M$  = Precipitação média mensal

$P$  = Precipitação média anual



Number	Equation	Author(s)
1	$R_x = 3.76 * \left(\frac{M_x^2}{P}\right) + 42.77$	Oliveira Jr. and Medina (1990)
2	$R_x = 36.849 * \left(\frac{M_x^2}{P}\right)^{1.0852}$	Morais et al. (1991)
3	$R_x = (0.66 * M_x) + 8.88$	Oliveira Jr. (1988)
4	$R_x = 42.307 * \left(\frac{M_x^2}{P}\right) + 69.763$	Silva (2001)
5	$R_x = 0.13 * (M_x^{1.24})$	Leprun (1981)
6	$R_x = 12.592 * \left(\frac{M_x^2}{P}\right)^{0.6030}$	Val et al. (1986)
7	$R_x = 68.73 * \left(\frac{M_x^2}{P}\right)^{0.841}$	Lombardi Neto and Moldenhauer (1992)
8	$R_x = 19.55 + (4.20 * M_x)$	Rufino et al. (1993)

$$A = \underline{R} \times K \times LS \times C \times P$$

Fig. 1. Equations used to determine the monthly/annual values of the erosivity according to the area of the territory and their respective authors. Eqs. number (1), (2), (4), (6), and (7) were based from the Fournier's model. Eqs. (3) and (8) are linear models and Eq. (5) is an exponential model.  $R_x$  is  $R$  factor ( $\text{MJ mm ha}^{-1} \text{ h}^{-1} \text{ year}^{-1}$ ) for month  $x$ ,  $M_x$  is average monthly precipitation depth (mm), and  $P$  is average annual precipitation (mm) (Silva, 2001).

## K (erodibilidade do solo)

- Susceptibilidade de um solo ao processo erosivo pela água e enxurrada
- Depende de:
  - Textura, estrutura, conteúdo de matéria orgânica, e permeabilidade.

$$A = R \times \underline{K} \times LS \times C \times P$$

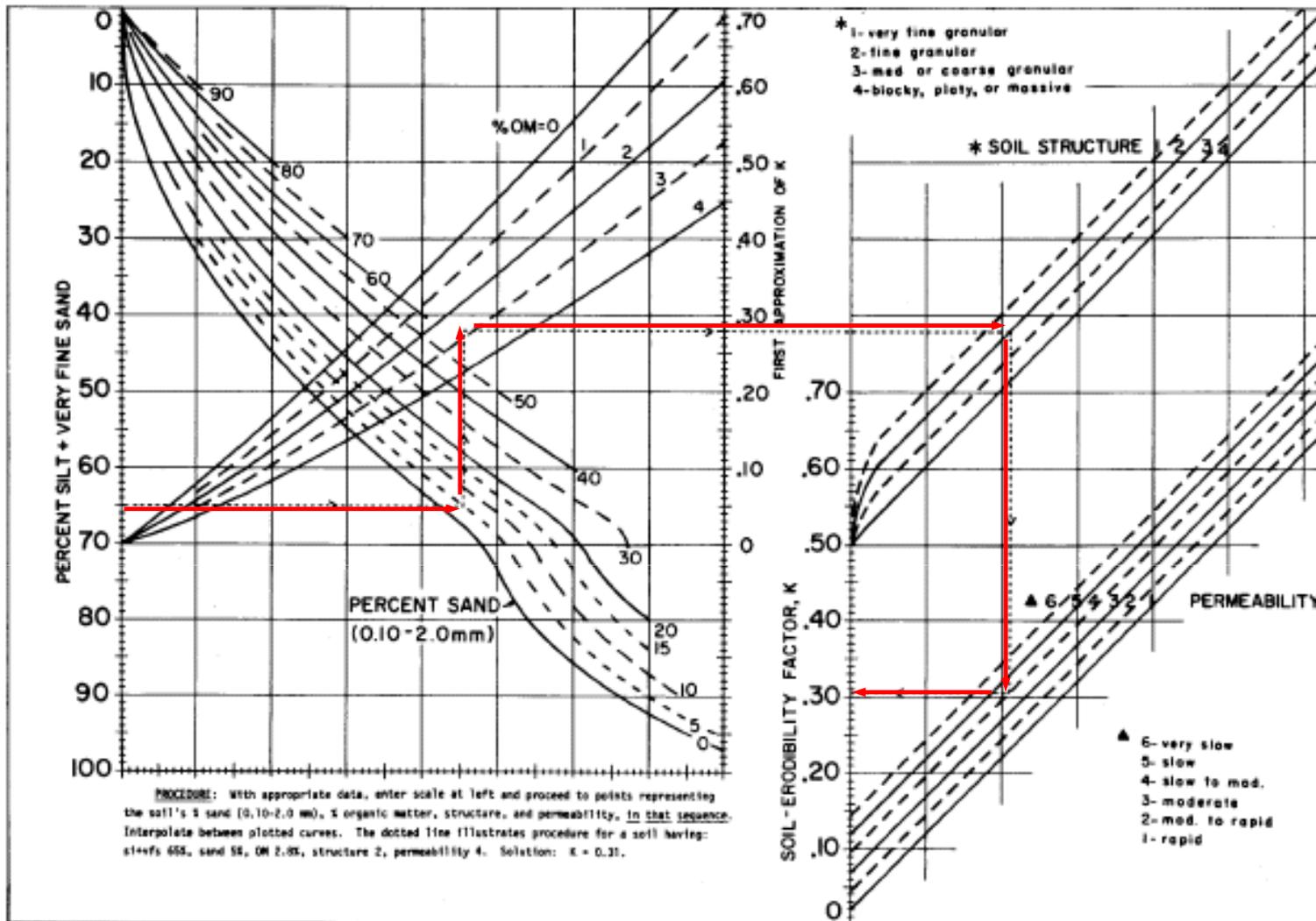
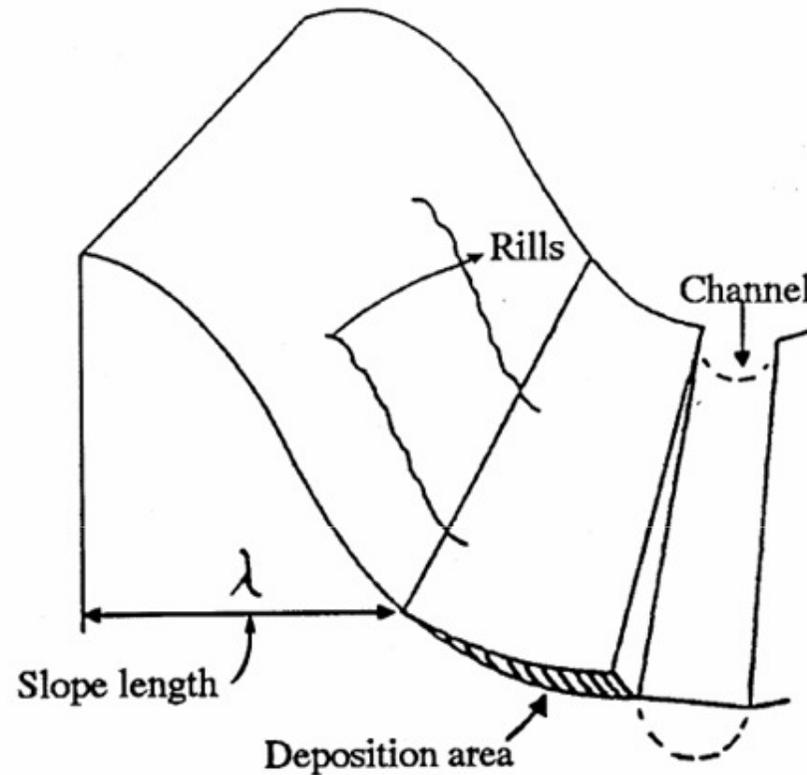


FIGURE 3.—The soil-erodibility nomograph. Where the silt fraction does not exceed 70 percent, the equation is  $100 K = 2.1 M^{0.4} (10^{-3}) (12 - a) + 3.25 (b - 2) + 2.5 (c - 3)$  where  $M = (\text{percent si} + \text{vfs}) (100 - \text{percent c})$ ,  $a = \text{percent organic matter}$ ,  $b = \text{structure code}$ , and  $c = \text{profile permeability class}$ .

## Nomograma da Erodibilidade do Solo

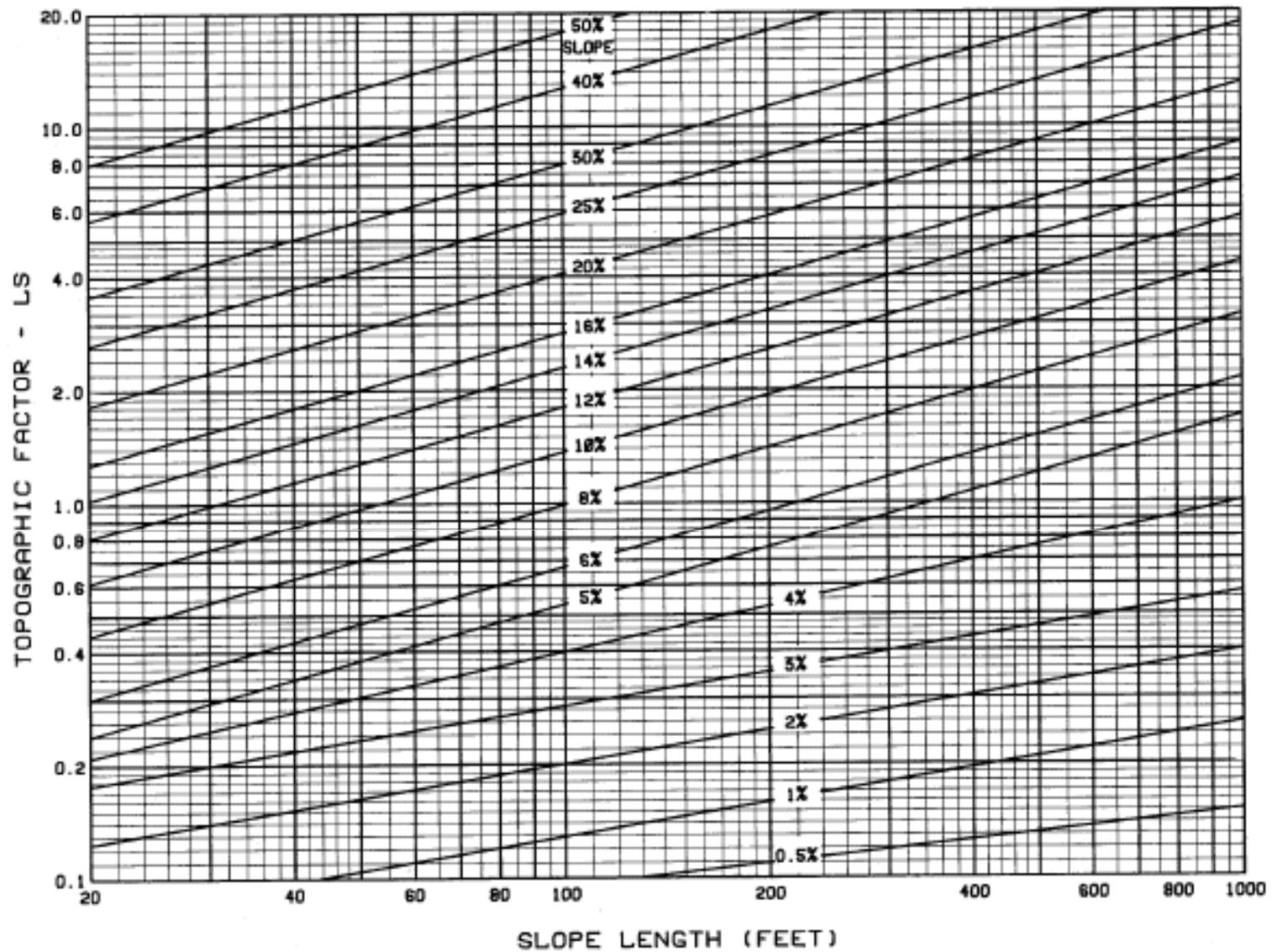
$$A = R \times \underline{K} \times LS \times C \times P$$

## LS (comprimento de rampa e declividade)



- Razão da perda do solo sob certas condições de topografia em relação a um local com um comprimento de rampa e declividade padrões.

$$A = R \times K \times \underline{LS} \times C \times P$$



## Fator Topográfico LS

$$A = R \times K \times \underline{LS} \times C \times P$$

## C (fator de cultivo/preparo)

- Razão da perda do solo por um uso do solo sob condições específicas em relação à áreas em pousio ou preparo contínuo.

<b>Crop</b>	<b>Fator</b>
Milho grãos	0.40
Milho silagem, Feijão & Canola	0.50
Cereais	0.35
Cultivos hortícolas	0.50
Frutíferas	0.10
Feno e Pastagens	0.02

<b>Preparo</b>	<b>Fator</b>
Aração de outono	1.00
Aração de primavera	0.90
Preparo com mulch	0.60
Preparo em nível	0.35
Preparo em talhões	0.25
Plantio Direto	0.25

$$A = R \times K \times LS \times \underline{C} \times P$$

## P (práticas conservacionistas)

- Razão da perda do solo de uma prática conservacionista em relação a um preparo morro abaixo.

<b>Prática</b>	<b>Fator P</b>
Morro Abaixo	1.00
Plantio cruzado	0.75
Plantio em nível	0.50
Plantio em faixas, cruzado	0.37
Plantio em faixas, em nível	0.25

$$A = R \times K \times LS \times C \times \underline{P}$$

# WEPP

## Water Erosion Prediction Project

- ✦ Foster, G.R. and L.J. Lane (compilers). 1987. User Requirements. USDA-Water Erosion Prediction Project. NSERL Report #1, USDA-ARS National Soil Erosion Research Laboratory, West Lafayette, IN.

