



Escola Politécnica da
Universidade de São Paulo

PME 3380
Lista G

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São Paulo

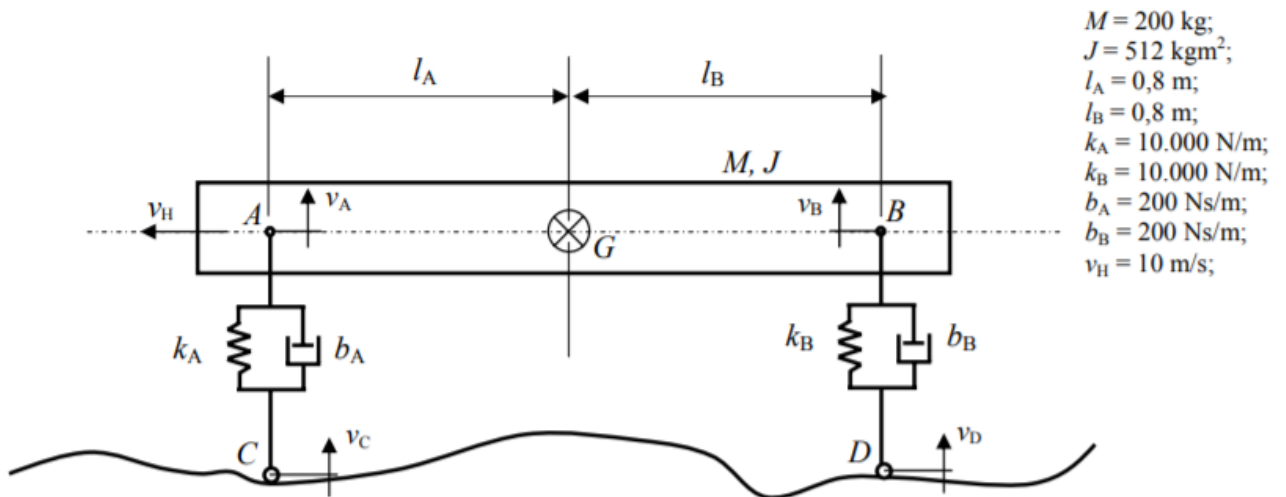
2020

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1 PRIMEIRO EXERCÍCIO

O primeiro exercício consiste na obtenção do modelo que descreve o problema do meio-carro, representado na imagem abaixo:



Os desenvolvimentos feitos podem ser observados a seguir:

\vec{v}_H
 \vec{v}_A
 \vec{v}_B
 \vec{v}_C
 \vec{v}_D

$TQMA:$
 $\vec{M}_G^{ext} = m (\vec{G} \cdot \vec{G}) \wedge \vec{\omega}_G + \int \vec{r} \wedge \vec{v} \, dk$
 $= \sum \vec{r} \wedge \vec{F}_j = - (l_A \cos \alpha \vec{i} \wedge (-k_A(x_A - x_C) + b_A(\dot{x}_A - \dot{x}_C)))$
 $+ (l_B \cos \alpha \vec{i} \wedge (-k_B(x_B - x_D) + b_B(\dot{x}_B - \dot{x}_D)))$

$\Rightarrow \cos \alpha = 1 \Rightarrow \int \vec{r} \wedge \vec{v} = l_A(x_A - x_C) \dot{x}_A - l_B(x_B - x_D) \dot{x}_B + l_A b_A(\dot{x}_A - \dot{x}_C) - l_B b_B(\dot{x}_B - \dot{x}_D)$

$TMB:$
 $\vec{R} = m \vec{a}_G \Rightarrow m \cdot \vec{v}_G = -k_A(x_A - x_C) - k_B(x_B - x_D) - b_A(\dot{x}_A - \dot{x}_C) - b_B(\dot{x}_B - \dot{x}_D)$

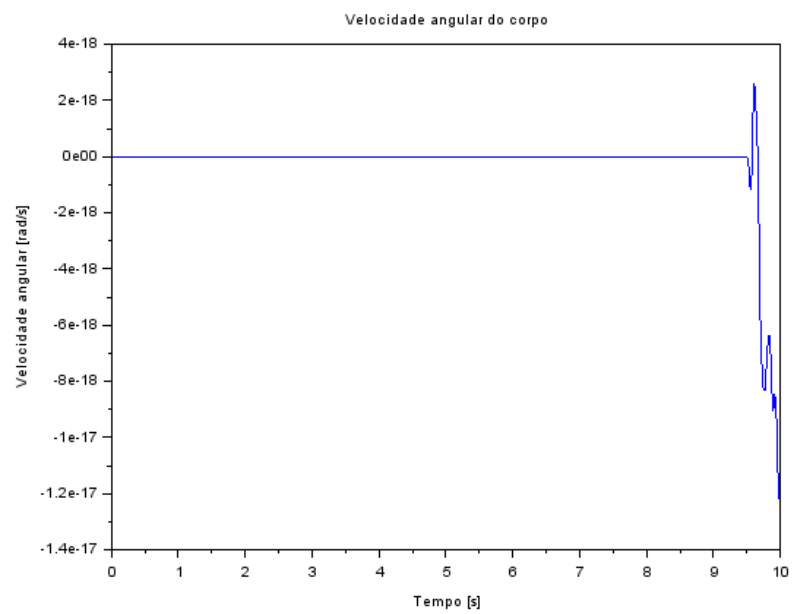
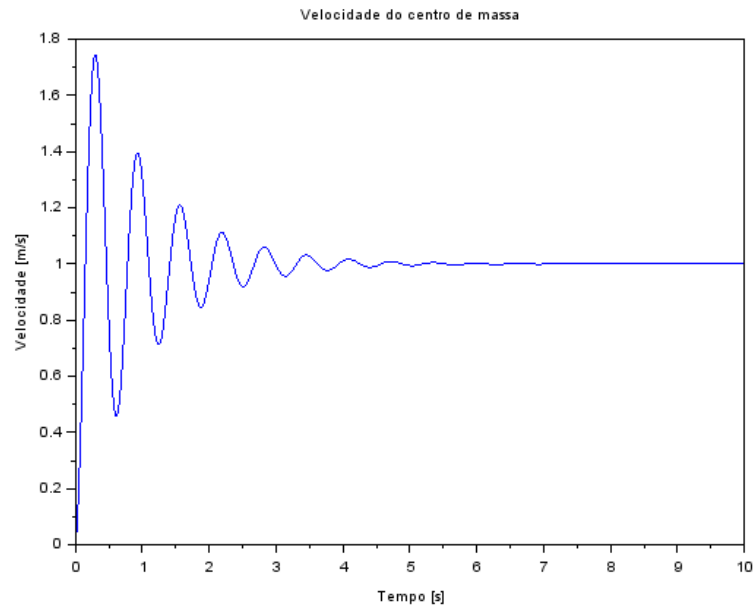
$V_A \vec{j} = V_G \vec{j} + \omega \vec{k} \wedge (-l_A \vec{i}) \Rightarrow V_A = V_G - \omega l_A$
 $V_B \vec{j} = V_G \vec{j} + \omega \vec{k} \wedge (l_B \vec{i}) \Rightarrow V_B = V_G + \omega l_B$

$$\begin{bmatrix} \dot{x}_A \\ \dot{x}_B \\ V_G \\ \dot{\omega} \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 & -l_A \\ 0 & 0 & 1 & l_B \\ -k_A/m & -k_B/m & -(b_A + b_B)/m & \frac{b_A l_A - b_B l_B}{m} \\ \frac{l_A k_A}{J} & -\frac{l_B k_B}{J} & \frac{l_A b_A - l_B b_B}{J} & -\frac{(b_A l_A^2 + b_B l_B^2)}{J} \end{bmatrix} \begin{bmatrix} x_A \\ x_B \\ V_G \\ \omega \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ k_A/m & k_B/m & b_A/m & b_B/m \\ -l_A k_A & l_B k_B & -l_A b_A & l_B b_B \end{bmatrix} \begin{bmatrix} x_C \\ x_D \\ \dot{x}_C \\ \dot{x}_D \end{bmatrix}$$

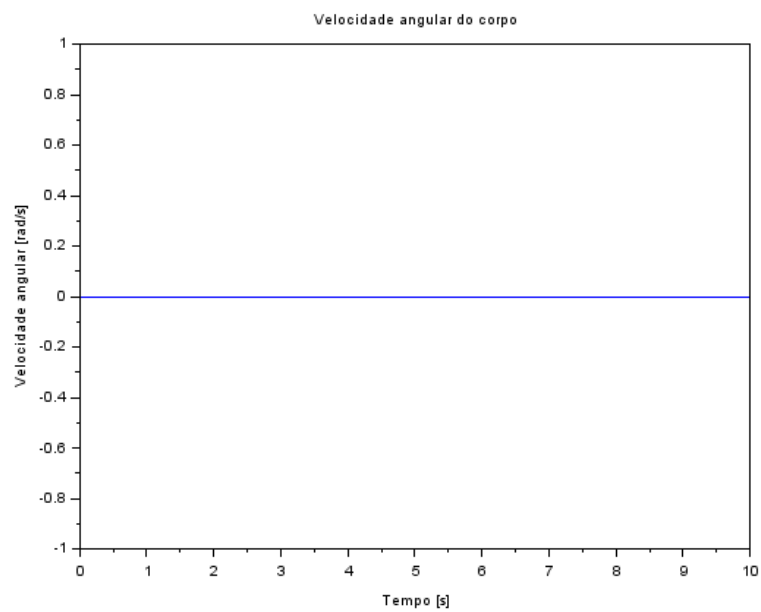
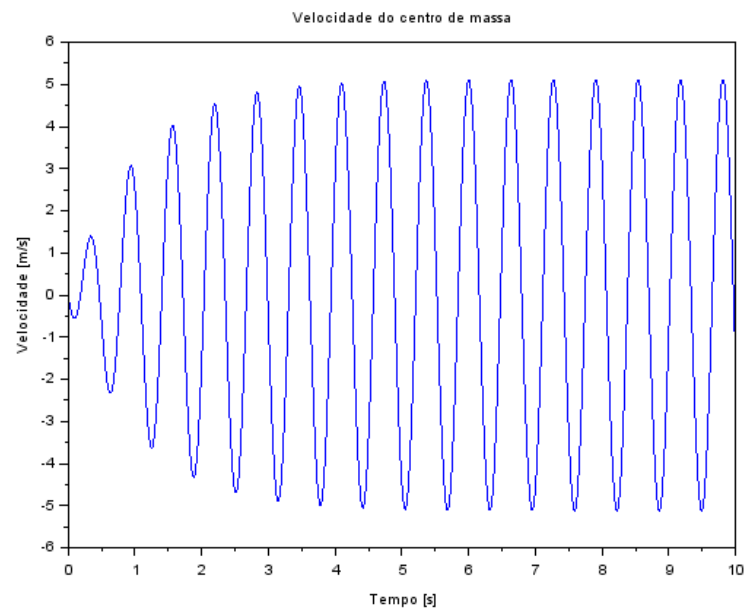
$\zeta_D = \frac{l_A + l_B}{V_H}$