# Water Erosion Prediction Project (WEPP)

- Desenvolvido em 1987
- Modelo baseado em processos físicos que simula todo o processo de erosão
- Pode prever a distribuição espacial e temporal da perda e deposição líquida do solo

Process Based Models: Mass balance differential equation

$$\delta(cq)/\delta x + \delta(ch)/\delta t + S = 0$$

$c$  = Sediment concentration ( $\text{kg}/\text{m}^3$ )

$q$  = Runoff discharge ( $\text{m}^2/\text{s}$ )

$x$  = Distance in the direction of flow (m)

$h$  = Depth of flow (m)

$t$  = Time (s)

$S$  = Source/sink term ( $\text{kg}/(\text{m}^2\text{s})$ )

WEPP

$$dG/dx = D_r + D_i$$

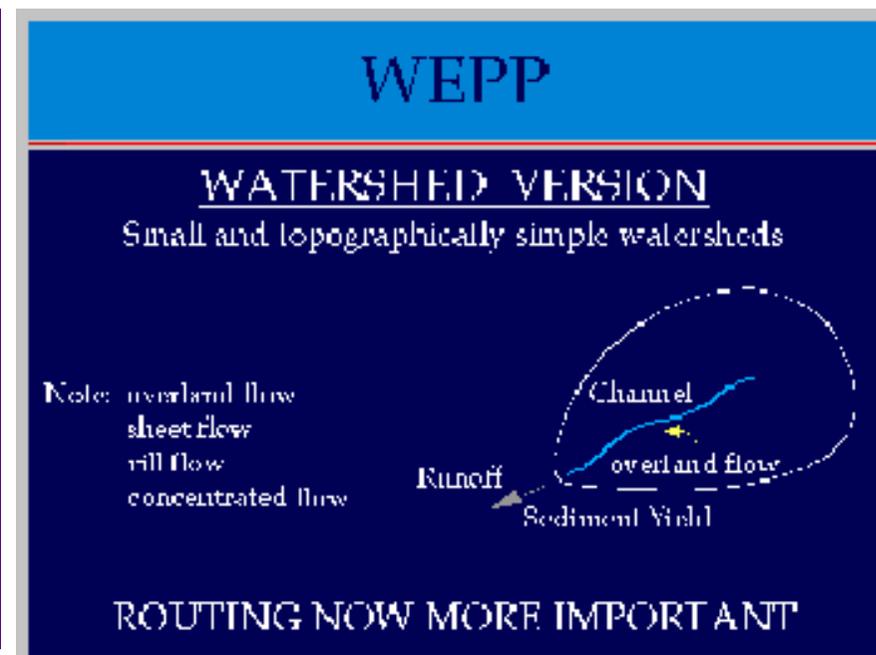
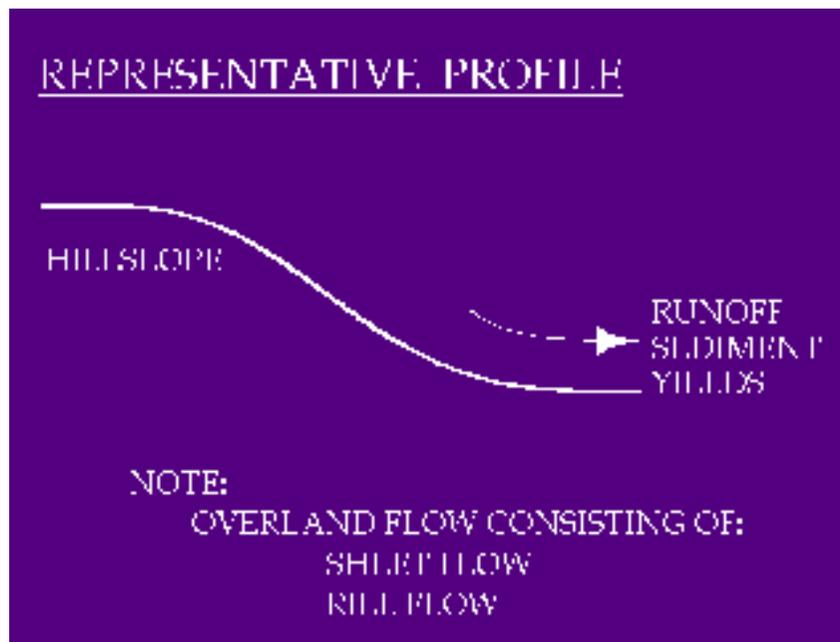
$G$  = Sediment load per unit width in the flow ( $\text{kg}/(\text{m s})$ ) =  $cq$

$D_r$  = net rill erosion rate per unit area of rill bottom ( $\text{kg}/(\text{m}^2 \text{s})$ ) (+ or -)

$D_i$  = Interrill sediment delivery to rill ( $\text{kg}/(\text{m}^2 \text{s})$ )

# Aplicações do modelo WEPP

- Vertente
  - Substituição direta da USLE
  - Pode prever a perda e deposição do solo numa vertente
- Microbacia hidrográfica
  - Desprendimento, transporte e deposição de sedimentos em sistemas fluviais e na vertente



WDRP model for Windows - [default]

File Edit View Option Tools Window Help

Region Info

Slope File: PP\_1

Climate File: A012\_sun1

State: NSW  
Station: PENRITH SYDNEY NW

Penrith Sydney NW  
Climate

Single Storm Simulation	Value	Units
Single Storm Precipitation	14.00	mm
Single Storm Runoff	7.27	mm
Single Storm Soil Loss	0.058	kg/ha2
Single Storm Sediment Yield	0.576	t/ha

Manager  
Slope  
Soil

0.0 80.0

Meters

0.0 80.0

Management	Segment Length (m)	Average Detachment (t/ha)	Detachment Length (m)	Average Deposition (t/ha)	Deposition Length (m)	Soil Name	Segment Length (m)	Average Detachment (t/ha)	Detachment Length (m)	Average Deposition (t/ha)	Deposition Length (m)
UNCOVERED	80.0	0.58	80.0	0.00	0.0	UNCOVERED	80.0	0.58	80.0	0.00	0.0

Soil Loss Graph Graphical Output Return Periods Text Output Run Options Run

For Help, press F1

**Table 9.1.** Comparison of the main model characteristics

Erosion model	Event based	Empirical equation for simulating erosion	Interface to Arc/Info	Simulation of transport, deposition, etc.	Required input data	Maximum number of grid cells	User friendliness
USLE	No	Yes	No	No	+	n.i.	Yes
RUSLE/MUSLE	Yes	Yes	No	No	+	n.i.	Yes
EPIC	No	Yes	No	No	+++	n.i.	No
AGNPS	Yes	Yes	Yes	Yes	++	1 900	Yes
CREAMS	No	Yes	No	Yes	++	n.i.	No
GLEAMS	No	Yes	No	Yes	++	n.i.	No
ANSWERS	Yes	No	No	Yes	++	1 700	Yes
EROSION-2D/3D	Yes	No	Yes	Yes	++	50 000	Yes
KINEROS	Yes	N.I.	No	Yes	+++	n.i.	No
OPUS	Yes	No	No	Yes	+++	n.i.	No
SPUR I/II	Yes	Yes	No	No	+++	n.i.	No
WEPP	Yes	No	Yes	Yes	+++	n.i.	No
EUROSEM	Yes	No	Yes	Yes	+++	n.i.	No

n.i. No information;

+ Few;

++ Moderate;

+++ Many.

# Modelagem de erosão:

Der Tropenlandwirt, Beiträge zur tropischen Landwirtschaft und Veterinärmedizin,  
101. Jahrgang, Oktober 2000, S. 107 - 118.

## Comparison of Three Water Erosion Prediction Methods ( $^{137}\text{Cs}$ , WEPP, USLE) in South-East Brazilian Sugarcane Production

G. Sparovek<sup>\*1</sup>, O.O.S. Bacchi<sup>2</sup>, E. Schnug<sup>2\*</sup>, S.B.L. Ranieri<sup>3</sup> and I.C. De Maria<sup>\*\*\*</sup>

**Key words:** Erosion prediction,  $^{137}\text{Cs}$ , WEPP, USLE, sugarcane, Brazil.



PERGAMON

Computers & Geosciences 28 (2002) 661–668

COMPUTERS  
GEOSCIENCES

www.elsevier.com/locate/cageo



ELSEVIER

Computers & Geosciences 31 (2005) 1270–1276

COMPUTERS  
GEOSCIENCES

www.elsevier.com/locate/cageo

Short note

### Runoff mapping using WEPP erosion model and GIS tools

Quirijn de Jong van Lier<sup>a,\*</sup>, Gerd Sparovek<sup>a</sup>, Dennis C. Flanagan<sup>b</sup>,  
Elke M. Bloem<sup>c</sup>, Ewald Schnug<sup>c</sup>

<sup>a</sup>University of São Paulo, CP 9, 13418-900, Piracicaba (SP), Brazil

<sup>b</sup>USDA-Agricultural Research Service, National Soil Erosion Research Laboratory, 275 S. Russell Street, West Lafayette, IN 47907, USA

<sup>c</sup>Institute of Plant Nutrition and Soil Science, Federal Agricultural Research Center (FAL), Bundesallee 50, D-38116, Braunschweig, Germany

Received 15 September 2003; received in revised form 22 March 2005; accepted 22 March 2005

Erosion database interface (EDI): a computer program for georeferenced application of erosion prediction models

Simone Beatriz Lima Ranieri<sup>a</sup>, Quirijn de Jong van Lier<sup>a,\*</sup>, Gerd Sparovek<sup>a</sup>,  
Dennis C. Flanagan<sup>b</sup>

<sup>a</sup>University of São Paulo, CP 9, 13418-900 Piracicaba (SP), Brazil

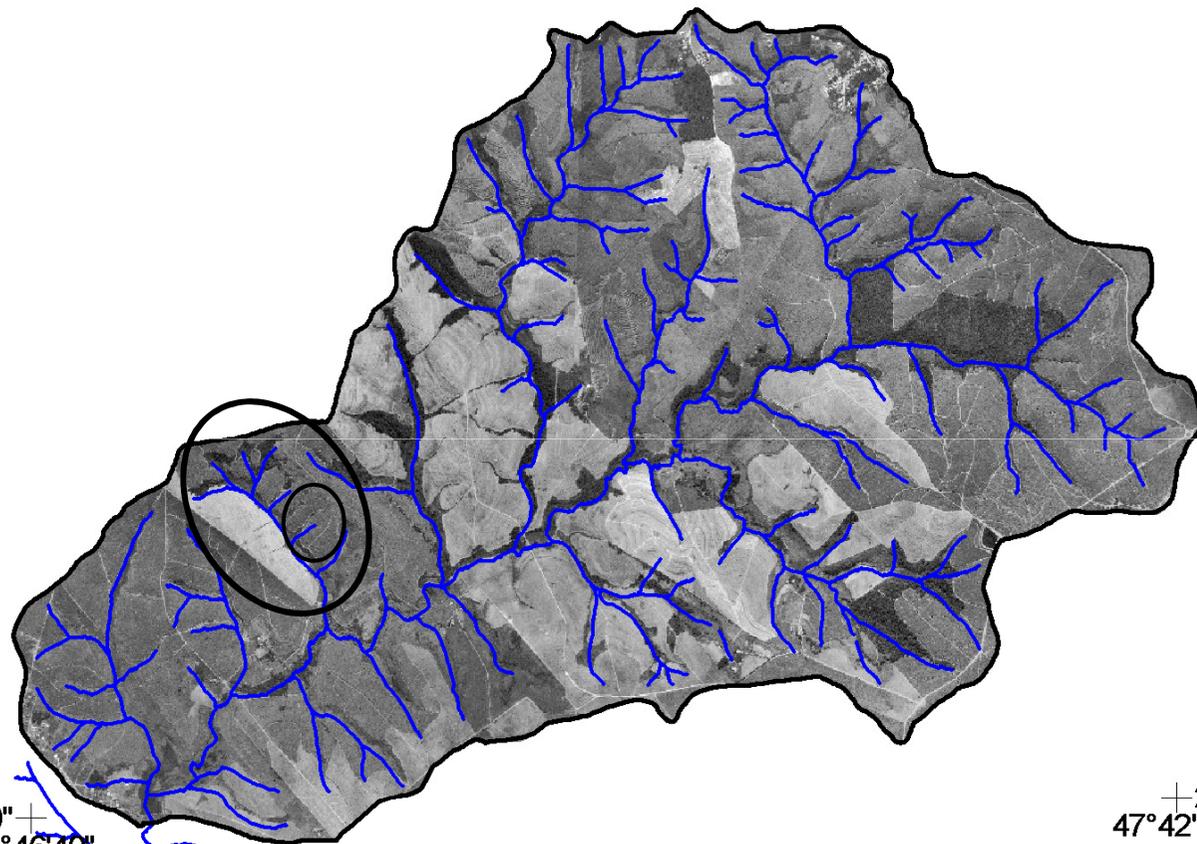
<sup>b</sup>USDA-Agricultural Research Service, National Soil Erosion Research Laboratory, 1196 Building Soil, West Lafayette, IN 47907-1196, USA

Received 3 August 2000; received in revised form 19 April 2001; accepted 12 July 2001

# MBH- Ceveiro

47°46'40"  
22°37'11" +

47°42'40"  
+22°37'11"



22°39'50" +  
47°46'40"

+22°39'50"  
47°42'40"