2 SIMULAÇÃO DO MEIO-CARRO

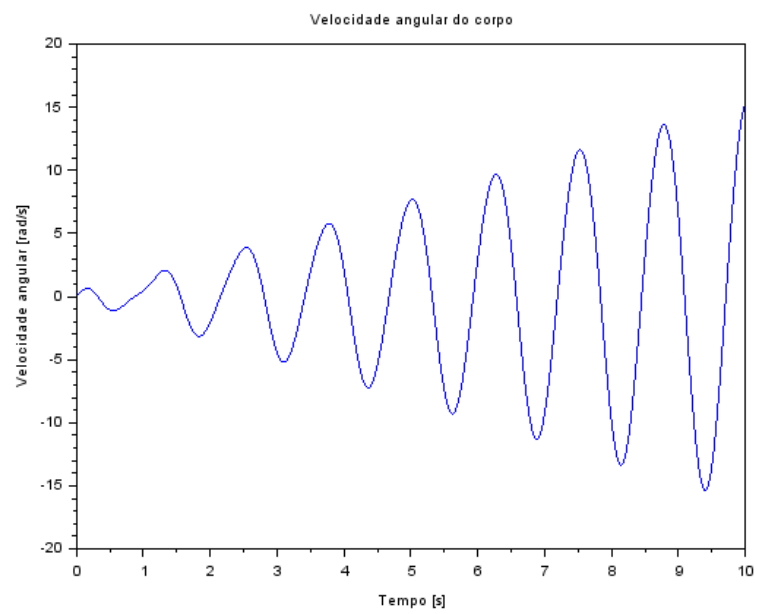
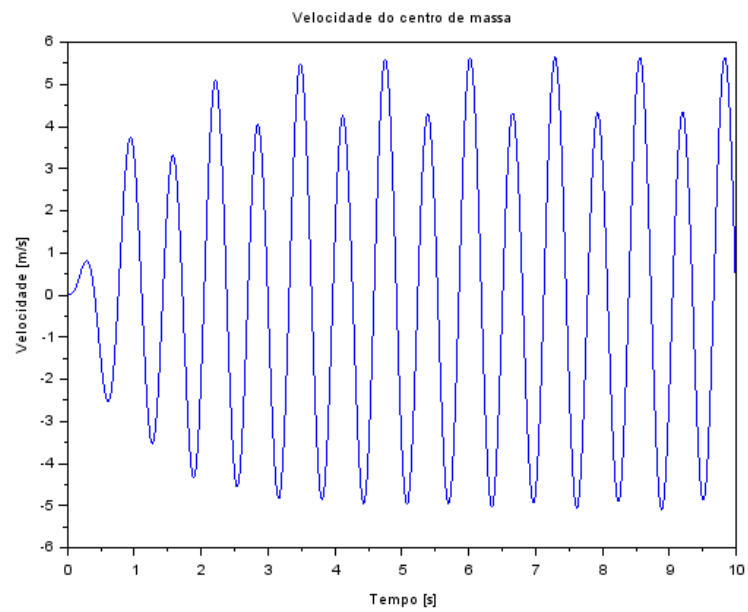
2.1 SIMULAÇÃO 1



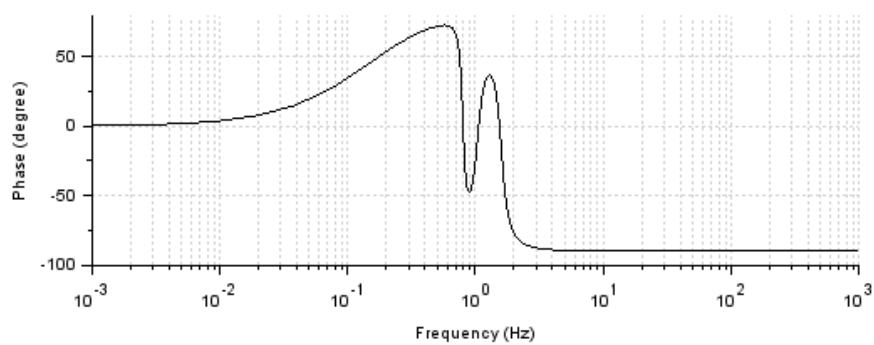
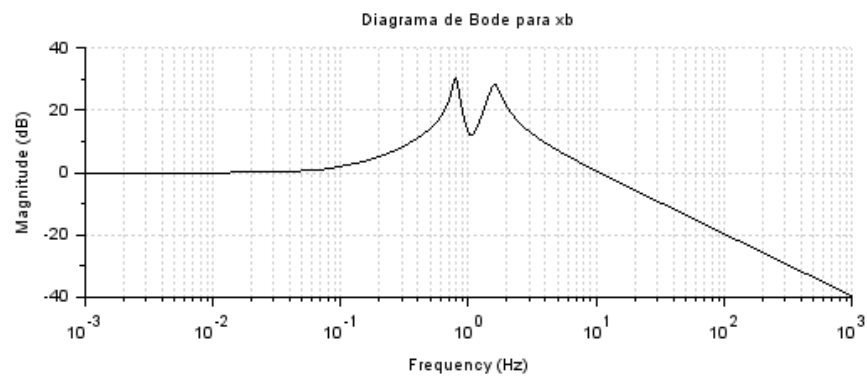
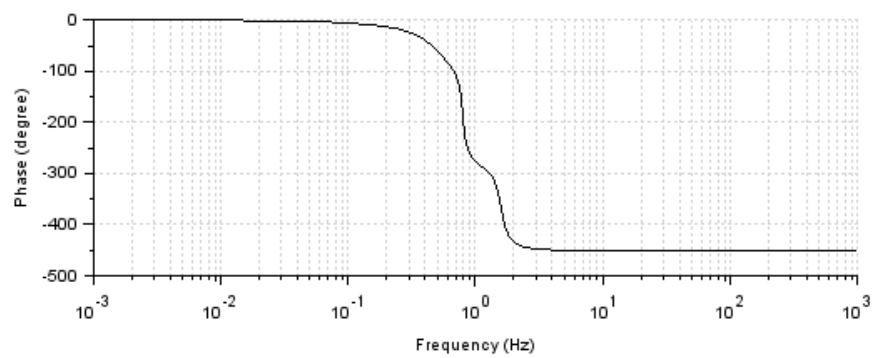
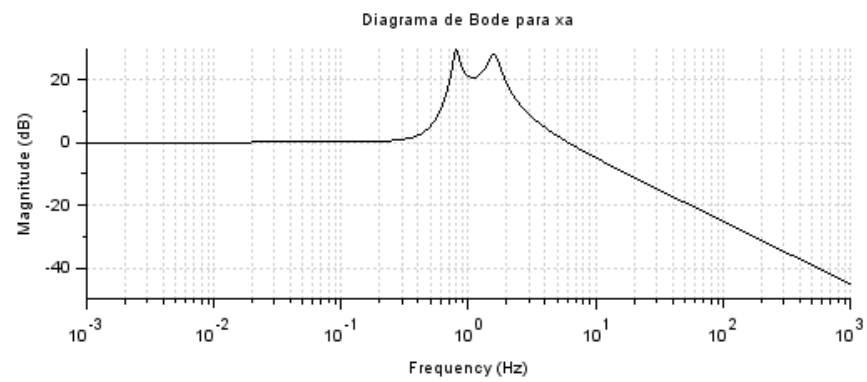
2.2 SIMULAÇÃO 2

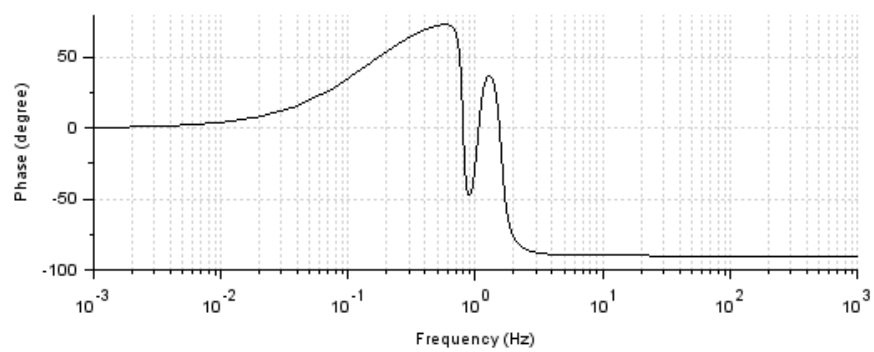
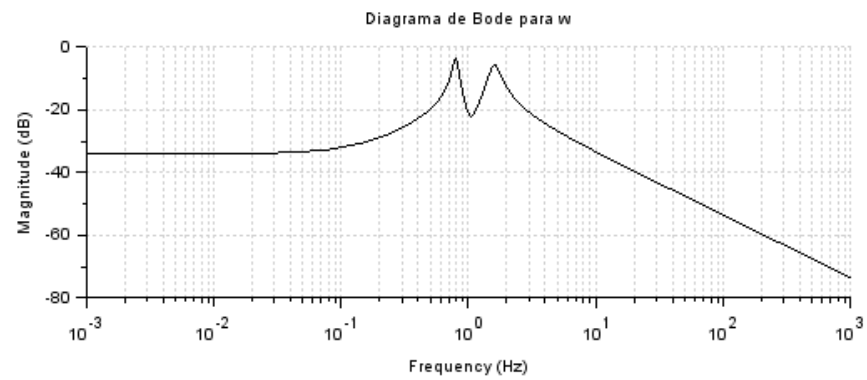
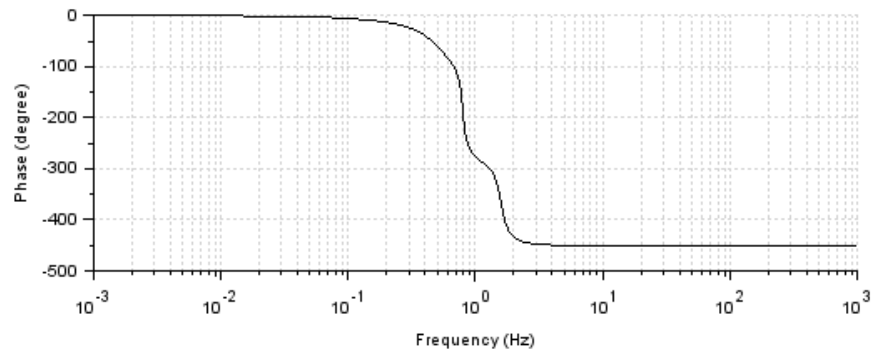
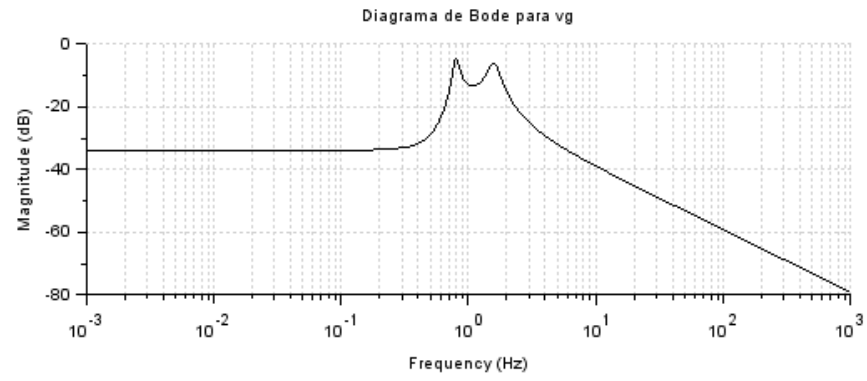