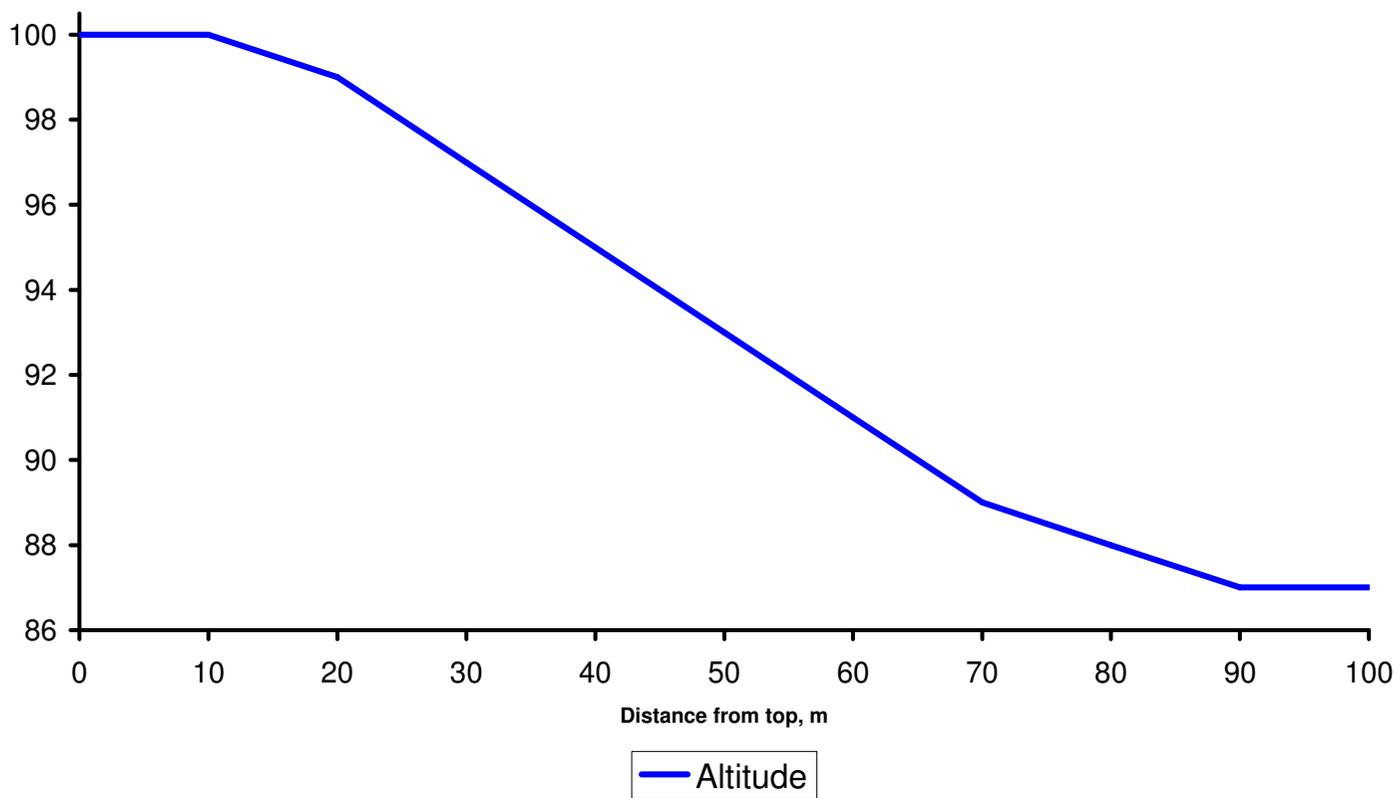
Modelos:

• <sup>137</sup>Cs

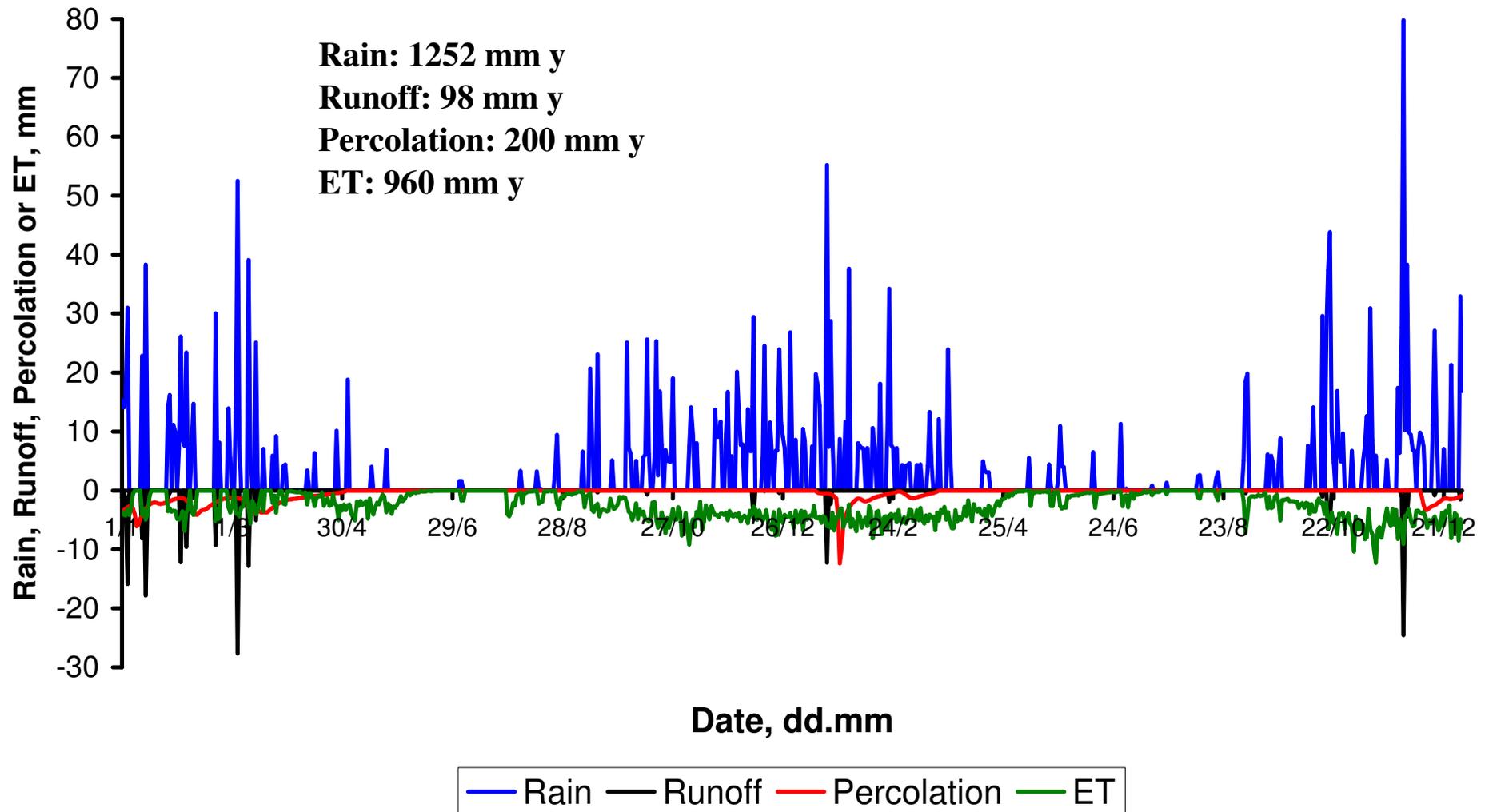
- USLE
- Wepp

Rel. Altitude, m

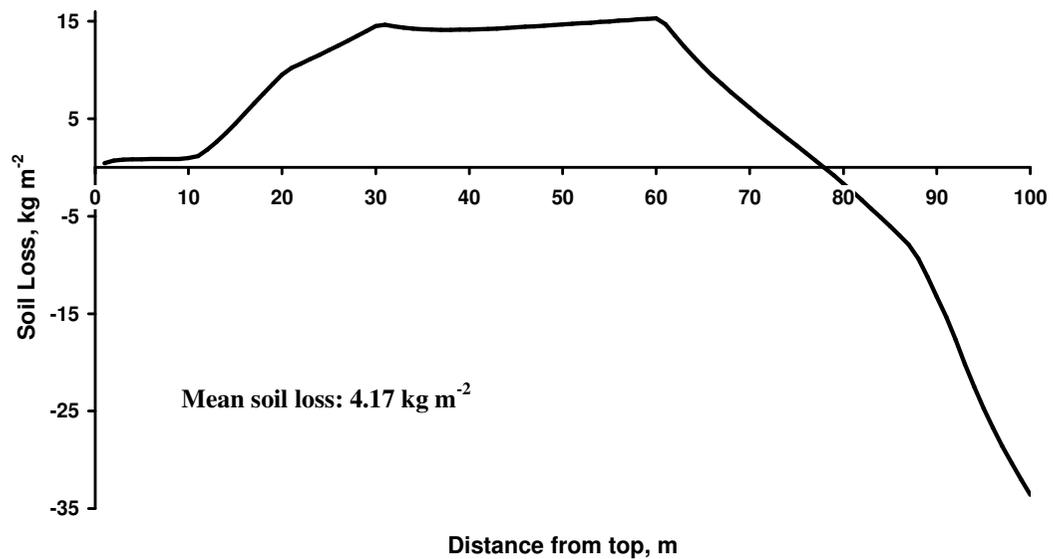
WEPP simulation profile (Piracicaba, Brazil)



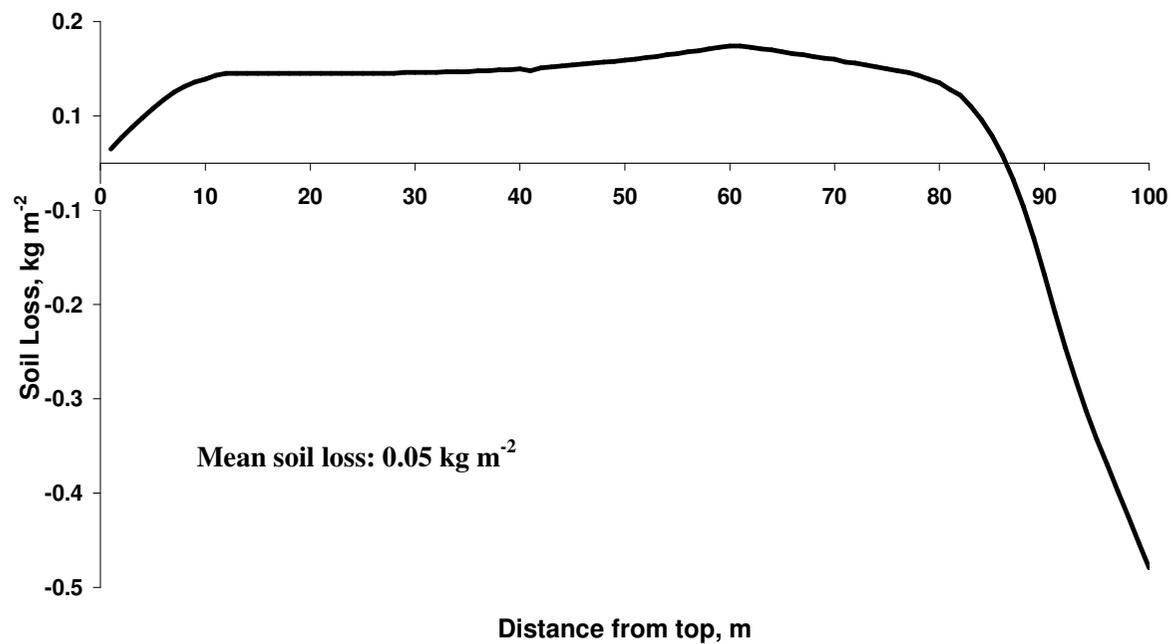
## Rain, runoff, percolation and ET (cane)



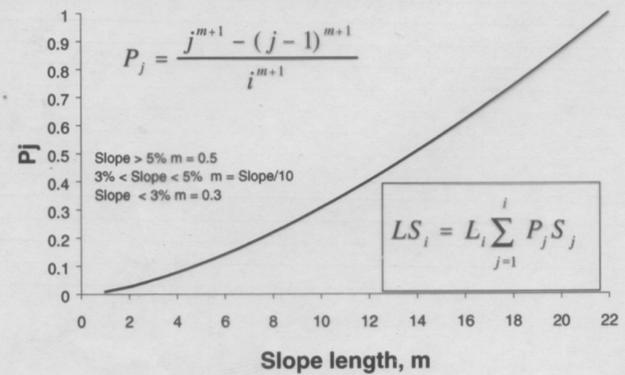
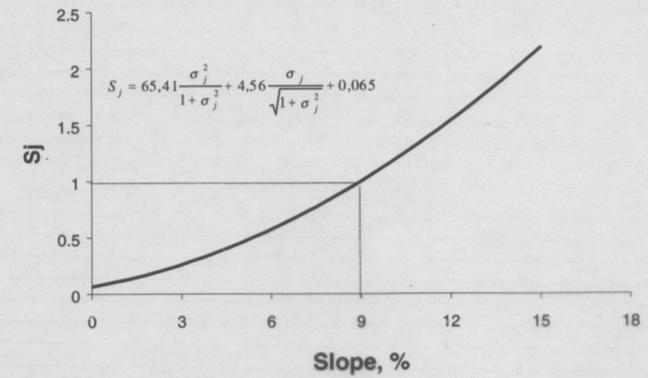
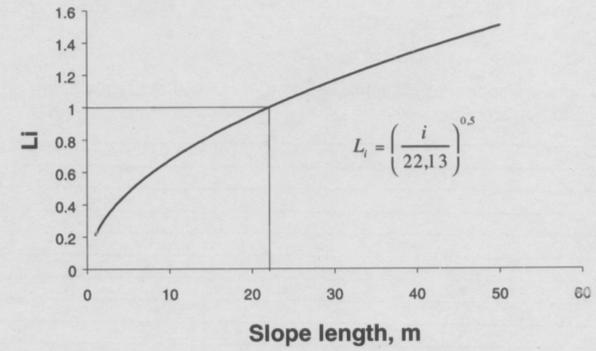
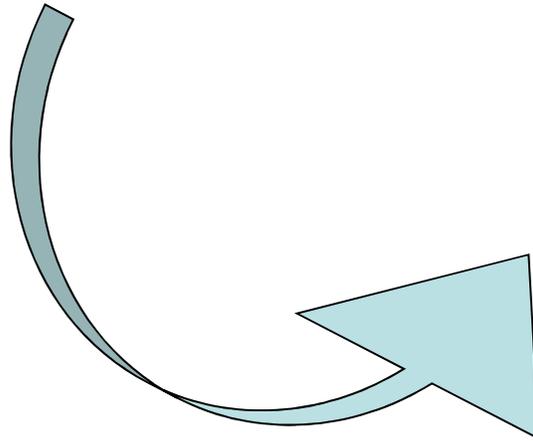
**WEPP simulation soil loss (Corn, Brazil)**

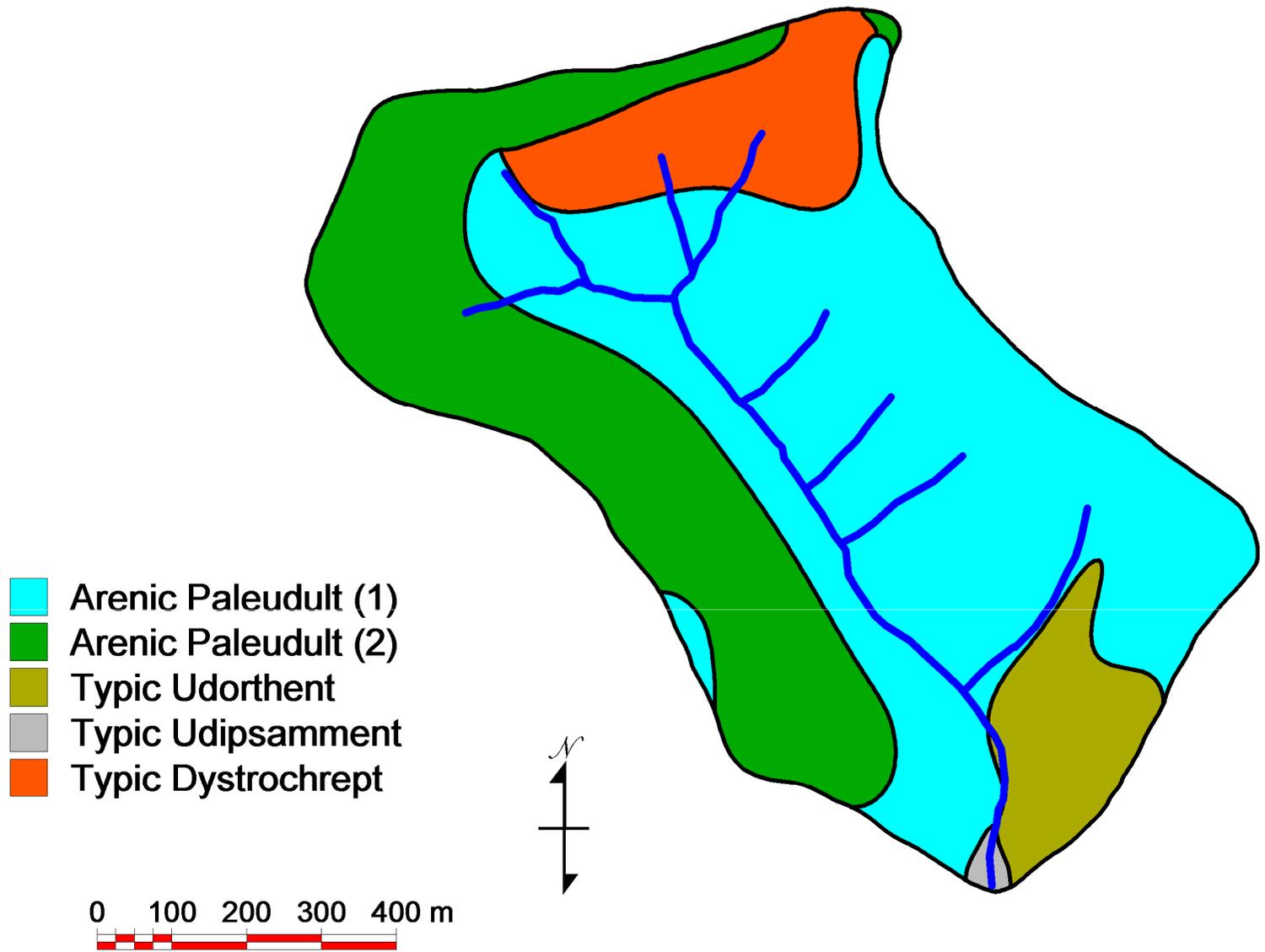


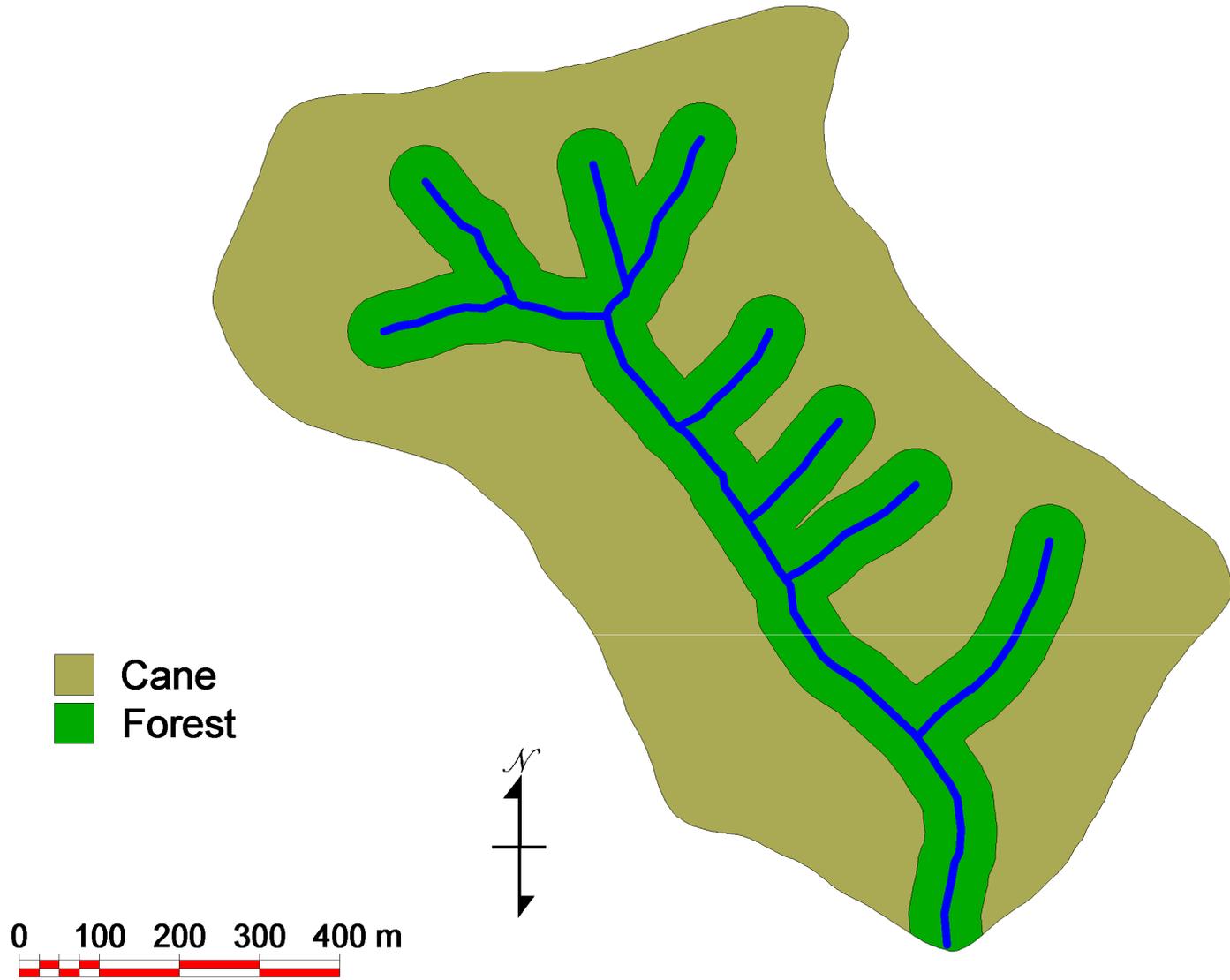
**WEPP simulation soil loss (Forest, Brazil)**