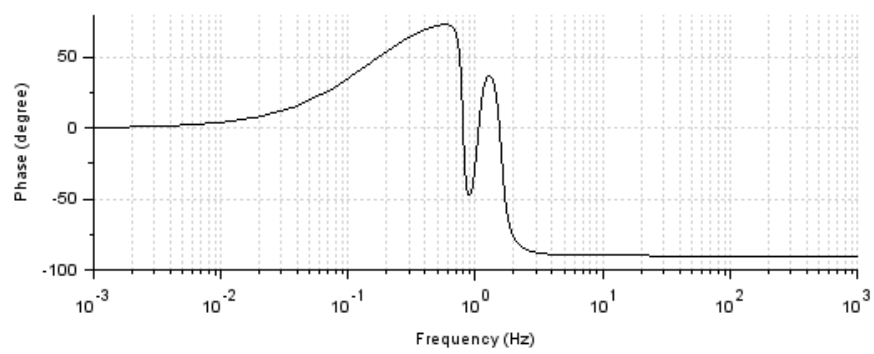
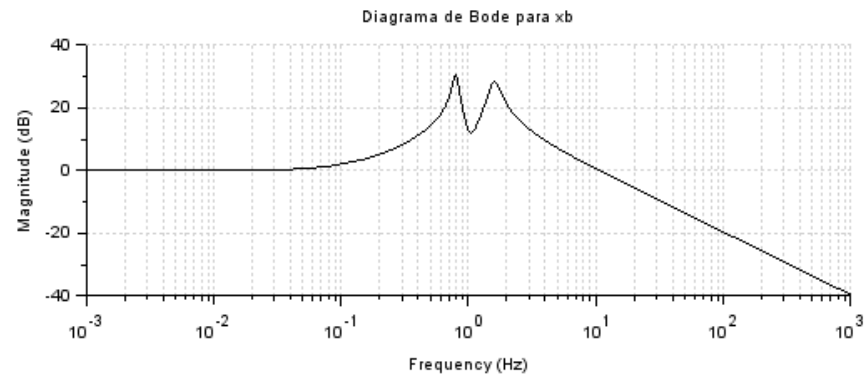
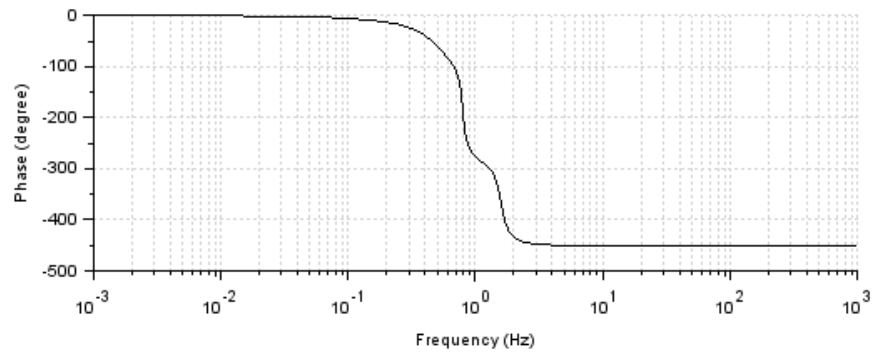
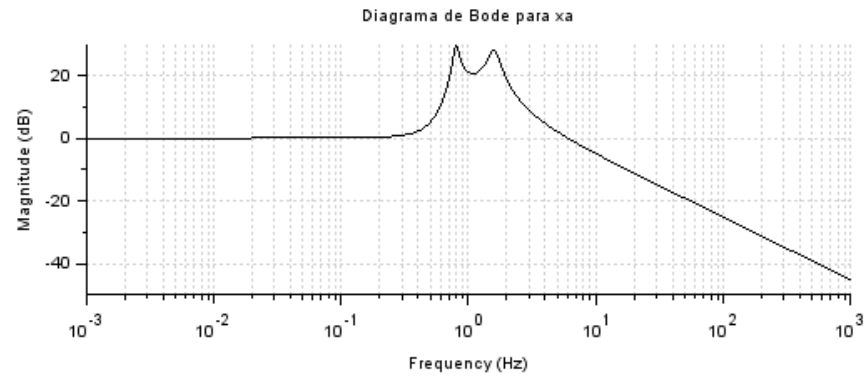
2.3 SIMULAÇÃO 3