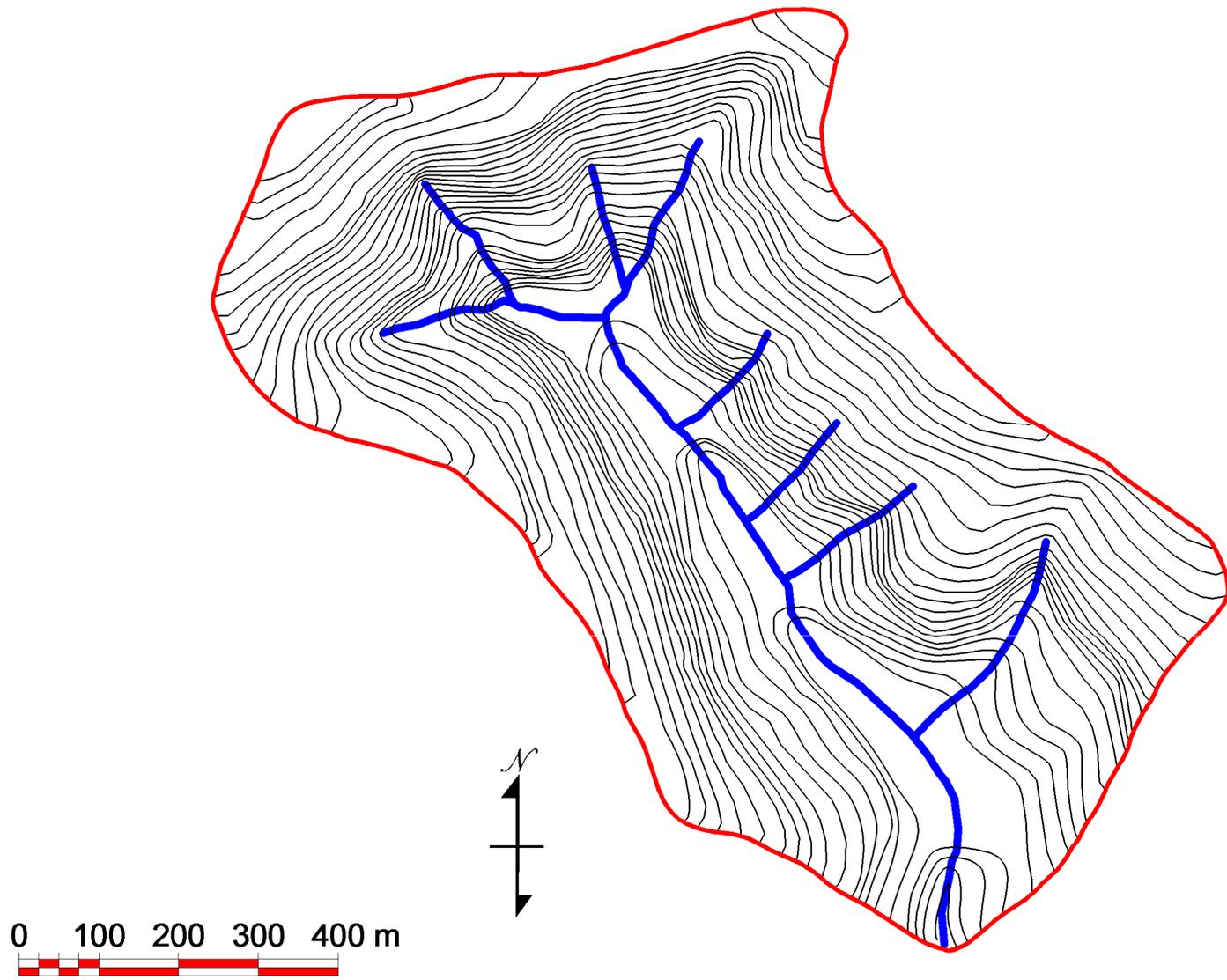


$$A = EI_{30} K L S C P$$

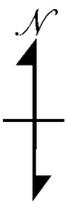


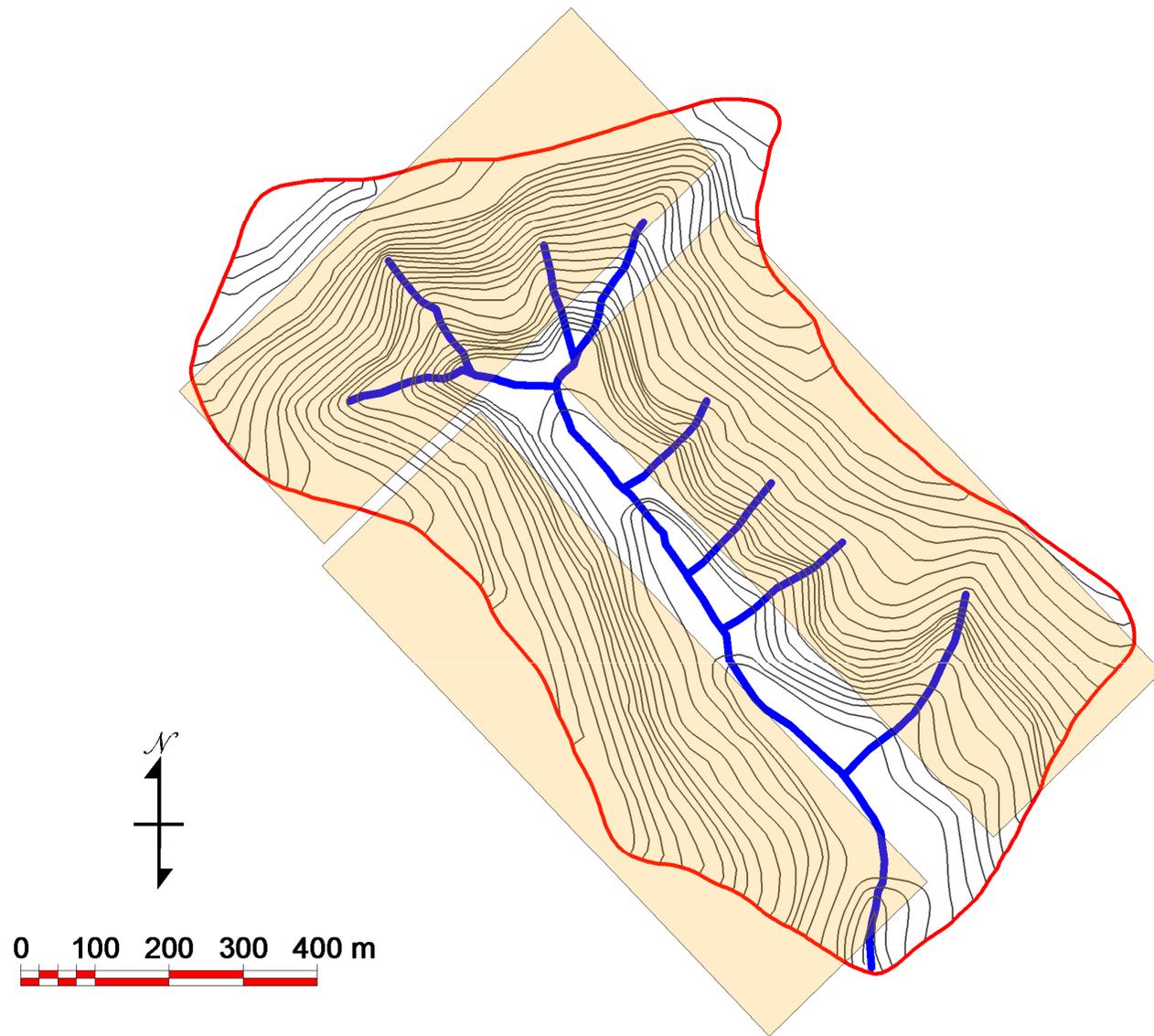






0 100 200 300 400 m





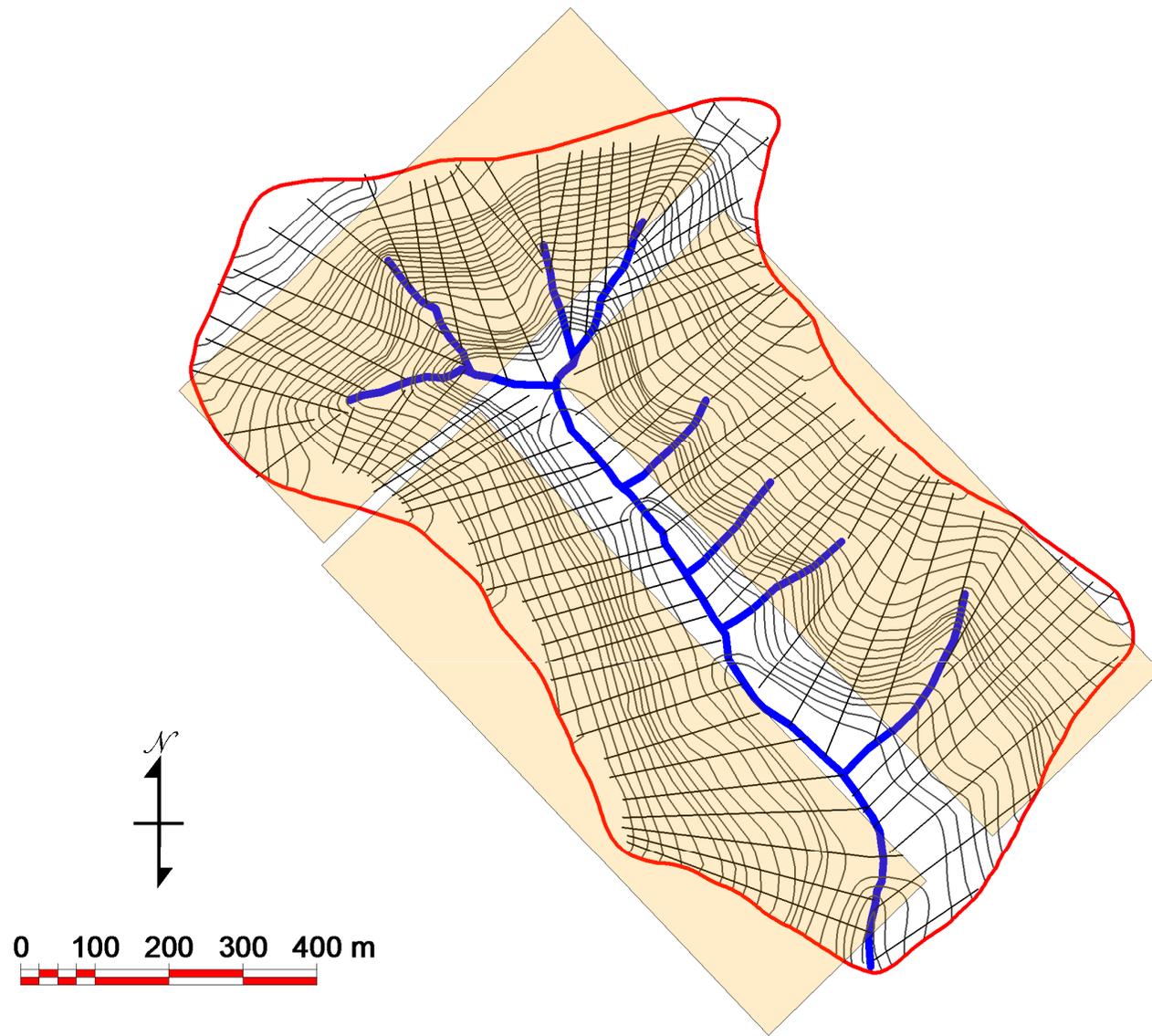


Table 1

Example of input text format database file used for erosion calculations by EDI for WEPP and USLE in Ceveiro watershed for hillslopes 1 and 2 from a total of 84 hillslopes

X <sup>a</sup>	Y <sup>b</sup>	Z <sup>c</sup>	Soil <sup>d</sup>	Land use <sup>e</sup>	Hillslope <sup>f</sup>
215972.14	7492357.91	500	5	1	1
215990.84	7492351.37	498	5	1	1
216012.30	7492343.87	496	5	1	1
216036.98	7492335.24	494	5	1	1
216064.13	7492325.75	492	5	1	1
216093.04	7492315.65	490	5	1	1
216109.58	7492309.86	488	5	1	1
216125.73	7492304.22	486	5	1	1
216145.52	7492297.30	484	3	1	1
216168.09	7492289.41	482	3	1	1
216188.68	7492282.21	480	3	1	1
216196.28	7492279.56	478	3	1	1
216204.46	7492276.70	476	3	1	1
216218.54	7492271.77	474	3	1	1
216236.58	7492265.47	472	3	1	1
216253.16	7492259.67	470	3	1	1
216263.90	7492255.92	468	3	1	1
216274.53	7492252.20	466	3	1	1
216288.76	7492247.23	464	23	1	1
215972.28	7492367.25	500	5	1	2
215992.31	7492362.44	498	5	1	2
216010.06	7492358.18	496	5	1	2
216033.34	7492352.59	494	5	1	2
216061.82	7492345.76	492	5	1	2
216091.39	7492338.66	490	5	1	2
216108.31	7492334.60	488	5	1	2
216123.42	7492330.97	486	5	1	2
216143.98	7492326.04	484	5	1	2
216169.89	7492319.82	482	3	1	2
216191.85	7492314.55	480	3	1	2
216204.36	7492311.55	478	3	1	2
216215.97	7492308.76	476	3	1	2
216229.35	7492305.55	474	3	1	2
216249.48	7492300.72	472	3	1	2
216268.06	7492296.26	470	3	1	2
216279.50	7492293.51	468	3	1	2
216291.42	7492290.65	466	3	1	2

<sup>a</sup>Easting in Universal Transverse Mercator (UTM) coordinates (zone 23S, ellipsoid IUGG 1967, datum South American 1969 Brazil).

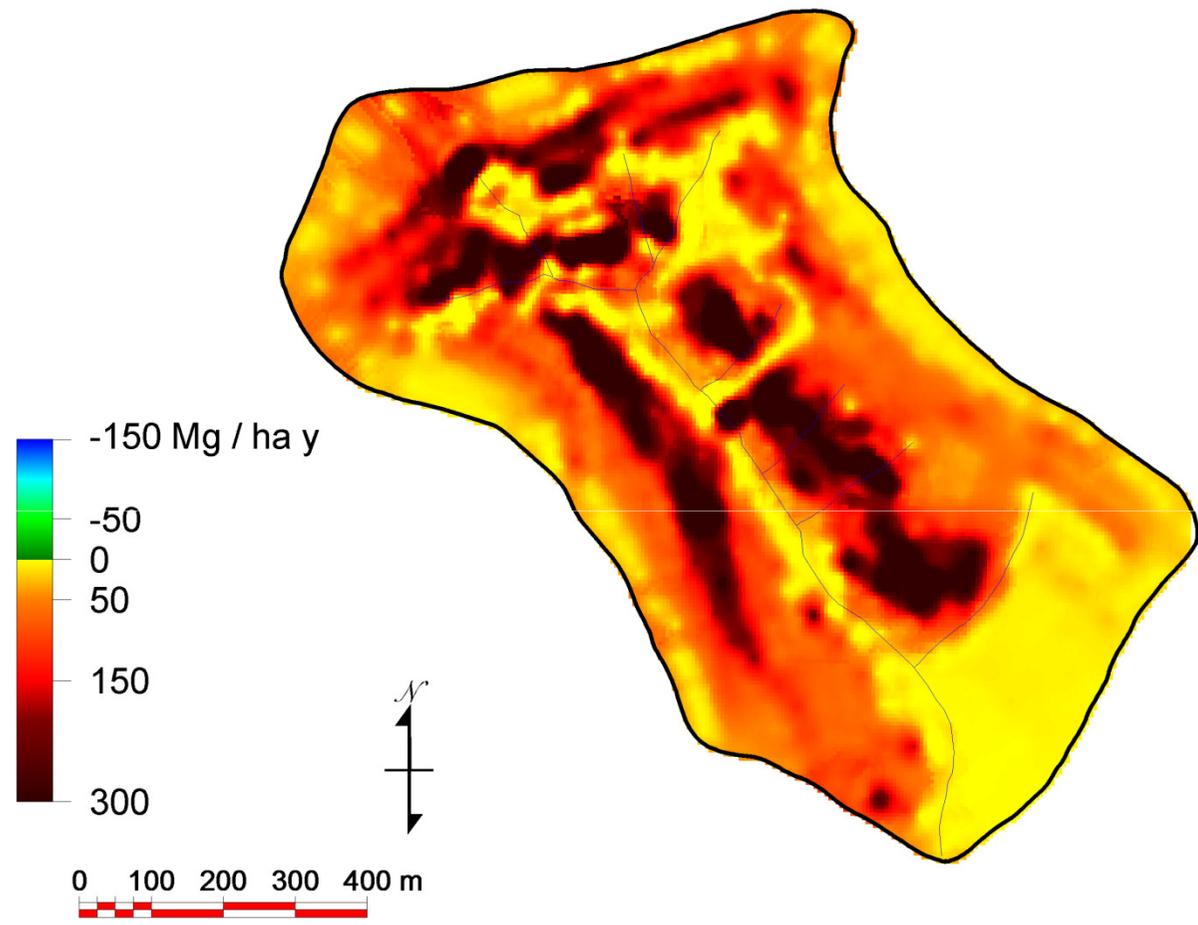
<sup>b</sup>Northing in UTM coordinates.

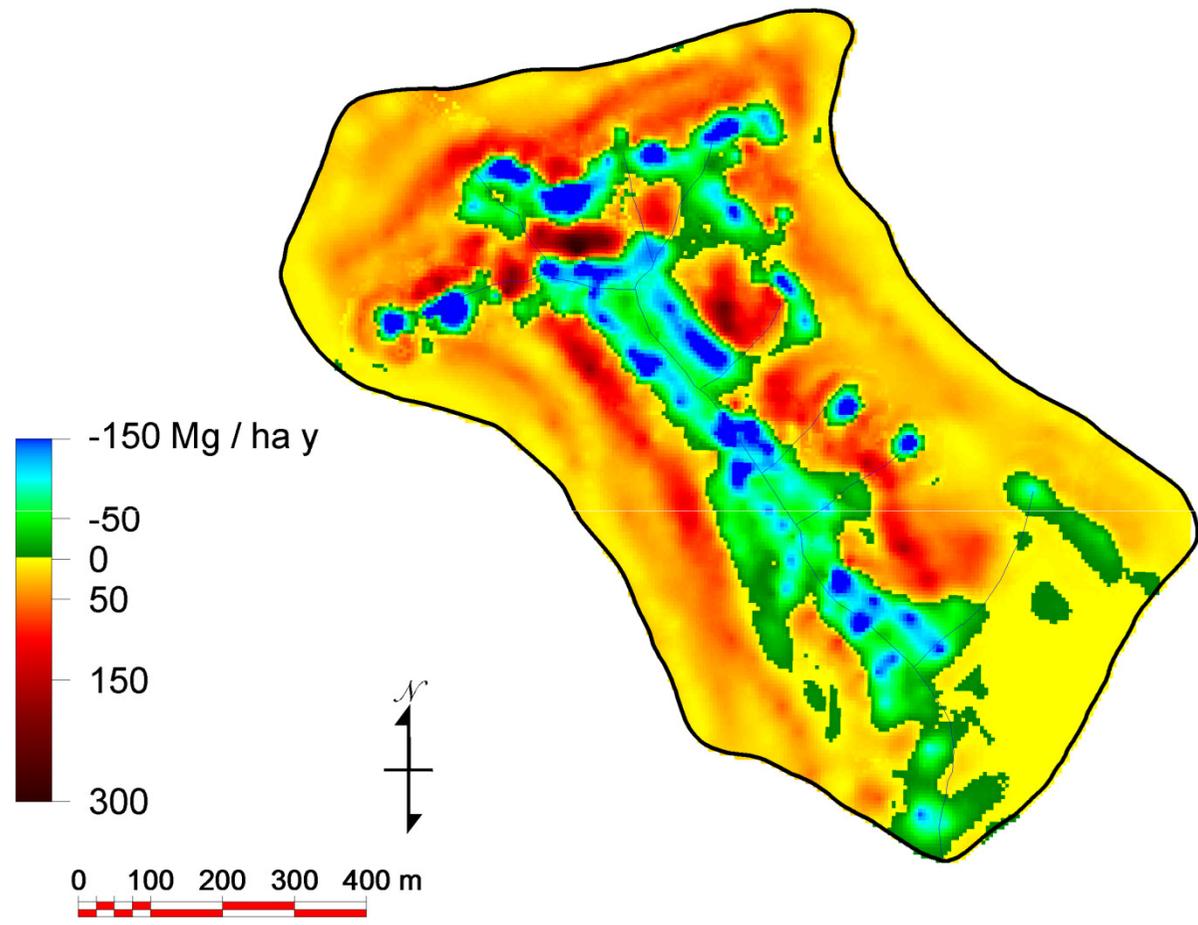
<sup>c</sup>Altitude (BSL) in metric units extracted from the digital contour line map from the Ceveiro watershed.

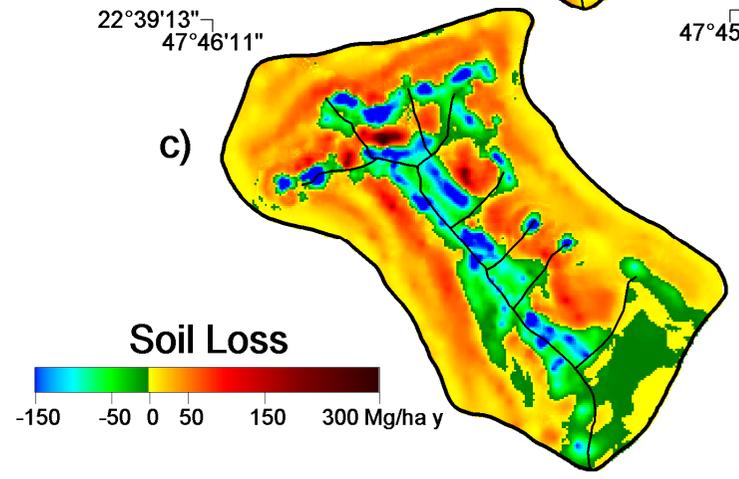
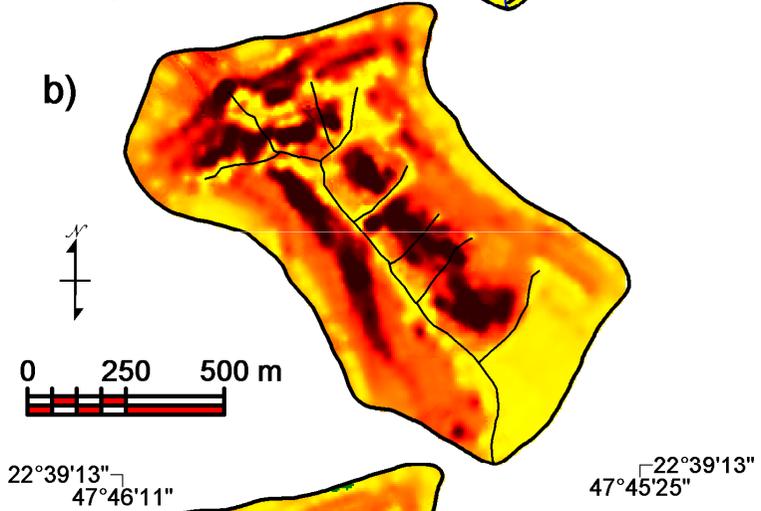
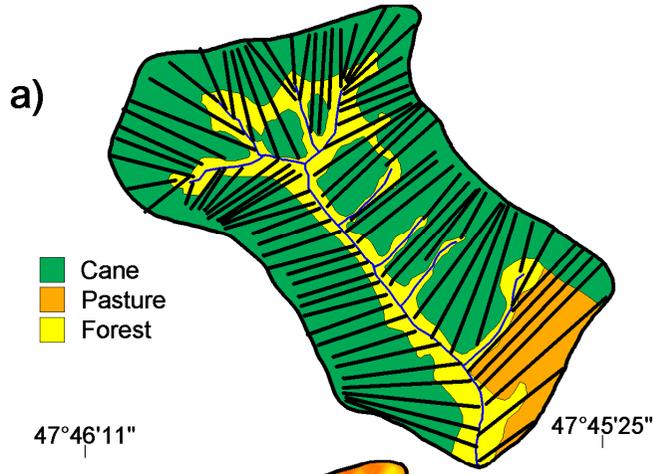
<sup>d</sup>Soil type, where 3—Arenic Paleudult; 5—Typic Dystrachrept and 23—Typic Udorthent.

<sup>e</sup>Land use, where 1—sugarcane.

<sup>f</sup>Hillslope number.

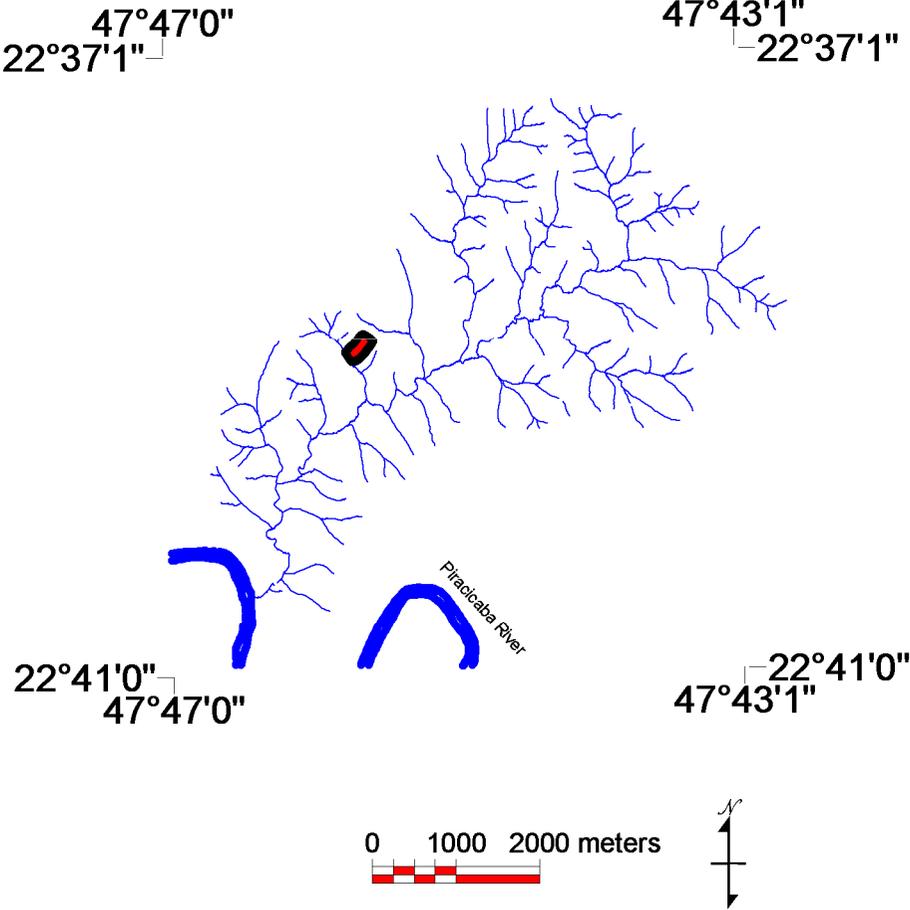




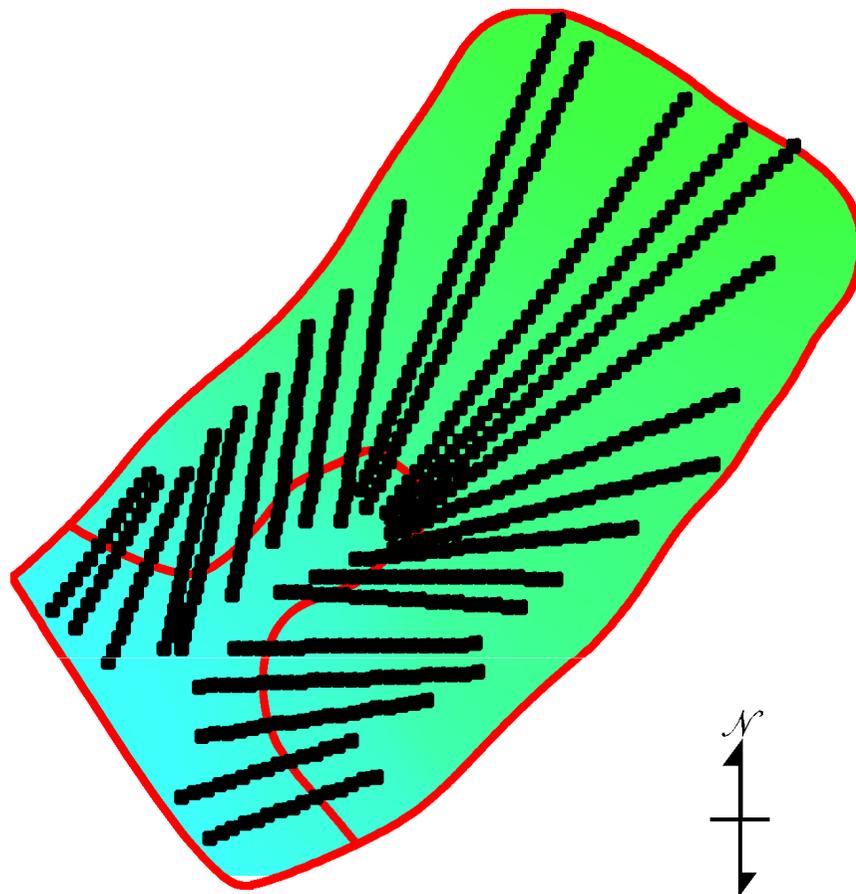


# Ceveiro Watersehd

Area: 6 ha  
Soil: Arenic Paleudult  
Climate: Cwa  
Rainfall: 1,200 mm y

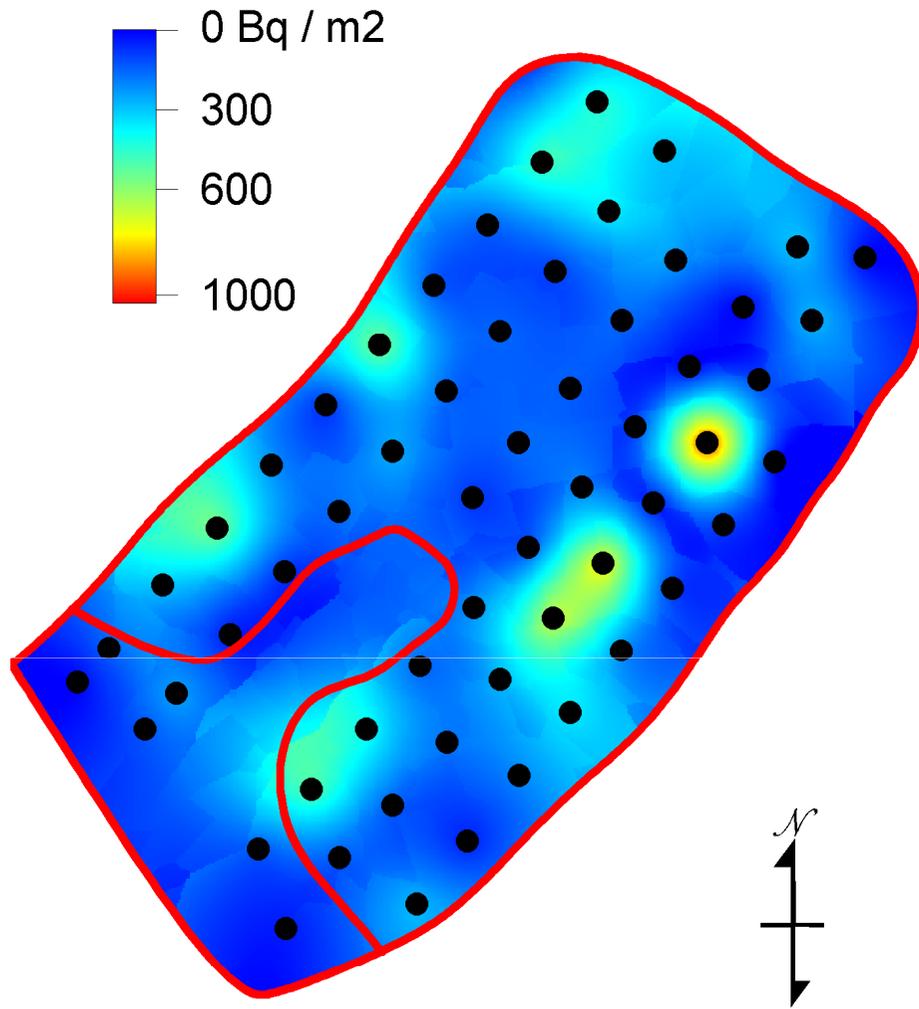






WEPP and USLE estimation points



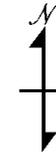
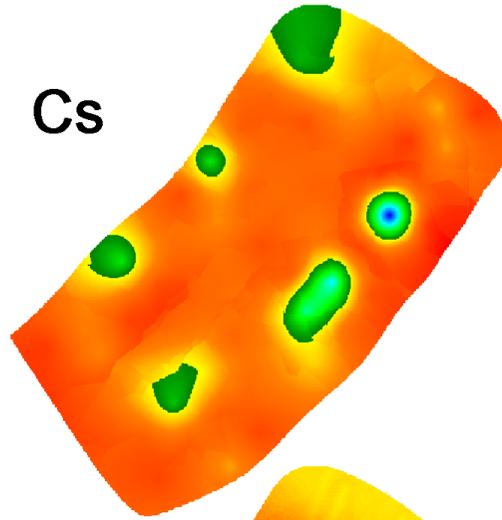


$^{137}\text{Cs}$  activity

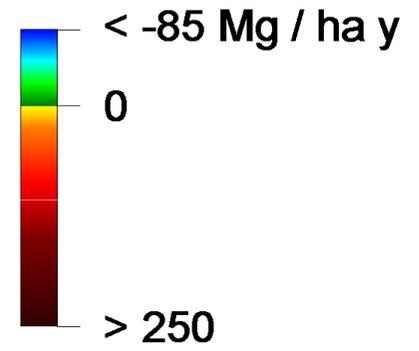
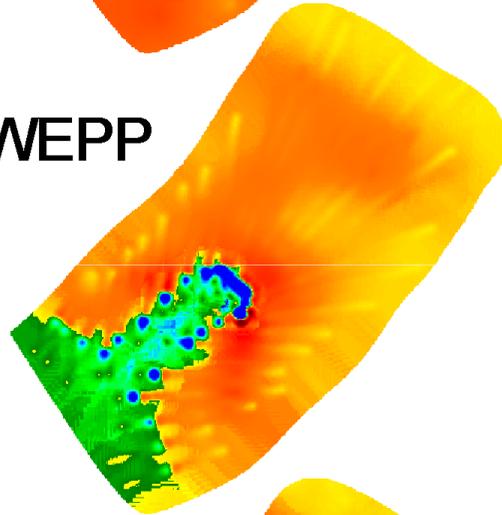