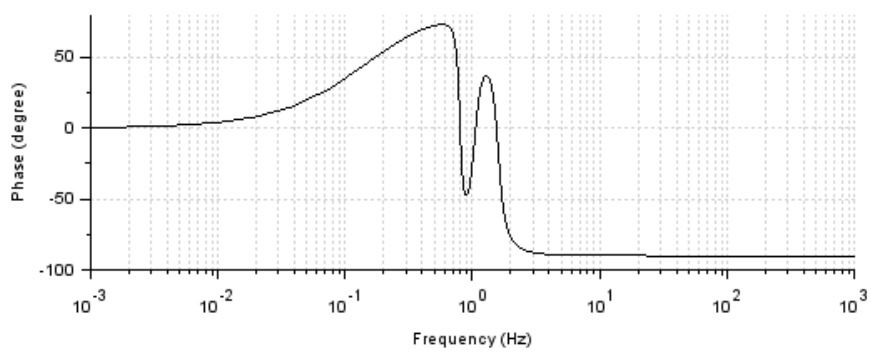
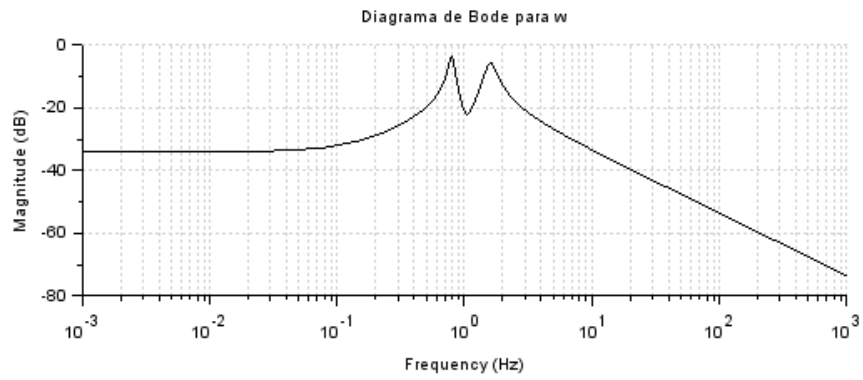
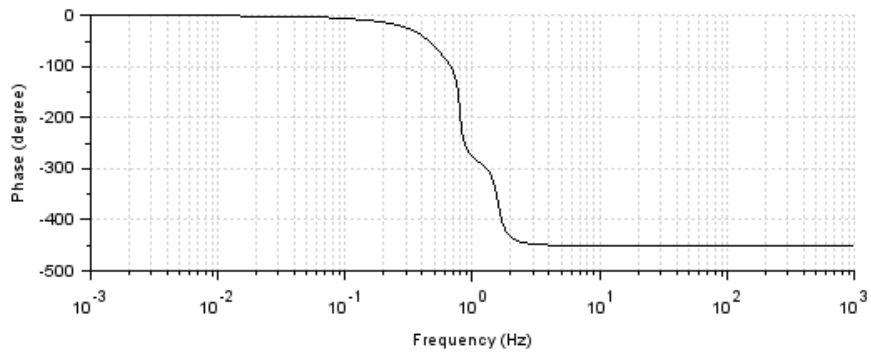
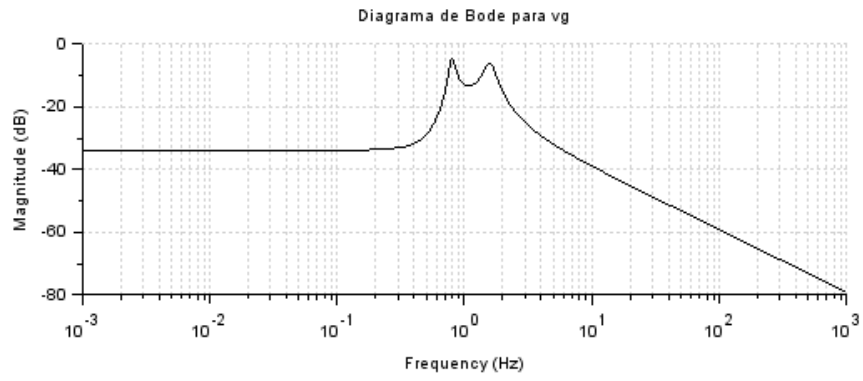