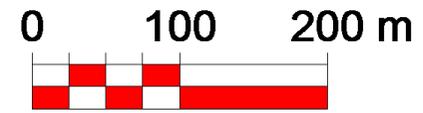
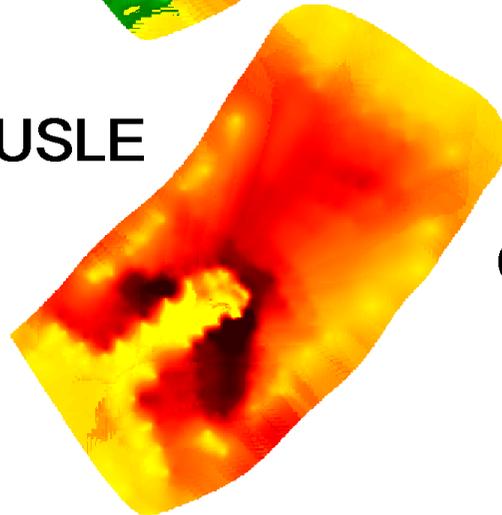
Cs



WEPP



USLE



WEPP output results are contained in several files, among those the files with extension .wtr. These files are optionally created and contain detailed information about accumulated runoff estimates at the lower end of each OFE for each day ( $d$ ) of each one of the  $n$  years ( $y$ ) of the simulation ( $Qac_{ofe,d,y}$ ,  $\text{mm d}^{-1}$  or  $10^{-3} \text{m}^3$  runoff water per  $\text{m}^2$  of contributing area per day). The .wtr files are read by EDI, and daily runoff values are extracted and transformed into annual means for each OFE ( $\bar{Q}ac_{ofe}$ ,  $\text{mm y}^{-1}$ ).

$$\bar{Q}ac_{ofe} = \frac{\sum_{y=1}^n \sum_{d=1}^{365} Qac_{ofe,d,y}}{n}. \quad (1)$$

To estimate runoff values within each OFE, the accumulated runoff volume from the top of the hillslope to the bottom of each OFE ( $Vac_{ofe}$ ,  $\text{m}^3 \text{yr}^{-1}$ ) is computed as

$$Vac_{ofe} = \bar{Q}ac_{ofe} Lac_{ofe} W \times 10^{-3}, \quad (2)$$

where  $Lac_{ofe}$  (m) is the distance between the top of the hillslope and the bottom of the OFE and  $W$  (m) is the width of the OFEs. Assuming mass conservation, the volume of runoff produced by each OFE ( $V_{ofe}$ ,  $\text{m}^3 \text{y}^{-1}$ ) can be calculated as

$$V_{ofe} = Vac_{ofe} - Vac_{ofe-1} \quad (3)$$

and from  $V_{ofe}$  the average runoff for the OFE ( $Qavg_{ofe}$ ,  $\text{mm y}^{-1}$ ) can be computed as

$$Qavg_{ofe} = \frac{V_{ofe}}{L_{ofe} W} \times 10^3, \quad (4)$$

where  $L_{ofe}$  (m) is the length of the OFE. As an OFE is defined as a portion of a hillslope with equal soil and management, infiltration rate and runoff production may be assumed constant along one OFE. Therefore it

may be assumed that

$$\begin{aligned} Qavg_{ofe} &= \frac{Qtop_{ofe} + Qbot_{ofe}}{2} \\ &= \frac{Qbot_{ofe-1} + Qbot_{ofe}}{2} \Rightarrow Qbot_{ofe} \\ &= 2Qavg_{ofe} - Qbot_{ofe-1}, \end{aligned} \quad (5)$$

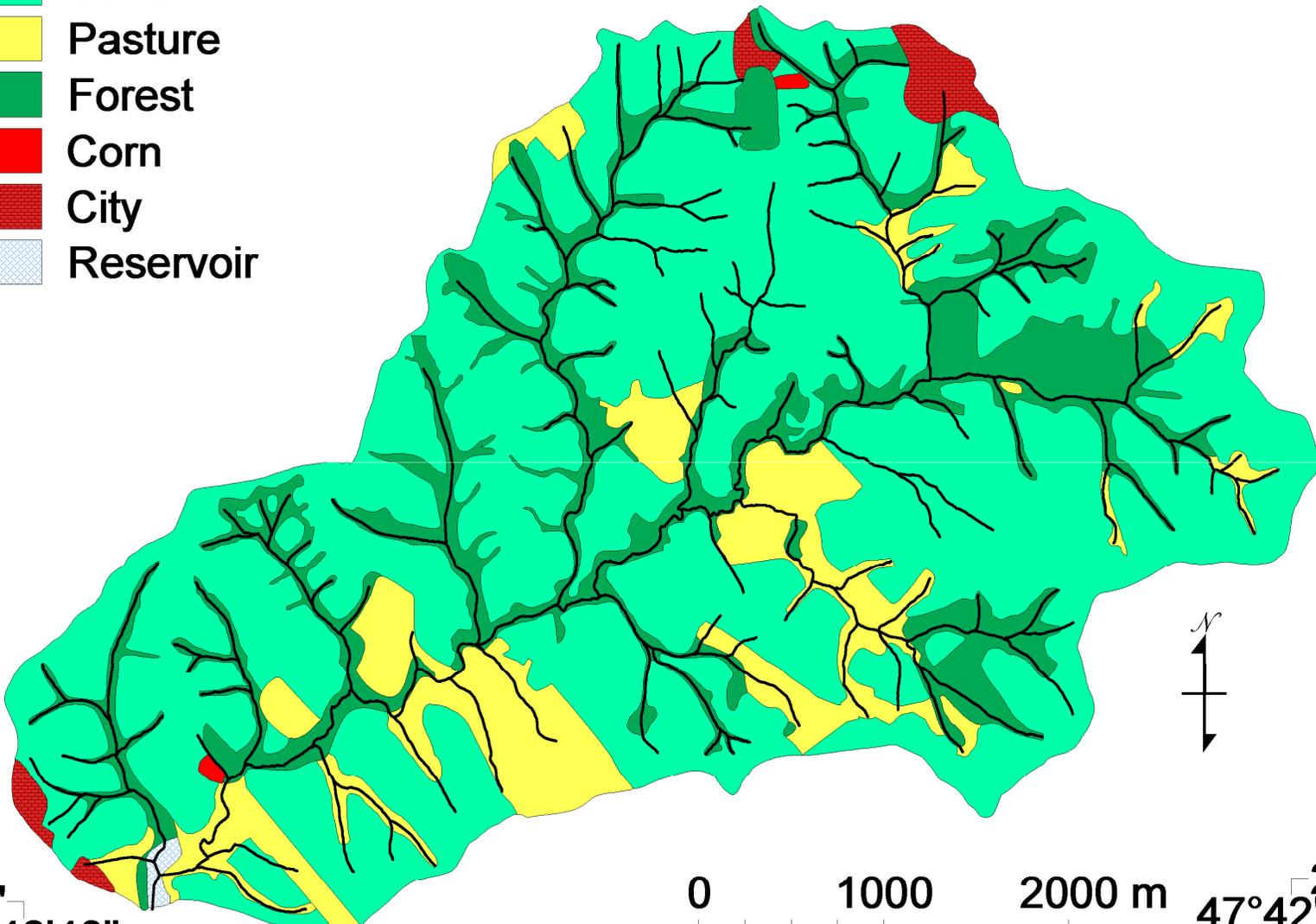
where  $Qtop_{ofe}$  ( $\text{mm yr}^{-1}$ ) and  $Qbot_{ofe}$  ( $\text{mm yr}^{-1}$ ) are the runoff values at the top and the bottom of each OFE, respectively. If it is assumed that runoff at the top of each hillslope equals zero (i.e.,  $Qtop_1 = Qbot_0 = 0$ ), this approach allows estimation of  $Qbot_{ofe}$  for each OFE by interpolating linearly between OFE bottom values. The runoff within each OFE can also be computed. After this, the coordinates not considered by WEPP processing are restored by EDI, and a file containing coordinates and runoff estimates in text format is created.

Order	X	Y	Soil Loss	Runoff
1	218623.1	7495027.6	0.23	17.492
2	218635.2	7495044.9	0.3	18.818
3	218558	7495297.7	0.51	21.247
4	218605	7495182.1	0.79	23.84
5	217093.8	7494673.1	0.87	24.974
6	215438.6	7492096.5	0.91	26.288
7	215386.1	7492204	0.91	26.356
8	218514.1	7495278.6	0.71	27.538
9	218612.8	7495043.8	0.67	27.743
10	215342.7	7492603.4	1.98	32.247
11	217410.8	7494984.7	1.27	34.976
12	217025	7494528.7	2.82	35.833
13	215332.3	7492605.9	2.43	37.158
14	217566.4	7495122.6	1.34	37.971
15	218536.2	7494999	1.48	38.893
16	215366.3	7492602.6	2.47	39.092
17	215363.5	7493013.2	2.83	39.238
18	217018.1	7494509.3	2.95	40.162
19	217024.7	7494524.6	3.14	40.885
20	215353.5	7492601.7	1.92	41.606
21	215375.6	7493012.4	3.24	41.735
22	215380.6	7492605.5	3.15	42.471
23	215973.5	7492327.9	2.92	42.821

47°46'40"  
22°37'1"

47°42'40"  
22°37'1"

- Cane
- Pasture
- Forest
- Corn
- City
- Reservoir



22°39'50"  
47°46'40"

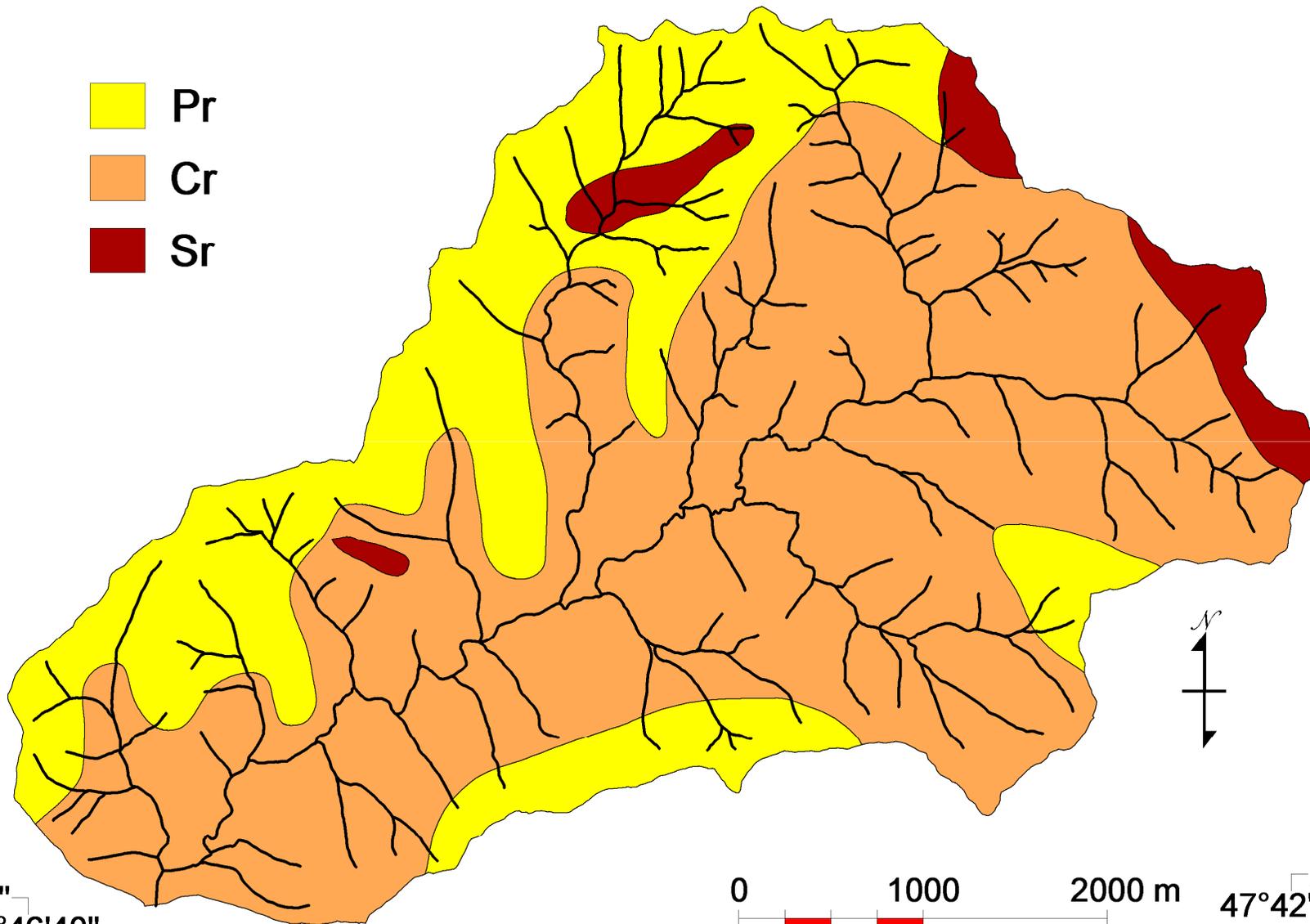
0 1000 2000 m

22°39'50"  
47°42'40"

47°46'40"  
22°37'1"

47°42'40"  
22°37'1"

- Pr
- Cr
- Sr



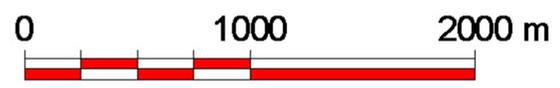
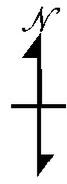
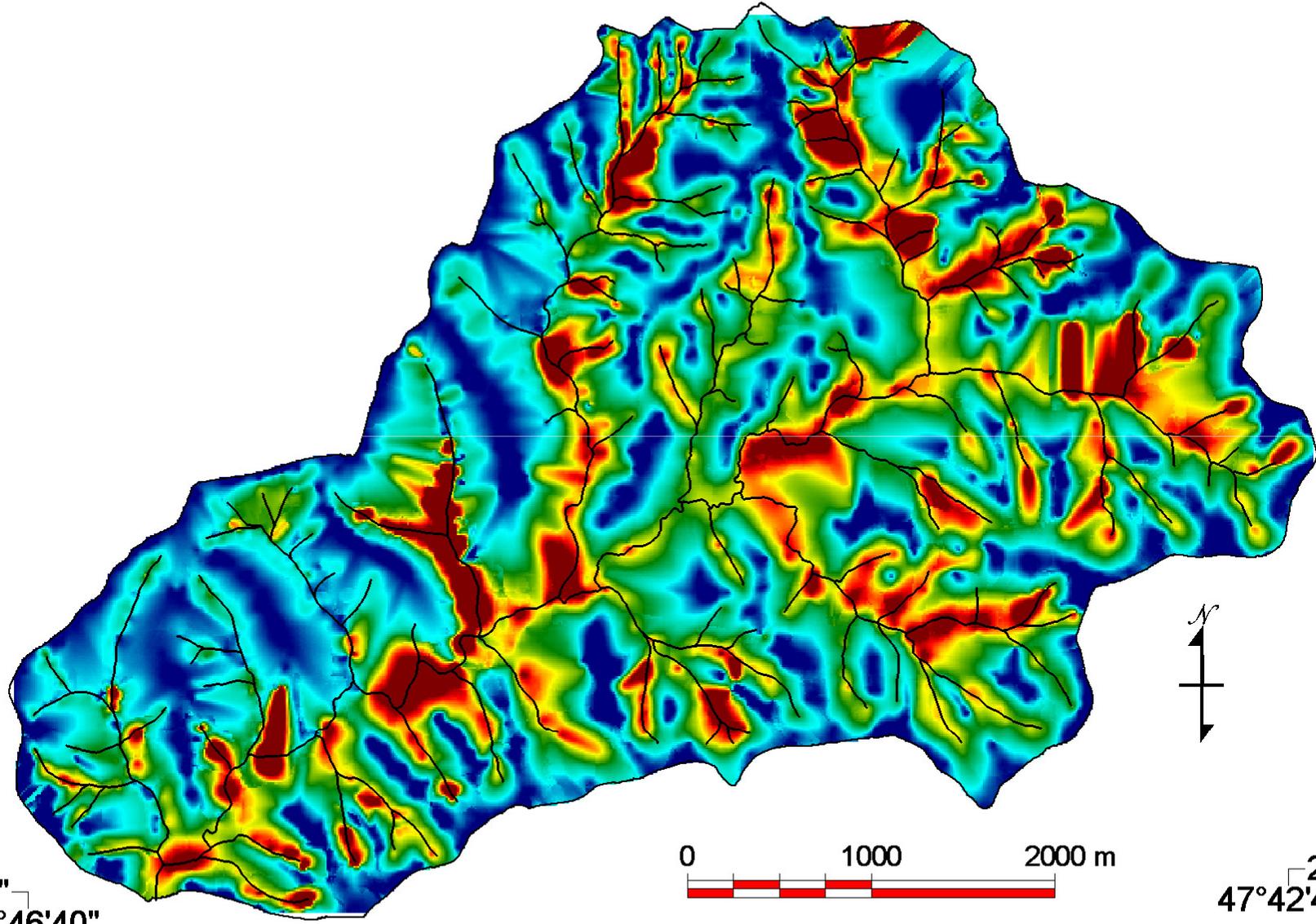
22°39'50"  
47°46'40"

0 1000 2000 m

22°39'50"  
47°42'40"

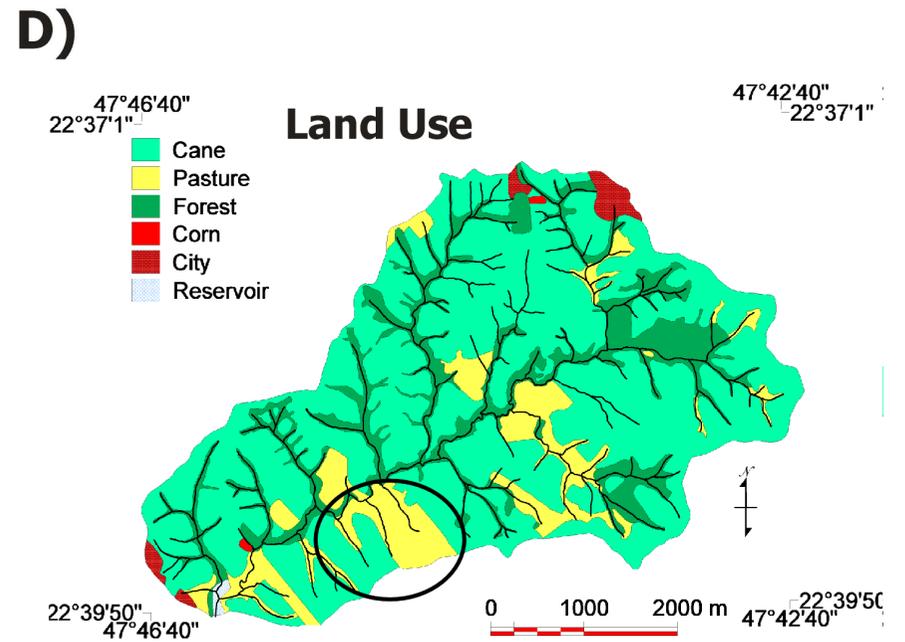
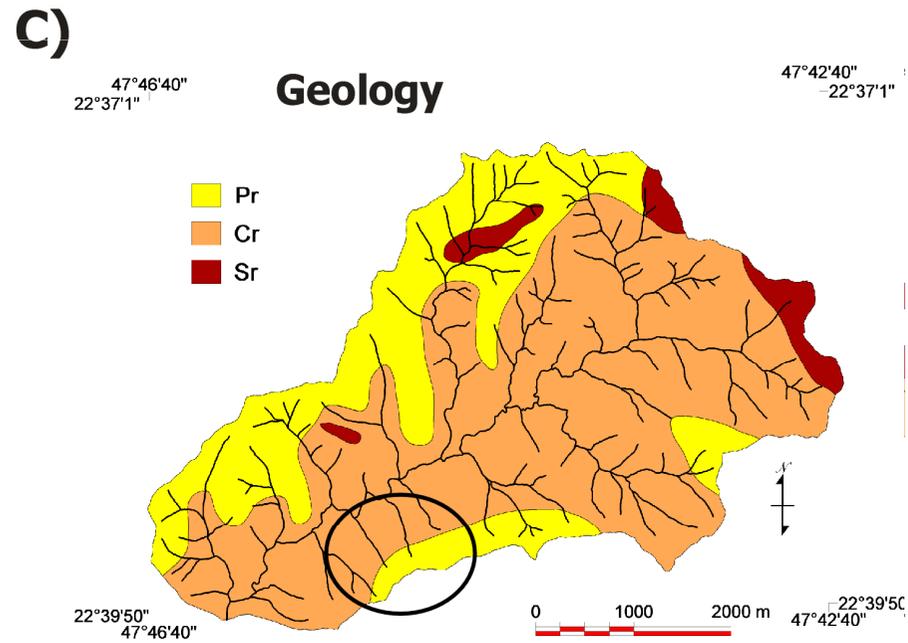
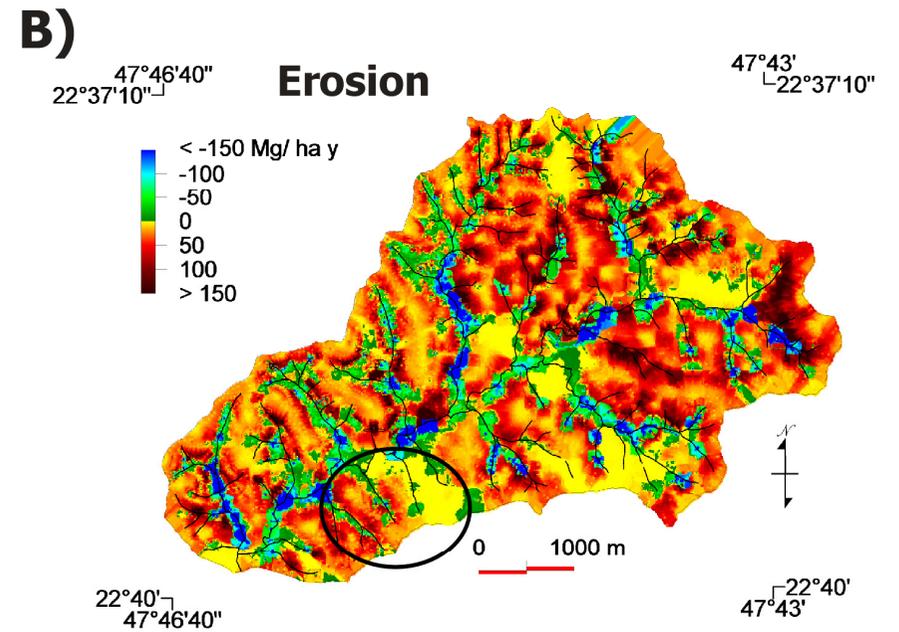
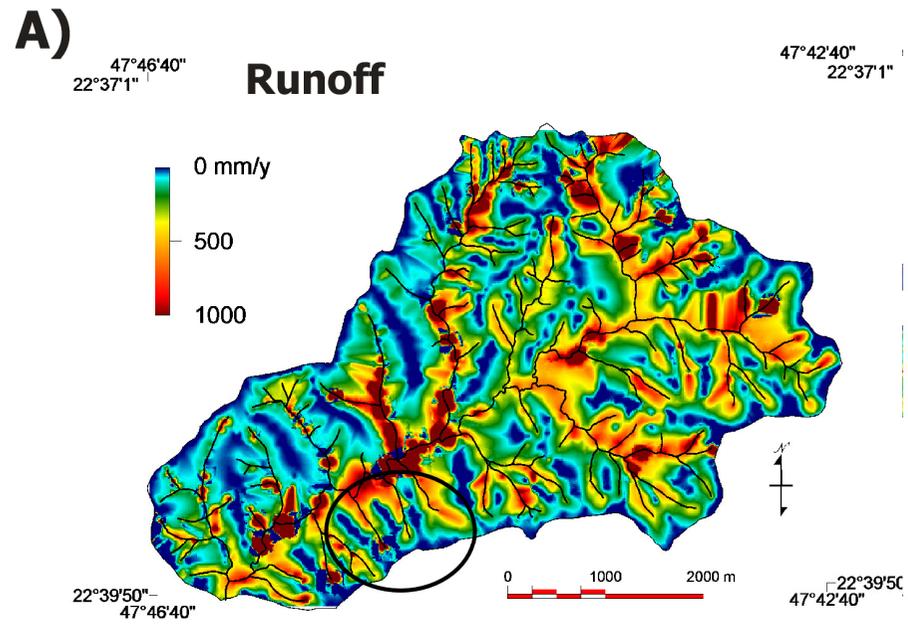
47°46'40"  
22°37'1"

47°42'40"  
22°37'1"



22°39'50"  
47°46'40"

22°39'50"  
47°42'40"



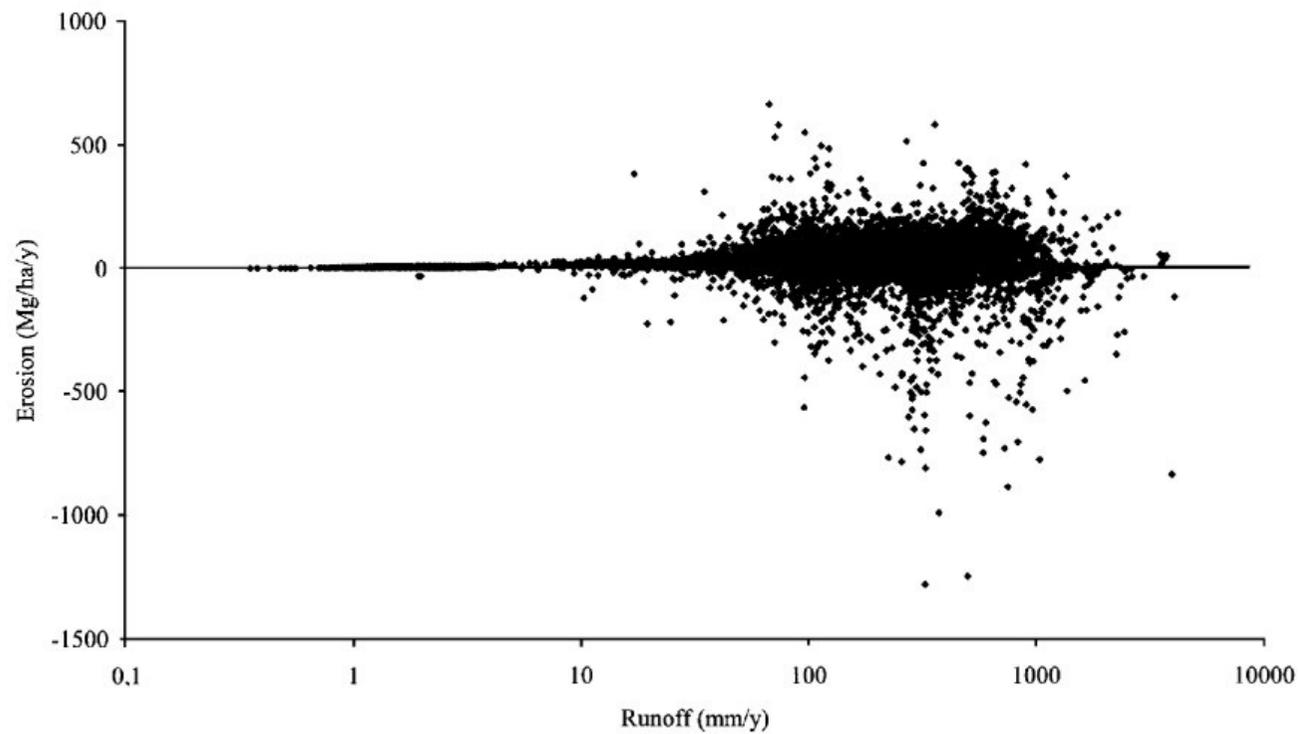


Fig. 3. WEPP 100-year simulation mean soil erosion estimates plotted against runoff estimates for Ceveiro watershed (negative erosion values indicate deposition in WEPP).