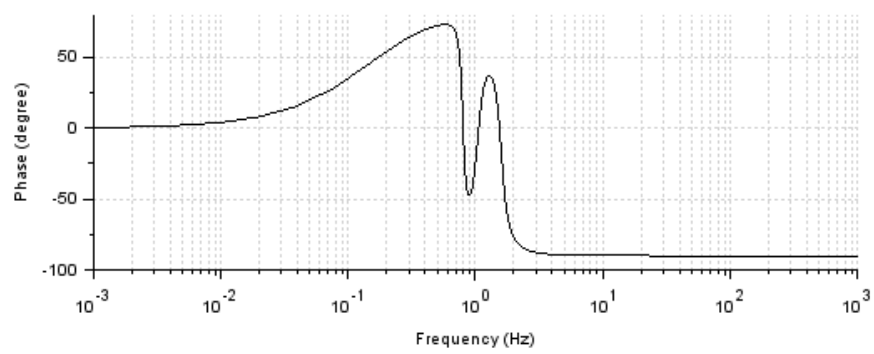
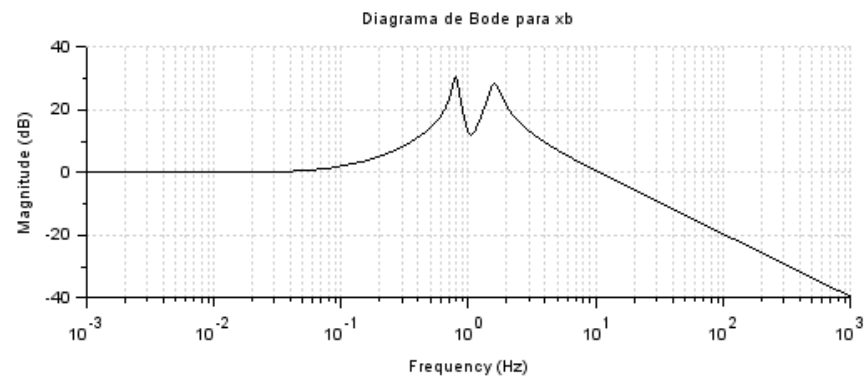
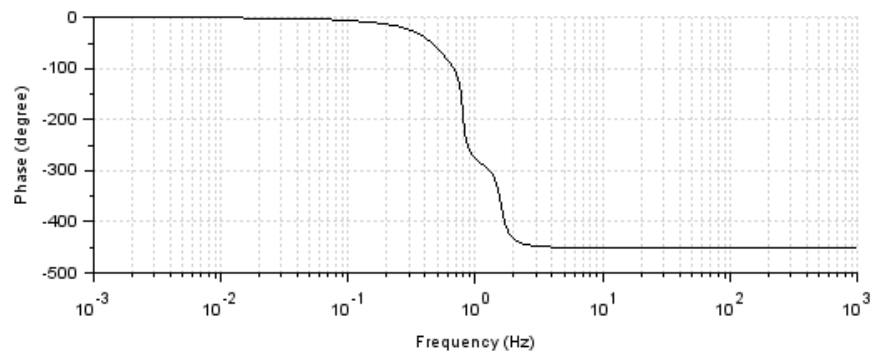
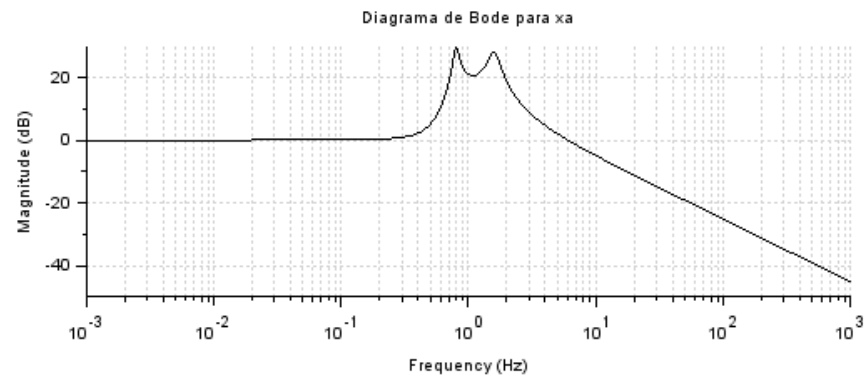
2.4 DIAGRAMAS DE BODE

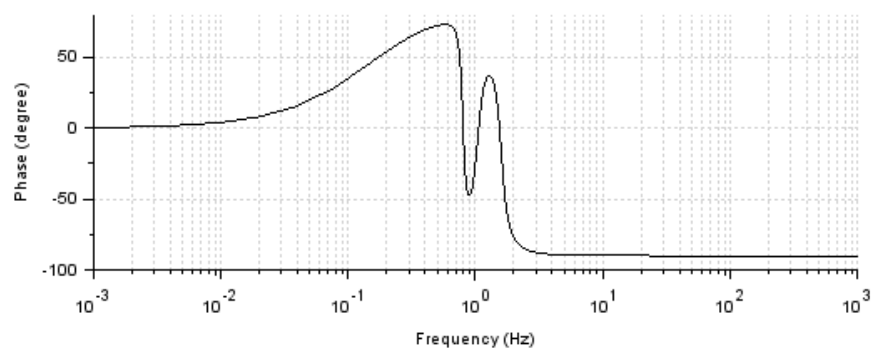
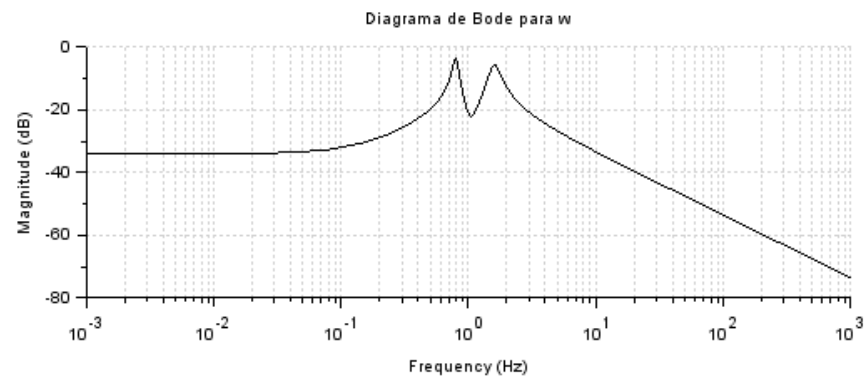
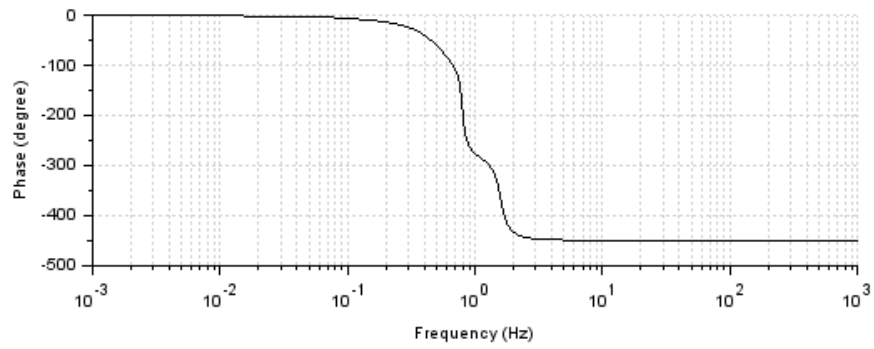
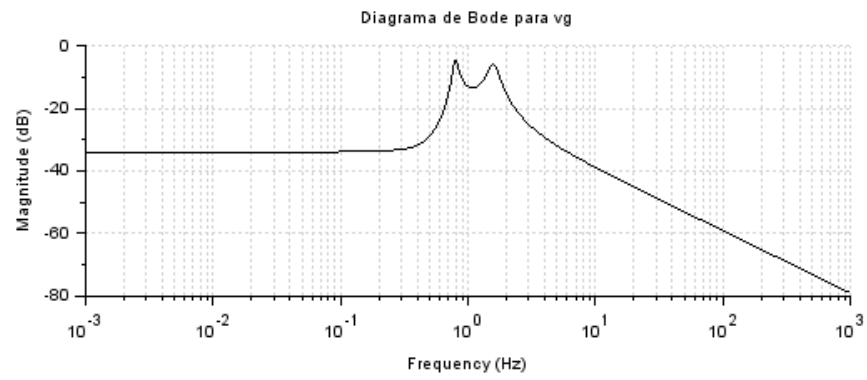






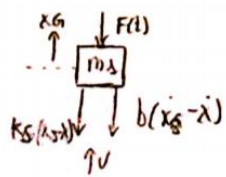




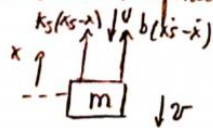


3 EXERCÍCIO 2

① massa suspensa:



② massa não suspensa



TAMB:

$$m_s \ddot{x}_s = v - k_s(x_s - x) - b(\dot{x}_s - \dot{x}) - F(t)$$

$$m \ddot{x} = -v + k_s(x_s - x) + b(\dot{x}_s - \dot{x}) - \mathcal{V}$$

4 APÊNDICE

```
//PME 3380-Lista G  
//Mauricio Chung Leiman - 10772571
```

```
//parametros do problema
```

```
m=200;  
j = 512;  
la = 0.8;  
lb = 0.8;  
ka = 10000;  
kb = 10000;  
ba = 200;  
bb = 200;  
vh = 10;
```

```
//vetor tempo
```

```
t = linspace(0, 10, 1000);
```

```
//condicoes iniciais
```

```
xa0 = 0;  
xb0 = 0;  
vg0 = 0;  
w0 = 0;  
simulacao = 1
```

```
//possibilidades de simulacao
```

```
if simulacao == 1 then  
function fun=u1(t), fun = t, endfunction  
if t < td then  
function fun=u2(t), fun = 0, endfunction  
else  
function fun=u2(t), fun = t, endfunction  
end
```

```
function fun=u3(t), fun = 1, endfunction  
if t < td then  
function fun=u4(t), fun = 0, endfunction  
else  
function fun=u4(t), fun = 1, endfunction  
end
```

```
elseif simulacao == 2 then  
function fun=u1(t), fun = -cos(9.8995*t)/9.8995, endfunction  
function fun=u2(t), fun = -cos(9.8995*t)/9.8995, endfunction  
function fun=u3(t), fun = sin(9.8995*t), endfunction  
function fun=u4(t), fun = sin(9.8995*t), endfunction
```

```
elseif simulacao == 3 then  
function fun=u1(t), fun = -cos(9.8995*t)/4.9875, endfunction  
function fun=u2(t), fun = cos(4.9875*t)/4.9875, endfunction  
function fun=u3(t), fun = sin(4.9875*t), endfunction  
function fun=u4(t), fun = -sin(4.9875*t), endfunction  
end
```

```
//espaco de estados
```

```
function dy=meiocarro(t,y)  
dy(1)=y(3)-la*y(4);  
dy(2)=y(3)+lb*y(4);  
dy(3)=-((ka/m)*y(1) - (kb/m)*y(2) - ((ba+bb)/m)*y(3) + ((ba*la - bb*lb)/m)*y(4) + (ka/M)*u1(t) + (kb/M)*u2(t) + (ba/M)*u3(t) + (bb/M)*u4(t);  
dy(4)=(la*ka/j)*y(1) - (lb*kb/j)*y(2) + ((la*ba - lb*bb)/j)*y(3) - ((ba*la^2 - ba*la^2)/M)*y(4) - (la*ka/j)*u1(t) + (la*ka/j)*u2(t) - (la*ba/j)*u3(t) + (lb*bb/j)*u4(t);  
endfunction
```

```
//integracao
```

```

resultado = ode([xa0; xb0; vg0; w0], 0, t, meiocarro);
xa = resultado(1,:);
xb = resultado(2,:);
vg = resultado(3,:);
w = resultado(4,:);

//plots
scf(1)
xtitle("Velocidade do centro de massa");
xlabel("Tempo [s]");
ylabel("Velocidade [m/s]");
plot(t,vg);

scf(2)
xtitle("Velocidade angular do corpo");
xlabel("Tempo [s]");
ylabel("Velocidade angular [rad/s]");
plot(t,w);

//parte 2
a = [0,0,1,-la;0,0,1,la;-ka/m,-kb/m,-(ba+bb)/m,(ba*la - bb*lb)/m;la*ka/j,-lb*kb/j,(la*ba-lb*bb)/j,-(ba*la^2 + bb*lb^2)/j];
b = [0,0,0,0;0,0,0,0;ka/m,kb/m,ba/m,bb/m;-la*ka/j,-lb*kb/j,-la*ba/j,-lb*bb/j];
solucao = syslin('c',a,b,[1,1,1,1]);
X = ss2tf(solucao);
scf(3);
bode(X(1,1));
xtitle("Diagrama de Bode para xa");
scf(4);
bode(X(1,2));
xtitle("Diagrama de Bode para xb");
scf(5);
bode(X(1,3));
xtitle("Diagrama de Bode para vg");
scf(6);
bode(X(1,4));
xtitle("Diagrama de Bode para w");

```